

6.009: Fundamentals of Programming

Week 4 Lecture: UC Search and Informed Search

- Review of BFS/DFS
- Finding Minimum-cost Paths
- Heuristics

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Graph Search (Path Finding)

- Some set V of vertices (sometimes called states)
- Some collection E of edges connecting vertices

Search Algorithms

Example: Eight Puzzle

Start

1	2	3
4	5	6
7	8	

Goal

	1	2
3	4	5
6	7	8

Rearrange board by sequentially sliding tiles into the free spot.

Eight Puzzle

Rearrange board by sequentially sliding tiles into the free spot.

1	2	3
4	5	6
7	8	

Eight Puzzle

Rearrange board by sequentially sliding tiles into the free spot.

1	2	3
4	5	
7	8	6

Eight Puzzle

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4		5
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7	4	5
	8	6

Eight Puzzle

Rearrange board by sequentially sliding tiles into the free spot.

1	2	3
7	4	5
8		6

Eight Puzzle

Rearrange board by sequentially sliding tiles into the free spot.

1	2	3
7	4	5
8	6	

Eight Puzzle

Rearrange board by sequentially sliding tiles into the free spot.

1	2	3
7	4	
8	6	5

Eight Puzzle

Rearrange board by sequentially sliding tiles into the free spot.

1	2	
7	4	3
8	6	5

Eight Puzzle

Rearrange board by sequentially sliding tiles into the free spot.

1		2
7	4	3
8	6	5

Eight Puzzle

Rearrange board by sequentially sliding tiles into the free spot.

1	4	2
7		3
8	6	5

Eight Puzzle

Rearrange board by sequentially sliding tiles into the free spot.

1	4	2
7	6	3
8		5

Eight Puzzle

Rearrange board by sequentially sliding tiles into the free spot.

1	4	2
7	6	3
	8	5

Eight Puzzle

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1	4	2
	6	3
7	8	5

Eight Puzzle

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1	4	2
6		3
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Eight Puzzle

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Eight Puzzle

Rearrange board by sequentially sliding tiles into the free spot.

	1	2
3	4	5
6	7	8

That solution took twenty-two moves.

How difficult is this problem?

Check Yourself!

1	2	3
4	5	6
7	8	

	1	2
3	4	5
6	7	8

How many different board configurations (vertices) exist?

1. $8^2 = 64$
2. $9^2 = 81$
3. $8! = 40,320$
4. $9! = 362,880$

Eight Puzzle

1	2	3
4	5	6
7	8	

	1	2
3	4	5
6	7	8

Is the solution with 22 moves optimal? Do shorter solutions exist?

Do we have to look at all 362,880 configurations to be sure?

Search Algorithm

Develop an algorithm to systematically conduct a search.

Analyze how well the algorithm performs.

Optimize the algorithm:

- find the “best” solution (i.e., minimum path length)
- by considering as few cases as possible.

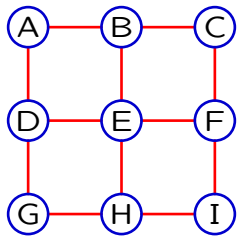
Last Week's Algorithms

Graph Search Algorithm:

- Initialize **visited set**
 - Initialize **agenda** (list of paths to consider)
 - Repeat the following:
 - Remove one path from the agenda
 - For each child (of that path's terminal vertex):
 - ★ If it satisfies the goal condition, return a path.
 - ★ Otherwise, if it is not already in the visited set:
 - ▷ Add the new path to the agenda
 - ▷ Add the new vertex to the visited set
- until **goal is found** or **agenda is empty**

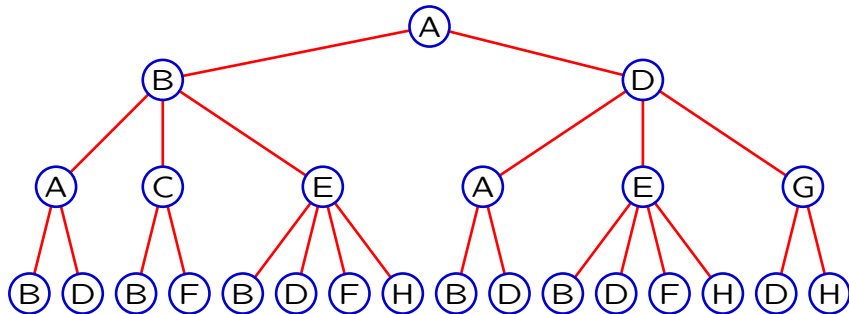
Example

Find shortest path between 2 points on a rectangular grid.



Order Matters

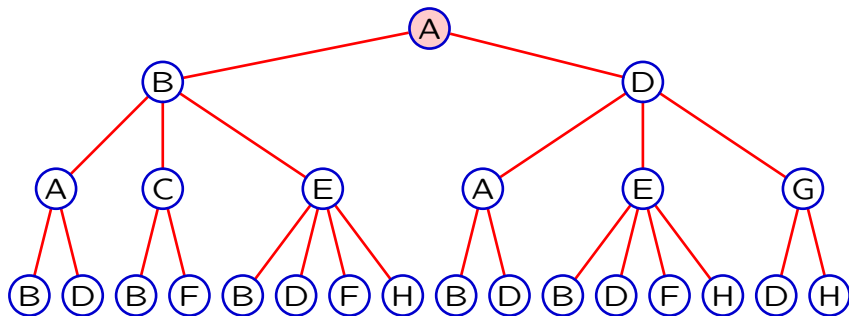
Replace first path in agenda by its children:



step Agenda

Order Matters

Replace first path in agenda by its children:

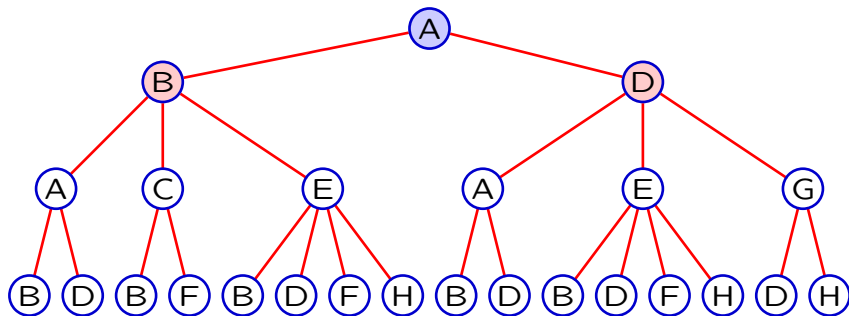


step Agenda

0: **A**

Order Matters

Replace first path in agenda by its children:



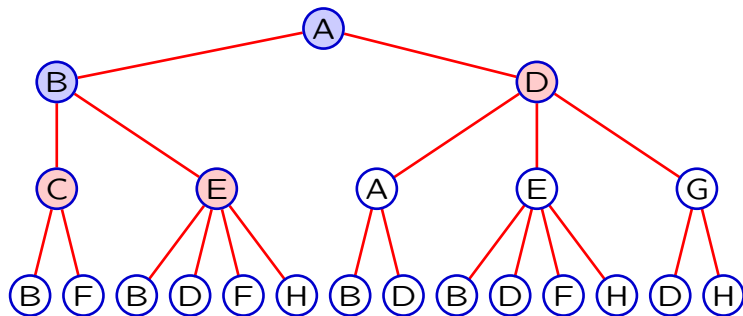
step Agenda

0: A

1: AB AD

Order Matters

Replace first path in agenda by its children:



step Agenda

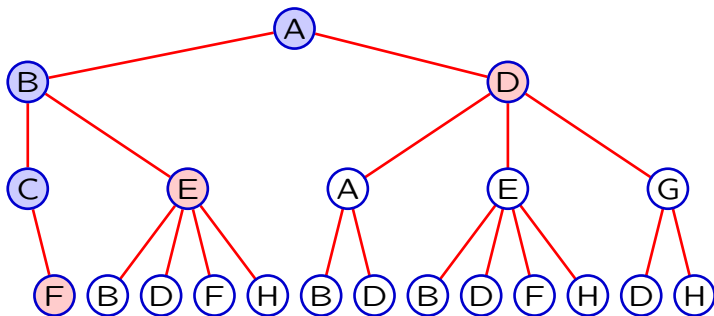
0: A

1: AB AD

2: ABC ABE AD

Order Matters

Replace first path in agenda by its children:



step Agenda

0: A

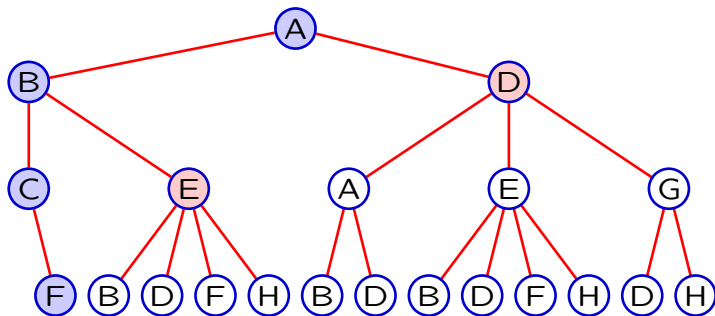
1: AB AD

2: ABC ABE AD

3: ABCF ABE AD

Order Matters

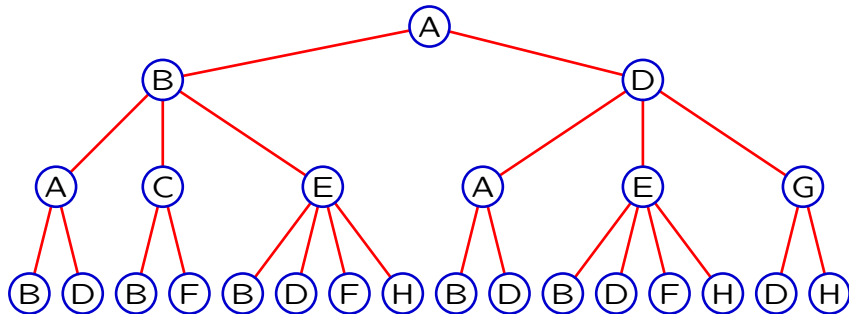
Replace first path in agenda by its children:



Depth-first Search

Order Matters

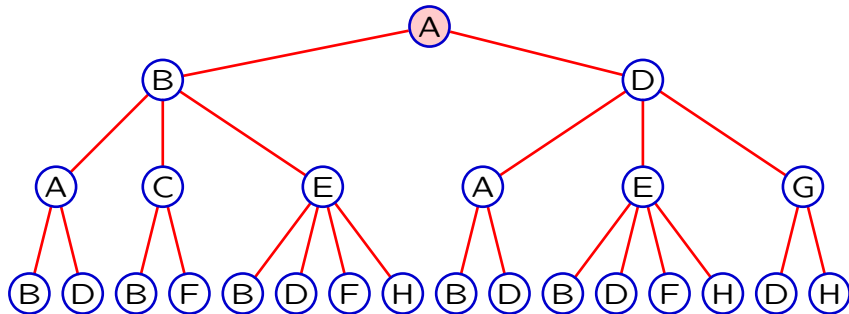
Replace last path in agenda by its children:



step Agenda

Order Matters

Replace last path in agenda by its children:

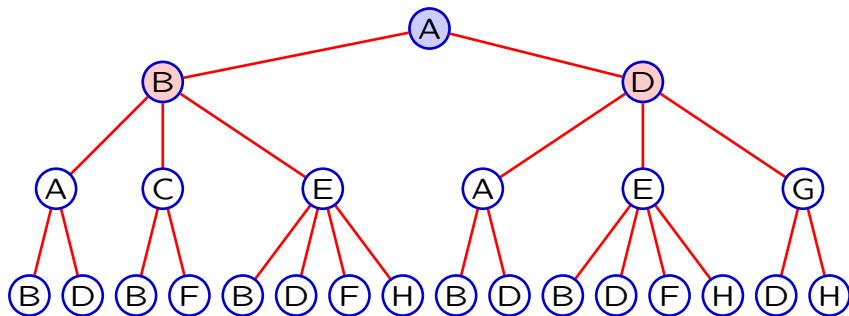


step Agenda

0: **A**

Order Matters

Replace last path in agenda by its children:



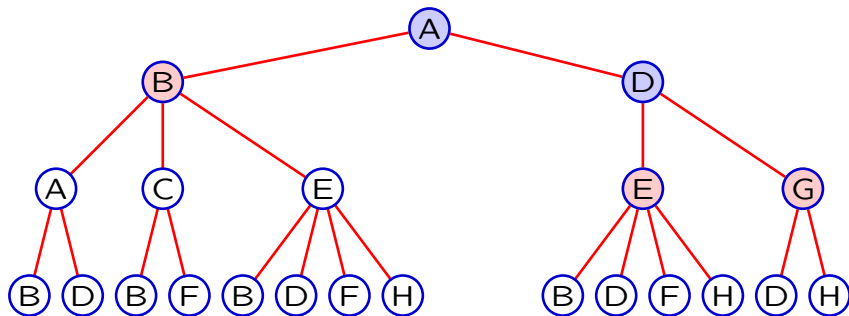
step Agenda

0: A

1: AB AD

Order Matters

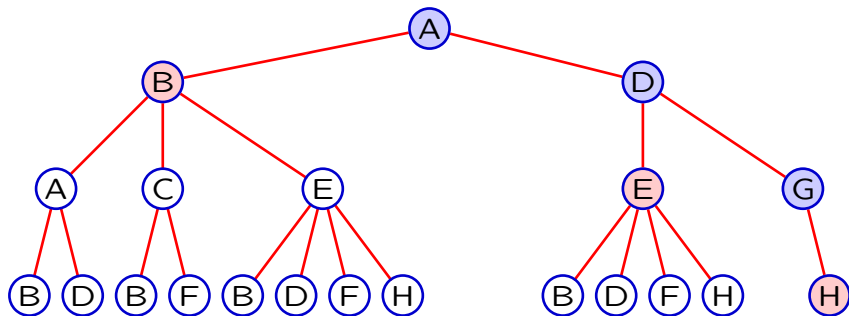
Replace last path in agenda by its children:



step	Agenda
0:	A
1:	AB AD
2:	AB ADE ADG

Order Matters

Replace last path in agenda by its children:



step Agenda

0: A

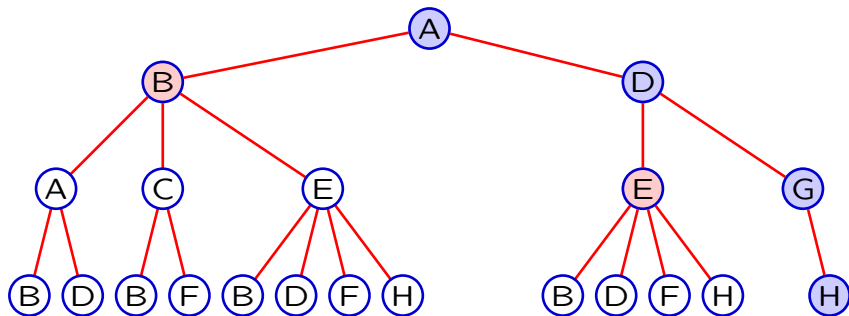
1: AB AD

2: AB ADE ADG

3: AB ADE ADGH

Order Matters

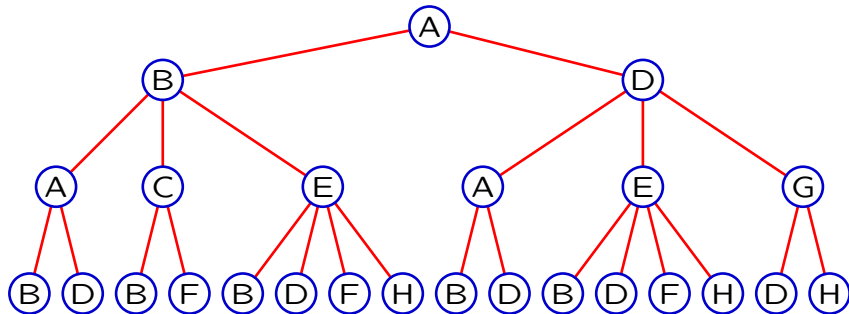
Replace last path in agenda by its children:



also **Depth-first Search**

Order Matters

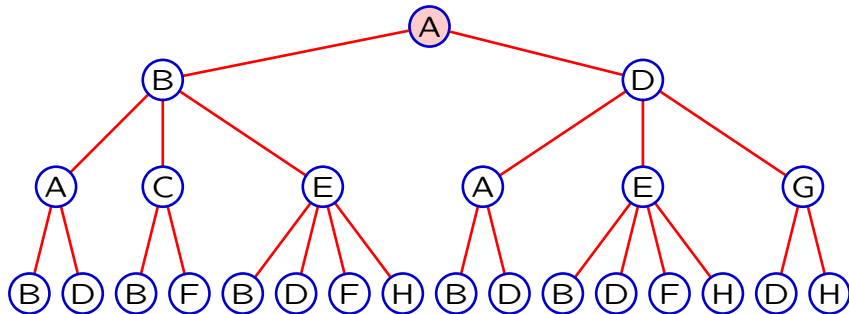
Remove first path from agenda. Add its children to end of agenda.



step Agenda

Order Matters

Remove first path from agenda. Add its children to end of agenda.

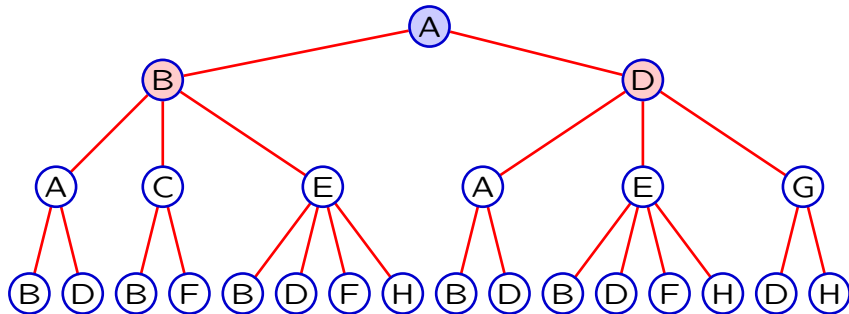


step Agenda

0: **A**

Order Matters

Remove first path from agenda. Add its children to end of agenda.



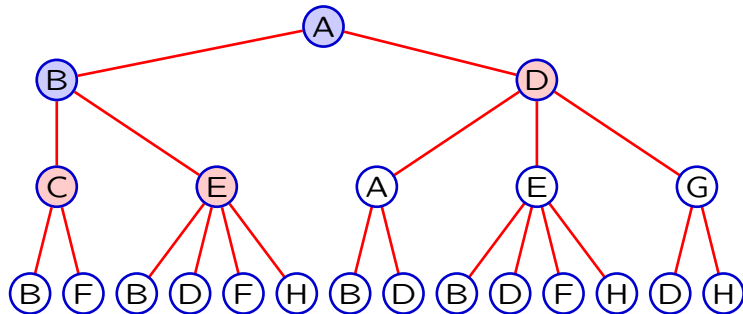
step Agenda

0: A

1: AB AD

Order Matters

Remove first path from agenda. Add its children to end of agenda.



step Agenda

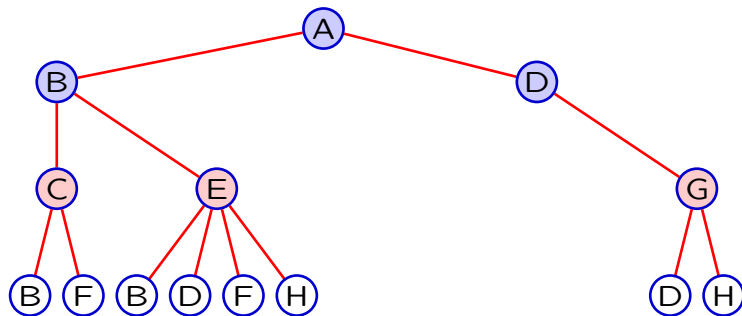
0: A

1: AB AD

2: AD ABC ABE

Order Matters

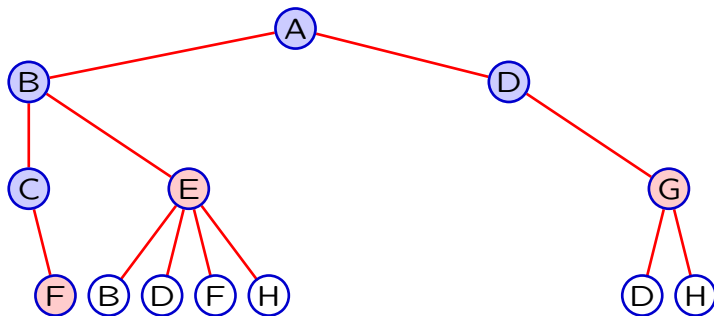
Remove first path from agenda. Add its children to end of agenda.



step	Agenda
0:	A
1:	AB AD
2:	AD ABC ABE
3:	ABC ABE ADG

Order Matters

Remove first path from agenda. Add its children to end of agenda.



step Agenda

1: AB AD

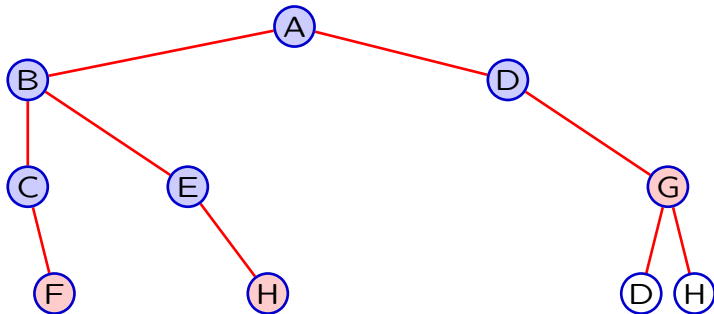
2: AD ABC ABE

3: **ABC** ABE ADG

4: ABE ADG **ABCF**

Order Matters

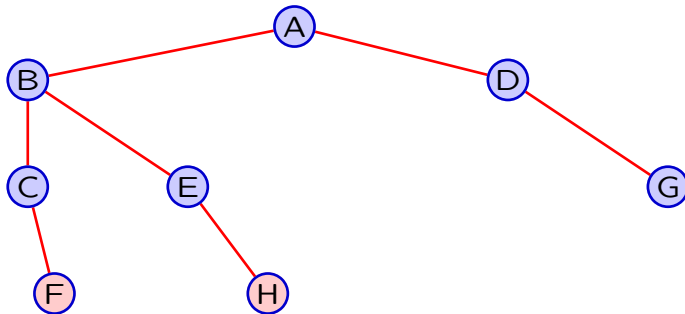
Remove first path from agenda. Add its children to end of agenda.



step	Agenda
2:	AD ABC ABE
3:	ABC ABE ADG
4:	ABE ADG ABCF
5:	ADG ABCF ABEH

Order Matters

Remove first path from agenda. Add its children to end of agenda.



step Agenda

3: ABC ABE ADG

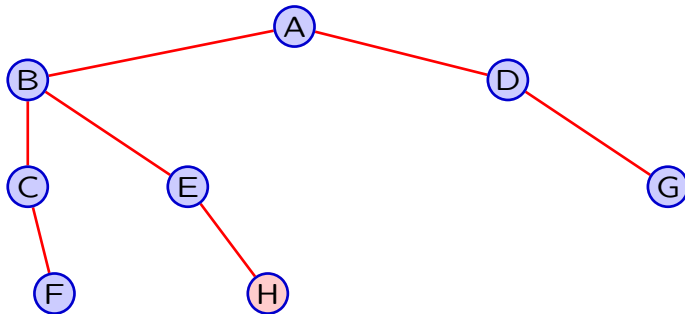
4: ABE ADG ABCF

5: **ADG** ABCF ABEH

6: ABCF ABEH

Order Matters

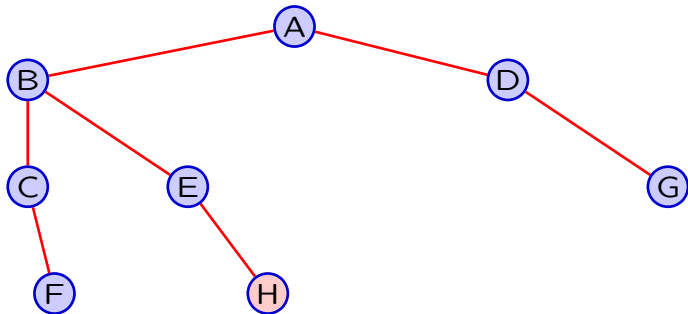
Remove first path from agenda. Add its children to end of agenda.



step	Agenda
4:	ABE ADG ABCF
5:	ADG ABCF ABEH
6:	ABCF ABEH
7:	ABEH ABCFI

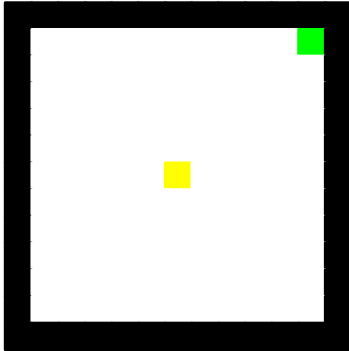
Order Matters

Remove first path from agenda. Add its children to end of agenda.

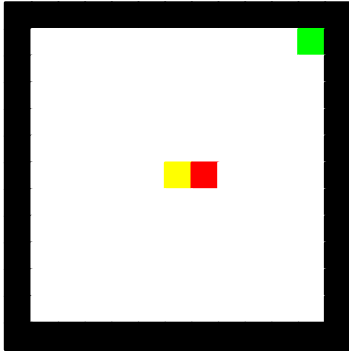


Breadth-first Search

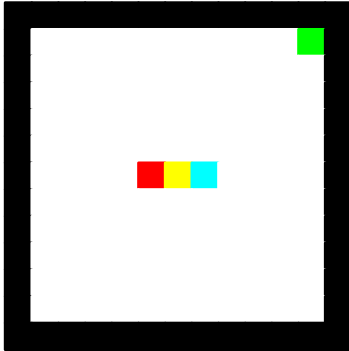
Grid: BFS 1



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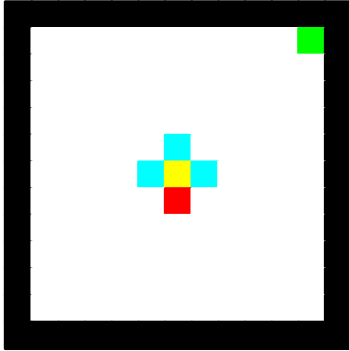


Grid: BFS 1

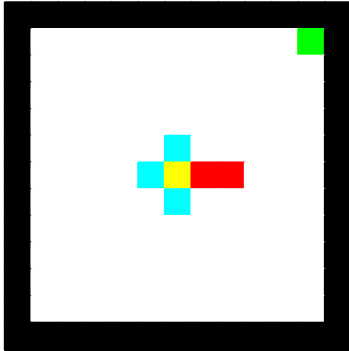


Grid: BFS 1

Grid: BFS 1

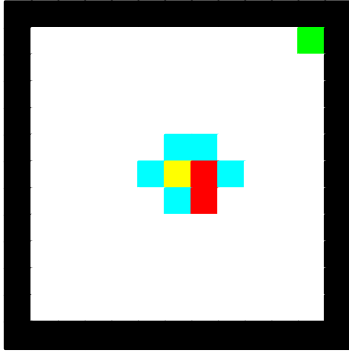


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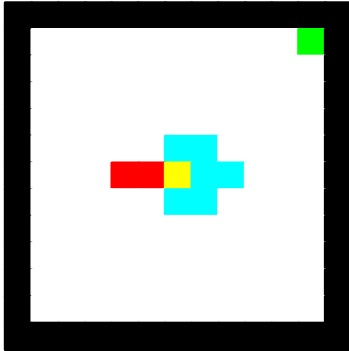


Grid: BFS 1

Grid: BFS 1

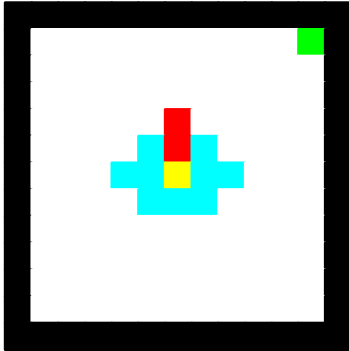


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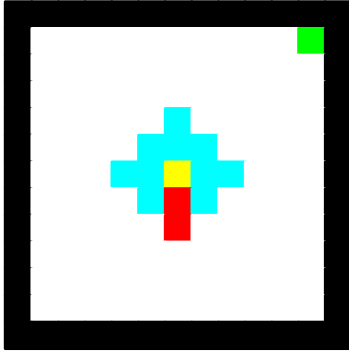


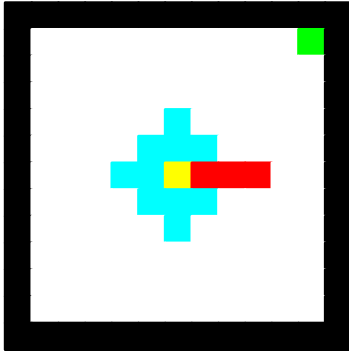
Grid: BFS 1

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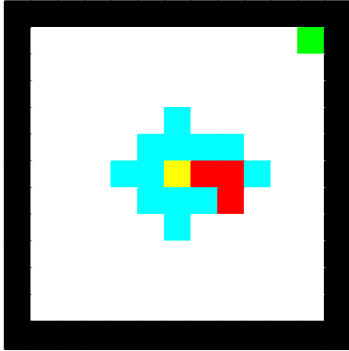


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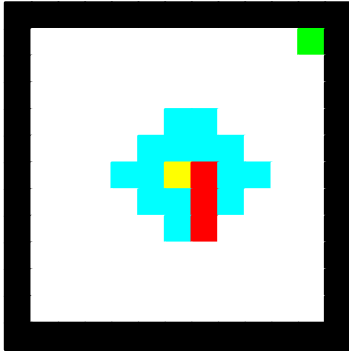




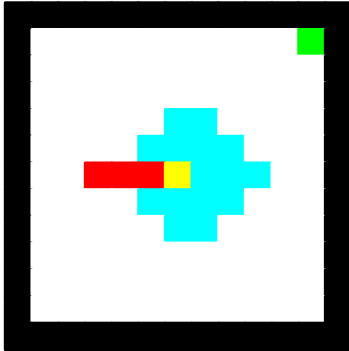
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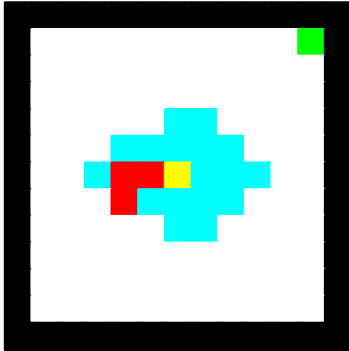


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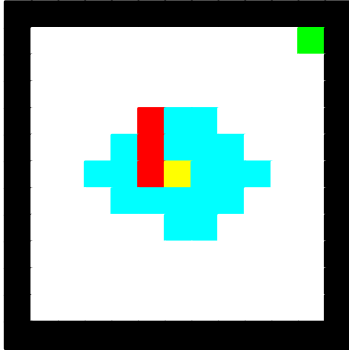


Grid: BFS 1

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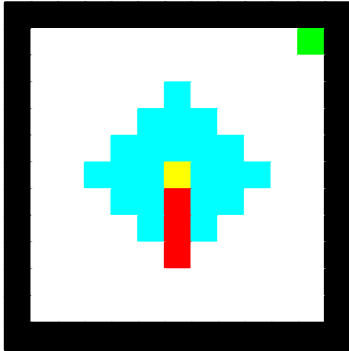
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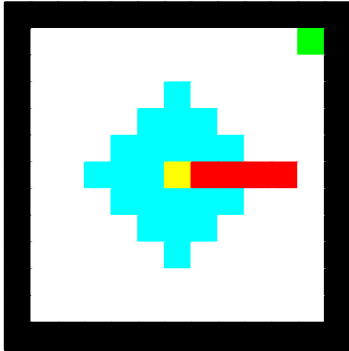


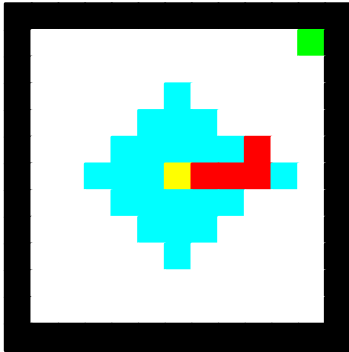
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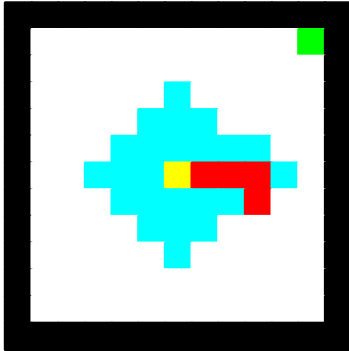
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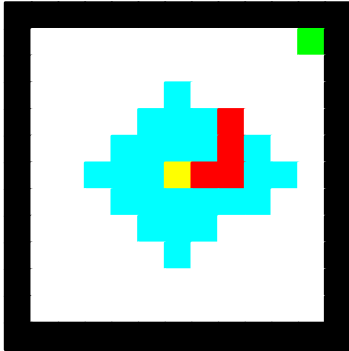




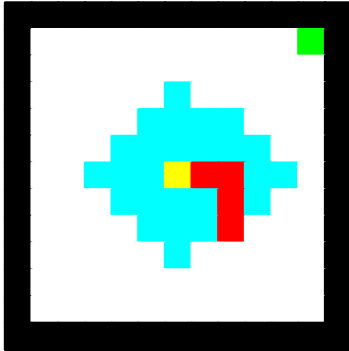




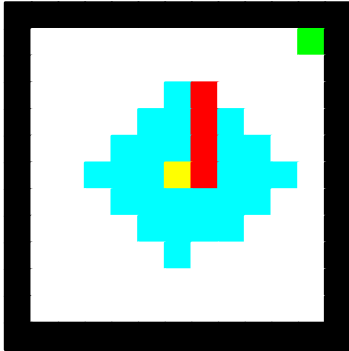
Grid: BFS 1



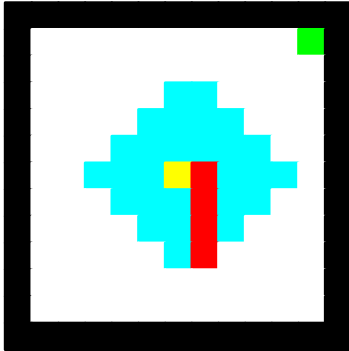
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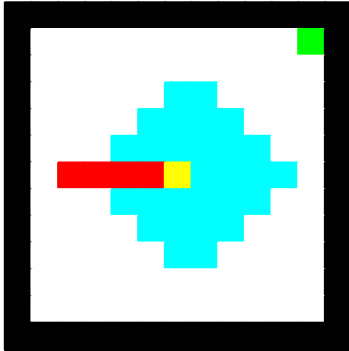


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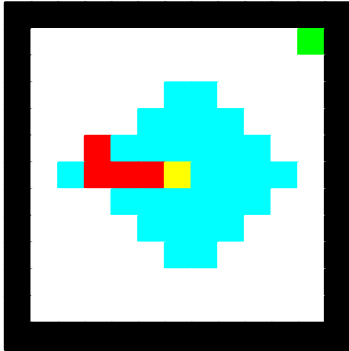


Grid: BFS 1

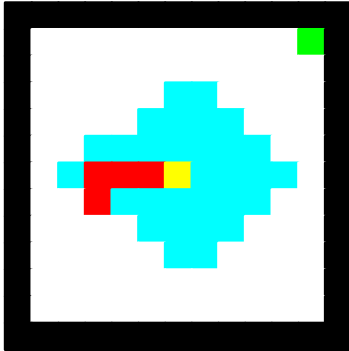




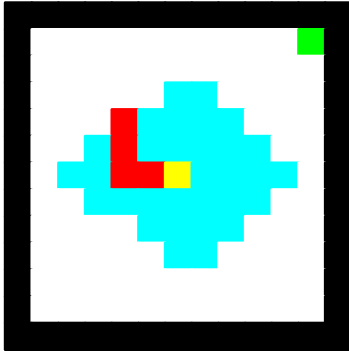
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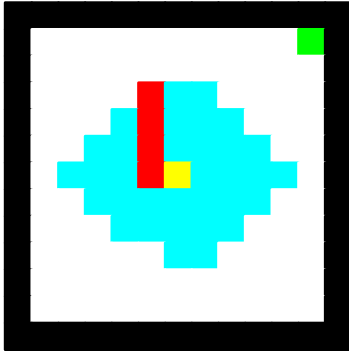


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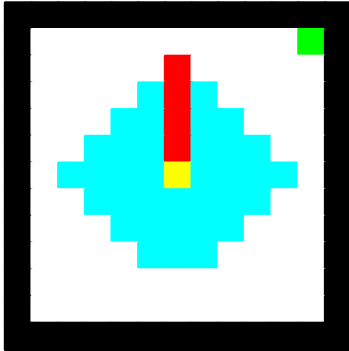
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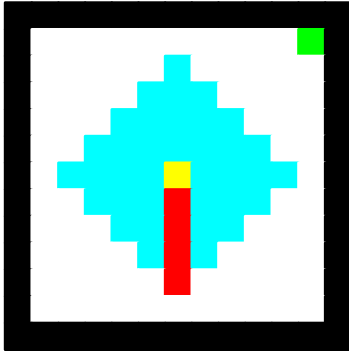


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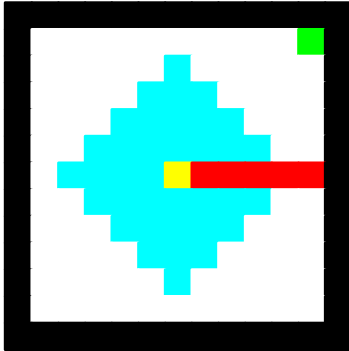
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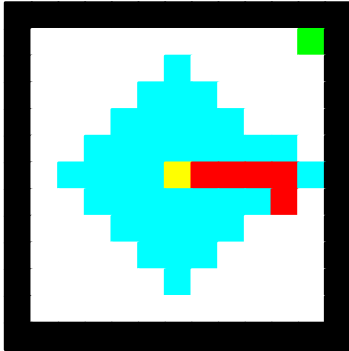
Grid: BFS 1



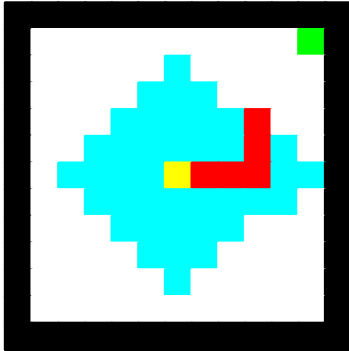
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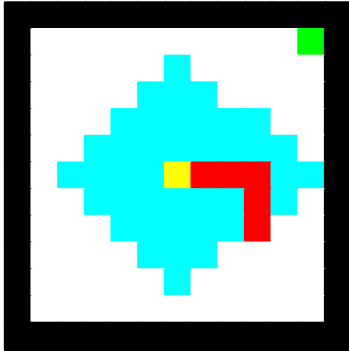
Grid: BFS 1



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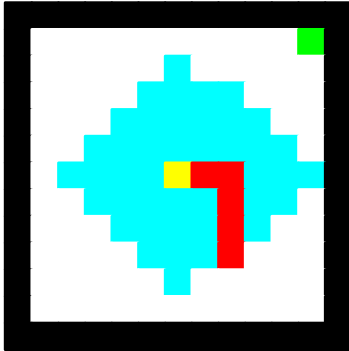


Grid: BFS 1

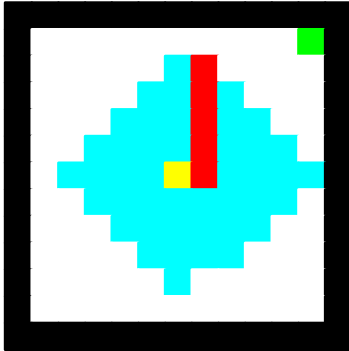


Grid: BFS 1

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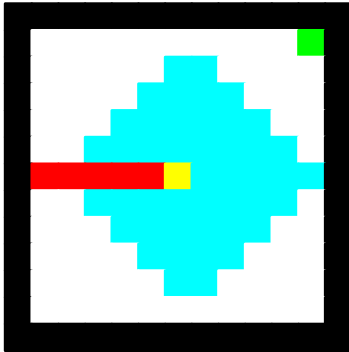


Grid: BFS 1

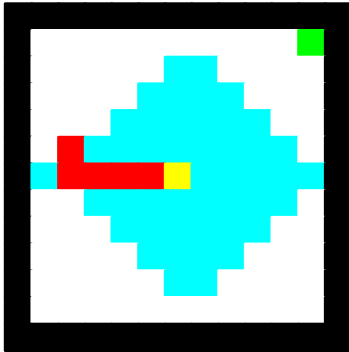


Grid: BFS 1

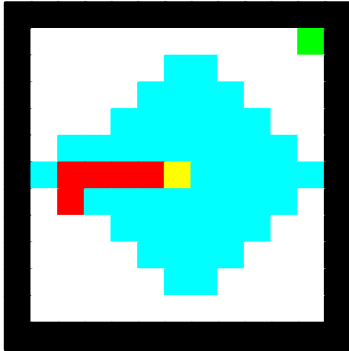
Grid: BFS 1



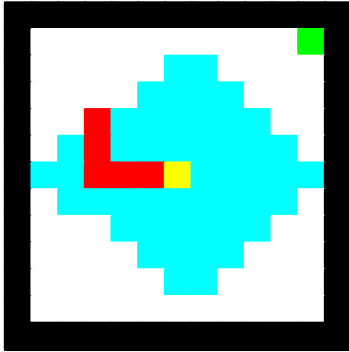
Grid: BFS 1



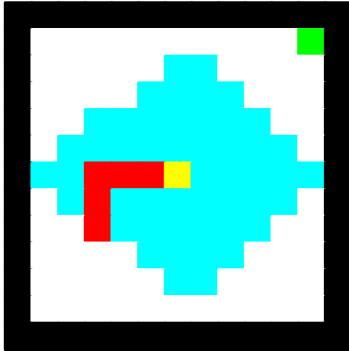
Grid: BFS 1



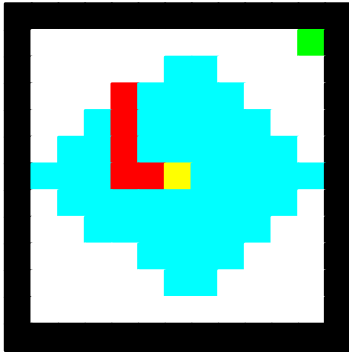
Grid: BFS 1



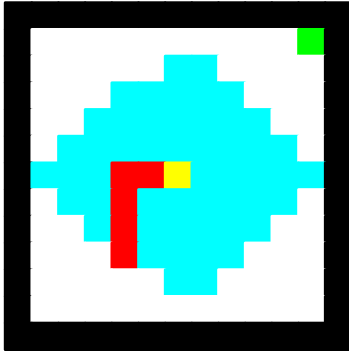
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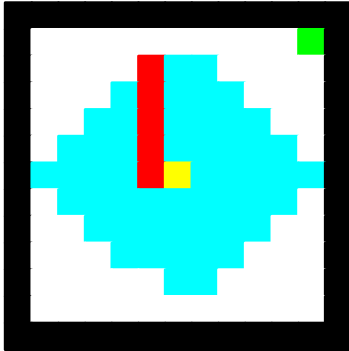
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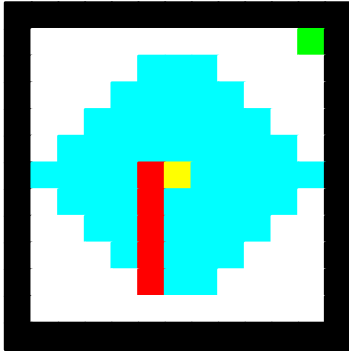
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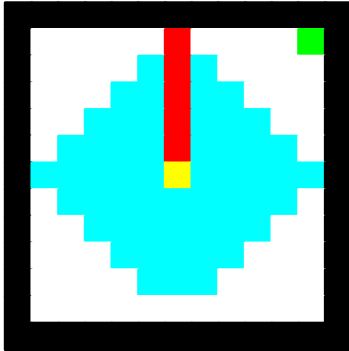
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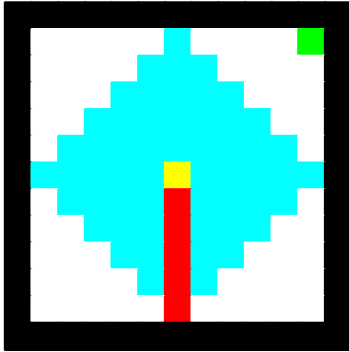
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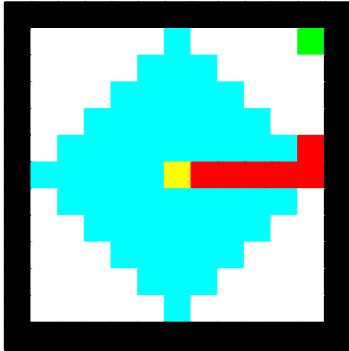
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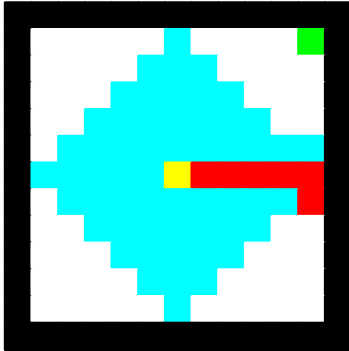


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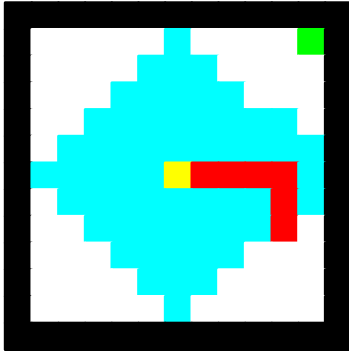
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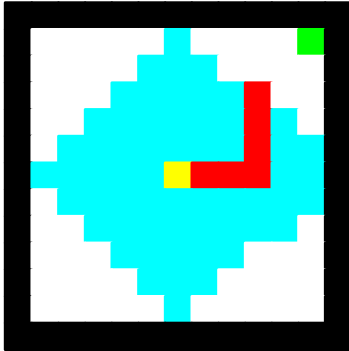


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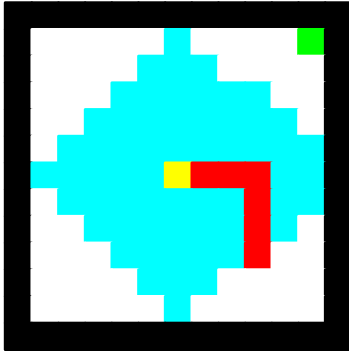
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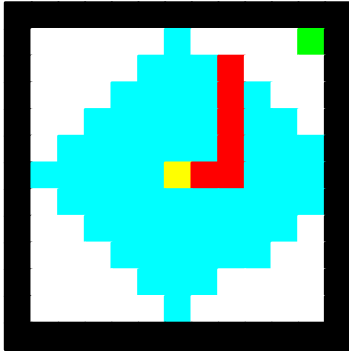
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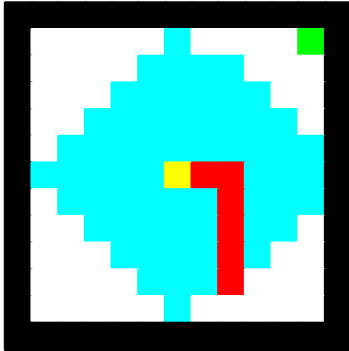
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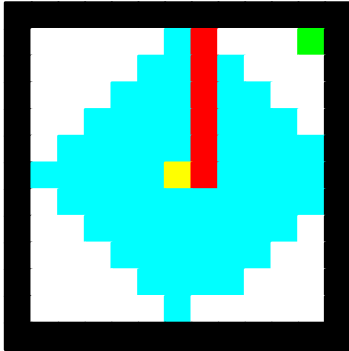
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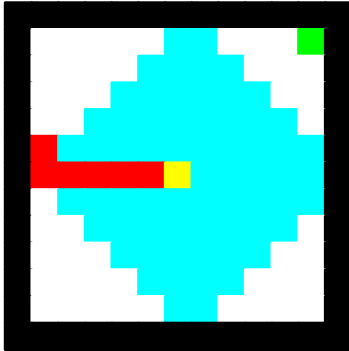


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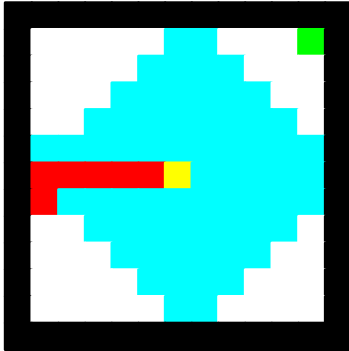


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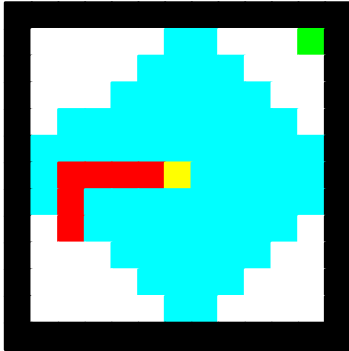


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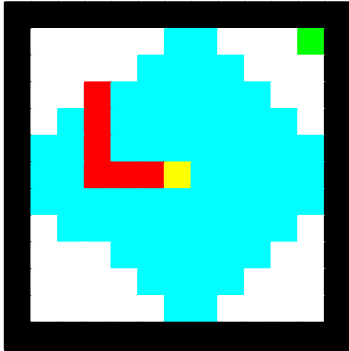


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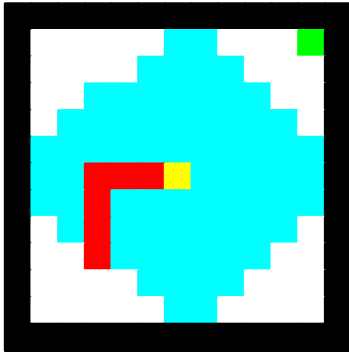
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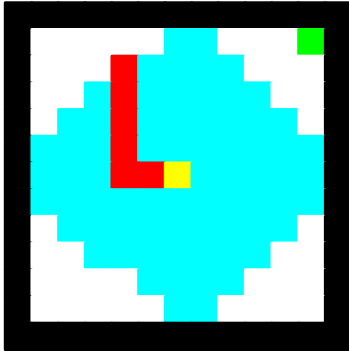
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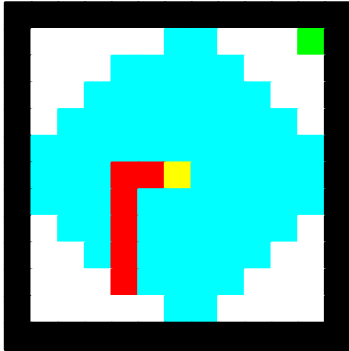
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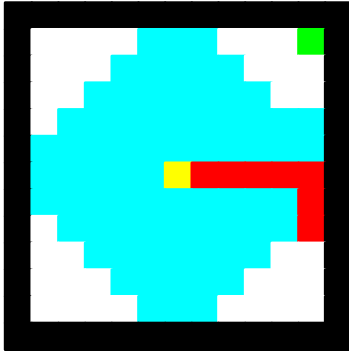


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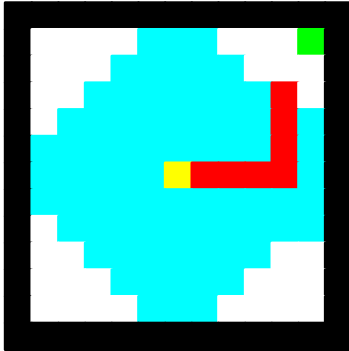
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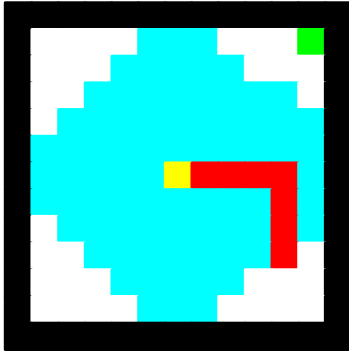
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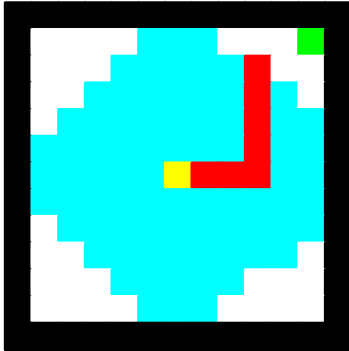
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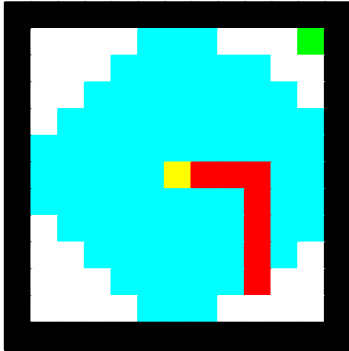
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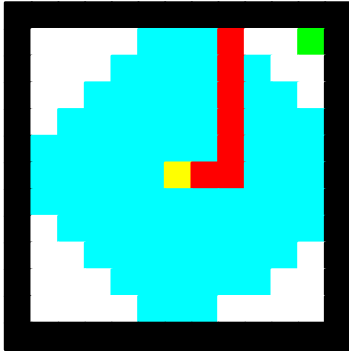
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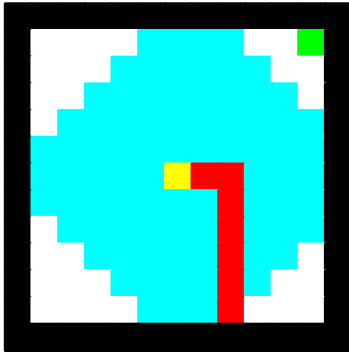
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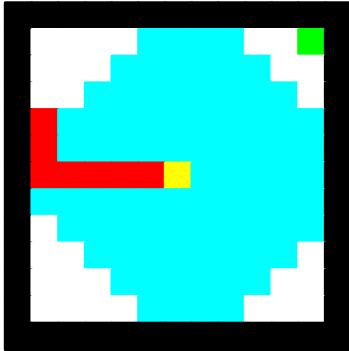
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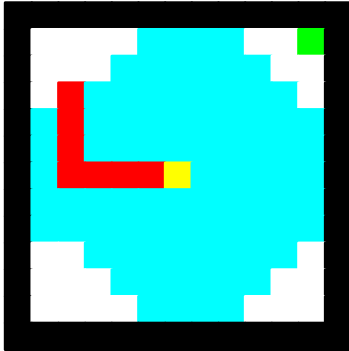


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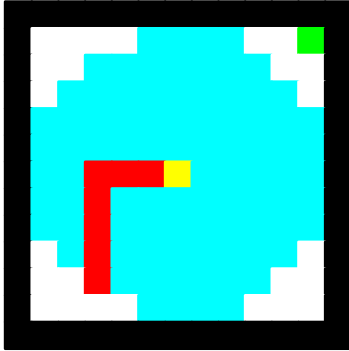
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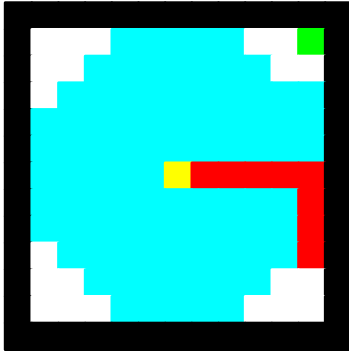


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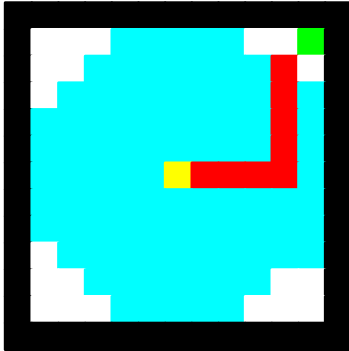
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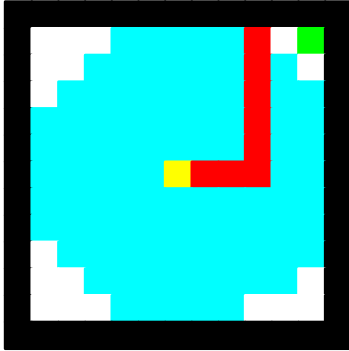


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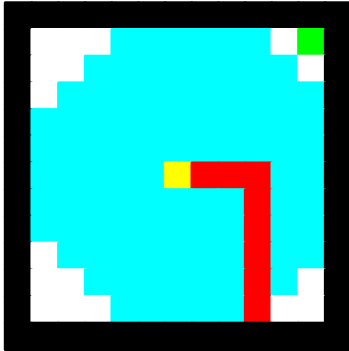


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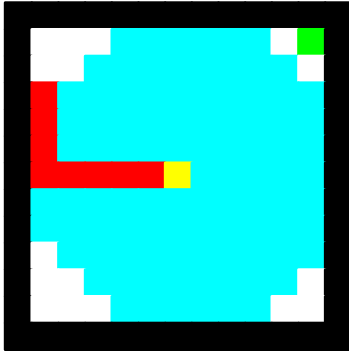
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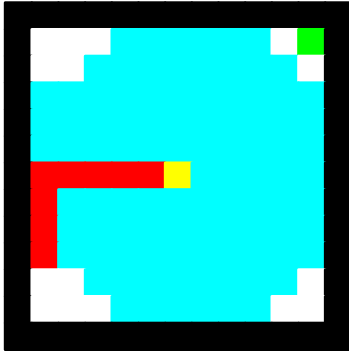
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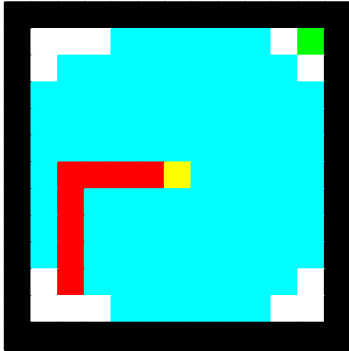


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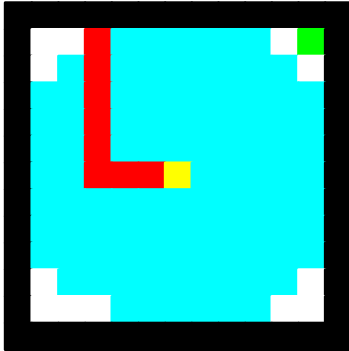


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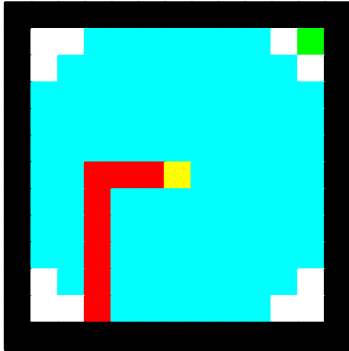
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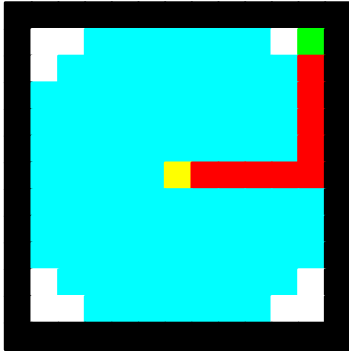
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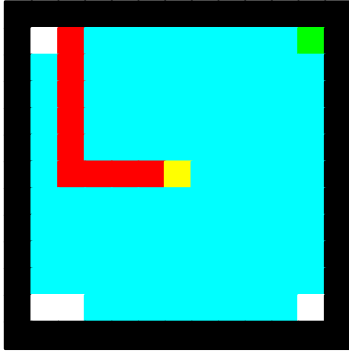
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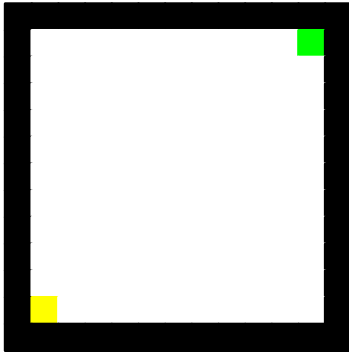
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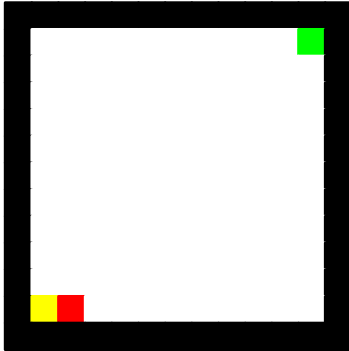


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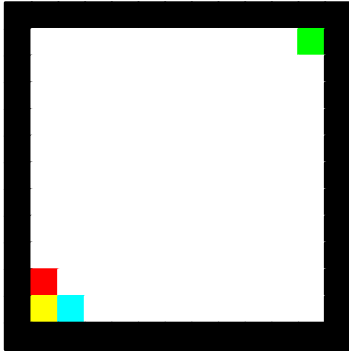
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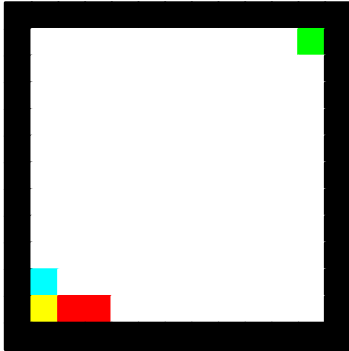
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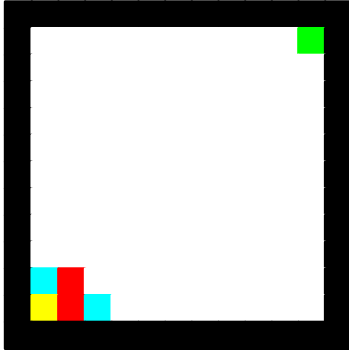
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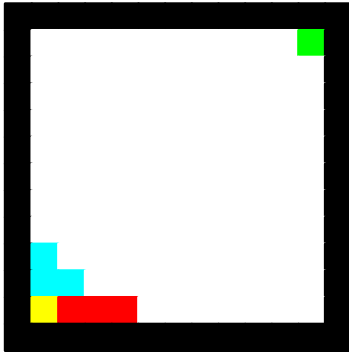


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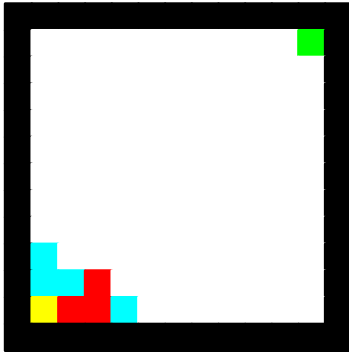


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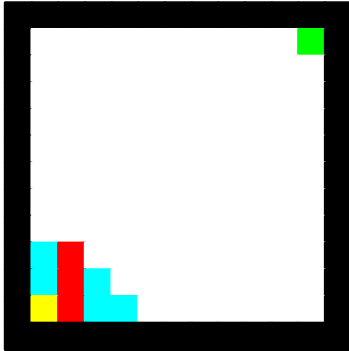
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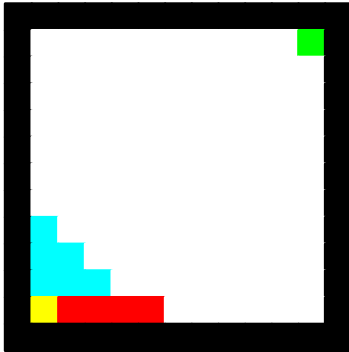


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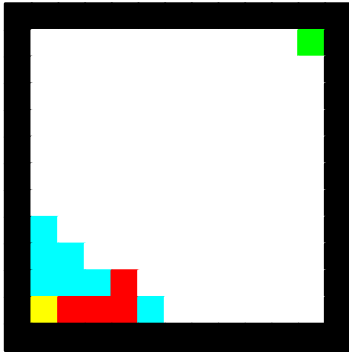


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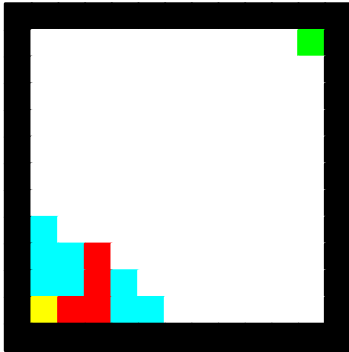
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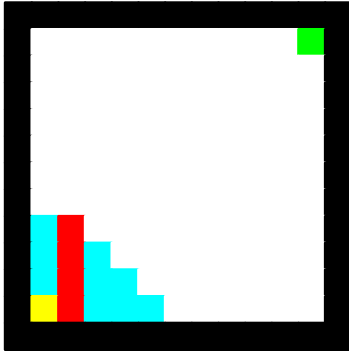
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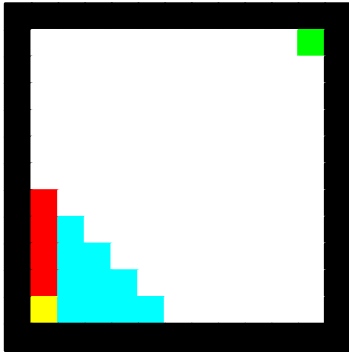
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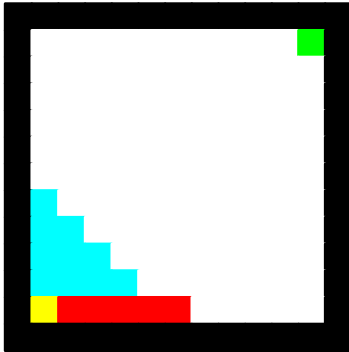
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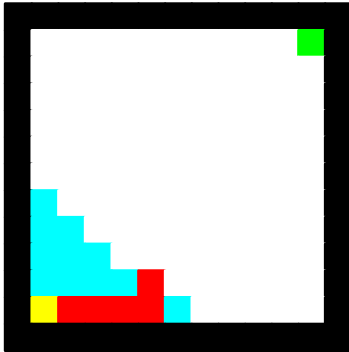
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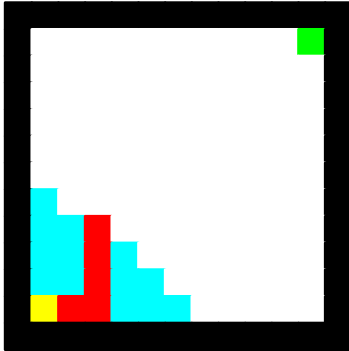


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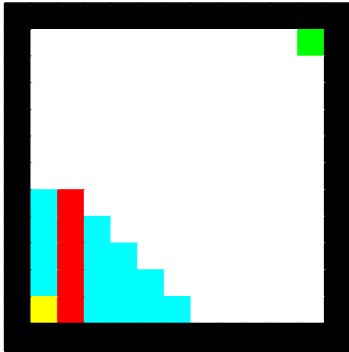


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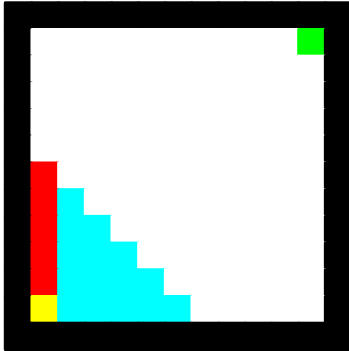
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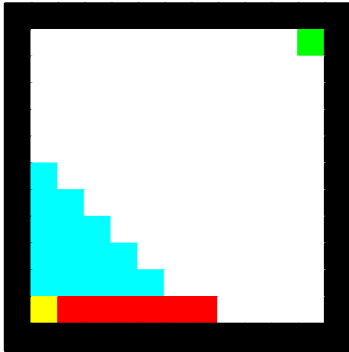


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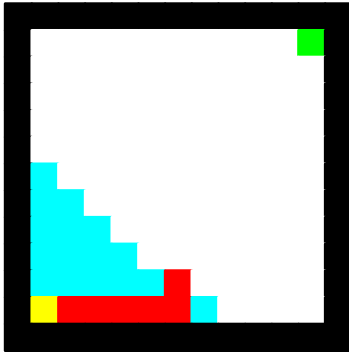


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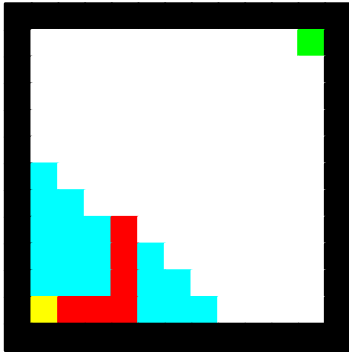


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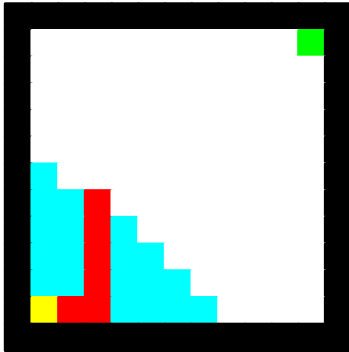


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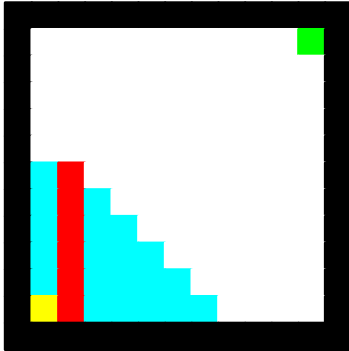
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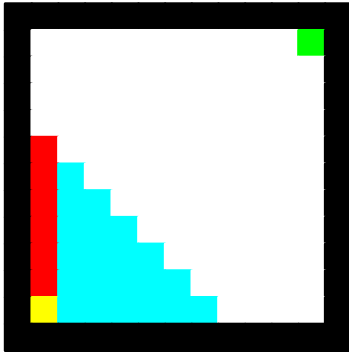
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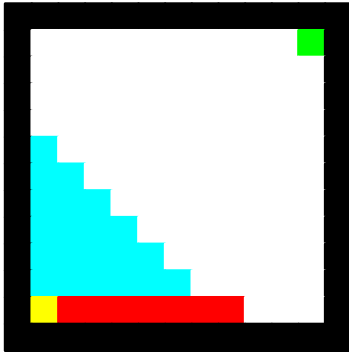
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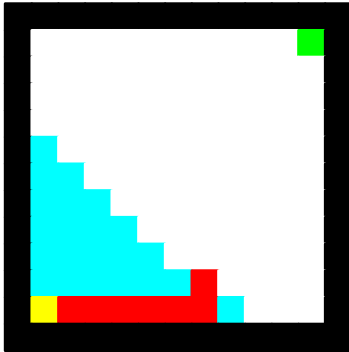


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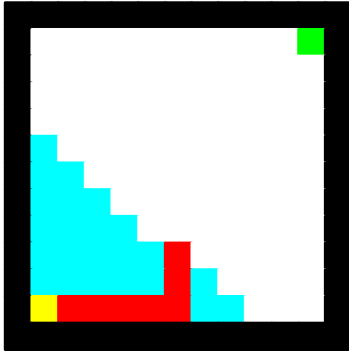


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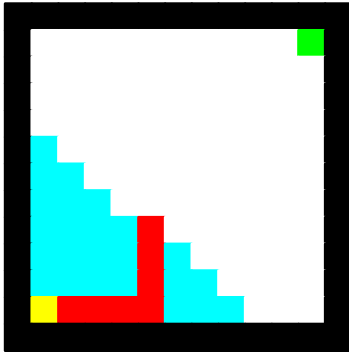




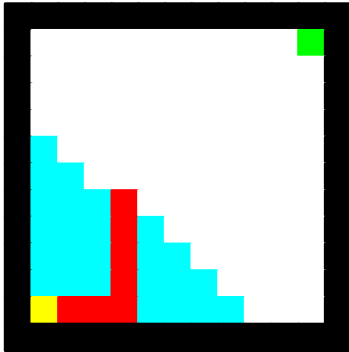
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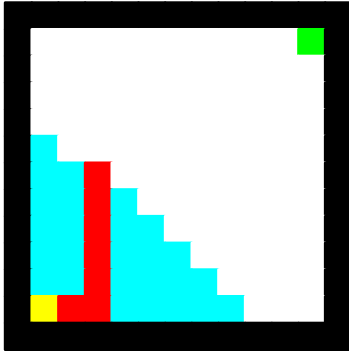
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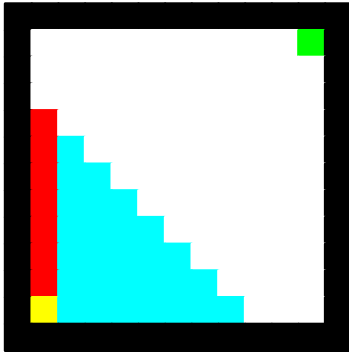
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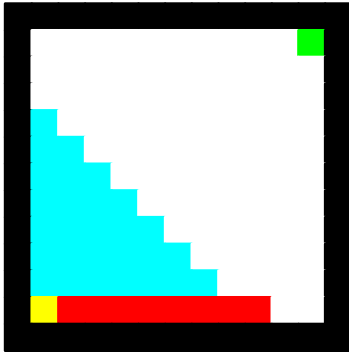


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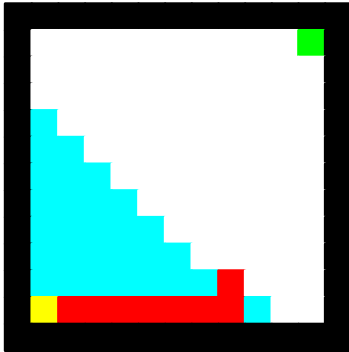


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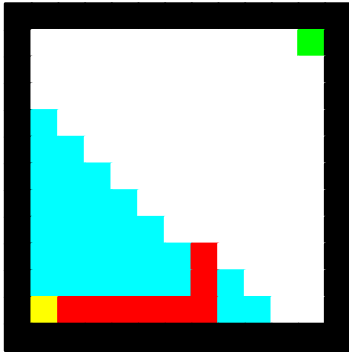




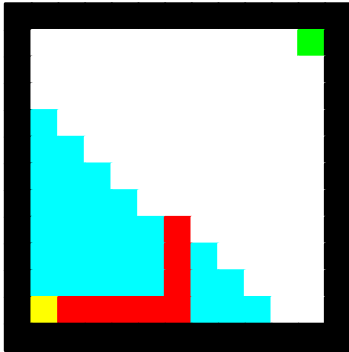
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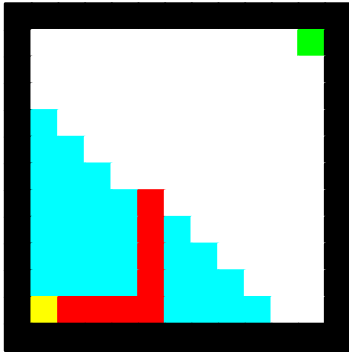
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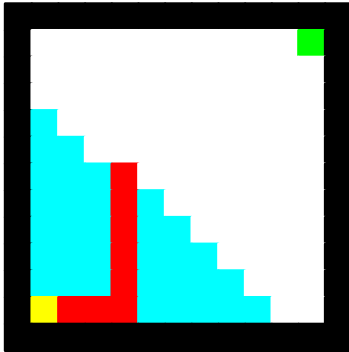
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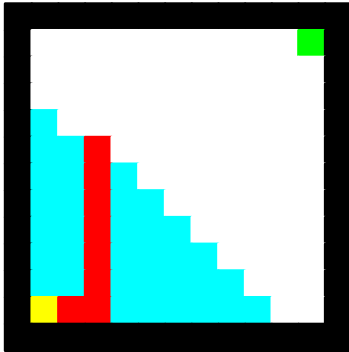
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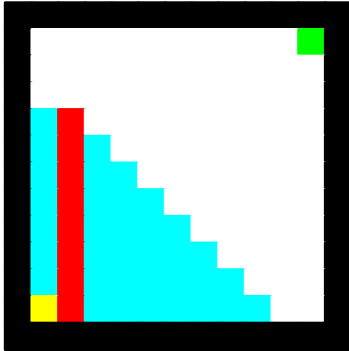


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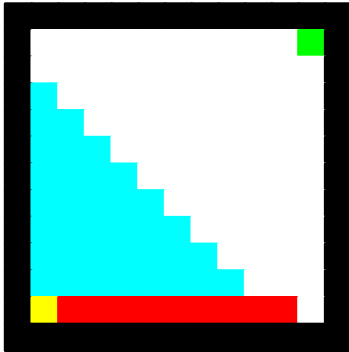


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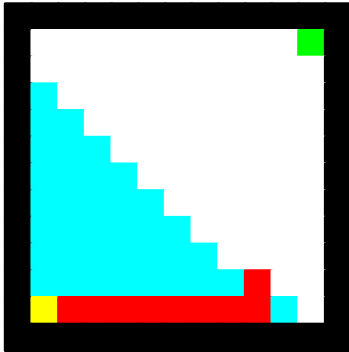


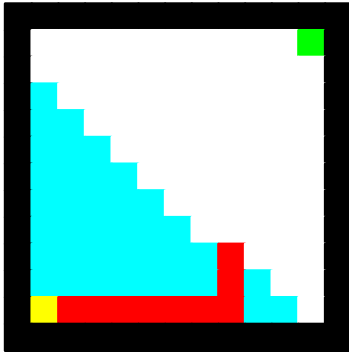


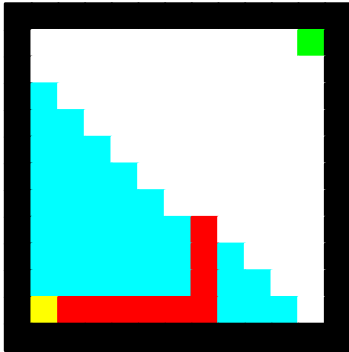
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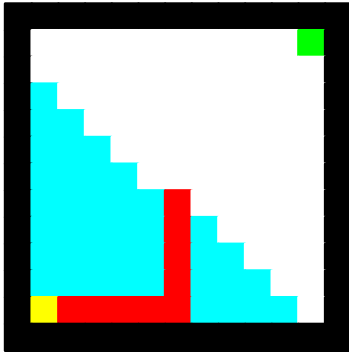


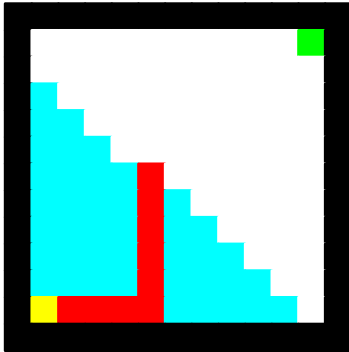
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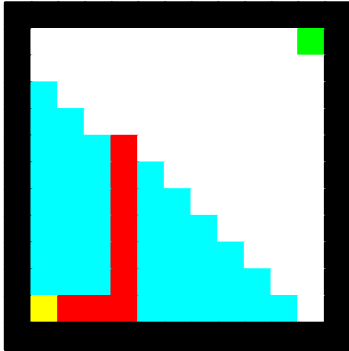




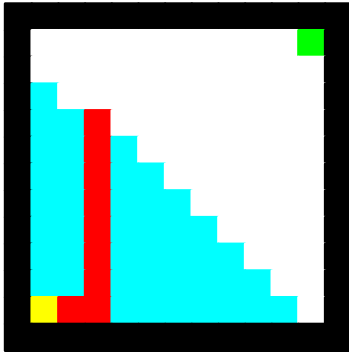


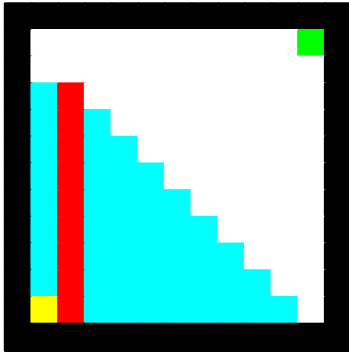


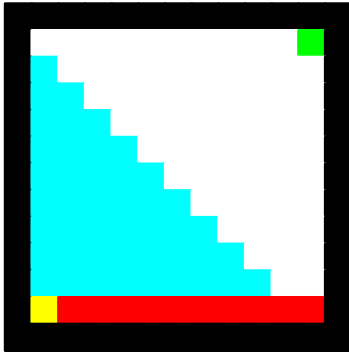


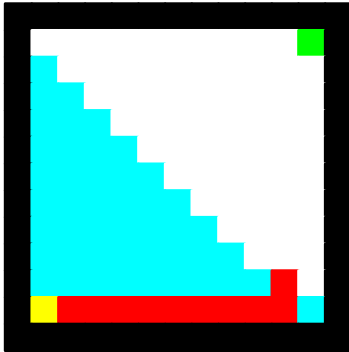


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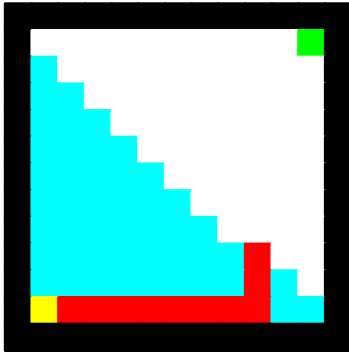




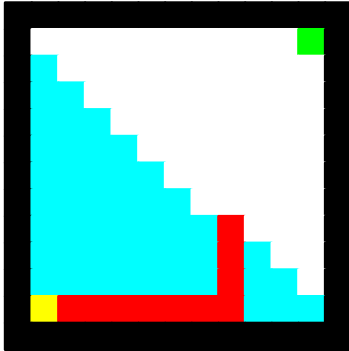


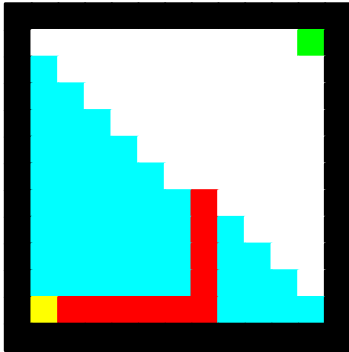


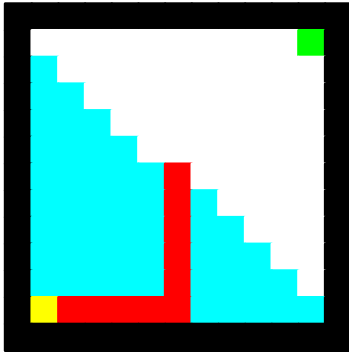
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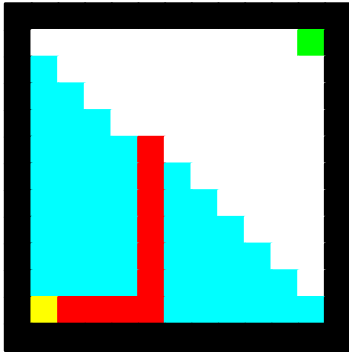


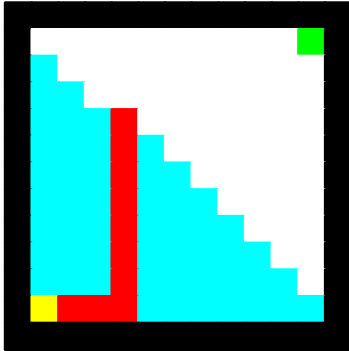
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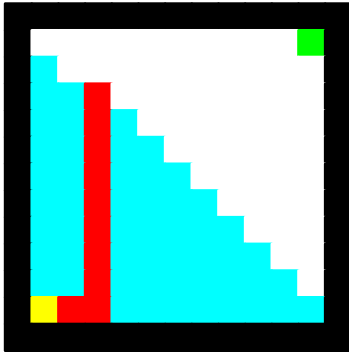


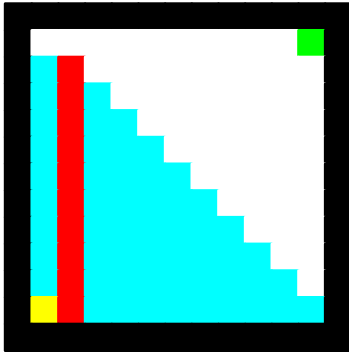




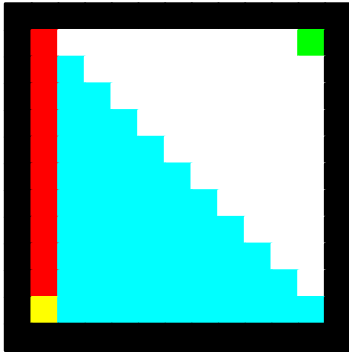


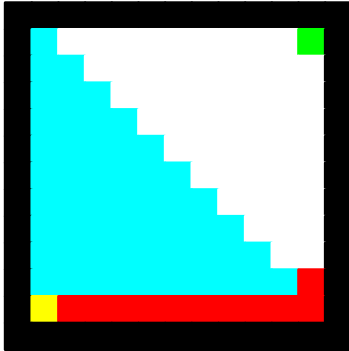




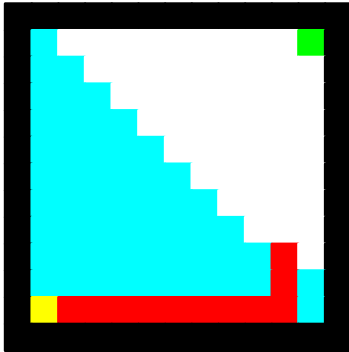


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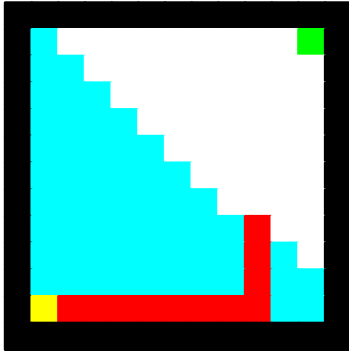




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Grid: BFS 2

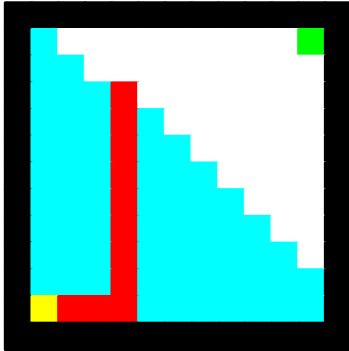


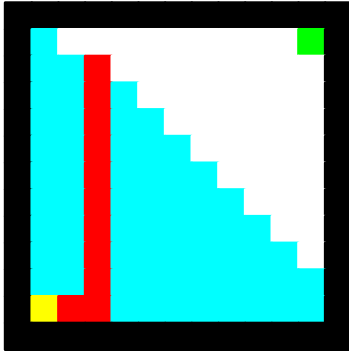
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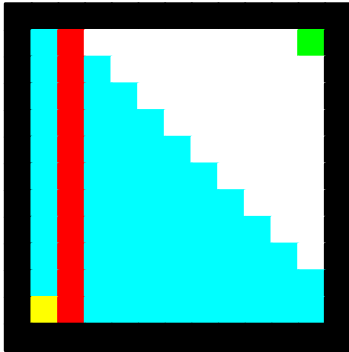
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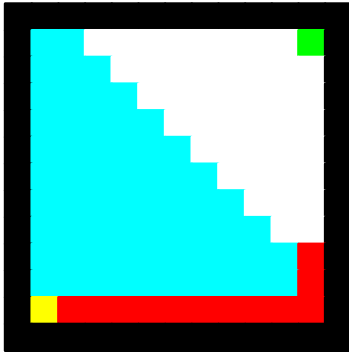




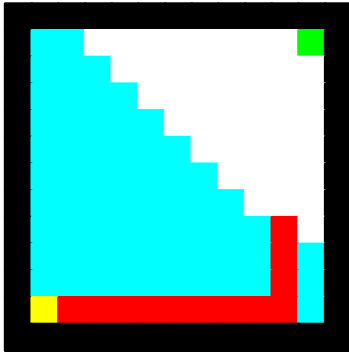
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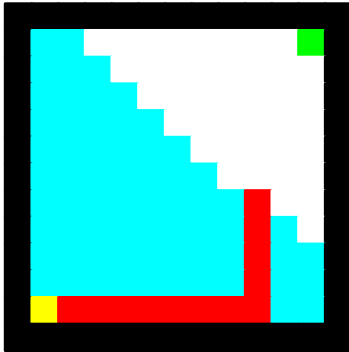
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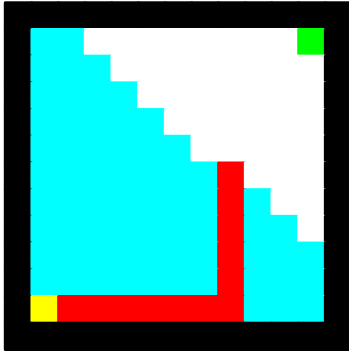


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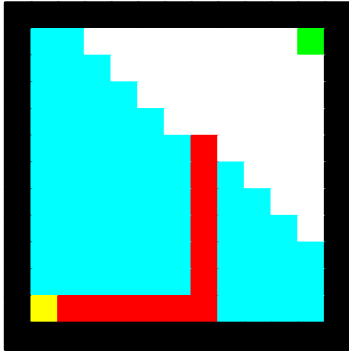


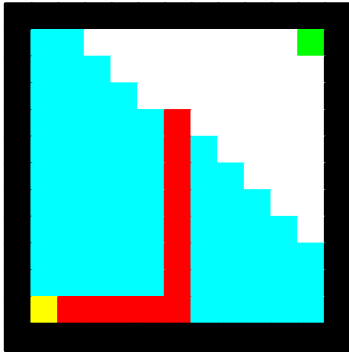
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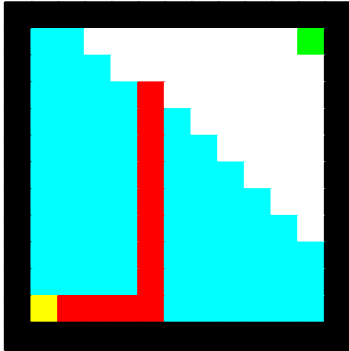




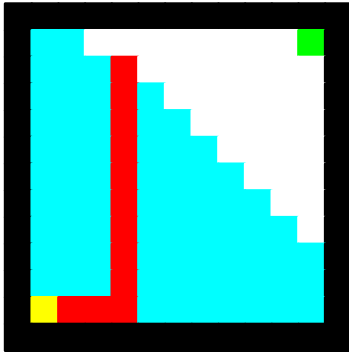
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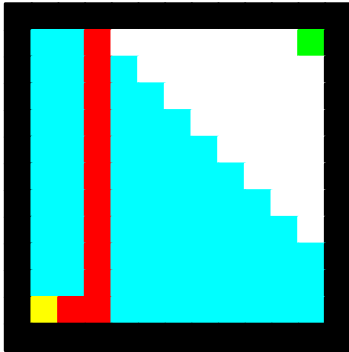




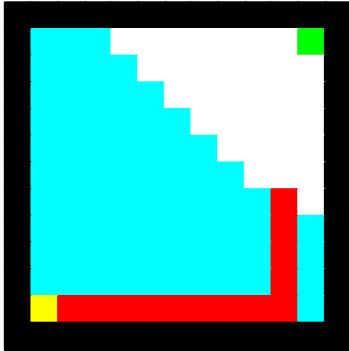
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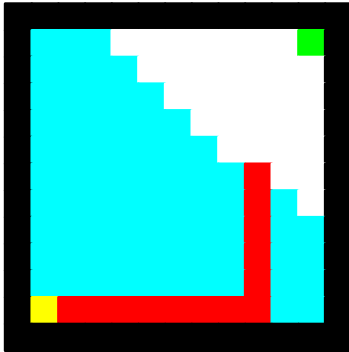


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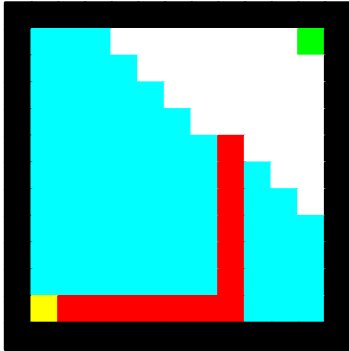


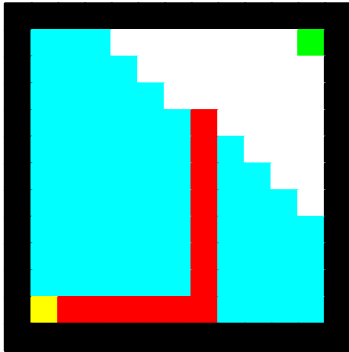
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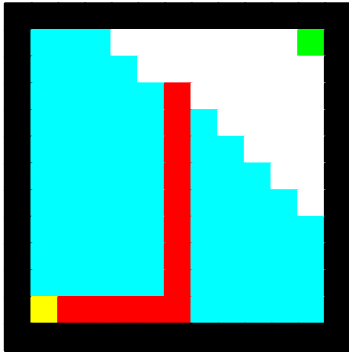


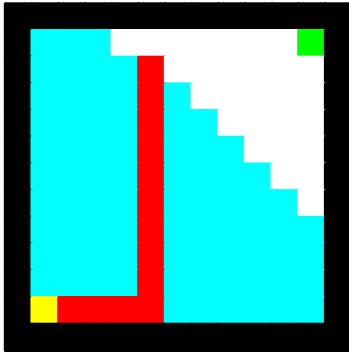
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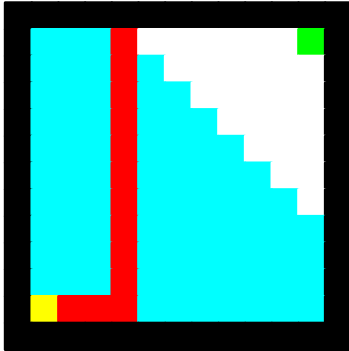




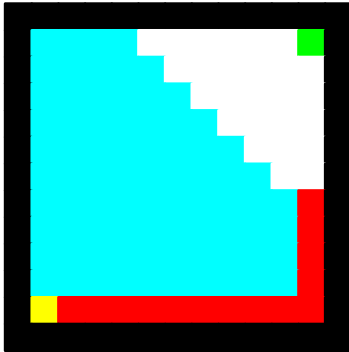
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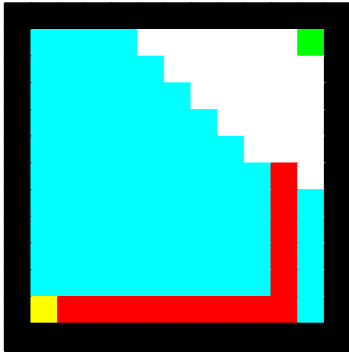




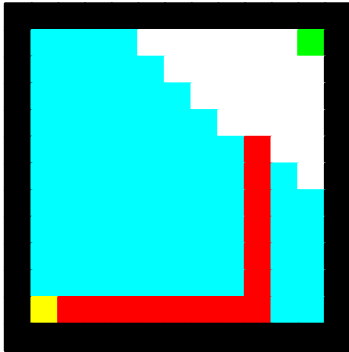
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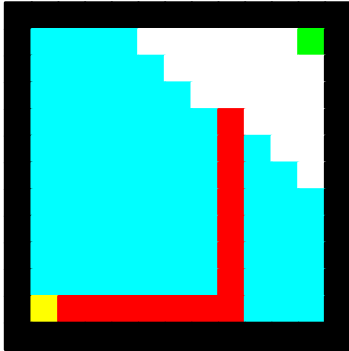
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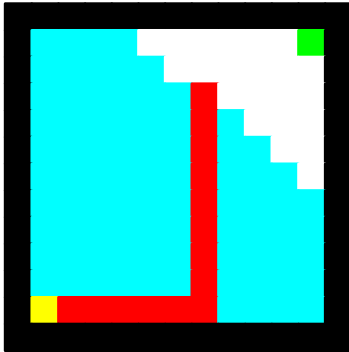


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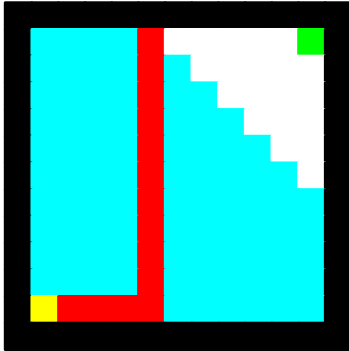


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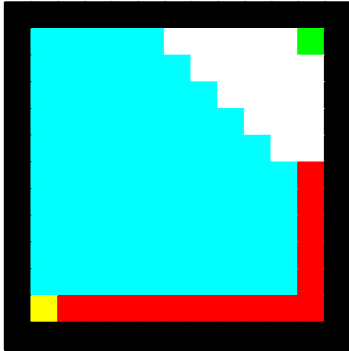




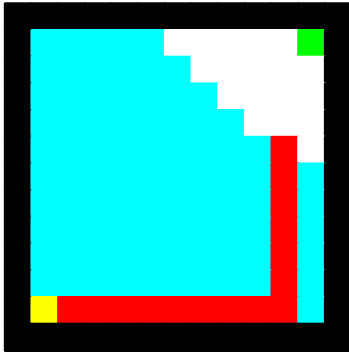
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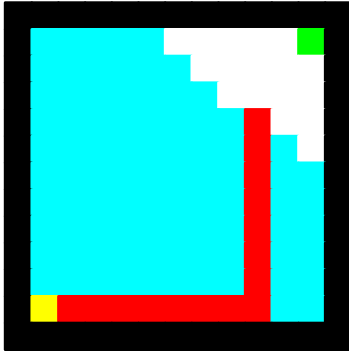


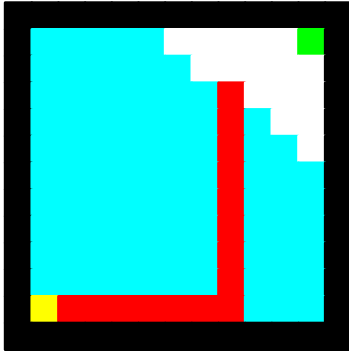
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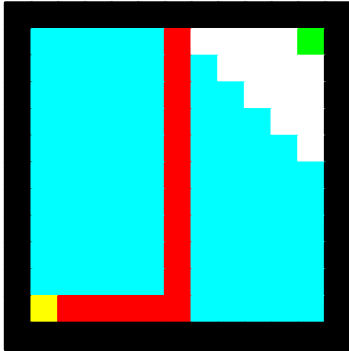
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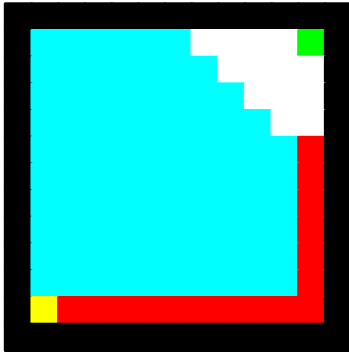




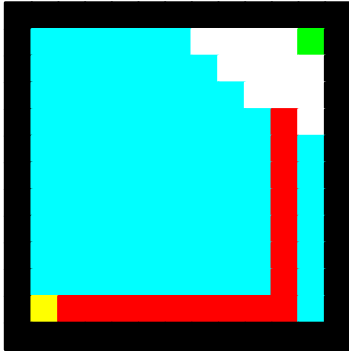
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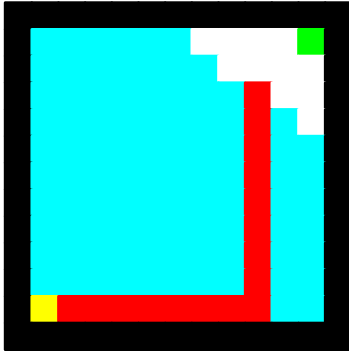
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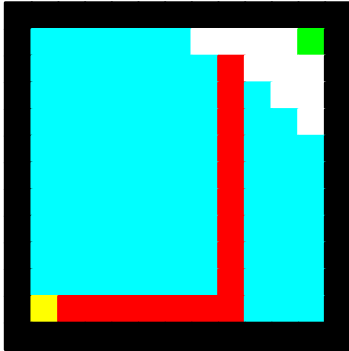
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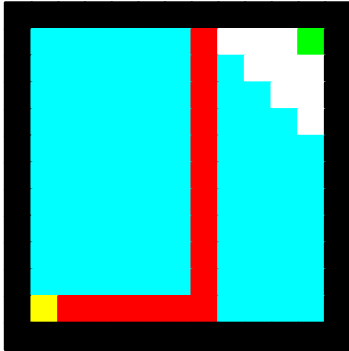
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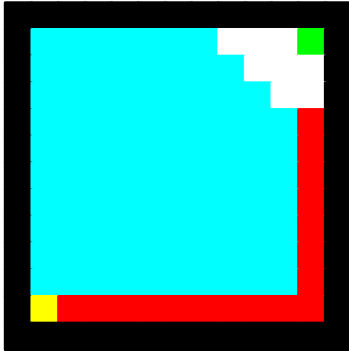


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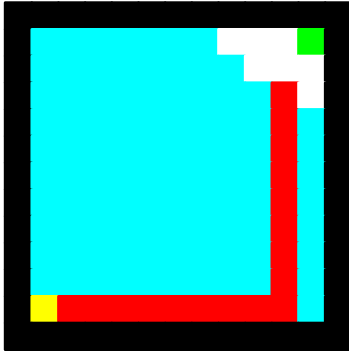


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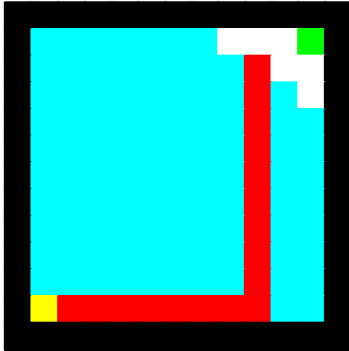




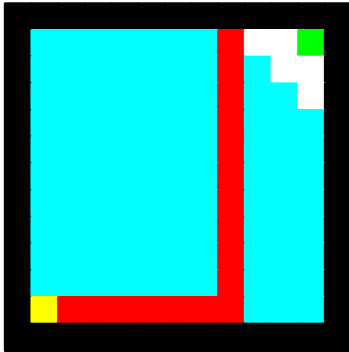
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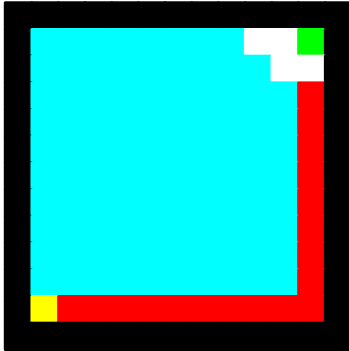
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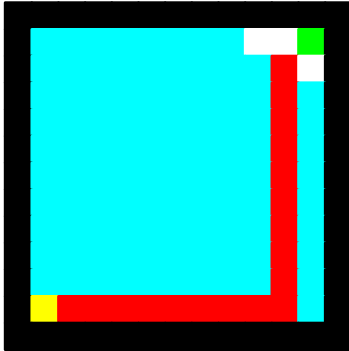
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Grid: BFS 2

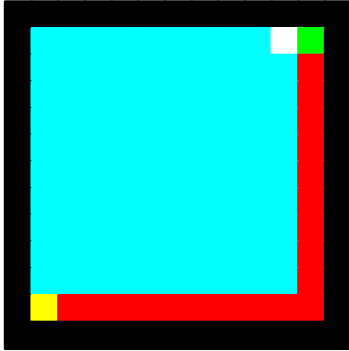


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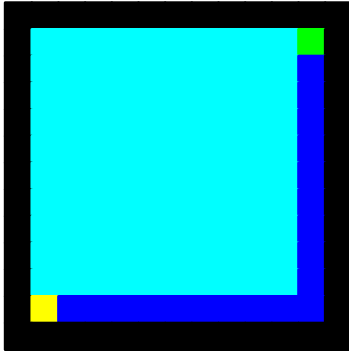


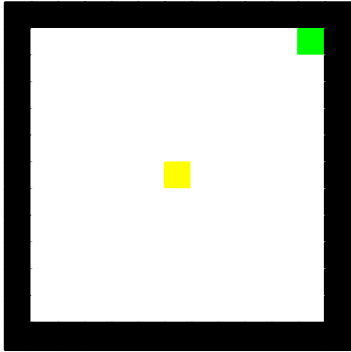
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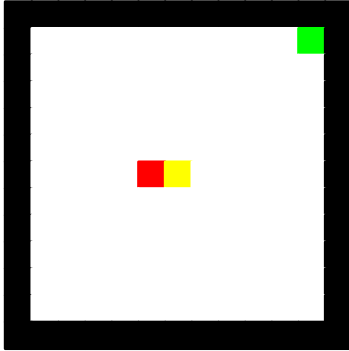
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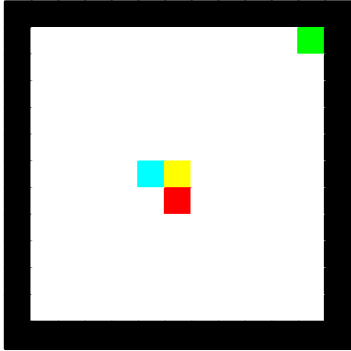


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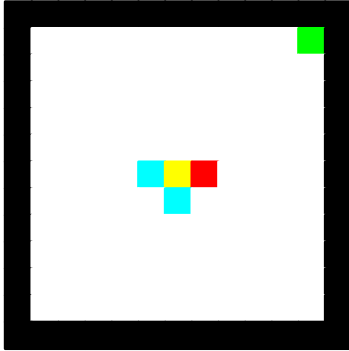


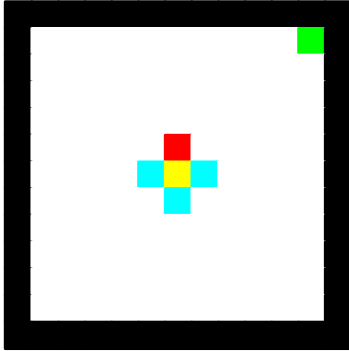


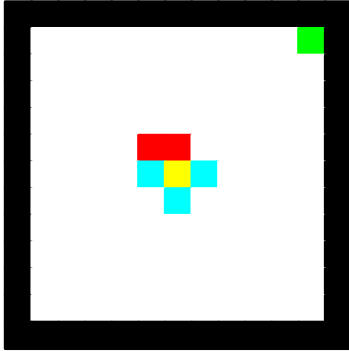


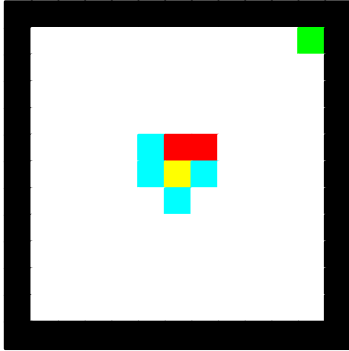


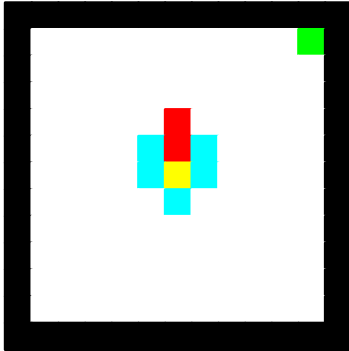
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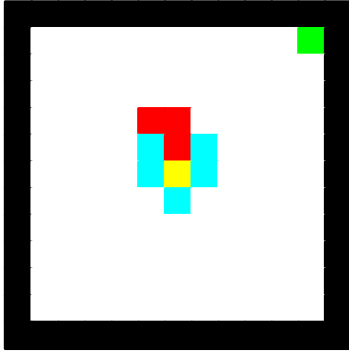


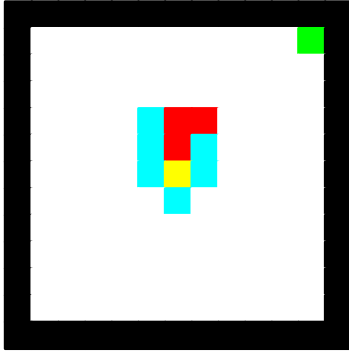


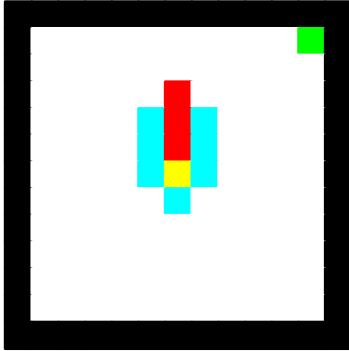


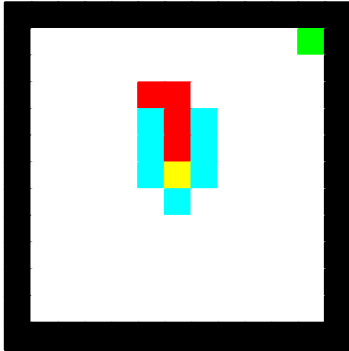


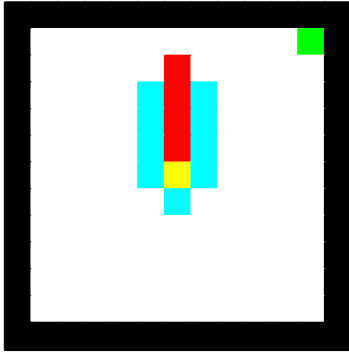


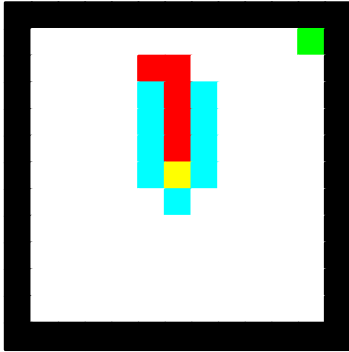


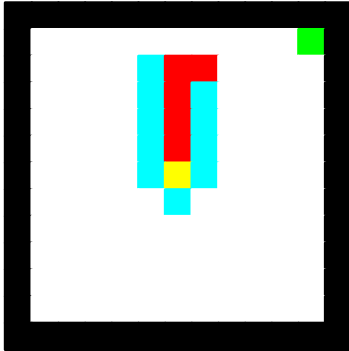


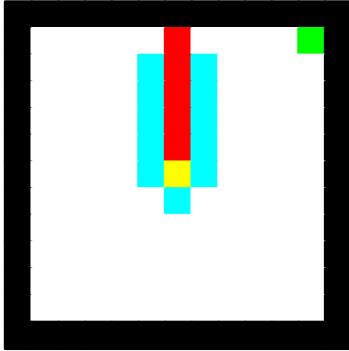


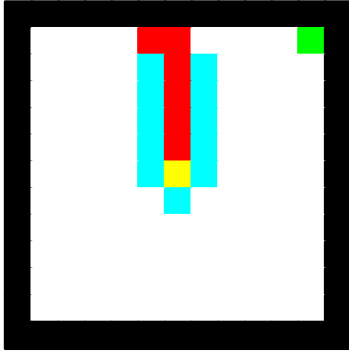


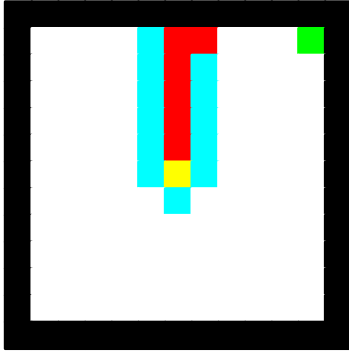


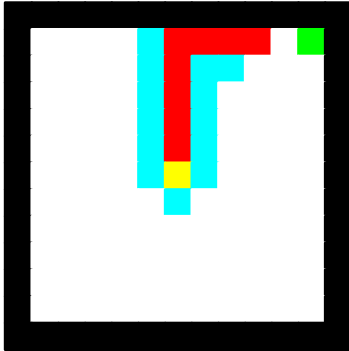


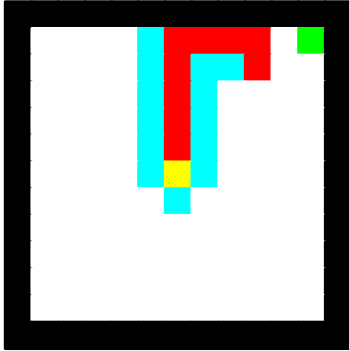


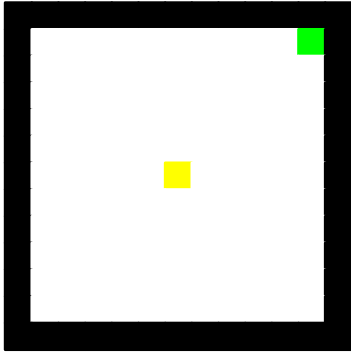


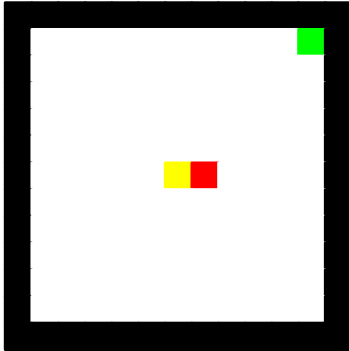


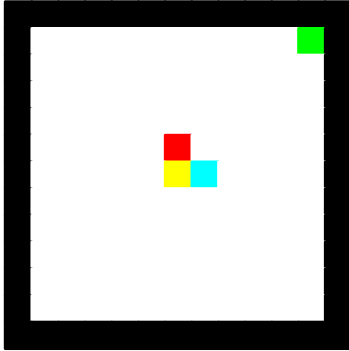


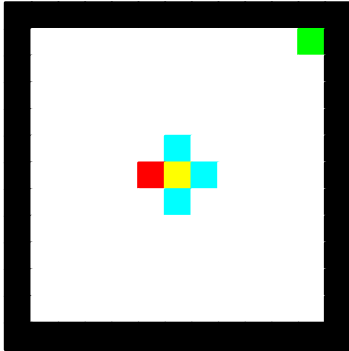


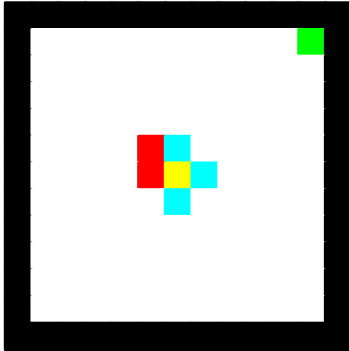


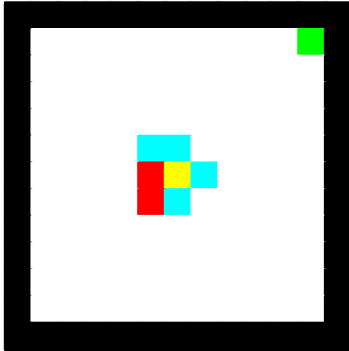


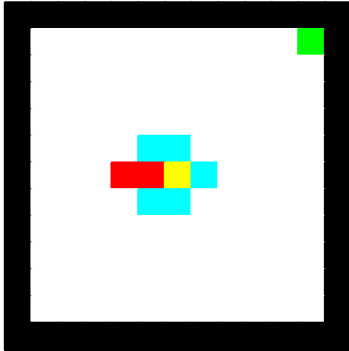


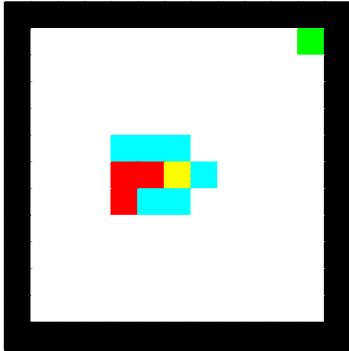


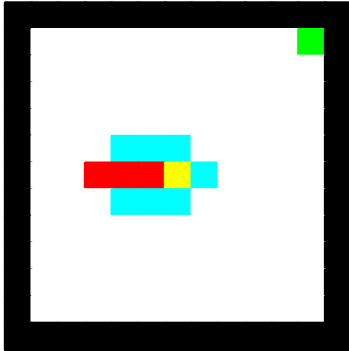


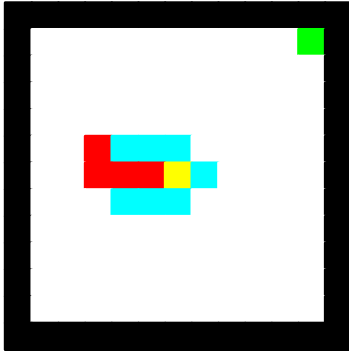


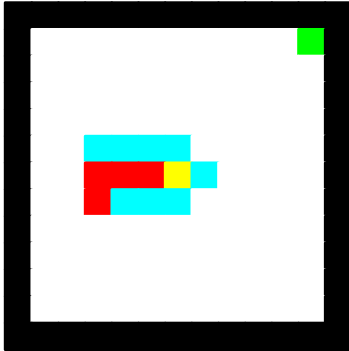


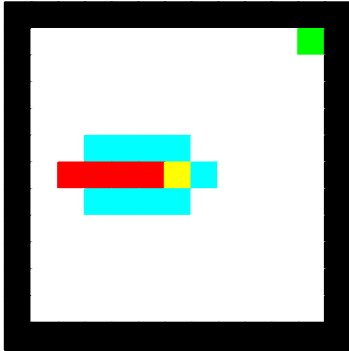


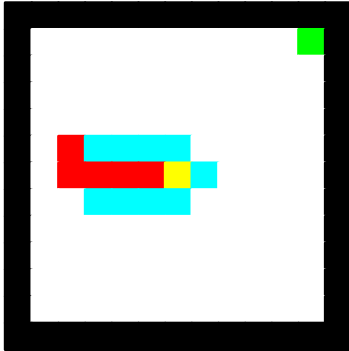


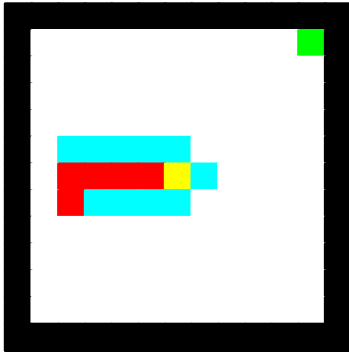


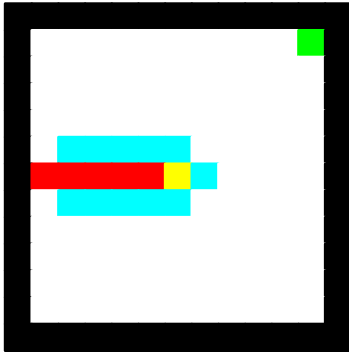


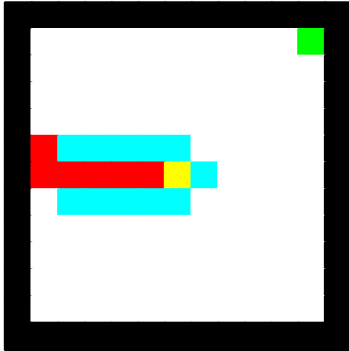


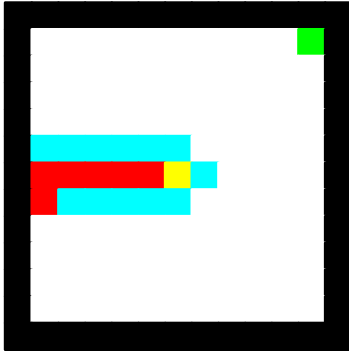


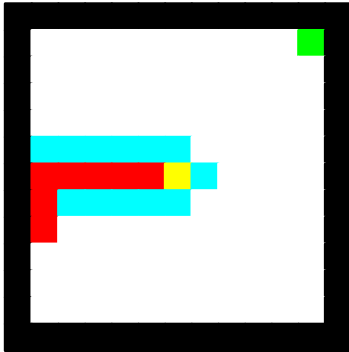


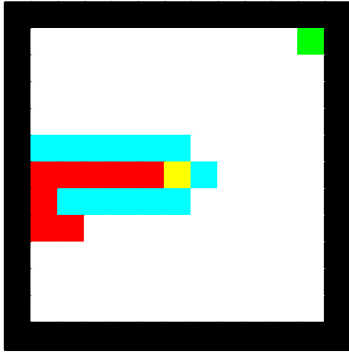


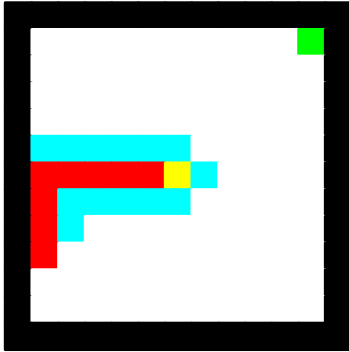


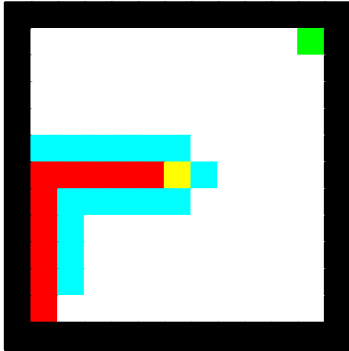


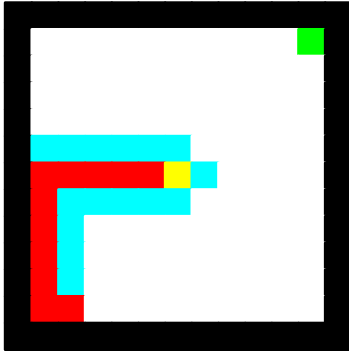


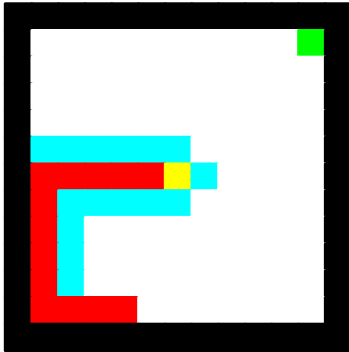


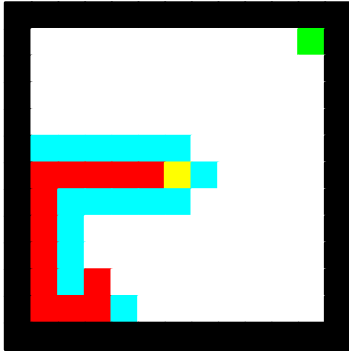


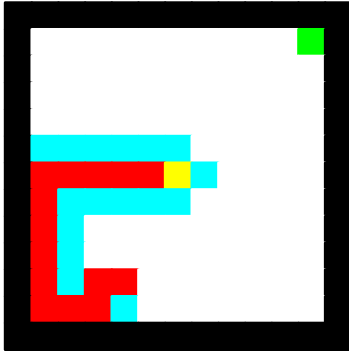


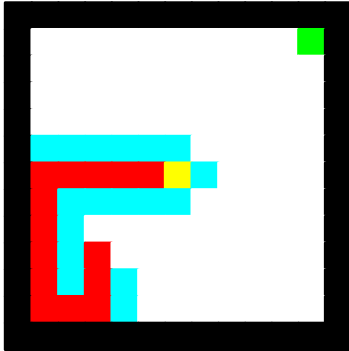


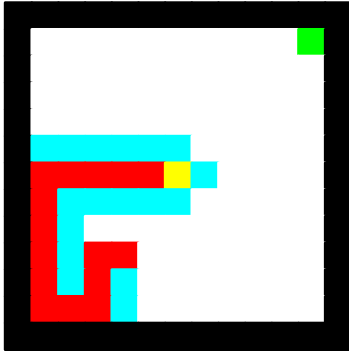


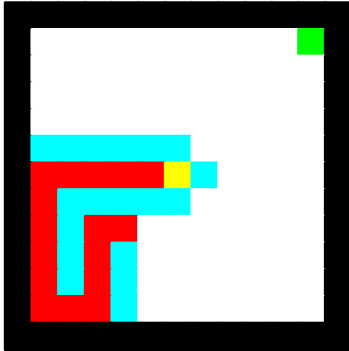


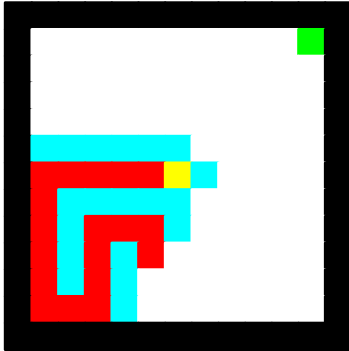


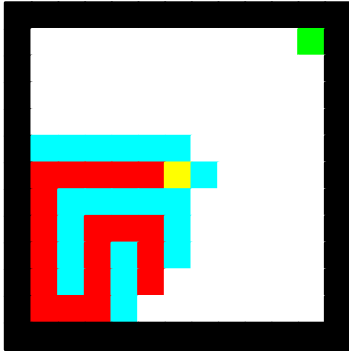


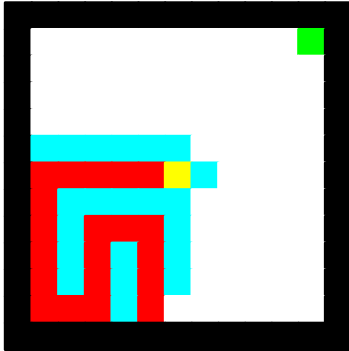


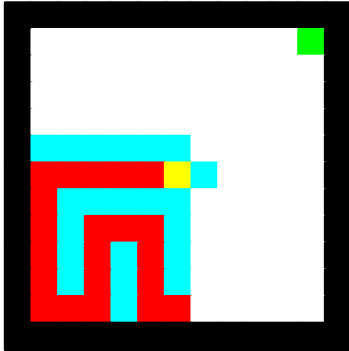


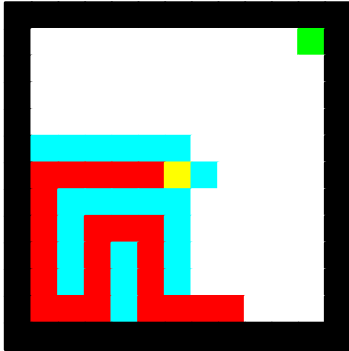


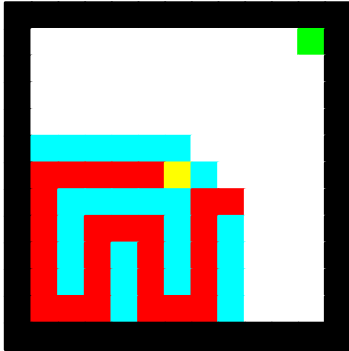


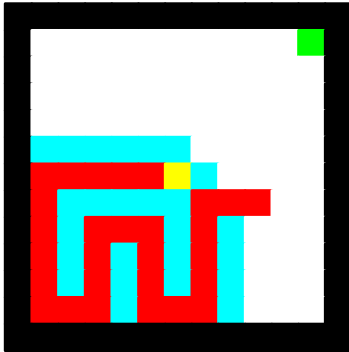


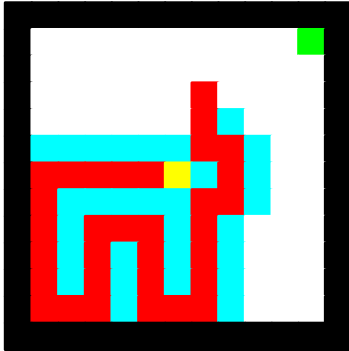


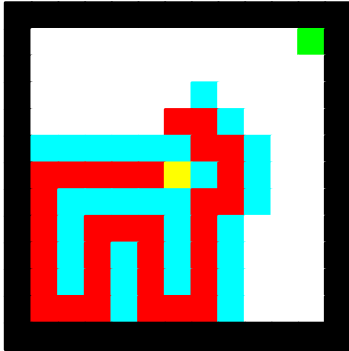


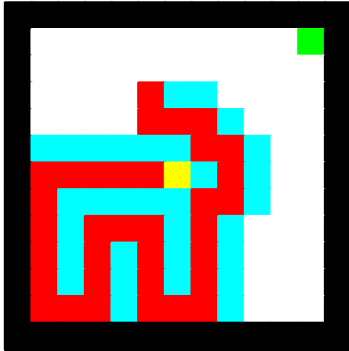


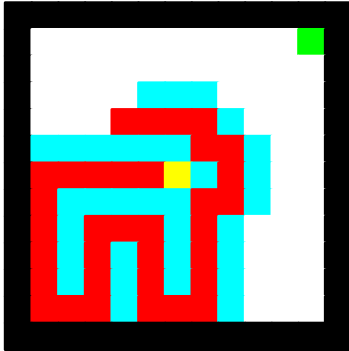


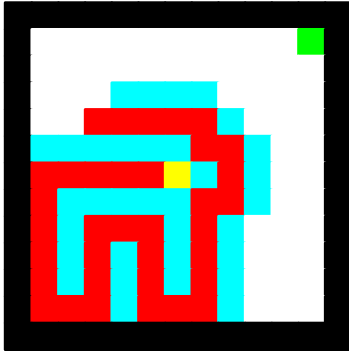


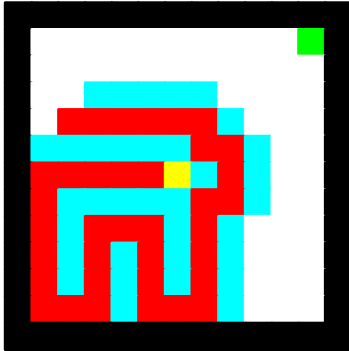


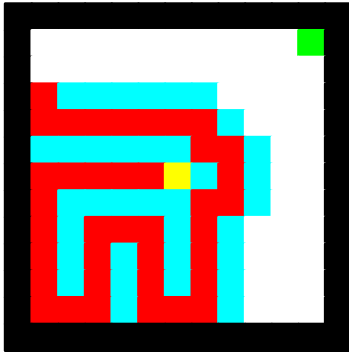


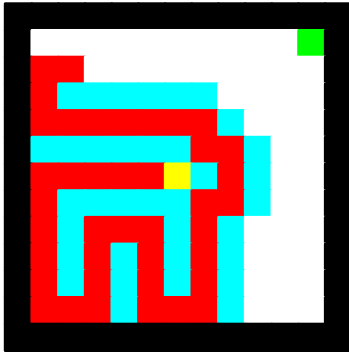


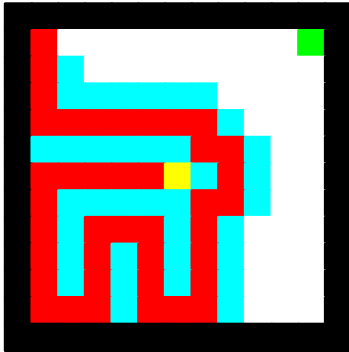


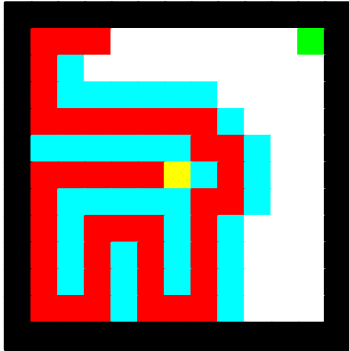


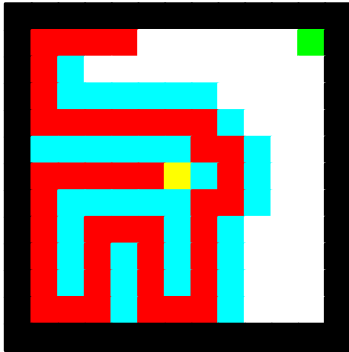


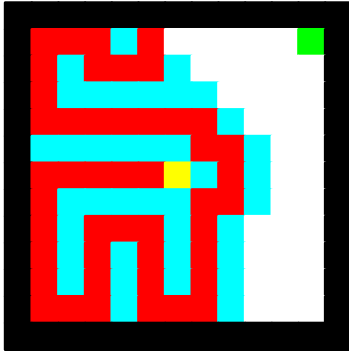


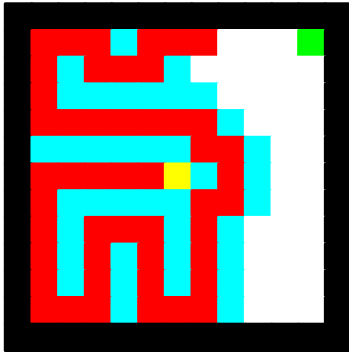


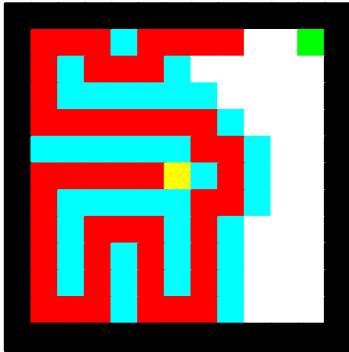


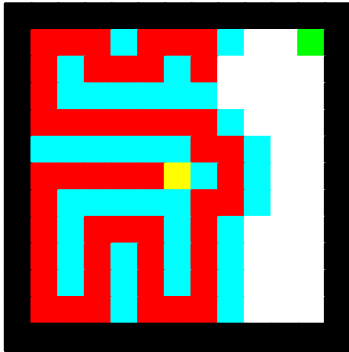


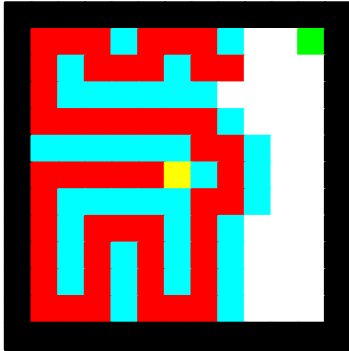


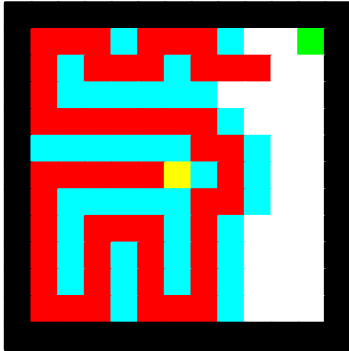


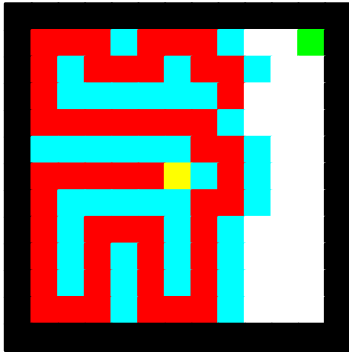


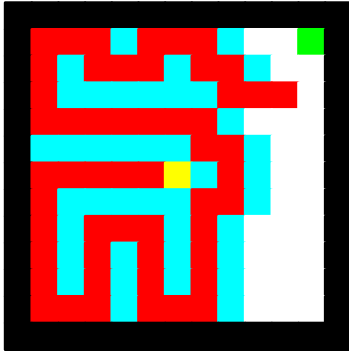


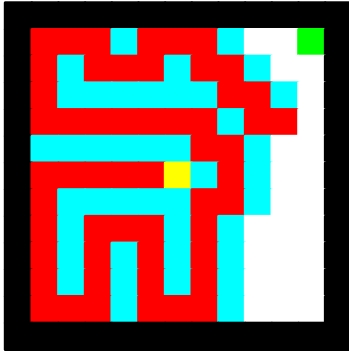


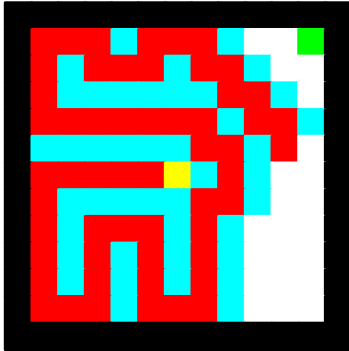


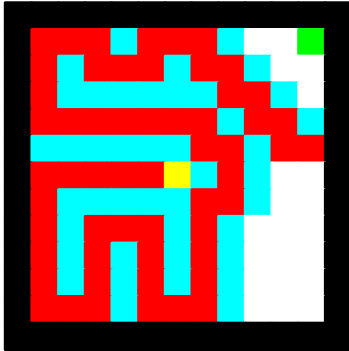


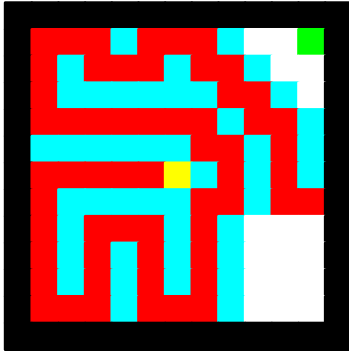


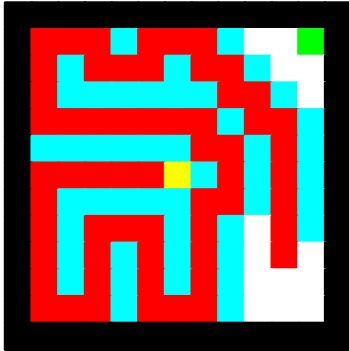


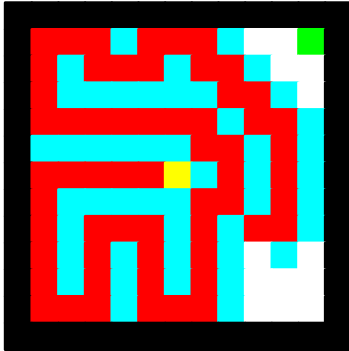


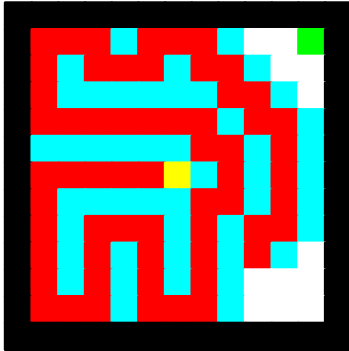


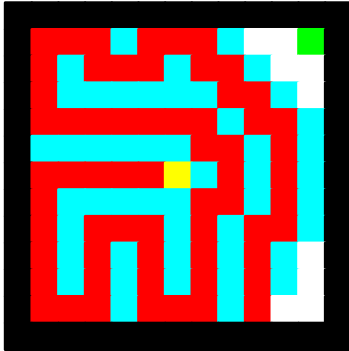


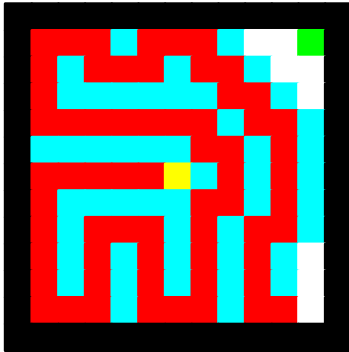


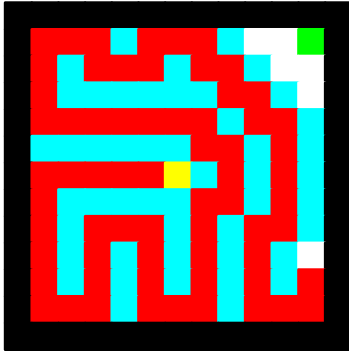


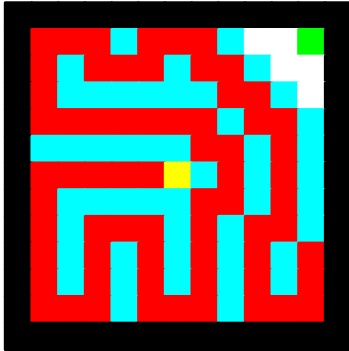












More Examples

Properties of BFS/DFS

BFS

- Always returns a shortest path to a goal vertex, if a goal vertex exists in the set of vertices reachable from the start vertex.
- May run forever in an infinite domain if there is no solution.
- Generally requires more memory than depth-first search.

DFS

- Always returns **a** path to a goal vertex, if a goal vertex exists in the set of vertices reachable from the start vertex **and the search domain is finite**.
- May run forever in an infinite domain.
- Doesn't necessarily find the shortest path.
- Efficient in the amount of space it requires to store the agenda.

16 Lines!

```
def search(successors, start_vertex, goal_test, dfs=False):
    if goal_test(start_vertex):
        return [start_vertex]
    else:
        agenda = [(start_vertex, None)]
        visited = {start_vertex}
        while len(agenda) > 0:
            parent_path = agenda.pop(-1 if dfs else 0)
            for child_vertex in successors(parent_path[0]):
                child_path = (child_vertex, parent)
                if goal_test(child_vertex):
                    return flatten_path(child)
                if child_vertex not in visited:
                    agenda.append(child)
                    visited.add(child_vertex)
        return None
```


Today: Adding Costs

BFS is guaranteed always to return the shortest possible path (in terms of total number of edges traversed) to the goal.

Suppose that some edges are more beneficial than others to traverse, though. BFS's sense of optimality does not take that information into account.

Today, we'll develop a new algorithm that takes into account a sense of how desirable each edge is.

What is a Graph?

Set V of vertices (or "states")

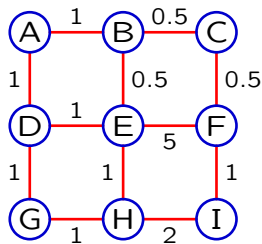
Set E of edges connecting vertices

Set W of edge costs (or "weights")

New goal: rather than finding the *shortest* path, we want to find a path with minimum total *cost*

Example

Find path $E \rightarrow I$, minimizing total cost



Uniform-Cost Search

Consider searching for **least-cost** paths instead of *shortest* paths. Instead of popping from agenda based on when nodes were added, pop based on of the cost of the paths they represent.

By considering paths in order of increasing cost, we guarantee that we return a path to the goal that has minimal cost.

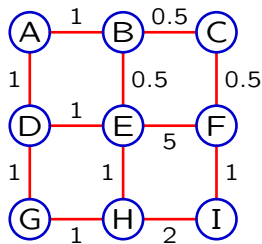
Uniform-Cost Search

Uniform Cost Search:

- Initialize **expanded set**
 - Initialize agenda (list of paths to consider)
 - Repeat the following:
 - Remove one path from the agenda
 - **If its terminal vertex is in the expanded set, ignore it.**
 - **If its terminal vertex satisfies the goal condition, return a path.**
 - **Add its terminal vertex to the expanded set**
 - Add each child to the agenda if its terminal vertex is **not already in the expanded set** itemize
- until **goal is found** or **agenda is empty**

Example

Find path $E \rightarrow I$, minimizing total cost



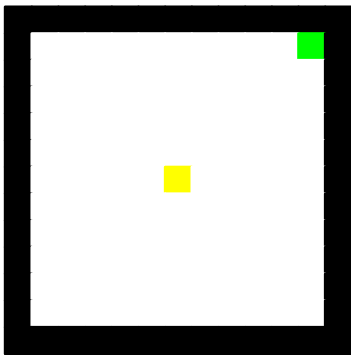
More Examples

More Examples

Problem?

So far, our searches have radiated outward from the starting point.

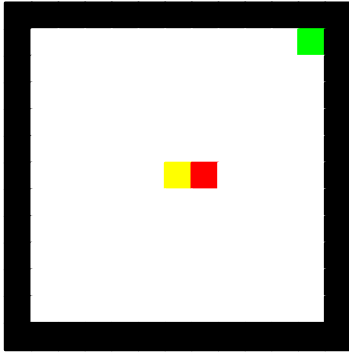
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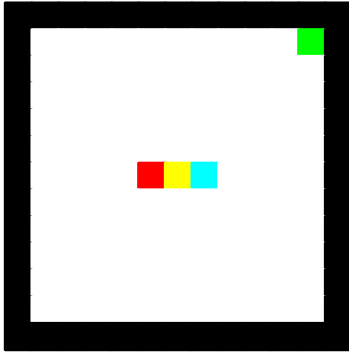
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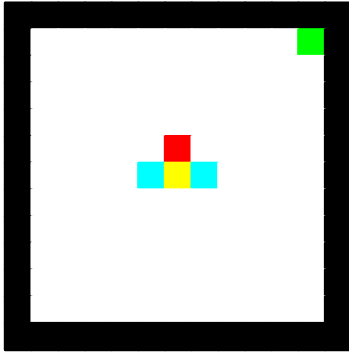
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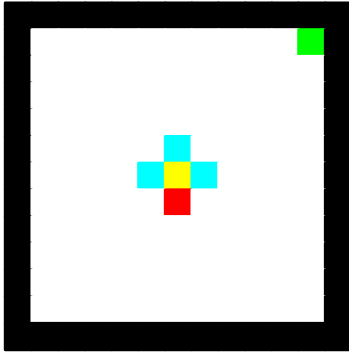
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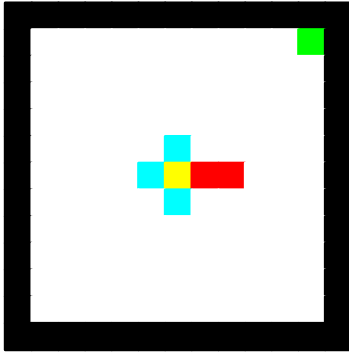
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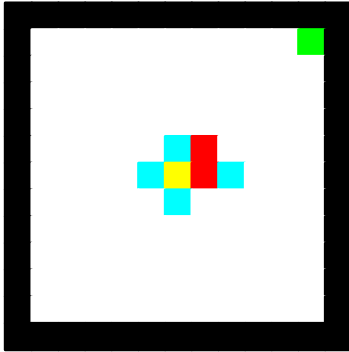
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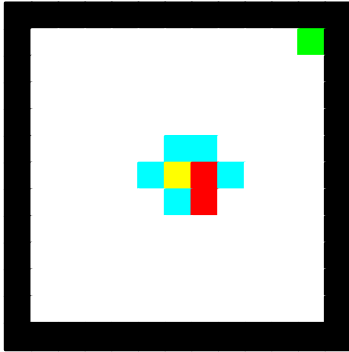
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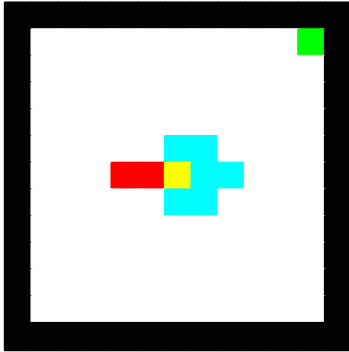
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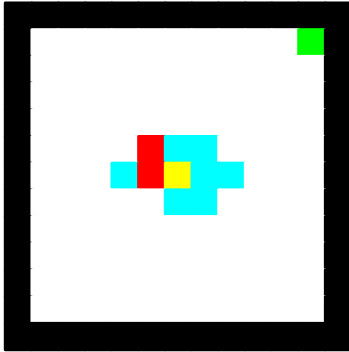
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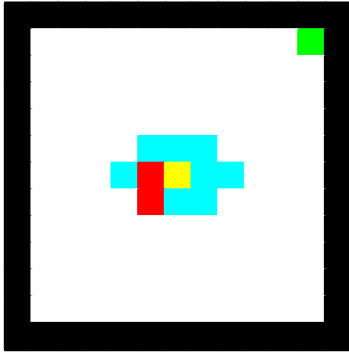
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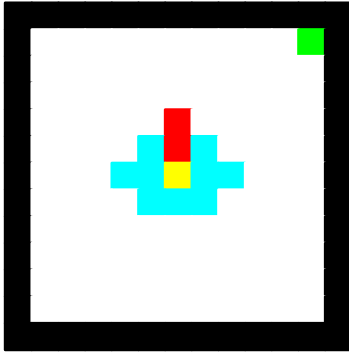
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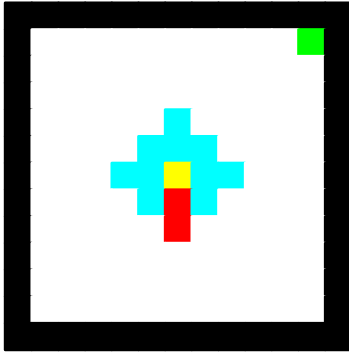
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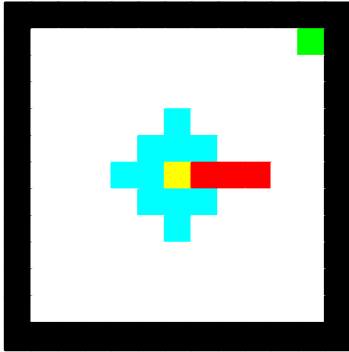
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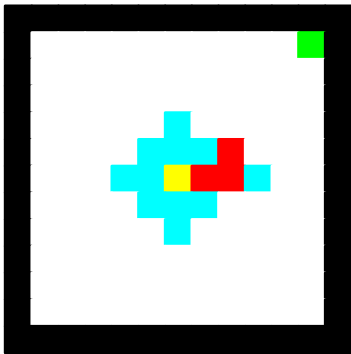
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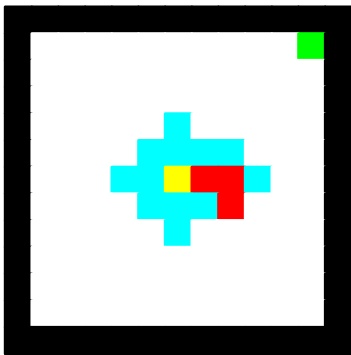
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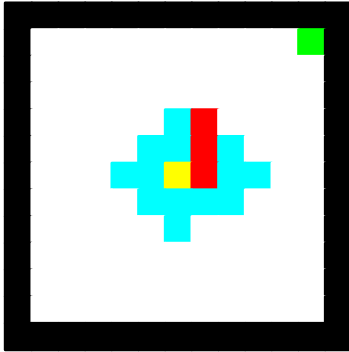
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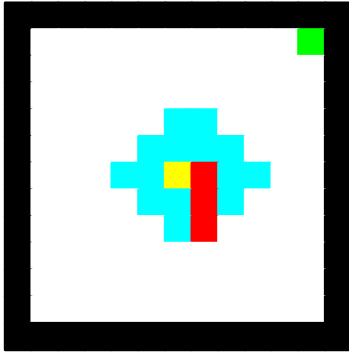
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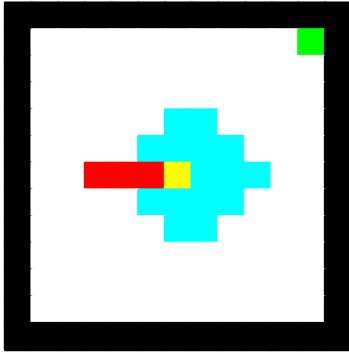
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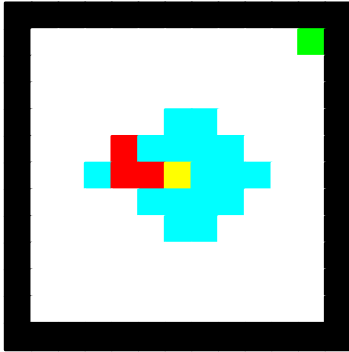
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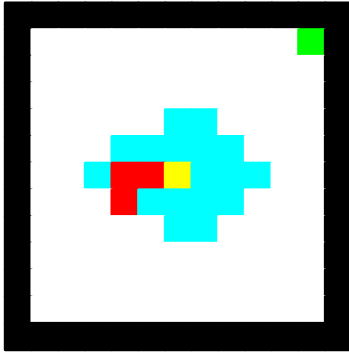
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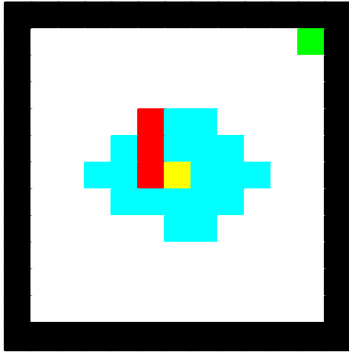
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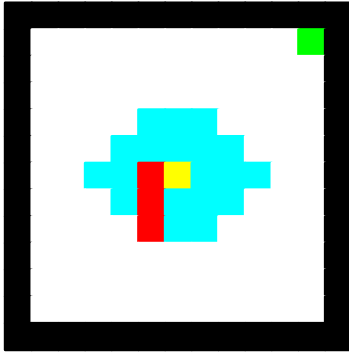
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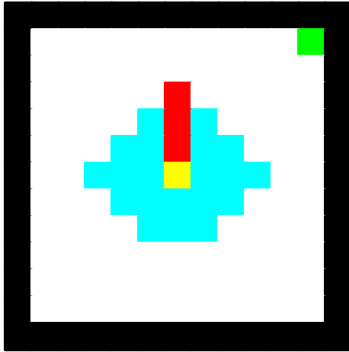
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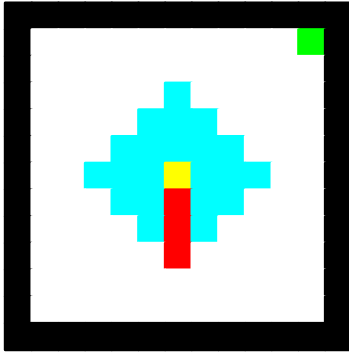
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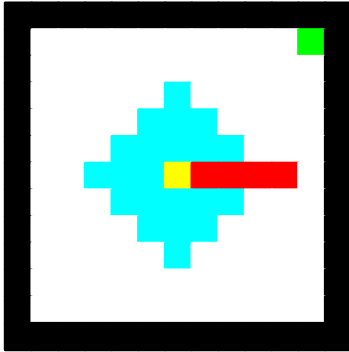
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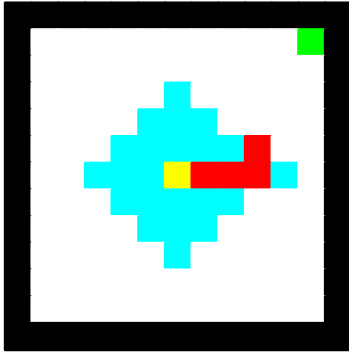
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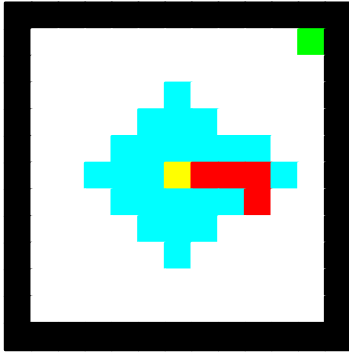
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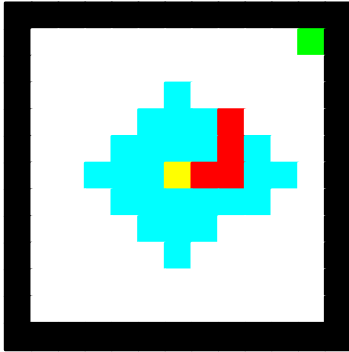
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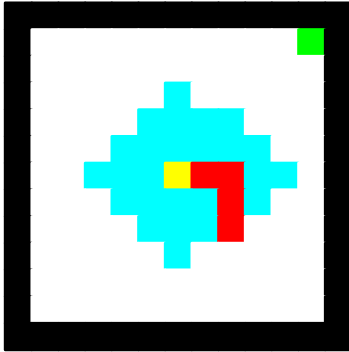
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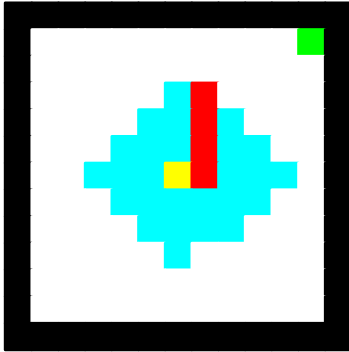
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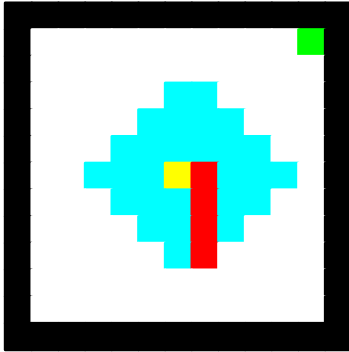
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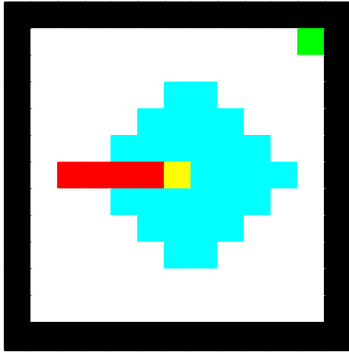
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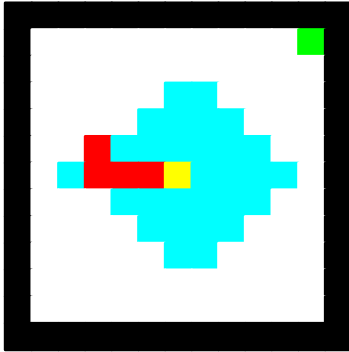
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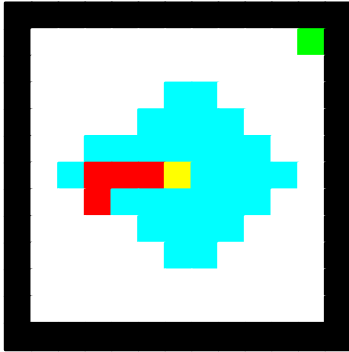
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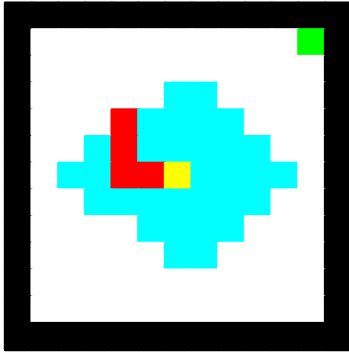
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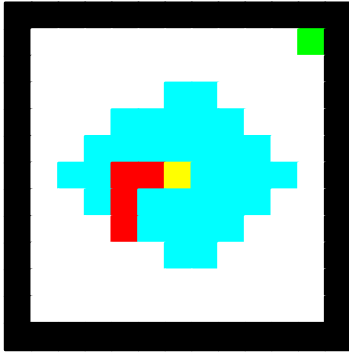
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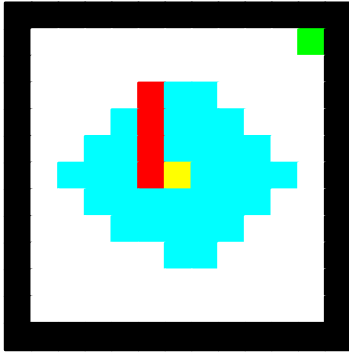
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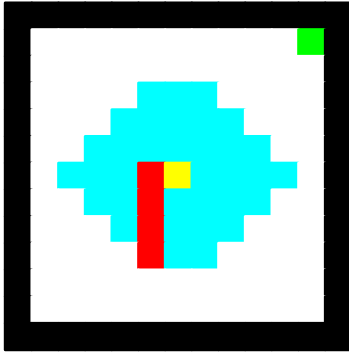
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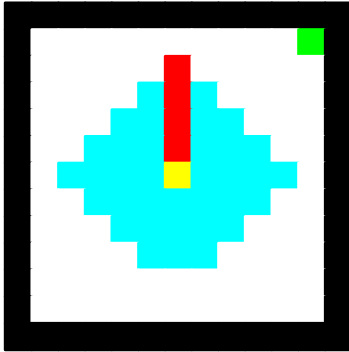
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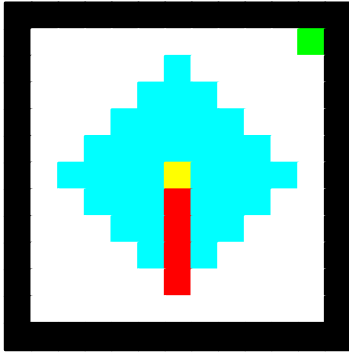
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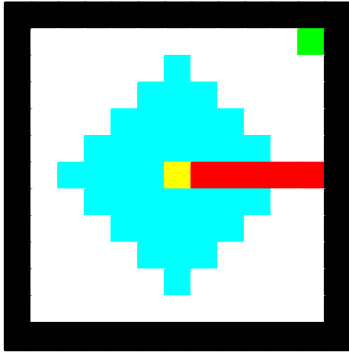
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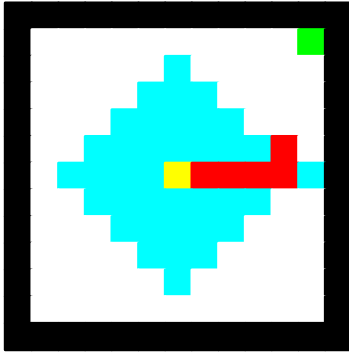
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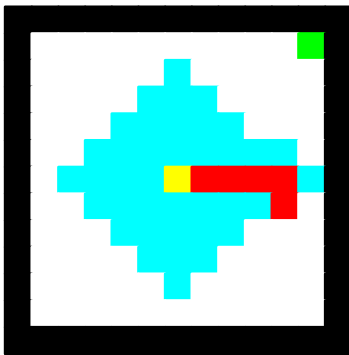
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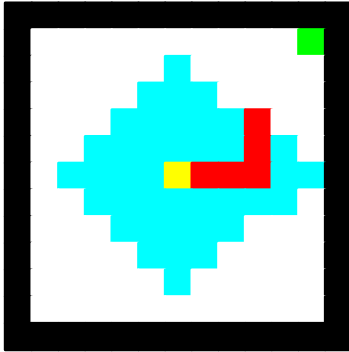
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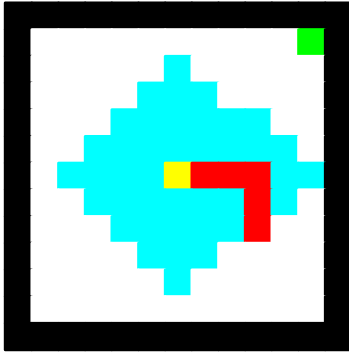
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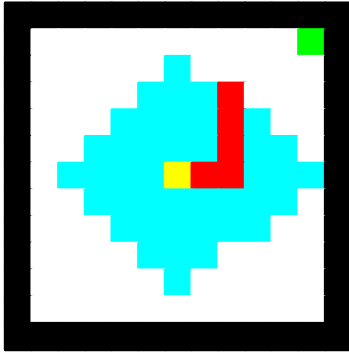
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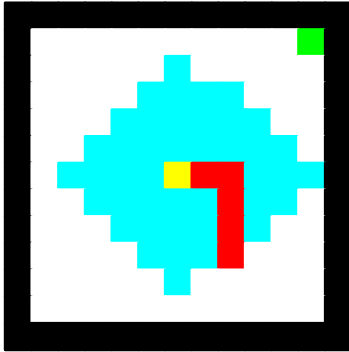
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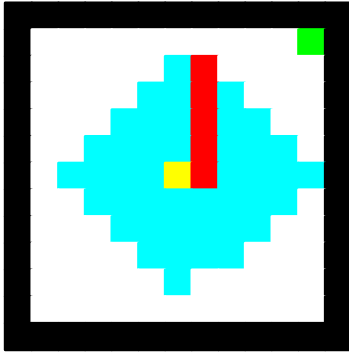
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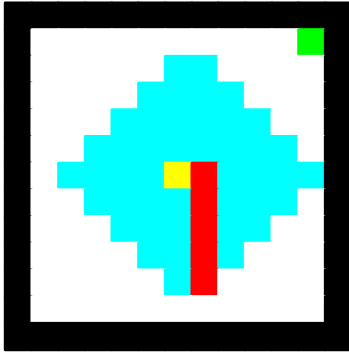
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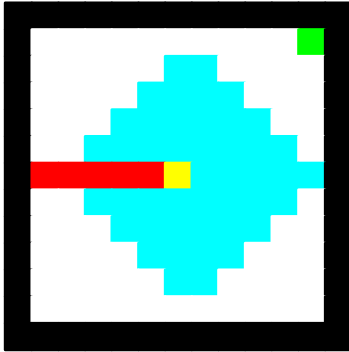
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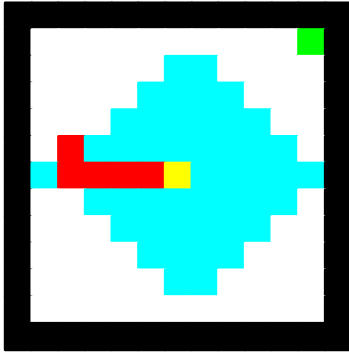
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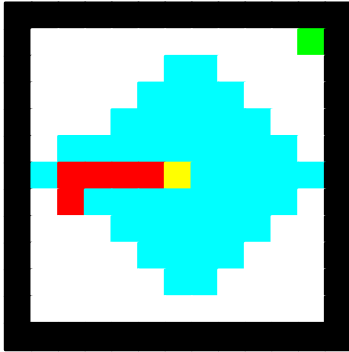
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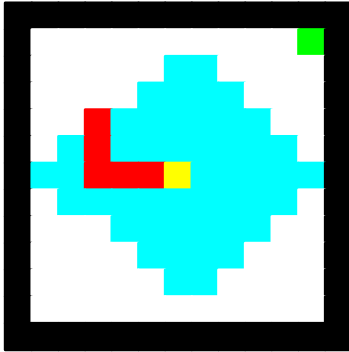
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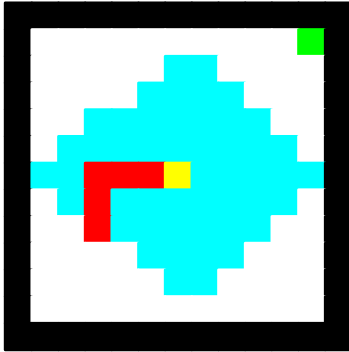
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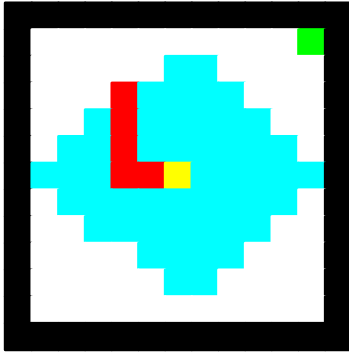
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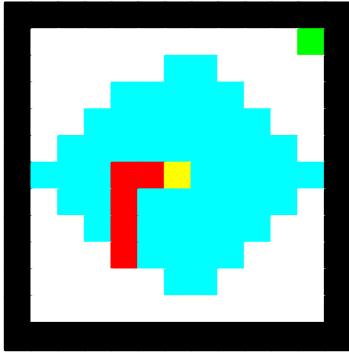
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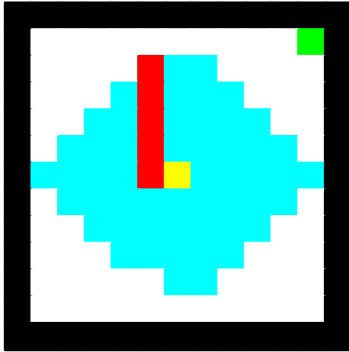
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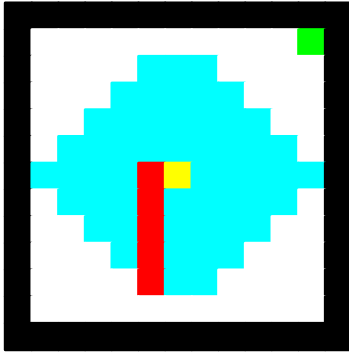
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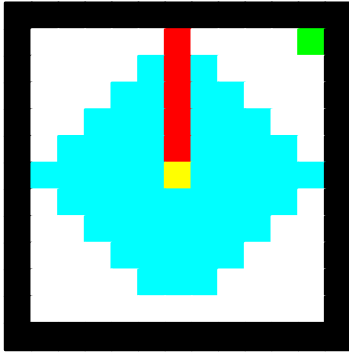
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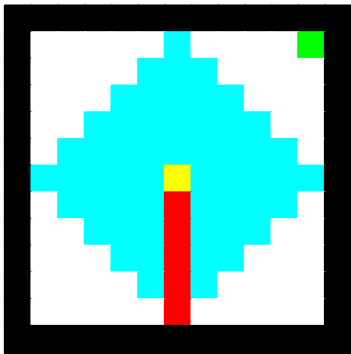
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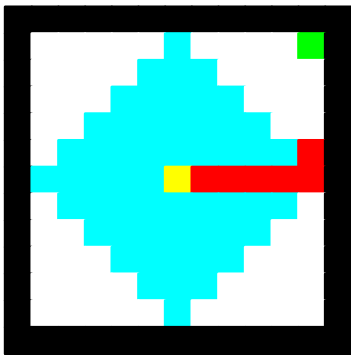
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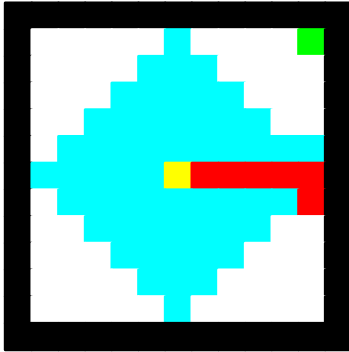
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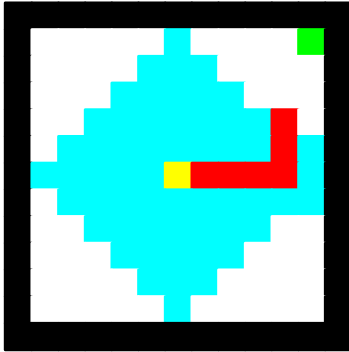
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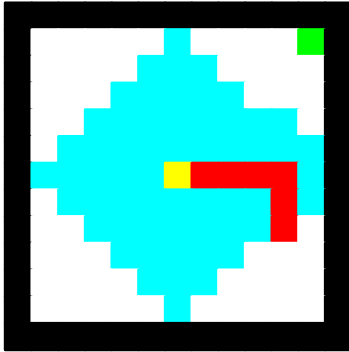
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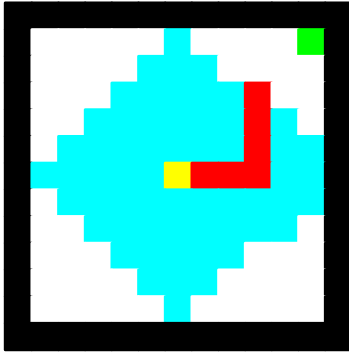
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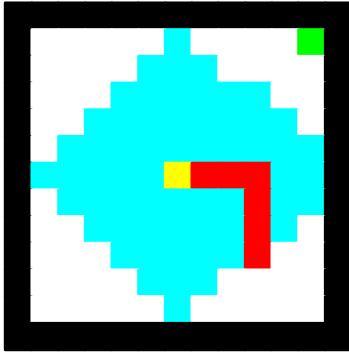
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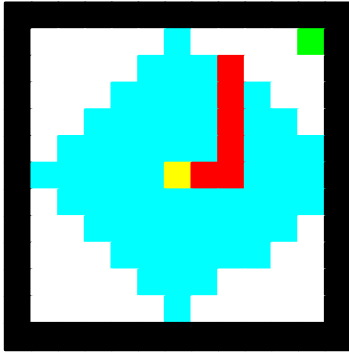
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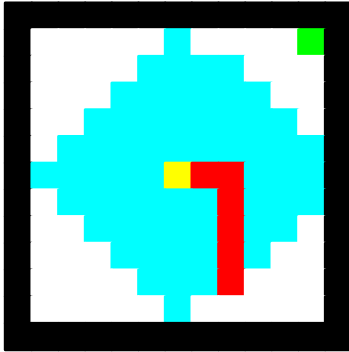
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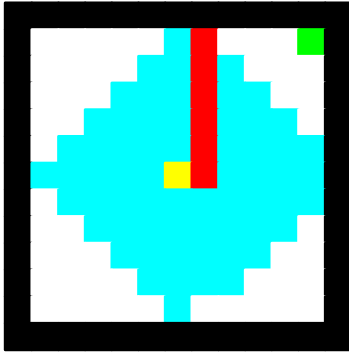
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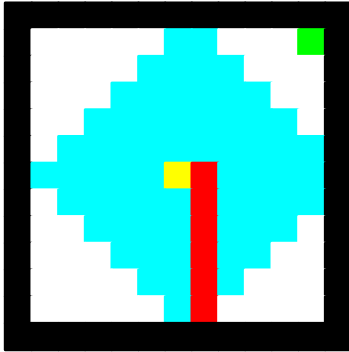
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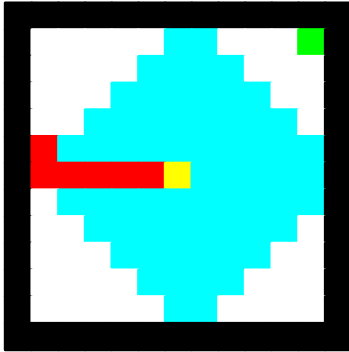
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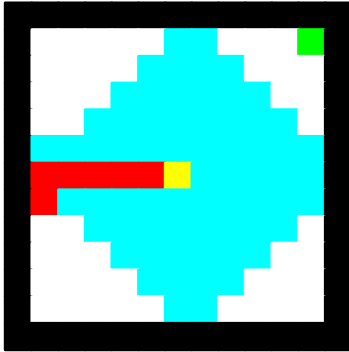
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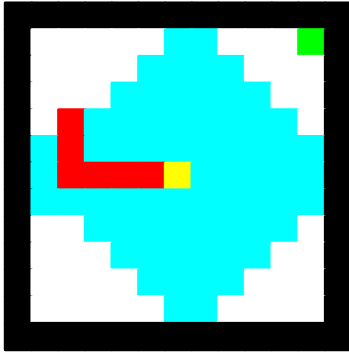
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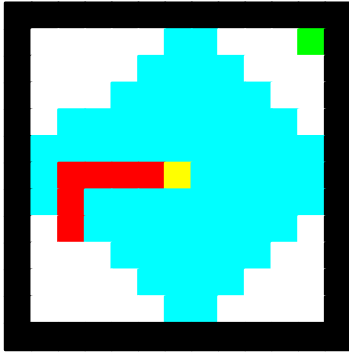
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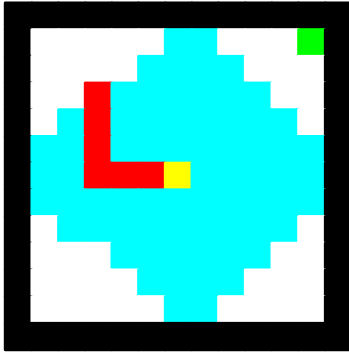
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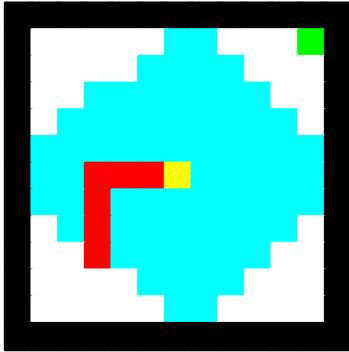
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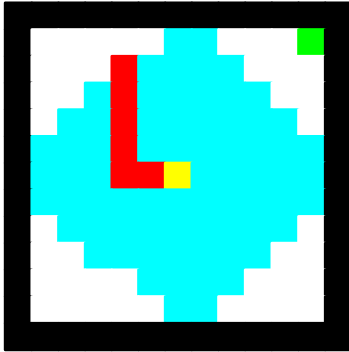
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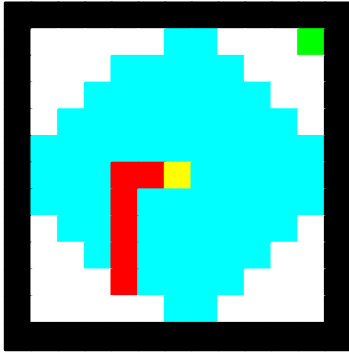
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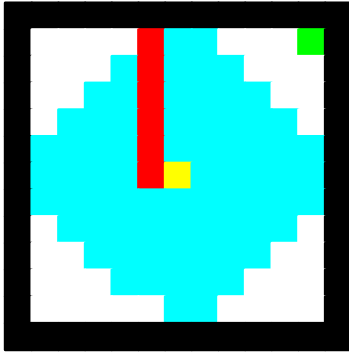
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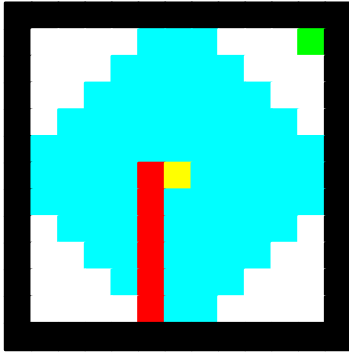
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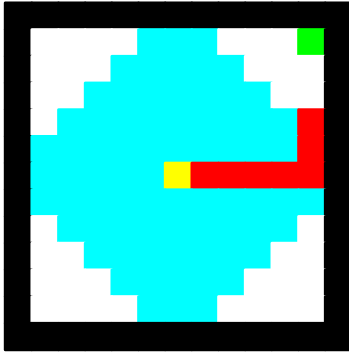
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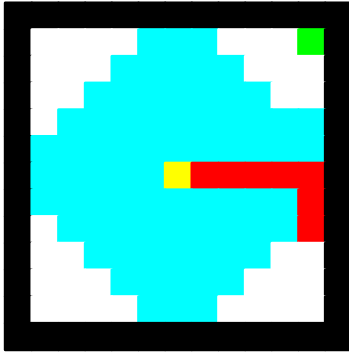
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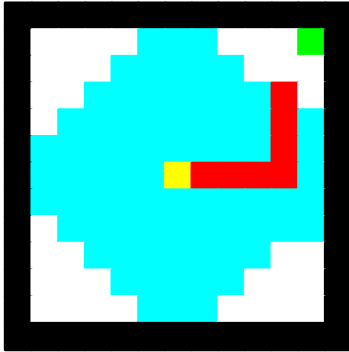
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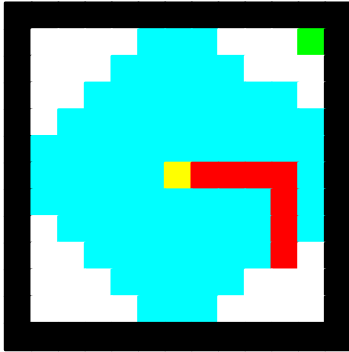
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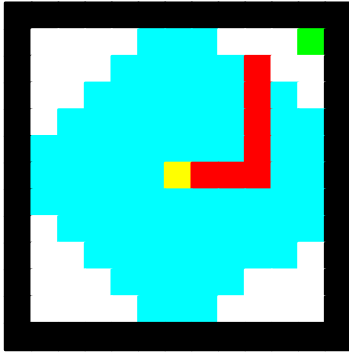
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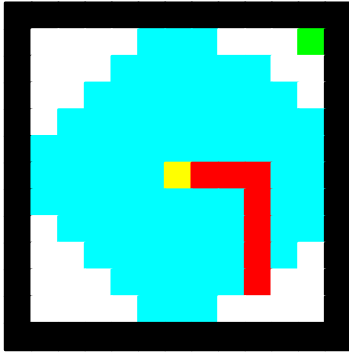
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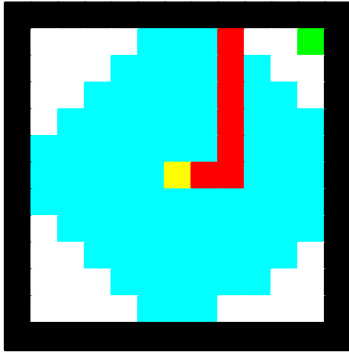
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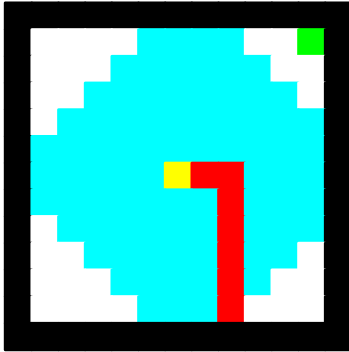
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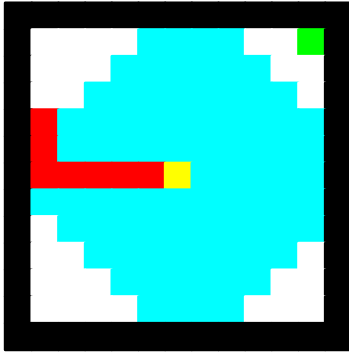
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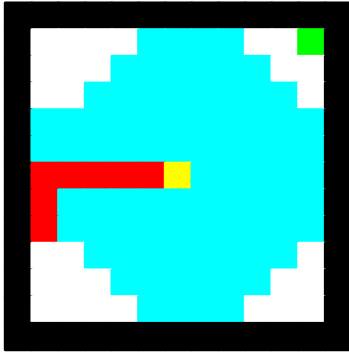
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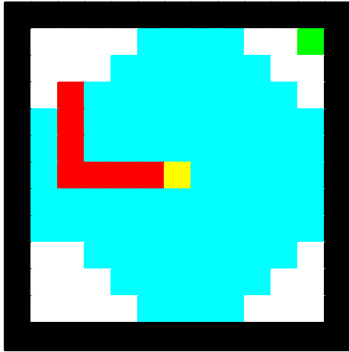
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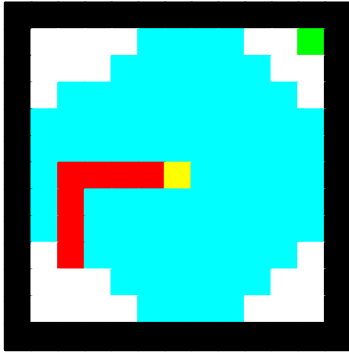
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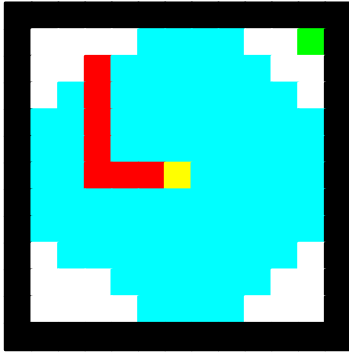
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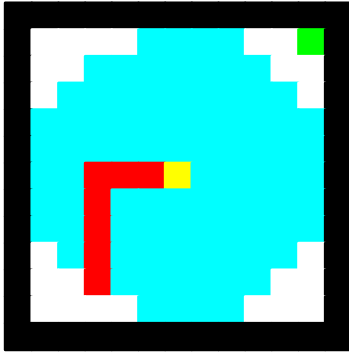
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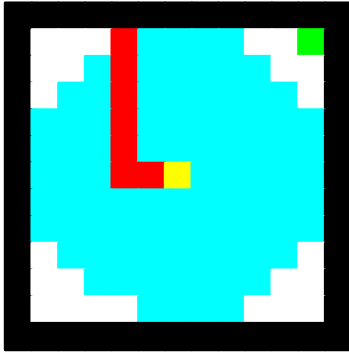
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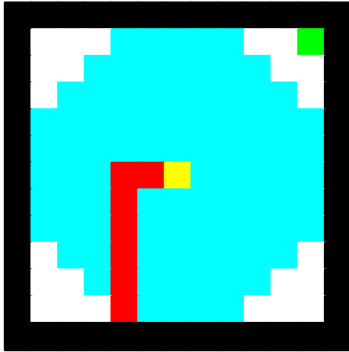
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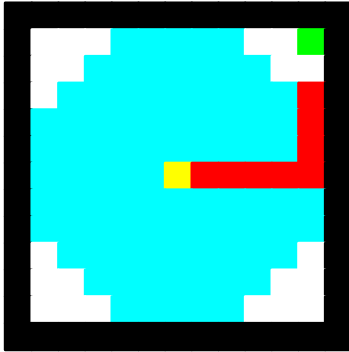
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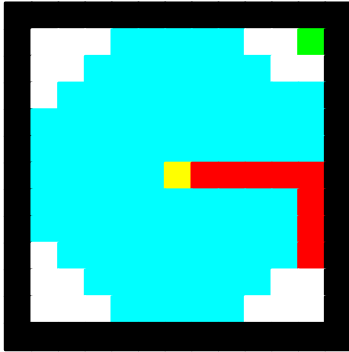
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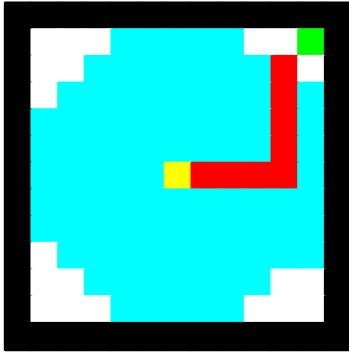
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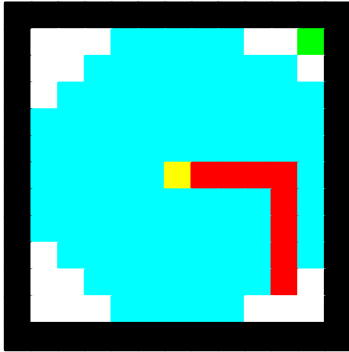
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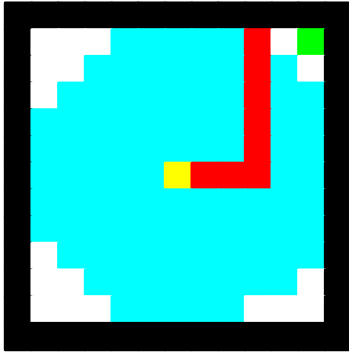
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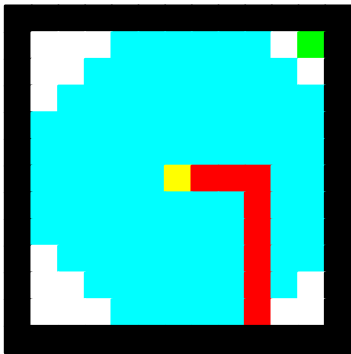
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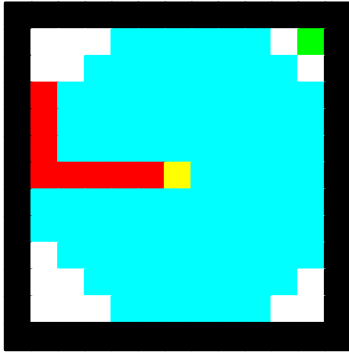
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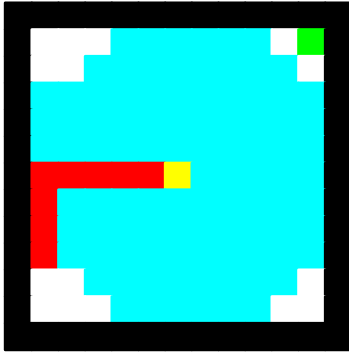
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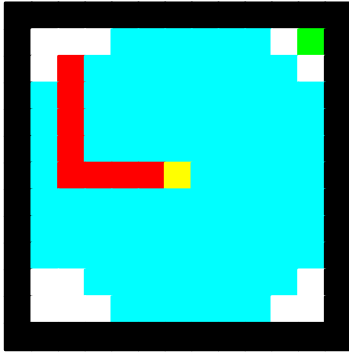
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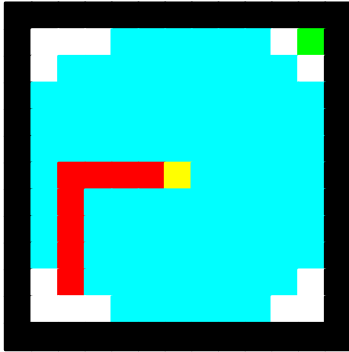
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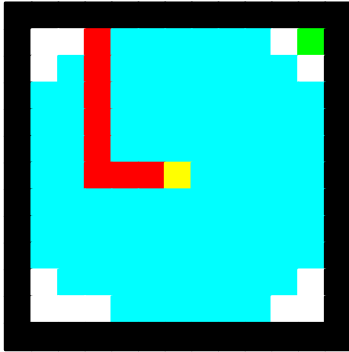
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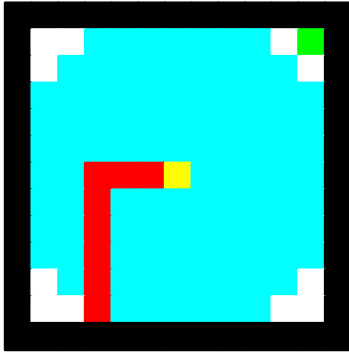
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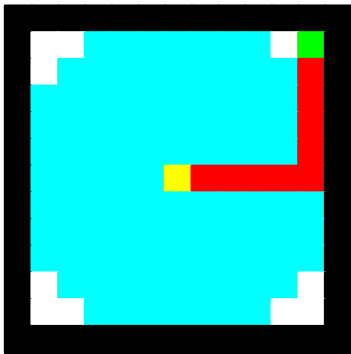
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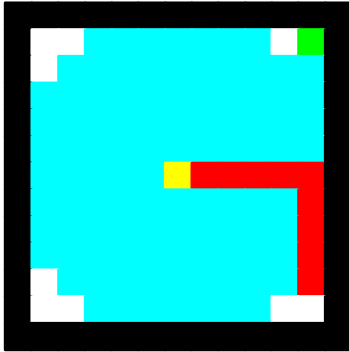
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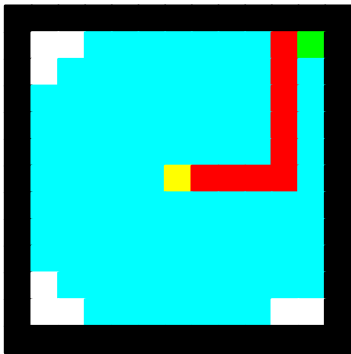
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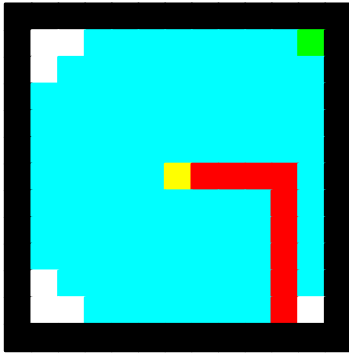
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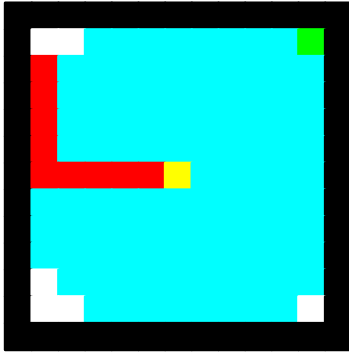
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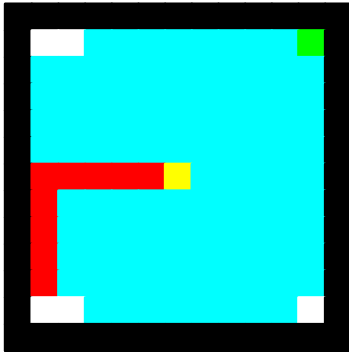
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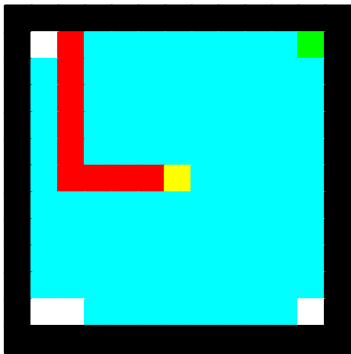
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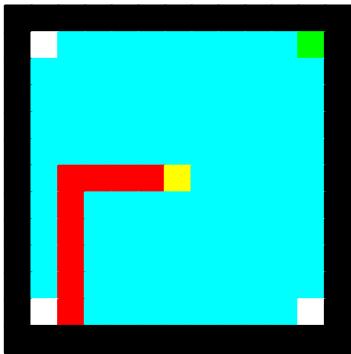
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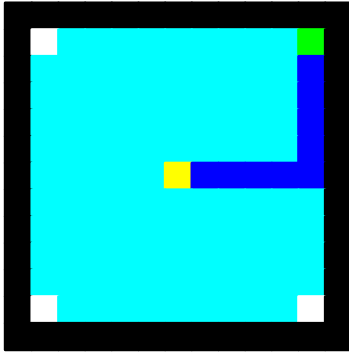
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Heuristics

So far, we have sorted our agenda based on:

$g(n)$ = the path cost from the start to n

Thus, any values with the same $g(n)$ will be considered at roughly the same time, regardless of whether they are moving "in the right direction" or not.

We can do better by including another function, which we'll call a **heuristic**:

$h(n)$ = an estimate of the remaining cost from n to the goal

Since we want to minimize total path cost, we can instead sort by:

$f(n) = g(n) + h(n)$

$f(n)$ = an estimate of total cost from start to goal through n

Heuristics

Including a heuristic function makes this an "informed" search: it uses information not only about the path so far, but about the nature of the goal, to focus its attention toward the goal. The resulting algorithm (UC search with a heuristic) is often referred to as A^* ("A-star").

This can have a dramatic effect on the amount of the search space we explore.

Heuristics and Optimality

In order to guarantee that we still get an optimal path, our heuristic needs a couple of properties:

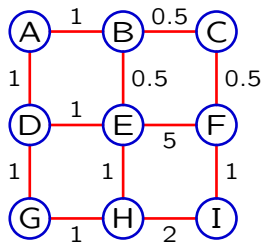
- **admissibility:** $h(n)$ never overestimates the actual cost of the lowest-cost path from n to the goal
- **consistency:** roughly, $h(n)$ does not increase as n gets closer to the goal.

The ideal heuristic should be

- as close as possible to actual cost (without exceeding it)
- easy to calculate

Example

Find path $E \rightarrow I$, A^* , heuristic: $h(s) = M(s, I)/2$

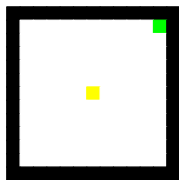


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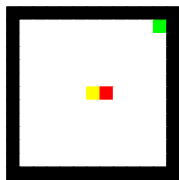


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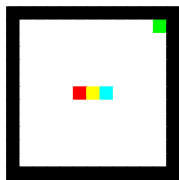


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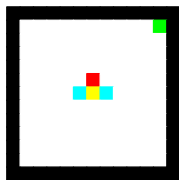


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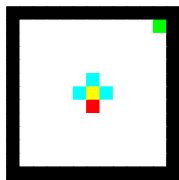


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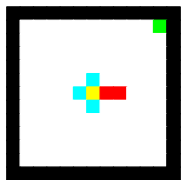


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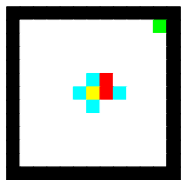


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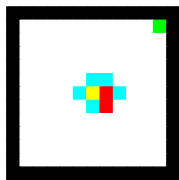


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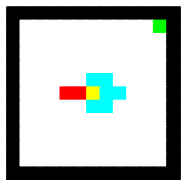


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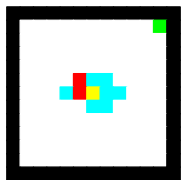


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3. $\max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
4. $2 * \min(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
5. $2 * \max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$

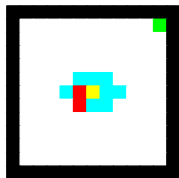


Check Yourself!

Consider searching in a 4-direction grid, and let (r_0, c_0) and (r_1, c_1) represent the current and goal locations.

How many of the following heuristics are **admissible**?

1. $\text{abs}(r_0 - r_1) + \text{abs}(c_0 - c_1)$ (i.e. Manhattan distance)
2. $\min(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
3. $\max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
4. $2 * \min(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
5. $2 * \max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$

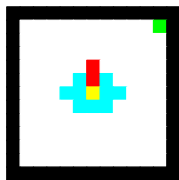


Check Yourself!

Consider searching in a 4-direction grid, and let (r_0, c_0) and (r_1, c_1) represent the current and goal locations.

How many of the following heuristics are **admissible**?

1. $\text{abs}(r_0 - r_1) + \text{abs}(c_0 - c_1)$ (i.e. Manhattan distance)
2. $\min(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
3. $\max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
4. $2 * \min(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
5. $2 * \max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$

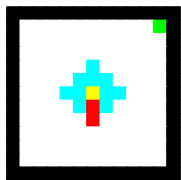


Check Yourself!

Consider searching in a 4-direction grid, and let (r_0, c_0) and (r_1, c_1) represent the current and goal locations.

How many of the following heuristics are **admissible**?

1. $\text{abs}(r_0 - r_1) + \text{abs}(c_0 - c_1)$ (i.e. Manhattan distance)
2. $\min(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
3. $\max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
4. $2 * \min(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
5. $2 * \max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$

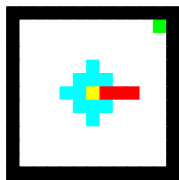


Check Yourself!

Consider searching in a 4-direction grid, and let (r_0, c_0) and (r_1, c_1) represent the current and goal locations.

How many of the following heuristics are **admissible**?

1. $\text{abs}(r_0 - r_1) + \text{abs}(c_0 - c_1)$ (i.e. Manhattan distance)
2. $\min(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
3. $\max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
4. $2 * \min(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
5. $2 * \max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$

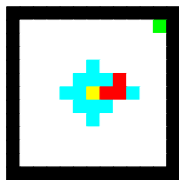


Check Yourself!

Consider searching in a 4-direction grid, and let (r_0, c_0) and (r_1, c_1) represent the current and goal locations.

How many of the following heuristics are **admissible**?

1. $\text{abs}(r_0 - r_1) + \text{abs}(c_0 - c_1)$ (i.e. Manhattan distance)
2. $\min(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
3. $\max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
4. $2 * \min(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
5. $2 * \max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$

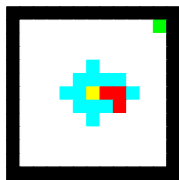


Check Yourself!

Consider searching in a 4-direction grid, and let (r_0, c_0) and (r_1, c_1) represent the current and goal locations.

How many of the following heuristics are **admissible**?

1. $\text{abs}(r_0 - r_1) + \text{abs}(c_0 - c_1)$ (i.e. Manhattan distance)
2. $\min(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
3. $\max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
4. $2 * \min(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
5. $2 * \max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$

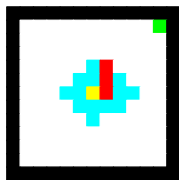


Check Yourself!

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How many of the following heuristics are **admissible**?

1. $\text{abs}(r_0 - r_1) + \text{abs}(c_0 - c_1)$ (i.e. Manhattan distance)
2. $\min(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
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4. $2 * \min(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
5. $2 * \max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$

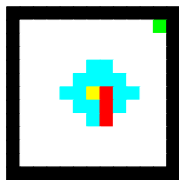


Check Yourself!

Consider searching in a 4-direction grid, and let (r_0, c_0) and (r_1, c_1) represent the current and goal locations.

How many of the following heuristics are **admissible**?

1. $\text{abs}(r_0 - r_1) + \text{abs}(c_0 - c_1)$ (i.e. Manhattan distance)
2. $\min(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
3. $\max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
4. $2 * \min(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
5. $2 * \max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$

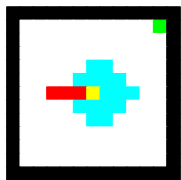


Check Yourself!

Consider searching in a 4-direction grid, and let (r_0, c_0) and (r_1, c_1) represent the current and goal locations.

How many of the following heuristics are **admissible**?

1. $\text{abs}(r_0 - r_1) + \text{abs}(c_0 - c_1)$ (i.e. Manhattan distance)
2. $\min(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
3. $\max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
4. $2 * \min(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
5. $2 * \max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$

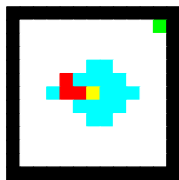


Check Yourself!

Consider searching in a 4-direction grid, and let (r_0, c_0) and (r_1, c_1) represent the current and goal locations.

How many of the following heuristics are **admissible**?

1. $\text{abs}(r_0 - r_1) + \text{abs}(c_0 - c_1)$ (i.e. Manhattan distance)
2. $\min(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
3. $\max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
4. $2 * \min(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
5. $2 * \max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$

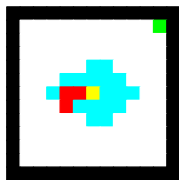


Check Yourself!

Consider searching in a 4-direction grid, and let (r_0, c_0) and (r_1, c_1) represent the current and goal locations.

How many of the following heuristics are **admissible**?

1. $\text{abs}(r_0 - r_1) + \text{abs}(c_0 - c_1)$ (i.e. Manhattan distance)
2. $\min(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
3. $\max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
4. $2 * \min(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
5. $2 * \max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$

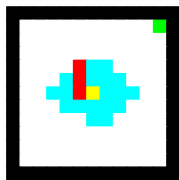


Check Yourself!

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How many of the following heuristics are **admissible**?

1. $\text{abs}(r_0 - r_1) + \text{abs}(c_0 - c_1)$ (i.e. Manhattan distance)
2. $\min(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
3. $\max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
4. $2 * \min(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
5. $2 * \max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$

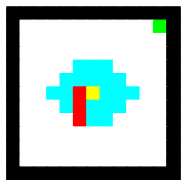


Check Yourself!

Consider searching in a 4-direction grid, and let (r_0, c_0) and (r_1, c_1) represent the current and goal locations.

How many of the following heuristics are **admissible**?

1. $\text{abs}(r_0 - r_1) + \text{abs}(c_0 - c_1)$ (i.e. Manhattan distance)
2. $\min(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
3. $\max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
4. $2 * \min(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
5. $2 * \max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$

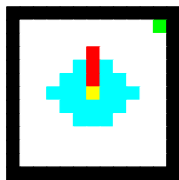


Check Yourself!

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How many of the following heuristics are **admissible**?

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2. $\min(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
3. $\max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
4. $2 * \min(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
5. $2 * \max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$

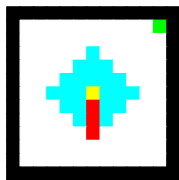


Check Yourself!

Consider searching in a 4-direction grid, and let (r_0, c_0) and (r_1, c_1) represent the current and goal locations.

How many of the following heuristics are **admissible**?

1. $\text{abs}(r_0 - r_1) + \text{abs}(c_0 - c_1)$ (i.e. Manhattan distance)
2. $\min(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
3. $\max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
4. $2 * \min(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
5. $2 * \max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$

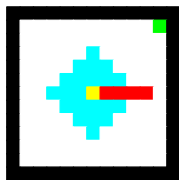


Check Yourself!

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How many of the following heuristics are **admissible**?

1. $\text{abs}(r_0 - r_1) + \text{abs}(c_0 - c_1)$ (i.e. Manhattan distance)
2. $\min(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
3. $\max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
4. $2 * \min(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
5. $2 * \max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$

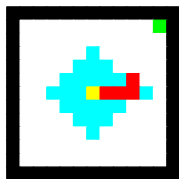


Check Yourself!

Consider searching in a 4-direction grid, and let (r_0, c_0) and (r_1, c_1) represent the current and goal locations.

How many of the following heuristics are **admissible**?

1. `abs(r0-r1)+abs(c0-c1)` (i.e. Manhattan distance)
2. `min(abs(r0-r1),abs(c0-c1))`
3. `max(abs(r0-r1),abs(c0-c1))`
4. `2*min(abs(r0-r1),abs(c0-c1))`
5. `2*max(abs(r0-r1),abs(c0-c1))`

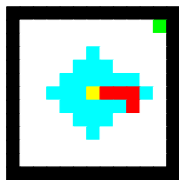


Check Yourself!

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How many of the following heuristics are **admissible**?

1. $\text{abs}(r_0 - r_1) + \text{abs}(c_0 - c_1)$ (i.e. Manhattan distance)
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4. $2 * \min(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
5. $2 * \max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$

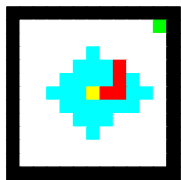


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5. $2 * \max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$

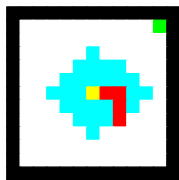


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2. $\min(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
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5. $2 * \max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$

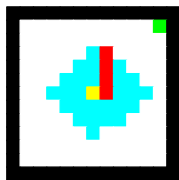


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5. $2 * \max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$

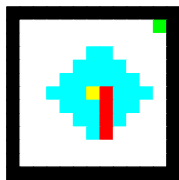


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5. $2 * \max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$

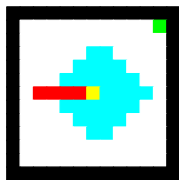


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5. $2 * \max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$

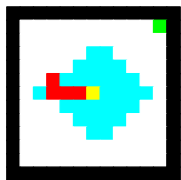


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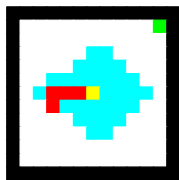


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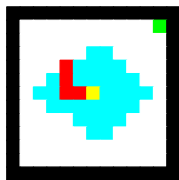


Check Yourself!

Consider searching in a 4-direction grid, and let (r_0, c_0) and (r_1, c_1) represent the current and goal locations.

How many of the following heuristics are **admissible**?

1. $\text{abs}(r_0 - r_1) + \text{abs}(c_0 - c_1)$ (i.e. Manhattan distance)
2. $\min(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
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4. $2 * \min(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
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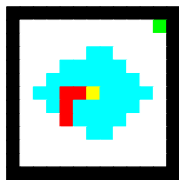


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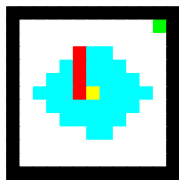


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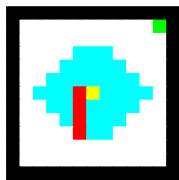


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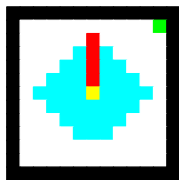


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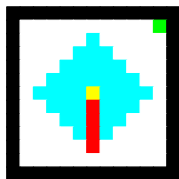


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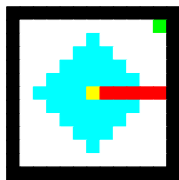


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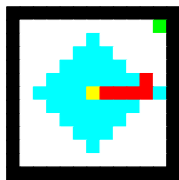


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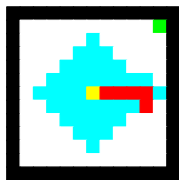


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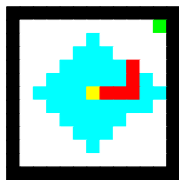


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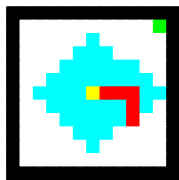


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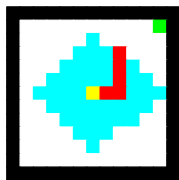


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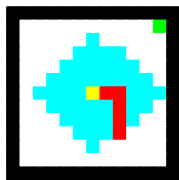


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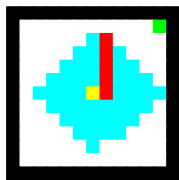


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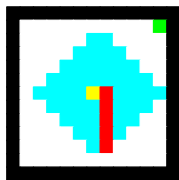


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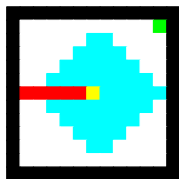


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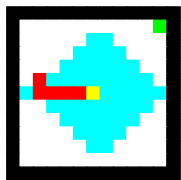


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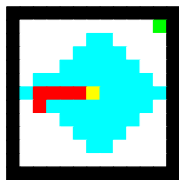


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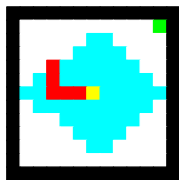


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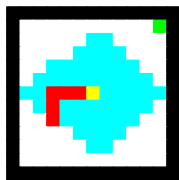


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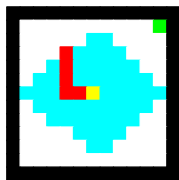


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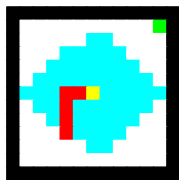


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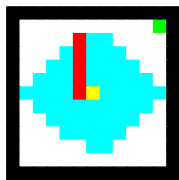


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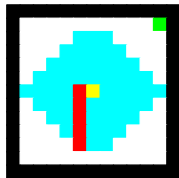


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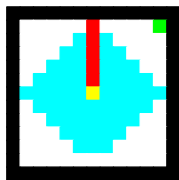


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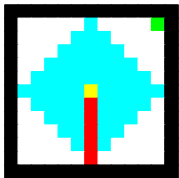


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3. $\max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
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5. $2 * \max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$

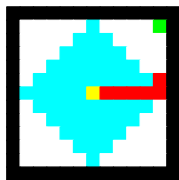


Check Yourself!

Consider searching in a 4-direction grid, and let (r_0, c_0) and (r_1, c_1) represent the current and goal locations.

How many of the following heuristics are **admissible**?

1. $\text{abs}(r_0 - r_1) + \text{abs}(c_0 - c_1)$ (i.e. Manhattan distance)
2. $\min(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
3. $\max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
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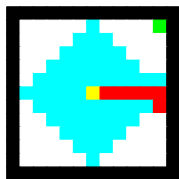


Check Yourself!

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How many of the following heuristics are **admissible**?

1. $\text{abs}(r_0 - r_1) + \text{abs}(c_0 - c_1)$ (i.e. Manhattan distance)
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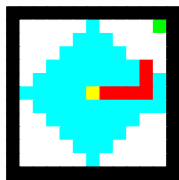


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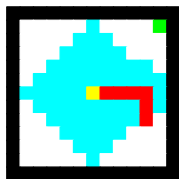


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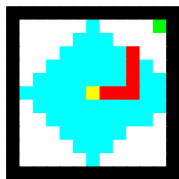


Check Yourself!

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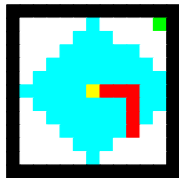


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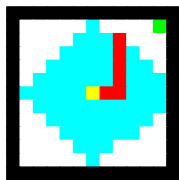


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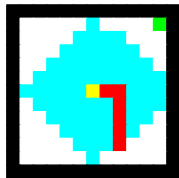


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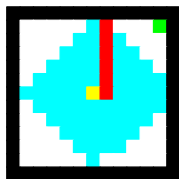


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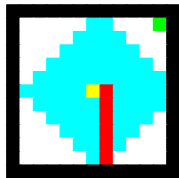


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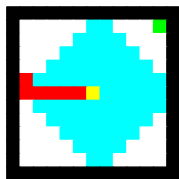


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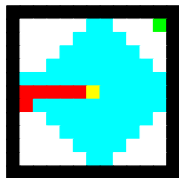


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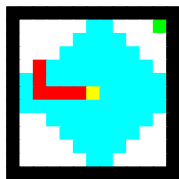


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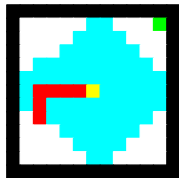


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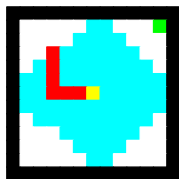


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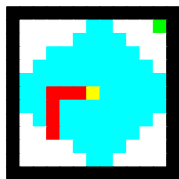


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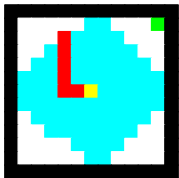


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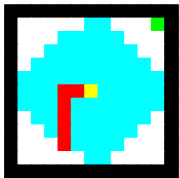


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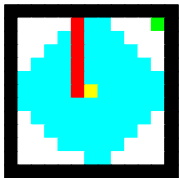


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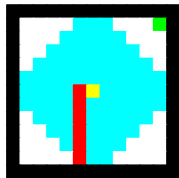


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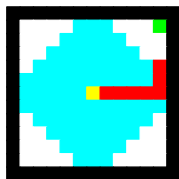


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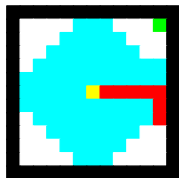


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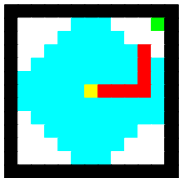


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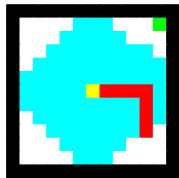


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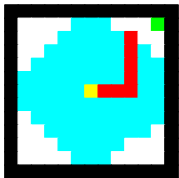


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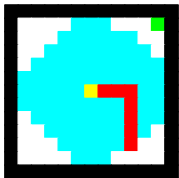


Check Yourself!

Consider searching in a 4-direction grid, and let (r_0, c_0) and (r_1, c_1) represent the current and goal locations.

How many of the following heuristics are **admissible**?

1. $\text{abs}(r_0 - r_1) + \text{abs}(c_0 - c_1)$ (i.e. Manhattan distance)
2. $\min(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
3. $\max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
4. $2 * \min(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
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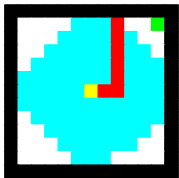


Check Yourself!

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How many of the following heuristics are **admissible**?

1. $\text{abs}(r_0 - r_1) + \text{abs}(c_0 - c_1)$ (i.e. Manhattan distance)
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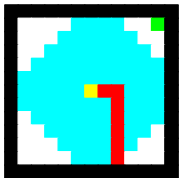


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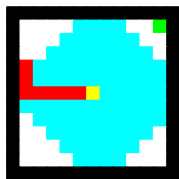


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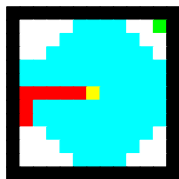


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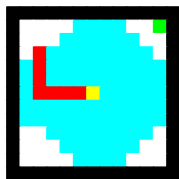


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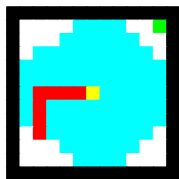


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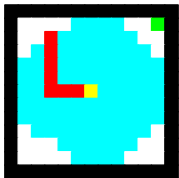


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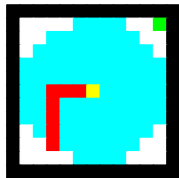


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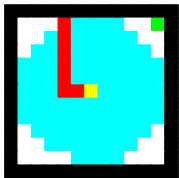


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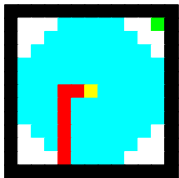


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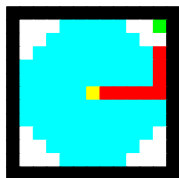


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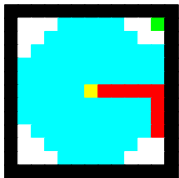


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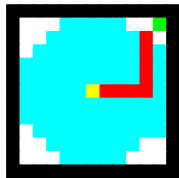


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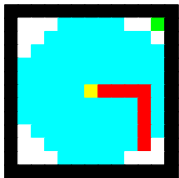


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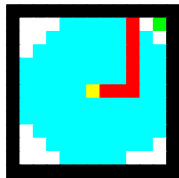


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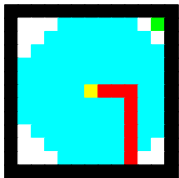


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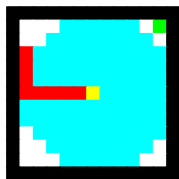


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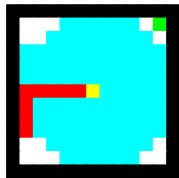


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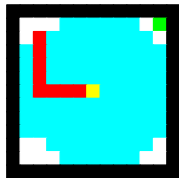


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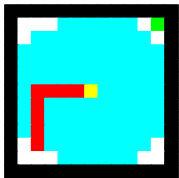


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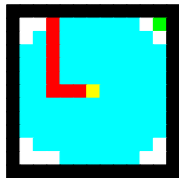


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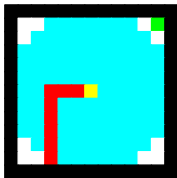


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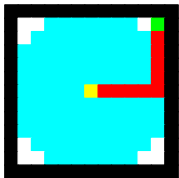


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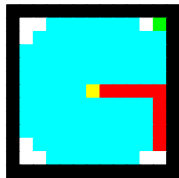


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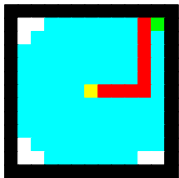


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1. $\text{abs}(r_0 - r_1) + \text{abs}(c_0 - c_1)$ (i.e. Manhattan distance)
2. $\min(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
3. $\max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
4. $2 * \min(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
5. $2 * \max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$

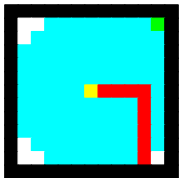


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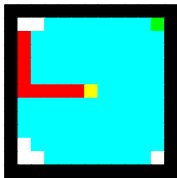


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5. $2 * \max(\text{abs}(r_0 - r1), \text{abs}(c_0 - c_1))$

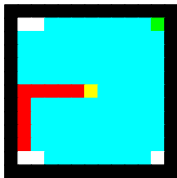


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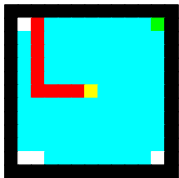


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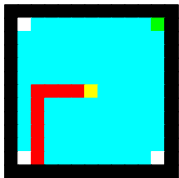


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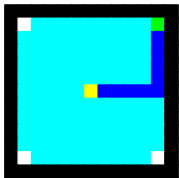


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3. $\max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
4. $2 * \min(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
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Check Yourself!

Consider searching in a 4-direction grid, and let (r_0, c_0) and (r_1, c_1) represent the current and goal locations.

Which of the admissible heuristics minimizes the number of paths expanded?

1. $\text{abs}(r_0 - r_1) + \text{abs}(c_0 - c_1)$ (i.e. Manhattan distance)
2. $\min(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
3. $\max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
4. $2 * \min(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$
5. $2 * \max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$

Compare

Heuristic	Paths Expanded
$\text{abs}(r_0 - r_1) + \text{abs}(c_0 - c_1)$	42
$\min(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$	114
$\max(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$	60
$2 * \min(\text{abs}(r_0 - r_1), \text{abs}(c_0 - c_1))$	72

Heuristics: Eight Puzzle

Consider three heuristic functions for the "eight puzzle":

- a. $h(n) = 0$
- b. $h(n) = \text{number of tiles out of place}$
- c. $h(n) = \text{sum over tiles of Manhattan distances to their goals}$

Let $M_i = \#$ of moves in the best solution with heuristic i

Let $E_i = \#$ of paths expanded during search with heuristic i

Which of the following is/are true?

- 1. $M_a = M_b = M_c$
- 2. $E_a = E_b = E_c$
- 3. $M_a > M_b > M_c$
- 4. $E_a \geq E_b \geq E_c$

Compare

Heuristic	Expanded Solution	Cost
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a	84,516	22
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b	8,329	22
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c	1,348	22
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End

End
