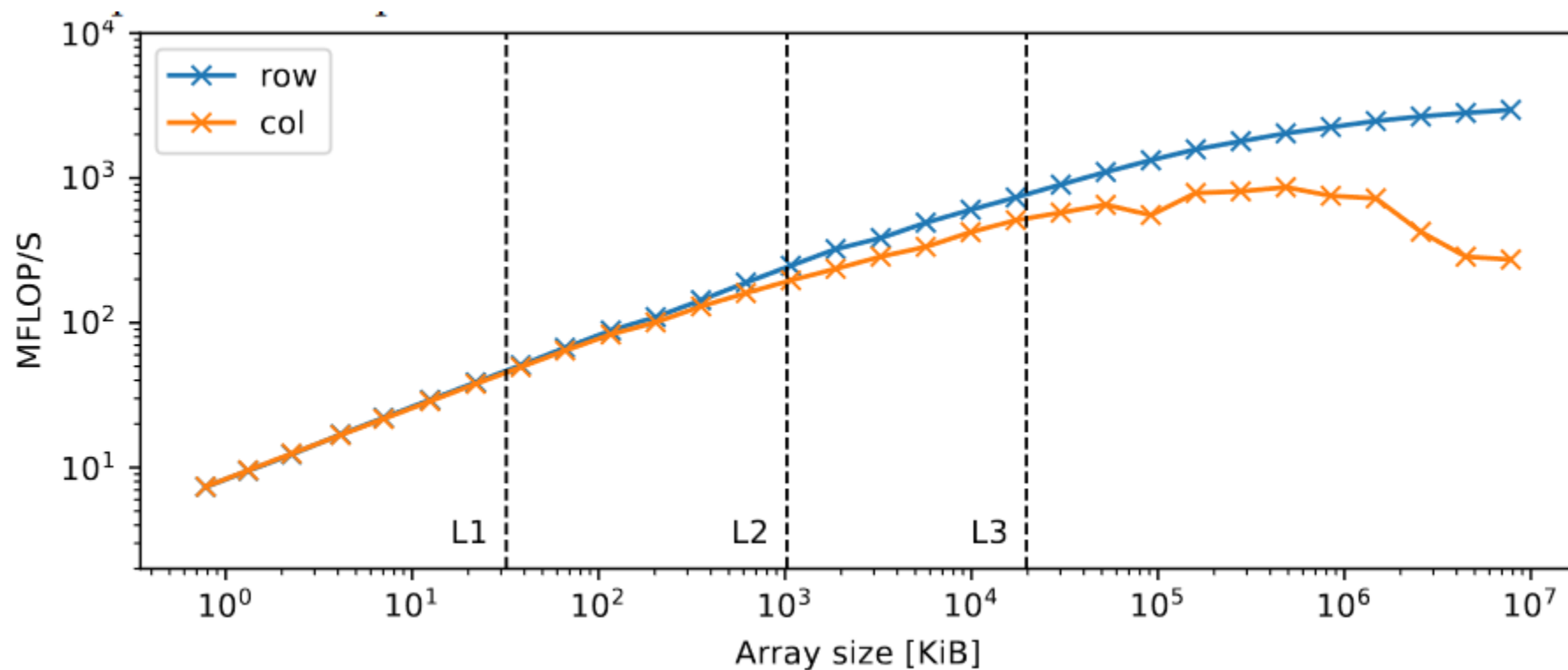


Week 4 – Profiling and High-Performance NumPy

02613 Python and High-Performance Computing

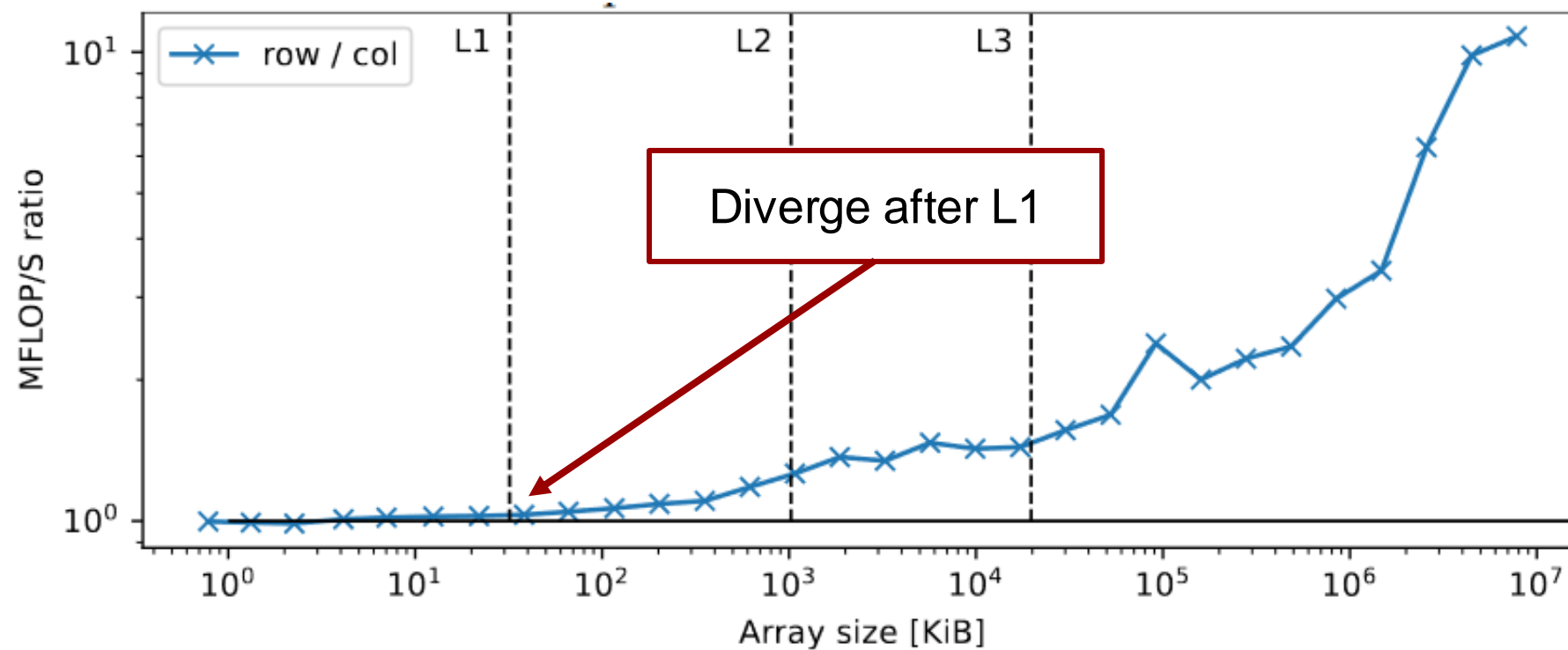
Last week on 02613

Performance plots



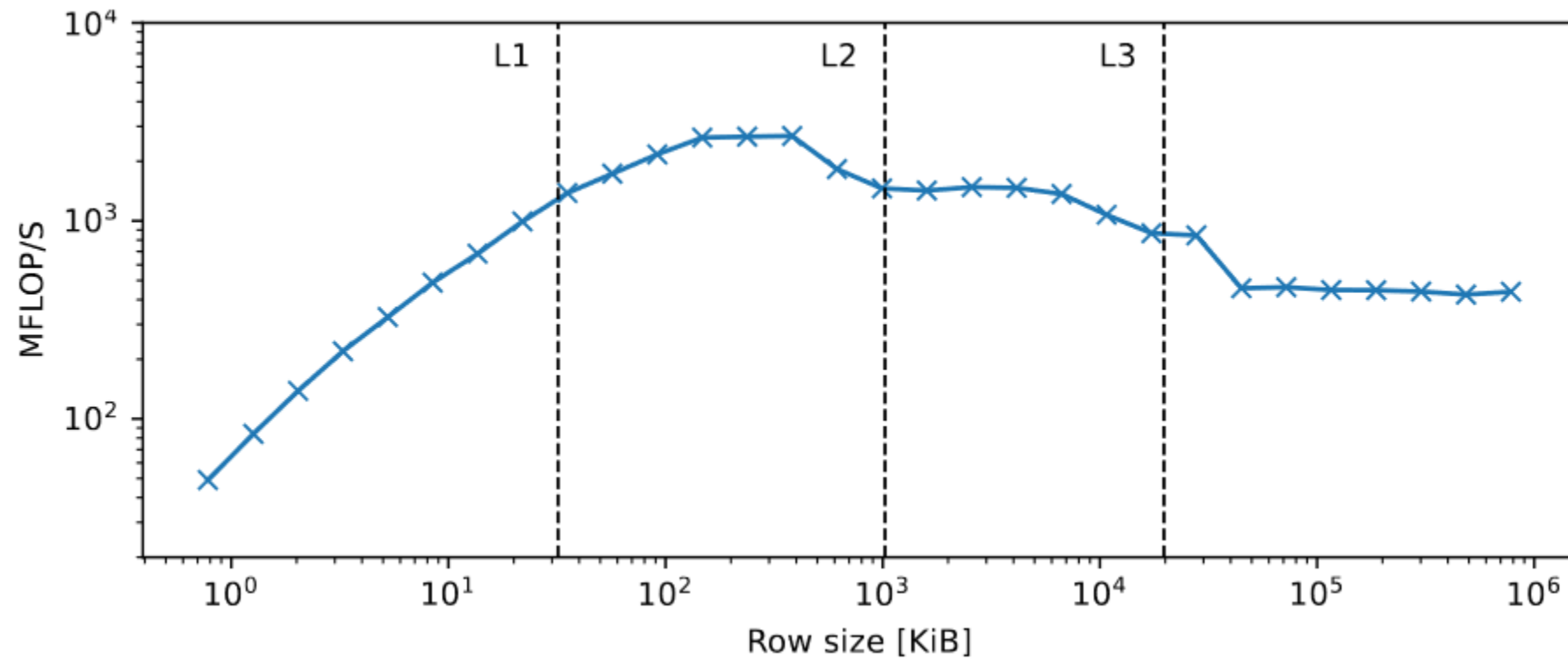
Last week on 02613

Performance plots



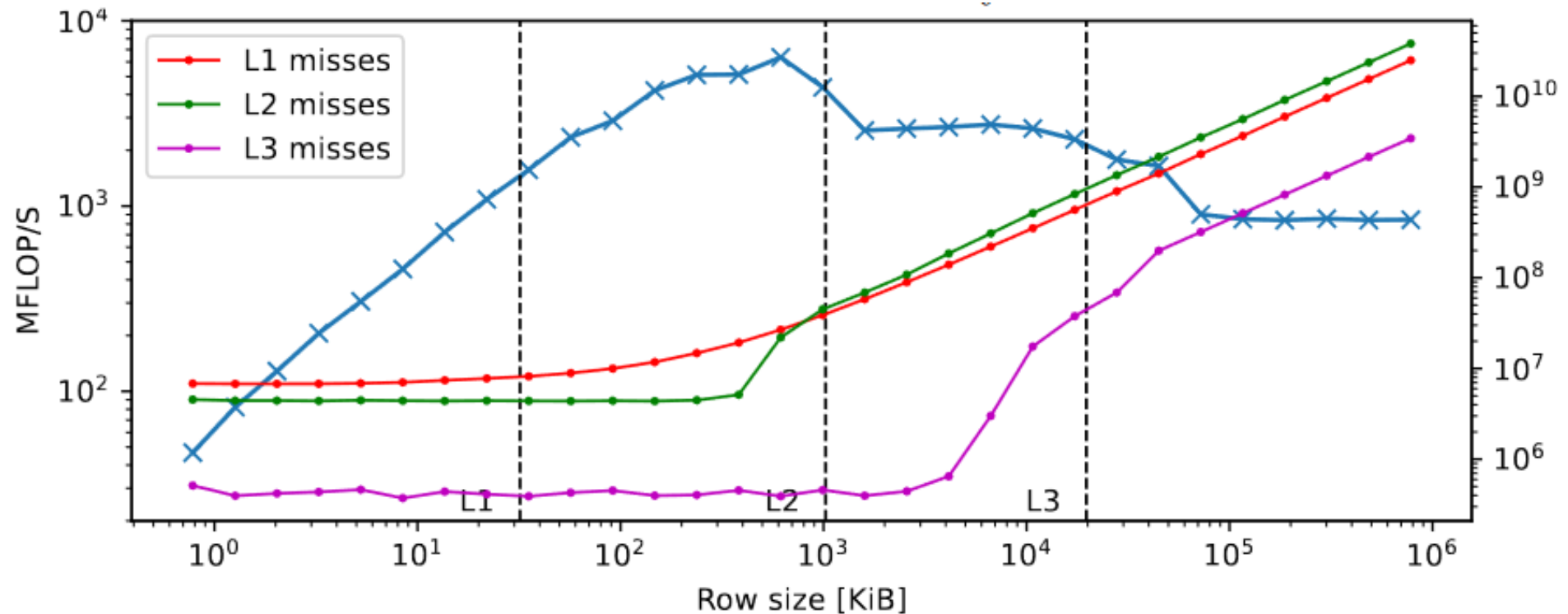
Last week on 02613

Performance plots



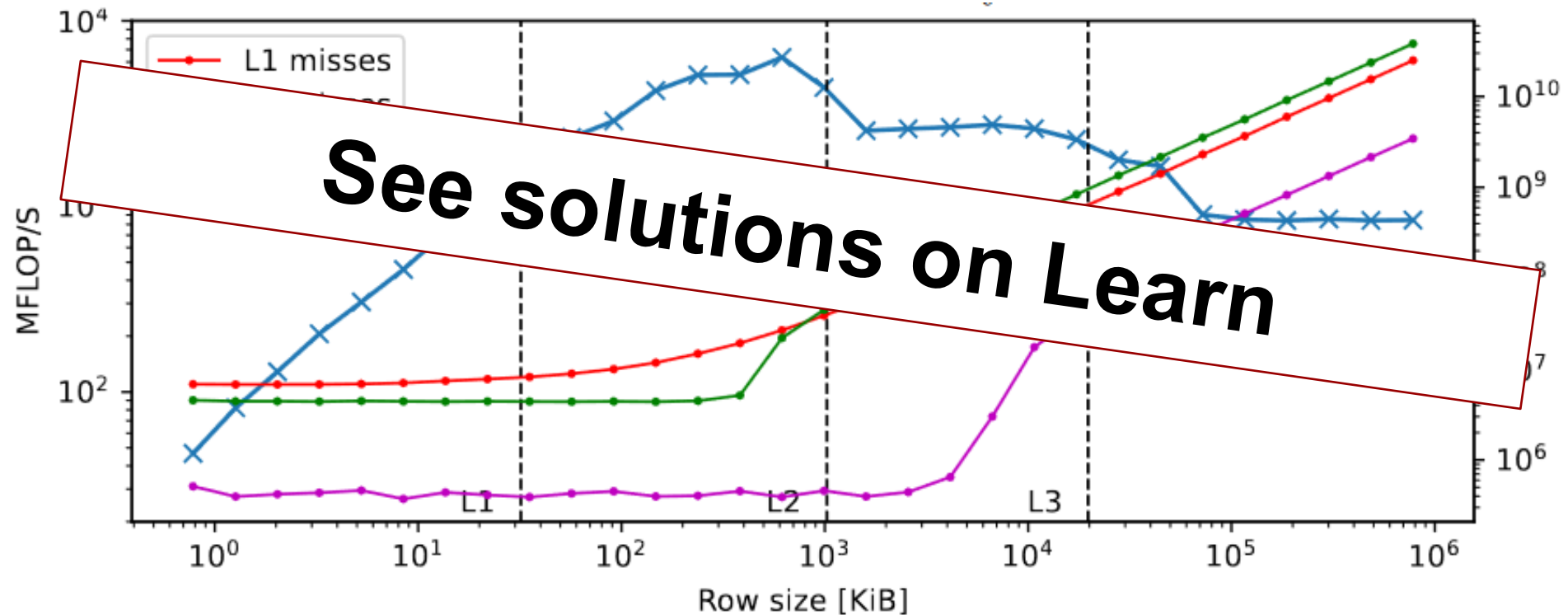
Last week on 02613

Performance plots



Last week on 02613

Performance plots



Today

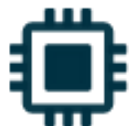
1. NumPy

2. Profiling



NumPy

Quantum Computing



[QuTiP](#)
[PyQuil](#)
[Qiskit](#)
[PennyLane](#)

Statistical Computing



[Pandas](#)
[statsmodels](#)
[Xarray](#)
[Seaborn](#)

Signal Processing



[SciPy](#)
[PyWavelets](#)
[python-control](#)

Image Processing



[Scikit-image](#)
[OpenCV](#)
[Mahotas](#)

Graphs and Networks



[NetworkX](#)
[graph-tool](#)
[igraph](#)
[PyGSP](#)

Astronomy



[AstroPy](#)
[SunPy](#)
[SpacePy](#)

Cognitive Psychology



[PsychoPy](#)

Bioinformatics



[BioPython](#)
[Scikit-Bio](#)
[PyEnsembl](#)
[ETE](#)

Bayesian Inference



[PyStan](#)
[PyMC3](#)
[ArviZ](#)
[emcee](#)

Mathematical Analysis



[SciPy](#)
[SymPy](#)
[cvxpy](#)
[FEniCS](#)

Chemistry



[Cantera](#)
[MDAnalysis](#)
[RDKit](#)
[PyBaMM](#)

Geoscience



[Pangeo](#)
[Simpeg](#)
[ObsPy](#)
[Fatiando a Terra](#)

Geographic Processing



[Shapely](#)
[GeoPandas](#)
[Folium](#)

Architecture & Engineering



[COMPAS](#)
[City Energy Analyst](#)
[Sverchok](#)

numpy.org



PyTorch



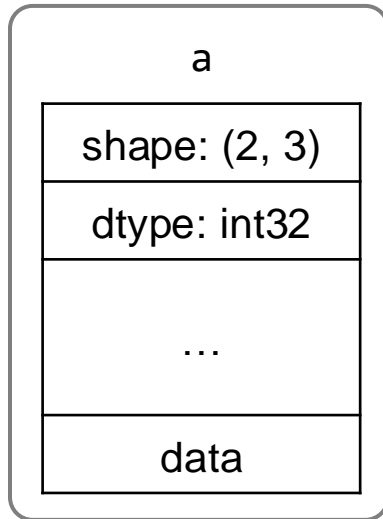
What is a NumPy array

```
>>> a = np.array([[1, 2, 3], [4, 5, 6]])
```

1	2	3
4	5	6

What is a NumPy array

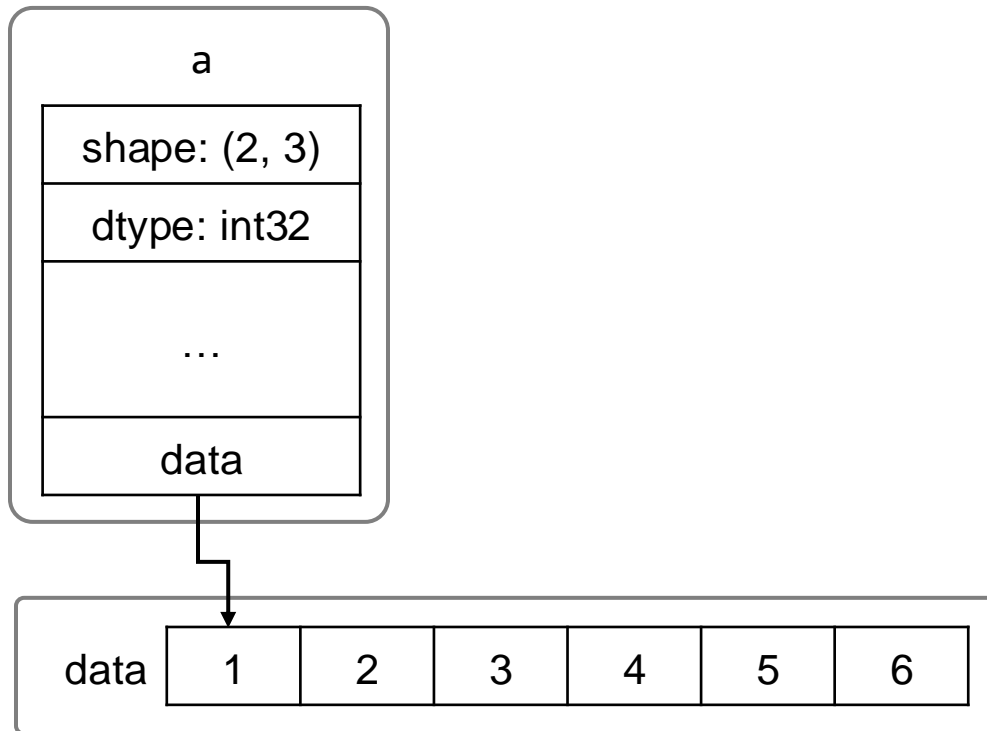
```
>>> a = np.array([[1, 2, 3], [4, 5, 6]])
```



1	2	3
4	5	6

What is a NumPy array

```
>>> a = np.array([[1, 2, 3], [4, 5, 6]])
```



1	2	3
4	5	6

Caches: multidimensional arrays

X =

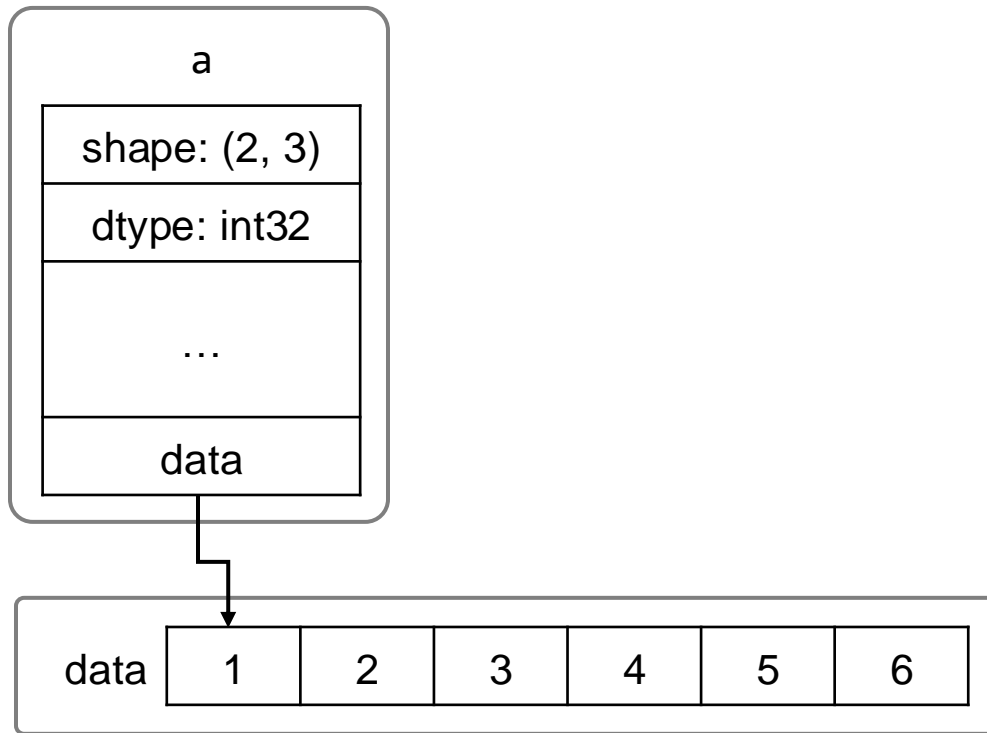
				3,5														

X =

Row 1	Row 2		Row 3	Row 3
-------	-------	--	-------	-------

What is a NumPy array

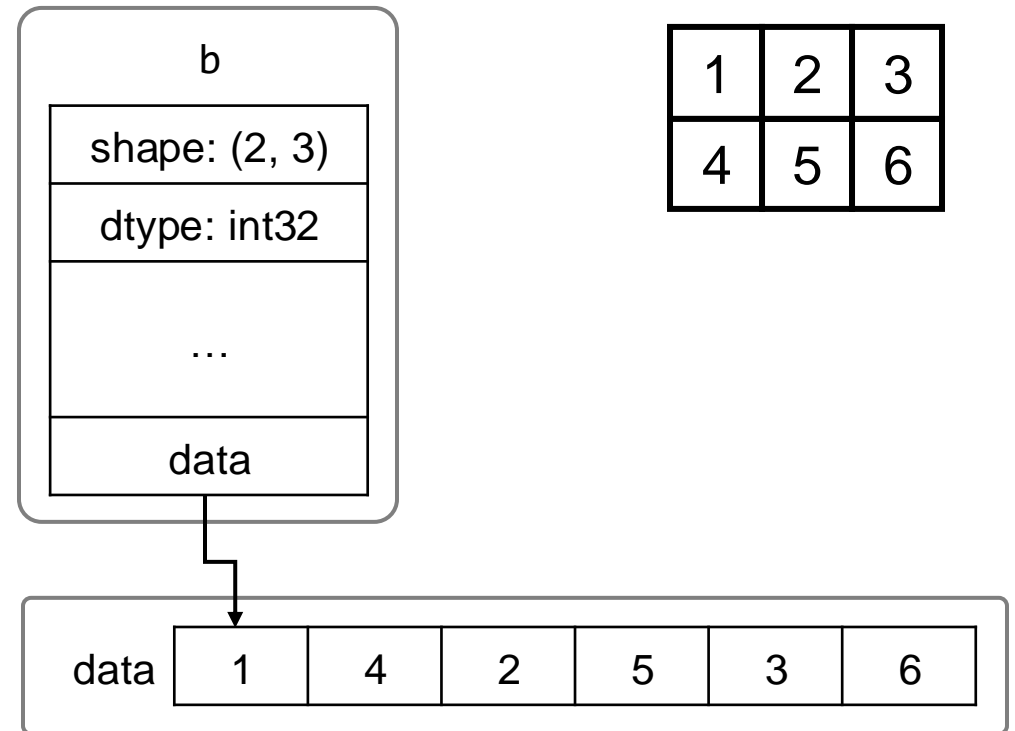
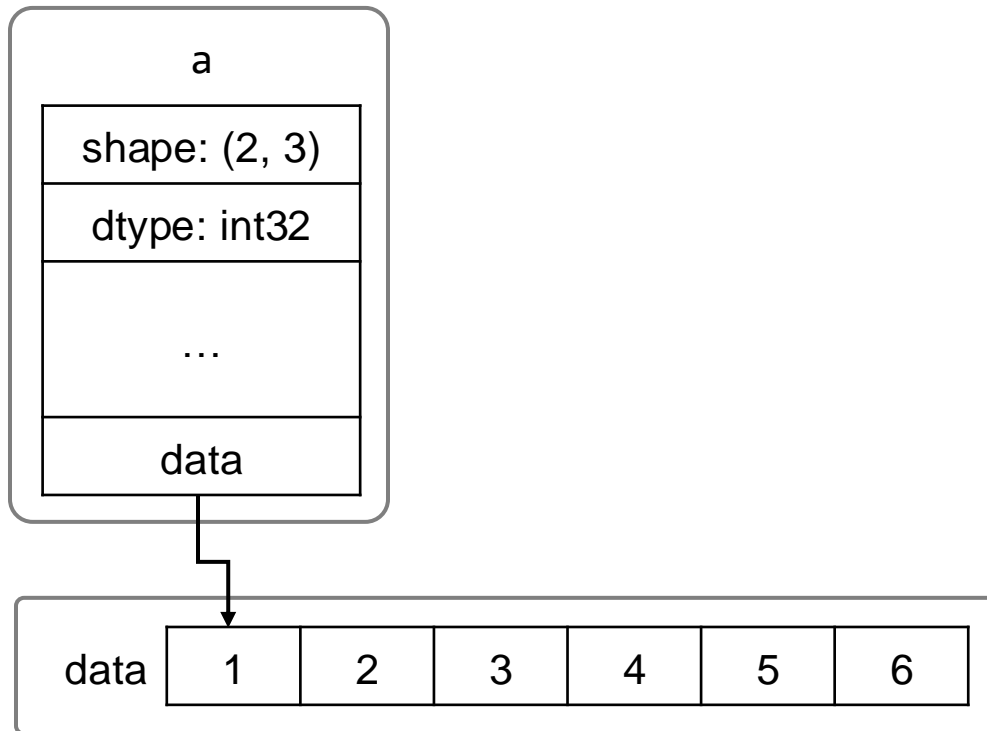
```
>>> a = np.array([[1, 2, 3], [4, 5, 6]])
```



1	2	3
4	5	6

What is a NumPy array

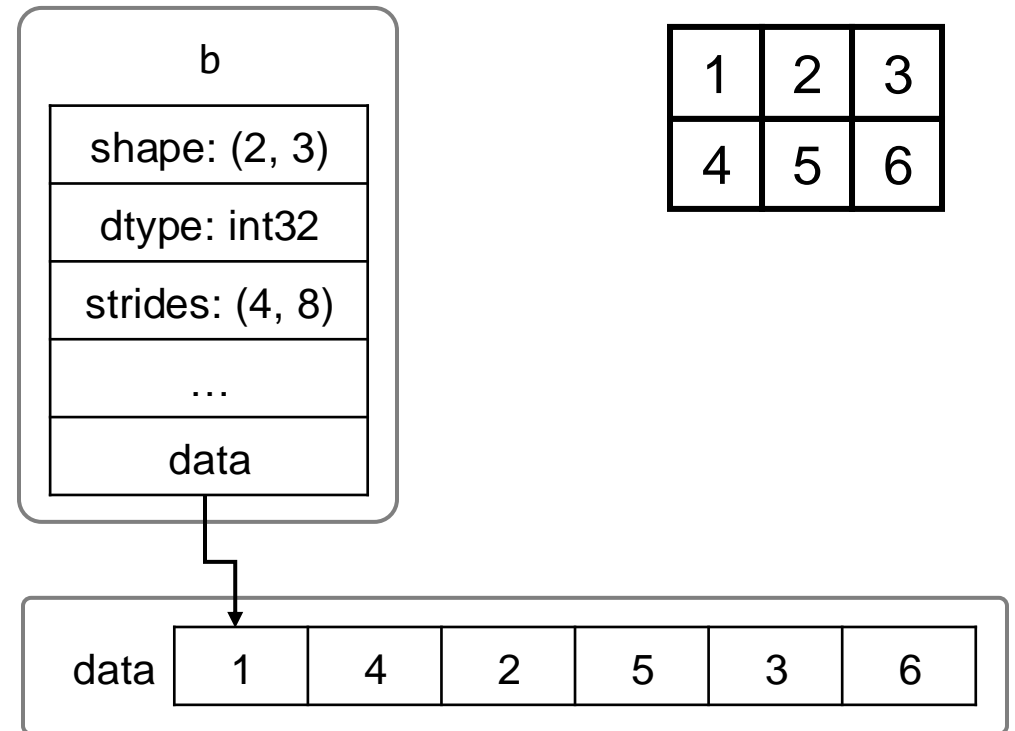
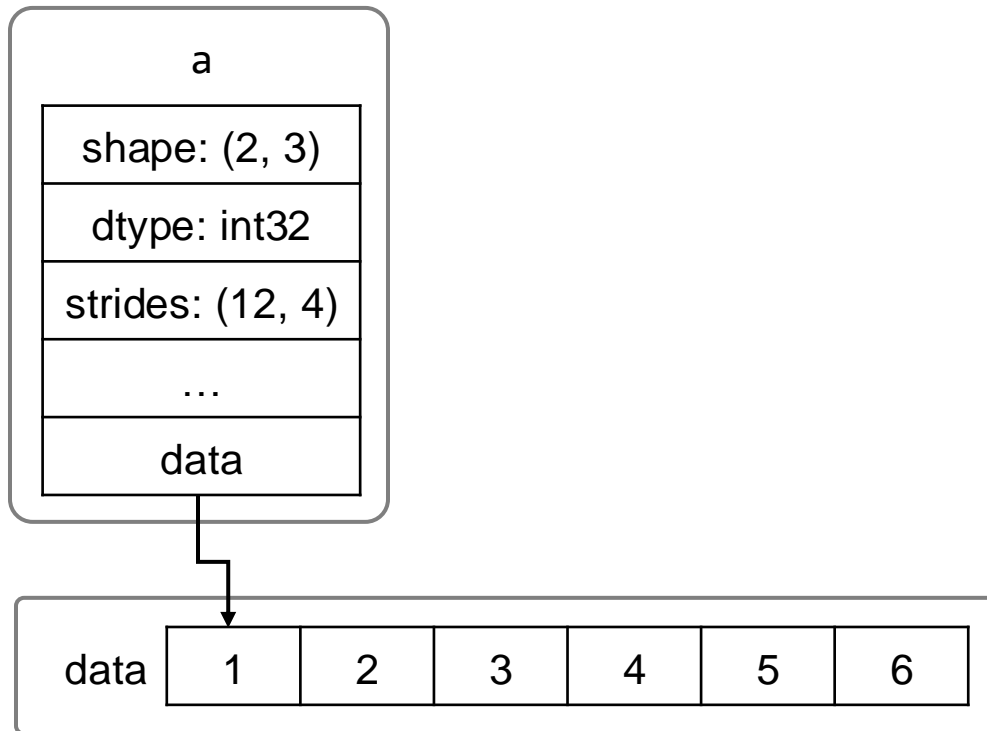
```
>>> a = np.array([[1, 2, 3], [4, 5, 6]])  
>>> b = np.array([[1, 2, 3], [4, 5, 6]],  
                  order='F') # F=Fortran
```



1	2	3
4	5	6

What is a NumPy array

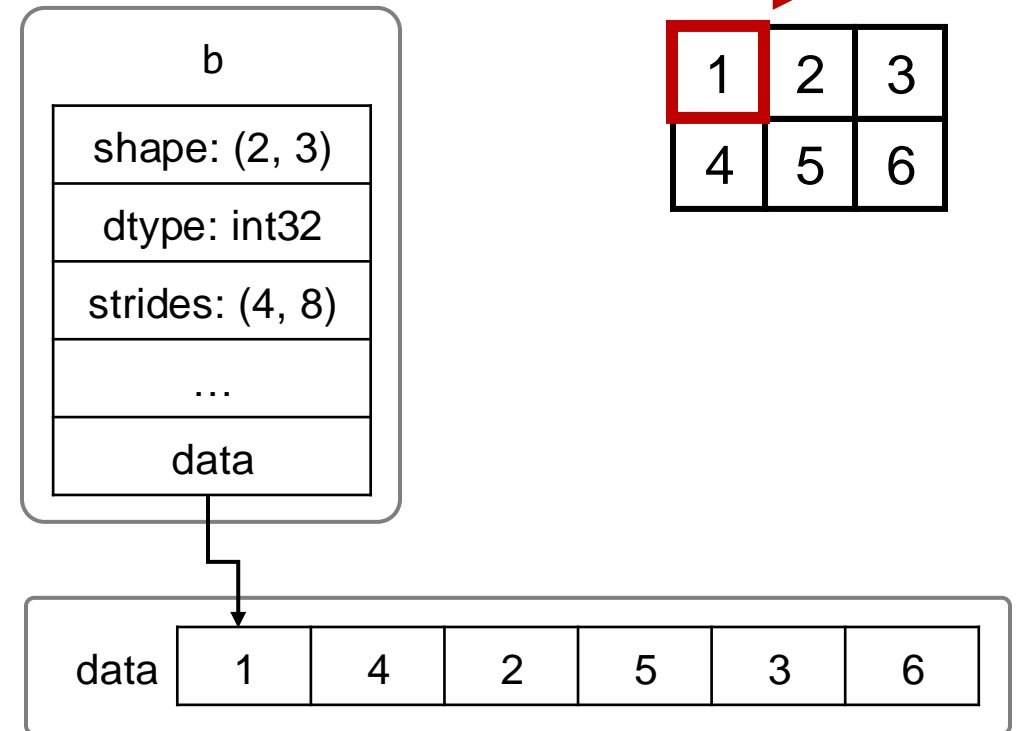
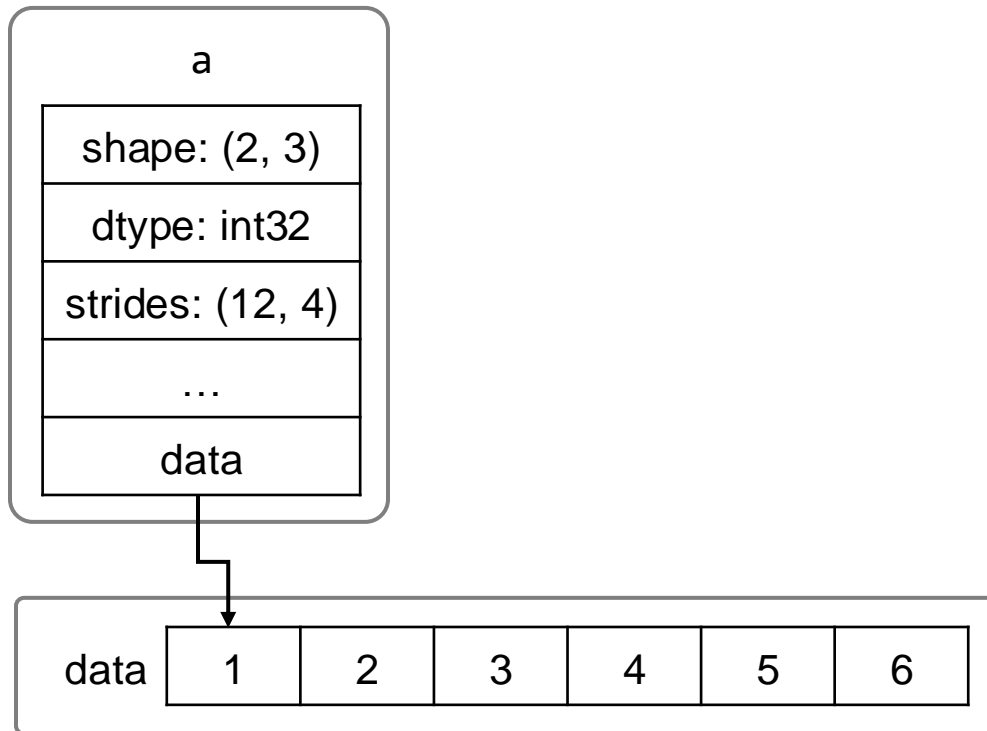
```
>>> a = np.array([[1, 2, 3], [4, 5, 6]])  
>>> b = np.array([[1, 2, 3], [4, 5, 6]],  
                  order='F') # F=Fortran
```



1	2	3
4	5	6

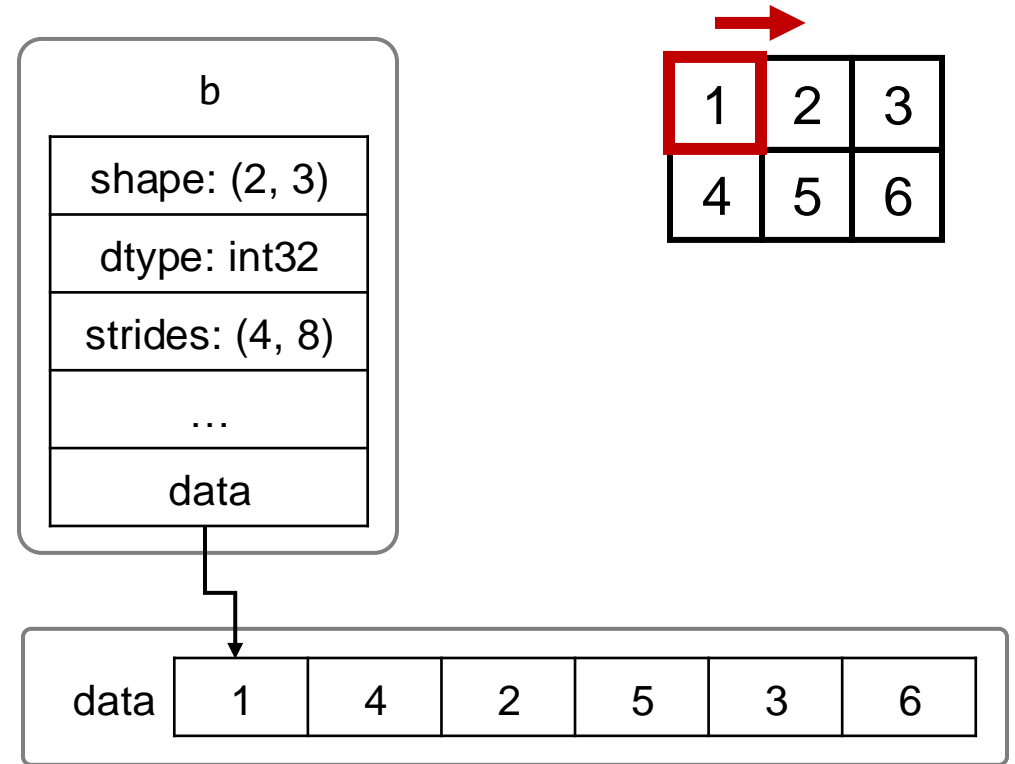
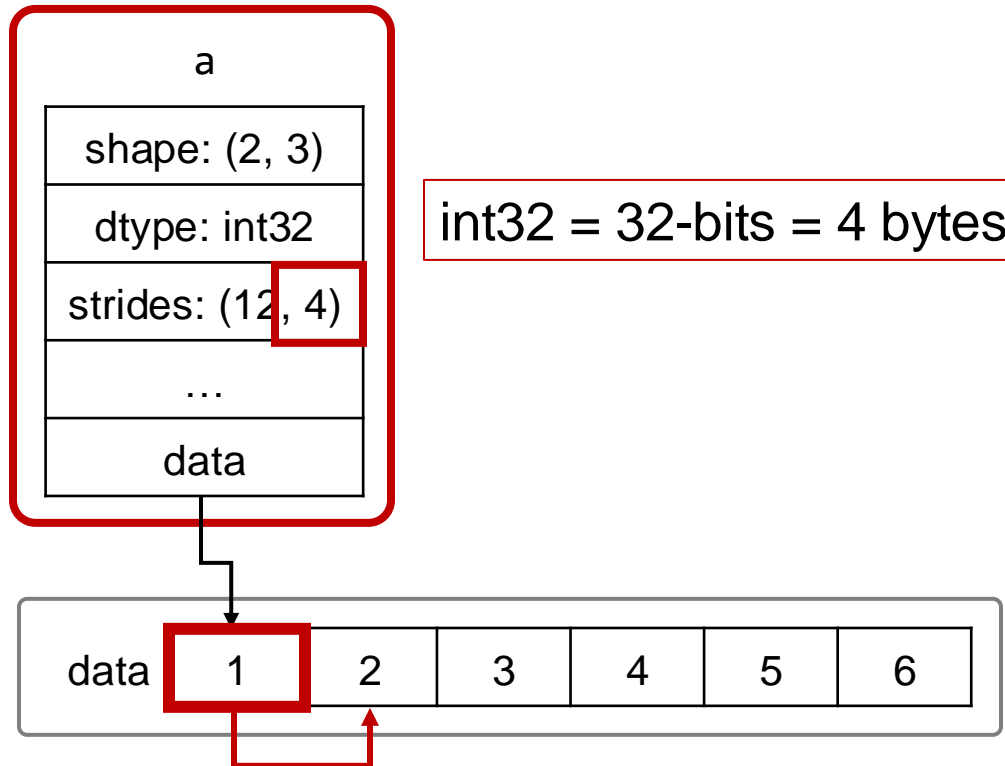
What is a NumPy array

```
>>> a = np.array([[1, 2, 3], [4, 5, 6]])  
>>> b = np.array([[1, 2, 3], [4, 5, 6]],  
                  order='F') # F=Fortran
```



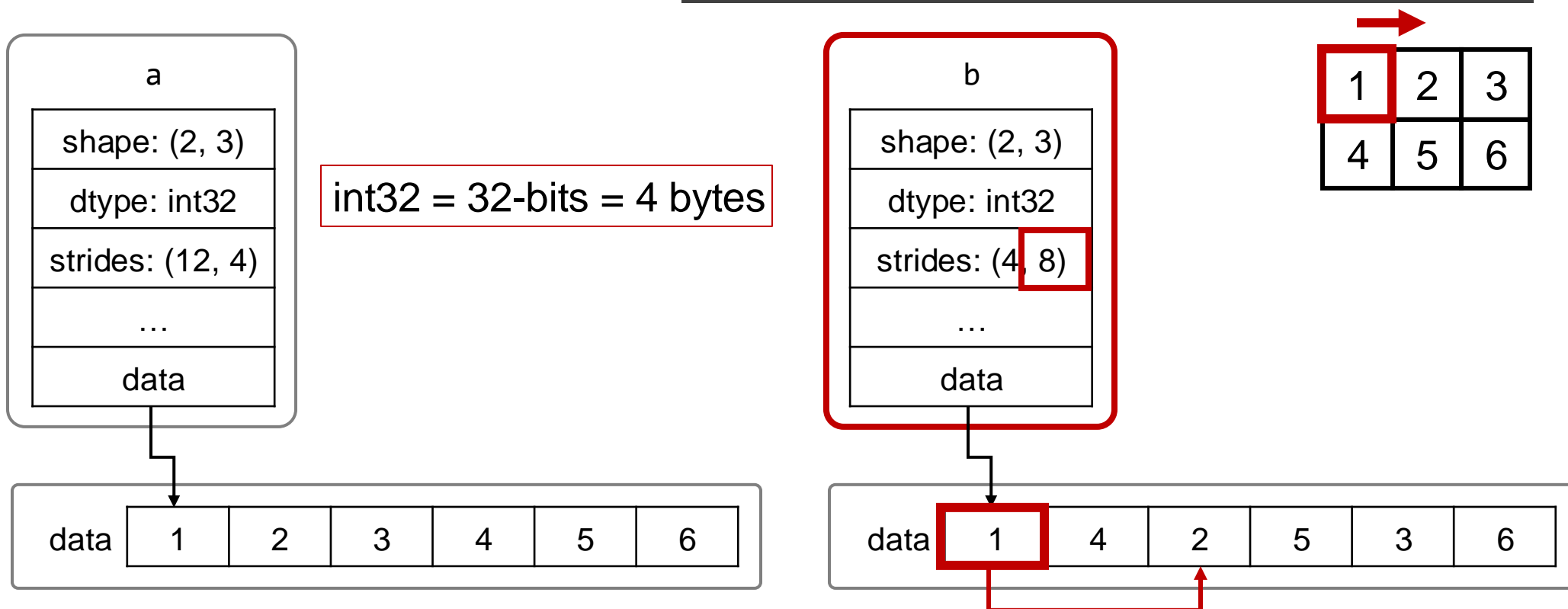
What is a NumPy array

```
>>> a = np.array([[1, 2, 3], [4, 5, 6]])
>>> b = np.array([[1, 2, 3], [4, 5, 6]],
                  order='F') # F=Fortran
```



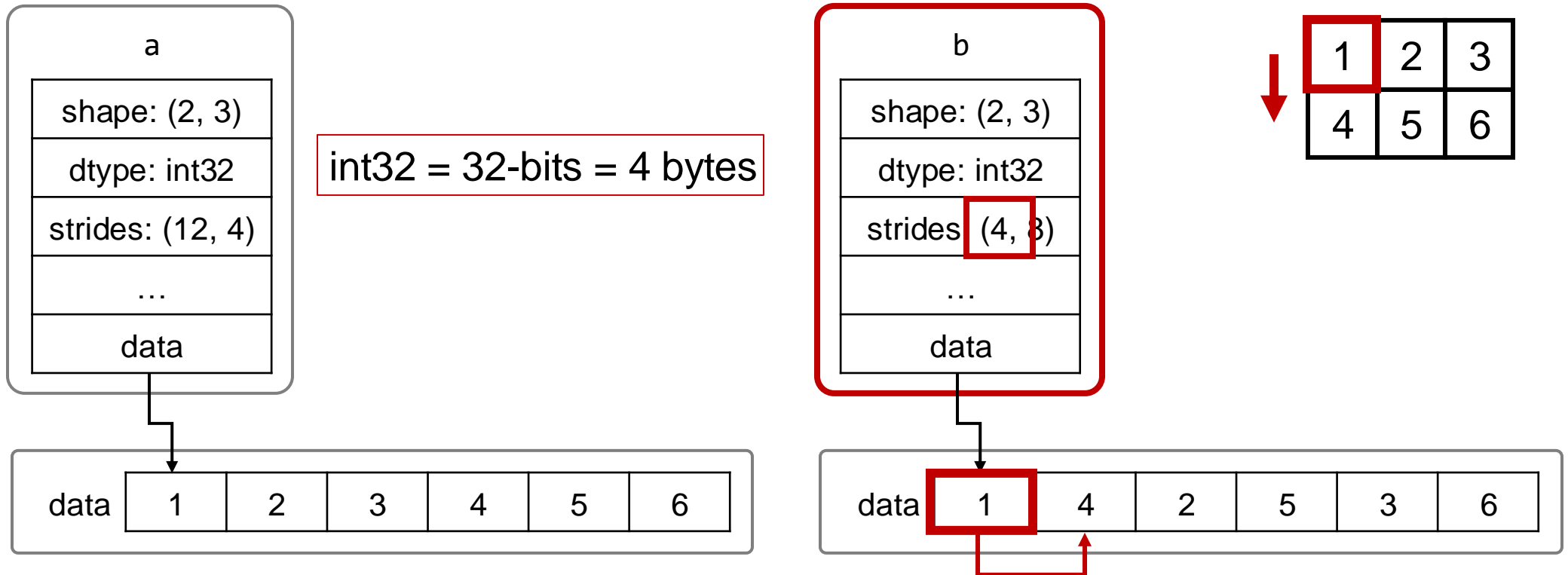
What is a NumPy array

```
>>> a = np.array([[1, 2, 3], [4, 5, 6]])  
>>> b = np.array([[1, 2, 3], [4, 5, 6]],  
                  order='F') # F=Fortran
```



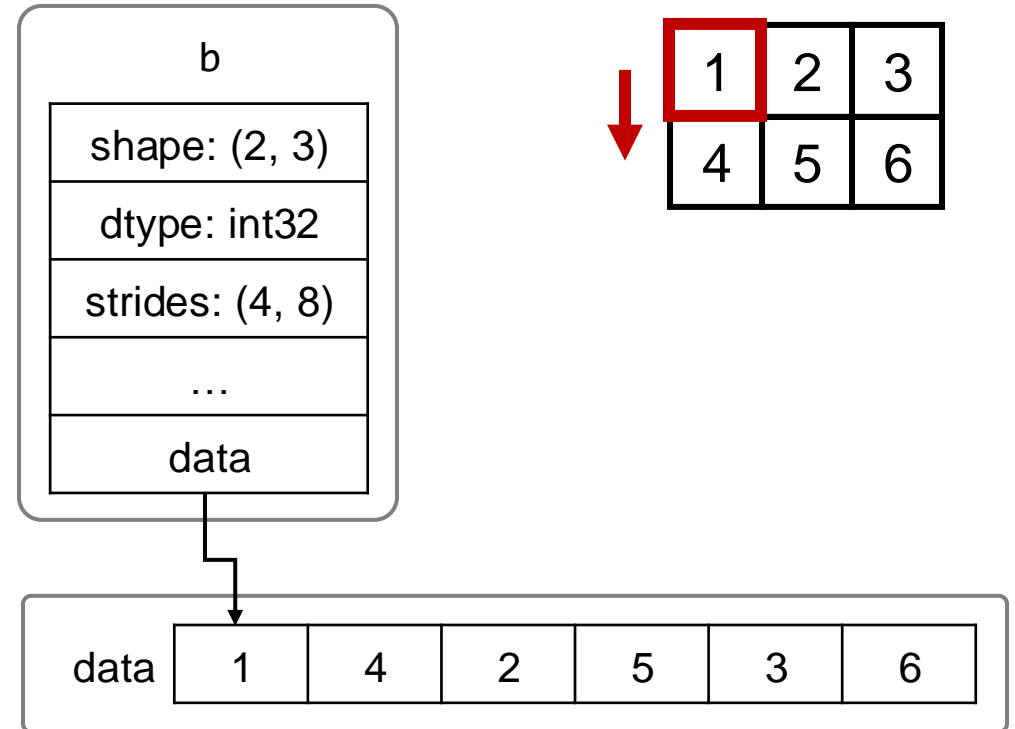
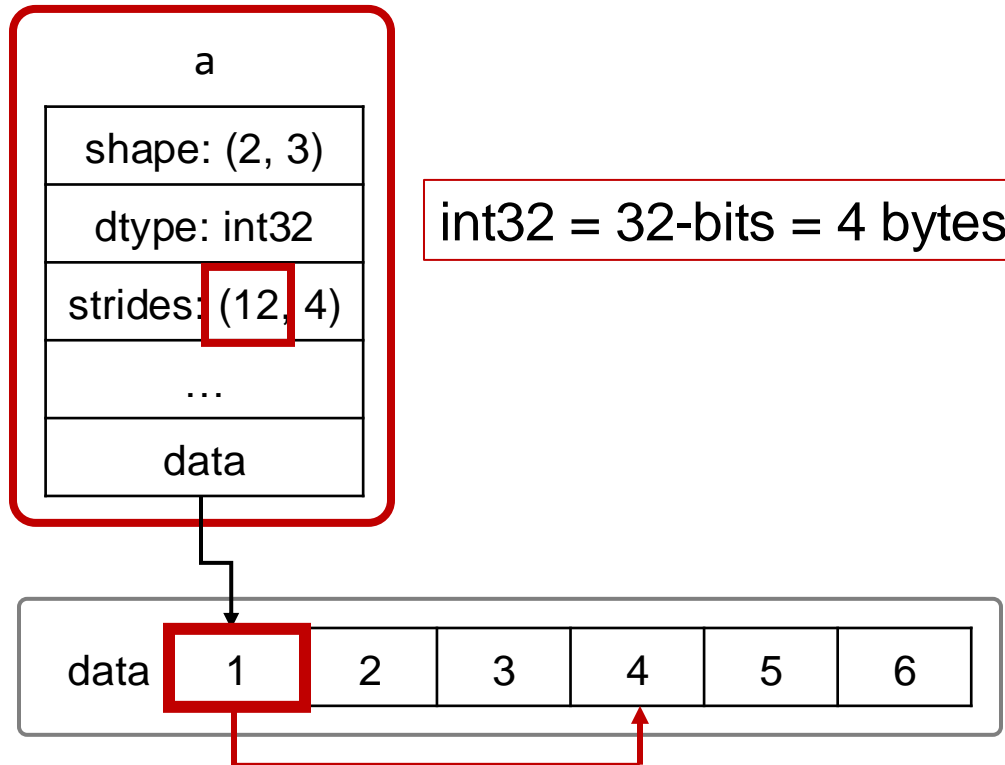
What is a NumPy array

```
>>> a = np.array([[1, 2, 3], [4, 5, 6]])  
>>> b = np.array([[1, 2, 3], [4, 5, 6]],  
                  order='F') # F=Fortran
```



What is a NumPy array

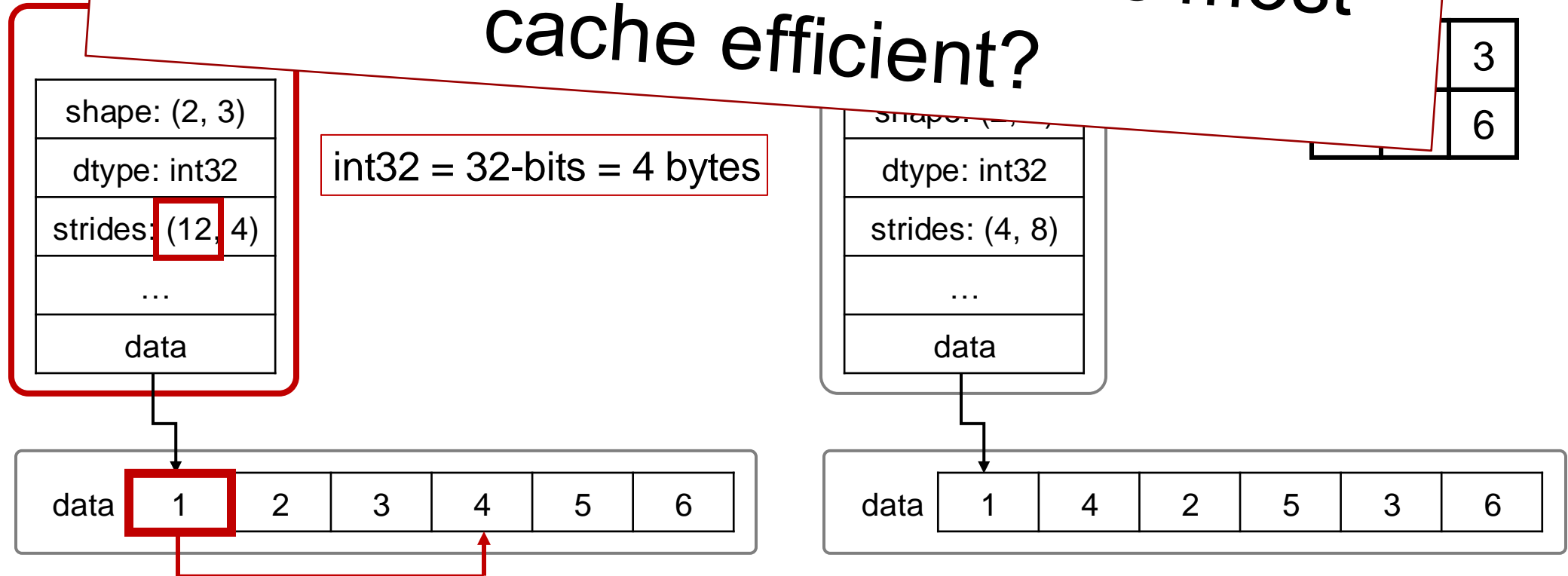
```
>>> a = np.array([[1, 2, 3], [4, 5, 6]])  
>>> b = np.array([[1, 2, 3], [4, 5, 6]],  
                  order='F') # F=Fortran
```



What is a NumPy array

```
>>> a = np.array([[1, 2, 3], [4, 5, 6]])  
>>> b = np.array([[1, 2, 3], [4, 5, 6]],  
                  dtype=np.float64)  
>>> a
```

Question: what direction is most cache efficient?



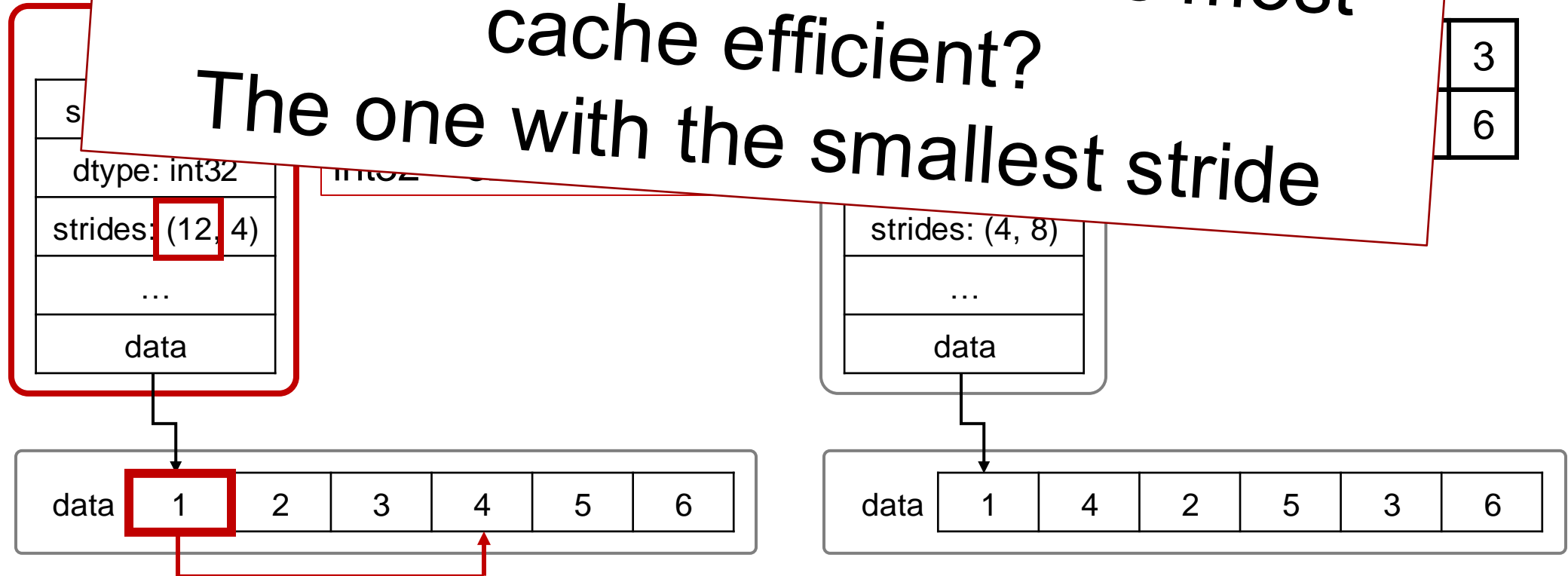
What is a NumPy array

```
>>> a = np.array([[1, 2, 3], [4, 5, 6]])
```

```
b = np.array([[1, 2, 3], [4, 5, 6]],
```

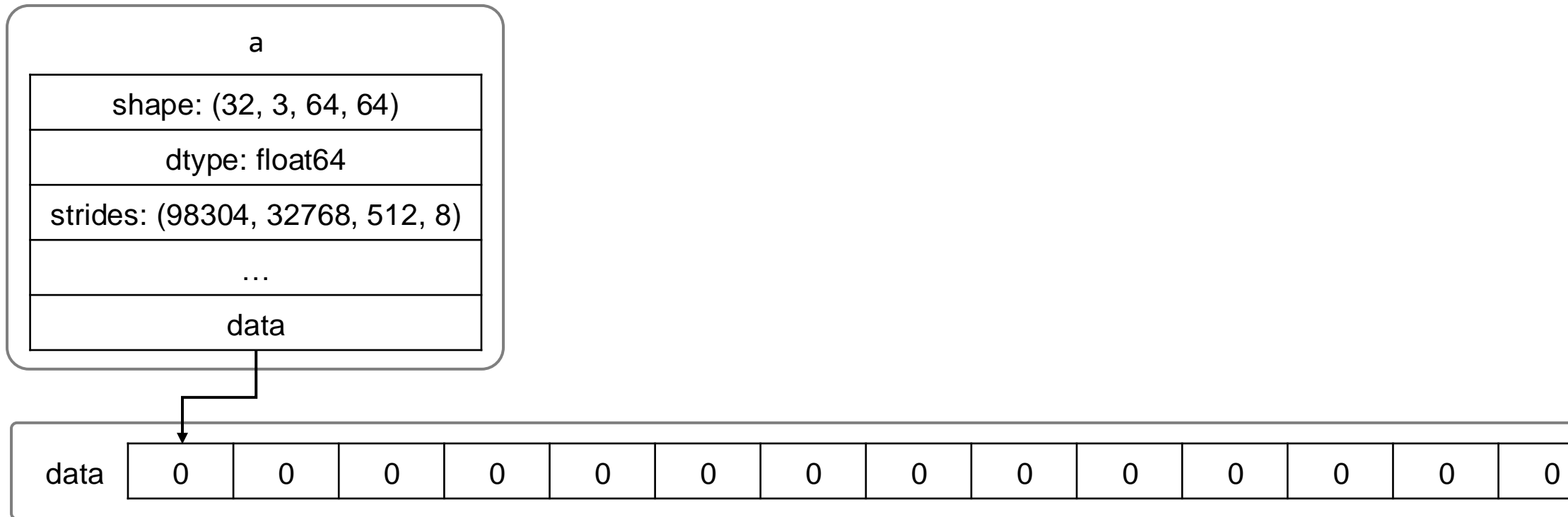
an

Question: what direction is most
cache efficient?
The one with the smallest stride



What is a NumPy array

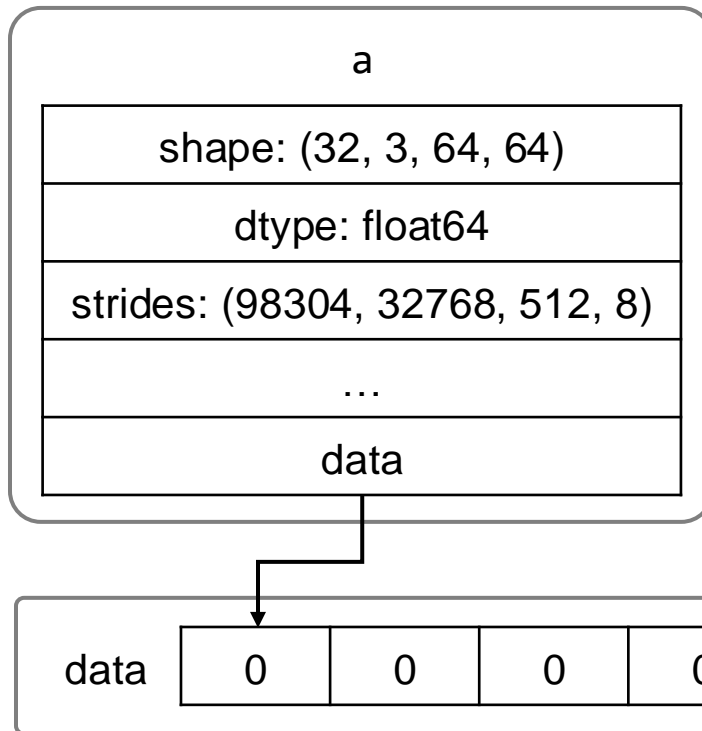
```
>>> a = np.zeros((32, 3, 64, 64))
```



What is a NumPy array

```
>>> a = np.zeros((32, 3, 64, 64))  
>>> a[2, 1, 4, 8]
```

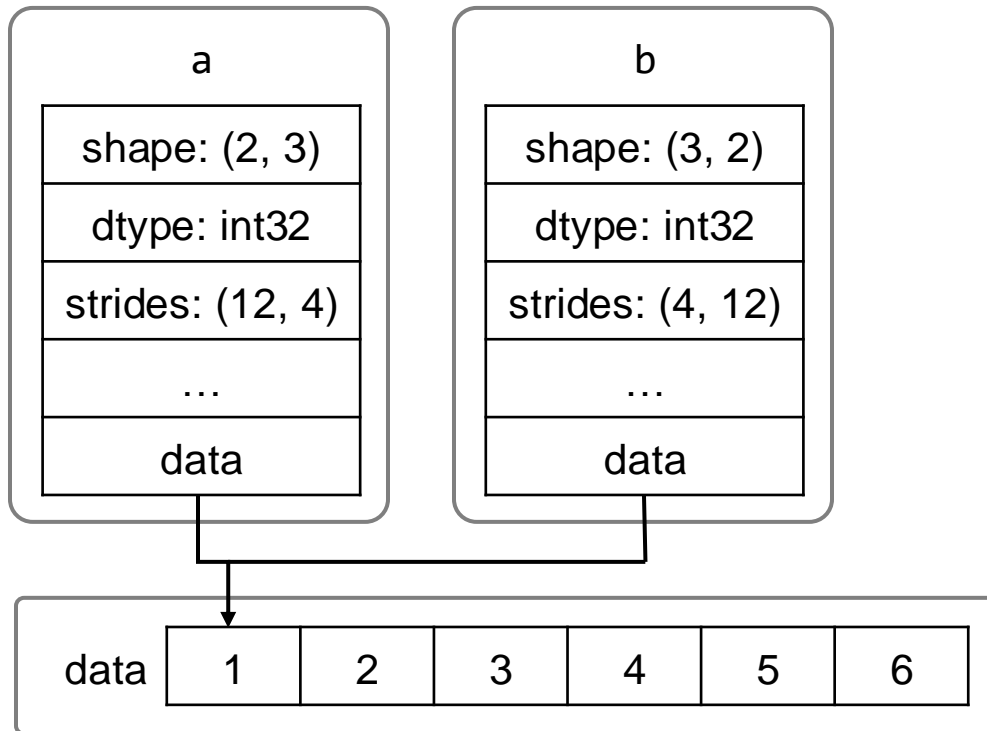
```
index = 2 * strides[0]  
       + 1 * strides[1]  
       + 4 * strides[2]  
       + 8 * strides[3]
```



NumPy: Views vs Copies

Views vs Copies

```
>>> a = np.array([[1, 2, 3], [4, 5, 6]])
>>> b = a.T # Transpose
```



a =

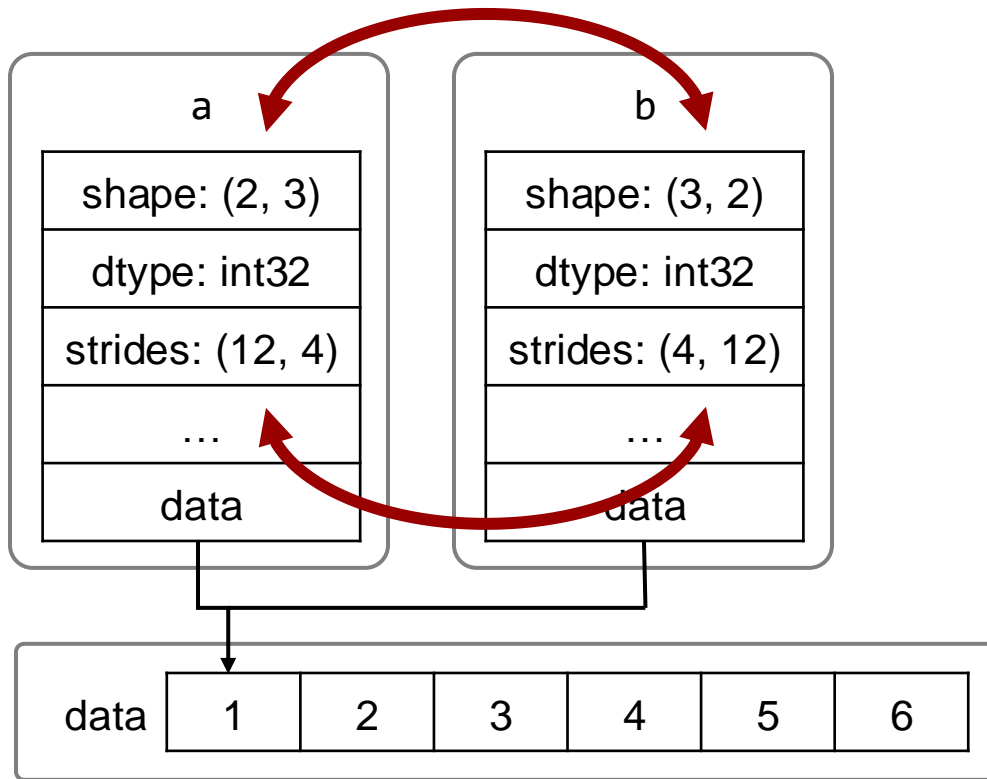
1	2	3
4	5	6

b =

1	4
2	5
3	6

Views vs Copies

```
>>> a = np.array([[1, 2, 3], [4, 5, 6]])  
>>> b = a.T # Transpose
```



a =

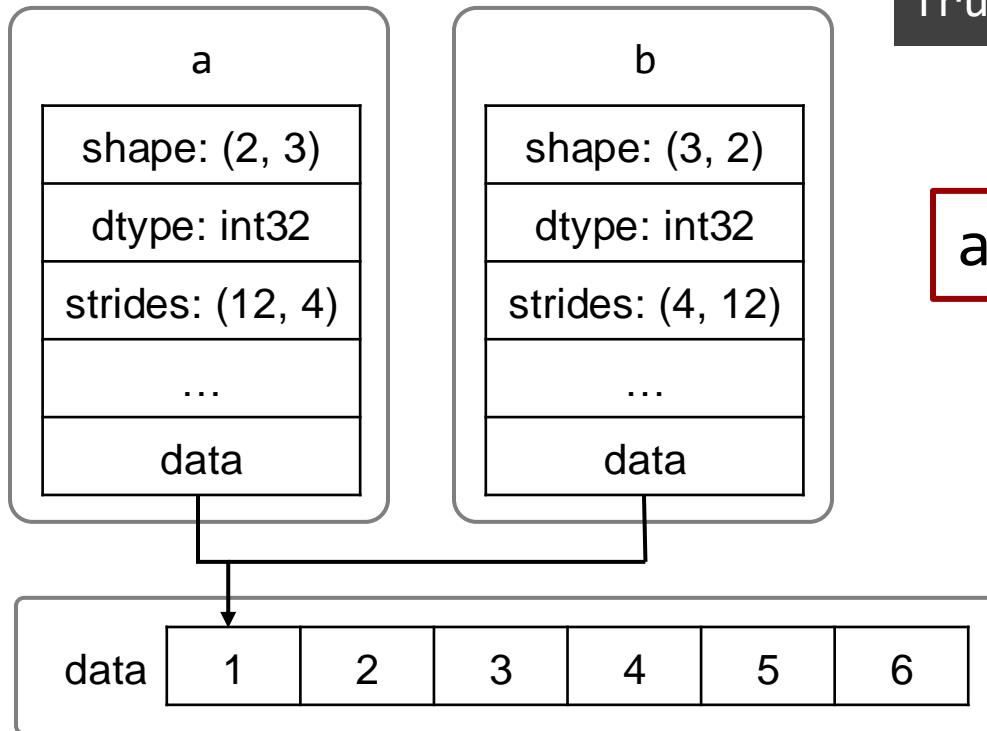
1	2	3
4	5	6

b =

1	4
2	5
3	6

Views vs Copies

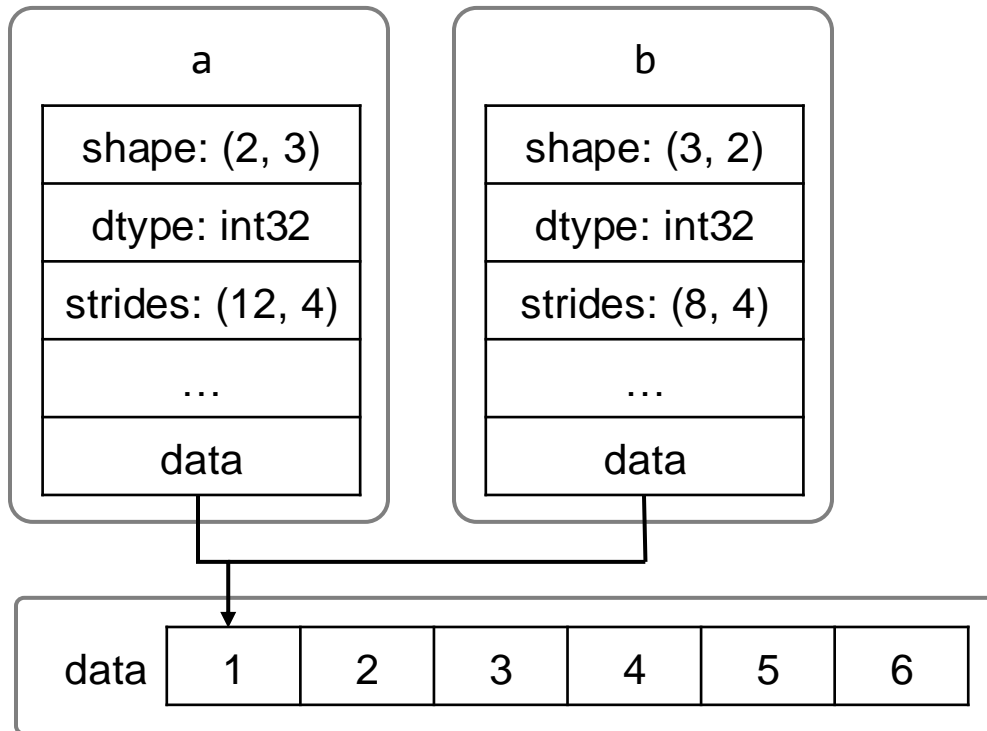
```
>>> a = np.array([[1, 2, 3], [4, 5, 6]])  
>>> b = a.T # Transpose  
>>> np.shares_memory(a, b)  
True
```



a and b are *views* to the same data

Views vs Copies

```
>>> a = np.array([[1, 2, 3], [4, 5, 6]])  
>>> b = a.reshape(3, 2)
```



`a` =

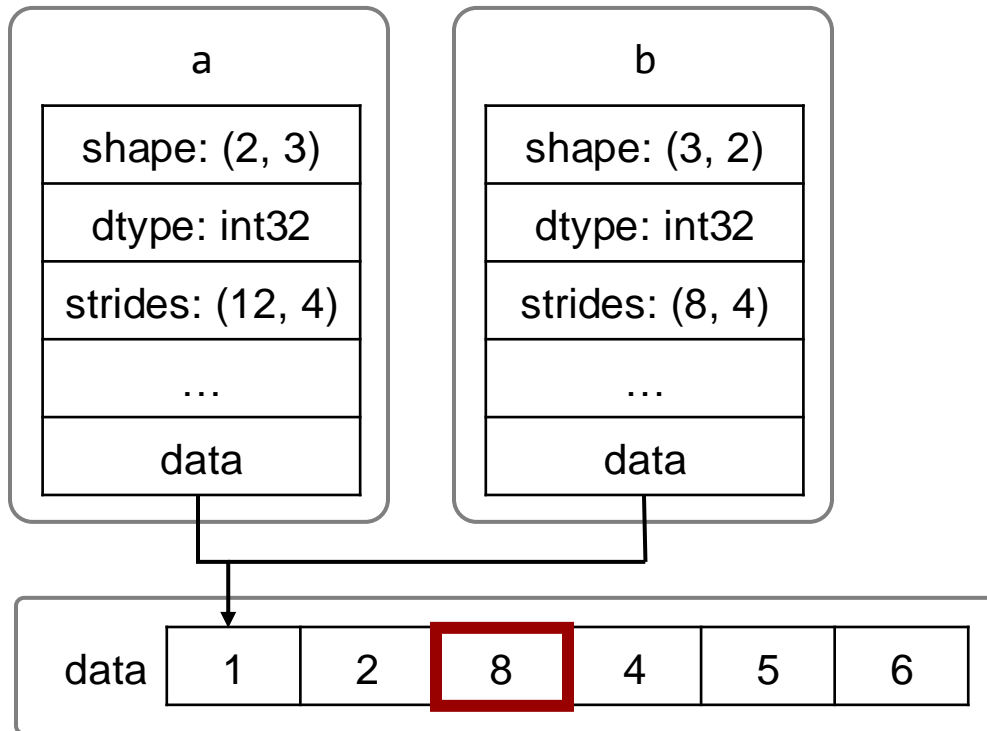
1	2	3
4	5	6

`b` =

1	2
3	4
5	6

Views vs Copies

```
>>> a = np.array([[1, 2, 3], [4, 5, 6]])  
>>> b = a.reshape(3, 2)  
>>> b[1, 0] = 8
```



a =

1	2	8
4	5	6

b =

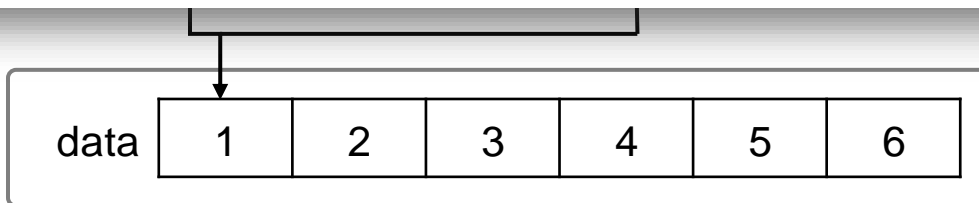
1	2
8	4
5	6

Views vs Copies

```
>>> a = np.array([[1, 2, 3], [4, 5, 6]])  
>>> b = a.reshape(3, 2)  
>>> b[1, 0] = 8
```

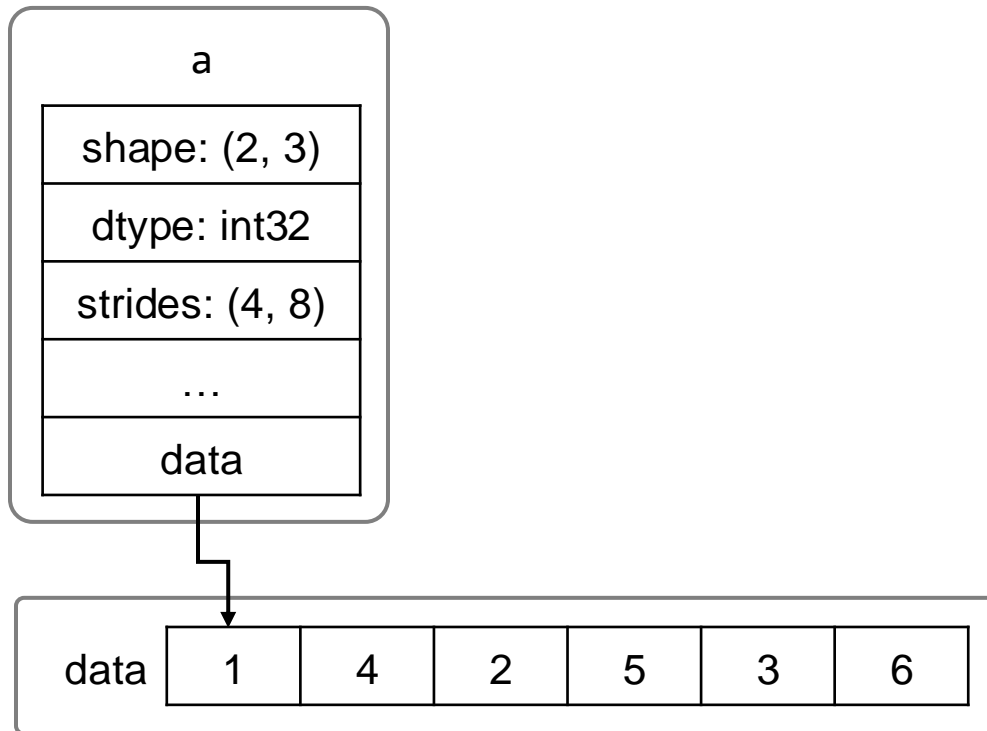
Returns: `reshaped_array : ndarray`

This will be a new view object if possible; otherwise, it will be a copy. Note there is no guarantee of the *memory layout* (C- or Fortran-contiguous) of the returned array.



Views vs Copies

```
>>> a = np.array([[1, 2, 3], [4, 5, 6]],  
                  order='F') # Fortran  
>>> b = a.reshape(3, 2)
```



Visual representation of the arrays:

`a` =

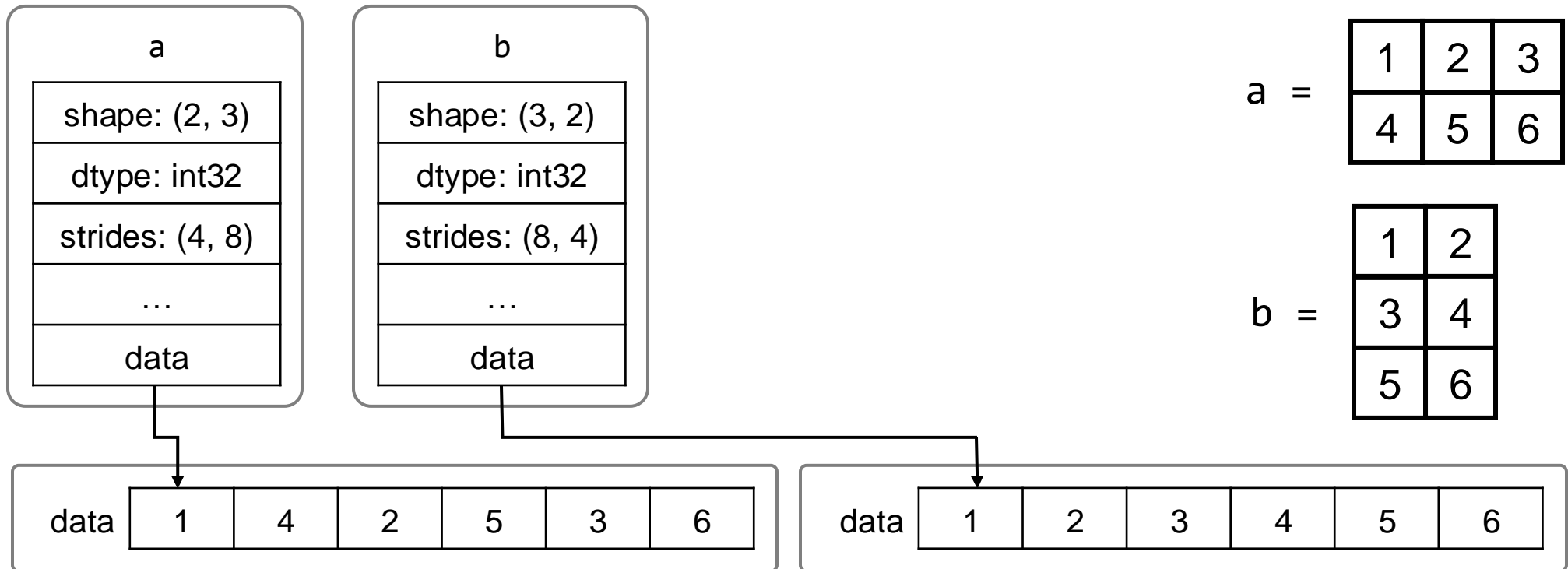
1	2	3
4	5	6

`b` =

1	2
3	4
5	6

Views vs Copies

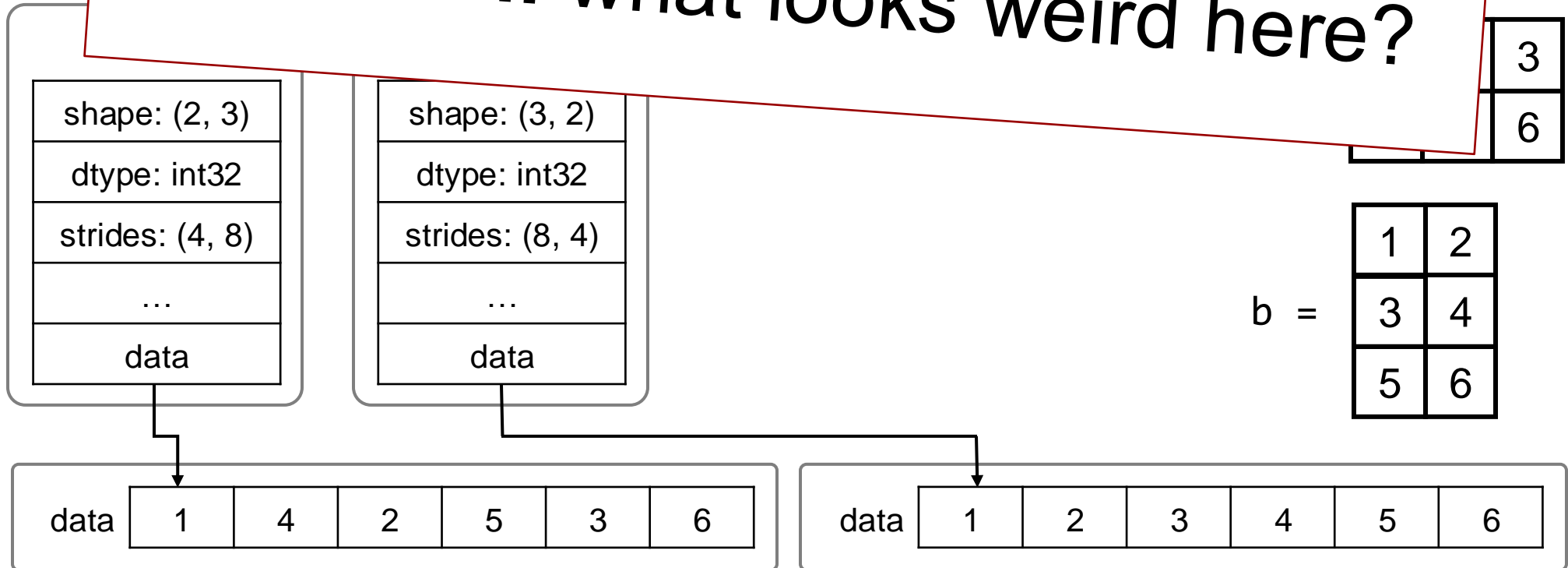
```
>>> a = np.array([[1, 2, 3], [4, 5, 6]],  
                  order='F') # Fortran  
>>> b = a.reshape(3, 2)
```



Views vs Copies

```
>>> a = np.array([[1, 2, 3], [4, 5, 6]],
                  order='F') # Fortran
```

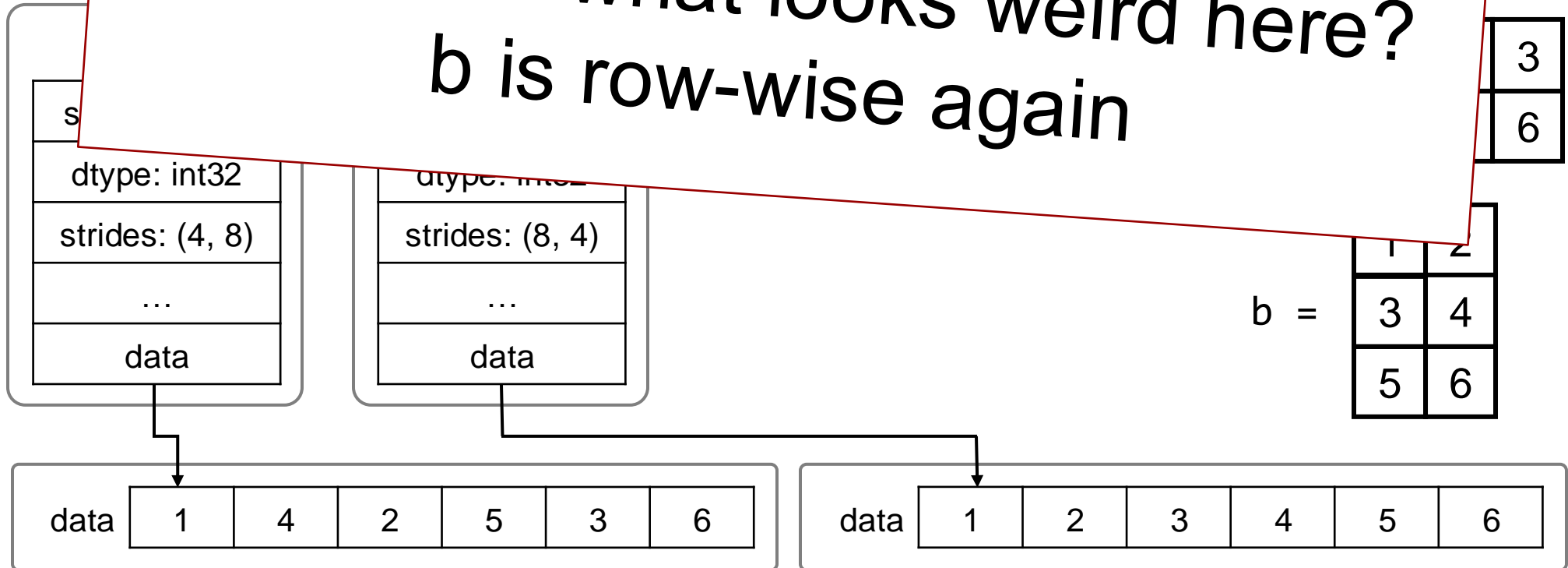
Question: what looks weird here?



Views vs Copies

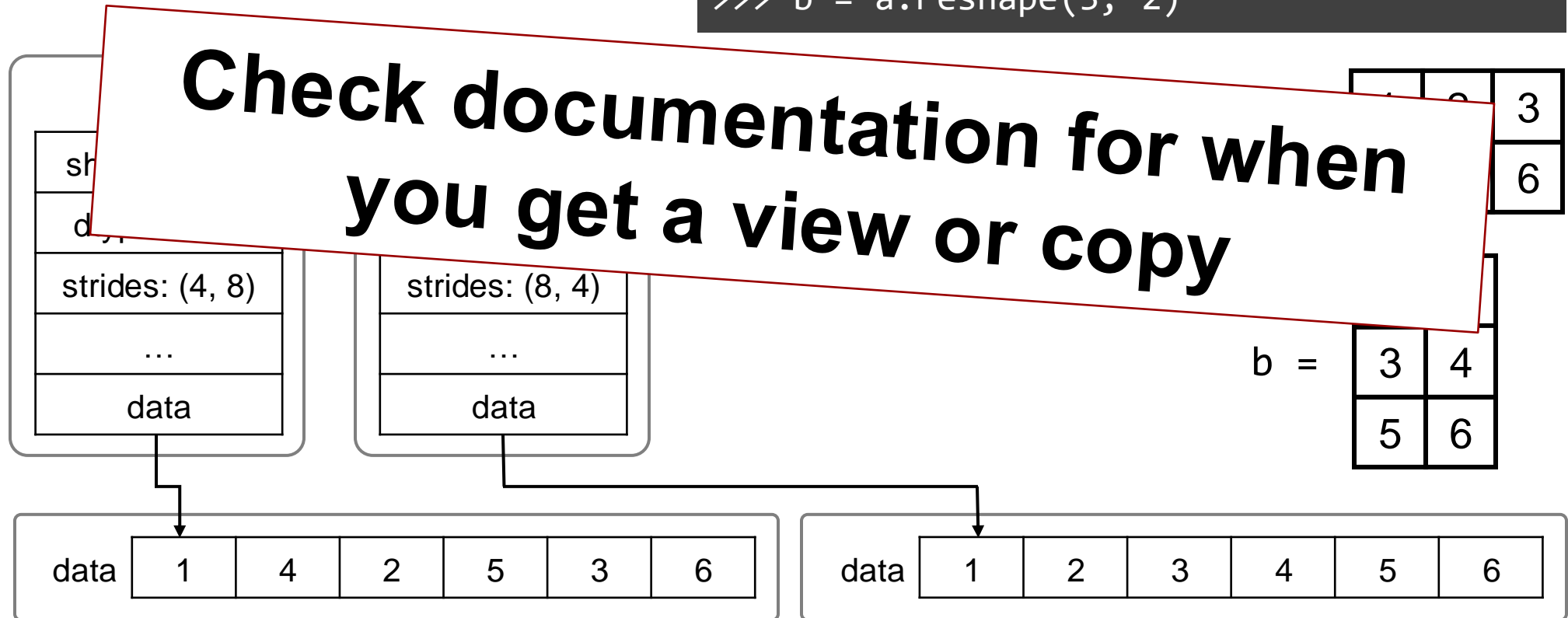
```
>>> a = np.array([[1, 2, 3], [4, 5, 6]],
                  order='F') # Fortran
```

Question: what looks weird here?
b is row-wise again



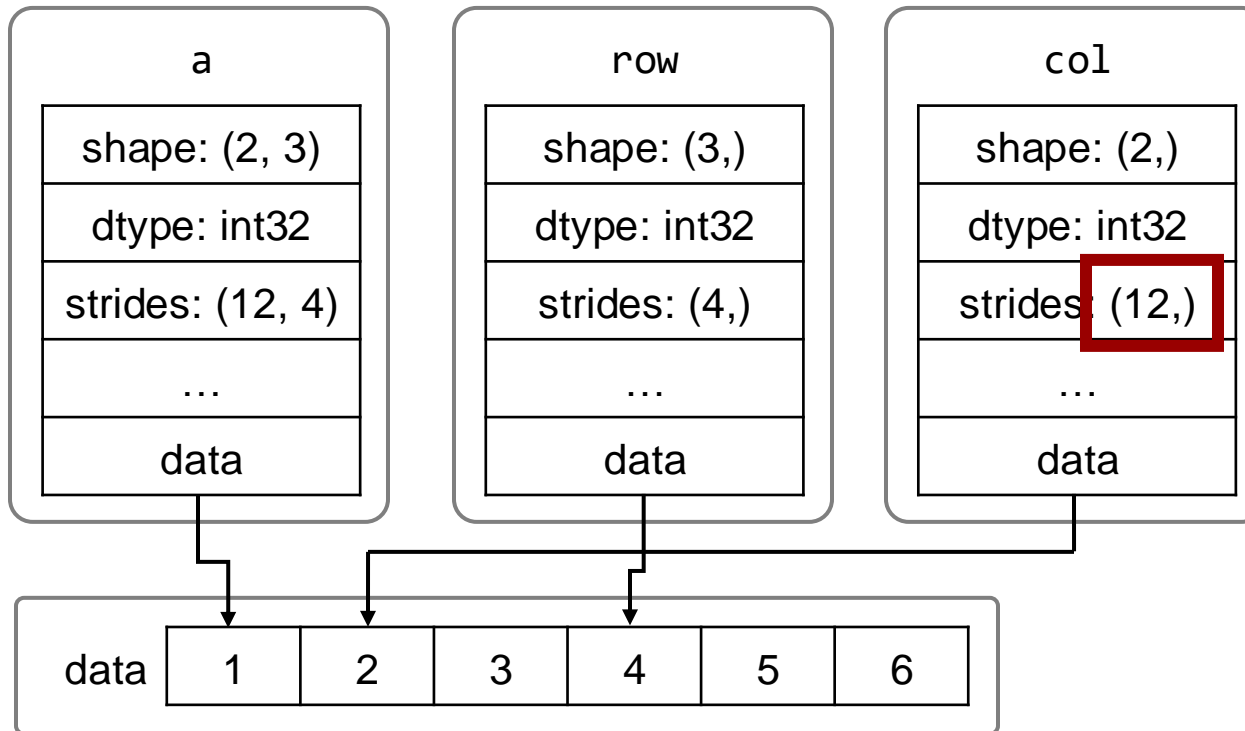
Views vs Copies

```
>>> a = np.array([[1, 2, 3], [4, 5, 6]],  
                  order='F') # Fortran  
>>> b = a.reshape(3, 2)
```



Views vs Copies: Indexing

```
>>> a = np.array([[1, 2, 3], [4, 5, 6]])  
>>> row, col = a[1, :], a[:, 1]
```

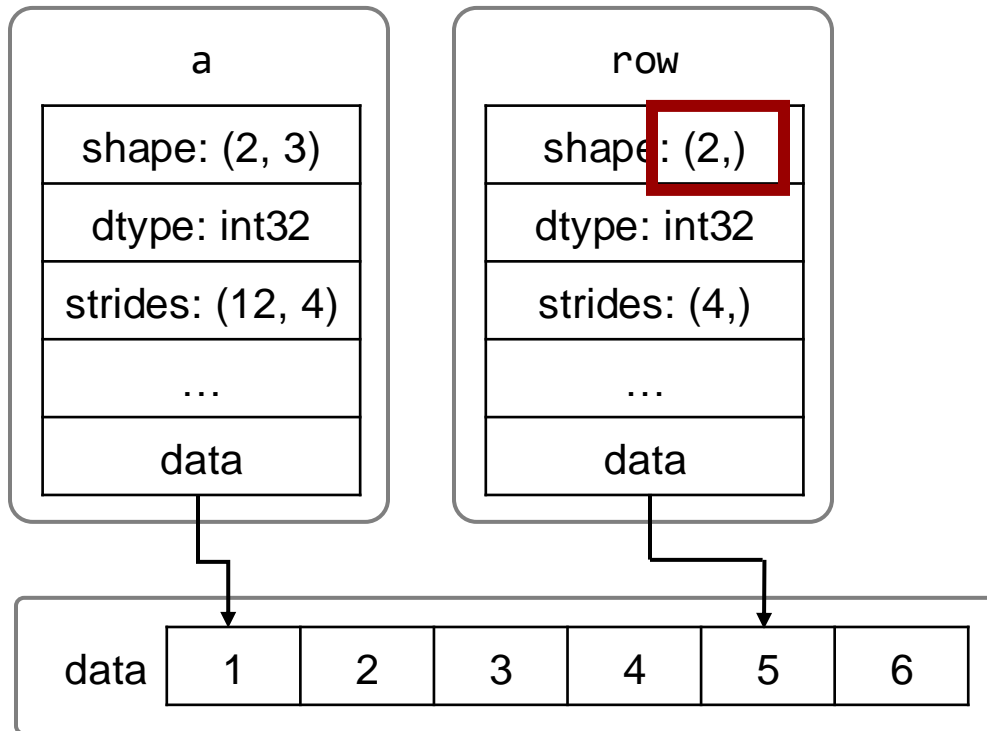


`a` =

1	2	3
4	5	6

Views vs Copies: Indexing

```
>>> a = np.array([[1, 2, 3], [4, 5, 6]])  
>>> row = a[1, 1:]; row  
array([5, 6])
```

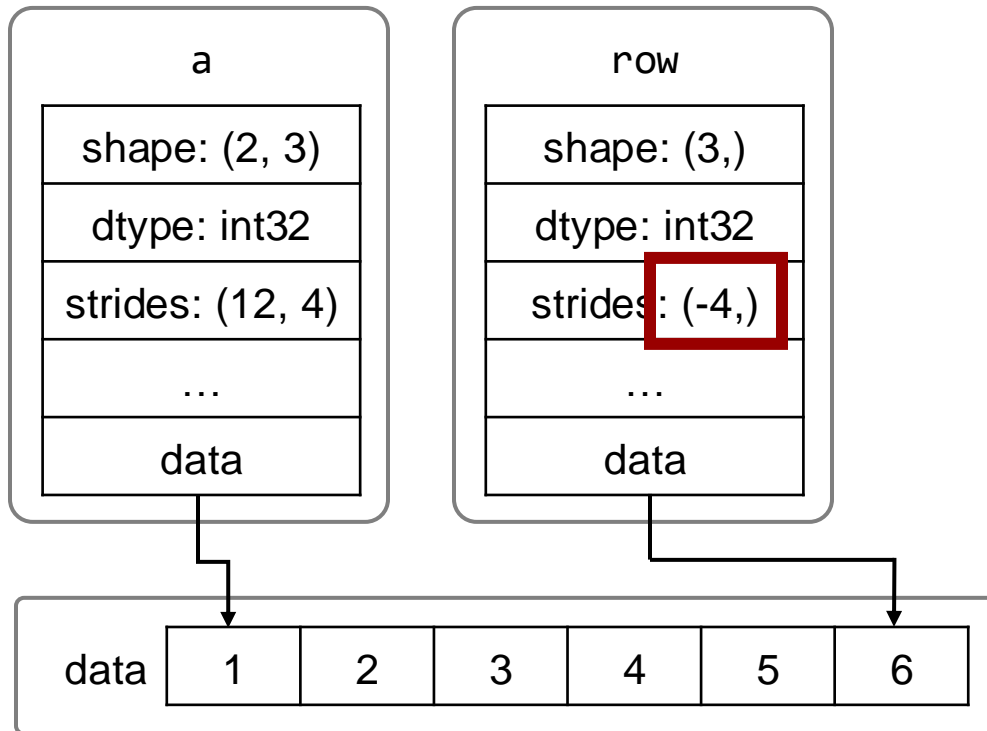


a =

1	2	3
4	5	6

Views vs Copies: Indexing

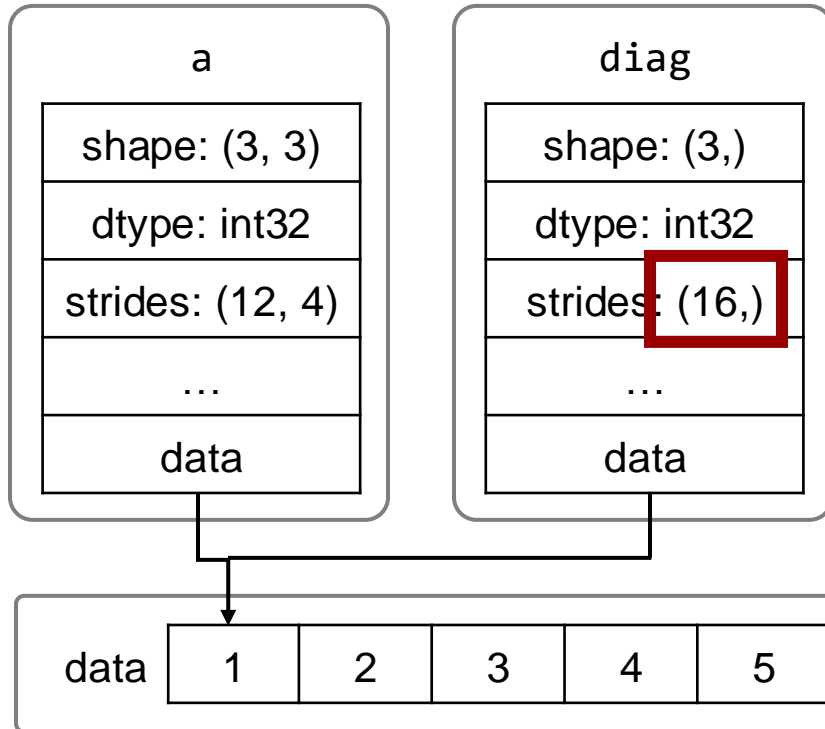
```
>>> a = np.array([[1, 2, 3], [4, 5, 6]])  
>>> row = a[1, ::-1]; row  
array([6, 5, 4])
```



a =

1	2	3
4	5	6

Views vs Copies: Indexing



```
>>> a = np.array([[1, 2, 3],  
                  [4, 5, 6],  
                  [7, 8, 9]])  
  
>>> diag = a.reshape(-1)[::4]  
>>> diag  
array([1, 5, 9])
```

a =

1	2	3
4	5	6
7	8	9



Quiz time!

[menti.com](https://www.menti.com)

Mentimeter

NumPy: Broadcasting

Broadcasting

```
>>> a = np.array([[1, 2, 3], [4, 5, 6]])  
>>> b = np.array([2, 3, 4])  
>>> a + b  
array([[ 3,  5,  7],  
       [ 6,  8, 10]])
```

a =

1	2	3
4	5	6

b =

2	3	4
---	---	---

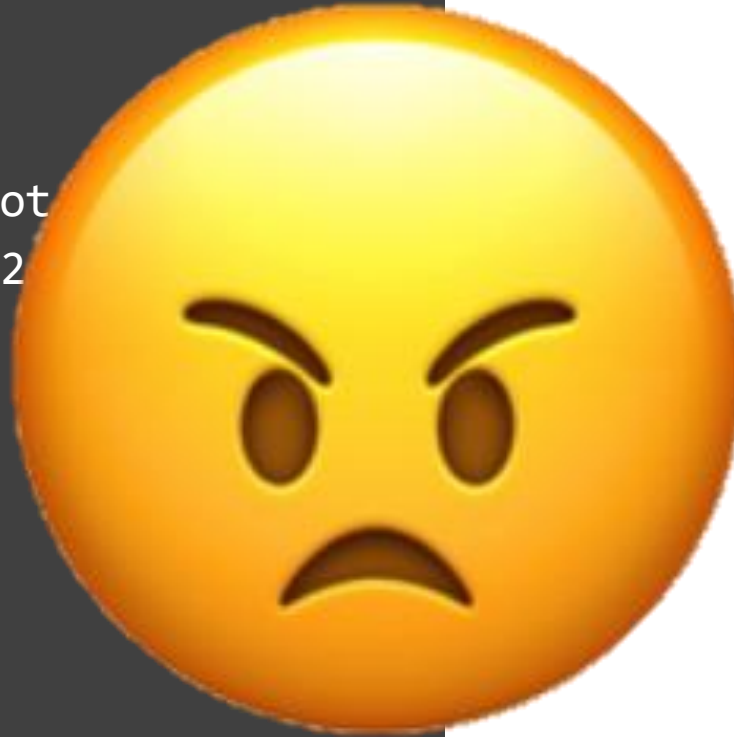
Broadcasting

```
>>> a = np.array([[1, 2, 3], [4, 5, 6]])  
>>> b = np.array([2, 3])  
>>> a + b  
...  
ValueError: operands could not be broadcast  
together with shapes (2,3) (2,)
```

a =	1	2	3
	4	5	6
b =	2	3	

Broadcasting

```
>>> a = np.array([[1, 2, 3], [4, 5, 6]])  
>>> b = np.array([2, 3])  
>>> a + b  
...  
ValueError: operands could not  
be broadcast together with shapes (2,3) (2,)
```



a =

1	2	3
4	5	6

b =

2	3
---	---

Broadcasting

```
>>> a.shape  
(2, 3, )  
>>> b.shape  
(3, )
```


Broadcasting

```
>>> a.shape  
      (2, 3,)  
>>> b.shape  
      (3,)
```

1. Line up the shapes to the right

Broadcasting

```
>>> a.shape  
(2, 3,)  
>>> b.shape  
(1, 3,)
```

1. Line up the shapes to the right
2. Left-pad the shortest with 1s

Broadcasting

```
>>> a.shape  
(2, 3,)  
>>> b.shape  
(2, 3,)
```

1. Line up the shapes to the right
2. Left-pad the shortest with 1s
3. If an element is 1, replace with larger

Broadcasting

```
>>> a.shape  
(2, 3,)  
>>> b.shape  
(2, 3,)
```

1. Line up the shapes to the right
2. Left-pad the shortest with 1s
3. If an element is 1, replace with larger
4. If all elements match: broadcasted!

Broadcasting

```
>>> a.shape  
(2, 3, )  
>>> b.shape  
(2, )
```

1. Line up the shapes to the right
2. Left-pad the shortest with 1s
3. If an element is 1, replace with larger
4. If all elements match: broadcasted!

Broadcasting

```
>>> a.shape  
(2, 3,)  
>>> b.shape  
(2,)
```

1. Line up the shapes to the right
2. Left-pad the shortest with 1s
3. If an element is 1, replace with larger
4. If all elements match: broadcasted!


Broadcasting

```
>>> a.shape  
(2, 3,)  
>>> b.shape  
(1, 2,)
```

1. Line up the shapes to the right
2. Left-pad the shortest with 1s
3. If an element is 1, replace with larger
4. If all elements match: broadcasted!

Broadcasting

```
>>> a.shape  
(2, 3,)  
>>> b.shape  
(2, 2,)
```



Mismatch!

1. Line up the shapes to the right
2. Left-pad the shortest with 1s
3. If an element is 1, replace with larger
4. If all elements match: broadcasted!

Broadcasting

```
>>> a.shape
(2, 3,)
>>> b.shape
(2,)
>>> b = b[:, None] # Add dimension
>>> b.shape
(2, 1,)
```

1. Line up the shapes to the right
2. Left-pad the shortest with 1s
3. If an element is 1, replace with larger
4. If all elements match: broadcasted!

Broadcasting

```
>>> a.shape
(2, 3,)
>>> b.shape
(2,)
>>> b = b[:, None] # Add dimension
>>> b.shape
(2, 1,)
```

1. Line up the shapes to the right
2. Left-pad the shortest with 1s
3. If an element is 1, replace with larger
4. If all elements match: broadcasted!

Broadcasting

```
>>> a.shape
(2, 3,)
>>> b.shape
(2,)
>>> b = b[:, None] # Add dimension
>>> b.shape
(2, 3,)
```

1. Line up the shapes to the right
2. Left-pad the shortest with 1s
3. If an element is 1, replace with larger
4. If all elements match: broadcasted!

Broadcasting

```
>>> a.shape  
(128, 3, 64, 64,)  
   N, C, W, H
```

Stack of 128 RGB images
of shape 64 x 64

1. Line up the shapes to the right
2. Left-pad the shortest with 1s
3. If an element is 1, replace with larger
4. If all elements match: broadcasted!

Broadcasting

```
>>> a.shape  
(128, 3, 64, 64,)  
>>> m.shape  
(3,)
```

Stack of 128 RGB images
of shape 64 x 64

1. Line up the shapes to the right
2. Left-pad the shortest with 1s
3. If an element is 1, replace with larger
4. If all elements match: broadcasted!

Broadcasting

Stack of 128 RGB images
of shape 64 x 64

```
>>> a.shape
(128, 3, 64, 64,)
>>> m.shape
(3,)
>>> a - m
...
ValueError: operands could not be broadcast
together with shapes (128,3,64,64) (3,)
```

1. Line up the shapes to the right
2. Left-pad the shortest with 1s
3. If an element is 1, replace with larger
4. If all elements match: broadcasted!

Broadcasting

Stack of 128 RGB images
of shape 64 x 64

```
>>> a.shape
(128, 3, 64, 64,)
>>> m.shape
(3,)

>>> a - m
...
ValueError: operands could not be broadcast
together with shapes (128,3,64,64) (3,)
```

1. Line up the shapes to the right
2. Left-pad the shortest with 1s
3. If an element is 1, replace with larger
4. If all elements match: broadcasted!

Broadcasting

Stack of 128 RGB images
of shape 64 x 64

```
>>> a.shape
(128, 3, 64, 64,)
>>> m.shape
( 1, 1, 1, 3,)
>>> a - m
...
ValueError: operands could not be broadcast
together with shapes (128,3,64,64) (3,)
```

1. Line up the shapes to the right
2. Left-pad the shortest with 1s
3. If an element is 1, replace with larger
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Stack of 128 RGB images
of shape 64 x 64

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>>> a.shape
(128, 3, 64, 64,)
>>> m.shape
(128, 3, 64, 3,)
>>> a - m
...
ValueError: operands could not be broadcast
together with shapes (128,3,64,64) (3,)
```

1. Line up the shapes to the right
2. Left-pad the shortest with 1s
3. If an element is 1, replace with larger
4. If all elements match: broadcasted!

Broadcasting

Stack of 128 RGB images
of shape 64 x 64

```
>>> a.shape
(128, 3, 64, 64,)
>>> m.shape
(3,)
>>> m = m[:, None, None] # Add dimensions
>>> m.shape
(3, 1, 1,)
>>> a - m
>>>
```

1. Line up the shapes to the right
2. Left-pad the shortest with 1s
3. If an element is 1, replace with larger
4. If all elements match: broadcasted!

Broadcasting

Stack of 128 RGB images
of shape 64 x 64

```
>>> a.shape
(128, 3, 64, 64,)
>>> m.shape
(3,)
>>> m = m[:, None, None] # Add dimensions
>>> m.shape
(3, 1, 1,)
>>> a - m
>>>
```

1. Line up the shapes to the right
2. Left-pad the shortest with 1s
3. If an element is 1, replace with larger
4. If all elements match: broadcasted!

Broadcasting

Stack of 128 RGB images
of shape 64 x 64

```
>>> a.shape
(128, 3, 64, 64,)
>>> m.shape
(3,)
>>> m = m[:, None, None] # Add dimensions
>>> m.shape
(1, 3, 1, 1,)
>>> a - m
>>>
```

1. Line up the shapes to the right
2. Left-pad the shortest with 1s
3. If an element is 1, replace with larger
4. If all elements match: broadcasted!

Broadcasting

Stack of 128 RGB images
of shape 64 x 64

```
>>> a.shape
(128, 3, 64, 64,)
>>> m.shape
(3,)
>>> m = m[:, None, None] # Add dimensions
>>> m.shape
(128, 3, 64, 64,)
>>> a - m
>>>
```

1. Line up the shapes to the right
2. Left-pad the shortest with 1s
3. If an element is 1, replace with larger
4. If all elements match: broadcasted!

Broadcasting

Stack of 128 RGB images
of shape 64 x 64

```
>>> a.shape
(128, 3, 64, 64,)
>>> m.shape
(3,)
>>> m = m[:, None, None] # Add dimensions
>>> m.shape
(3, 1, 1,)
>>> a - m
>>> m[None].shape
(1, 3, 1, 1,)
```

1. Line up the shapes to the right
2. Left-pad the shortest with 1s
3. If an element is 1, replace with larger
4. If all elements match: broadcasted!

Broadcasting

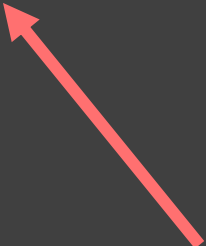
```
>>> a.shape  
(2, 3,)  
>>> b.shape  
(3,)
```

Broadcasting

```
>>> a.shape
(2, 3,)
>>> b.shape
(3,)
>>> a, b = np.broadcast_arrays(a, b)
>>> print(f"a: {a.shape}, b: {b.shape}")
a: (2, 3), b: (2, 3)
```


Broadcasting

```
>>> a.shape
(2, 3,)
>>> b.shape
(3,)
>>> a, b = np.broadcast_arrays(a, b)
>>> print(f"a: {a.shape}, b: {b.shape}")
a: (2, 3), b: (2, 3)
>>> print(f"a: {a.strides}, b: {b.strides}")
a: (24, 8), b: (0, 8)
```





Quiz time!

[menti.com](https://www.menti.com)

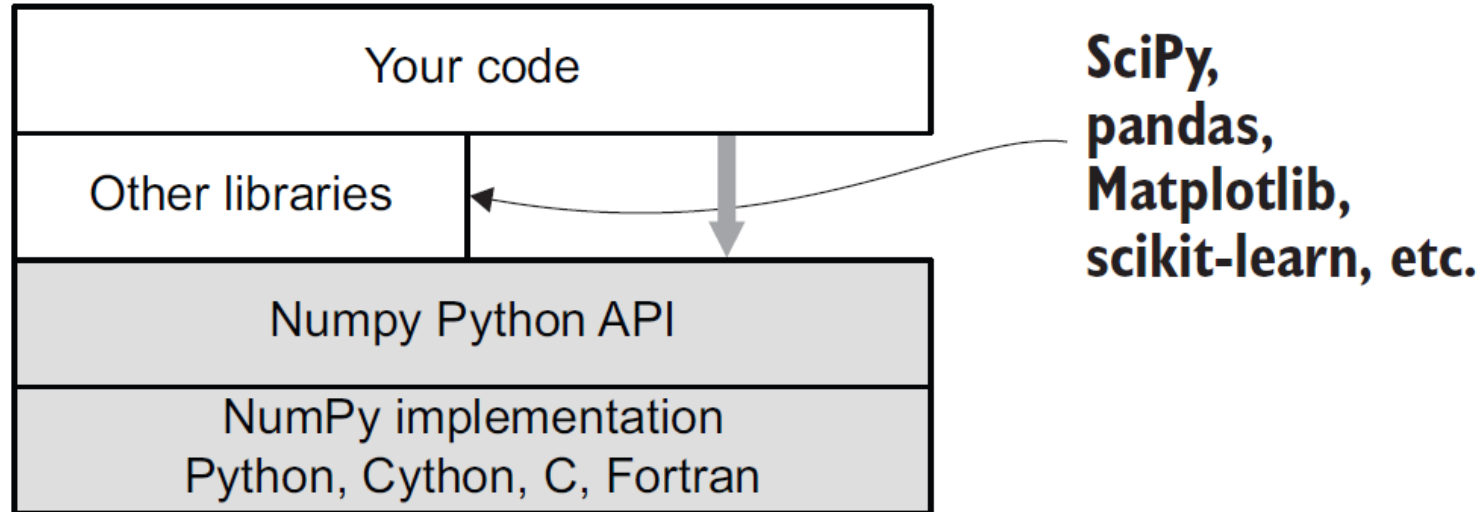
Mentimeter

NumPy Backends:

The foundation of the

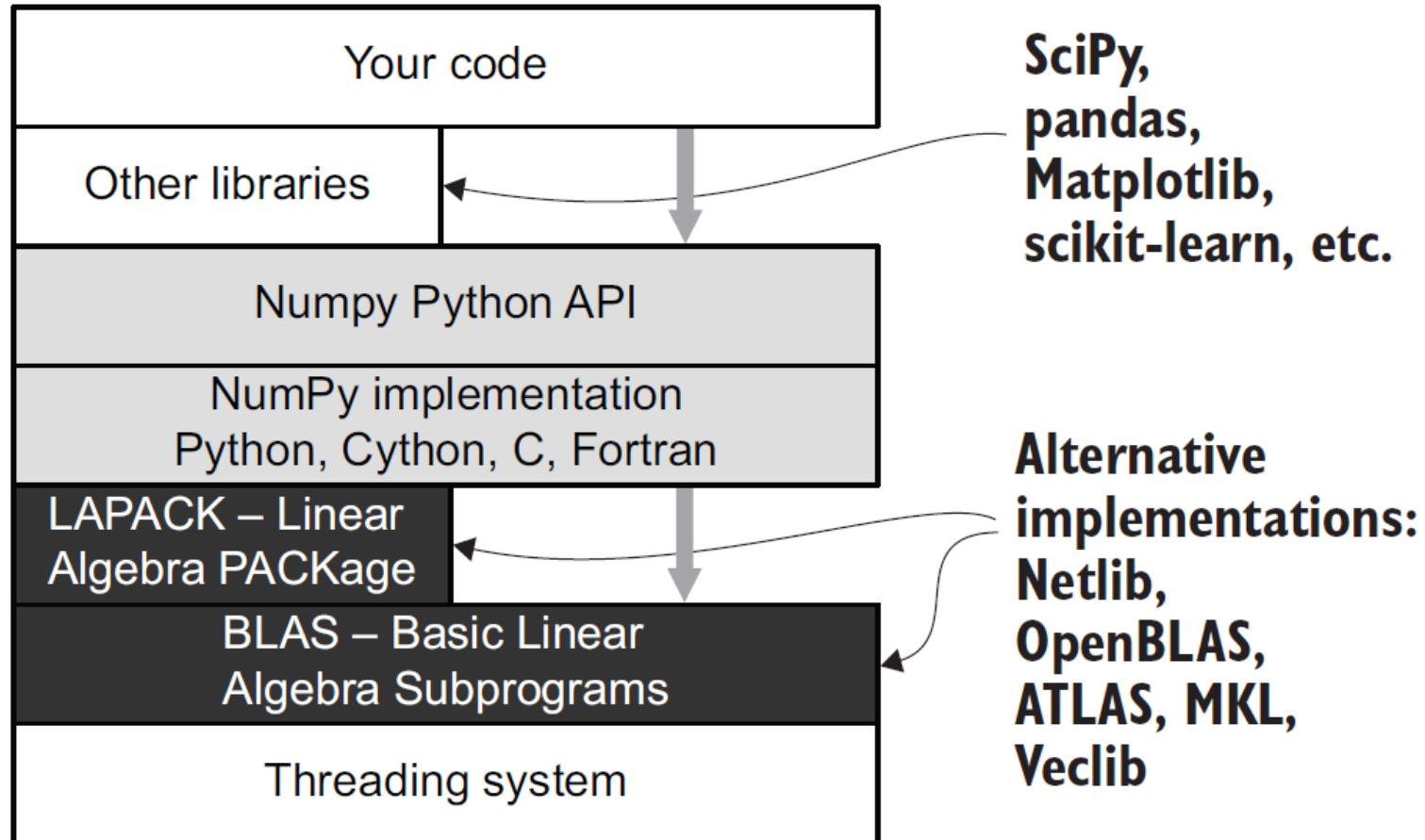
foundation

NumPy backends



Fast Python - Figure 4.11

NumPy backends



Fast Python - Figure 4.11

NumPy backends

```
$ conda install numpy
```

```
$ pip install numpy
```

```
$ conda install -c conda-forge numpy
```

NumPy backends

```
$ conda install numpy
$ python
>>> import numpy as np
>>> np.show_config()
Build Dependencies:
  blas:
    detection method: pkgconfig
    found: true
    include directory: ...
    lib directory:
    name: mkl-sdl
    openblas configuration: unknown
...
```

```
$ pip install numpy
$ python
>>> import numpy as np
>>> np.show_config()
...
"Build Dependencies": {
  "blas": {
    "name": "openblas64",
    "found": true,
    "version": "0.3.23.dev",
    "detection method": "pkgconfig",
    "include directory": ...,
    "lib directory": "/usr/local/lib",
    "openblas configuration": ...
  }
}
```

```
$ conda install -c conda-forge numpy
$ python
>>> import numpy as np
>>> np.show_config()
...
"Build Dependencies": {
  "blas": {
    "name": "blas",
    "found": true,
    "version": "3.9.0",
    "detection method": "pkgconfig",
    "include directory": ...,
    "lib directory": ...,
    "openblas configuration": ...
  }
}
```

NumPy backends: My Laptop

```
$ conda install numpy
$ python numpy_bench.py
```

Dotted two 4096x4096 matrices in:
1.76 s.

Dotted two vectors of length 524288 in:
0.28 ms.

SVD of a 2048x1024 matrix in:
0.72 s.

Cholesky decomposition of a
2048x2048 matrix in:
0.17 s.

Eigendecomposition of a 2048x2048
matrix in:
6.77 s.

```
$ pip install numpy
$ python numpy_bench.py
```

Dotted two 4096x4096 matrices in:
1.49 s.

Dotted two vectors of length 524288 in:
0.29 ms.

SVD of a 2048x1024 matrix in:
1.48 s.

Cholesky decomposition of a
2048x2048 matrix in:
0.19 s.

Eigendecomposition of a 2048x2048
matrix in:
8.01 s.

```
$ conda install -c conda-forge numpy
$ python numpy_bench.py
```

Dotted two 4096x4096 matrices in:
1.76 s.

Dotted two vectors of length 524288 in:
0.30 ms.

SVD of a 2048x1024 matrix in:
0.77 s.

Cholesky decomposition of a
2048x2048 matrix in:
0.18 s.

Eigendecomposition of a 2048x2048
matrix in:
6.92 s.

<https://web.archive.org/web/20230130105308/https://markus-beuckelmann.de/blog/boosting-numpy-blas.html>

NumPy backends: HPC with XeonGold6226R

```
$ conda install numpy
$ python numpy_bench.py
Dotted two 4096x4096 matrices in:
2.02 s.
```

```
Dotted two vectors of length 524288 in:
0.35 ms.
```

```
SVD of a 2048x1024 matrix in:
1.11 s.
```

```
Cholesky decomposition of a
2048x2048 matrix in:
0.30 s.
```

```
Eigendecomposition of a 2048x2048
matrix in:
9.23 s.
```

```
$ pip install numpy
$ python numpy_bench.py
Dotted two 4096x4096 matrices in:
2.00 s.
```

```
Dotted two vectors of length 524288 in:
0.37 ms.
```

```
SVD of a 2048x1024 matrix in:
1.24 s.
```

```
Cholesky decomposition of a
2048x2048 matrix in:
0.35 s.
```

```
Eigendecomposition of a 2048x2048
matrix in:
8.70 s.
```

```
$ conda install -c conda-forge numpy
$ python numpy_bench.py
Dotted two 4096x4096 matrices in:
1.97 s.
```

```
Dotted two vectors of length 524288 in:
0.36 ms.
```

```
SVD of a 2048x1024 matrix in:
1.12 s.
```

```
Cholesky decomposition of a
2048x2048 matrix in:
0.32 s.
```

```
Eigendecomposition of a 2048x2048
matrix in:
8.48 s.
```

<https://web.archive.org/web/20230130105308/https://markus-beuckelmann.de/blog/boosting-numpy-blas.html>

NumPy backends: HPC with XeonE5_2650v4

```
$ conda install numpy
$ python numpy_bench.py
Dotted two 4096x4096 matrices in:
4.02 s.
```

```
Dotted two vectors of length 524288 in:
0.27 ms.
```

```
SVD of a 2048x1024 matrix in:
1.30 s.
```

```
Cholesky decomposition of a
2048x2048 matrix in:
0.22 s.
```

```
Eigendecomposition of a 2048x2048
matrix in:
10.32 s.
```

```
$ pip install numpy
$ python numpy_bench.py
Dotted two 4096x4096 matrices in:
4.59 s.
```

```
Dotted two vectors of length 524288 in:
0.27 ms.
```

```
SVD of a 2048x1024 matrix in:
1.46 s.
```

```
Cholesky decomposition of a
2048x2048 matrix in:
0.22 s.
```

```
Eigendecomposition of a 2048x2048
matrix in:
10.81 s.
```

```
$ conda install -c conda-forge numpy
$ python numpy_bench.py
Dotted two 4096x4096 matrices in:
4.69 s.
```

```
Dotted two vectors of length 524288 in:
0.28 ms.
```

```
SVD of a 2048x1024 matrix in:
1.62 s.
```

```
Cholesky decomposition of a
2048x2048 matrix in:
0.24 s.
```

```
Eigendecomposition of a 2048x2048
matrix in:
12.83 s.
```

<https://web.archive.org/web/20230130105308/https://markus-beuckelmann.de/blog/boosting-numpy-blas.html>

Profiling

Profiling

”Premature optimization is the root of all evil.”
- Donald E. Knuth

Structured Programming with `go to` Statements

DONALD E. KNUTH

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A consideration of several different examples sheds new light on the problem of creating reliable, well-structured programs that behave efficiently. This study focuses largely on two issues: (a) improved syntax for iterations and error exits, making it possible to write a larger class of programs clearly and efficiently without `go to` statements; (b) a methodology of program design, beginning with readable and correct, but possibly inefficient programs that are systematically transformed if necessary into efficient and correct, but possibly less readable code. The discussion brings out opposing points of view about whether or not `go to` statements should be abolished; some merit is found on both sides of this question. Finally, an attempt is made to define the true nature of structured programming, and to recommend fruitful directions for further study.

Keywords and phrases: structured programming, `go to` statements, language design, event indicators, recursion, Boolean variables, iteration, optimization of programs, program transformations, program manipulation systems searching, Quicksort, efficiency

CR categories: 4.0, 4.10, 4.20, 5.20, 5.5, 6.1 (5.23, 5.24, 5.25, 5.27)

There is no doubt that the grail of efficiency leads to abuse. Programmers waste enormous amounts of time thinking about, or worrying about, the speed of noncritical parts of their programs, and these attempts at efficiency actually have a strong negative impact when debugging and maintenance are considered. We *should* forget about small efficiencies, say about 97 % of the time: premature optimization is the root of all evil.

Yet we should not pass up our opportunities in that critical 3 %. A good programmer will not be lulled into complacency by such reasoning, he will be wise to look carefully at the critical code; but only *after* that code has been identified. It is often a mistake to make a priori judgments about what parts of a program are really critical, since the universal experience of programmers who have been using measurement tools has been that their intuitive guesses fail. After work-

There is no doubt that the grail of efficiency leads to abuse. Programmers waste enormous amounts of time thinking about, or worrying about, the speed of noncritical parts of their programs, and these attempts at efficiency actually have a strong negative impact when debugging and maintenance are considered. We *should* forget about small details, but not about the whole. *97% of the time: pre-*

Measure first; then act

ties in that critical 3%. A good programmer will not be lulled into complacency by such reasoning, he will be *wise to look carefully at the critical code; but only after that code has been identified. It is often a mistake to make a priori judgments* about what parts of a program are really critical, since the universal experience of programmers who have been using measurement tools has been that their intuitive guesses fail. After work-

Profiling

So far...

```
t = time()
for _ in range(num_repetitions):

    2 * mat[:, 2]
t = time() - t
avg = t / num_repetitions
```


Profiling: function level

```
import time

def fast(x):
    result = x + 2
    return result

def slow(x):
    # Job security
    time.sleep(3)
    result = x * x
    return result

print(fast(10))
print(slow(10))
```

script.py

```
$ python script.py
12
100
```

Profiling: function level

```
import time

def fast(x):
    result = x + 2
    return result

def slow(x):
    # Job security
    time.sleep(3)
    result = x * x
    return result

print(fast(10))
print(slow(10))
```

script.py

```
$ python -m cProfile -s cumulative script.py
```

Run cProfile module

Profiling: function level

```
import time

def fast(x):
    result = x + 2
    return result

def slow(x):
    # Job security
    time.sleep(3)
    result = x * x
    return result

print(fast(10))
print(slow(10))
```

script.py

```
$ python -m cProfile -s cumulative script.py
```

Sort results by cumulative time

Profiling: function level

```
import time

def fast(x):
    result = x + 2
    return result

def slow(x):
    # Job security
    time.sleep(3)
    result = x * x
    return result

print(fast(10))
print(slow(10))
```

script.py

```
$ python -m cProfile -s cumulative script.py
```

```
12
```

```
100
```

```
8 function calls in 3.000 seconds
```

Ordered by: cumulative time

ncalls	totttime	percall	cumtime	percall	filename:lineno(function)
1	0.000	0.000	3.000	3.000	{built-in method builtins.exec}
1	0.000	0.000	3.000	3.000	script.py:1(<module>)
1	0.000	0.000	3.000	3.000	script.py:8(slow)
1	3.000	3.000	3.000	3.000	{built-in method time.sleep}
2	0.000	0.000	0.000	0.000	{built-in method builtins.print}
1	0.000	0.000	0.000	0.000	{method 'disable' of...
1	0.000	0.000	0.000	0.000	script.py:3(fast)

Profiling: function level

```
import time

def fast(x):
    result = x + 2
    return result

def slow(x):
    # Job security
    time.sleep(3)
    result = x * x
    return result

print(fast(10))
print(slow(10))
```

script.py

```
$ python -m cProfile -s cumulative script.py
```

```
12
```

```
100
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```
8 function calls in 3.000 seconds
```

Ordered by: cumulative time

ncalls	totttime	percall	cumtime	percall	filename:lineno(function)
1	0.000	0.000	3.000	3.000	{built-in method builtins.exec}
1	0.000	0.000	3.000	3.000	script.py:1(<module>)
1	0.000	0.000	3.000	3.000	script.py:8(slow)
1	3.000	3.000	3.000	3.000	{built-in method time.sleep}
2	0.000	0.000	0.000	0.000	{built-in method builtins.print}
1	0.000	0.000	0.000	0.000	{method 'disable' of...
1	0.000	0.000	0.000	0.000	script.py:3(fast)

Profiling: function level

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import time

def fast(x):
    result = x + 2
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script.py

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$ python -m cProfile -s cumulative script.py
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8 function calls in 3.000 seconds
```

Ordered by: cumulative time

ncalls	totttime	percall	cumtime	percall	filename:lineno(function)
1	0.000	0.000	3.000	3.000	{built-in method builtins.exec}
1	0.000	0.000	3.000	3.000	script.py:1(<module>)
1	0.000	0.000	3.000	3.000	script.py:8(slow)
1	3.000	3.000	3.000	3.000	{built-in method time.sleep}
2	0.000	0.000	0.000	0.000	{built-in method builtins.print}
1	0.000	0.000	0.000	0.000	{method 'disable' of...
1	0.000	0.000	0.000	0.000	script.py:3(fast)

Profiling: function level

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import time

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    result = x + 2
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```

script.py

```
$ python -m cProfile -s cumulative script.py
```

```
12
```

```
100
```

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8 function calls in 3.000 seconds
```

Ordered by: cumulative time

ncalls	totttime	percall	cumtime	percall	filename:lineno(function)
1	0.000	0.000	3.000	3.000	{built-in method builtins.exec}
1	0.000	0.000	3.000	3.000	script.py:1(<module>)
1	0.000	0.000	3.000	3.000	script.py:8(slow)
1	3.000	3.000	3.000	3.000	{built-in method time.sleep}
2	0.000	0.000	0.000	0.000	{built-in method builtins.print}
1	0.000	0.000	0.000	0.000	{method 'disable' of...}
1	0.000	0.000	0.000	0.000	script.py:3(fast)

Profiling: function level

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import time

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    result = x + 2
    return result

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    # Job security
    time.sleep(3)
    result = x * x
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script.py

```
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```

```
12
```

```
100
```

```
8 function calls in 3.000 seconds
```

Ordered by: cumulative time

ncalls	totttime	percall	cumtime	percall	filename:lineno(function)
1	0.000	0.000	3.000	3.000	{built-in method builtins.exec}
1	0.000	0.000	3.000	3.000	script.py:1(<module>)
1	0.000	0.000	3.000	3.000	script.py:8(slow)
1	3.000	3.000	3.000	3.000	{built-in method time.sleep}
2	0.000	0.000	0.000	0.000	{built-in method builtins.print}
1	0.000	0.000	0.000	0.000	{method 'disable' of...
1	0.000	0.000	0.000	0.000	script.py:3(fast)

Profiling: function level

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print(fast(10))
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script.py

```
$ python -m cProfile -s cumulative script.py
```

```
12
```

```
100
```

```
8 function calls in 3.000 seconds
```

Ordered by: cumulative time

ncalls	tottime	percall	cumtime	percall	filename:lineno(function)
1	0.000	0.000	3.000	3.000	{built-in method builtins.exec}
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1	3.000	3.000	3.000	3.000	{built-in method time.sleep}
2	0.000	0.000	0.000	0.000	{built-in method builtins.print}
1	0.000	0.000	0.000	0.000	{method 'disable' of...
1	0.000	0.000	0.000	0.000	script.py:3(fast)

Profiling: function level

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import time

def fast(x):
    result = x + 2
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    # Job security
    time.sleep(3)
    result = x * x
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script.py

```
$ python -m cProfile -s cumulative script.py
```

```
12
```

```
100
```

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8 function calls in 3.000 seconds
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Ordered by: cumulative time

ncalls	totttime	percall	cumtime	percall	filename:lineno(function)
1	0.000	0.000	3.000	3.000	{built-in method builtins.exec}
1	0.000	0.000	3.000	3.000	script.py:1(<module>)
1	0.000	0.000	3.000	3.000	script.py:8(slow)
1	3.000	3.000	3.000	3.000	{built-in method time.sleep}
2	0.000	0.000	0.000	0.000	{built-in method builtins.print}
1	0.000	0.000	0.000	0.000	{method 'disable' of...
1	0.000	0.000	0.000	0.000	script.py:3(fast)

Profiling: function level

```
import time

def fast(x):
    result = x + 2
    return result

def slow(x):
    # Job security
    time.sleep(3)
    result = x * x
    return result

print(fast(10))
print(slow(10))
```

script.py

```
$ python -m cProfile -s cumulative script.py
12
100
8 function calls in 3.000 seconds
```

Ordered by: cumulative time

		tottime/ncalls		cumtime/ncalls	
ncalls	tottime	percall	cumtime	percall	filename:lineno(function)
1	0.000	0.000	3.000	3.000	{built-in method builtins.exec}
1	0.000	0.000	3.000	3.000	script.py:1(<module>)
1	0.000	0.000	3.000	3.000	script.py:8(slow)
1	3.000	3.000	3.000	3.000	{built-in method time.sleep}
2	0.000	0.000	0.000	0.000	{built-in method builtins.print}
1	0.000	0.000	0.000	0.000	{method 'disable' of...}
1	0.000	0.000	0.000	0.000	script.py:3(fast)

Profiling: function level

```
import time

def fast(x):
    result = x + 2
    return result

def slow(x):
    # Job security
    time.sleep(3)
    result = x * x
    return result

print(fast(10))
print(slow(10))
```

script.py

```
$ python -m cProfile -s cumulative script.py
12
100
```

Profiling: function level

```
import time

def fast(x):
    result = x + 2
    return result

def slow(x):
    # Job security
    time.sleep(3)
    result = x * x
    return result

print(fast(10))
print(slow(10))
```

script.py

```
$ python -m cProfile -o script.prof script.py
12
100
```

Profiling: function level

```
import time

def fast(x):
    result = x + 2
    return result

def slow(x):
    # Job security
    time.sleep(3)
    result = x * x
    return result

print(fast(10))
print(slow(10))
```

script.py

```
$ python -m cProfile -o script.prof script.py
12
100
$ snakeviz script.prof
```

Profiling: function level

SnakeViz

Reset Root

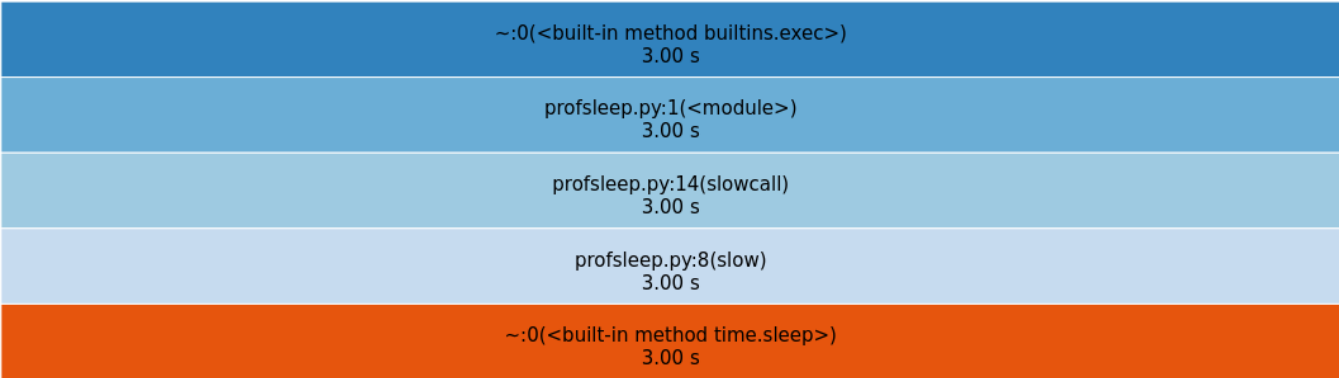
Reset Zoom

Style: Icicle

Depth: 10

Cutoff: 1 / 1000

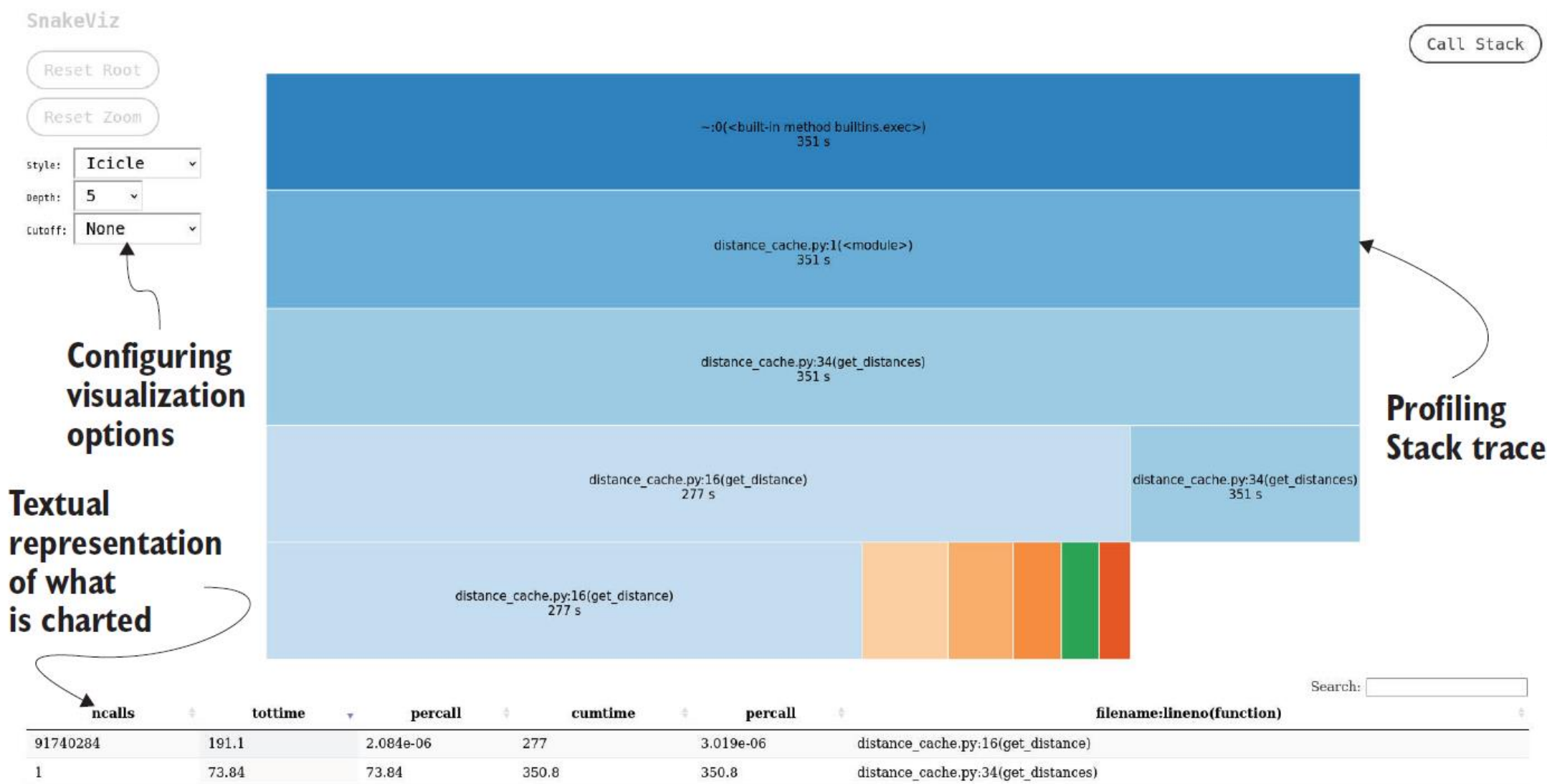
Call Stack



Search:

	ncalls		tottime		percall		cumtime		percall		filename:lineno(function)
1	3		3		3		3		3		~:0(<built-in method time.sleep>)
2	7.565e-05		3.782e-05		7.565e-05		3.782e-05		3.782e-05		~:0(<built-in method builtins.print>)
1	1.473e-05		1.473e-05		3		3		3		profsleep.py:1(<module>)
1	8.189e-06		8.189e-06		3		3		3		~:0(<built-in method builtins.exec>)

Profiling: function level



Fast Python – Figure 2.1

Profiling: line level

```
import time
```

```
def fast(x):  
    result = x + 2  
    return result
```

```
def slow(x):  
    # Job security  
    time.sleep(3)  
    result = x * x  
    return result
```

```
print(fast(10))  
print(slow(10))
```

script.py

Profiling: line level

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script.py

```
$ kernprof -l script.py
12
100
Wrote profile results to script.py.lprof
Inspect results with:
python -m line_profiler -rmt "script.py.lprof"
```

Profiling: line level

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$ python -m line_profiler -rmt "script.py.lprof"
```

```
Timer unit: 1e-06 s
```

```
Total time: 3.00014 s
```

```
File: script.py
```

```
Function: slow at line 7
```

Line #	Hits	Time	Per Hit	% Time	Line Contents
7					@profile
8					def slow(x):
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10	1	3000132.9	3e+06	100.0	time.sleep(3)
11	1	2.2	2.2	0.0	result = x * x
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3.00 seconds - script.py:7 - slow
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Profiling: when to use what

Timing

Low overhead, very manual, no locations

Good for measuring performance

Function profiling

Low-ish overhead, automatic, rough locations

Good for zooming in on problem areas

Line profiling

High overhead, mostly automatic, precise locations

Good for pinning the exact problem, but should not be the start

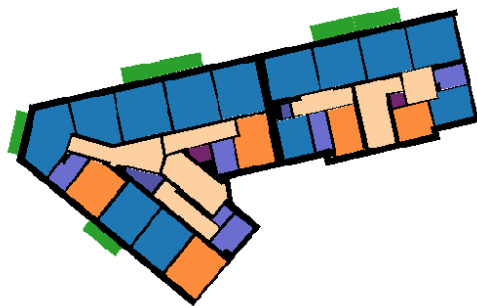
Mini-project

Mini-project now on Learn

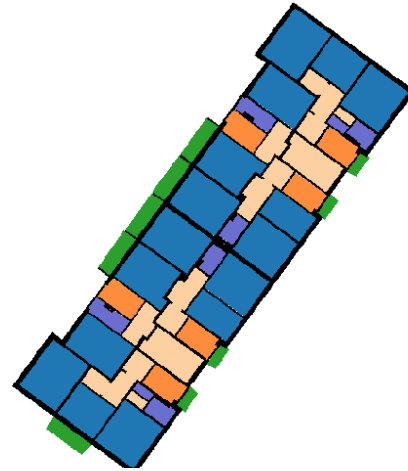
- Hand-in on Learn
04.05.2025 (Sunday of semester week 12) 23:55
- Hand-in: PDF report and zip-file with code + job scripts in groups of 3-4. Make groups on Learn.
- Must *hand in and pass* project to attend the exam!

Mini-project: Wall Heating

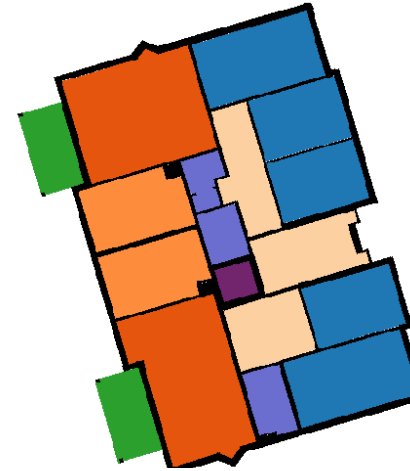
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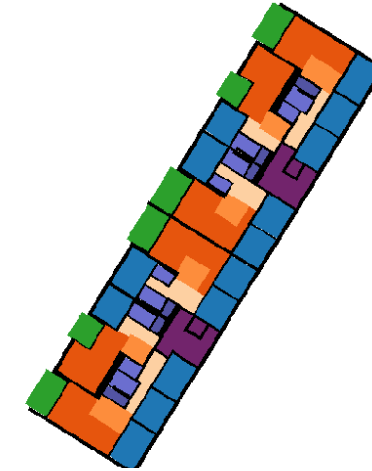
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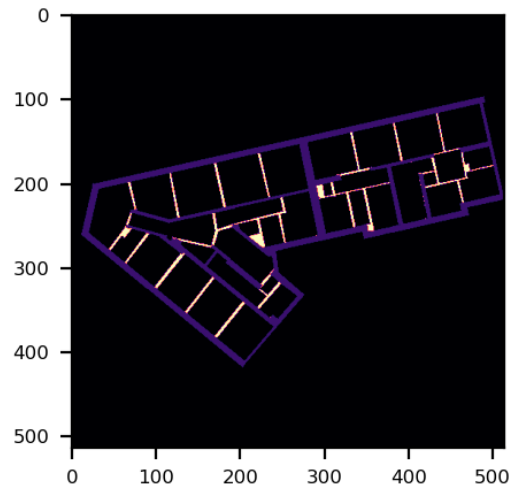
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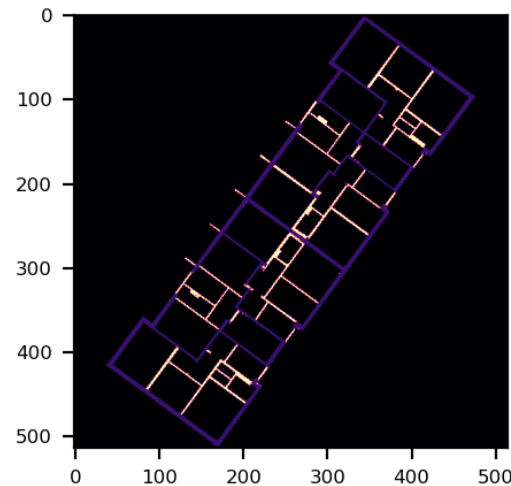
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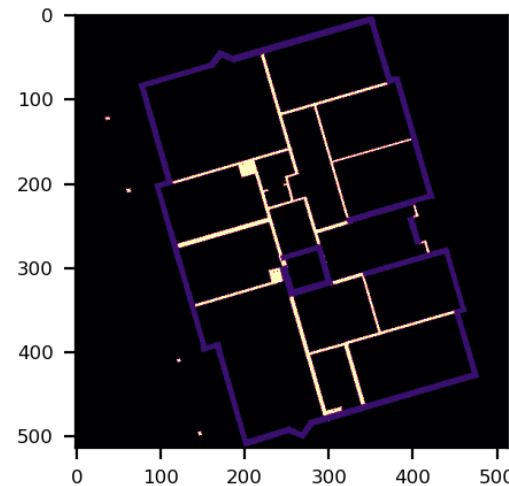
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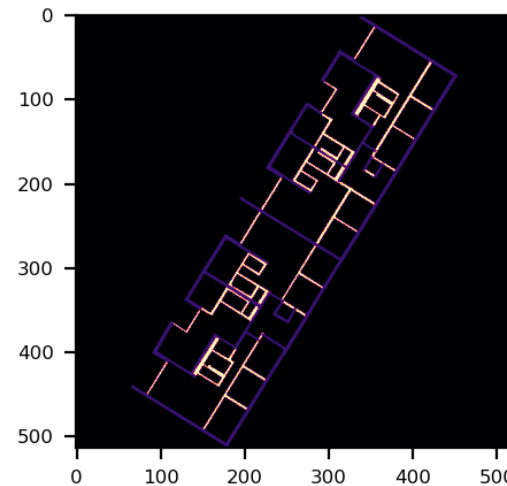
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ID: 10786

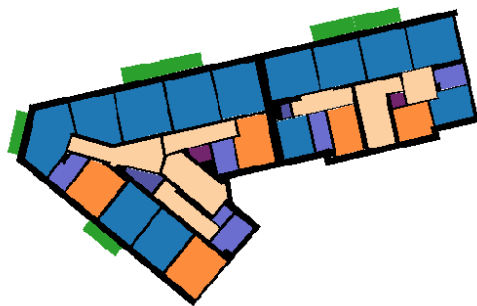


ID: 11117

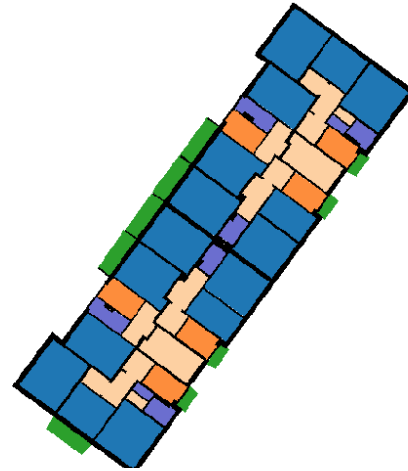


Mini-project: Wall Heating

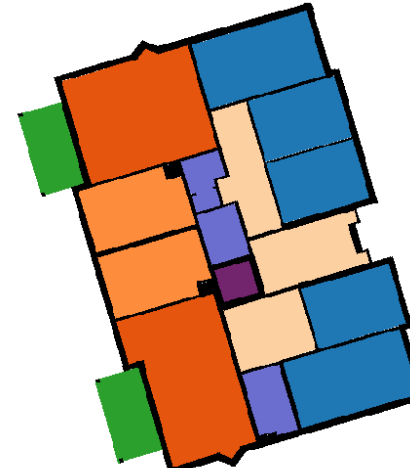
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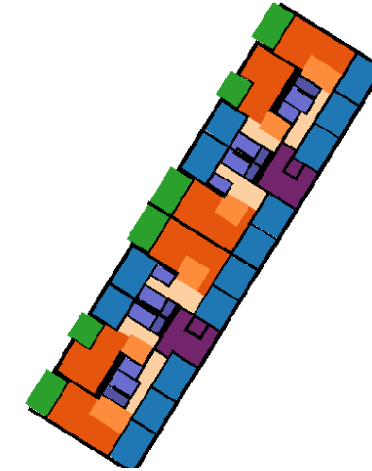
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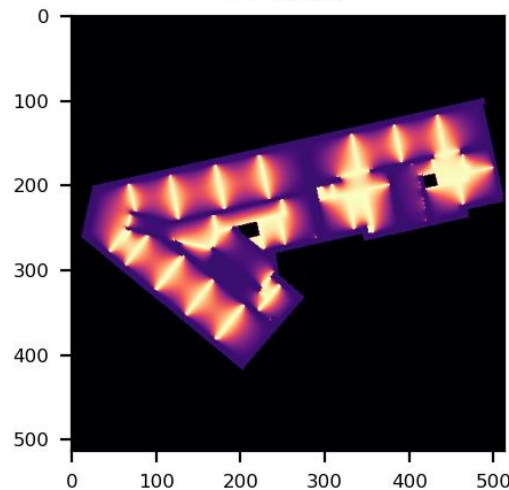
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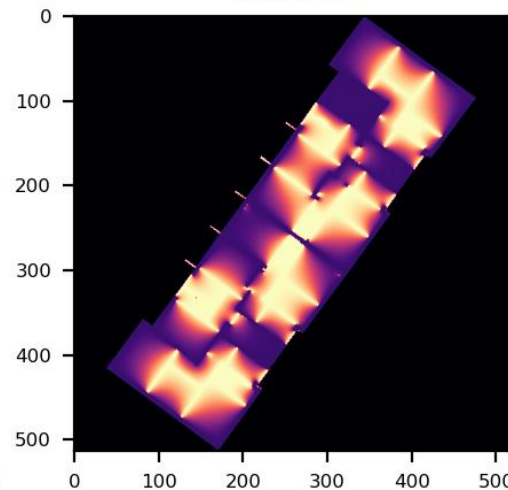
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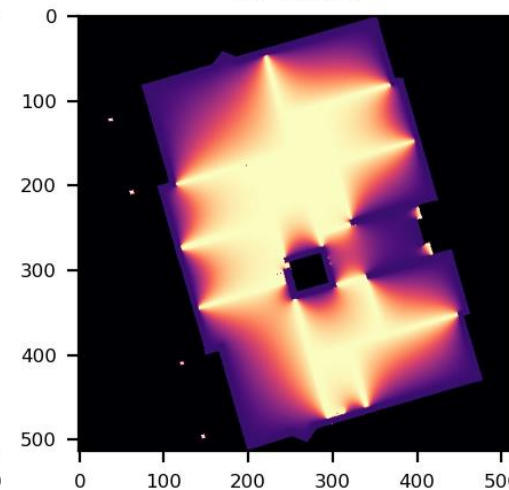
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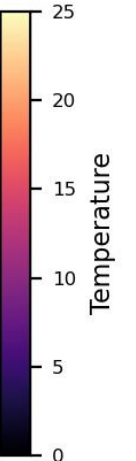
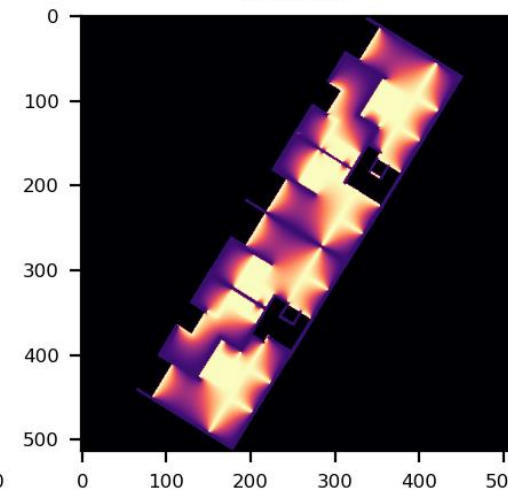
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Mini-project: Wall Heating

ID: 10000

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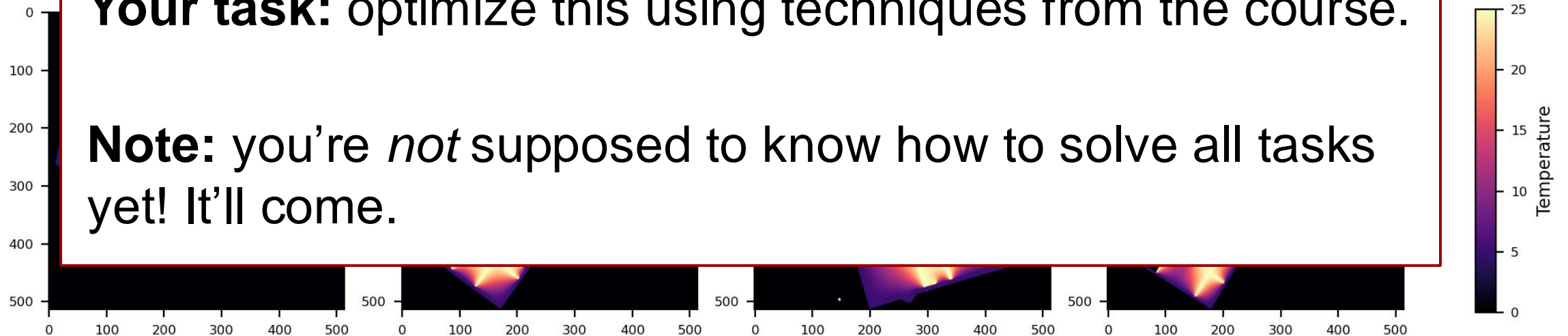
ID: 11117

Project has sample script to simulate heat and compute summary statistics.

Please do **NOT** run sample script for all floorplans!

Your task: optimize this using techniques from the course.

Note: you're *not* supposed to know how to solve all tasks yet! It'll come.



Today's exercise

Play with profiling and NumPy optimizations

- Use the different profilers to discover hotspots
- Fix them!
- Data is prepared on the cluster:
`/dtu/projects/02613_2025/data/locations/`

Useful concepts

Add dimension to NumPy array

```
x[:, None]    # Add dimension at end  
x[None]       # Add dimension at begin  
x[:, None, :] # Add dimension in the middle
```

cProfile for function profiling

```
python -m cProfile -s cumulative script.py # In terminal  
  
python -m cProfile -o script.prof script.py # In snakeviz GUI  
snakeviz script.prof
```

kernprof for line profiling

```
@profile # Decorator for profiled functions  
  
kernprof -l script.py # 1. Run profiling  
python -m line_profiler -rmt "script.py.lprof" # 2. Show results
```

Change to work node

```
linuxsh
```

Submit job script

```
bsub < submit.sh
```

Job status

```
bstat / bjobs
```

Check job output

```
bpeek / bpeek <JOBID>
```

Kill job

```
bkill <JOBID>
```