

# SEM 2019 / WEEK 1: Exercise 1.2

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## a) LINEAR REGRESSION

In this exercise a linear regression model was built for one continuous observed dependent variable (y1) with two covariates (x1 and x3). The data “ex3.1” was first manually imported into R and saved as .Rdata -file with R code lines:

```
df <- ex3.1
save(df, file="df.Rdata")
```

Here is a summary of the variables:

```
load("df.Rdata")
summary(df)
```

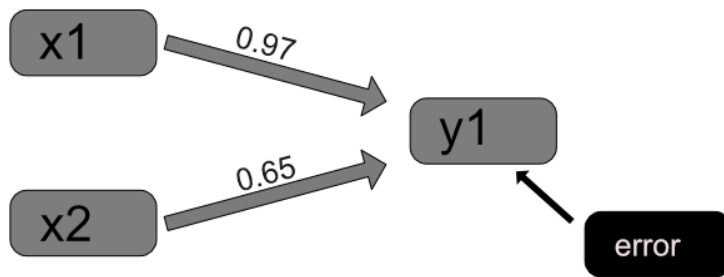
##	V1	V2	V3
## Min.	:-4.1163	Min. :-3.145148	Min. :-3.13875
## 1st Qu.:	-0.5269	1st Qu.:-0.749801	1st Qu.:-0.75466
## Median :	0.4288	Median : 0.023194	Median :-0.04029
## Mean :	0.4848	Mean : 0.001289	Mean :-0.04216
## 3rd Qu.:	1.5721	3rd Qu.: 0.755620	3rd Qu.: 0.71940
## Max. :	5.1110	Max. : 2.920440	Max. : 2.87514

Then a model was built according to instructions (y1 is the dependent variable, x1 and x3 are independent explanatory variables):

```
y1 <- df$V1
x1 <- df$V2
x3 <- df$V3

model <- lm(y1 ~ x1 + x3)
summary(model)
```

```
##
## Call:
## lm(formula = y1 ~ x1 + x3)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -3.1506 -0.5752  0.0235  0.5663  3.1899
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  0.51096    0.04356   11.73  <2e-16 ***
## x1           0.96949    0.04163   23.29  <2e-16 ***
## x3           0.64904    0.04451   14.58  <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.9731 on 497 degrees of freedom
## Multiple R-squared:  0.609, Adjusted R-squared:  0.6075
```



```
## F-statistic: 387.1 on 2 and 497 DF, p-value: < 2.2e-16
```

According to the results both covariates x1 and x3 are statistically significant ( $p < 0.001$ ). They both have a positive effect on the variable y1: when x1 increases one unit, the variable y1 increases 0.97 units (when x3 is considered a constant) and when x3 increases one unit, the variable y1 increases 0.65 units (when x1 is considered a constant). The model explains around 60% of the variance in the variable y1 (Adjusted R-squared = 0.6075).

The graph of the model is on top of this page (drawn with Affinity Designer):

## b) EXPLORATORY FACTOR ANALYSIS

In this part an exploratory factor analysis is conducted according to instructions. The data file “ex4.1a” was imported manually into R and then wrangled so that the analysis could be run. The wrangling code is here:

```
df2 <- ex4.1a
```

```
colnames(df2) <- c("y1", "y2", "y3", "y4", "y5", "y6", "y7", "y8", "y9", "y10", "y11", "y12")
```

```
save(df2, file="df2.Rdata")
```

Let us view a summary of the data:

```
load("df2.Rdata")
summary(df2)
```

```
##          y1          y2          y3
##  Min.   :-2.886760  Min.   :-3.69059  Min.   :-2.588919
## 1st Qu.: -0.682516  1st Qu.: -0.61723  1st Qu.: -0.673121
## Median :  0.013133  Median :  0.06940  Median : -0.071101
## Mean    :  0.008001  Mean    :  0.03339  Mean    :  0.003162
## 3rd Qu.:  0.700274  3rd Qu.:  0.69136  3rd Qu.:  0.689685
## Max.    :  2.529128  Max.    :  2.79520  Max.    :  2.967696
##          y4          y5          y6
##  Min.   :-3.214602  Min.   :-2.94869  Min.   :-2.500254
## 1st Qu.: -0.577758  1st Qu.: -0.56400  1st Qu.: -0.630876
## Median : -0.006558  Median :  0.04973  Median : -0.007958
## Mean    :  0.073489  Mean    :  0.06330  Mean    :  0.062216
## 3rd Qu.:  0.768797  3rd Qu.:  0.76779  3rd Qu.:  0.792593
## Max.    :  2.892782  Max.    :  3.74102  Max.    :  3.253644
##          y7          y8          y9
##  Min.   :-2.798568  Min.   :-3.581810  Min.   :-2.76235
## 1st Qu.: -0.631859  1st Qu.: -0.608176  1st Qu.: -0.64894
```

```
## Median : 0.002374 Median : 0.030146 Median :-0.04405
## Mean :-0.003501 Mean : 0.009048 Mean : 0.02085
## 3rd Qu.: 0.688036 3rd Qu.: 0.692113 3rd Qu.: 0.69171
## Max. : 3.446497 Max. : 2.827687 Max. : 2.93974
## y10 y11 y12
## Min. :-3.62913 Min. :-2.747190 Min. :-3.442931
## 1st Qu.: -0.75897 1st Qu.: -0.680559 1st Qu.: -0.706488
## Median : 0.01185 Median : 0.024163 Median :-0.008250
## Mean :-0.03686 Mean : 0.001595 Mean :-0.002375
## 3rd Qu.: 0.63595 3rd Qu.: 0.692018 3rd Qu.: 0.655408
## Max. : 3.03250 Max. : 3.273354 Max. : 2.971878
```

The data consists of 500 rows and 12 columns. Let us conduct the exploratory factor analysis with 4 factors as instructed:

```
analysis <- factanal(df2, factors = 4)
print(analysis)
```

```
##
## Call:
## factanal(x = df2, factors = 4)
##
## Uniquenesses:
## y1 y2 y3 y4 y5 y6 y7 y8 y9 y10 y11 y12
## 0.588 0.346 0.594 0.581 0.424 0.543 0.462 0.470 0.498 0.520 0.376 0.559
##
## Loadings:
## Factor1 Factor2 Factor3 Factor4
## y1 0.637
## y2 0.807
## y3 0.632
## y4 0.645
## y5 0.757
## y6 0.673
## y7 0.733
## y8 0.727
## y9 0.706
## y10 0.691
## y11 0.789
## y12 0.659
##
## Factor1 Factor2 Factor3 Factor4
## SS loadings 1.576 1.544 1.467 1.453
## Proportion Var 0.131 0.129 0.122 0.121
## Cumulative Var 0.131 0.260 0.382 0.503
##
## Test of the hypothesis that 4 factors are sufficient.
## The chi square statistic is 25.36 on 24 degrees of freedom.
## The p-value is 0.386
```

The hypothesis that four factors is sufficient is supported by the p-value (chi square statistic = 25.36,  $p = 0.386$ ). A graph of the model is presented on the next page.

