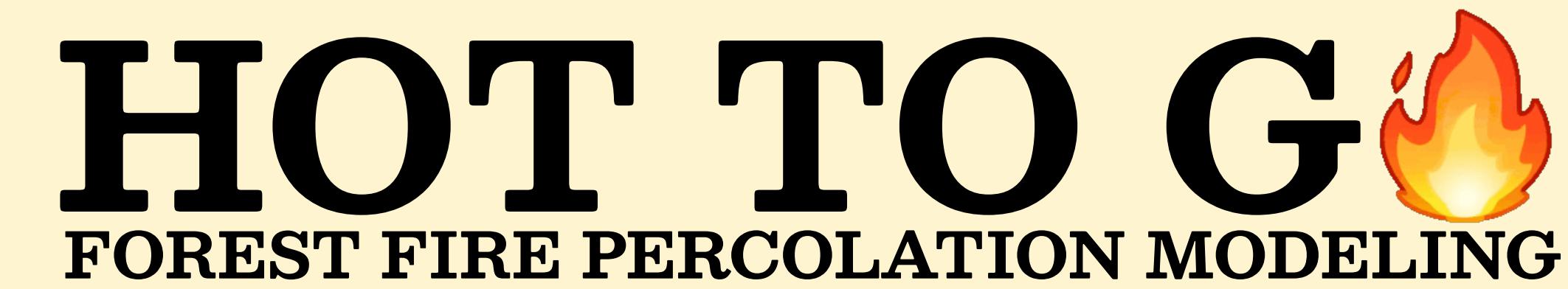


# Complex System Simulation



Intro

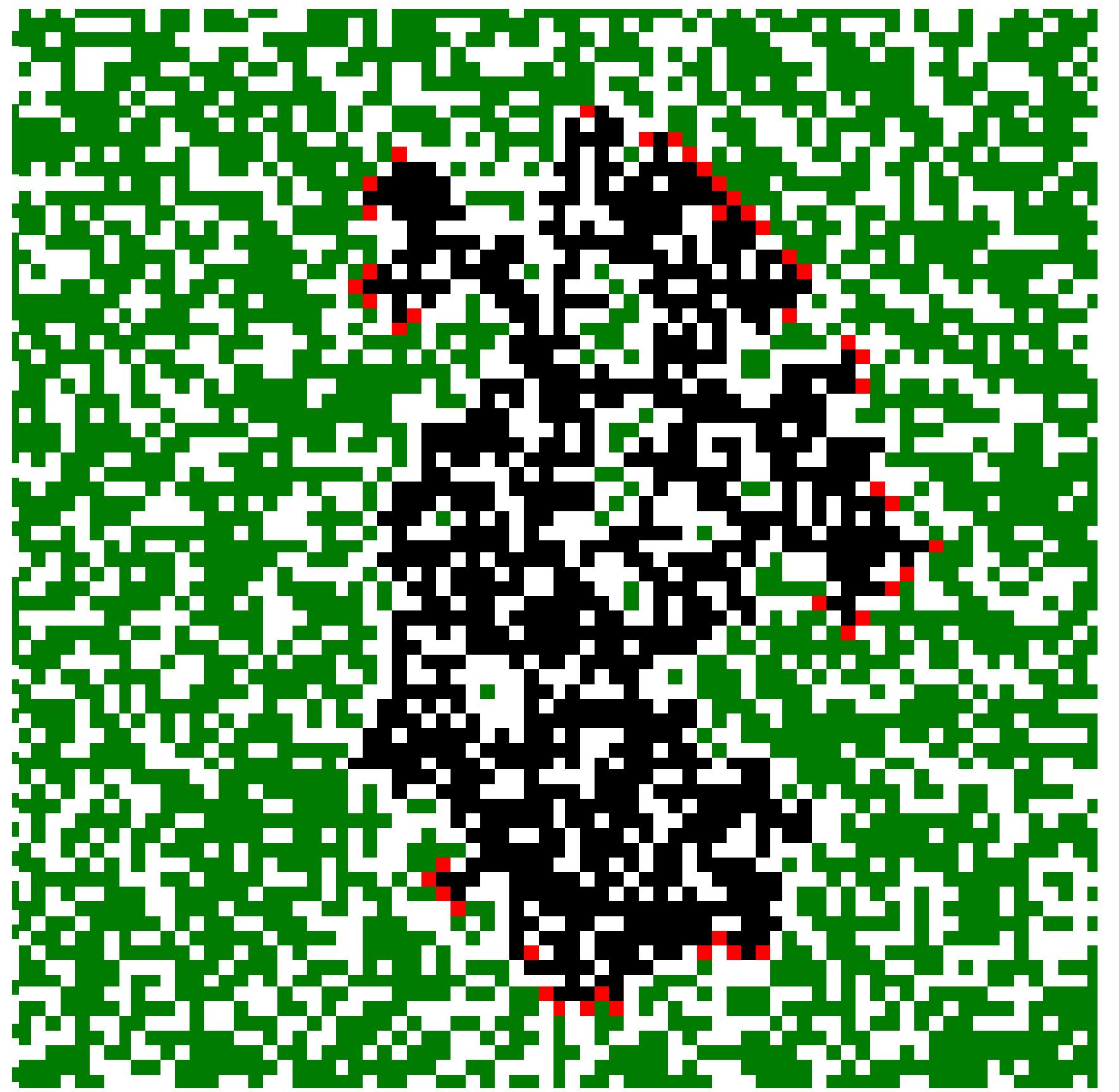
The Model

Results

MIKKO BRANDON, VICTORIA PETERSON, YOAD VAN PRAAG, RINSKE OSKAMP



# Introduction



# Research Questions

1

Do **forest fires** exhibit characteristics of **criticality**?

2

How does introducing **wind** into the system affect the critical density and does it still exhibit criticality?

3

How do **environmental influences** affect the critical density and does it still exhibit criticality?

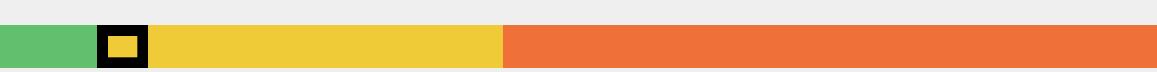
4

How does a combination of a variety of **burnable vegetation types** and environmental influences affect the critical density and does it still exhibit criticality?



# Model

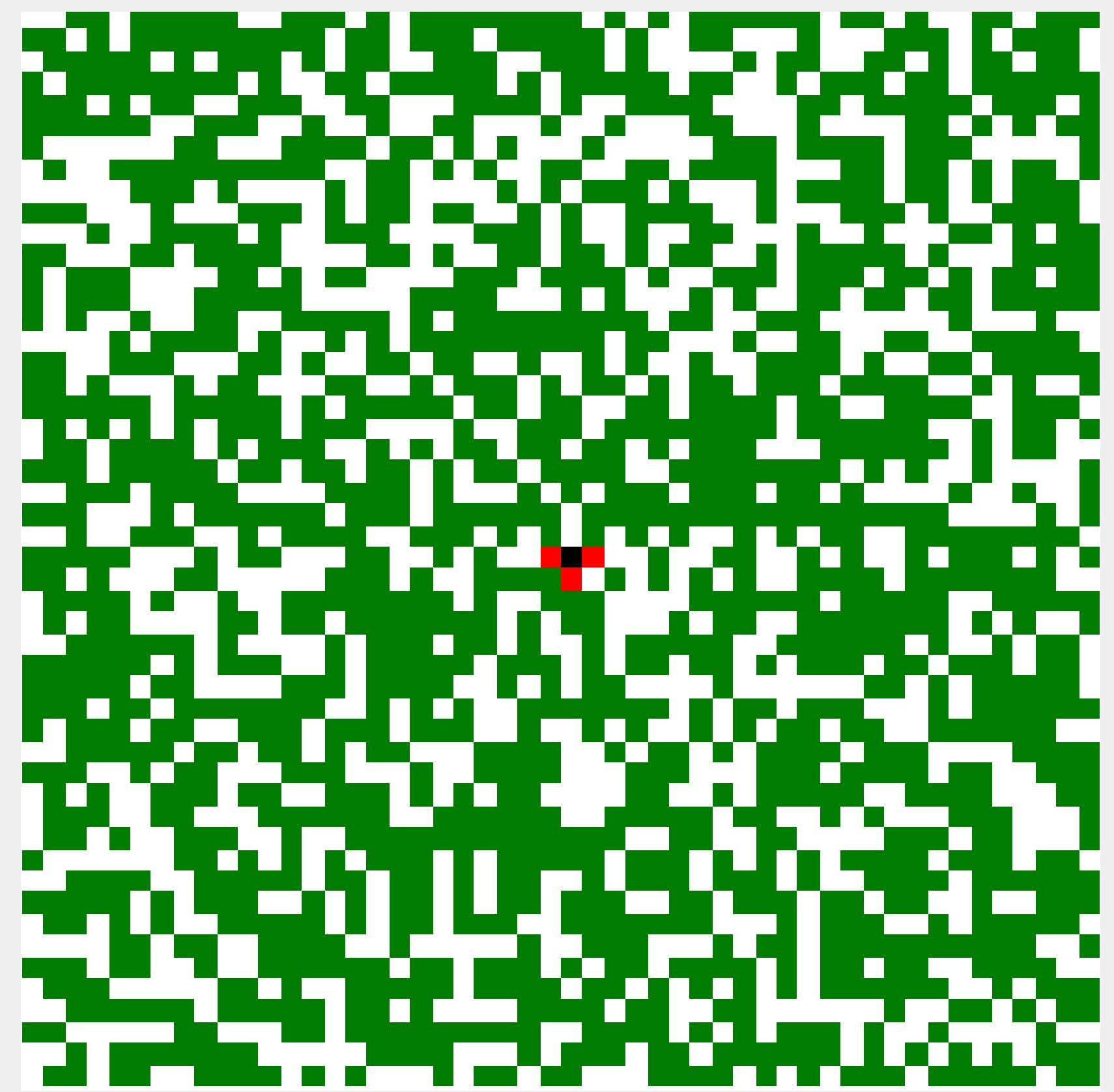
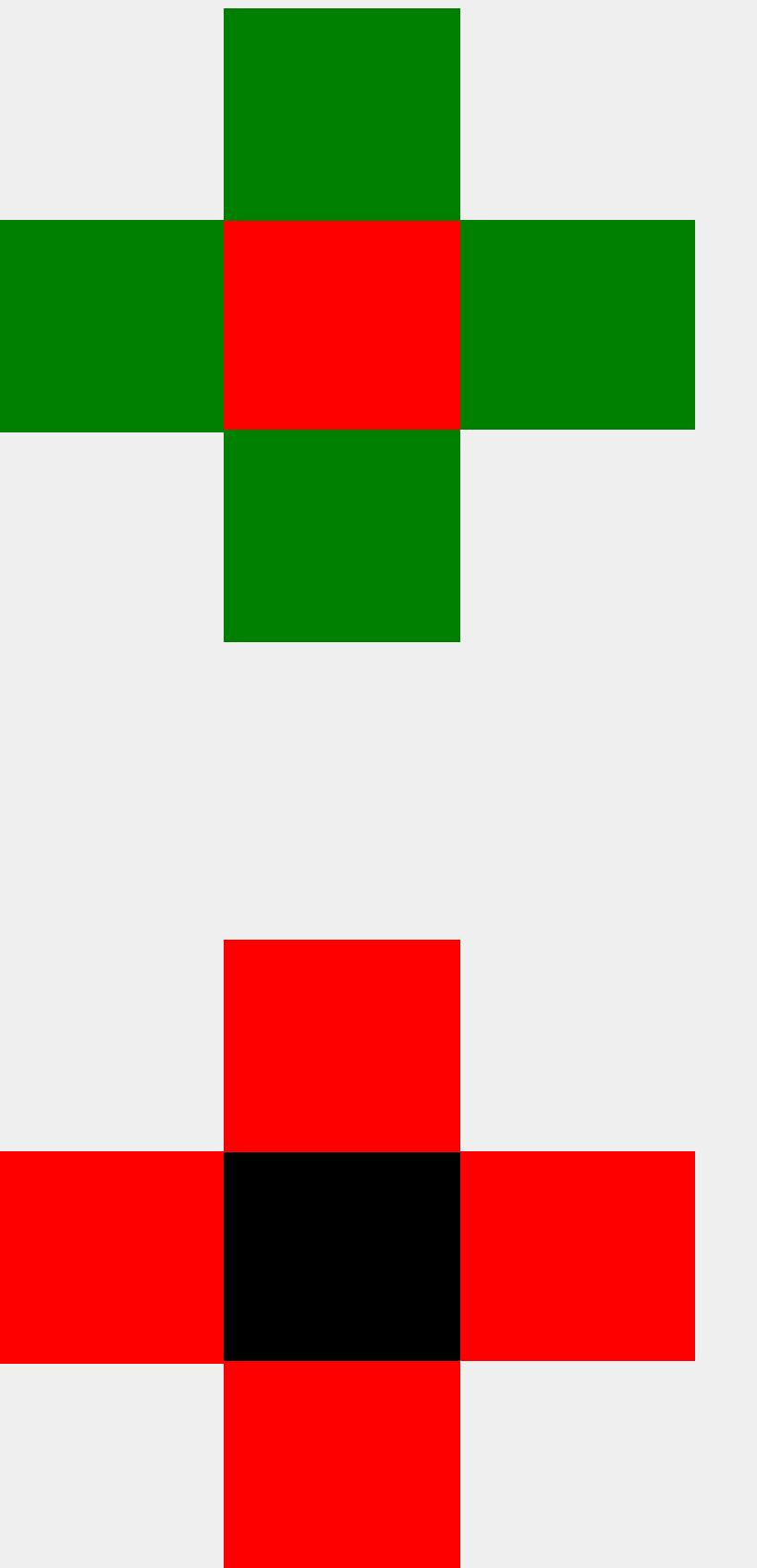
Modeling a forest fire and its  
reaction to external factors



# The Model

Forest Fire model  
control parameters

Grid size	50
Density	0.6



- Tree
- Burning site
- Burned site
- Empty site

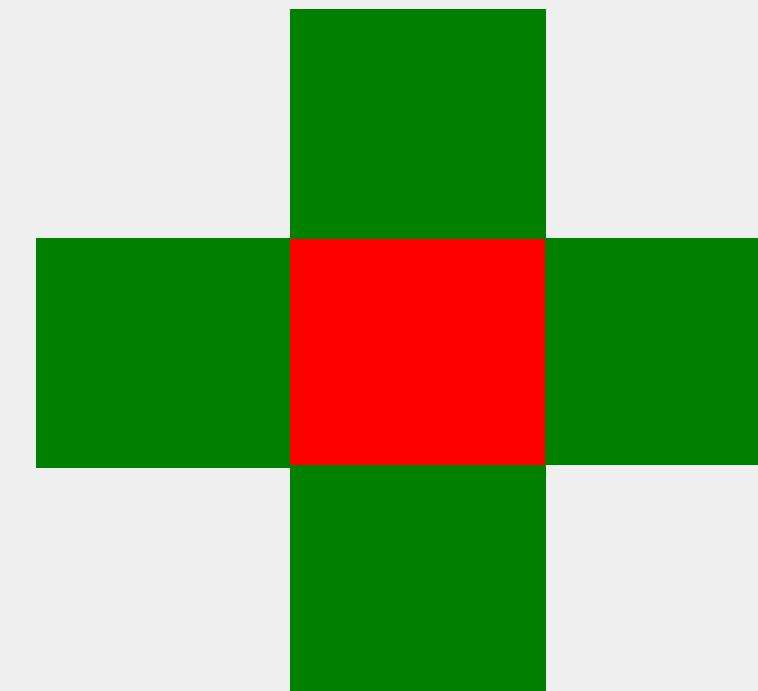


# Wind in the Model

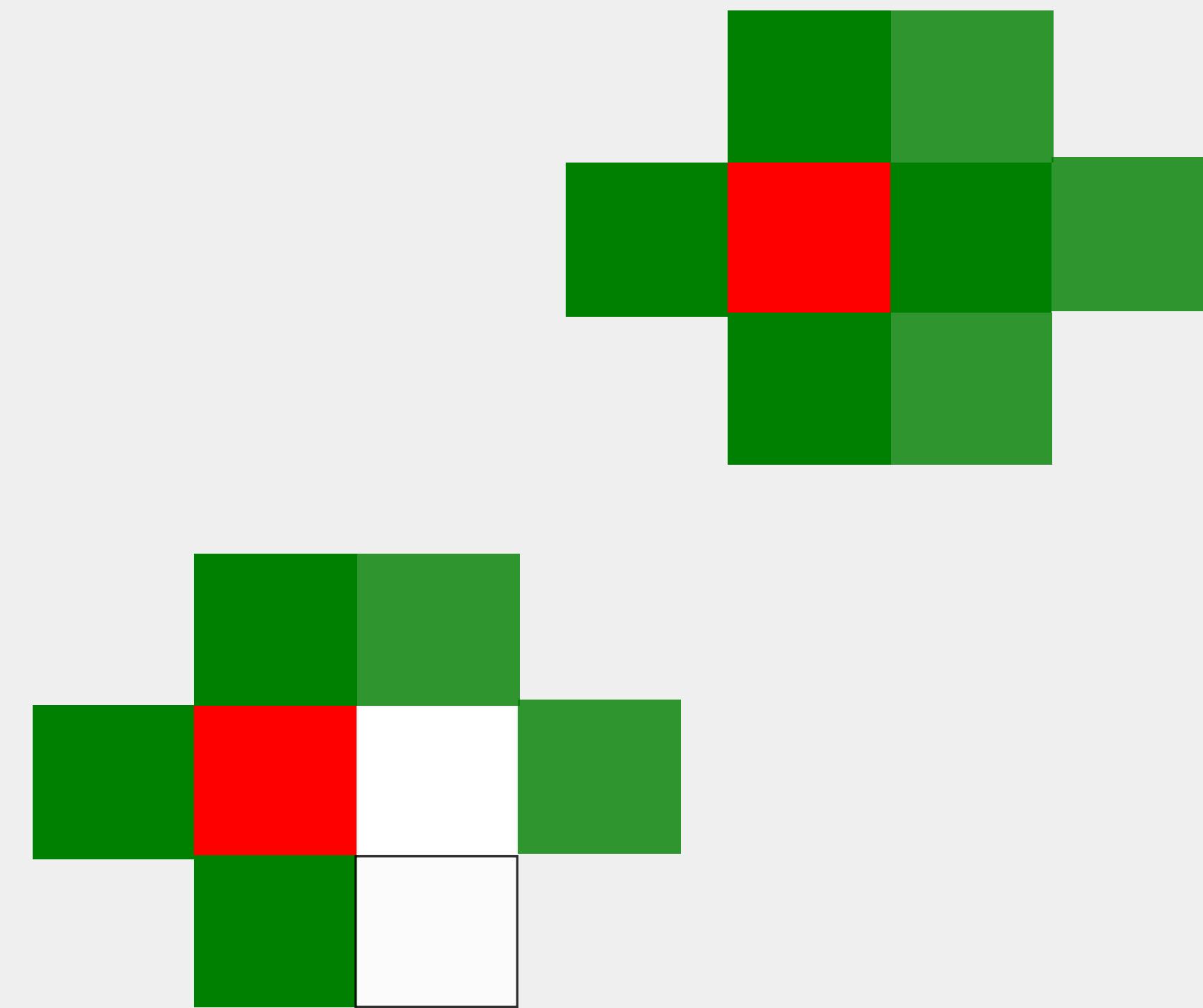
Forest Fire model  
control parameters

Grid size	50
Density	0.6
Wind	Yes

Neighborhood in the Base Model



Neighborhood in the Wind Model



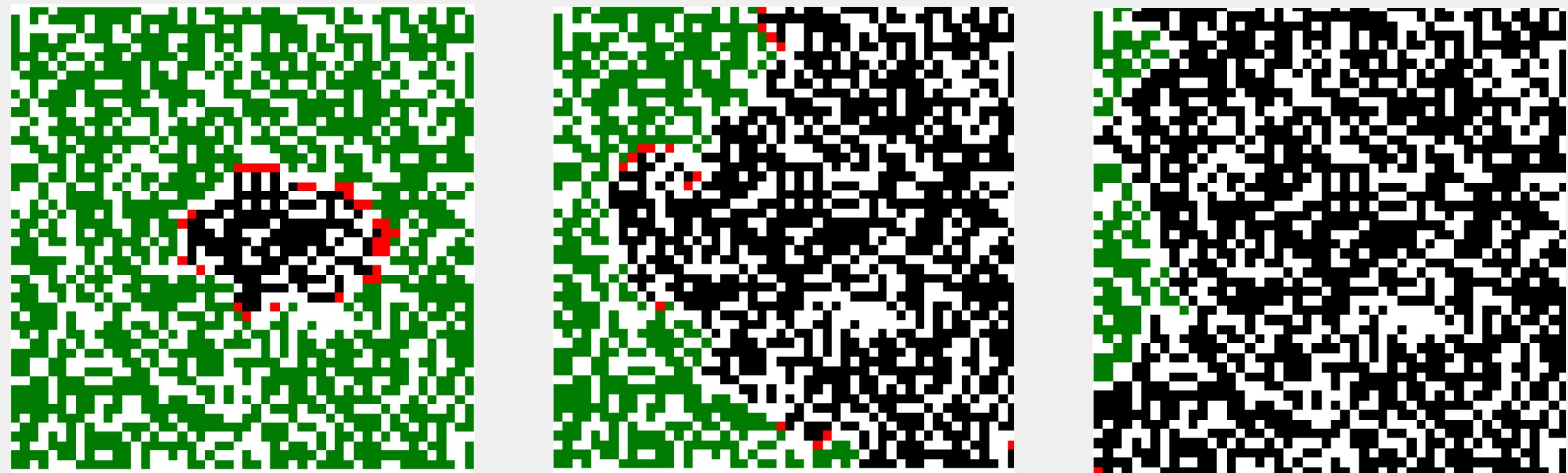
- Tree
- Burning site
- Burned site
- Empty site



# Wind in the Model

Forest Fire model  
control parameters

Grid size	50
Density	0.6
Wind	Yes



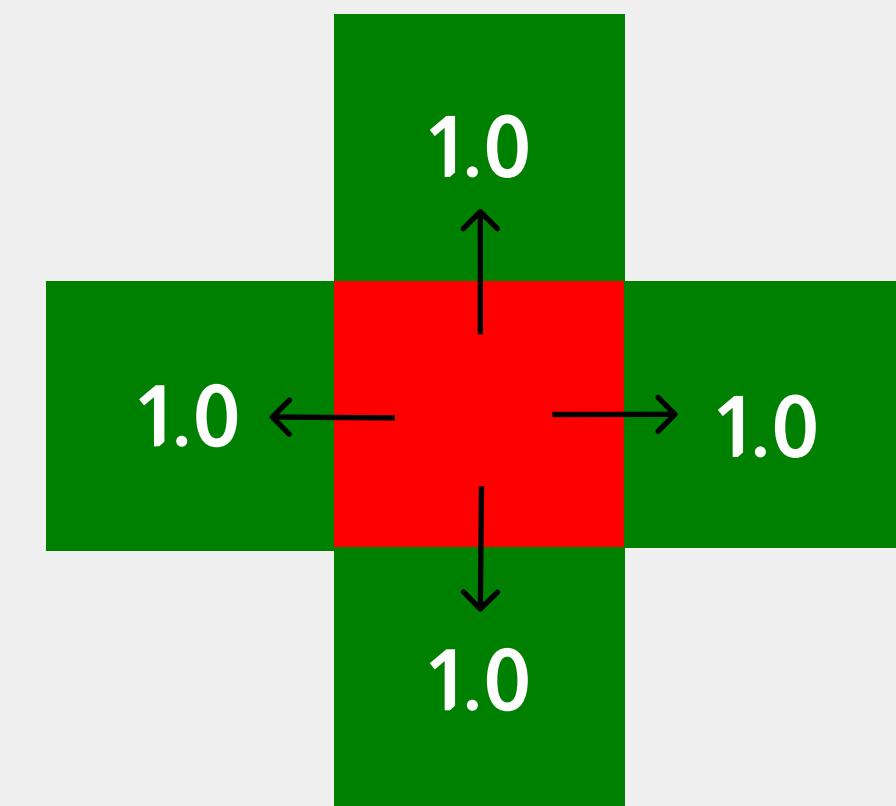
- [Green square] Tree
- [Red square] Burning site
- [Black square] Burned site
- [White square] Empty site

# Spreading Probability in the Model

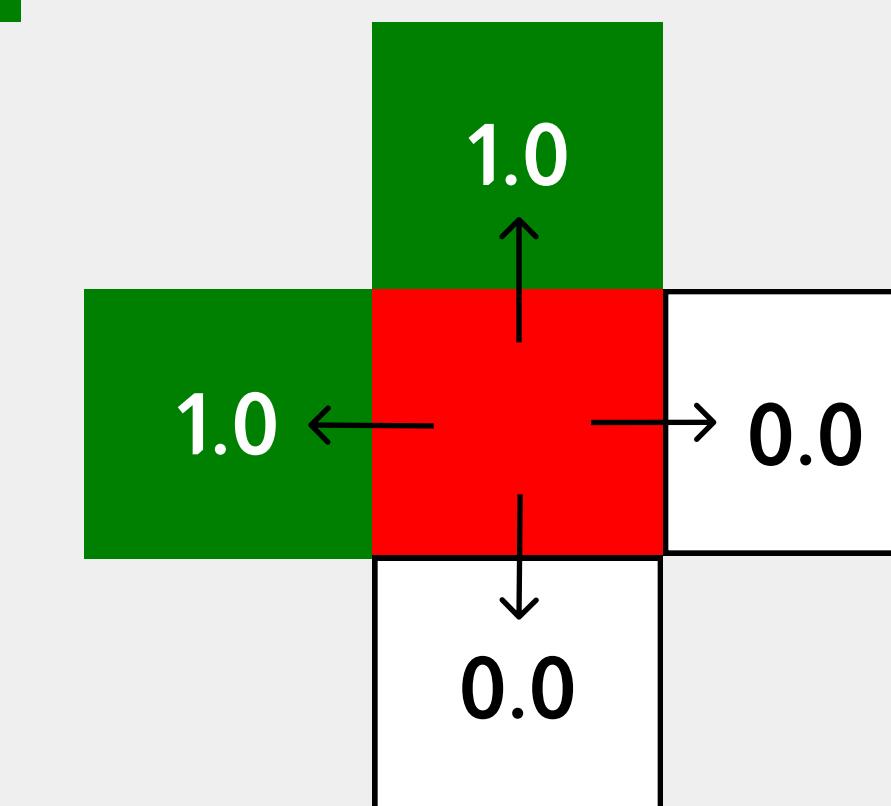
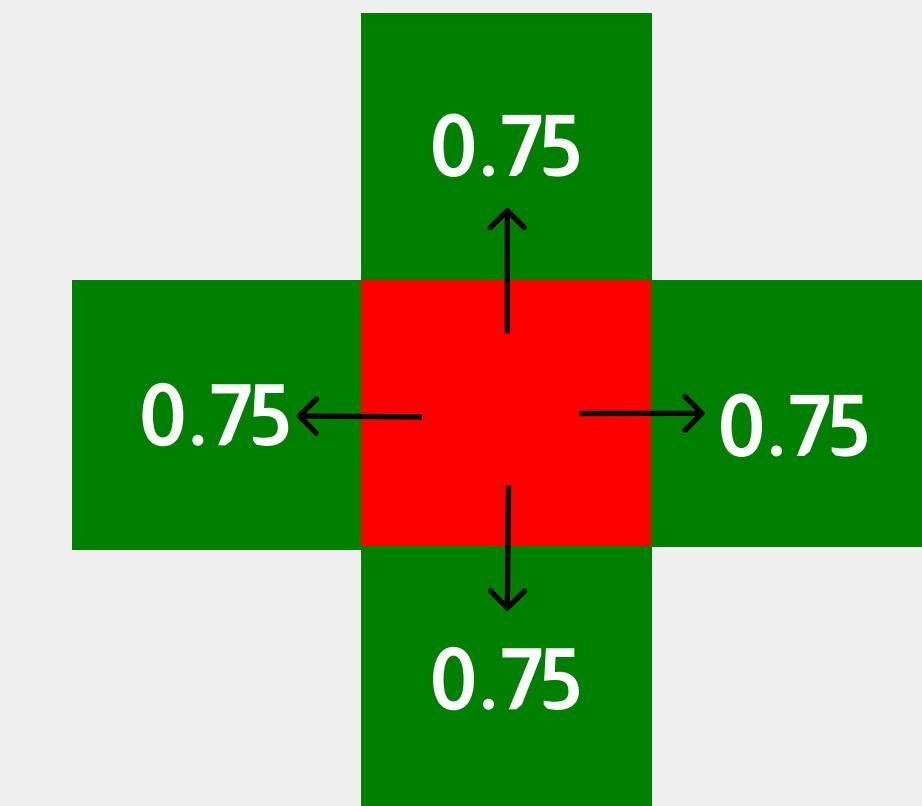
Forest Fire model  
control parameters

Grid size	50
Density	0.6
Wind	No
Spreading probability	0.75

Neighborhood in the Base Model



Neighborhood in the probabilistic Model



- Tree
- Burning site
- Burned site
- Empty site

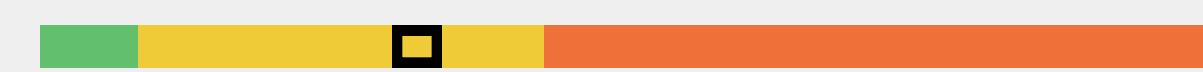
# Spreading Probability in the Model

Forest Fire model  
control parameters

Grid size	50
Density	0.6
Wind	No
Spreading probability	0.75



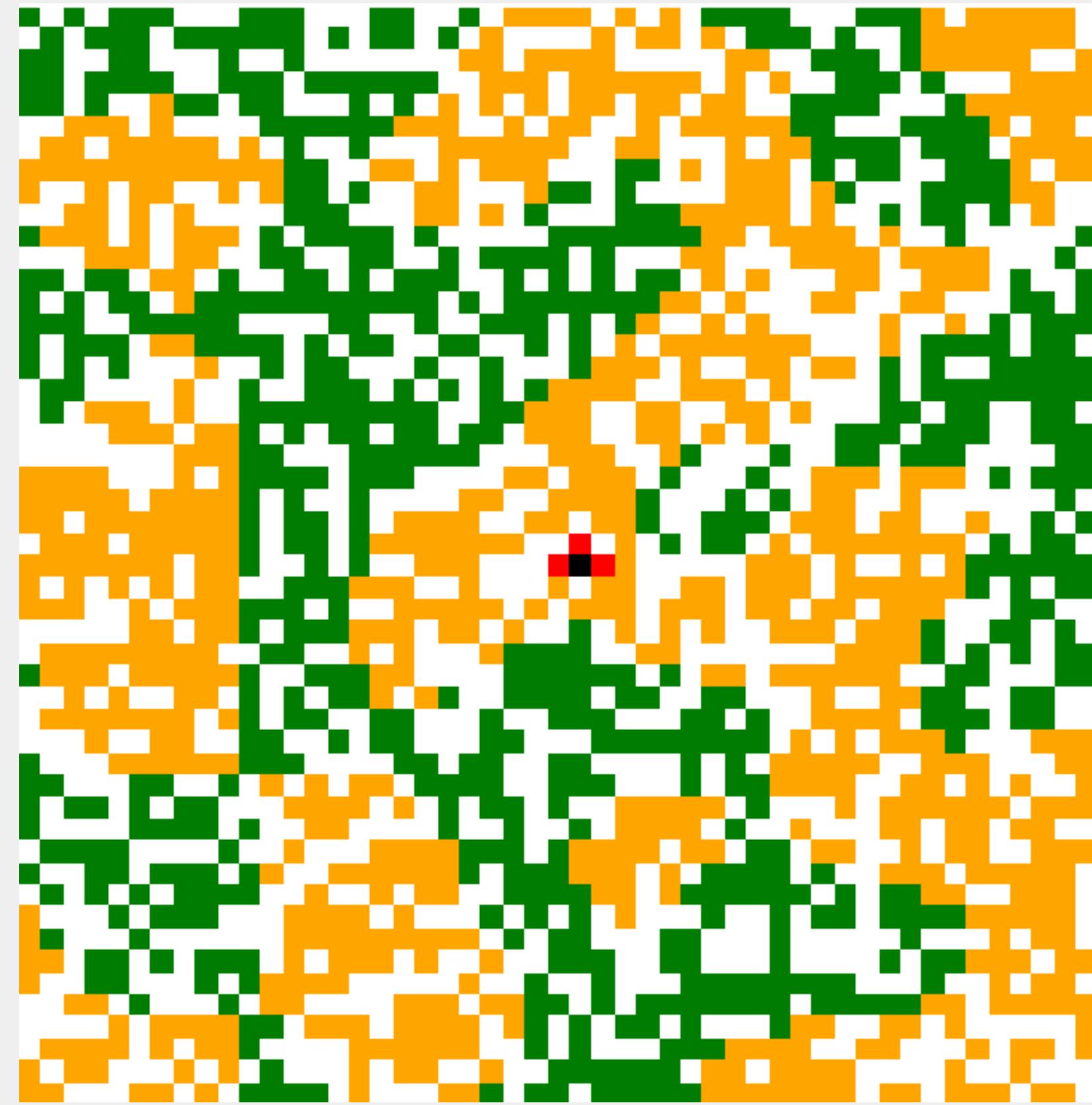
- Tree
- Burning site
- Burned site
- Empty site



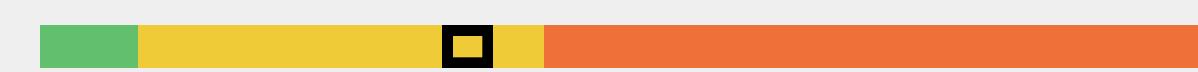
# Types of Vegetation in the Model

Forest Fire model  
control parameters

Grid size	50
Density	0.6
Wind	No
Spreading probability	0.75
Plant tree proportion	0.5



- Tree
- Plant
- Burning site
- Burned site
- Empty site

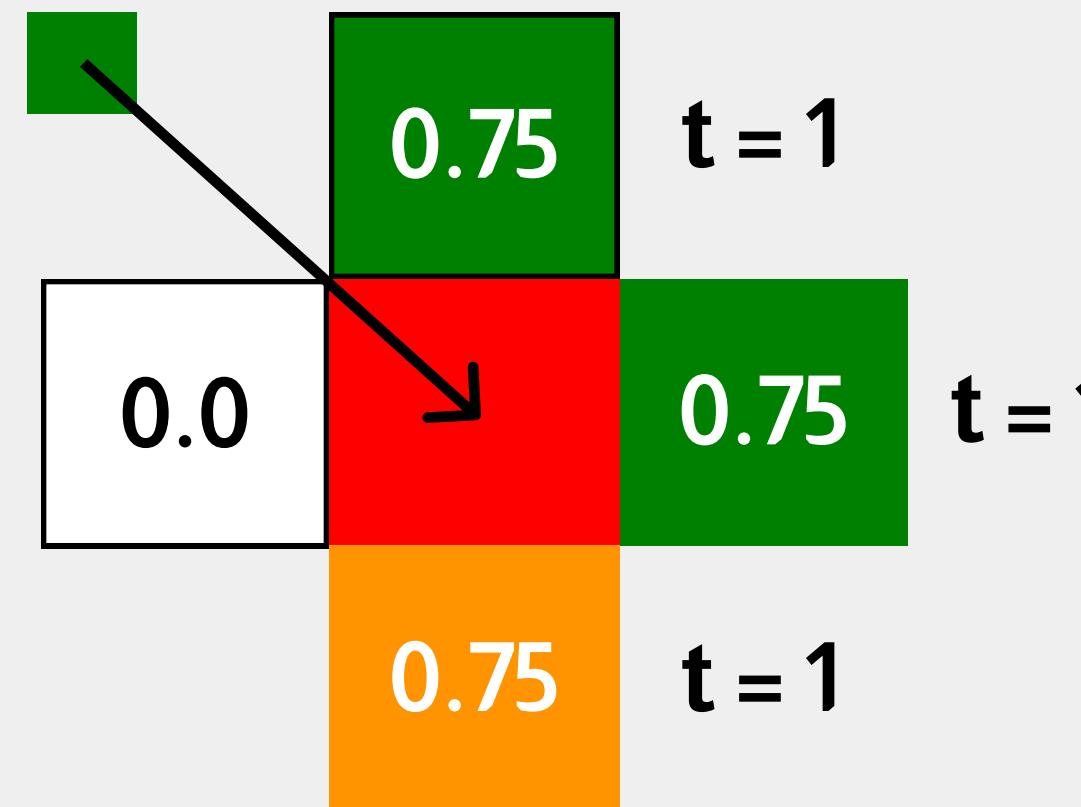


# Burn Time of Vegetation in the Model

Forest Fire model  
control parameters

Grid size	50
Density	0.6
Wind	No
Spreading probability	0.75
Plant tree proportion	0.5
Tree burn time	3
Plant burn time	1

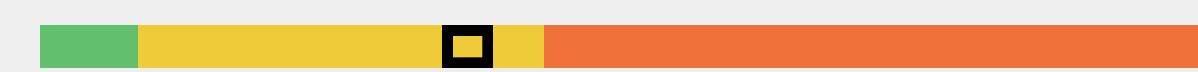
A Burnt Tree has 3 opportunities to Ignite Neighbors



Probability of a tree  
igniting a neighboring cell  
0.75

$$P_s$$

- Tree
- Plant
- Burning site
- Burned site
- Empty site

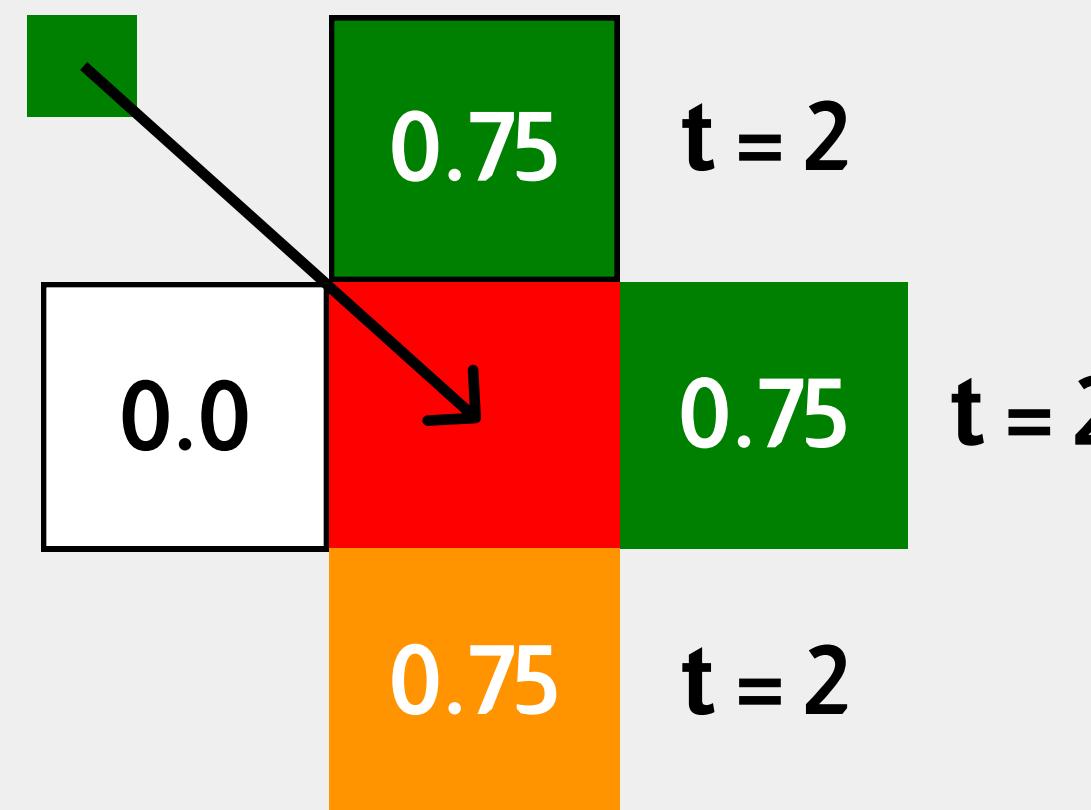


# Burn Time of Vegetation in the Model

Forest Fire model  
control parameters

Grid size	50
Density	0.6
Wind	No
Spreading probability	0.75
Plant tree proportion	0.5
Tree burn time	3
Plant burn time	1

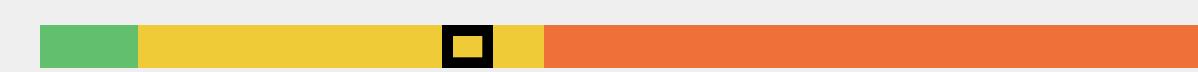
A Burnt Tree has 3 opportunities to Ignite Neighbors



Probability of a tree  
igniting a neighboring cell  
 $0.75 + 0.75(1-0.75) = 0.9375$

$$P_s + P_s(1 - P_s)^{i-1}$$

- Tree
- Plant
- Burning site
- Burned site
- Empty site

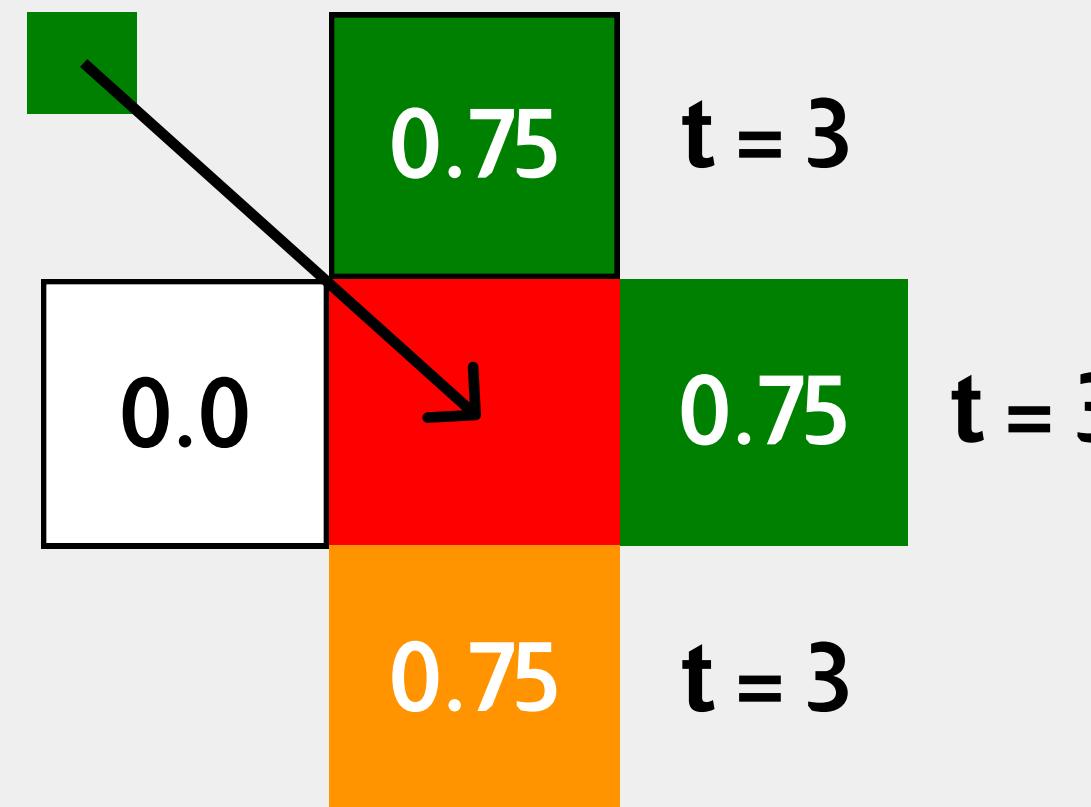


# Burn Time of Vegetation in the Model

Forest Fire model  
control parameters

Grid size	50
Density	0.6
Wind	No
Spreading probability	0.75
Plant tree proportion	0.5
Tree burn time	3
Plant burn time	1

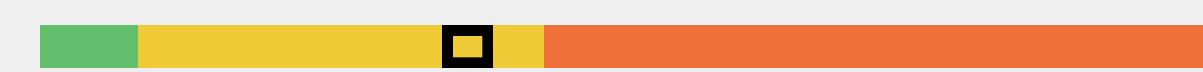
A Burnt Tree has 3 opportunities to Ignite Neighbors



Probability of a tree  
igniting a neighboring cell  
 $0.9375 + 0.75(1-0.75)^2 = 0.98$

$$\Delta_{tree} = \sum_{i=1}^{\infty} P_s (1 - P_s)^{i-1}$$

- Tree
- Plant
- Burning site
- Burned site
- Empty site



# Burn Time of Vegetation in the Model

Forest Fire model  
control parameters

Grid size	50
Density	0.6
Wind	No
Spreading probability	0.75
Plant tree proportion	0.5
Tree burn time	3
Plant burn time	1

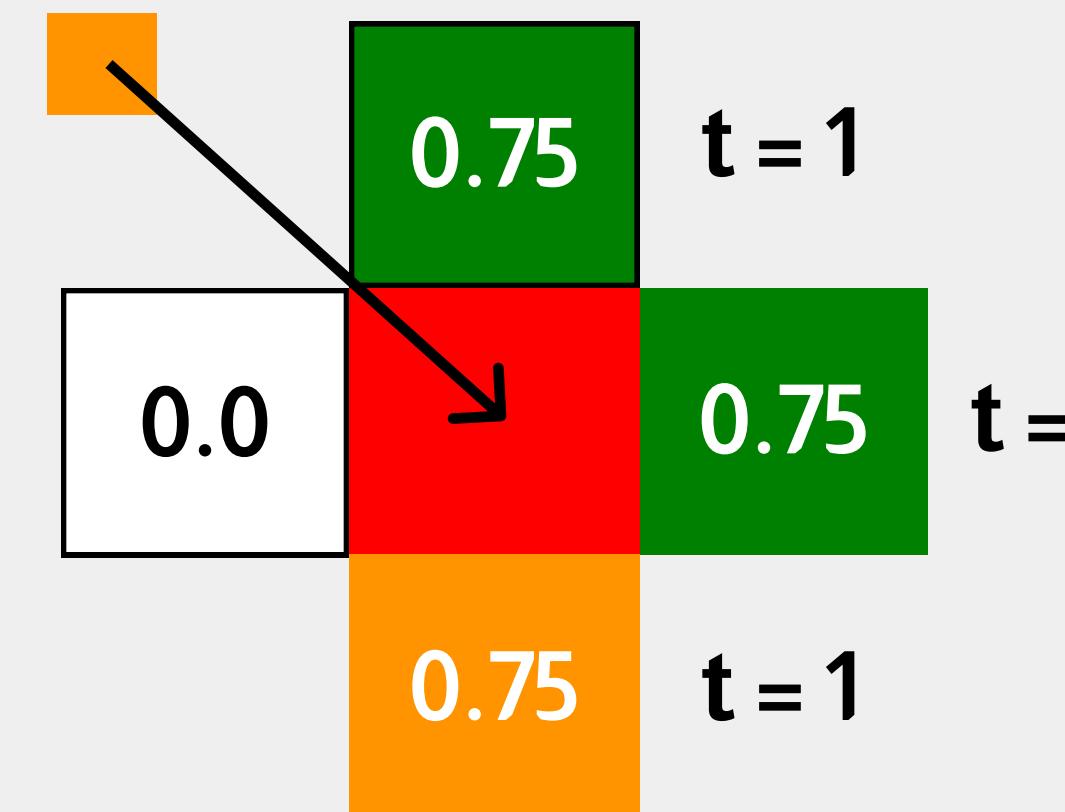
A Burnt Tree has 3 opportunities to Ignite Neighbors



General

$$\Delta_{tree} = \sum_{i=1}^{\infty} P_s (1 - P_s)^{i-1}$$

A Burnt Plant has 1 opportunity to Ignite Neighbors



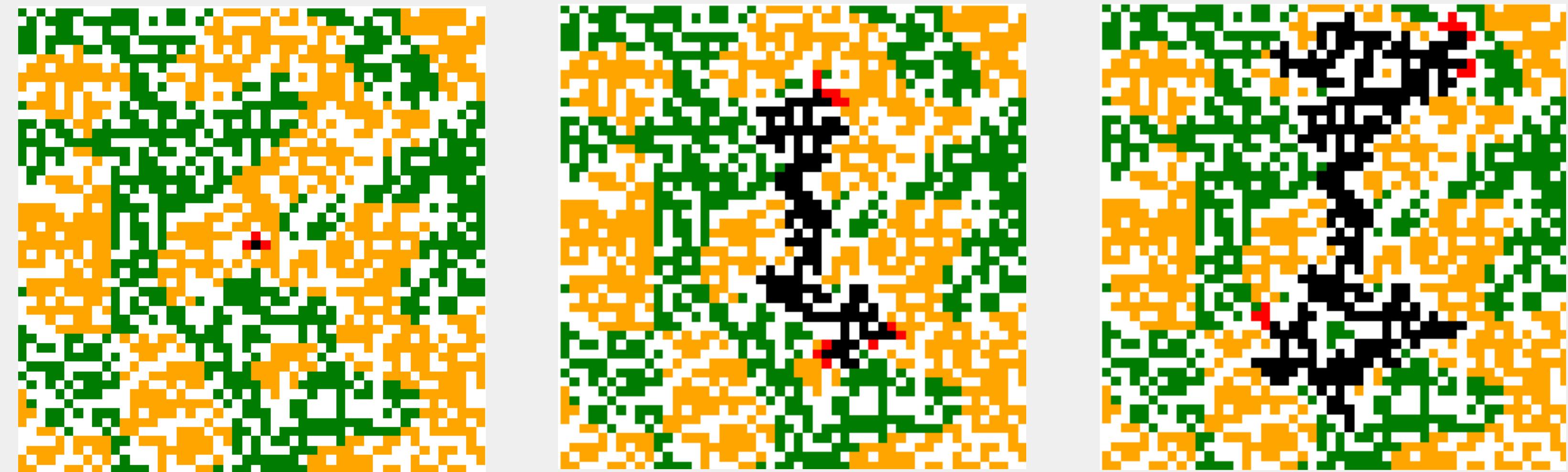
- Tree
- Plant
- Burning site
- Burned site
- Empty site



# Vegetation Noise in the Model

Forest Fire model  
control parameters

Grid size	50
Density	0.6
Wind	No
Spreading probability	0.75
Plant tree proportion	0.5
Tree burn time	3
Plant burn time	1



- Tree
- Plant
- Burning site
- Burned site
- Empty site

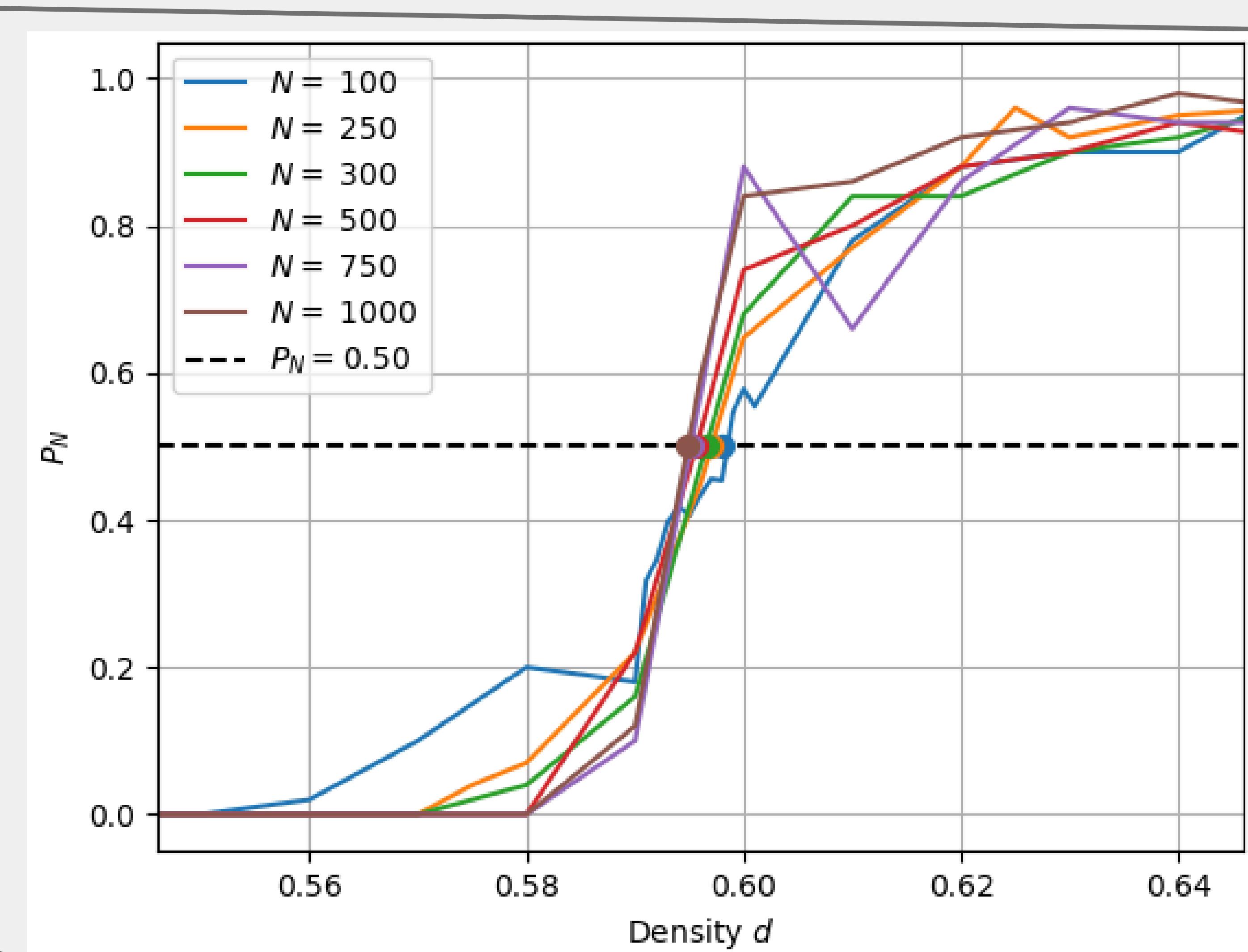
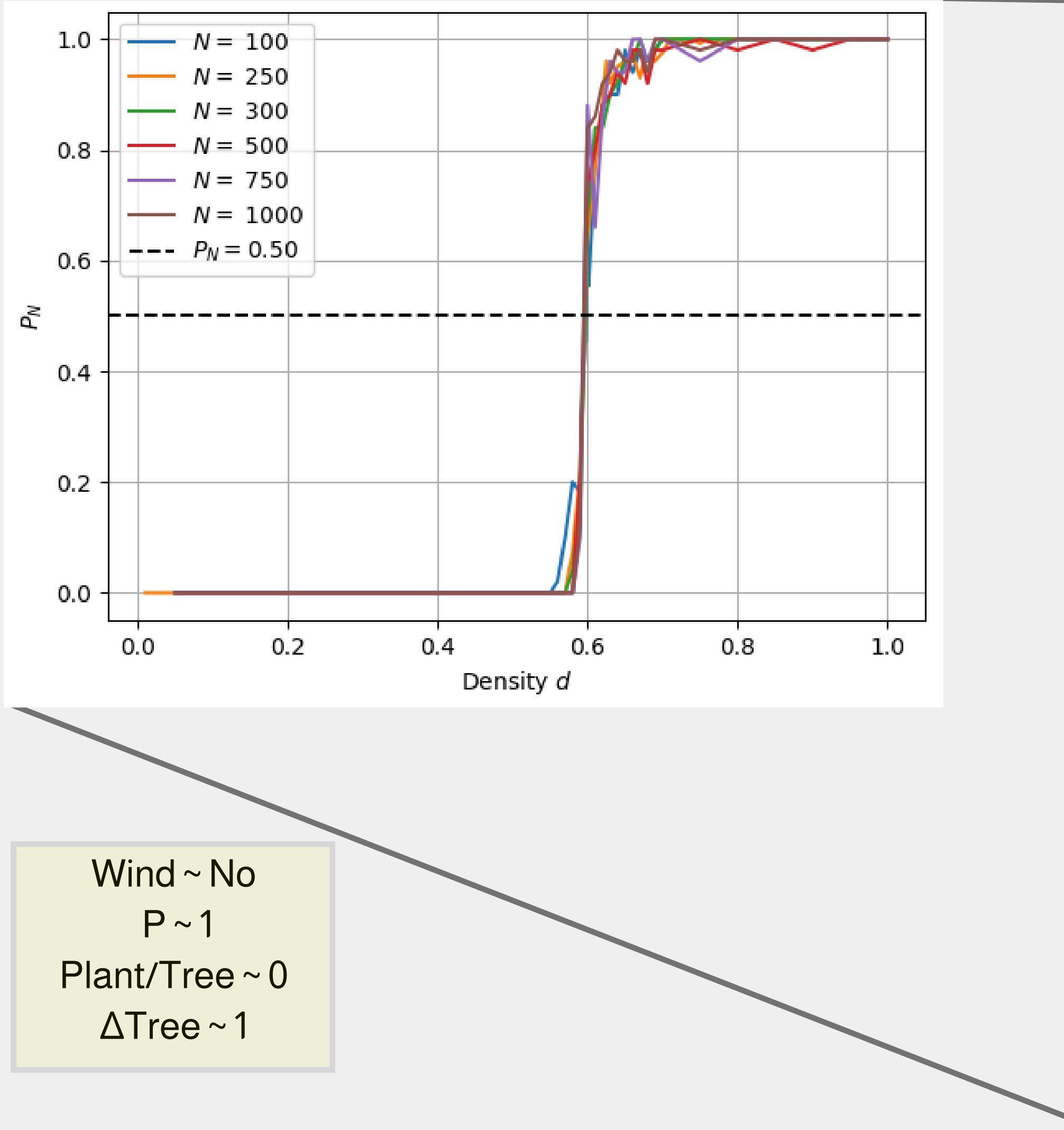


# Results

Percolation, Critical Densities and  
Behavior at the Critical Density

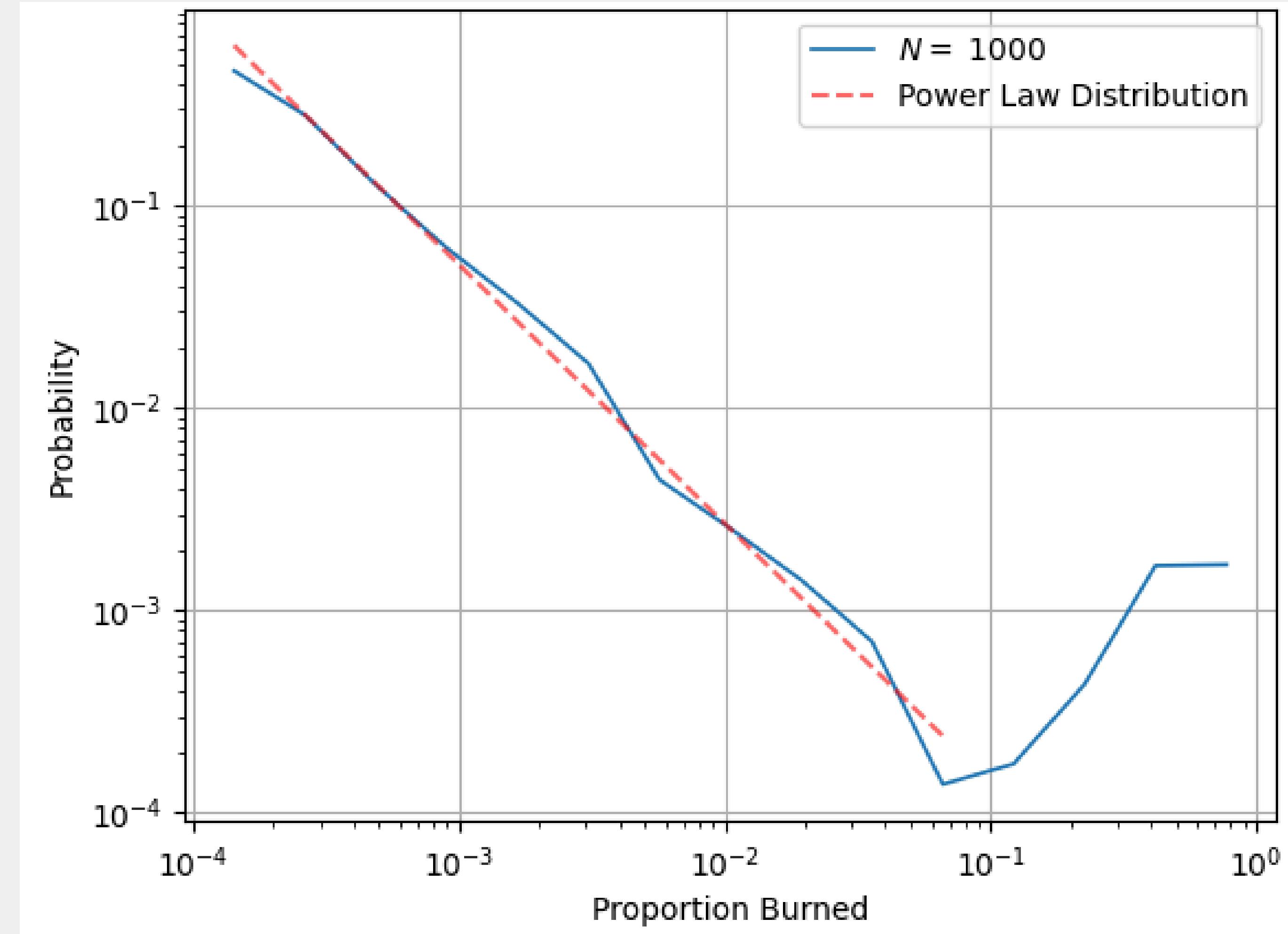


# Percolation Base Model



# Behavior at the Critical Density

Wind  $\sim$  No  
 $P \sim 1$   
 Plant/Tree  $\sim 0$   
 $\Delta$ Tree  $\sim 1$

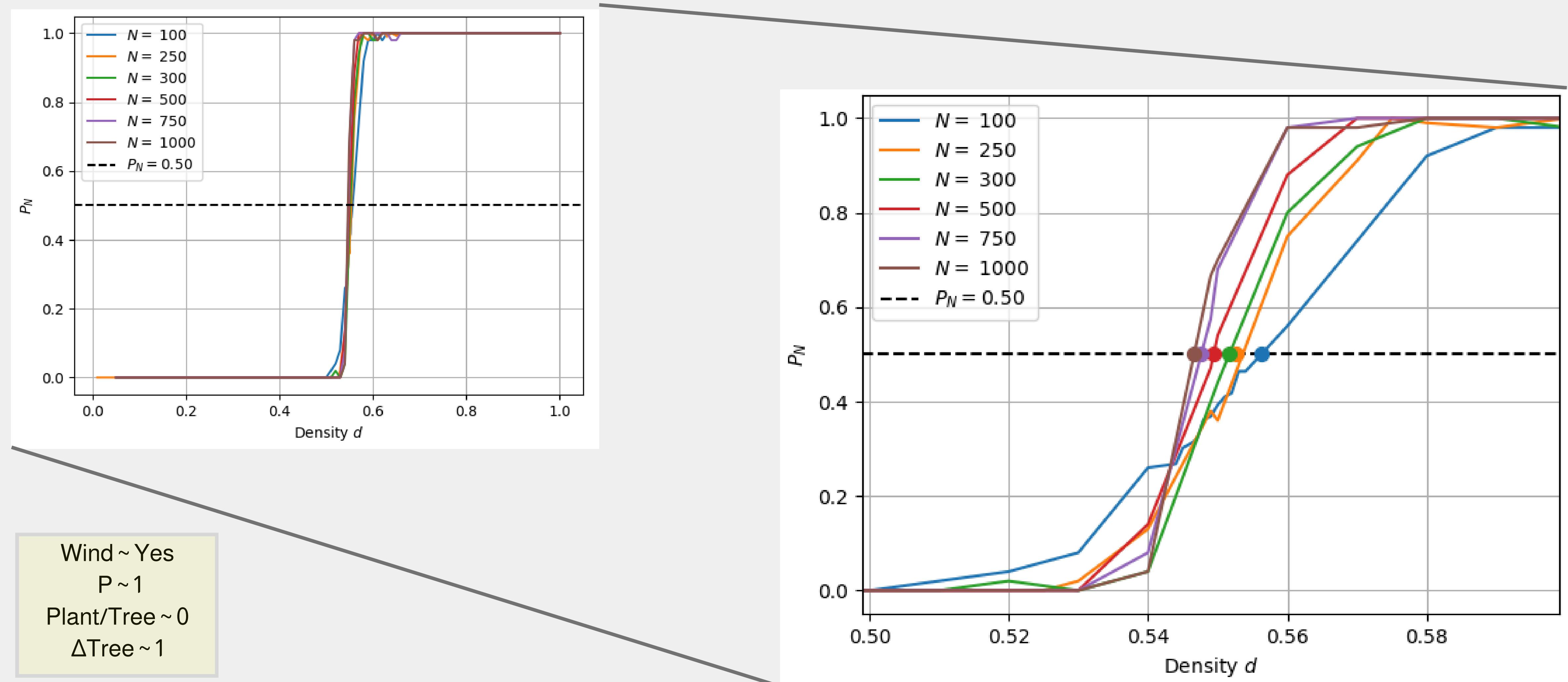


**Critical Density**  
 $\sim 0.596$

**KS Test**  
 $KS = 0.236$   
 $P\text{-value} = 0.778 > 0.05$

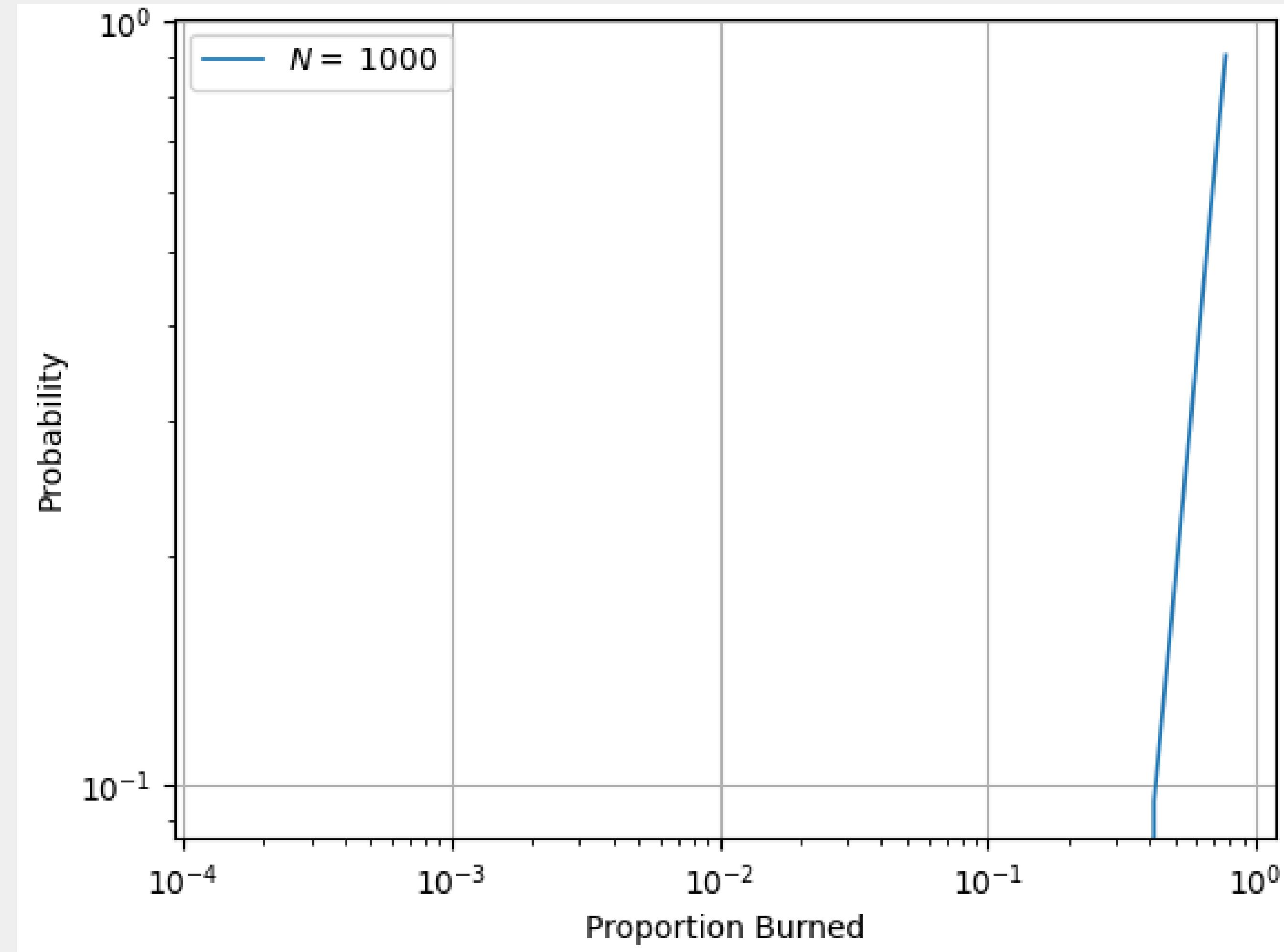


# Effect on Percolation of Adding Wind to the Model



# Behavior at the Critical Density

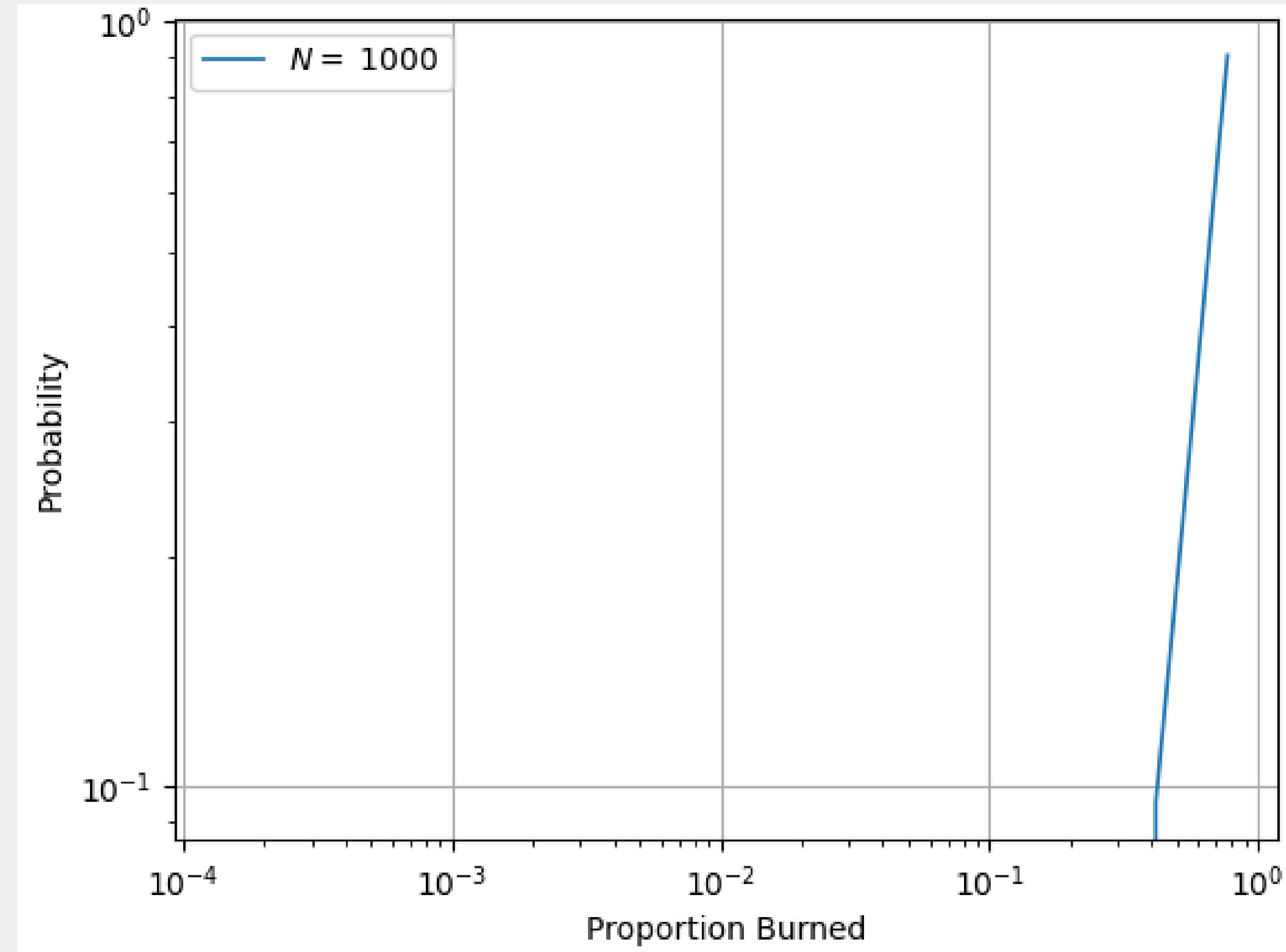
Wind ~ Yes  
 $P \sim 1$   
Plant/Tree ~ 0  
 $\Delta T_{\text{tree}} \sim 1$



**Critical Density**  
 $\sim 0.549$

# Behavior at the Critical Density

Wind ~ Yes  
 $P \sim 1$   
Plant/Tree ~ 0  
 $\Delta T_{\text{Tree}} \sim 1$



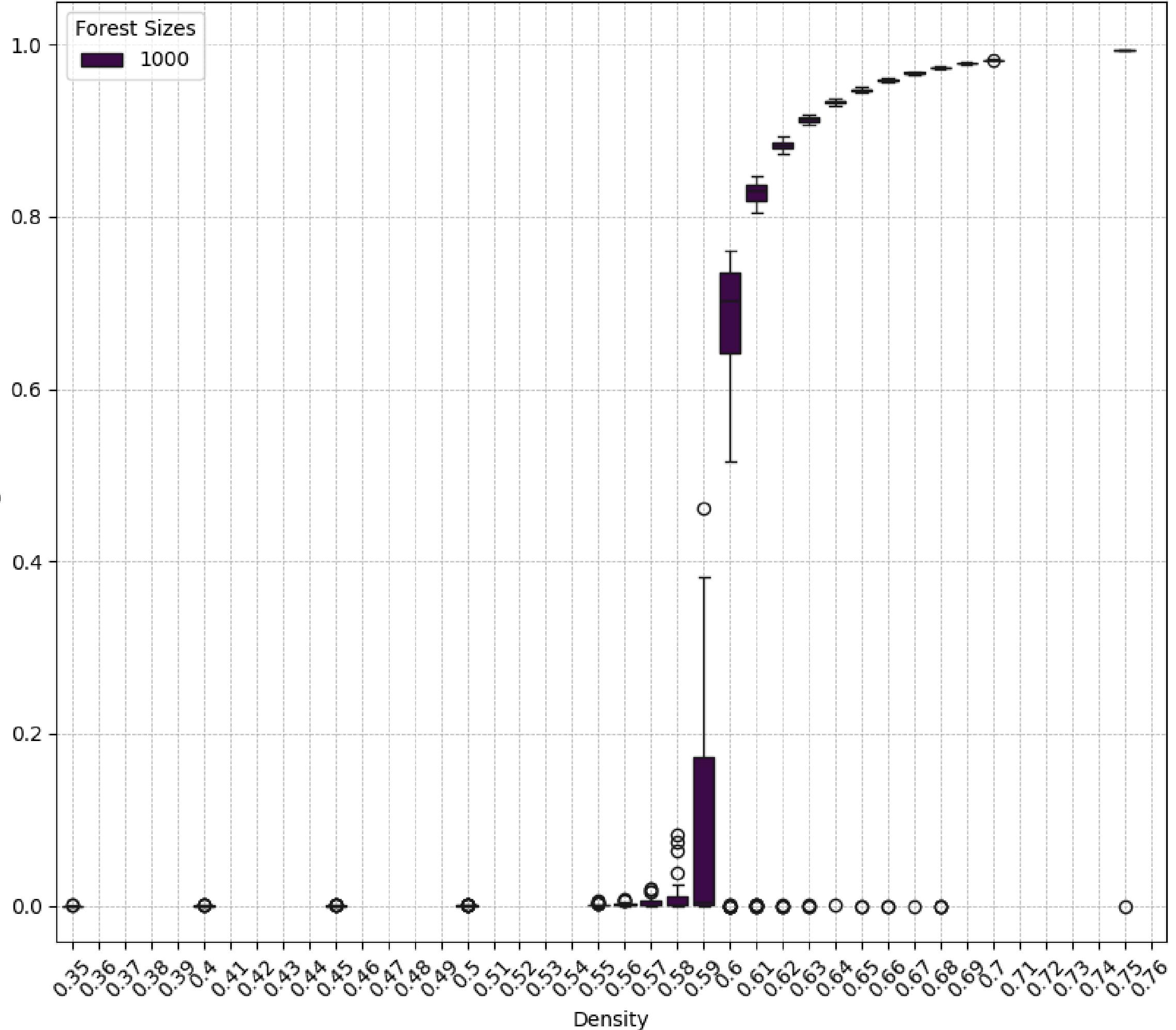
Critical Density  
 $\sim 0.549$

KS Test  
No power law fit

# Variance in the Wind Model

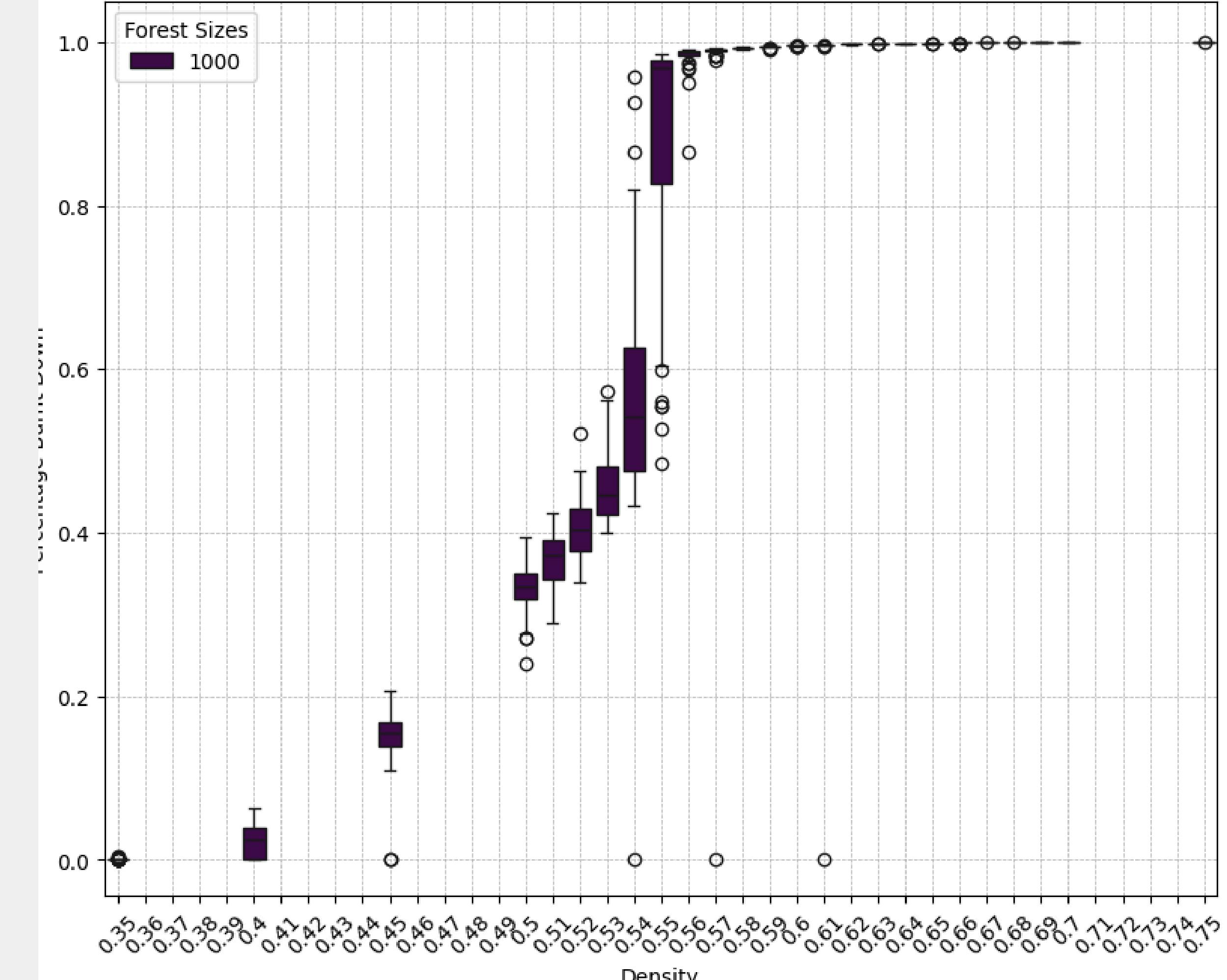
## Base Model

Distribution of Burnt Percentage Over Different Densities



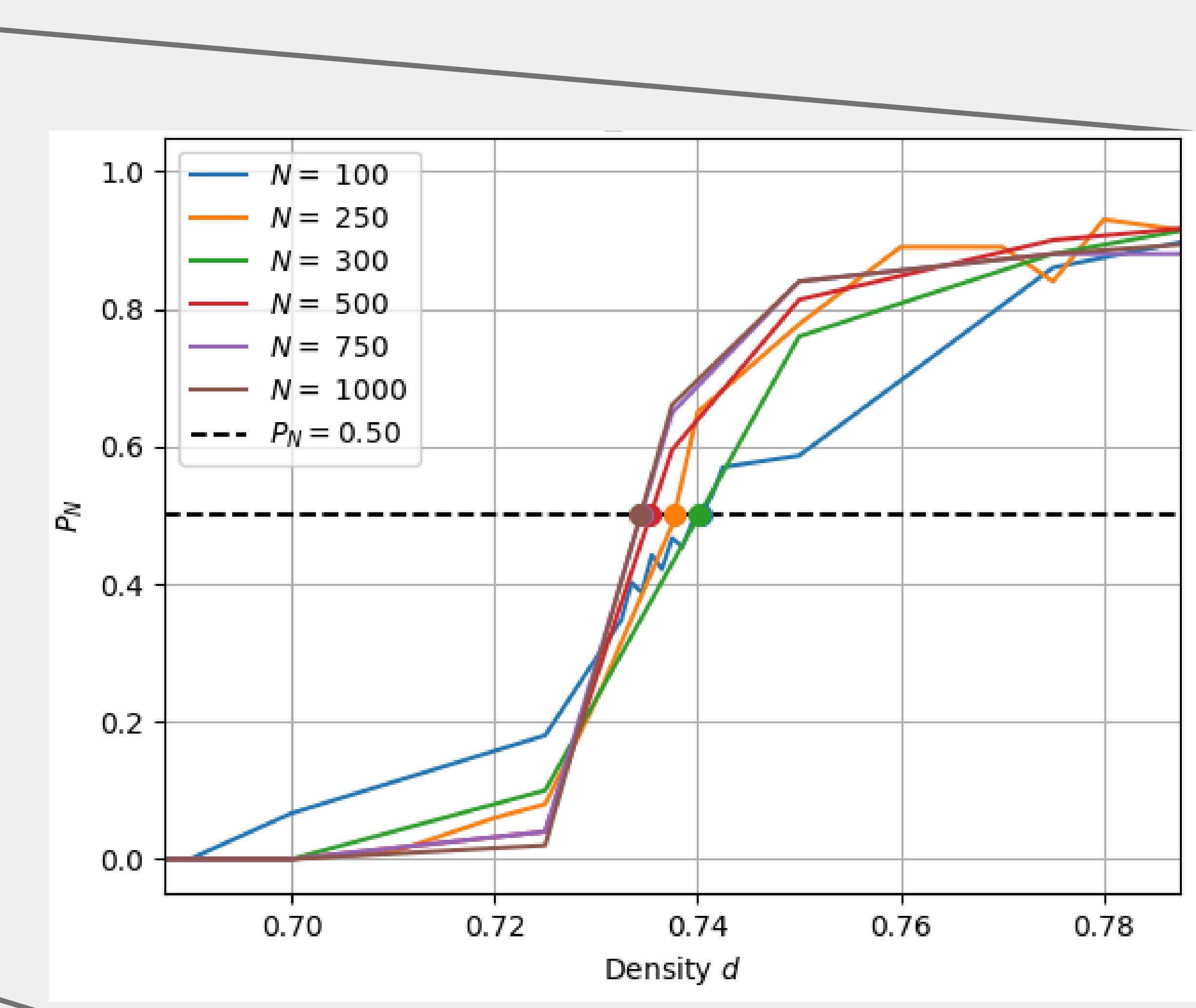
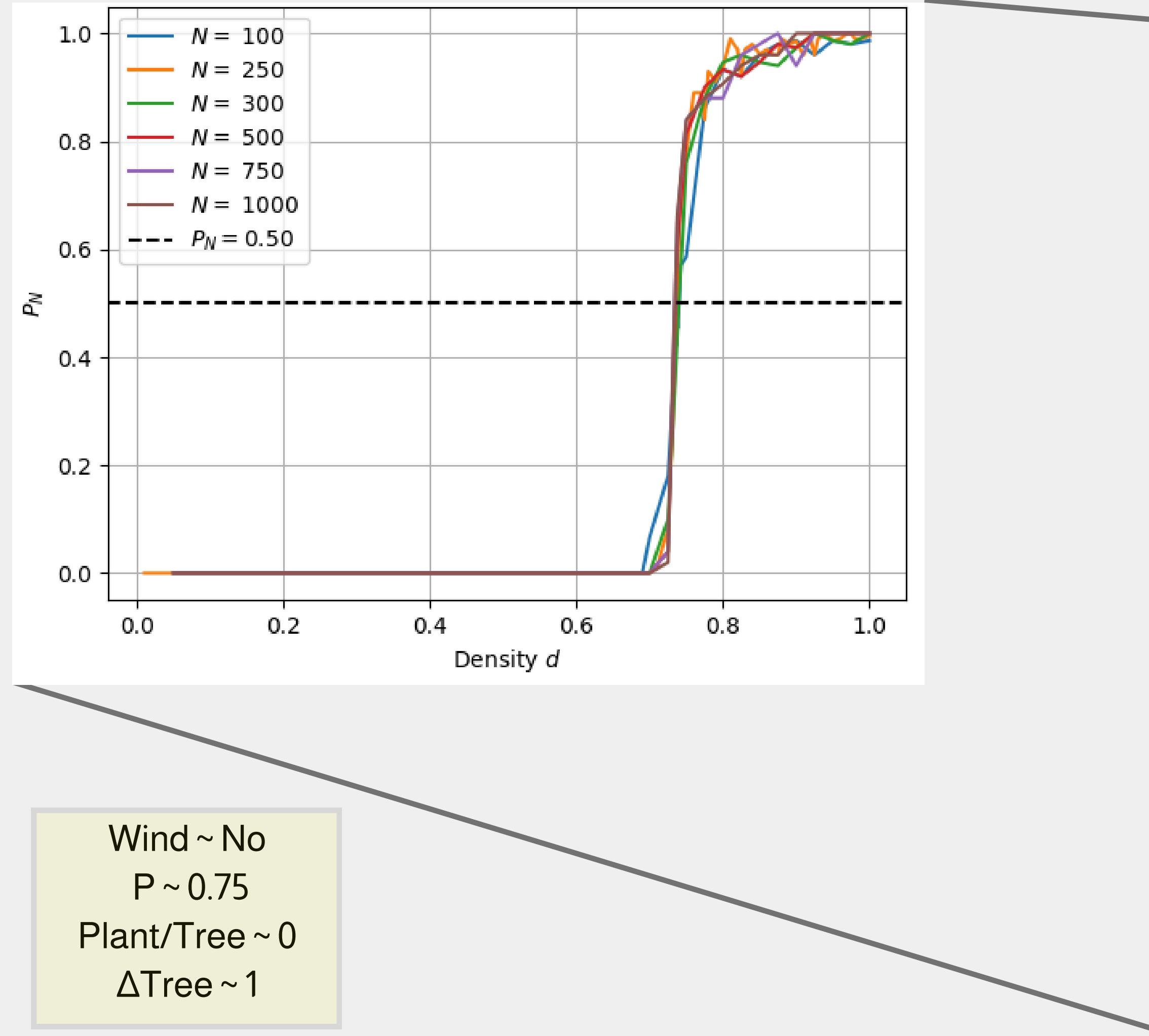
## Wind Model

Distribution of Burnt Percentage Over Different Densities



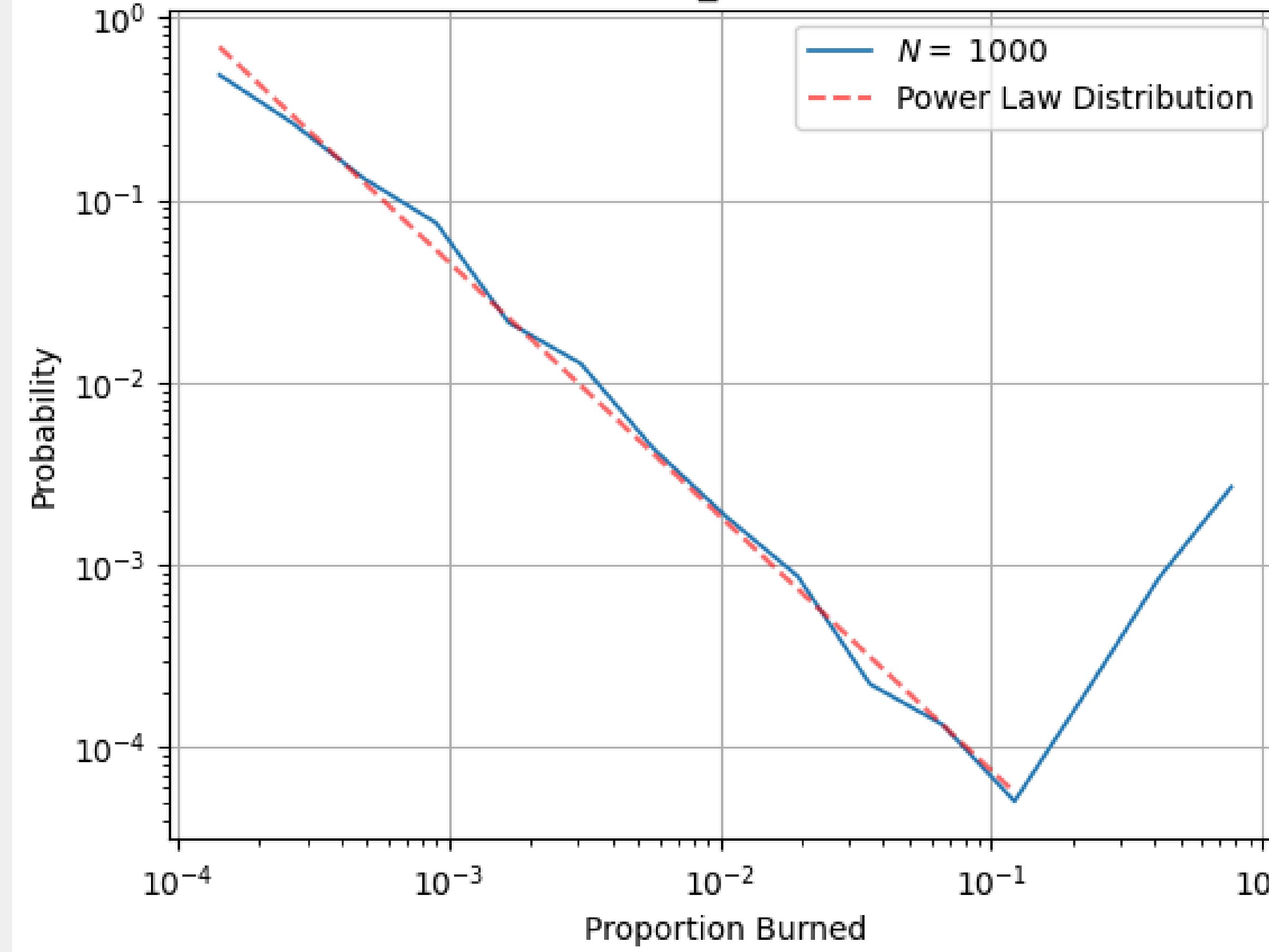


# Effect on Percolation of Adding Probability to the Model



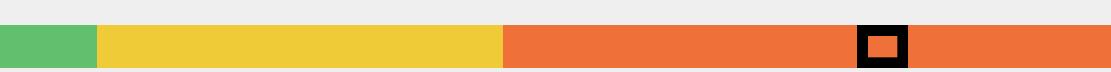
# Behavior at the Critical Density

Wind ~ No  
P ~ 0.75  
Plant/Tree ~ 0  
 $\Delta$ Tree ~ 1

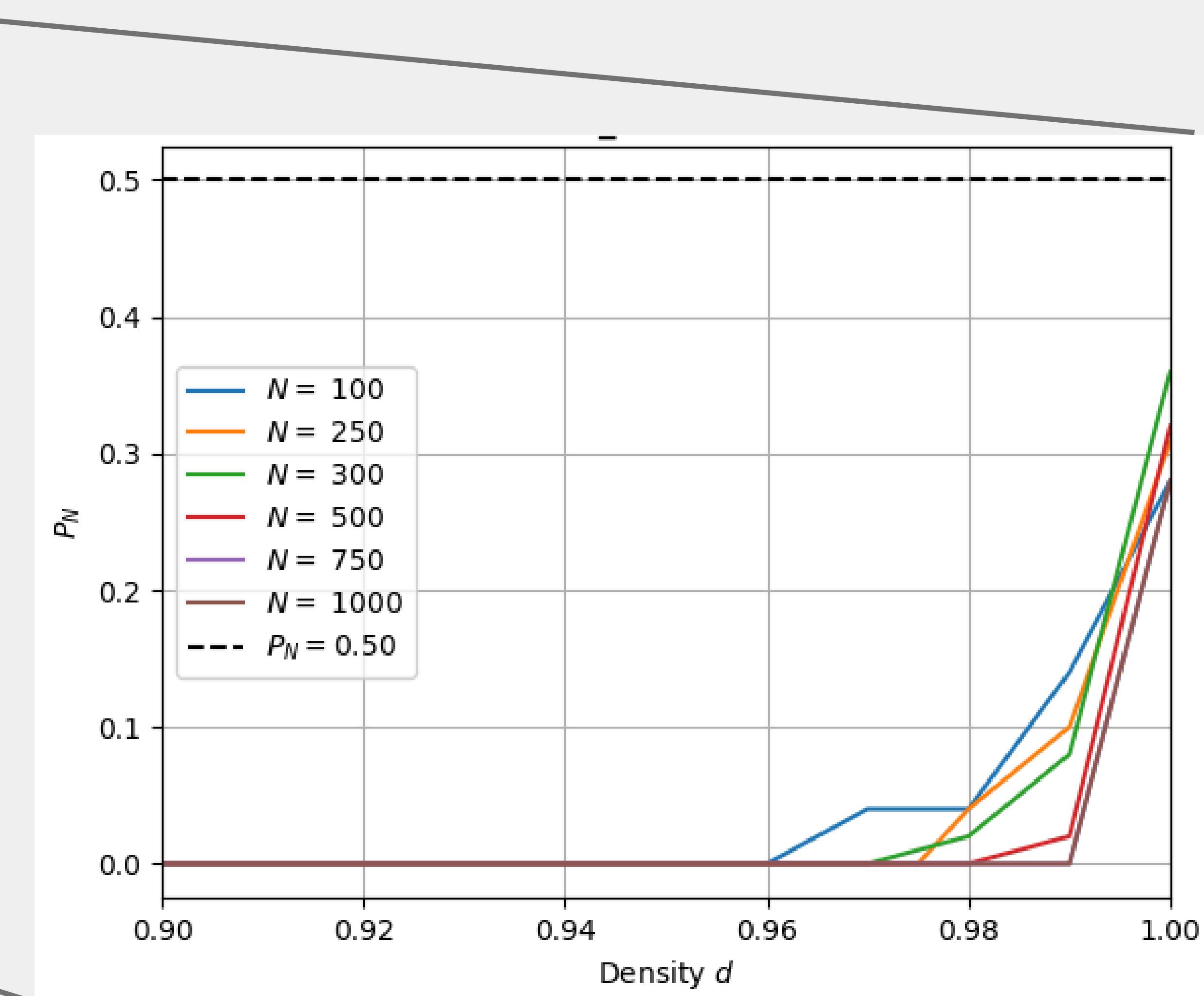
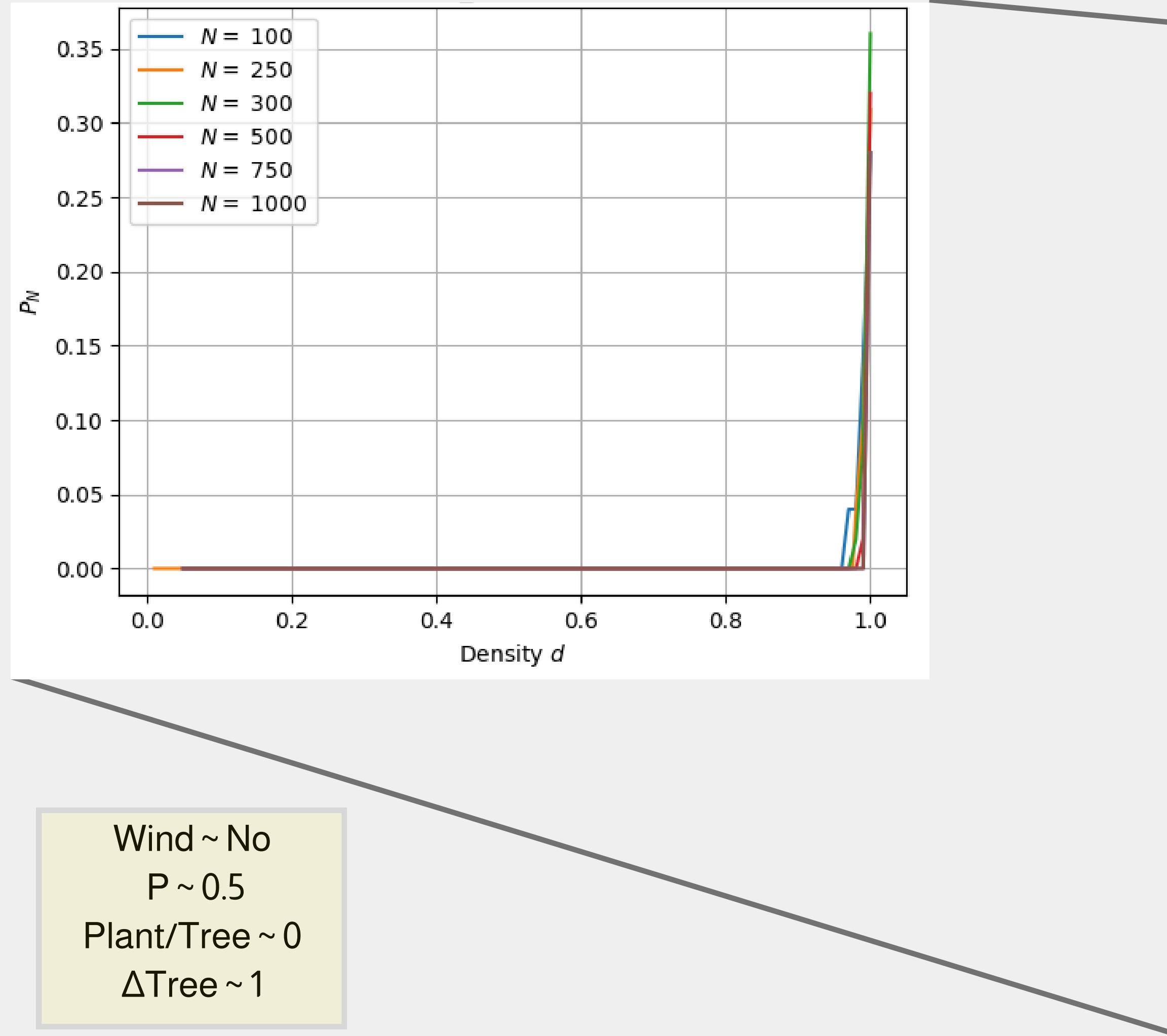


**Critical Density**  
~ 0.7375

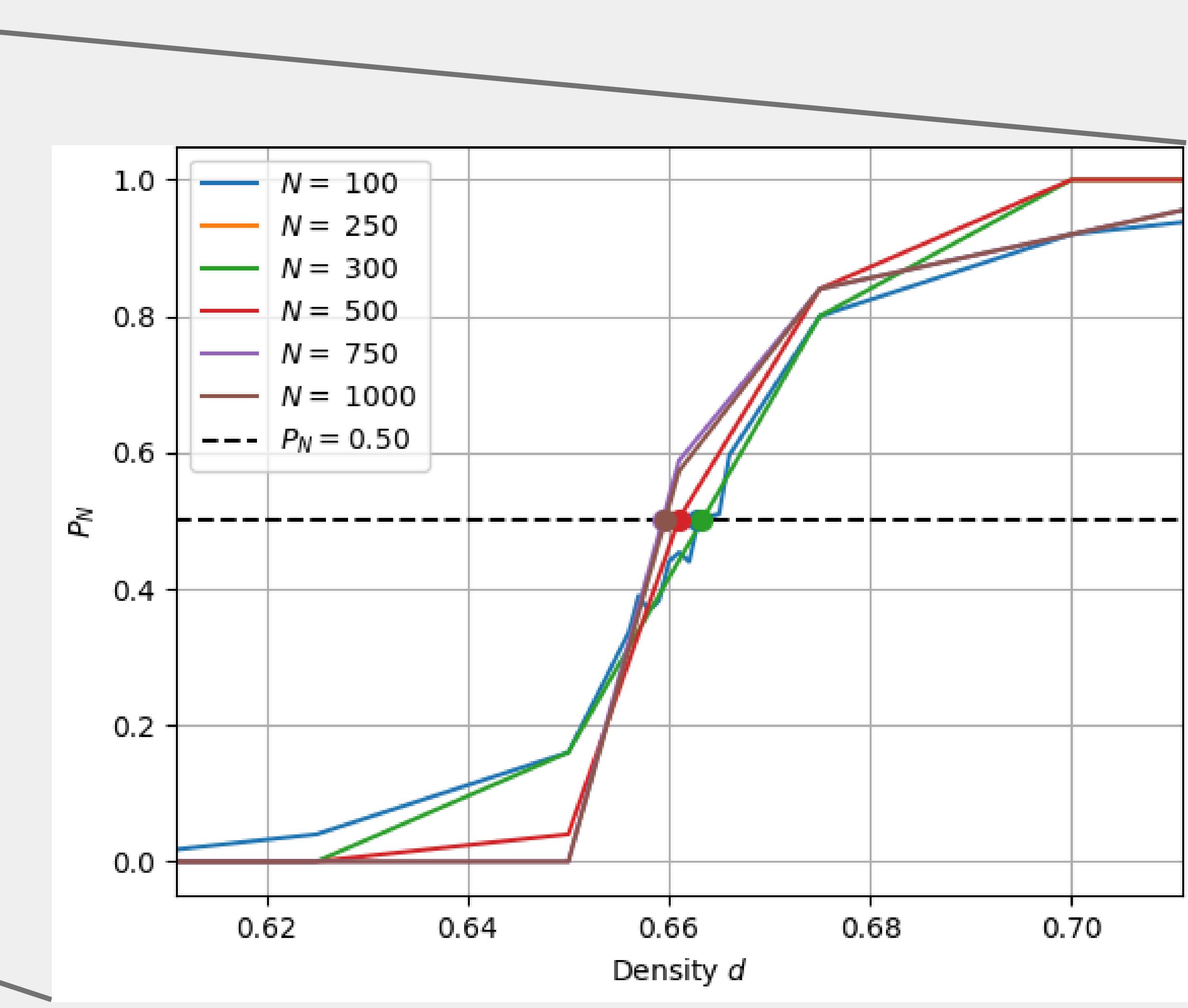
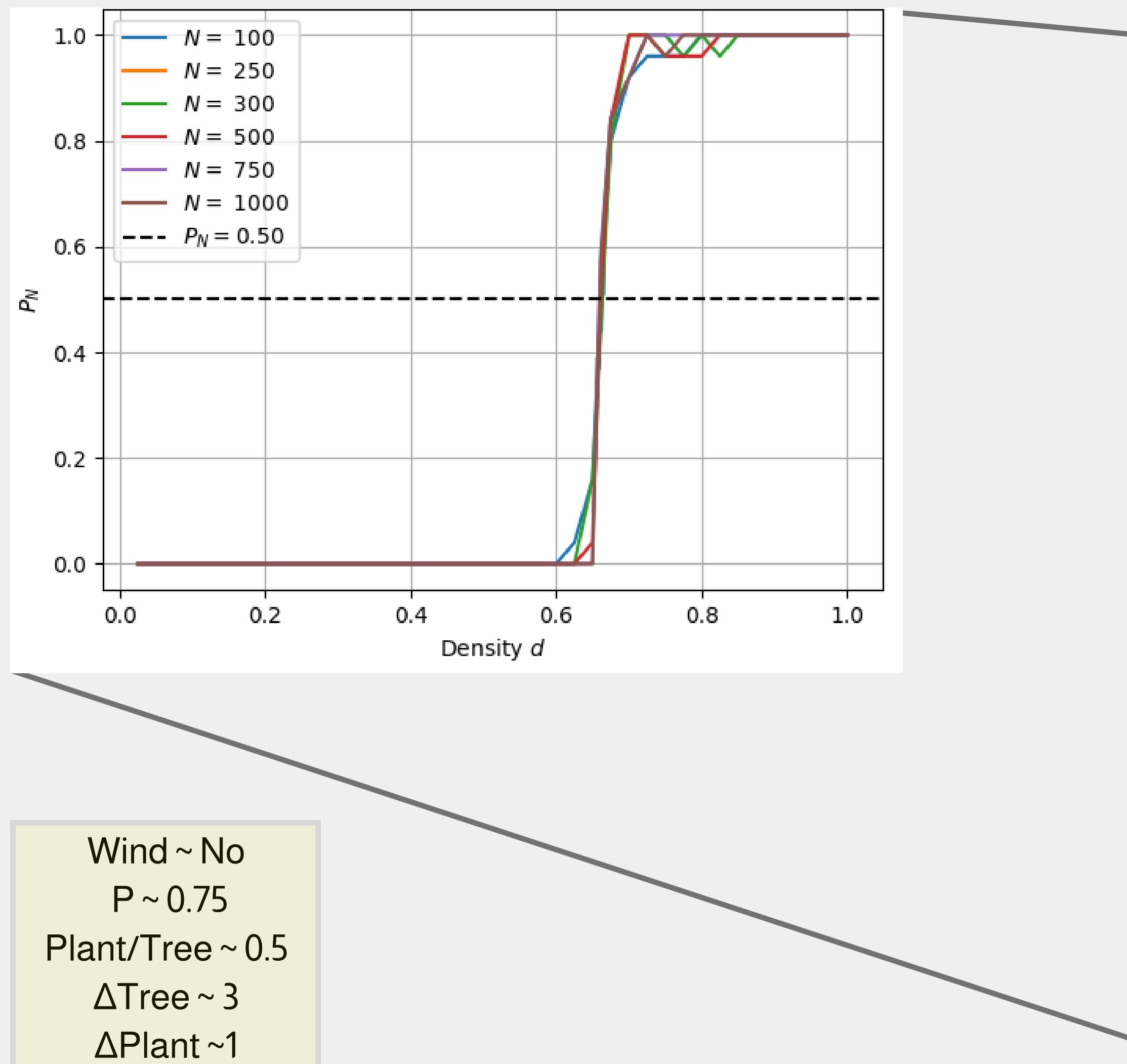
**KS Test**  
KS = 0.15  
P-value = 0.990 > 0.05



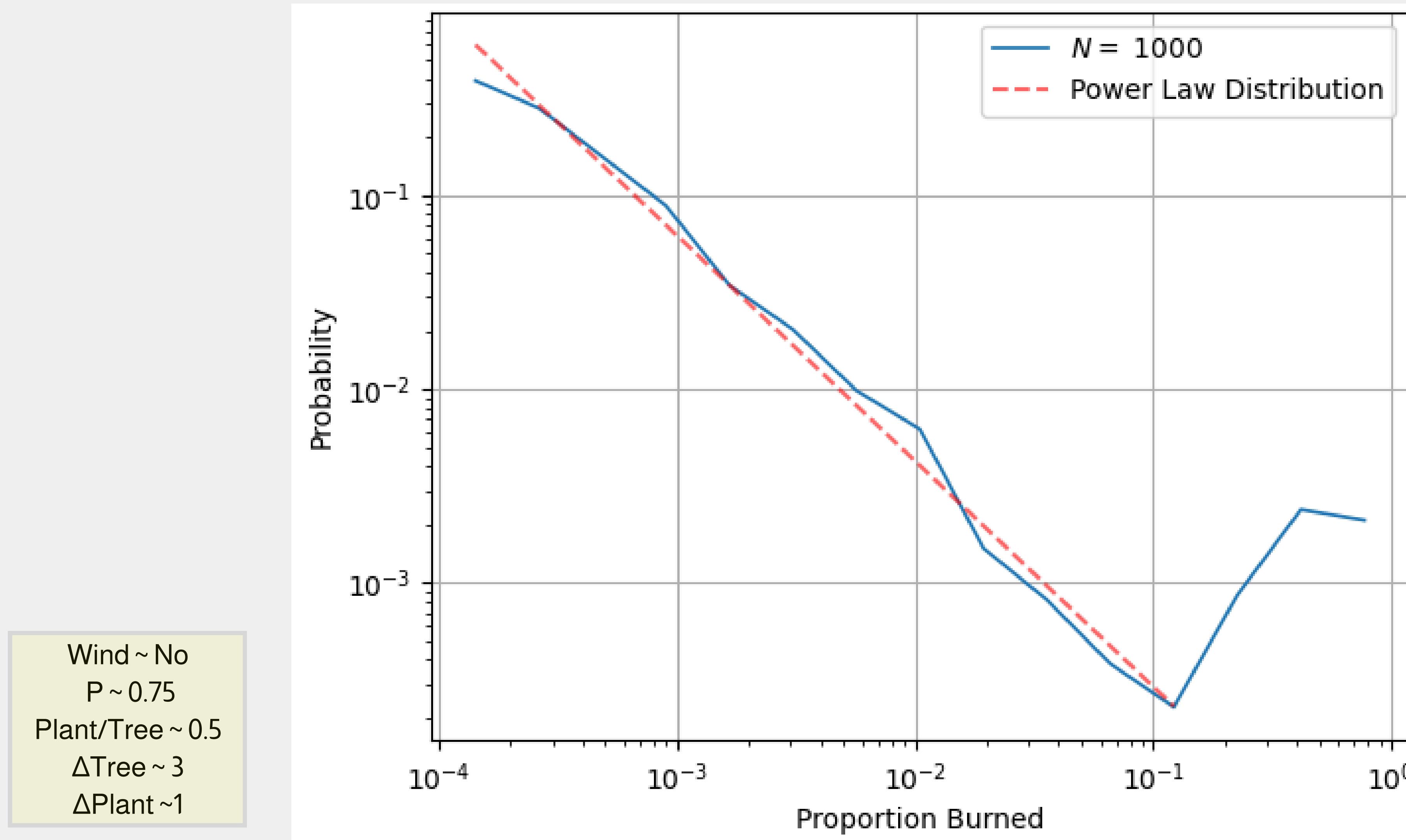
# Effect on Percolation of Adding Probability to the Model



# Effect on Percolation of Adding Vegetation types to the Model



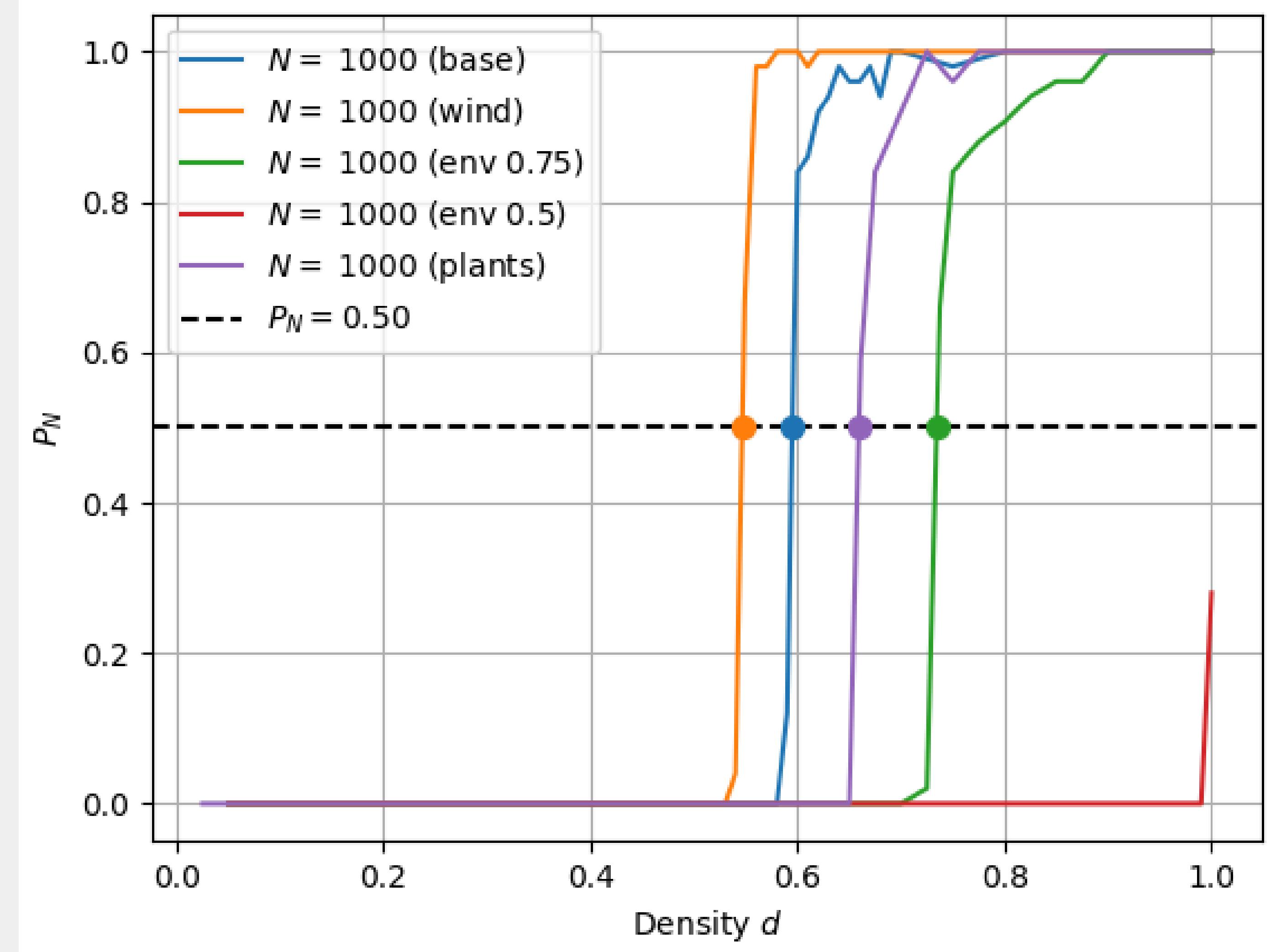
# Behavior at the Critical Density



**Critical Density**  
 $\sim 0.661$

**KS Test**  
KS = 0.15  
P-value = 0.990  $>$  0.05

# Comparing the different systems



# Conclusions

1

Do forest fires exhibit characteristics of criticality?

**The forest fire model exhibits characteristics of criticality!**

2

How does introducing wind into the system affect the critical density and does it still exhibit criticality?

**Including wind in the system breaks the criticality**

3

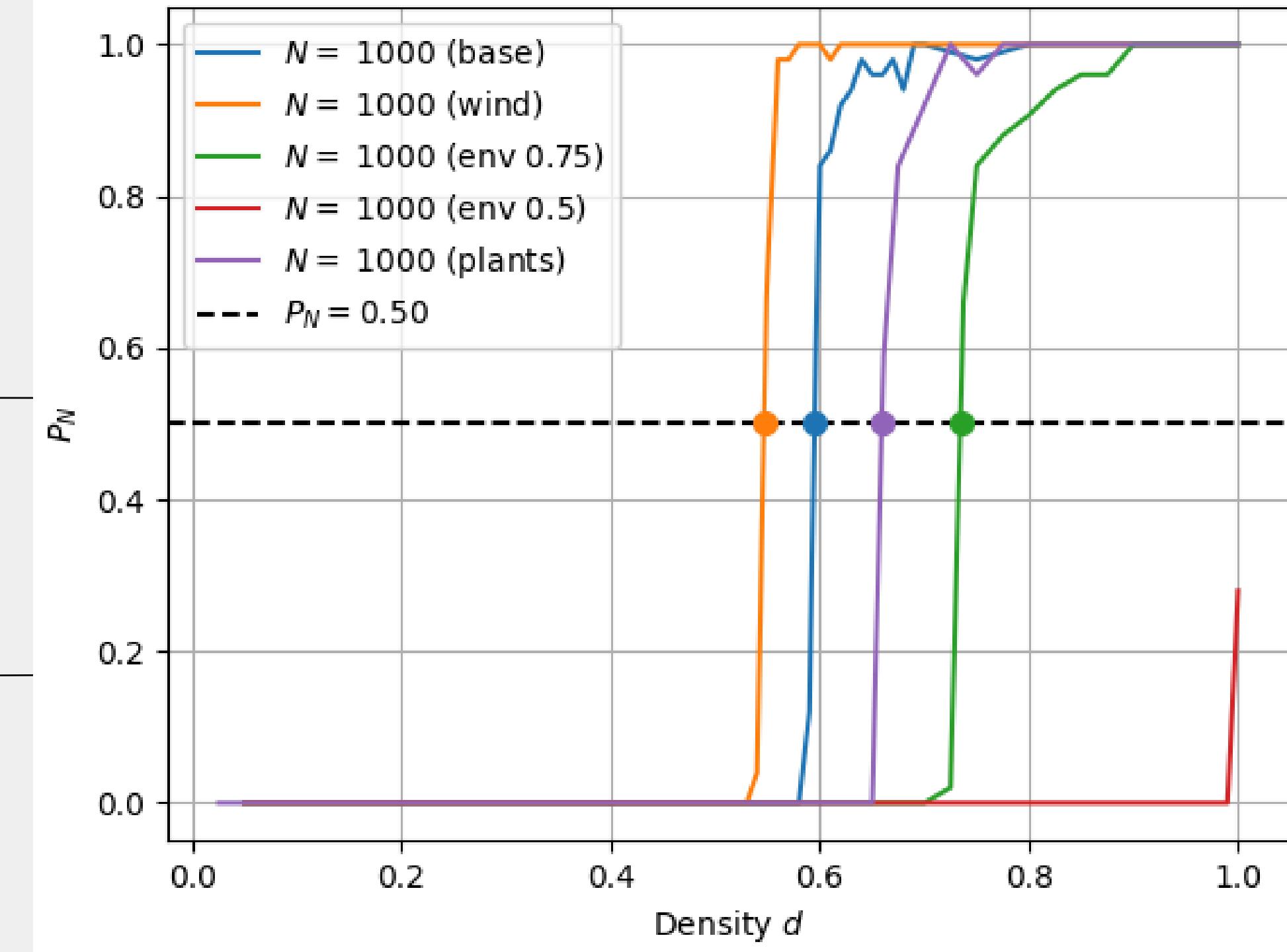
How do environmental influences affect the critical density and does it still exhibit criticality?

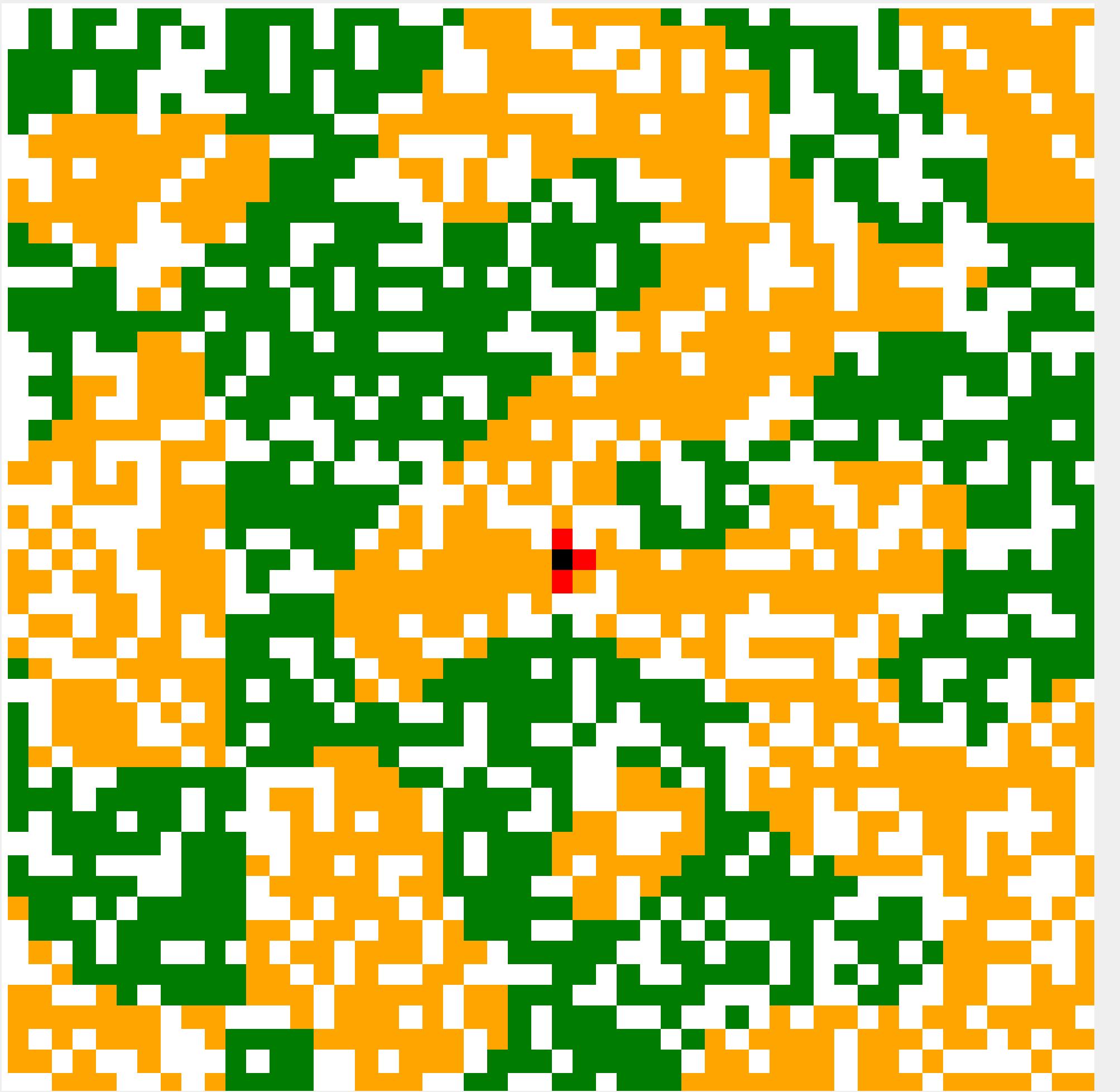
**Lowering the spreading probability makes the critical density shift towards 1.0 before disappearing**

4

How does a combination of a variety of burnable vegetation and environmental influences affect the critical density and does it still exhibit criticality?

**Adding longer-burning vegetation makes the critical density shift back toward base model**





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# APPENDIX

# Bibliography

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Beer, T., & Enting, I. G. (1990). Fire spread and percolation modelling. *Mathematical and Computer Modelling*, 13(11), 77-96.

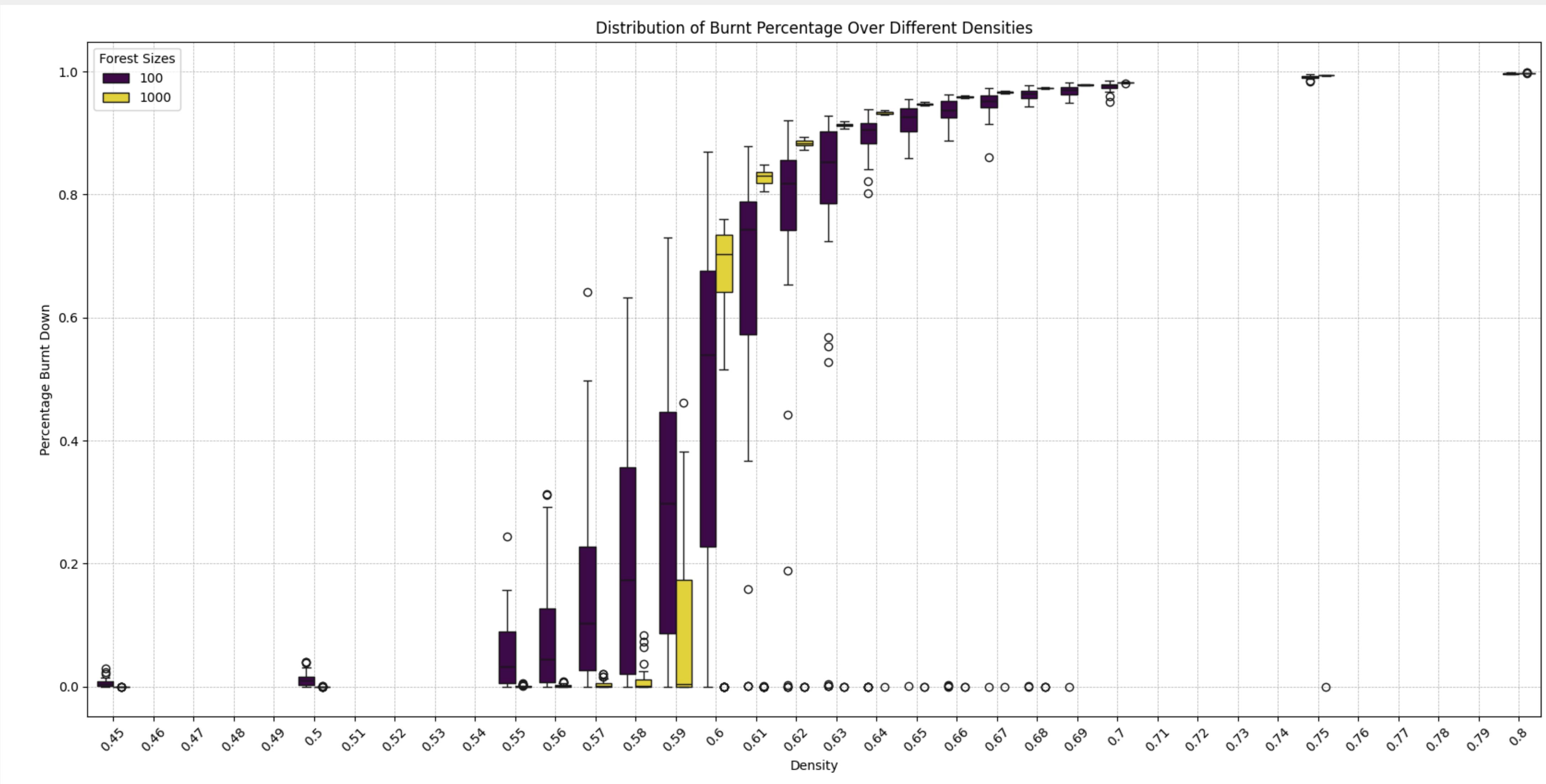
Duane, A., Miranda, M. D., & Brotons, L. (2021). Forest connectivity percolation thresholds for fire spread under different weather conditions. *Forest Ecology and Management*, 498, 119558.

Galeano Sancho, D. (2015). Percolation theory and fire propagation in a forest.

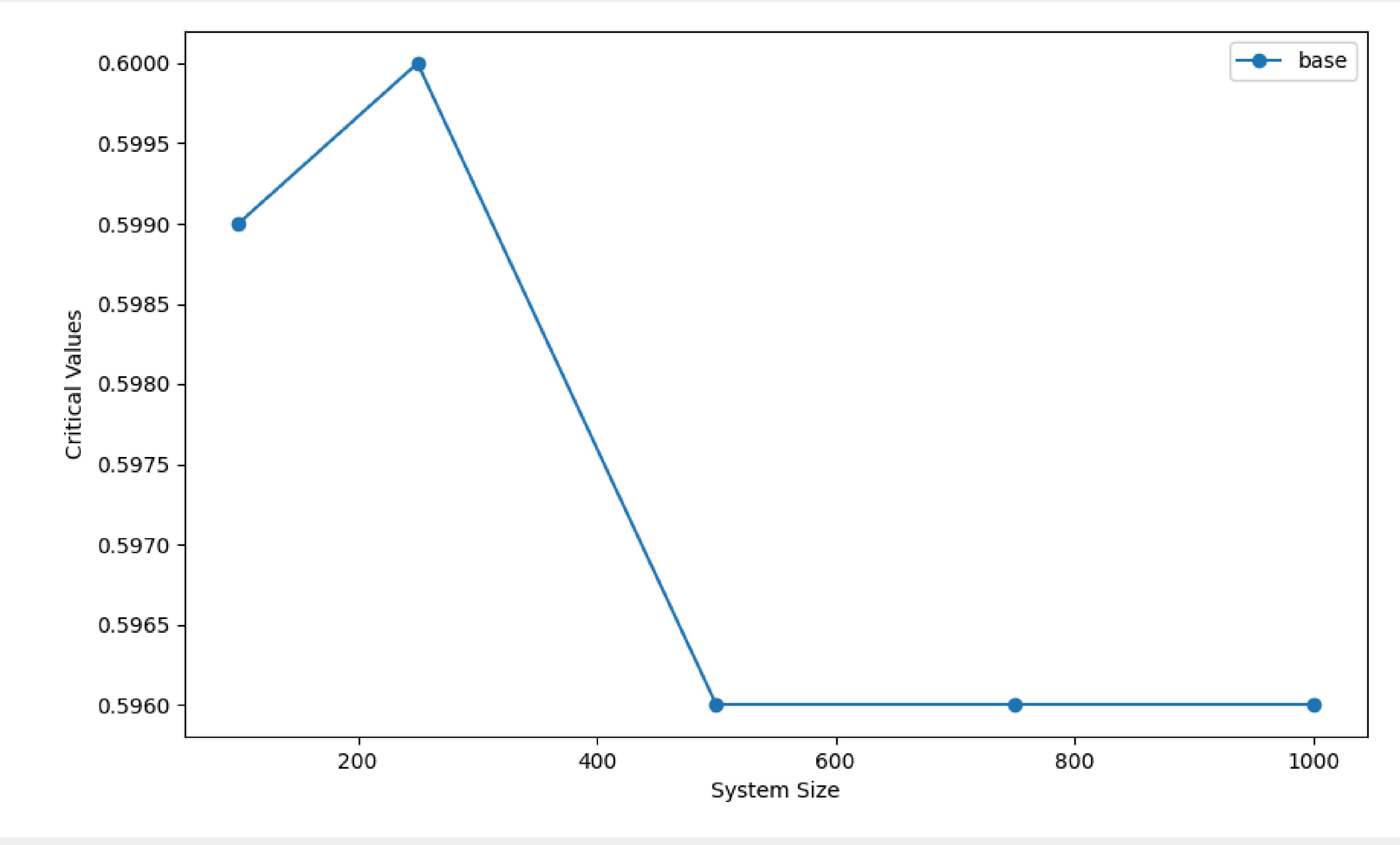
Perestrelo, S. A., Grácio, M. C., Ribeiro, N. D. A., & Lopes, L. M. (2022). A multi-scale network with percolation model to describe the spreading of forest fires. *Mathematics*, 10(4), 588.

Von Niessen, W., & Blumen, A. (1986). Dynamics of forest fires as a directed percolation model. *Journal of Physics A: Mathematical and General*, 19(5), L289.

# Burnt Percentage Variance Base Model

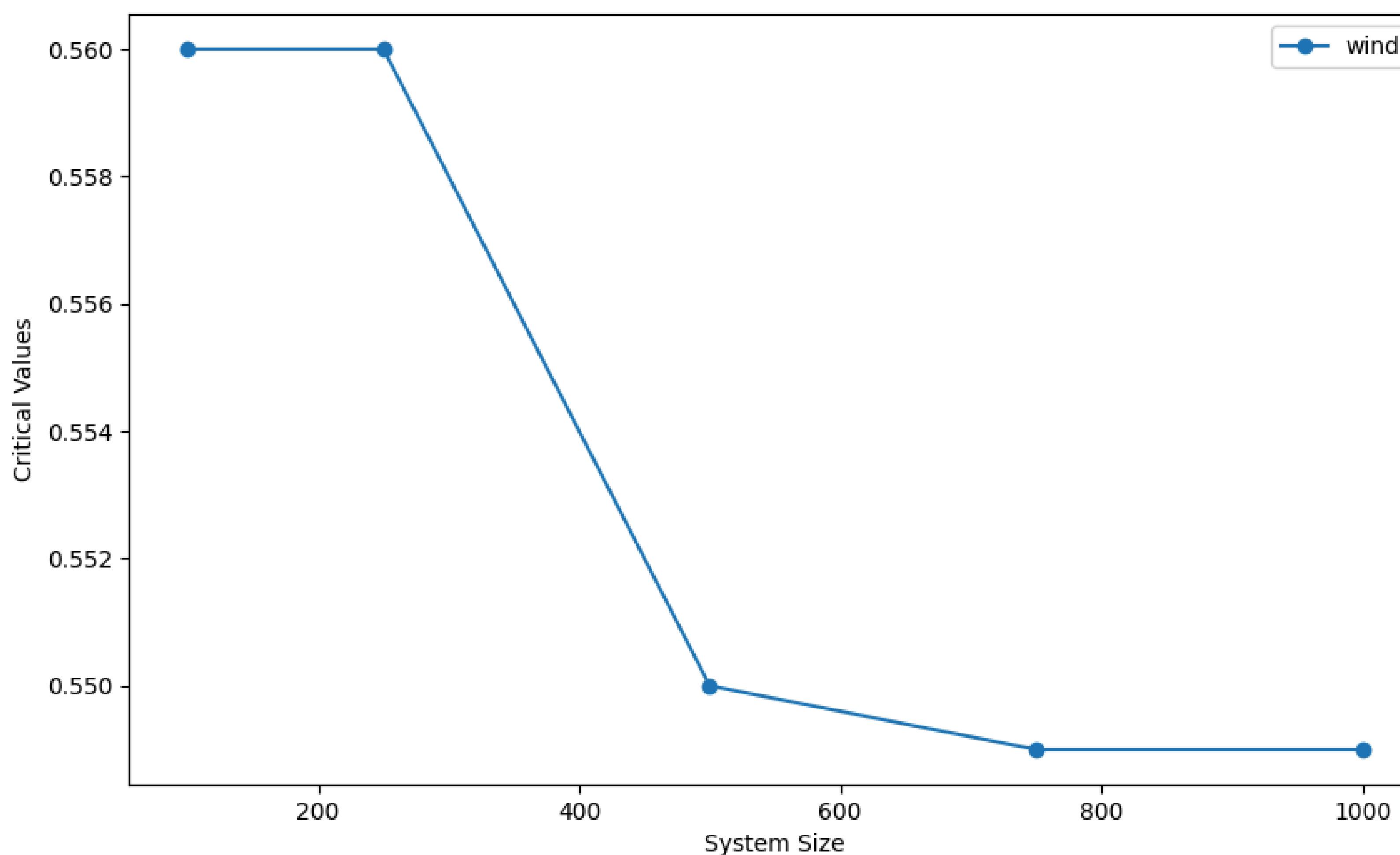


# Critical Density over System Size for Base Model



Wind ~ No  
P ~ 1  
Plant/Tree ~ 0  
 $\Delta$ Tree ~ 1

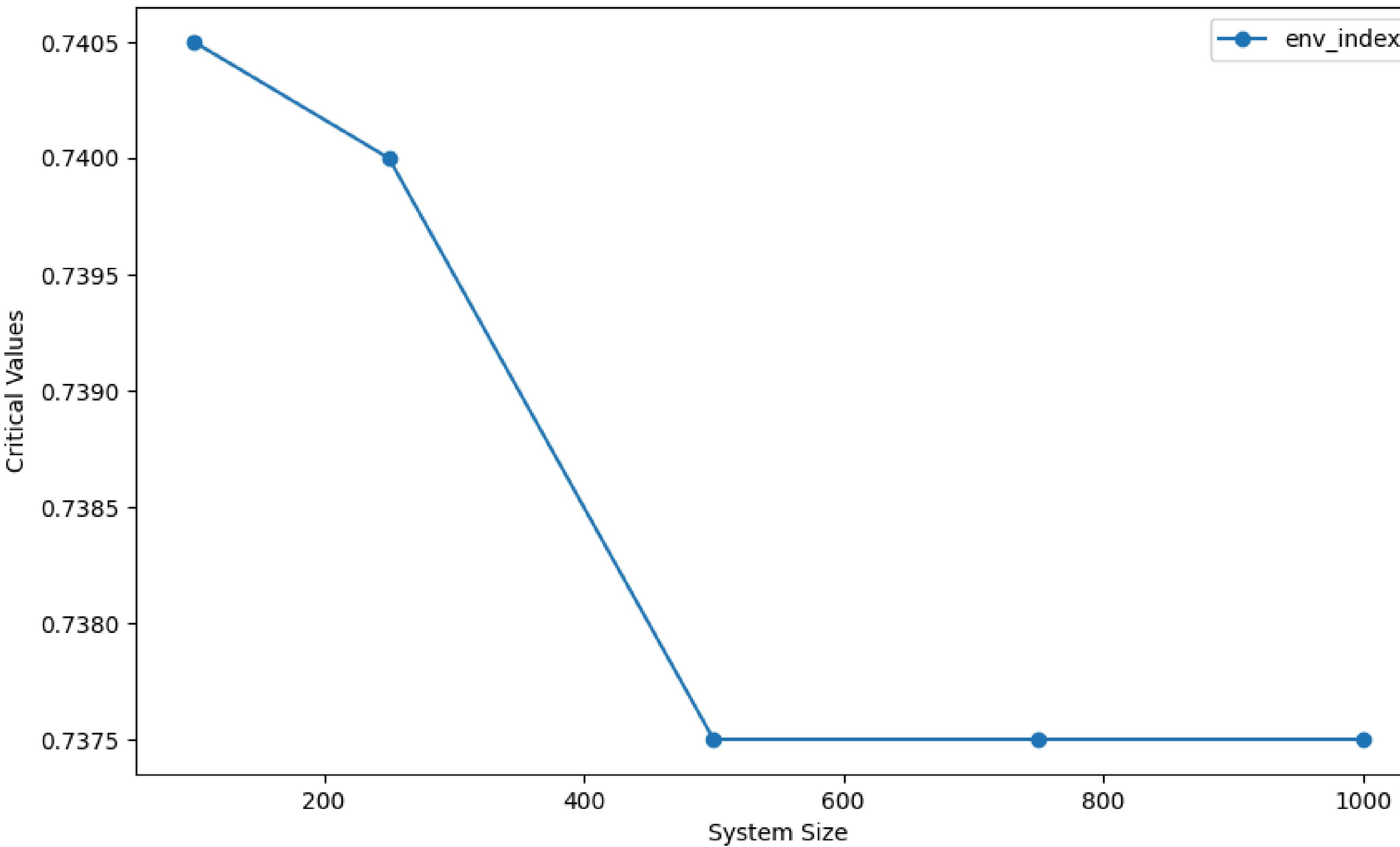
# Critical Density for Base Model with Wind



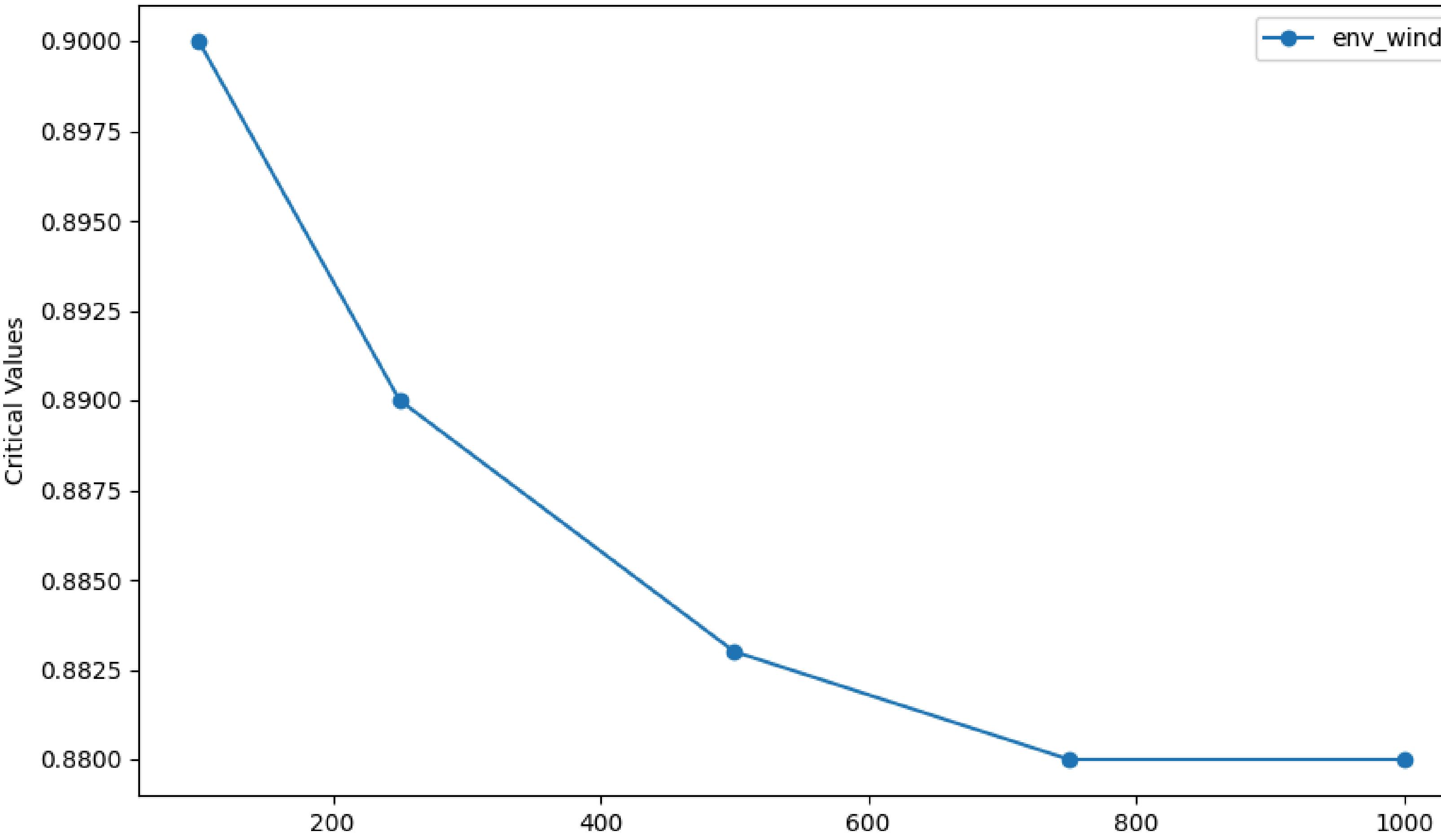
Wind ~ Yes  
P ~ 1  
Plant/Tree ~ 0  
 $\Delta$ Tree ~ 1

# Critical Density for Env Index 0.75

Wind ~ No  
P ~ 0.75  
Plant/Tree ~ 0  
 $\Delta$ Tree ~ 1



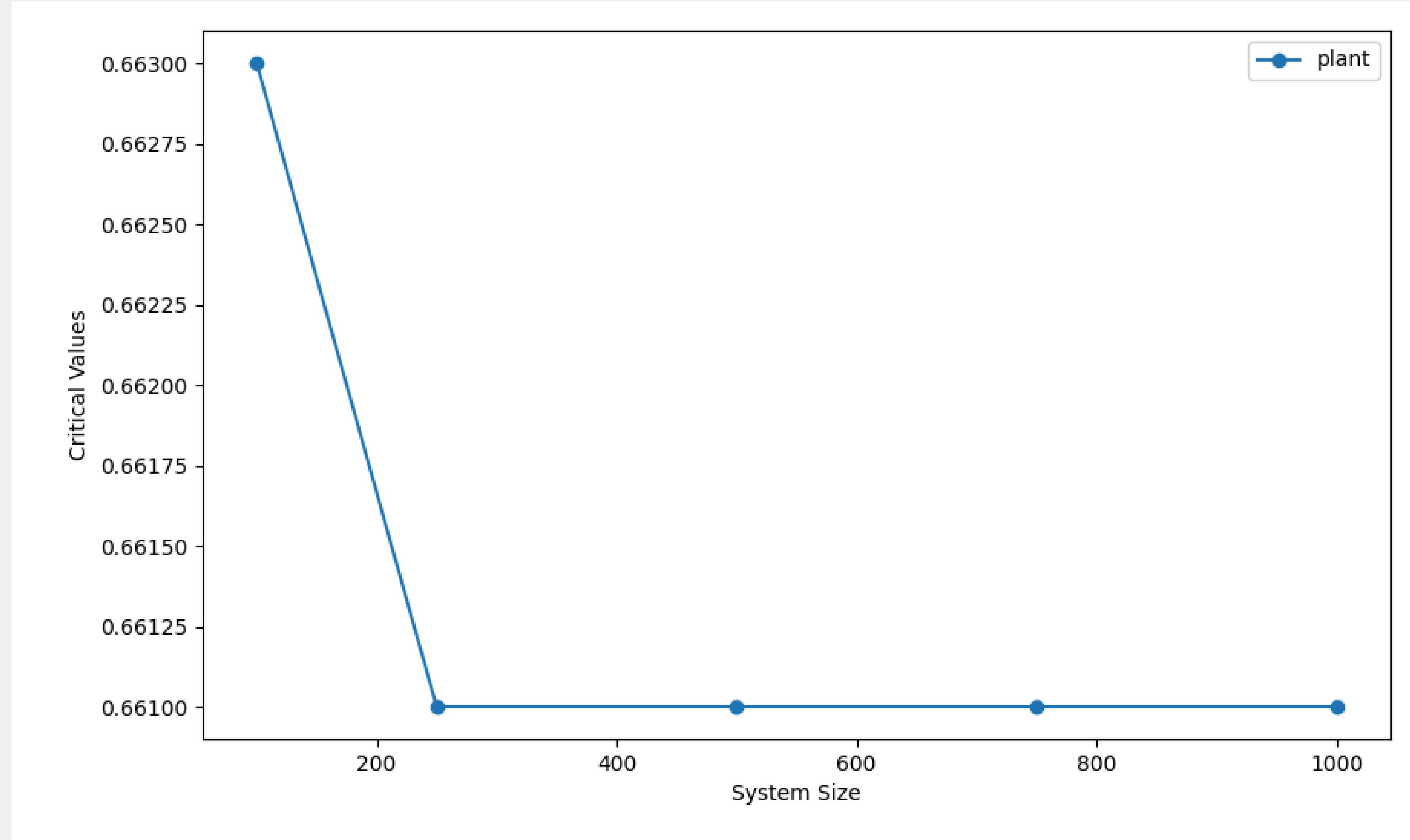
# Critical Density for Env Index 0.5 with Wind



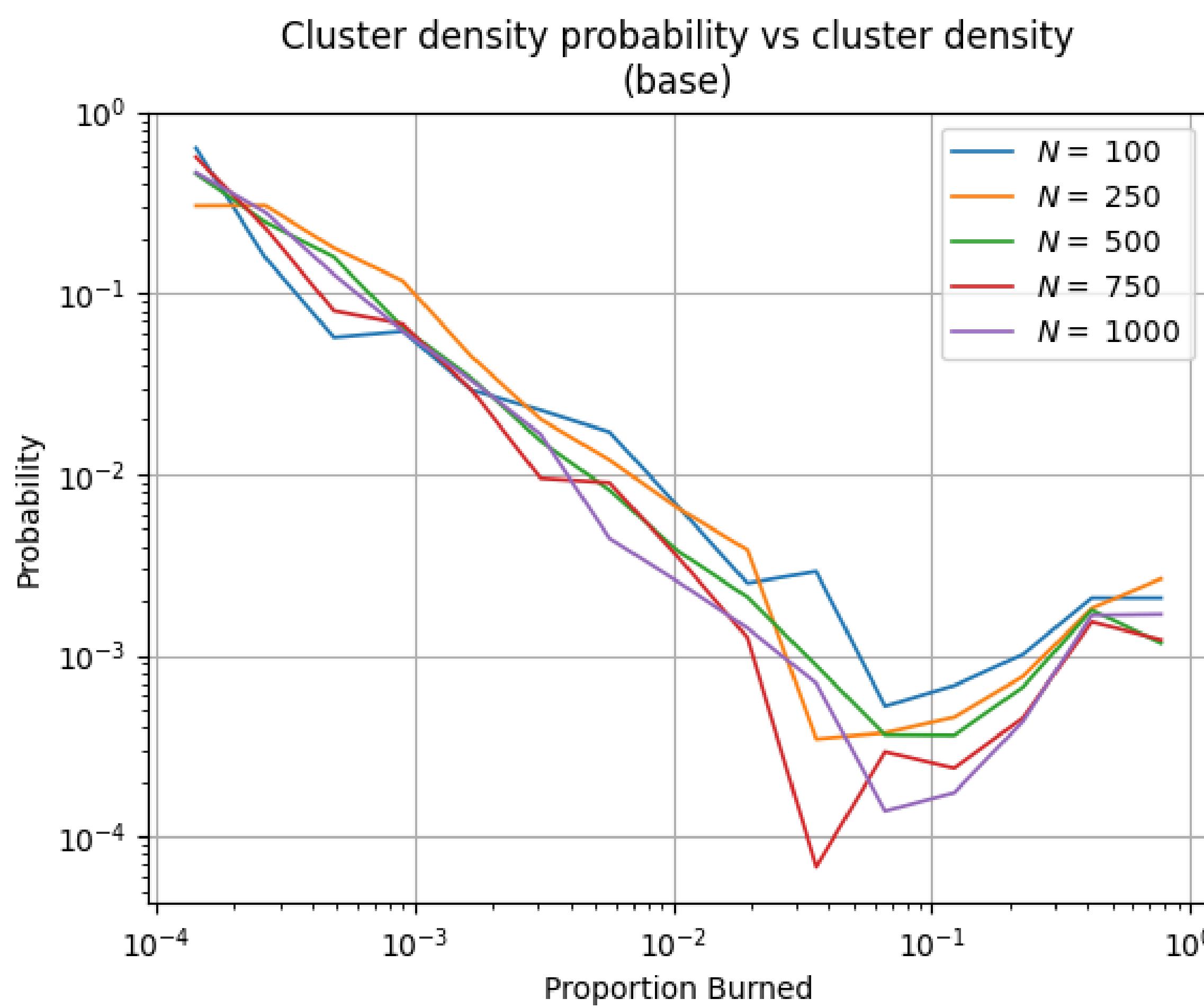
Wind ~ Yes  
P ~ 0.5  
Plant/Tree ~ 0  
 $\Delta$ Tree ~ 1

# Critical Density for Plant/Tree Burn Time Dif

Wind ~ No  
P ~ 0.75  
Plant/Tree ~ 0.5  
 $\Delta$ Tree ~ 3

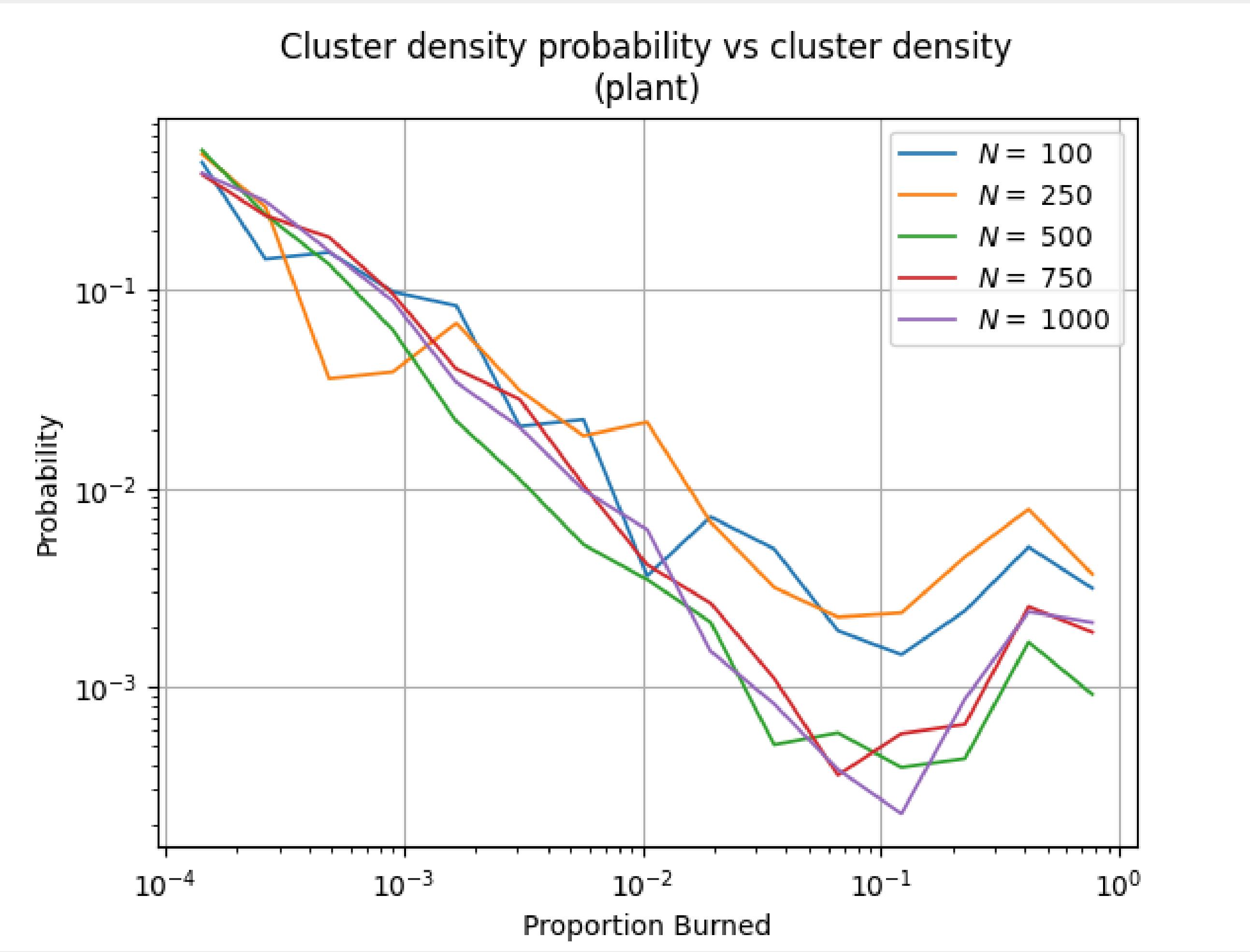


# Data Collapse Base Model



Wind ~ No  
P ~ 1  
Plant/Tree ~ 0  
 $\Delta$ Tree ~ 1

# Data Collapse Plant Model



Wind ~ No  
P ~ 1  
Plant/Tree ~ 0  
 $\Delta$ Tree ~ 1