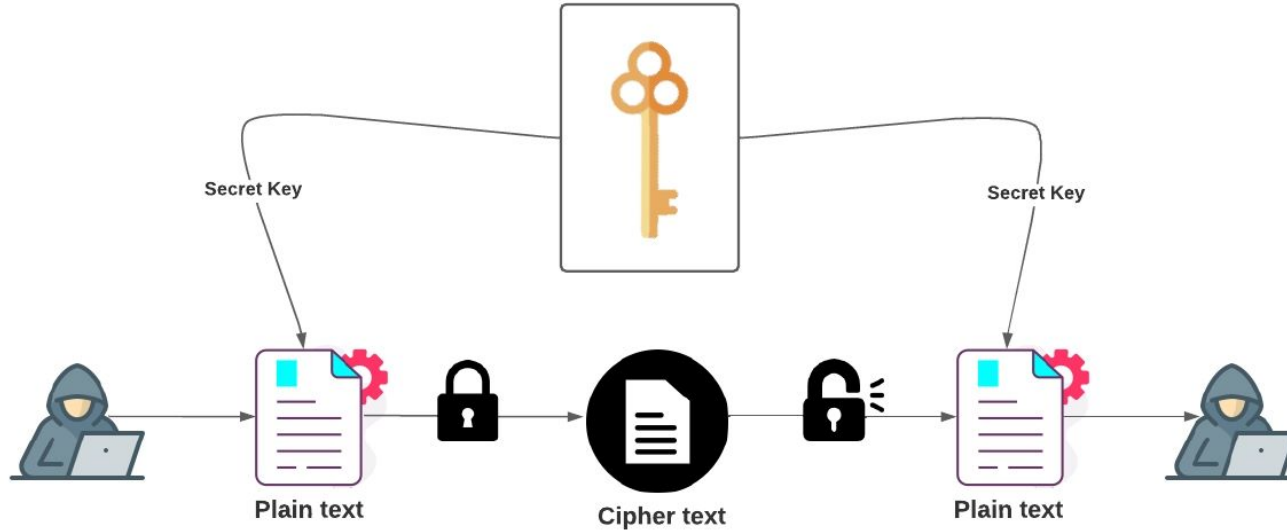


## Unit 3 Cryptography

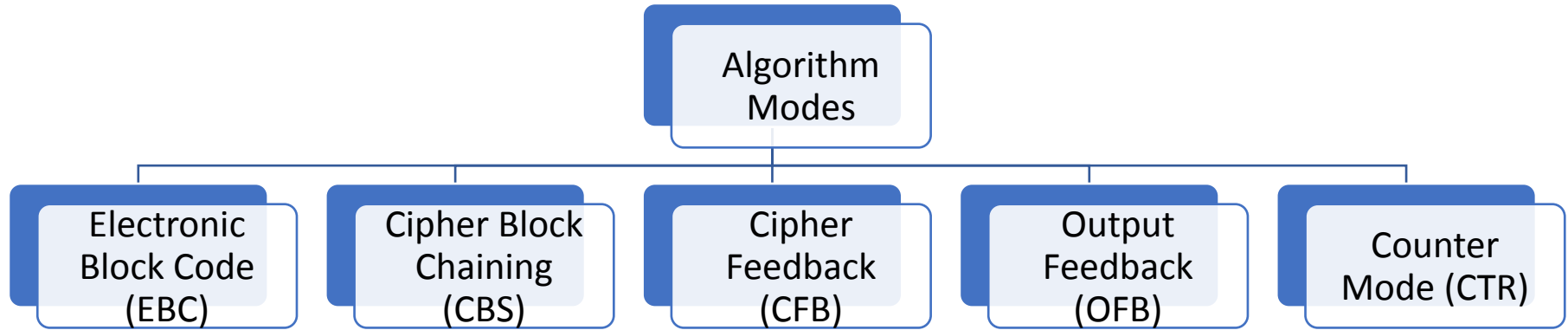


# Cryptography & Network Security

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- **Cipher Modes**
  - **Electronic Code Book Mode**
  - **Cipher Block Chaining Mode**
  - **Cipher Feedback Mode**
  - **Stream Cipher Mode**
  - **Counter Mode**
- **Public Key Algorithm**
  - **RSA**
- **Digital Signatures**
  - **Symmetric-key**
  - **Public key**
  - **Message Digest (SHA, MD5)**

# Cipher Modes



# Electronic Block Code (EBC)

- Message is broken into **independent blocks** which are encrypted
- Each block is a **value** which is substituted, **like a codebook**, hence name
- each block is **encoded independently** of the other blocks
- **Uses:** secure transmission of single values

# Electronic Block Code (EBC)

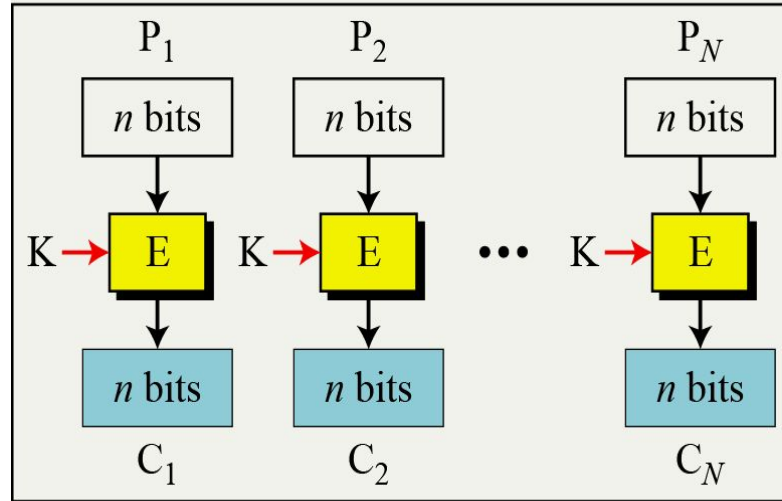
E: Encryption

D: Decryption

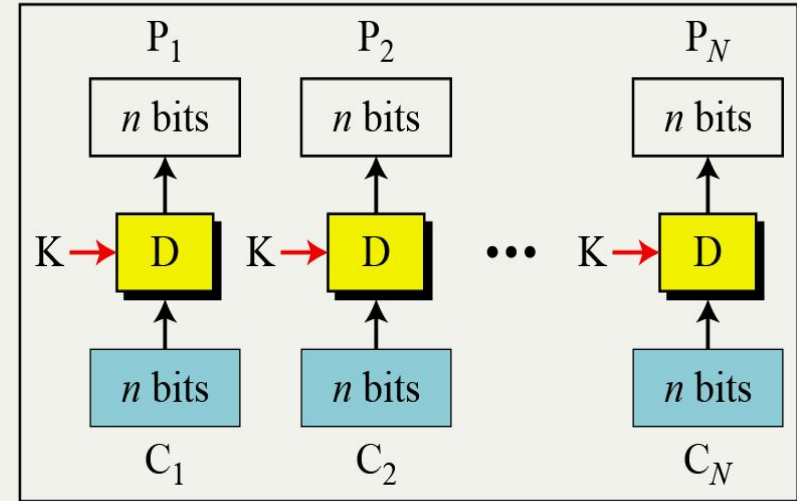
$P_i$ : Plaintext block  $i$

$C_i$ : Ciphertext block  $i$

K: Secret key



Encryption



Decryption

# Electronic Block Code (EBC)

- **Benefits**

- ✓ Parallel encryption of blocks of bits is possible, thus it is a faster way of encryption.
- ✓ Simple way of block cipher.

- **Problems**

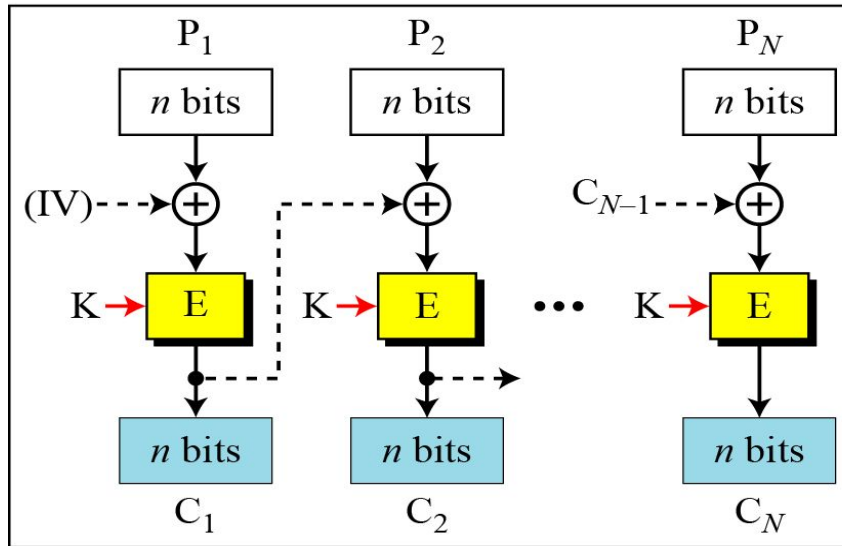
- ✓ message repetitions may show in ciphertext
- ✓ weakness is due to the encrypted message blocks being independent
- ✓ main use is sending a few blocks of data

# Cipher Block Chaining (CBC)

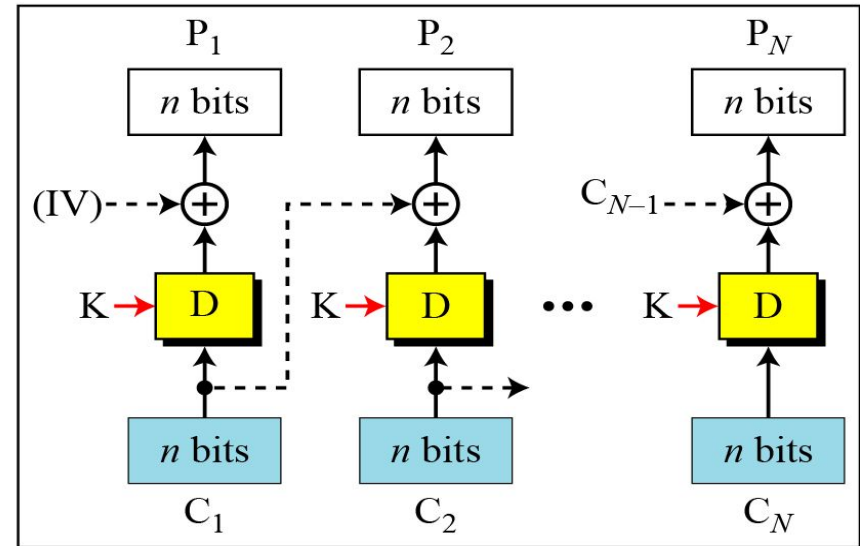
- Message is broken into **blocks**
- Linked together in encryption operation
- Each **previous cipher blocks** is **chained** with **current plaintext block**, hence name
- Use **Initial Vector (IV)** to start process
- **Uses:** bulk data encryption, authentication

# Cipher Block Chaining (CBC)

E: Encryption      D : Decryption  
 $P_i$ : Plaintext block  $i$        $C_i$ : Ciphertext block  $i$   
K: Secret key      IV: Initial vector ( $C_0$ )



Encryption



Decryption



# Cipher Block Chaining (CBC)

- Problems

- ✓ A ciphertext block depends on all blocks before it
- ✓ Any change to a block affects all following ciphertext blocks
- ✓ Need Initialization Vector (IV)
  - ✗ which must be known to sender and receiver
  - ✗ if sent in clear, attacker can change bits of first block, and change IV to compensate

# Cipher Feedback (CFB)

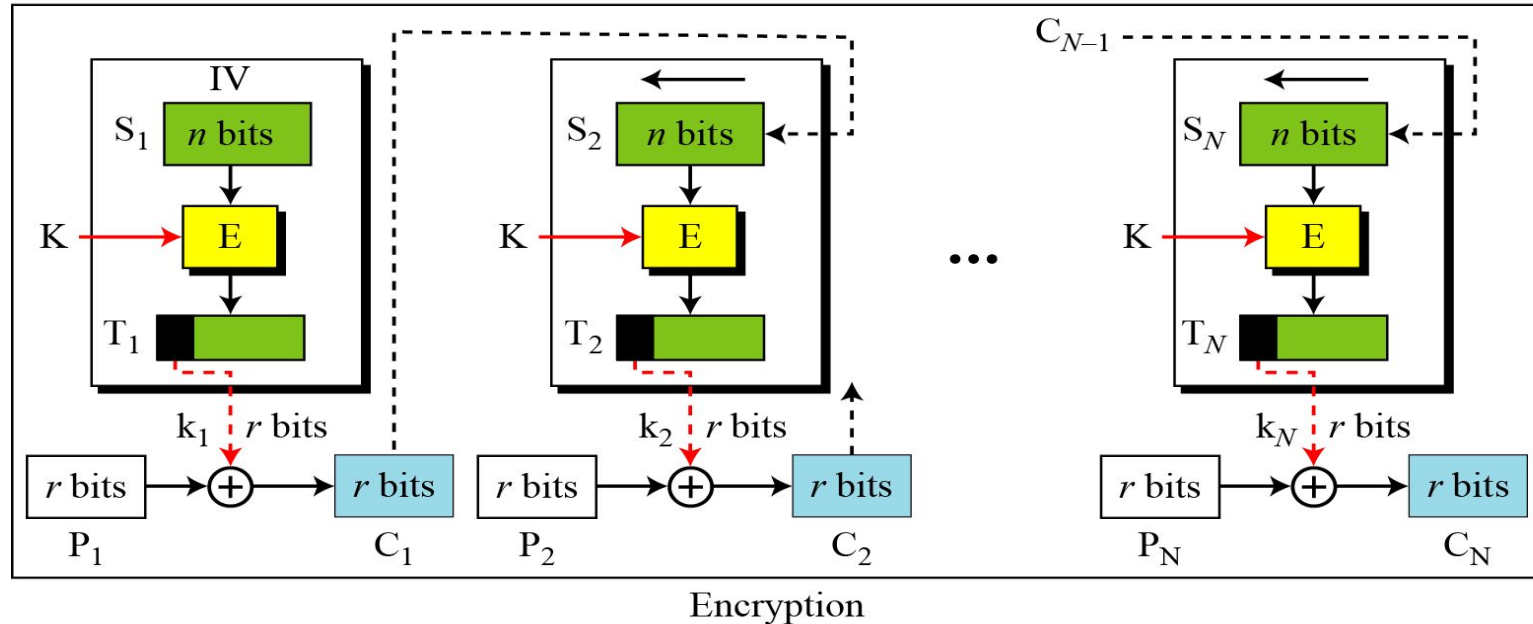
- At times we need to use block cipher that works as streams cipher Eg. Telnet
- Generic Steps
  - ✓ Take 64 bit **Initial Vector (IV)** store it in **shift register**, Encrypt it to get EIV
  - ✓ Perform XOR of Leftmost **r** bits of Plain text (PT) and Leftmost **r** bits of **EIV** call it **C<sub>i</sub>**
  - ✓ Shift left **IV** by **r bits** and insert **C<sub>i</sub>** to its right
  - ✓ Repeat step 1 to 3

# Cipher Feedback (CFB)

E : Encryption  
 $P_i$ : Plaintext block  $i$   
K: Secret key

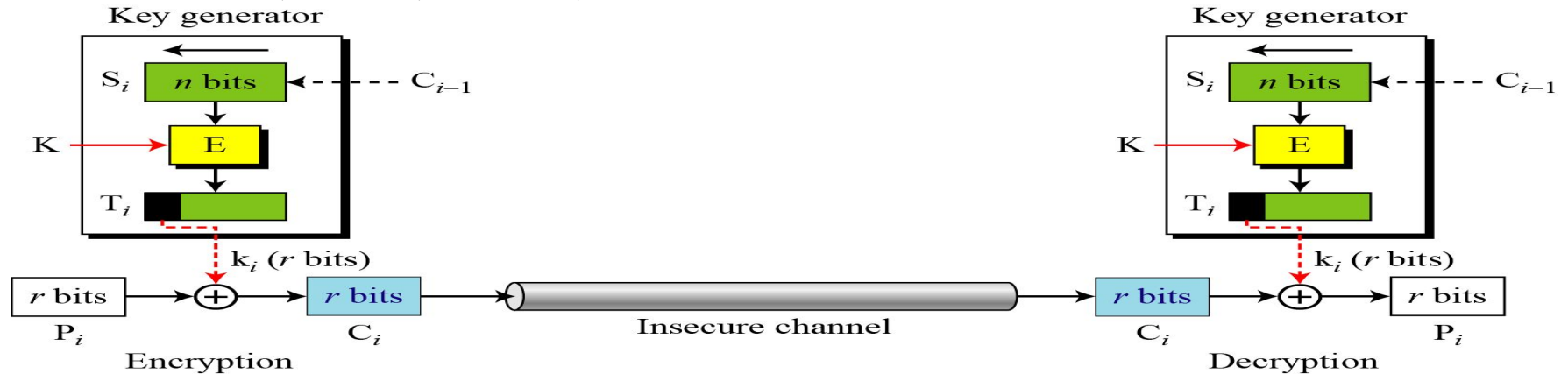
D : Decryption  
 $C_i$ : Ciphertext block  $i$   
IV: Initial vector ( $S_1$ )

$S_i$ : Shift register  
 $T_i$ : Temporary register



# Cipher Feedback (CFB)

- Message is treated as a stream of bits
- Added to the output of the block cipher
- Result is feedback for next stage (hence name)
- Standard allows any number of bit (1,8, 64 or 128 etc) to be feedback
- ✓ denoted CFB-1, CFB-8, CFB-64, CFB-128 etc



# Cipher Feedback (CFB)

- Problems

- ✓ Appropriate when data arrives in bits/bytes
- ✓ Most common stream mode
- ✓ Errors propagate for several blocks after the error

# Output Feedback (OFB)

- At times we need to use **block cipher that works as streams cipher**
- In this mode **each bit** in the ciphertext is independent of the previous bit or bits.
- This avoids error propagation.
- **Generic Steps**
- ✓ Take 64 bit **IV** store it in **shift register**, Encrypt it to get **EIV** call it **Ti**
- ✓ Perform XOR of **Leftmost r bits of PT** and **Leftmost r bits of EIV** call it **Ci**
- ✓ **Shift left IV** by **r bits** and insert **r bits of EIV (Ti)** to its right

# Output Feedback (OFB)

E : Encryption

$P_i$  : Plaintext block  $i$

K : Secret key

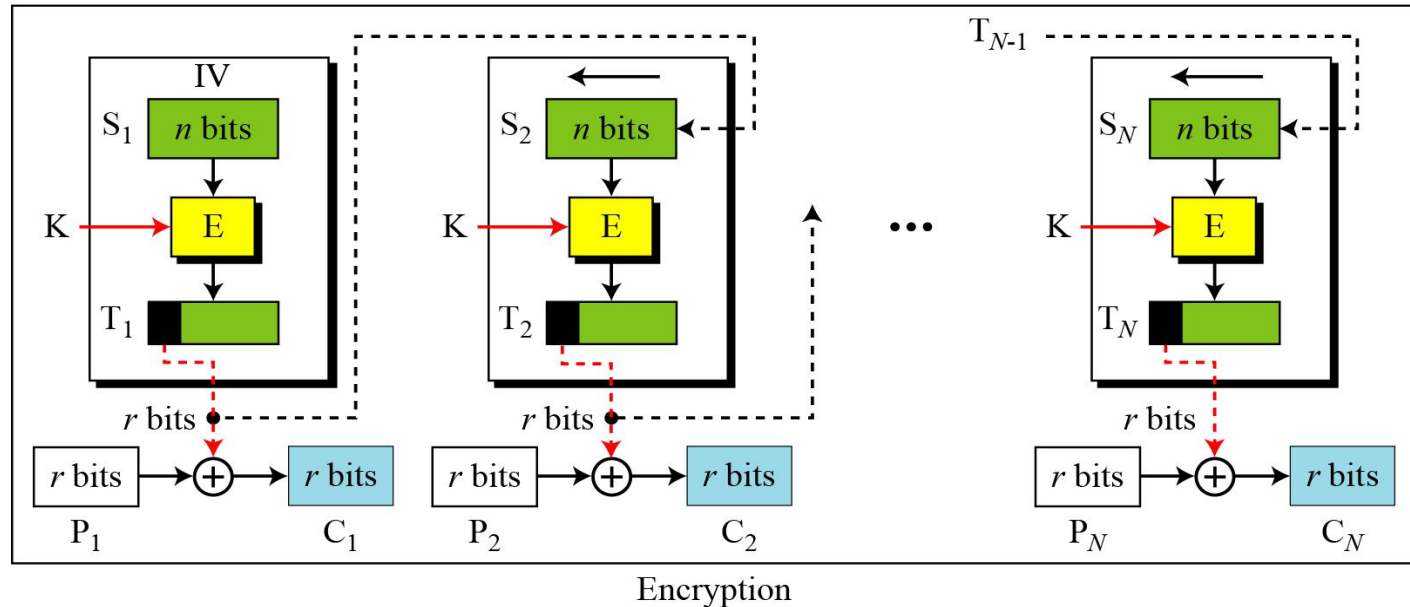
D : Decryption

$C_i$  : Ciphertext block  $i$

IV : Initial vector ( $S_1$ )

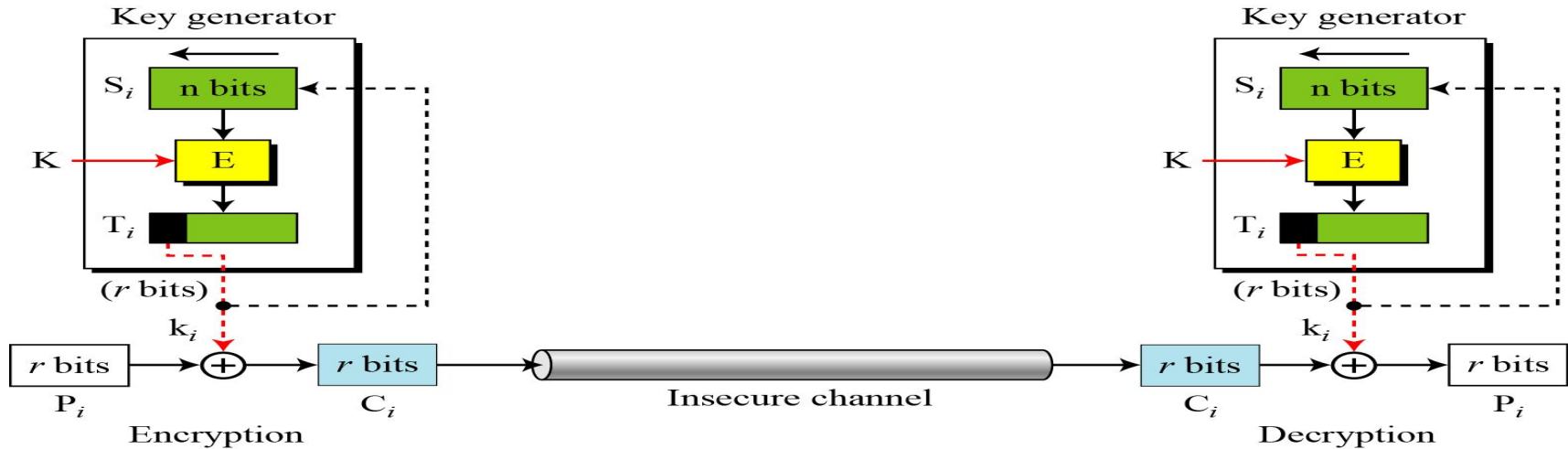
$S_i$  : Shift register

$T_i$  : Temporary register



# Output Feedback (OFB)

- Message is treated as a stream of bits
- Output of cipher is added to message
- Output is then feed back (hence name)





# Output Feedback (OFB)

- **Problems**

- ✓ bit errors do not propagate
- ✓ more vulnerable to message stream modification
- ✓ a variation of a Vernam cipher
- ✓ sender & receiver must remain in sync
- ✓ originally specified with m-bit feedback
- ✓ subsequent research has shown that only full block feedback (ie CFB-64 or CFB-128) should ever be used

# Counter Mode (CTR)

- At times we need to use block cipher that works as streams cipher
- In the counter (CTR) mode, there is no feedback.
- The pseudorandomness in the key stream is achieved using a **IV = counter**.
- No Chaining process is used.

# Counter Mode (CTR)

$E$  : Encryption

$P_i$  : Plaintext block  $i$

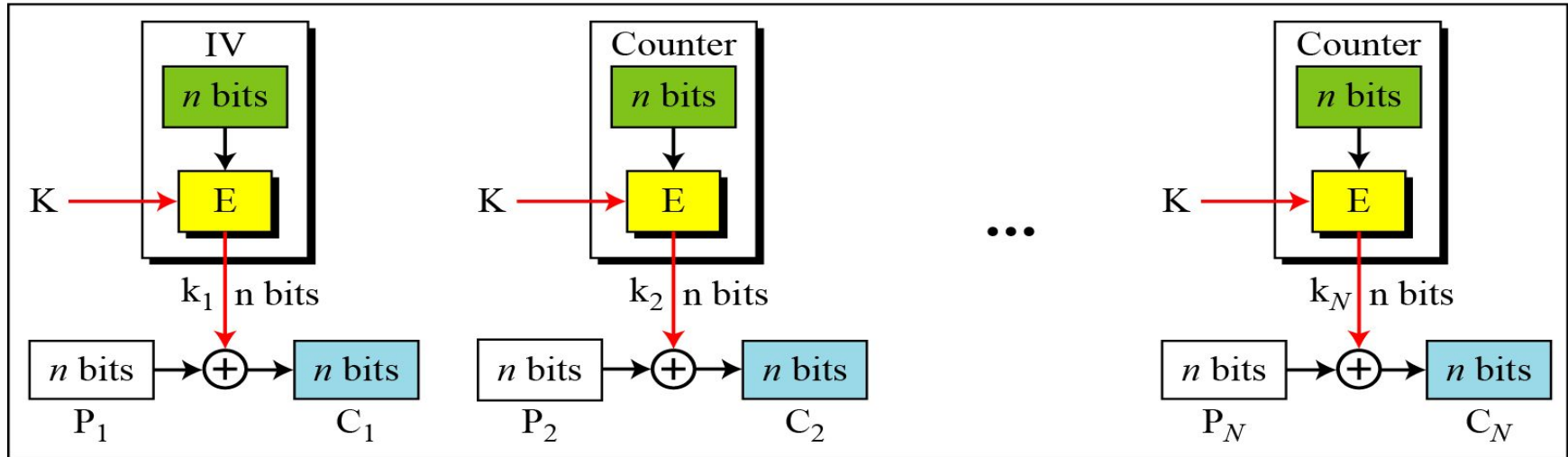
$K$  : Secret key

IV: Initialization vector

$C_i$  : Ciphertext block  $i$

$k_i$  : Encryption key  $i$

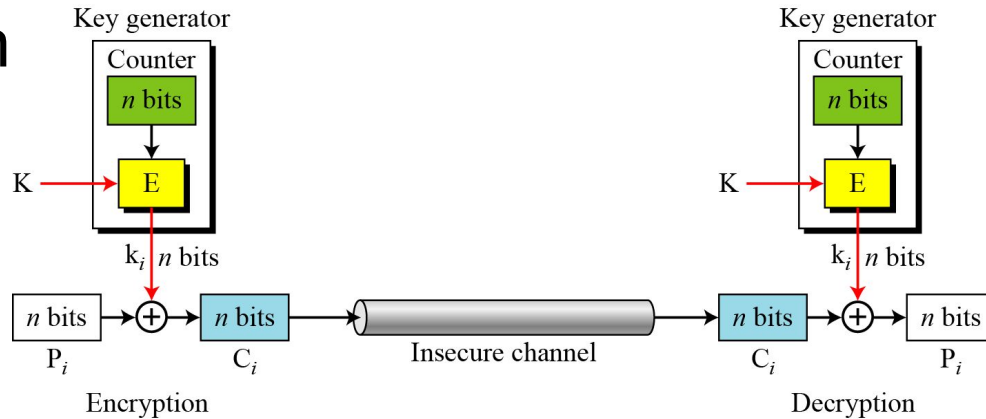
The counter is incremented for each block.



Encryption

# Counter Mode (CTR)

- Similar to OFB but encrypts counter value rather than any feedback value
- Must have a different key and counter value for every plaintext block (never reused)
- **Uses:** h



# Counter Mode (CTR)

- **Benefits & Problems**

- ✓ can do parallel encryption in hardware or software
- ✓ can reprocess in advance of need
- ✓ good for burst high speed links
- ✓ random access to encrypted data blocks
- ✓ must ensure never reuse key/counter values

# RSA Algorithm

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- Ron Rivest, Adi Shamir and Len Aldeman have developed this algorithm (Rivest-Shamir-Adleman).
- It is a block cipher which converts plain text into cipher text and vice versa at receiver side.
- The algorithm works as follow
  1. Select two prime numbers  $p$  and  $q$  where  $p \neq q$ .
  2. Calculate  $n = p * q$ .
  3. Calculate  $\Phi(n) = (p-1) * (q-1)$ .
  4. Select  $e$  such that,  $e$  is relatively prime to  $\Phi(n)$   
i.e.  $(e, \Phi(n)) = 1$  and  $1 < e < \Phi(n)$
  5. Calculate  $d = e \text{ mod } \Phi(n)$  or  $ed = 1 \text{ mod } \Phi(n)$ .
  6. Public key =  $\{e, n\}$ , private key =  $\{d, n\}$ .
  7. Find out cipher text using the formula,  
 $C = P \text{ mod } n$  where,  $P < n$  and  
 $C = \text{Cipher text}$ ,  $P = \text{Plain text}$ ,  $e = \text{Encryption key}$  and  
 $n = \text{block size}$ .
  8.  $P = C \text{ mod } n$ . Plain text  $P$  can be obtain using the given formula.
  9. where,  $d = \text{decryption key}$ .

# RSA Algorithm

---

## Example: 1

1. Two prime numbers  $p = 13, q = 11$ .
2.  $N = p * q = 13 * 11 = 143$ .
3.  $\Phi(n) = (13 - 1) * (12 - 1) = 12 * 10 = 120$ .
4. Select  $e = 13, \gcd(13, 120) = 1$ .
5. Finding  $d$ :

$$e * d \bmod \Phi(n) = 1$$

$$13 * d \bmod 120 = 1$$

(How to find:  $d * e = 1 \bmod \Phi(n) \rightarrow d = ((\Phi(n) * i) + 1) / e$

$$d = (120 + 1) / 13 = 9.30 (\because i = 1)$$

$$d = (240 + 1) / 13 = 18.53 (\because i = 2)$$

$$d = (360 + 1) / 13 = 27.76 (\because i = 3)$$

$$d = (480 + 1) / 13 = 37 (\because i = 4)$$

# RSA Algorithm

---

## Example: 1

6. Public key = {13, 143} and private key = {37, 143}.

7. Encryption : Plain text  $P = 13$ . (where,  $P < n$ )

$$C = P^e \bmod n = 13^{13} \bmod 143 = 52.$$

$$\boxed{C = 52}$$

8. Decryption:

$$P = C^d \bmod n = 52^{37} \bmod 143 = 13.$$

$$\boxed{P = 13}$$



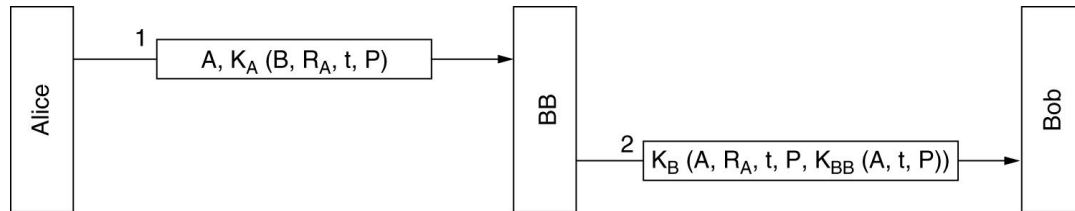
# DIGITAL SIGNATURES

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- Symmetric-Key Signatures
- Public-Key Signatures
- Message Digests

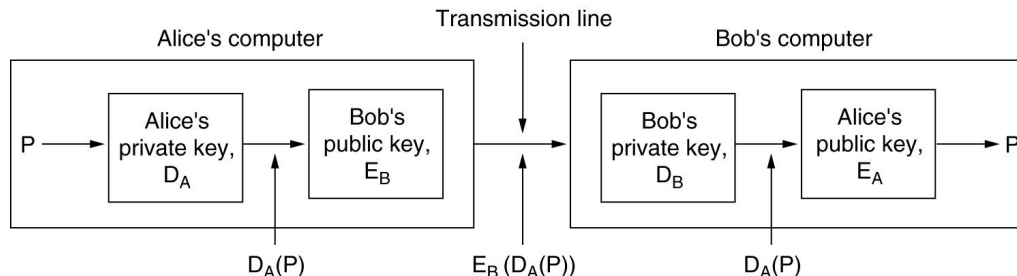
# Symmetric-Key Signatures

- One approach to digital signatures is to have a central authority that knows everything and whom everyone trusts, say, Big Brother (BB).
- Each user then chooses a secret key and carries it by hand to BB's office.
- Thus, only Alice and BB know Alice's secret key,  $K_A$ , and so on.
- When Alice wants to send a signed plaintext message,  $P$ , to her banker, Bob, she generates  $K_A(B, R_A, t, P)$ , where  $B$  is Bob's identity,  $R_A$  is a random number chosen by Alice,  $t$  is a timestamp to ensure freshness, and  $K_A(B, R_A, t, P)$  is the message encrypted with her key,  $K_A$ . Then she sends it as depicted in Figure.
- BB sees that the message is from Alice, decrypts it, and sends a message to Bob as shown.
- The message to Bob contains the plaintext of Alice's message and also the signed message  $K_{BB}(A, t, P)$ . Bob now carries out Alice's request.



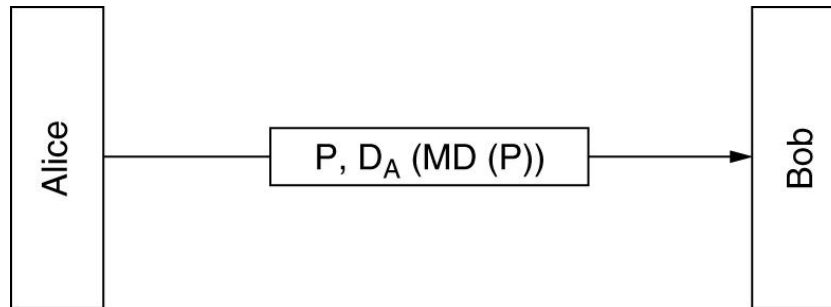
# Public-Key Signatures

- Public-key cryptography can make an important contribution in this area.
- Let us assume that the public-key encryption and decryption algorithms have the property that  $E(D(P)) = P$ , in addition, of course, to the usual property that  $D(E(P)) = P$ . (RSA has this property, so the assumption is not unreasonable.)
- Assuming that this is the case, Alice can send a signed plaintext message,  $P$ , to Bob by transmitting  $E_B(D_A(P))$ . Note carefully that Alice knows her own (private) key,  $D_A$ , as well as Bob's public key,  $E_B$ , so constructing this message is something Alice can do.
- When Bob receives the message, he transforms it using his private key, as usual, yielding  $D_A(P)$ , as shown in Fig. 8-19. He stores this text in a safe place and then applies  $E_A$  to get the original plaintext.



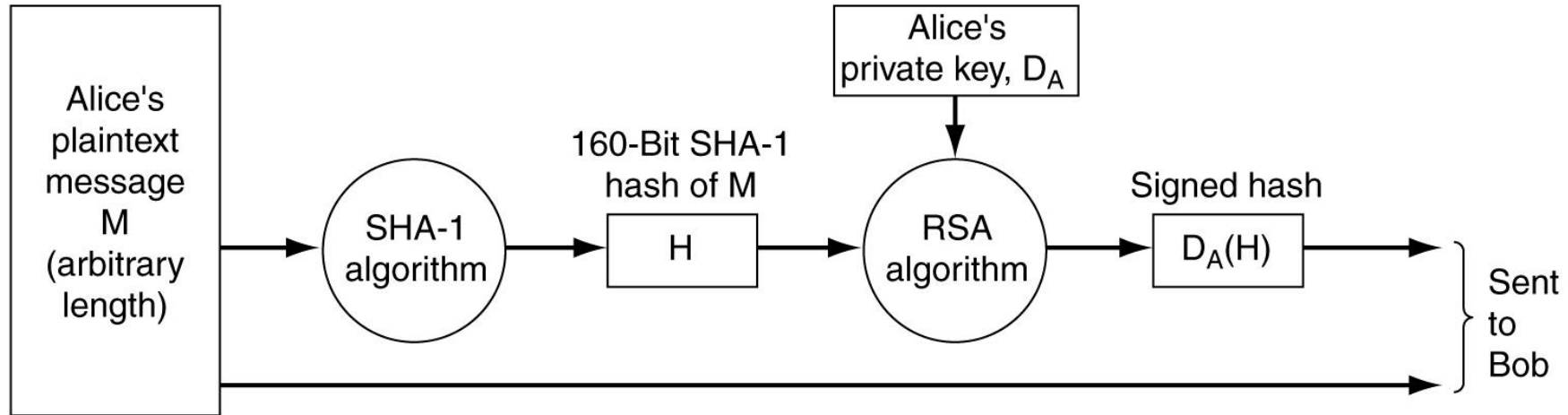
# Message Digest

- This scheme is based on the idea of a one-way hash function that takes an arbitrarily long piece of plaintext and from it computes a fixed-length bit string.
- This hash function, MD, often called a message digest, has four important properties:
  1. Given  $P$ , it is easy to compute  $MD(P)$ .
  2. Given  $MD(P)$ , it is effectively impossible to find  $P$ .
  3. Given  $P$ , no one can find  $P'$  such that  $MD(P') = MD(P)$ .
  4. A change to the input of even 1 bit produces a very different output.



# Message Digest-SHA-1 and SHA-2

- A variety of message digest functions have been proposed. One of the most widely used functions is SHA-1 (Secure Hash Algorithm 1) (NIST, 1993).
- Like all message digests, it operates by mangling bits in a sufficiently complicated way that every output bit is affected by every input bit.
- SHA-1 was developed by NSA and blessed by NIST in FIPS 180-1. It processes input data in 512-bit blocks, and it generates a 160-bit message digest.



# Message Digest-MD5

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- MD5 (Rivest, 1992) is the fifth in a series of message digests designed by Ronald Rivest. Very briefly, the message is padded to a length of 448 bits (modulo 512).
- Then the original length of the message is appended as a 64-bit integer to give a total input whose length is a multiple of 512 bits.
- Each round of the computation takes a 512-bit block of input and mixes it thoroughly with a running 128-bit buffer.
- For good measure, the mixing uses a table constructed from the sine function.
- The point of using a known function is to avoid any suspicion that the designer built in a clever back door through which only he can enter.
- This process continues until all the input blocks have been consumed.
- The contents of the 128-bit buffer form the message digest.

# THANK YOU