Paris School of Economics

Michał Miktus, Mateusz Szmidt

Machine learning approach to trade flows estimation

Final project for Trade Policy in Analysis and Policy in Economics

Contents

ntroduction
. Literature review
Data exploration
Neural network approach
. Results
Concluding remarks
Bibliography
Appendix A
Appendix B
Appendix C
Annondiy D

List of Figures

2.1.	Trade flows between Poland and its trading partners	10
2.2.	Histogram of flows over the history	10
2.3.	Histogram of flows in specific years	11
2.4.	Pairplots	12
3.1.	Activation functions	14

List of Tables

2.2.	Variables and their description	8
2.1.	Summary statistics	Ć
4.1.	Results of Poisson Pseudo-Maximum Likelihood estimation	16
4.2.	Results of neural network	17

Introduction

Since the pioneer work of Tinbergen (1962), the gravity equations has been widely implemented in the estimation of bilateral trade flows. The fundamental insight that the volume of trade between two countries is proportional to the product of an index of their economic sizes diminished by the measures of "trade resistance" between them has shaped the empirical specifications mainly due to the surprisingly good fit to the majority of data sets of both regional, as well as international trade flows. Over time the Tinbergen (1962) approach has been modified and enhanced, not to mention the supplementary theoretical underpinnings such as additional measures of trade resistance in spite of the classical ones (geographic distance, a dummy for common borders or dummies for Commonwealth memberships) or better estimation methods, allowing for the inclusion of zero-trade flows in the framework.

The following paper aims to implement the modern machine learning algorithms in the framework of gravity modeling in order to predict the bilateral trade flows. Machine learning can be viewed as an application of artificial intelligence (AI) which provides systems the ability to automatically learn and improve from experience without being explicitly programmed. In other words, machine learning focuses on the development of computer programs that can access data and use it learn for themselves, without human intervention or assistance, and adjust actions accordingly. The latest advancements in machine learning allowed to effortlessly identify patterns in data and use them to automatically make predictions or decisions. To the authors' best knowledge, the following paper is the first try in implementing the above-mentioned framework to the trade policy analysis.

In addition, due to the familiarity of both authors to the Polish trade environment, the Poland trade relations has been chosen as a workhorse illustration. Obtained results prove that a neural network approach can be viewed as a grievous challenger to the classical estimation methods, such as Poisson Pseudo-Maximum Likelihood models or ordinary fixed panel data estimators.

The paper is organized as follows: the first chapter consists of the brief literature review, including the common gravity models and the estimation techniques, followed by the data characterization. Next sections provide a detailed description of the neural network approach enhanced by the hyper-parameters tuning and outline the main results. The paper is completed with the concluding remarks with potential extensions, references and appendices with codes in R and Python.

Literature review

The traditional gravity model was developed in the 1960s to explain factory-to-consumer trade (Tinbergen (1962)). The above-mentioned concept was at the heart of the first clear microfoundations of the gravity equation – the seminal Anderson (1979), proposing a theoretical explanation of the gravity equation based on constant elasticity of substitution preferences of nations producing a single differentiated product. In parallel, the monopolistic competition versions were introduced (Krugman (1980), Bergstrand (1985)), followed by the work of Anderson and Van Wincoop (2003), expanding appropriate econometric techniques and introducing the microeconomic framework to the previously promoted monopolistic competition. Subsequent theoretical refinements have further focused on showing that the gravity equation can be derived from trade models with heterogeneous firms (Helpman et al. (2008)).

Simultaneously, the estimation techniques were progressing, starting from the basic least square estimator and its correspondent panel data version, meaning the fixed effect estimator. The endogeneity issues guided to the establishment of instrumental variables and two step least squares methodologies in the gravity models framework. Therefore, the Poisson Pseudo-Maximum Likelihood (henceforth PPML) model, introduced by Santos Silva and Tenreyro (2006), as well as zero-inflated models were proposed in order to solve the mentioned problems. Over the years, they became the flagship framework for the bilateral trade flows estimation with some dominance of PPML, mainly due to its statistical properties such as robustness to different forms of heteroskedasticity.

However, the aforementioned advantage was often criticized over the years, not to mention Martin and Pham (2008) who admitted that PPML estimator is in fact less biased than formerly used methods, but not necessarily fully unbiased. This view was further supported by Martínez-Zarzoso (2013) who compared it within a family of GLS models, arguing that the appropriate estimation method should be chosen with a greater caution. Consequently, authors attempt to propose a machine learning neural network algorithm as a potential competitor to the Poisson Pseudo-Maximum Likelihood estimator in the context of bilateral trade flows.

Data exploration

For the first part of the data, namely the set of explanatory variables, the CEPII statistics were used, resulting in annual data of 60 variables at the cross country level. Then, using 3 digit ISO codes the dataset was joined with the trade flows information. Nevertheless, in contrary to the first, fully available online dataset, in order to obtain data on flows from Comtrade database, a data scrapper needed to be created. The authors expanded and modified the scrapping function delivered by Comtrade which in the end allowed to bypass all the limitations build into basic API and optimize the time of data scrapping. The exact code can be found in Appendix A.

The final variables used in the calculations, along with their descriptions, are presented in the table Variables and their description, while the basic summary statistics are illustrated in the table Summary statistics.

Table 2.2: Variables and their description ${\cal L}$

Variable	Description
yr	Year
rt3ISO	Standard ISO code for reporting country (three letters)
pt3ISO	Standard ISO code for partner country (three letters)
contig	Dummy for contiguity
$_{ m heg_d}$	Dummy if parter country is current or former hegemon of origin
col _fr	Dummy for reporting and partner countries colonial relationship post 1945
colony sibling	Dummy for reporting and partner countries ever in colonial relationship Dummy for reporting and partner countries ever in sibling relationship i.e. two colonies of the same empire
$comleg_pretrans$	Dummy if reporting and partner countries share common legal origins before transition
$comleg_posttrans$	Dummy if reporting and partner countries share common legal origins after transition
transition_legalchange	Dummy if common legal origin changed since transition
legold_d	Legal system of partner country before transition. This variable takes the values: fr for French, ge for German, sc for Scandinavian, so for Socialist and uk for British legal origin
legnew_d	Legal system of partner country after transition. This variable takes the values: fr for French, ge for German, sc for Scandinavian, so for Socialist and uk for British legal origin
gatt_d	Dummy if partner country is GATT/WTO member
fta_wto	Dummy for Regional Trade Agreement
eu_to_acp	Dummy for ACP country exporting to EC/EU member
gsp_o_d flaggsp_o_d	Dummy if origin is donator in Generalized System of Preferences (GSP) Report changes in Roses data on <gsp_o_d>. No gsp recorded in Rose; Data directly from Rose; Changes in data from Rose; Assumption that gsp continues after 1999</gsp_o_d>
eu o	Dummy if reporting country a member of the European Union
eu_d	Dummy if partner country a member of the European Union
Trade value total	Total value of trade between reporting and partner countries
distw	Weighted bilateral distance between reporting and partner countries in kilometer (population weighted)
pop_o	Population of reporting country total in million
pop_d	Population of partner country total in million
gdp _o	GDP of reporting country (current US\$)
$\operatorname{gdp}_{\operatorname{d}}$	GDP of partner country (current US\$)
gdpcap _o	GDP per capita of reporting country (current US\$)
$gdpcap_d$	GDP per capita of partner country (current US\$)
$area_d$	Area of partner country in sq. kilometers
$\operatorname{tdiff}^{\overline{\overline{\overline{\overline{\overline{\overline{\overline}}}}}}}$	Time difference between reporting and partner countries in number of
$\operatorname{comrelig}$	hours. For countries which stretch over more than one time zone the respective time zone is generated via the mean of all its time zones (for instance: Russia, Canada, USA) Religious proximity (Disdier and Mayer (2007)) is an index calculated by
	adding the products of the shares of Catholics, Protestants and Muslims in the exporting and importing countries. It is bounded between 0 and 1 and is maximum if the country pair has a religion which (1) comprises a vast majority of the population and (2) is the same in both countries.

Table 2.1: Summary statistics

Variable	count	unique	top	freq	mean	std	min	25%	20%	75%	max	cova
gatt_o	4060.00	N_{aN}	NaN	NaN	1.00	0.00	1.00	1.00	1.00	1.00	1.00	0.00
area_o	4060.00	$_{ m NaN}$	$_{ m NaN}$	NaN	312685.00	0.00	312685.00	312685.00	312685.00	312685.00	312685.00	0.00
yr	4060.00	NaN	NaN	NaN	2004.49	6.31	1994.00	1999.00	2005.00	2010.00	2015.00	0.00
o_dod	4060.00	ZaZ ;	NaN;	ZaZ Z	38.33	0.22	38.00	38.15	38.23	38.54	38.66	0.01
gdp_o	4060.00	NaN	NaN	NaN	3.19e+11	1.55e+11	1.09e+11"	1.72e + 11	3.04e+11	4.77e+11	5.45e + 11	84.0
gapcap_o	4060.00	NaN NaN	NaN N°N	NaN N°N	8339.74	4052.41	0.00	4483.24	1 00	12554.55	14341.80	0.49 77
dist.w	4060.00	NaN	NeN	ZeZ	6140.89	3899.61	387.07	2603.11	5845.77	8583.18	17653.91	0.64
en o	4060.00	NaN	NaN	NaN	0.55	0.50	0.00	0.00	1.00	1.00	1.00	0.91
tdiff	4060.00	NaN	NaN	NaN	3.38	3.12	0.00	1.00	2.00	6.00	12.00	0.92
comrelig	4060.00	$_{\rm NaN}$	$_{\rm NaN}$	NaN	0.25	0.28	0.00	0.01	0.11	0.45	0.79	1.15
gdpcap_d	4060.00	NaN	NaN	NaN	10410.33	16066.97	64.81	864.06	3223.29	13299.54	116612.88	1.54
p_o_dsg	4060.00	NaN	$_{NaN}$	NaN	0.24	0.43	0.00	0.00	0.00	0.00	1.00	1.80
fta_wto	4060.00	NaN	$_{ m NaN}$	NaN	0.23	0.42	0.00	0.00	0.00	0.00	1.00	1.84
eu_to_acp	4060.00	$_{ m NaN}$	N_aN	N_{aN}	0.21	0.40	00.00	0.00	0.00	0.00	1.00	1.96
comleg_pretrans	4060.00	N_aN	N_aN	NaN	0.17	0.38	0.00	0.00	0.00	0.00	1.00	2.20
transition_legalchange	4060.00	NaN	NaN	NaN	0.13	0.34	0.00	0.00	0.00	0.00	1.00	2.55
area_d	4060.00	NaN	NaN	NaN	719321.80	1956801.49	25.00	25713.00	119902.00	547244.00	17075400.00	2.72
p—nə	4060.00	NaN :	NaN ;	ZaZ Z	0.11	0.32	0.00	0.00	0.00	0.00	1.00	2.81
comleg_posttrans	4060.00	ZaZ Z	Na Na Na Na Na Na Na Na Na Na Na Na Na N	Z SZ	0.10	0.30	0.00	0.00	0.00	0.00	1.00	2.96
p_dod	4060.00	NaN	NaN	NaN	34.23	129.66	1.00	1.69	6.66	21.70	1371.22	3.79
gap_d	4060.00	NaN N-N	NaN N-N	NaN	2.64e+11	I.13e+12	1.09e+07	3.1be+09	1.4be+10	1.04e+11	1.80e+13	4.30
Irade_value_total	4060.00	NaN	NaN	NaN	1.12e+09	5.30e+09	0.00	1.52e+06	2.34e+U/	2.35e+08	1.03e+11	47.74
config	4060.00	NaN	Nan	NaN	0.04	0.19	0.00	0.00	0.00	0.00	1.00	5.04 6.03
Similar	4060.00	NaN	NaN	NaN	0.03	0.10	0.00	00.0	00.0	0.00	1.00	0.02 13 55
coloury col fr	4060.00	N S N	N S N	N Z	0.01	0.07	00.0	0.00	00.0	0.00	1.00	13.00
hes d	4060.00	NaN	NaN	Na.N	0.01	0.07	0.00	00.0	0.00	0.00	1.00	13.55
rt3ISO	4060.00	1	POL	4060	NaN	NaN	NaN	NaN	NaN	NaN	NaN	NaN
pt3ISO	4060.00	190	ARE	22	NaN	NaN	NaN	NaN	NaN	NaN	NaN	NaN
iso2_o	4060.00	1	PL	4060	$N_{a}N$	NaN	NaN	$_{\rm NaN}$	NaN	NaN	NaN	$_{NaN}$
iso2_d	4060.00	190	BZ	22	NaN	NaN	NaN	NaN	NaN	$_{\rm NaN}$	$_{ m NaN}$	$_{\rm NaN}$
comlang_off	4060.00	$_{ m NaN}$	$_{ m NaN}$	NaN	0.00	0.00	0.00	0.00	0.00	0.00	0.00	$_{NaN}$
comlang_ethno	4060.00	N_aN	N_aN	NaN	0.00	0.00	0.00	0.00	0.00	0.00	0.00	$_{\mathrm{NaN}}$
comcol	4060.00	NaN	NaN	NaN	0.00	0.00	0.00	0.00	0.00	0.00	0.00	NaN
col45	4060.00	NaN	NaN	NaN	0.00	0.00	0.00	0.00	0.00	0.00	0.00	NaN
hego	4060.00	ZaZ Z	Z SZ	ZaZ Z	0.00	0.00	0.00	0.00	0.00	0.00	0.00	NaN S
col_to	4060.00	NaN	NaN	NaN	0.00	0.00	0.00	0.00	0.00	0.00	0.00	Nan
curcol	4060.00	NaN	NaN	NoN	00.0	0.00	00.00	00.0	00.0	0.00	0.00	NoN
Cuisib	4060.00	NaN	NaN	NaN	00.0	0.00	00.0	00.0	00.0	00.0	0.00	NaN
legold o	4060.00		5	4060	Ne.N	Se N	Ne.N	S.S.	NeN Ne	S.S.	Ne N	NeN
legold d	4060.00	H YC	f.	1759	NeN	NaN	NeN	NeN	NaN	NeN	NaN	NeN
legnew o	4060,00	· 	i a	4060	NaN	NaN	ZeZ	NeN	NaN	NaN	NaN	NaN
legnew d	4060.00	70	fr	2153	NaN	NaN	NaN	NaN	NaN	NaN	NaN	NaN
acp_to_eu	4060.00	NaN	$N_{a}N$	NaN	0.00	0.00	0.00	0.00	0.00	0.00	0.00	NaN
p_p_dsg	4060.00	NaN	$_{\rm NaN}$	NaN	0.00	0.00	0.00	0.00	0.00	0.00	0.00	$_{\rm NaN}$
flaggsp_o_d	4060.00	က	dsg ou	3099	N_aN	NaN	NaN	$_{NaN}$	NaN	N_aN	NaN	NaN
			recorded in Rose									
flaggsp_d_d	4060.00	1	dsg ou	4060	NaN	$N_{a}N$	NaN	$N_{a}N$	NaN	$N_{a}N$	NaN	NaN
			recorded in Rose									
			TIL ACCOUNT									

Where the columns denote respectively the variables described, the number of observations, the amount of unique values, the most frequent value (for categorical variables), the frequency of the most frequent value, the mean, the standard deviation, the minimum value, the first quantile, the median, the third quantile, the maximum value and finally the coefficient of variation.

Furthermore, due to the fact that the authors concentrated their attention on the trade flows of Poland with its partner, the following graphs demonstrate that Poland mainly trades with Unites States, China and Europe.

Trade flows between Poland and its trading partners.



Trade flows between Poland and its trading partners.



- (a) Trade flows between Poland and its world trading partners
- (b) Trade flows between Poland and its European trading partners

Figure 2.1: Trade flows between Poland and its trading partners

Moreover, the histogram of standarized trade flows of Poland from 1994 to 2015 certifies that there is a relatively large group of countries with which Poland is not involved in trading relations.

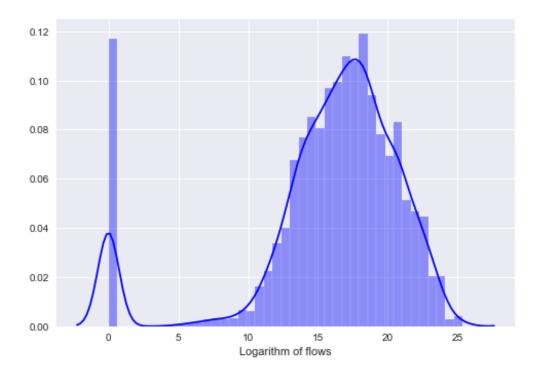


Figure 2.2: Histogram of flows over the history (overall)

The aforementioned fact it complemented with the histograms in specific years: 1994, 2000, 2009 and 2015. However, it can be noticed that the amount of trading partners was gradually increasing over time.

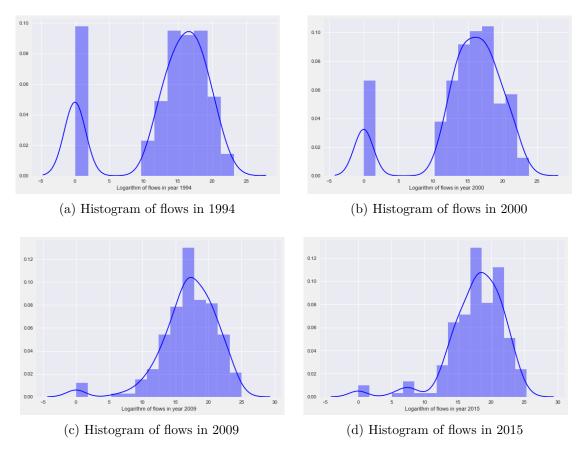


Figure 2.3: Histogram of flows in specific years

Finally, as the main interest of the following paper is the gravity model, the relations between total trade value, distance and partner country's GDP (standarized) are demonstrated in the pairplots graphs.

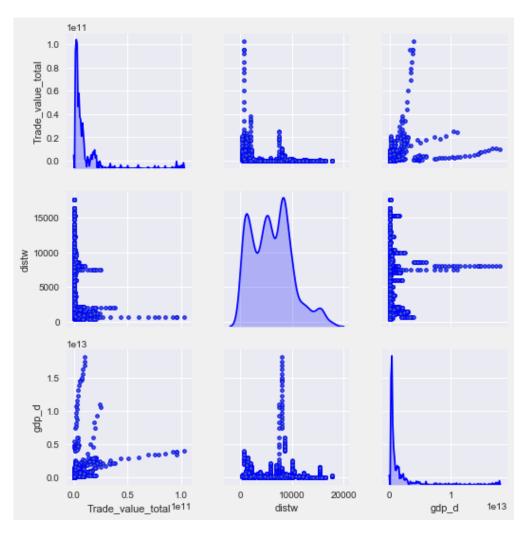


Figure 2.4: Pairplots between total trade value, distance and partner country's GDP (standarized)

Accordingly to the intuition, the value of trade is lower for the more distanced countries, while on contrary it seems to be positively correlated with the trading country's gross domestic product, which can be regarded as the proxy for the nation's size.

Neural network approach

The neural networks approach is a statistical framework allowing to find complex patterns of relations in the data. The intuition behind the above-mentioned concept is often compared to the way of how human nerve system functions. In a nutshell, it can be characterized as follows - in the first phase the external signal is received by receptors and transferred to the set of neurons. Then, during further stages, it is iteratively processed and passed to next set of neurons until the signal is finally decoded. The structure of the neural network model similarly compounds of 3 elements: the input layer of independent variables, set of "hidden layers" and finally the output layer with calculated results of a model. Given the structure, in each phase besides the last one, the values of nodes from former layer are affinely transformed and then nonlinear function in performed in order to obtain the values for each node of a new layer. The calculations are repeated until the last phase when the final value is accessed through a nonlinear function of affine product of nodes from previous layers. The aforementioned process, starting from an input data and aiming to compute the output, is called the forward propagation and can be seen as a function of coefficients coined within every single affine transformation taking place between all neighbouring layers.

As a result, the estimated trade flows from the neural network approach rely on finding the appropriate values of parameters under arbitrary selected structure of a model. Thus in the first stage, the values of the coefficients are randomly assigned and then the forward propagation is performed. Next, based on model's output and true values of the observable dependent variable, the arbitrary chosen loss function is calculated. It has to be underlined that due to the fact that the generated output is a result of forward propagation, the loss function can be also defined as a function of the same parameters. It allows to compute a derivative with respect to them and in the end, to recalibrate their values – such a process is called *backward propagation* and it is iteratively repeated together with forward propagation to minimize the loss function, optimizing the values of parameters.

Although the intuition and general process behind the estimation of neural network model were presented above, a plethora of aspects referred to depends on arbitrary chosen structure or so called *architecture of a model*. Therefore, some choices implemented in

the final, best suited to the data architecture of the model need to be elaborated.

Firstly, a number of hidden layers intuitively allows to approximate any continuous function more carefully, nevertheless adding any next layer is computationally costly. The charge born is strictly related to another element of a model's structure, namely the number of neurons in each layer. It has to be emphasised that the above-mentioned amount can be different depending on a layer but again bigger number directly translates into higher cost. Consequently, to take advantage of computer architecture and to optimize processing time, a power of 2 neurons in each layer were implemented, as suggested in the literature.

It has been already mentioned that each node is in fact defined as a function of the values of neurons from the former layer. It is thus beneficial to remark that it can be enforced that a node from hidden layer is a function of only a subset of nodes from a former one. Depending on the problem such an idea might be intuitive, not to mention the picture recognition, but it does not seem to be relevant in trade flows case. What is more, during the learning process such an exclusion of particular nodes may appear anyway, when the weights in affine transformations are relatively close to zero. Thus, the network with nodes being functions of all previous ones will be considered.

Moreover, the nonlinear transformation of a product of former nodes has to be defined. In the neural network framework, it is often called *an activation function*, aiming to activate the particular neuron on a hidden layer and assign to it some positive value when the particular pattern within a former nodes is observed. In a neural network literature, a particular set of functions can be observed, which by construction allows the model to be trained faster due to computational advantage while deriving derivatives and which satisfy the basic intuition behind activation. The most common ones are presented below.

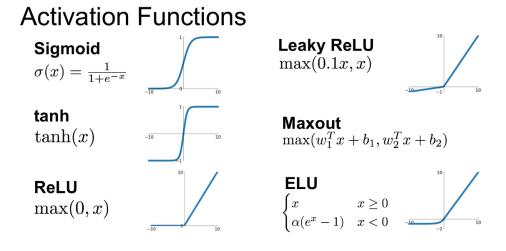


Figure 3.1: Activation functions¹

¹Source: https://bit.ly/2uh7NyV

The actually implemented in the end are sigmoid and relu. The first one was especially popular in the past, while the second one gained the popularity recently, outperforming the former with respect to the computational time.

At this stage, the part of hyper-parameters of models' structure directly connected to the forward propagation was covered. As far as the backward propagation choices are concerned, a loss function given the generated output has to be chosen. In the paper, the mean squared error was selected to validate the output. Moreover, in order to prevent the problem of overfitting, the regularization was implemented. The role of the aforementioned concept is simply to penalize the actual loss function of the model so that increase of the coefficients to some extent negatively affects the loss function. The value of a hyper-parameter of a penalty function identifies the size of marginal increase in a loss function alone to be compensated by the penalty.

Another regularization approach which can be implemented simultaneously is dropout. It serves to omit a fraction of randomly chosen nodes (along with their connections) on each layer while performing both forward and backward propagation. Thus, it enforces iterative deactivation of different neurons which diminish the pace of convergence but also stanches from overfitting the model. Nevertheless, it may simultaneously negatively influence the convergence, therefore a maximum number of iterations, in neural network framework called *epochs*, has to be specified. Choice of its value always brings a trade-off between a computational time and optimality of solution. One way (actually implemented in the paper) of meeting halfway is to set a threshold for marginal increase in loss function, ending the learning process sooner if the condition is fulfilled.

In fact, it is a learning process itself which determines the final performance of neural network framework. To fully define it, few more elements of a model's structure have to be recalled. As mentioned before, the estimation is based on calculating numerous derivatives with respect to all the parameters, according to the chain-rule, which in the end determines for a given set of parameters' values a point-gradient. However, as the neural networks tend to be defined over an enormous parameter space, the straightforward calculation of a gradient might be a complex task itself. Therefore, different optimization algorithms were implemented. The first one is Stochastic Gradient Decent (SGD), which calculates new iteration of parameters according to the specified learning rate, which is in turn another hyper-parameter of the model, defining the convergence speed. However, in standard SGD the learning rate is not scalable and it poorly handles updating the parameters of high variance. To deal with it, the second method is proposed, namely the Adam optimizer, which becomes gradually common recently. It allows to adjust the specified learning rate for each parameter and is often more efficient. Lastly, to speed up the whole process the hyper-parameter called batch size can be defined. The model chooses a subsample in a size of batch and performs an iteration using only selected observations. Therefore, it allows to train the model each time on different observation set and reduces the complexity of the whole process.

At this stage all the elements of model architecture are defined, allowing to implement the neural network on the presented grid of hyper-parameters and proceed with an estimation, with exact codes included in Appendix B.

Results

Fixed effect, dummy na rok, nie dajemy fixed effect, ale są możliwe na rządanie, , wypierdalamy bo colinearity socjo niesistotne ale

Table 4.1: Results of Poisson Pseudo-Maximum Likelihood estimation

	Estimate	Std. Error	t value	$\Pr(> t)$
Intercept	54.8905	20.4869	2.68	0.0074
$\operatorname{dist} \operatorname{log}$	-4.6382	2.5546	-1.82	0.0695
$\operatorname{comrelig}$	1.7794	5.4022	0.33	0.7419
$gatt_d$	0.5378	0.0527	10.20	0.0000
$legnew_d_so$	1.3770	2.7106	0.51	0.6115

Degrees of Freedom:

3148 Total 2947 Residual Null Deviance: 1.211e+13 Residual Deviance: 2.351e+11

CHUJ, kody odswiezyc

The following parameter space was considered during the estimation procedure:

As far as the main outcomes from the trade flows prediction through a neural network approach are concerned, the best performing ten models are presented in the following Results Table.

Table 4.2: Results of neural network

N	N_iter	Val_loss	Val_MSE	Loss	MSE	LR	L1	L2
1	38	0.176	0.176	0.037	0.037	0.5	0.000	0.000
2	61	0.197	0.197	0.04	0.04	0.5	0.000	0.000
3	38	0.224	0.224	0.046	0.046	0.5	0.000	0.000
4	185	0.249	0.249	0.041	0.041	0.1	0.000	0.000
5	40	0.252	0.252	0.043	0.043	0.5	0.000	0.000
6	102	0.364	0.364	0.07	0.07	0.1	0.000	0.000
7	47	0.465	0.465	0.065	0.065	0.5	0.000	0.000
8	22	0.624	0.496	0.214	0.093	0.5	0.000	0.158
9	86	0.509	0.509	0.103	0.103	0.1	0.000	0.000
10	12	0.635	0.513	0.216	0.099	0.5	0.000	0.100
N	First	Hidden	Batch	Epochs	Dropout	Opt	Losses	Activation
N 1	First 32	Hidden	Batch 32	Epochs 250	Dropout 0	Opt Adam	Losses	Activation relu
1	32	1	32	250	0	Adam	MSE	relu
$\frac{}{}$	32 8	1 2	32 128	250 250	0 0	Adam Adam	MSE MSE	relu relu
$\begin{array}{c} -1 \\ 2 \\ 3 \end{array}$	32 8 8	1 2 1	32 128 32	250 250 250	0 0 0	Adam Adam Adam	MSE MSE MSE	relu relu relu
1 2 3 4	32 8 8 16	1 2 1 2	32 128 32 128	250 250 250 250 250	0 0 0 0	Adam Adam Adam Adam	MSE MSE MSE MSE	relu relu relu relu
1 2 3 4 5	32 8 8 16 32	1 2 1 2	32 128 32 128 64	250 250 250 250 250 250	0 0 0 0 0	Adam Adam Adam Adam Adam	MSE MSE MSE MSE	relu relu relu relu relu
1 2 3 4 5 6	32 8 8 16 32 32	1 2 1 2 1 1	32 128 32 128 64 64	250 250 250 250 250 250 250	0 0 0 0 0	Adam Adam Adam Adam Adam Adam	MSE MSE MSE MSE MSE	relu relu relu relu relu relu
1 2 3 4 5 6 7	32 8 8 16 32 32 8	1 2 1 2 1 1	32 128 32 128 64 64 128	250 250 250 250 250 250 250 250	0 0 0 0 0 0	Adam Adam Adam Adam Adam Adam	MSE MSE MSE MSE MSE MSE	relu relu relu relu relu relu
1 2 3 4 5 6 7 8	32 8 8 16 32 32 8 32	1 2 1 2 1 1 1 2	32 128 32 128 64 64 128 64	250 250 250 250 250 250 250 250 250	0 0 0 0 0 0 0	Adam Adam Adam Adam Adam Adam Adam	MSE MSE MSE MSE MSE MSE MSE	relu relu relu relu relu relu relu relu

Where columns denote respectively: *Upper*: position in ranking, number of iterations to converge, loss for validation set, MSE for validation set, loss for test set, MSE for test set, learning rate, L1 penalty, L2 penalty; *Lower*: position in ranking, first layer size, number of hidden layers, batch size, maximum number of epochs, dropout, optimizer, losses, activation function;

Based on the aforementioned outcomes, the parameters space was restricted to:

params_final= {lr: $\{0.01\}$, l1: $\{0\}$, l2: $\{0\}$, first_neuron: $\{32\}$, hidden_layers: $\{1, 2\}$, batch_size: $\{32, 128\}$, epochs: $\{100000\}$, dropout: $\{0\}$, optimizer: $\{Adam\}$, losses: $\{mse\}$, activation: $\{relu\}$ }

Working paper dodać, partrząc na wyniki, ale dla estymacji (2h trwa jedna)

Concluding remarks

Here goes the conclusion.

REMEMBER TO CHANGE CODES

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Appendix A

```
1 # Data Scrapper for comtrade.un.org
2 # Authors Michal Miktus & Mateusz Szmidt
  # February 2019
  # Environment setup
  closeAllConnections()
  library (rjson)
  library (data.table)
11
  # Defining all functions necessary to scrap the data
13
  # Support function closing all conections (urls) opened during a scrapping
      process to avoid errors
  # It uses a vector of connections defined at the beginning of each process
  # and closes the opened ones when process ends
18
  connections dropper <- function(vector){</pre>
    new_connections <- getAllConnections()</pre>
20
    if (length (vector) < length (new_connections)) {</pre>
22
       connections_to_kill <- setdiff(new_connections, vector)</pre>
       for(i in 1:length(connections_to_kill)){
         con <- getConnection(i)</pre>
24
         close (con)
26
27
28
29
  # Support function Splitting numeric or string vector into vector of n-
30
      elements batches with "," separator
  # It allows to lower the number of queries
31
  vector_processing <- function(vector, n){</pre>
33
34
    # We consider a case when the set size of a batch is greater than the
35
        length of vector
36
    if (length (vector)> n) {
37
38
```

```
list <- split(vector,cut(seq_along(vector),ceiling(length(vector)/n) ,</pre>
39
            labels = F)
40
       j = 1
       vector <- c()
41
42
       for(i in list){
43
          subsample \leftarrow NULL
44
          for(ii in i){
45
            if(is.null(subsample)){
46
              subsample <- paste(subsample, ii, sep="")</pre>
47
48
            else subsample <- paste (subsample, ii, sep=",")
49
50
51
         # Self check if the split was performed correctly
52
          if(length(i) > n){
53
            print("Something went wrong!")
54
          vector[j] <- subsample
56
57
         j = j + 1
       }
58
     }
59
     else {
60
61
       vector\_ <- vector
62
       vector <- c()
       subsample <- NULL
63
       for(i in 1:length(vector_)){
64
          if(is.null(subsample)){
65
            subsample <- paste(subsample, vector_[i], sep="")</pre>
66
          else subsample <- paste(subsample, vector_[i], sep=",")
68
69
70
       vector [1] <- subsample
71
72
     return (vector)
73
74
75
76
  # Basic data scrapper for a single query
78 # Default values of parameters adjusted to download annuall data on trade
  # Source: https://comtrade.un.org/data/Doc/api/ex/r
79
80
  get.Comtrade <- function(url="http://comtrade.un.org/api/get?"</pre>
81
                                 , maxrec = 50000
82
                                 , type="C"
83
                                 , \operatorname{freq} = "A"
84
                                 ,px="HS"
85
                                 ,\mathbf{ps}="\operatorname{now}"
86
87
                                 , r
                                 , \mathbf{p}
88
                                 , rg="all"
89
```

```
, cc = "TOTAL"
 90
                                                                                ,fmt="json"
  91
  92
 93
        {
              string <- paste (url
  94
                                                         , " \max=" , \max ec , "&" \#\max maximum no. of records returned
  95
                                                            "type=",type, \mbox{\tt `\&"} #type of trade (c=commodities)
  96
                                                         , "freq=", freq, "&" \#frequency
  97
                                                         , "px=" ,px , "&" #classification , "ps=" ,ps , "&" #time period
  98
 99
                                                            "r=",\mathbf{r},"&" #reporting area
100
                                                            "p=",p,"&" #partner country
101
                                                         ,"rg=",rg,"&" #trade flow
,"cc=",cc,"&" #classification code
,"fmt=",fmt #Format
102
104
                                                         , sep = (sep =
106
              if(fmt == "csv") 
                   raw.data<- read.csv(string, header=TRUE)
109
                    return(list(validation=NULL, data=raw.data))
              } else {
                    if(fmt == "json") {
112
                         raw.data<- fromJSON(file=string)</pre>
113
114
                         data<- raw.data$dataset
                         validation <- unlist (raw.data$validation, recursive=TRUE)
115
                         ndata<- NULL
116
                          if(length(data) > 0) {
117
                               var.names<- names(data[[1]])
                               data<- as.data.frame(t( sapply(data,rbind)))
                               ndata<- NULL
                               for(i in 1:ncol(data)){
12
122
                                    data[sapply(data[,i],is.null),i]<- NA
123
                                    ndata <- cbind (ndata, unlist (data [, i]))
124
12
                               ndata <- as.data.frame(ndata)
                               colnames (ndata) <- var.names
126
                         return(list(validation=validation, data =ndata))
128
130
        }
133
        # Definining an object for an output of basic_scrapper function
134
        output <- setRefClass("scrapper_output", fields = list(data = "ANY", checked
                    = "ANY", hits = "ANY"))
136
137
       # Function scrapping the data on all possible connections
138
| # between countries defined in the input <vector> and all the partners
                   available
140 # for the years defined as <year>.
```

```
142 # To control for the number of queries we use the parameter <hits>.
4 H It allows to stop the process after 100 hits to not exceed an hourly
       limit of 100 queries
144
   basic_scrapper <- function(vector, year, hits){</pre>
145
146
     # Console output and definition of an output object
147
     print(paste("Trying for vector of", length(vector), "length."))
148
     current_connections <-getAllConnections()</pre>
149
     data <- NULL
     checked <- NULL
151
     # Looping over all batches of countries in a tryCatch block to avoid a
         failure of a process
     for (i in 1: length(vector)) \{
       tryCatch({
          print(i)
156
          out <- NULL
          unit <- get.Comtrade(r=vector[i], p="all", ps=toString(year), freq="A
158
          if (is.null(unit$data)){
160
            checked <- rbind (checked, vector [i])
161
            print(paste("No data available for year", year, "for" ,vector[i]))
162
163
164
          else {
            checked <- rbind(checked, vector[i])</pre>
165
            out <- unit$data
166
167
       },
       error = function(e){
          print(paste("Error for", i))
170
171
172
       # Stopping the process for 1 hour after 100 hits
174
       hits = hits + 1
175
176
       if(hits >= 100){
          Sys. sleep (3600)
178
          hits = 0
179
180
181
       # Output generation
182
       data <- rbind(data, out)
183
184
185
       # Dropping all connections opened during a process
       connections_dropper(current_connections)
186
187
188
     out <- output (data = data, checked = checked, hits = hits)
189
     return (out)
190
```

```
191 }
192
193
   # Main scrapping process using basic_scrapper function
194
   # It splits the year range into batches of length 5 to optimize the number
       of queries.
  # It also splits the list of countries into batches with initial length of
196
      5,
   # the batches where the error occured are joined and split again into
197
       batches of smaller size (up to 1).
198
   main_scrapper <- function(main_vector, from, to){</pre>
199
200
     # Definition of an output object and years range splitting into batches
20
         of 5
     main\_data <- NULL
202
     years <- vector_processing(seq(from, to), 5)
203
     hits = 0
204
205
     # Looping over the years
206
     for(i in 1:length(years)){
207
       vector <- main_vector
208
       cond <- TRUE
209
       data <- NULL
210
       try <- NULL
211
       split < -5
212
213
       # Scrapping the data for all connections between the countries for a
214
           given batch of years
       # It is continued until for none of a countries an error is reported
215
       while (cond) {
216
         print(paste("Scrapping for years:", years[i]))
21'
         print(paste("The number of countries checked in one hit is", split))
218
219
         unit <- basic_scrapper(vector, years[i], hits)
         data <- rbind(data, unit$data)
22
         hits <- unit $ hits
225
         try <- unique(rbind(unlist(try), unique(unlist(unit$checked))))</pre>
223
224
         # Vector of countires for which error is reported and so the queries
             will be repeated
         vector <- setdiff(unlist(strsplit(main_vector, "\\,")), unlist(</pre>
226
             strsplit(try, "\\,")))
227
            Checking if data for all countries is scrapped,
         # then if not splitting the vector of countries into batches of
229
             smaller size.
         if (length(vector) < 1){
230
           cond = FALSE
231
         else {
            split \leftarrow max(split - 1, 1)
234
            vector <- vector_processing(vector, split)</pre>
235
```

```
}
236
237
238
       # Overriding the state of the scrapping after each finished batch of
239
       main_data <- rbind(main_data, data)
240
       write.csv(file = "trade_data.csv", main_data)
241
242
     return (main_data)
243
244
245
   # Scrapping the data
246
247
248
   # Scrapping the list of the countries listed in the comtrade database
249
250
   download_reporters <- TRUE</pre>
251
   if (download_reporters){
252
     string <- "http://comtrade.un.org/data/cache/partnerAreas.json"</pre>
253
     reporters <- fromJSON(file=string)</pre>
254
     reporters <- as.data.frame(t(sapply(reporters$results,rbind)))
255
  }
256
257
258 # Adjusting the list of reporters for which the process works (removing "
       world " and "all")
   vector <-vector_processing(unlist(as.numeric(reporters$V1[3:length(
259
       reporters $V1)])), 5)
260
  \# Data scrapping for the range of dates available in comtrade database
261
  data <- main_scrapper(vector, 1962, 2018)
262
fwrite (file = "trade_data.csv", data)
```

Scrapper.R

Appendix B

```
Neural net created for the gravity model prediction for the Trade Policy
      class at PSE
  # Author: Michal Miktus at michal.miktus@gmail.com
  # Date: 21.02.2019
  # Import libraries
  import plotly.io as pio
  import \ plotly.graph\_objs \ as \ go
  import plotly plotly as py
  from plotly.offline import init_notebook_mode, iplot
  from matplotlib import pyplot as plt
  from scipy.stats import mstats
13 from statsmodels.distributions.empirical_distribution import ECDF
14 from sklearn.preprocessing import MinMaxScaler, StandardScaler
16 import os
17 import numpy as np
18 import pandas as pd
19 #import torch
20 import seaborn as sns
21 import keras
22 import tensorflow as tf
23 import talos as ta
24 from keras.optimizers import Adam, Nadam, SGD
25 from keras.activations import relu, elu, sigmoid, tanh
26 from keras.losses import mse
27 from talos.model.normalizers import lr_normalizer
28 from talos.model.layers import hidden_layers
  from talos.model.early_stopper import early_stopper
  %matplotlib inline
30
  # from plotly import tools
32
33
  # Set seed
35
_{37} random_state = 123
np.random.seed(random_state)
39 tf.set random seed (random state)
40 #torch.manual_seed(random_state)
```

```
# Supress scientific notation for pandas
43
  pd.options.display.float_format = '{:.5 f}'.format
44
45
  # Templates for graphs
46
47
  pio.templates.default = 'plotly_dark+presentation'
48
  sns.set(style="ticks", context="talk")
49
  plt.style.use("dark_background")
50
  init_notebook_mode(connected=True)
51
52
53
  # Path specifiation
54
  #path = "/Users/miktus/Documents/PSE/Trade policy/Model/"
56
  path = "C:/Repo/Trade/Trade-policy/"
57
  # Import data
59
60
  data = pd.read_csv(path + "/Data/final_data_trade.csv")
61
62
  # Data exploration only for Poland
63
  data = data.loc[data['rt3ISO'] == "POL"]
65
66
  data.columns
67
68
  # Number of trade partners
70
  data ["pt3ISO"]. unique(). shape
71
72
  data.info()
73
74
  # Dropping the duplicates from the dataset
75
  data = data.drop_duplicates(keep='first')
78
  # Handling missing data
79
80
  data.isnull().sum()
81
82
  data.dropna(thresh=data.shape[0] * 0.7, how='all', axis=1, inplace=True)
83
84
  data.dropna(axis=0, inplace=True)
  # data.fillna(data.mean(), inplace=True) # Or replace by the column mean
86
87
  # Desribe data
88
80
  description = data.describe(include='all')
90
  coef_variation = description.loc["std"] / description.loc["mean"]
91
  description.loc["cova"] = coef_variation
92
93 (description.sort_values(by="cova", axis=1)).T
```

```
94
95
   # Number of unique entries
96
97
   print (data.nunique())
98
99
   # Names of binary data (unstandarized)
100
   binary = []
   for columns in data:
103
       if (data.loc[:, columns].min() == 0) & (data.loc[:, columns].max() ==
104
           binary.append(columns)
106
   for columns in data.loc[:, binary]:
107
       print(data.loc[:, binary][columns].unique())
109
   # Remove iso_2o, iso_2d and family
110
111
   data.drop(columns=['iso2_d', 'iso2_o'], inplace=True)
112
   # Numeric variables
114
115
   data_numeric = data._get_numeric_data()
   data_numeric.drop(columns="yr", inplace=True)
117
   data_numeric.drop(columns=binary, inplace=True)
118
119
   # Visualisations
120
   # Numerical data distribution
   data_numeric.hist(figsize=(10, 10), bins=50, xlabelsize=8, ylabelsize=8)
124
   for i, col in enumerate (data_numeric.columns):
125
126
       plt.figure(i)
       sns.distplot(data_numeric[col], color="y")
12
128
   sns.distplot(data_numeric["tdiff"], color="y")
129
130
   sns.pairplot(data_numeric);
131
   sns.pairplot(data_numeric, vars=["pop_o", "tdiff"]) # kind="reg"/kind="kde"
133
134
135
   # Flows
136
   flows = data[['yr', 'rt3ISO', 'pt3ISO', 'Trade_value_total']]
   data_loc = pd.read_csv(path + "/Data/CountryLatLong.csv")
   data_loc.drop(columns=['Country'], inplace=True)
   data_loc.columns = ["CODE", "rt_Lat", "rt_Long"]
140
141
   flows = pd.merge(flows, data_loc, left_on="rt3ISO", right_on="CODE").drop('
142
      CODE', axis=1)
data_loc.columns = ["CODE", "pt_Lat", "pt_Long"]
```

```
flows = pd.merge(flows, data_loc, left_on="pt3ISO", right_on="CODE").drop('
       CODE', axis=1)
145
   flow_directions = []
146
   for i in range (len (flows)):
147
        flow_directions.append(
148
            dict (
149
                 type = 'scattergeo',
150
                locationmode = 'ISO-3',
                lon = [ flows['rt_Long'][i], flows['pt_Long'][i]],
lat = [ flows['rt_Lat'][i], flows['pt_Lat'][i]],
                 text = flows['pt3ISO'][i],
154
                mode = 'lines
155
                 line = dict(
156
                     width = flows['Trade_value_total'][i]*10,
                     color = 'red',
158
159
                 opacity = 200 * np.power(float(flows['yr'][i]) - float(flows['
                    yr'].min()),2)/float(np.power(float(flows['yr'].max()),2)),
            )
161
162
163
   layout = dict(
164
            title = 'Trade flows between Poland and its trading partners.',
168
            showlegend = False,
166
            geo = dict(
167
                scope='world',
168
                 projection=dict( type='robinson' ),
169
                showland = True,
                landcolor = 'rgb(243, 243, 243)'
17
                 countrycolor = 'rgb(204, 204, 204)',
            )
174
178
   fig = dict( data=flow_directions, layout=layout )
176
   iplot (fig, filename='Flows map')
177
178
   print(data['Trade_value_total'].describe())
179
180
   flows_winsorized = mstats.winsorize(data['Trade_value_total'], limits
181
       =[0.05, 0.05]
   layout = go. Layout (
182
        title="Basic histogram of flows (winsorized)")
183
184
   data_hist = [go.Histogram(x=flows_winsorized)]
185
   fig = go.Figure(data=data_hist, layout=layout)
186
187
   iplot (fig, filename='Basic histogram of flows')
188
   sns.distplot(data['Trade_value_total'], axlabel= "Basic histogram of flows"
189
       , color="y")
190
191
192 # Corr - to correct
```

```
193
   corr = ecdf_normalized_df.corr()
194
195
   sns.heatmap(corr[(corr >= 0.5) | (corr <= -0.5)],
196
                 cmap='viridis', vmax=1.0, vmin=-1.0, linewidths=0.1,
197
                 annot=True, annot_kws={"size": 8}, square=True)
198
190
   # Coef of variation
200
20
   layout = go.Layout(
202
        title="Coefficient of variation")
203
   data_cova = [go. Histogram(x=description.loc["cova"])]
205
   fig = go.Figure(data=data_cova, layout=layout)
   iplot (fig,
207
          filename="Coefficient of variation")
208
209
   \label{eq:cova} \mbox{high\_cova} = \mbox{description.loc} \left[ \mbox{"cova"} \right] . \mbox{where} (\mbox{lambda} \ x \colon \ x \ > \ 0.30) . \mbox{dropna}() . \mbox{sort}
210
        _values(ascending=False)
   high cova
211
212
213
214
   # Normalization
215
216
   minmax_normalized_df = pd.DataFrame(MinMaxScaler().fit_transform(data_
217
       numeric),
                                             columns=data_numeric.columns, index=
218
                                                  data_numeric.index)
219
   standardized_df = pd.DataFrame(StandardScaler().fit_transform(data_numeric)
220
        , columns=data_numeric.columns,
22
                                       index=data_numeric.index)
222
   ecdf_normalized_df = data_numeric.apply(
223
        lambda c: pd. Series (ECDF(c)(c), index=c.index)
224
22
   # Replace data by its standardized values
226
22'
   data[list(ecdf_normalized_df.columns.values)] = ecdf_normalized_df
228
229
230
   # Select only POL as rt3ISO
231
232
   data_PL = data.query("rt3ISO == 'POL',")
233
234
   data_PL.drop('rt3ISO', axis=1, inplace=True)
235
236
   data_PL.info()
   # One hot encoding
239
240 data_PL = pd.get_dummies(
```

```
data_PL, columns=["pt3ISO", "legold_o", "legold_d", "legnew_o", "legnew
241
                           _d", "flaggsp_o_d", "flaggsp_d_d"],
                  prefix = ["pt3ISO", "legold_o", "legold_d", "legnew_o", "legnew_d", "
    flaggsp_o_d", "flaggsp_d_d"])
242
243
       # Splitting the data
244
245
       \# train\_size = 0.9
246
       # train_cnt = math.floor(data_PL.shape[0] * train_size)
247
248
       splitting_yr = 2010
249
       x_train = data_PL.drop('Trade_value_total', axis=1).loc[data_PL['yr'] <=
251
                 splitting_yr]. values
                                                                       'Trade_value_total'].loc[data_PL['yr'] <=
       y_train = data_PL.loc[:,
                 splitting_yr]. values
       x_test = data_PL.drop('Trade_value_total', axis=1).loc[data_PL['yr'] >
253
                 splitting_yr]. values
       \label{eq:y_test} y\_test \ = \ data\_PL. \ loc \ [: , \ 'Trade\_value\_total']. \ loc \ [data\_PL \ 'yr'] \ > \ splitting\_test \ = \ data\_PL \ 'yr'] \ > \ splitting\_test \ = \ data\_PL \ 'yr'] \ > \ splitting\_test \ = \ data\_PL \ 'yr'] \ > \ splitting\_test \ = \ data\_PL \ 'yr'] \ > \ splitting\_test \ = \ data\_PL \ 'yr' \ 'yr''] \ > \ splitting\_test \ = \ data\_PL \ 'yr'' \ > \ splitting\_test \ = \ data\_PL \ 'yr'' \ > \ splitting\_test \ = \ data\_PL \ 'yr'' \ > \ splitting\_test \ = \ data\_PL \ 'yr'' \ > \ splitting\_test \ = \ data\_PL \ 'yr'' \ > \ splitting\_test \ = \ data\_PL \ 'yr'' \ > \ splitting\_test \ = \ data\_PL \ 'yr'' \ > \ splitting\_test \ = \ data\_PL \ 'yr'' \ > \ splitting\_test \ = \ data\_PL \ 'yr'' \ > \ splitting\_test \ = \ data\_PL \ 'yr'' \ > \ splitting\_test \ = \ data\_PL \ 'yr'' \ > \ splitting\_test \ = \ data\_PL \ 'yr'' \ > \ splitting\_test \ = \ data\_PL \ 'yr'' \ > \ splitting\_test \ = \ data\_PL \ 'yr'' \ > \ splitting\_test \ = \ data\_PL \ 'yr'' \ > \ splitting\_test \ = \ data\_PL \ 'yr'' \ > \ splitting\_test \ = \ data\_PL \ 'yr'' \ > \ splitting\_test \ = \ data\_PL \ 'yr'' \ > \ splitting\_test \ = \ data\_PL \ 'yr'' \ > \ splitting\_test \ = \ data\_PL \ 'yr'' \ > \ splitting\_test \ = \ data\_PL \ 'yr'' \ > \ splitting\_test \ = \ data\_PL \ 'yr'' \ > \ splitting\_test \ = \ data\_PL \ 'yr'' \ > \ splitting\_test \ = \ data\_PL \ 'yr'' \ > \ splitting\_test \ = \ data\_PL \ 'yr'' \ > \ splitting\_test \ = \ data\_PL \ 'yr'' \ > \ splitting\_test \ = \ data\_PL \ 'yr'' \ > \ splitting\_test \ = \ data\_PL \ 'yr'' \ > \ splitting\_test \ = \ data\_PL \ 'yr'' \ > \ splitting\_test \ = \ data\_PL \ 'yr'' \ > \ splitting\_test \ = \ data\_PL \ 'yr'' \ > \ splitting\_test \ = \ data\_PL \ 'yr'' \ > \ splitting\_test \ = \ data\_PL \ 'yr'' \ > \ splitting\_test \ = \ data\_PL \ 'yr'' \ > \ splitting\_test \ = \ data\_PL \ 'yr'' \ > \ splitting\_test \ = \ data\_PL \ 'yr'' \ > \ splitting\_test \ = \ data\_PL \ 'yr''' \ > \ splitting\_test \ = \ data\_PL \ 'yr'' \ > \ splitting\_test \ = \ data\_PL \ 'yr''' \ > \ splitting\_test \ > \ data\_PL \ 'yr
254
                yr]. values
255
       # Build NN class in PyTorch
256
257
       # A fully-connected ReLU network with one hidden layer, trained to predict
                y from x
       # by minimizing squared Euclidean distance.
260
261
        class ThreeLayerNet(torch.nn.Module):
262
                  \label{eq:def_def} \begin{array}{ll} \text{def} \ \_\_\text{init}\_\_(\text{self} \ , \ \underline{D}\_\text{in} \ , \ \underline{H}\_\text{in} \ , \ \underline{H}\_\text{out} \ , \ \underline{D}\_\text{out}) \colon \\ \end{array}
263
264
                            In the constructor we instantiate two nn. Linear modules and assign
265
                                    them as
                           member variables.
266
                            super(ThreeLayerNet, self).__init__()
268
                            self.linear1 = torch.nn.Linear(D_in, H_in)
269
                            self.linear2 = torch.nn.Linear(H_in, H_out)
                            self.linear3 = torch.nn.Linear(H_out, D_out)
27
279
                  def forward (self, x):
273
274
                            In the forward function we accept a Tensor of input data and we
275
                                    must return
                            a Tensor of output data. We can use Modules defined in the
                                     constructor as
                            well as arbitrary operators on Tensors.
277
278
                           h_relu_1 = self.linear1(x).clamp(min=0)
279
                           h_relu_2 = self.linear2(h_relu_1).clamp(min=0)
280
                           y_pred = self.linear3(h_relu_2)
281
                            return y_pred
282
283
```

```
\#x = torch.tensor(x_train).float()
   #y = torch.tensor(y_train).float()
287
288 # N is batch size; D_in is input dimension;
   # H is hidden dimension; D_out is output dimension.
289
{}_{290}\big|\,N,\  \, \underline{D}_{\underline{}}in\,\,,\  \, \underline{H}_{\underline{}}in\,\,,\  \, \underline{H}_{\underline{}}out\,\,,\  \, \underline{D}_{\underline{}}out\,\,=\,\,int\,(\,\underline{data}\underline{\ }PL.\,shape\,[\,0\,]\,)\,\,,\,\,\,int\,(\,(\,\underline{data}\underline{\ }PL.\,shape\,[\,1\,]\,))
       -1)), 50, 50, 1
29
   # Construct our model by instantiating the class defined above
292
   #model = ThreeLayerNet(D_in, H_in, H_out, D_out)
293
   # Construct our loss function and an Optimizer. The call to model.
295
        parameters ()
   # in the SGD constructor will contain the learnable parameters of the three
296
   # nn.Linear modules which are members of the model.
297
   #criterion = torch.nn.MSELoss(reduction='sum')
298
   #optimizer = torch.optim.SGD(model.parameters(), lr=1e-4)
299
   \#for t in range (5):
300
         # Forward pass: Compute predicted y by passing x to the model
   #
301
         y_pred = model(x)
302
   #
303
   #
   #
         # Compute and print loss
304
   #
         loss = criterion(y\_pred, y)
306
   #
         print(t, loss.item())
307
   #
         # Zero gradients, perform a backward pass, and update the weights.
   #
308
   #
         optimizer.zero_grad()
309
         loss.backward()
   #
310
         optimizer.step()
   #
311
312
   # Build NN class in Keras
313
314
315
316
   def build_model(x_train, y_train, x_val, y_val, params):
31'
        model = keras. Sequential()
318
        model.add(keras.layers.Dense(10, activation=params['activation'],
310
                                            input_dim=x_train.shape[1],
320
                                            use_bias=True,
32
                                            kernel_initializer='glorot_uniform',
322
                                            bias_initializer='zeros',
323
                                            kernel_regularizer=keras.regularizers.ll
324
                                                12 (11=params [ '11 '], 12=params [ '12 ']),
                                            bias_regularizer=None))
326
        model.add(keras.layers.Dropout(params['dropout']))
327
328
        # If we want to also test for number of layers and shapes, that's
329
             possible
        hidden_layers (model, params, 1)
330
331
        # Then we finish again with completely standard Keras way
332
```

```
model.add(keras.layers.Dense(1, activation=params['activation'], use_
333
            bias=True,
                                         kernel_initializer='glorot_uniform',
                                         bias_initializer='zeros',
335
                                         kernel_regularizer=keras.regularizers.l1_
336
                                             12(11=params['11'], 12=params['12']),
                                         bias_regularizer=None))
33
338
        model.compile(optimizer=params['optimizer'](lr=lr_normalizer(params['lr
339
            '], params['optimizer'])),
loss=params['losses'],
340
                        metrics=['mse'])
341
342
        history = model. fit (x_train, y_train,
343
                               validation_data=[x_val, y_val],
344
                               batch_size=params['batch_size'],
348
                               epochs=params['epochs'],
346
                               callbacks = [early_stopper(epochs=params['epochs'],
34
                                   mode='strict')],
                               verbose=0)
348
349
        # Finally we have to make sure that history object and model are
350
            returned
        return history, model
   # Then we can go ahead and set the parameters space
354
355
   params = \{ 'lr' : (0.5, 4, 4), 
356
               11 : (0.1, 40, 4),
35
               ^{,}12~^{,}:~\left(\,0\,.\,1\;,~40\;,~4\right)\;,
358
               "first\_neuron": \ [4\,,\ 8\,,\ 16]\,,
359
               \verb|'hidden_layers': [0, 1, 2], \\
360
               'batch_size': [32, 64],
361
               'epochs': [250],
362
               'dropout': (0, 0.5, 5)
363
               'optimizer': [Adam, SGD],
364
               'losses': [mse],
365
               'activation': [relu, sigmoid]}
366
367
   # Alternatively small parameters space
368
369
370
   params_small = \{ 'lr' : (0.5, 5, 2), \}
371
                      '11': (0.1, 50, 2),
372
                      '12': (0.1, 50, 2),
373
                      'first_neuron': [4],
374
                      'hidden_layers': [0],
375
                      'batch_size': [32], # [32, 64, 128, 256],
376
                      'epochs': [100],
37
                      'dropout': (0, 0.5, 2),
378
                      'optimizer': [Adam],
379
                      'losses': [mse],
380
```

```
\verb|`activation': [relu]| \\
381
382
   # Run the experiment
383
384
   os.chdir(path + "/Data/")
385
386
   t = ta.Scan(x=x\_train,
387
                  y=y_train ,
388
                  model=build\_model,
389
                  {\tt grid\_downsample}{=}1,
390
                  val\_split = 0.3,
391
                  params=params,
392
                  dataset_name='POL',
393
                  experiment_no='2')
```

Neural_net.py

Appendix C

```
# Code for the Trade Policy class at PSE
3 # Author: Michal Miktus at michal.miktus@gmail.com
  # Date: 23.02.2019
  #path <- '/Users/miktus/Documents/PSE/Trade policy/Model/'</pre>
  path <- 'C:/Repo/Trade/Trade-policy/</pre>
  setwd (path)
  set . seed (12345)
11
  # Load packages
  list.of.packages <- c("readstata13", "data.table")</pre>
17
18
  new.packages <- list.of.packages[!(list.of.packages %in% installed.packages
19
      () [, "Package"])]
  if(length(new.packages)) install.packages(new.packages, repos = "http://
      cran.us.r-project.org")
  invisible(lapply(list.of.packages, library, character.only = TRUE))
23
  # Useful functions
24
2.5
  RMSE = function (m, o) {
26
    sqrt(mean((m - o)^2, na.rm=TRUE))
27
28
29
  # Perform computations or load the data -
30
  data_cepii <- as.data.table(read.dta13(paste0(path, "Data/gravdata.dta")))
  data_trade <- fread(paste0(path, "Data/trade_data.csv"))</pre>
  # Delete cases for which the trading partner is unknown
35
36
  data_trade <- data_trade [complete.cases(data_trade[,pt3ISO])]
37
38
```

```
39 # Convert TradeValues to numeric, with emphasis on scientific notation
                      issues
40
        41
                     TradeValue)), scientific = FALSE))
       data_trade <- data_trade[, c('yr', 'TradeValue', 'rt3ISO', 'pt3ISO')]
data_trade <- unique(data_trade[, 'Trade_value_total' := sum(TradeValue),</pre>
42
43
                     by = c("yr", "rt3ISO", "pt3ISO")], by = c("yr", "rt3ISO", "pt3ISO",
                     Trade_value_total"))
        \begin{array}{ll} \mathbf{data\_trade} \, [ \; , \; \; \mathbf{TradeValue} \; := \; \mathbf{NULL} ] \end{array}
44
        data_trade <- data_trade [!data_trade[, pt3ISO == 'WLD']]
45
46
        # Merge data
47
48
        # Inner
49
50
        data_inner <- merge(data_trade, data_cepii, by.y = c('year', 'iso3_o', '
51
                     iso3_d'), by x = c('yr', 'rt3ISO', 'pt3ISO'))
        # table(data[, "yr"])
53
54
        data_cepii [ "year " > 1993]
55
56
       #Left
57
58
        data\_left \; < - \; merge(\, data\_trade \,, \; data\_cepii \, [\, "\, year \, " \, > \, 1993] \,, \; by \,. \, y \, = \, c \, (\, '\, year \, ' \, , \, data\_cepii \, [\, "\, year \, " \, > \, 1993] \,, \; by \,. \, y \, = \, c \, (\, '\, year \, ' \, , \, data\_cepii \, [\, "\, year \, " \, > \, 1993] \,, \; by \,. \, y \, = \, c \, (\, '\, year \, ' \, , \, data\_cepii \, [\, "\, year \, " \, > \, 1993] \,, \; by \,. \, y \, = \, c \, (\, '\, year \, ' \, , \, data\_cepii \, [\, "\, year \, " \, > \, 1993] \,, \; by \,. \, y \, = \, c \, (\, '\, year \, " \, , \, data\_cepii \, [\, "\, year \, " \, > \, 1993] \,, \; by \,. \, y \, = \, c \, (\, '\, year \, " \, , \, data\_cepii \, [\, "\, year \, " \, > \, 1993] \,, \; by \,. \, y \, = \, c \, (\, '\, year \, " \, , \, data\_cepii \, [\, "\, year \, " \, > \, 1993] \,, \; by \,. \, y \, = \, c \, (\, '\, year \, " \, , \, data\_cepii \, [\, "\, year \, " \, > \, 1993] \,, \; by \,. \, y \, = \, c \, (\, '\, year \, " \, , \, data\_cepii \, [\, "\, year \, " \, > \, 1993] \,, \; by \,. \, y \, = \, c \, (\, '\, year \, " \, , \, data\_cepii \, [\, "\, year \, " \, > \, 1993] \,, \; by \,. \, y \, = \, c \, (\, '\, year \, " \, , \, data\_cepii \, [\, "\, year \, " \, , \, data\_cepii \, [\, "\, year \, " \, , \, data\_cepii \, [\, "\, year \, " \, , \, data\_cepii \, [\, "\, year \, " \, , \, data\_cepii \, [\, "\, year \, " \, , \, data\_cepii \, [\, "\, year \, " \, , \, data\_cepii \, [\, "\, year \, " \, , \, data\_cepii \, [\, "\, year \, " \, , \, data\_cepii \, [\, "\, year \, " \, , \, data\_cepii \, [\, "\, year \, " \, , \, data\_cepii \, [\, "\, year \, " \, , \, data\_cepii \, [\, "\, year \, " \, , \, data\_cepii \, [\, "\, year \, " \, , \, data\_cepii \, [\, "\, year \, " \, , \, data\_cepii \, [\, "\, year \, " \, , \, data\_cepii \, [\, "\, year \, " \, , \, data\_cepii \, [\, "\, year \, " \, , \, data\_cepii \, [\, "\, year \, " \, , \, data\_cepii \, [\, "\, year \, " \, , \, data\_cepii \, [\, "\, year \, " \, , \, data\_cepii \, [\, "\, year \, " \, , \, data\_cepii \, [\, "\, year \, " \, , \, data\_cepii \, [\, "\, year \, " \, , \, data\_cepii \, [\, "\, year \, " \, , \, data\_cepii \, [\, "\, year \, " \, , \, data\_cepii \, [\, "\, year \, " \, , \, data\_cepii \, [\, "\, year \, " \, , \, data\_cepii \, [\, "\, year \, " \, , \, data\_cepii \, [\, "\, year \, " \, , \, data\_cepii \, [\, "\, year \, " \, , \, data\_cepii \, [\, "\, year \, " \, , \, da
                       'iso3_o', 'iso3_d'), by.x = c('yr', 'rt3ISO', 'pt3ISO'), all.y = T)
        data_left[, Trade_value_total := lapply(data_left[, "Trade_value_total"],
61
                     function (x) {ifelse (is.na(x), 0, x)})
       # Write whole dataset
63
64
        fwrite(data_left , 'Data/final_data_trade.csv')
```

DataCleaning.R

Appendix D

```
1 # Code for the Trade Policy class at PSE
  2 # Author: Michal Miktus at michal.miktus@gmail.com
       # Date: 23.02.2019
        path <- '/Users/miktus/Documents/PSE/Trade policy/Model/'</pre>
        # path <- 'C:/Repo/Trade/Trade-policy/'</pre>
        setwd (path)
        set . seed (12345)
       # Load packages
13
        list.of.packages <- c("readstata13", "data.table", "gravity", "dplyr", '</pre>
                     stargazer', 'caret')
       new.\,packages <- \ list.\,of.\,packages \, \verb|[!(list.of.packages \, \%in\% \, installed.\,packages \, |[!(list.of.packages \, \%in\% \, installed.\,packages \,
16
                     ()[, "Package"])]
         if(length(new.packages)) install.packages(new.packages, repos = "http://
17
                     cran.us.r-project.org")
18
         invisible (lapply (list.of.packages, library, character.only = TRUE))
19
20
       # Useful functions
22
       RMSE = function(m, o) \{
               sqrt(mean((m - o)^2, na.rm=TRUE))
24
25
26
       # Load the data
27
28
        data <- fread(paste0(path, "Data/data_PL.csv"))</pre>
29
        names(data) <- make.names(names(data), unique=TRUE)
30
       # Year variable
32
        year <- data[, 'yr']</pre>
34
       # Near zero variance variables
36
37
38 near <- nearZeroVar(data)
```

```
39 data <- data [, -near, with = FALSE]
40
     # Remove highly correlated data
41
42
     corr = cor(data)
43
44 hc = findCorrelation(corr, cutoff=0.8) # put any value as a "cutoff"
|hc| = sort(hc)
     data = data[, -hc, with = FALSE]
46
47
     # Add year (just for splitting)
48
49
      data[, yr := year]
50
51
      # Data split to compare the reults
52
     data_bef2010 \leftarrow data[yr <= 2010]
54
     \# data\_bef2010[, yr := NULL]
55
\frac{1}{1} \frac{1}
57 # data_aft2010 [, yr := NULL]
data_aft2010 [, dist_log := log(distw)]
59 var <- setdiff(names(data_bef2010), c("Trade_value_total", "distw", "V1", "
                yr"))
      # PPML: Poisson Pseudo Maximum Likelihood
     PPML <- ppml(dependent_variable= "Trade_value_total", distance="distw"
                additional_regressors = var, es = T, robust=TRUE, data = data_bef2010)
     summary (PPML)
      predictions <- predict (PPML, newdata = data_aft2010)
66 residuals <- predictions - data_aft2010[, "Trade_value_total"]
     MSE <- mean(sum(residuals^2)/length(unlist(residuals)))
     max(unlist(residuals))
68
69
70
     # Summary to latex
71
     stargazer (PPML)
73
     # FE -
74
75
      dependent <- c("Trade_value_total")</pre>
76
      continous <- \ c("\operatorname{distw}", "\operatorname{pop\_o}", "\operatorname{pop\_d}", "\operatorname{gdp\_o}", "\operatorname{gdp\_d}", "\operatorname{area\_d}", "
                tdiff ", "comrelig")
      log_variables <- paste("log(", continous, ")", sep = "")</pre>
      dummies <- setdiff(setdiff(names(data_bef2010), continous), dependent)
     linear_het <- as.formula(paste(paste("log(",dependent, ")", sep = "")),</pre>
                                                                                          paste(paste(log\_variables, collapse = " + ")
82
                                                                                                   , paste(dummies, collapse = " + "), sep
                                                                                                          " + "), sep = " ~ "))
     linear_het <- as.formula(paste(dependent,
84
                                                                                          paste(paste(log_variables, collapse = " + ")
85
                                                                                                    , paste (dummies, collapse = " + "), sep
```

```
= " + "), sep = " ~ "))
87 | FE \leftarrow lm(linear_het, data = data_bef2010)
  \#FE\$ coefficients \leftarrow lapply (coef(FE), function(x) {ifelse(is.na(x), as.
       numeric(0), as.numeric(x))
   summary(FE)
89
  MSE_FE_train <- (mean(FE$residuals^2))
90
   MSE FE train
91
92
   predictions <- predict (FE, newdata = data_aft2010)
93
   residuals = predictions - (data_aft2010[, 'Trade_value_total'])
94
   max(residuals)
95
   MSE_FE_test <- (sum(residuals^2)/length(unlist(residuals)))</pre>
97
   MSE_FE_test
98
   # Summary to latex
100
101
   stargazer (FE)
103
  # FE on test
104
105
106 # FE <- lm(linear_het, data = data_aft2010)
# MSE_FE_aft <- mean(sum(FE$residuals^2)/length(FE$residuals))
108 # MSE_FE_aft
```

Gravity.R