Tent Packing

```
In [ ]:
          1 from instrument import instrument
In [ ]:
          1 # Pack a tent with different sleeping bag shapes leaving no empty squares
           2 #
           3 # INPUTS:
          4 # tent_size = (rows, cols) for tent grid
                 missing_squares = set of (r, c) tuples giving location of rocks
                bag_list = list of sets, each decribing a sleeping bag shape
          6 #
          7 #
                  Each set contains (r, c) tuples enumerating contiguous grid
          8 #
                    squares occupied by the bag, coords are relative to the upper-
          9 #
                  left corner of the bag. You can assume every bag occupies
          10 #
                    at least the grid (0,0).
          11 #
          12 # Example bag list entries:
                  vertical 3x1 bag: { (0,0), (1,0), (2,0) }
          13 #
          14 #
                   horizontal 1x3 bag: { (0,0), (0,1), (0,2) }
                 square bag: { (0,0), (0,1), (1,0), (1,1) }
L-shaped bag: { (0,0), (1,0), (1,1) }
          15 #
          16 #
          17 #
                  C-shaped bag: \{ (0,0), (0,1), (1,0), (2,0), (2,1) \}
          18 #
                    reverse-C-shaped bag: \{ (0,0), (0,1), (1,1), (2,0), (2,1) \}
          19 #
          20 # OUTPUT:
          21 #
                 None if no packing can be found; otherwise a list giving the
          22 # placement and type for each placed bag expressed as a dictionary
          23 # with keys
          24 # "anchor": (r, c) for upper-left corner of bag
                  "shape": index of bag on bag list
          25 #
```

Recursive Pattern: build on result of sub-problem

```
In [ ]:
             def pack(tent_size, missing_squares, bag_list):
                 all_squares = set((r, c) for r in range(tent_size[0])
                                               for c in range(tent_size[1]))
           3
           4
           5
                 def first empty(covered squares):
                     """ returns (r, c) for first empty square, else None if no empty squares """
           6
           7
           8
           9
                 @instrument
          10
                 def helper(covered_squares):
                     """ input: set of covered squares (covered by rocks or bags)
          11
                         output: None if no packing can be found, else a list of placed bags"""
          12
          13
          14
                     # look for first empty square
          15
                     pass
          16
          17
                     # base case: no empty squares! We return an empty (successful) packing.
          18
                     pass
          19
          20
                     # try placing each type of bag at locn: if it fits, consider those
          21
                     # squares as covered and recursively solve resulting problem
          22
                     pass
          23
                     # oops, no bags fit at this locn -- no valid packing
          24
          25
                     return None
          26
          27
                 # get things started
                 return helper(missing_squares)
          28
In [ ]:
           1 bag list = [
               { (0,0), (1,0), (2,0) }, # vertical 3x1 bag
               { (0,0), (0,1), (0,2) }, # horizontal 1x3 bag
           3
               { (0,0), (0,1), (1,0), (1,1) }, # square bag
               { (0,0), (1,0), (1,1) }, # L-shaped bag
               \{ (0,0), (0,1), (1,0), (2,0), (2,1) \}, # C-shaped bag
           7
               \{ (0,0), (0,1), (1,1), (2,0), (2,1) \}, \# reverse C-shaped bag
           8
          10 # horizontal bag in 1x3 tent, no rocks => fits
          11 tent size = (1,3)
          12 rocks = set()
          13 print(pack(tent_size, rocks, bag_list))
In [ ]:
           1 # C-shaped bag in 3x2 tent, one rock => fits
           2 \text{ tent\_size} = (3,2)
           3 rocks = \{(1,1)\}
           4 print(pack(tent_size, rocks, bag_list))
In [ ]:
           1 # 5x5 tent with three rocks => fits
           2 tent_size = (5,5)
           3 rocks = \{(1,1),(1,3),(3,1)\}
           4 print(pack(tent_size, rocks, bag_list))
```

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In [ ]:
          1 # 5x5 tent with 4 rocks => fails
          2 tent_size = (5,5)
          3 rocks = \{(1,1),(1,3),(3,1),(3,3)\}
           4 print(pack(tent_size, rocks, bag_list))
```

What if we want all packings?

```
In [ ]:
           1 def all_packings(tent_size, missing_squares, bag_list):
                 # Put pack solution here, and then modify for all_packings.
                 # How do things change?
           3
                 pass
In [ ]:
           1 # Succeeds; more than one packing possible
           2 tent_size = (3,3)
           3 rocks = set()
           4 res = all_packings(tent_size, rocks, bag_list)
           5 print("NUMBER PACKINGS:", len(res) if res is not None else 0)
           6 print(res)
In [ ]:
           1 # More packings... (case 5)
           2 tent_size = (4,4)
           3 rocks = set()
           4 res = all_packings(tent_size, rocks, bag_list)
           5 print("NUMBER PACKINGS:", len(res) if res is not None else 0)
In [ ]:
           1 # 9x7 tent with scattered rocks -- Lots of possibilities (case 15)
           2 \text{ tent\_size} = (9,7)
           3 rocks = \{(0,2), (2,2), (2,4), (3,4), (7,4), (5,4), (5,5), (8,6), (7,1)\}
           4 res = all_packings(tent_size, rocks, bag_list)
           5 print("NUMBER PACKINGS:", len(res) if res is not None else 0)
In [ ]:
           1
```