

Q3.1 .

$$\left\{ \begin{array}{l} P(y = \bar{j} | x) \cdot 0 + P(y \neq \bar{j} | x) \cdot \lambda_s \\ = (1 - P(y = \bar{j} | x)) \cdot \lambda_s \quad \dots \text{Expected loss should} \\ \quad \text{we choose } \bar{j} \\ \text{Expected loss for reject} = \lambda_r. \end{array} \right.$$

\Rightarrow Expected loss of choosing $\bar{j} \leq \lambda_r$.

$$1 - P(y = \bar{j} | x) \leq \lambda_r / \lambda_s$$

$$P(y = \bar{j} | x) \geq 1 - \frac{\lambda_r}{\lambda_s} \quad \#$$

if we wanna minimize risk of choosing \bar{j} ,

Q 3.2.

if we adjust $\frac{\lambda_r}{\lambda_s}$ from $0 \rightarrow 1$.

$P(y = \bar{j} | x) \geq 1 - \frac{\lambda_r}{\lambda_s}$ will become harder to satisfy.

↓
this we can't change, it's info from data.

→ if at one point this inequality doesn't satisfy

say, $P(y = \bar{j} | x) \geq 1$ (impossible)

→ we aren't able to minimize risk of choosing \bar{j} so we should reject.

→ the other way is similar #