(pf).

Probability of events for a Poisson distribution [edit]

An event can occur 0, 1, 2, ... times in an interval. The average number of events in an interval is designated λ (lambda). λ is the event rate, also called the rate parameter. The probability of observing k events in an interval is given by the

$$P(k \text{ events in interval}) = e^{-\lambda} \frac{\lambda^k}{k!}$$

where

- $ullet \lambda$ is the average number of events per interval
- e is the number 2.71828... (Euler's number) the base of the natural logarithms
- k takes values 0, 1, 2, ...
- $k! = k \times (k-1) \times (k-2) \times ... \times 2 \times 1$ is the factorial of k.

$$P(X=Z) = Z = X + 1$$

$$= \sum_{i=0}^{Z} P(X=i) \cdot P(Y=Z-i)$$

$$= \sum_{i=0}^{Z} \frac{e^{\lambda_{i}}}{i!} \cdot \frac{e^{-\lambda_{2}}}{(Z-i)!}$$

$$= \sum_{i=0}^{Z} \frac{e^{\lambda_{i}}}{i!} \cdot \frac{e^{\lambda_{2}}}{(Z-i)!}$$

$$= \sum_{i=0}^{Z} \frac{e^{\lambda_{1}}}{i!} \cdot \frac{e^{-\lambda_{2}}}{(Z-i)!}$$

$$= \sum_{i=0}^{Z} \frac{e^{\lambda_{1}}}{i!} \cdot \frac{e^{\lambda_{1}}}{(Z-i)!}$$

$$= \sum_{i=0}$$

let
$$\lambda i + \lambda 2 = \lambda$$

$$= \underbrace{\frac{-\lambda}{2!}}_{\frac{2!}{2!}}$$

Ref: MIT OCW RES 6-012 Intro to Probability, Spring 2018