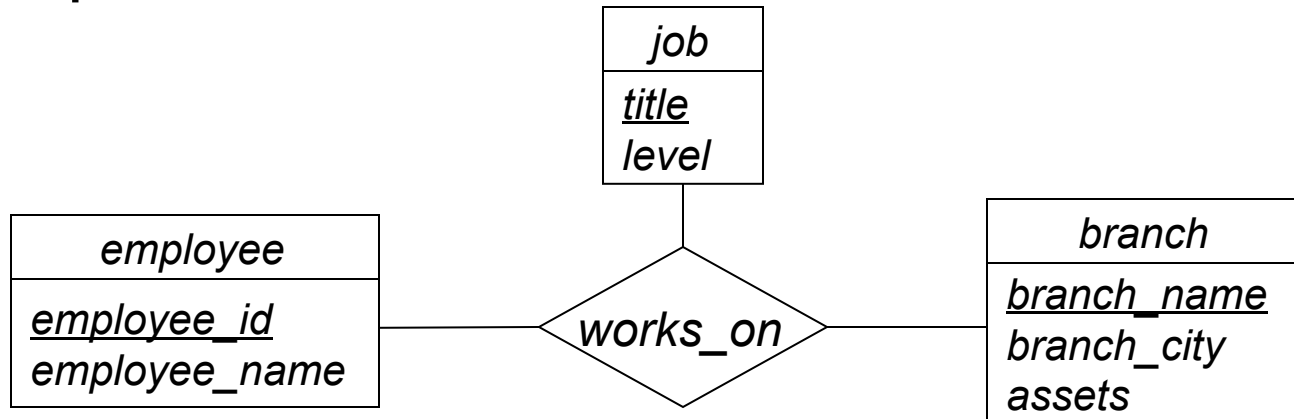


# ENTITY-RELATIONSHIP MODEL III

# N-ary Relationships

2

- Can specify relationships of degree  $> 2$  in E-R model
- Example:

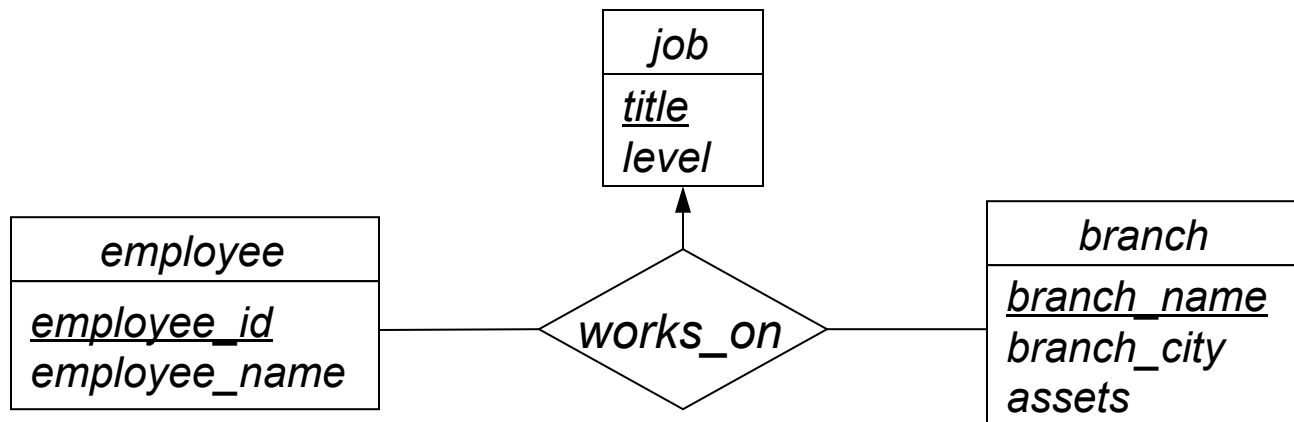


- Employees are assigned to jobs at various branches
- Many-to-many mapping: any combination of employee, job, and branch is allowed
- An employee can have several jobs at one branch

# N-ary Mapping Cardinalities

3

- Can specify *some* mapping cardinalities on relationships with degree  $> 2$
- Each combination of employee and branch can only be associated with one job:

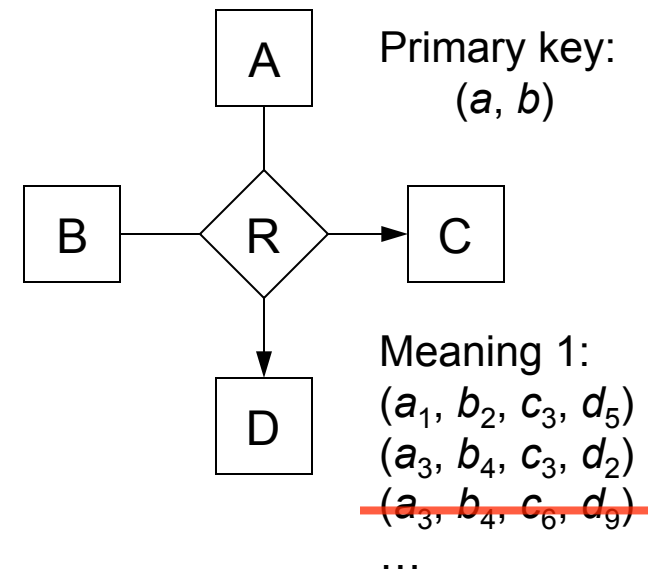


- Each employee can have only one job at each branch

# N-ary Mapping Cardinalities (2)

4

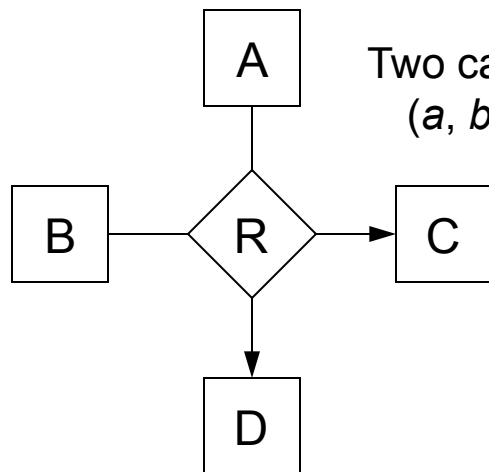
- For degree  $> 2$  relationships, we only allow at most one edge with an arrow
- Reason: multiple arrows on N-ary relationship-set is ambiguous
  - ▣ (several meanings have been defined for this in the past)
- Relationship-set  $R$  associating entity-sets  $A_1, A_2, \dots, A_n$ 
  - ▣ No arrows on edges  $A_1, \dots, A_i$
  - ▣ Arrows are on edges to  $A_{i+1}, \dots, A_n$
- Meaning 1 (the simpler one):
  - ▣ A particular combination of entities in  $A_1, \dots, A_i$  can be associated with at most one set of entities in  $A_{i+1}, \dots, A_n$
  - ▣ Primary key of  $R$  is union of primary keys from set  $\{A_1, A_2, \dots, A_i\}$



# N-ary Mapping Cardinalities (3)

5

- Relationship-set  $R$  associating entity-sets  $A_1, A_2, \dots, A_n$ 
  - ▣ No arrows on edges  $A_1, \dots, A_i$ ; arrows on edges to  $A_{i+1}, \dots, A_n$
- Meaning 2 (the insane one):
  - ▣ For each entity-set  $A_k$  ( $i < k \leq n$ ), a particular combination of entities from *all other* entity-sets can be associated with at most one entity in  $A_k$
  - ▣  $R$  has a candidate key for each arrow in N-ary relationship-set
  - ▣ For each  $k$  ( $i < k \leq n$ ), another candidate key of  $R$  is union of primary keys from entity-sets  $\{A_1, A_2, \dots, A_{k-1}, A_{k+1}, \dots, A_n\}$



Two candidate keys:  
 $(a, b, c), (a, b, d)$

Meaning 2:

$(a_1, b_2, c_3, d_5)$   
 $(a_3, b_4, c_3, d_2)$   
 $(a_1, b_2, c_1, d_4)$   
 $(a_3, b_4, c_5, d_7)$   
 ~~$(a_1, b_2, c_3, d_6)$~~   
 ~~$(a_3, b_4, c_8, d_2)$~~   
...

} All disallowed  
by meaning 1!

# N-ary Mapping Cardinalities (4)

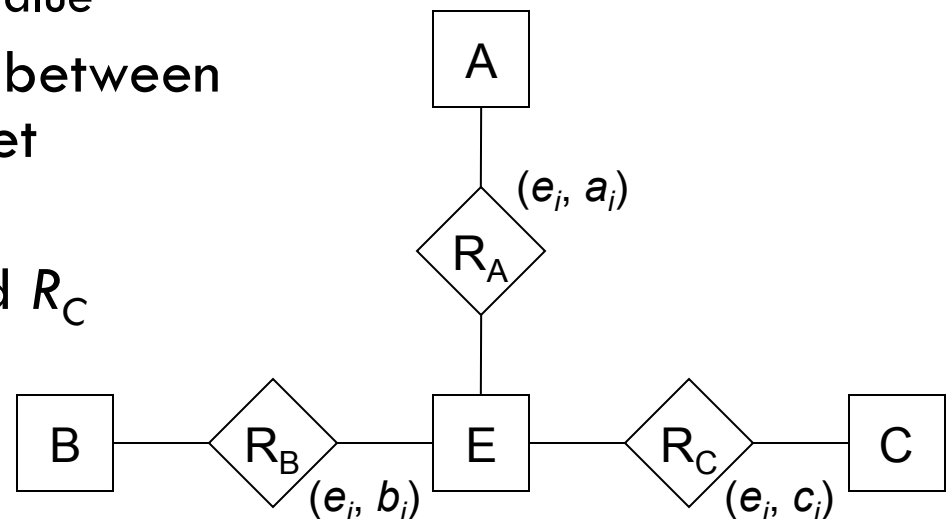
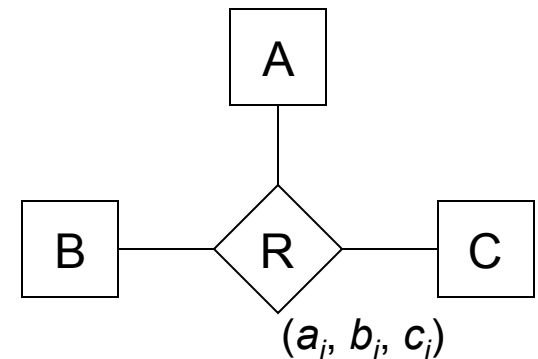
6

- Both interpretations of multiple arrows have been used in books and papers...
- If we only allow one edge to have an arrow, both definitions are equivalent
  - ▣ The ambiguity disappears

# Binary vs. N-ary Relationships

7

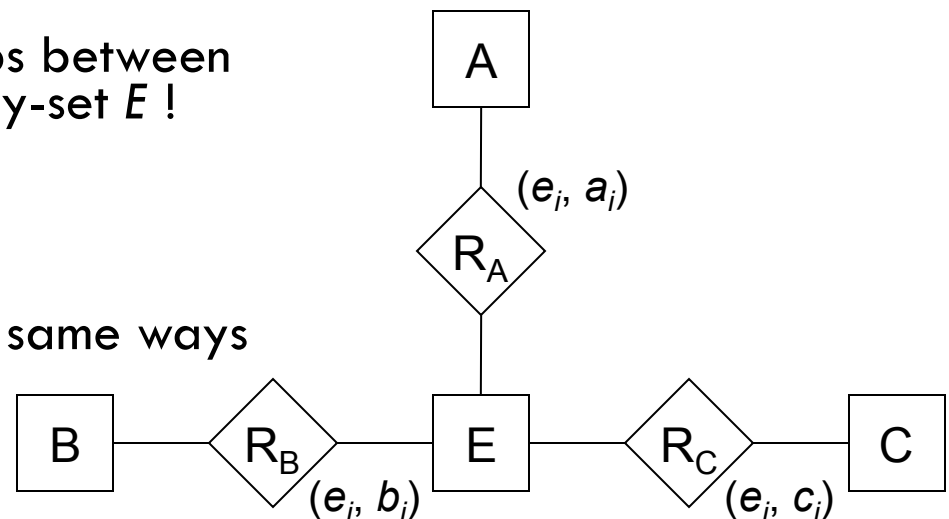
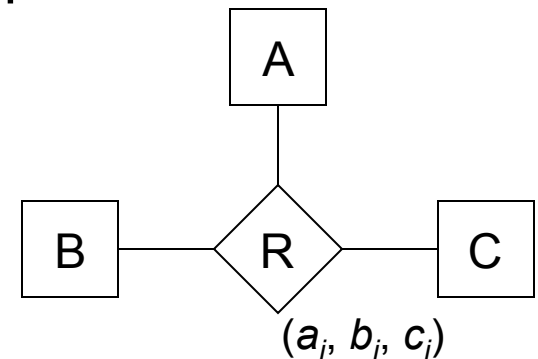
- Often have only binary relationships in DB schemas
- For degree  $> 2$  relationships, *could* replace with binary relationships
  - ▣ Replace N-ary relationship-set with a new entity-set  $E$ 
    - Create an identifying attribute for  $E$
    - e.g. an auto-generated ID value
  - ▣ Create a relationship-set between  $E$  and each other entity-set
  - ▣ Relationships in  $R$  must be represented in  $R_A$ ,  $R_B$ , and  $R_C$



# Binary vs. N-ary Relationships (2)

8

- **Are these representations identical?**
- Example: Want to represent a relationship between entities  $a_5$ ,  $b_1$  and  $c_2$ 
  - ▣ How many relationships can we actually have between these three entities?
- Ternary relationship set:
  - ▣ Can only store one relationship between  $a_5$ ,  $b_1$  and  $c_2$ , due to primary key of  $R$
- Alternate approach:
  - ▣ Can create many relationships between these entities, due to the entity-set  $E$  !
    - $(a_5, e_1), (b_1, e_1), (c_2, e_1)$
    - $(a_5, e_2), (b_1, e_2), (c_2, e_2)$
    - ...
  - ▣ Can't constrain in exactly the same ways





# Binary vs. N-ary Relationships (3)

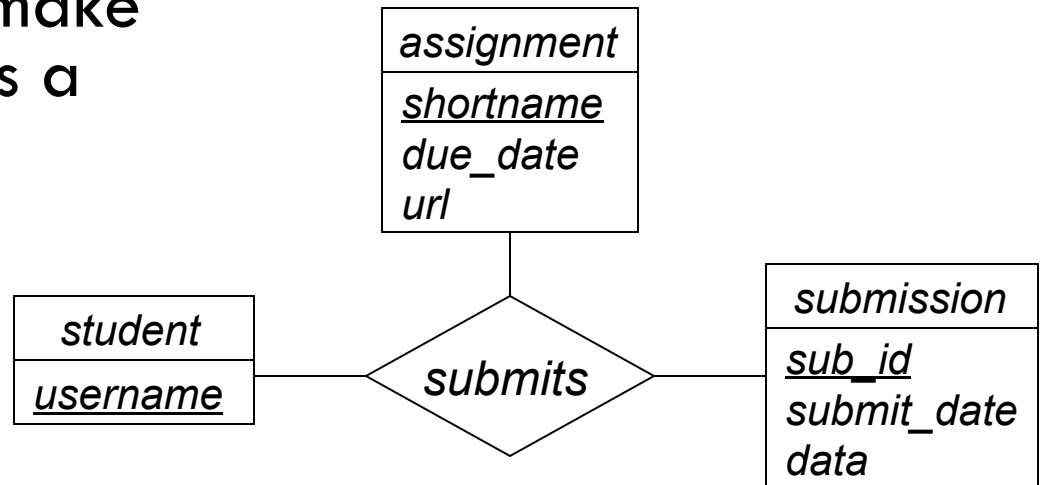
9

- Using binary relationships is sometimes more intuitive for particular designs
- Example: office-equipment inventory database
  - ▣ Ternary relationship-set *inventory*, associating *department*, *machine*, and *vendor* entity-sets
- What if vendor info is unknown for some machines?
  - ▣ For ternary relationship, must use *null* values to represent missing vendor details
  - ▣ With binary relationships, can simply not have a relationship between *machine* and *vendor*
- For cases like these, use binary relationships
  - ▣ If it makes sense to model as separate binary relationships, do it that way!

# Course Database Example

10

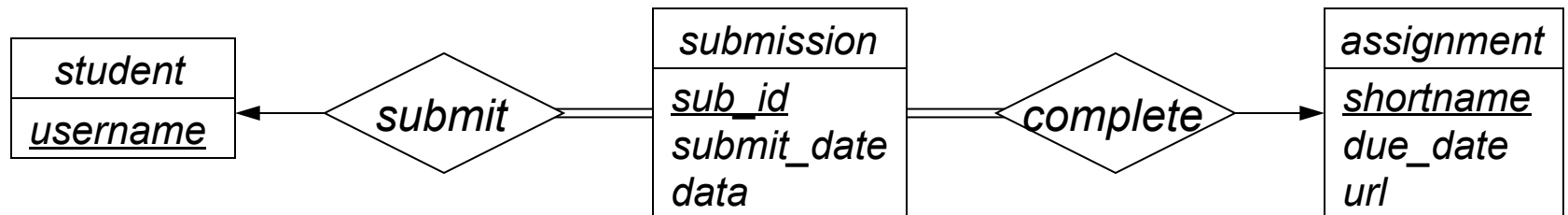
- What about this case:
  - ▣ Ternary relationship between *student*, *assignment*, and *submission*
  - ▣ Need to allow multiple submissions for a particular assignment, from a particular student
- In this case, it could make sense to represent as a ternary relationship
  - ▣ Doesn't make sense to have only two of these three entities in a relationship



# Course Database Example (2)

11

- Other ways to represent students, assignments and submissions?
- Can also represent as two binary relationships

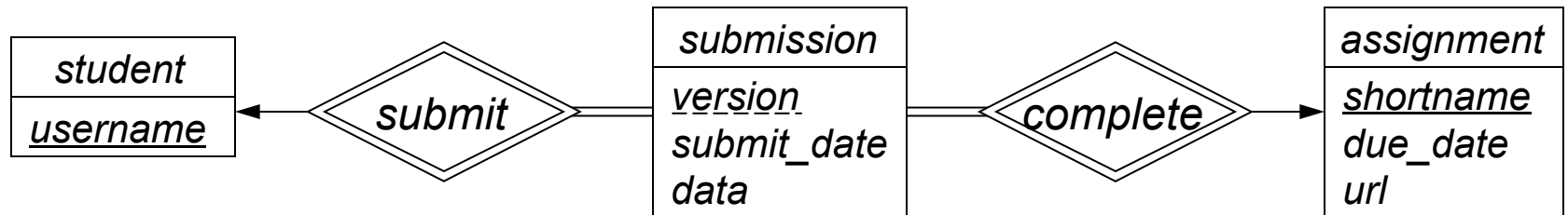


- Note the total participation constraints!
  - ▣ Required to ensure that every *submission* has an associated *student*, and an associated *assignment*
  - ▣ Also, two one-to-many constraints

# Course Database Example (3)

12

- Could even make *submission* a weak entity-set
  - ▣ Both *student* and *assignment* are identifying entities!



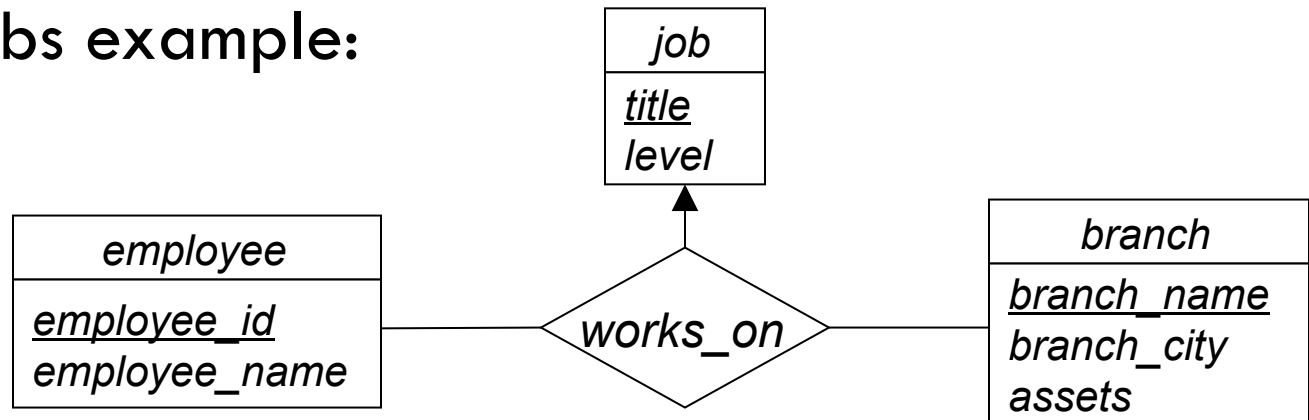
- Discriminator for *submission* is version number
- Primary key for *submission* ?
  - ▣ Union of primary keys from all owner entity-sets, plus discriminator
  - ▣ (*username*, *shortname*, *version*)

# Binary vs. N-ary Relationships

13

- Sometimes ternary relationships are best
  - ▣ Clearly indicates all entities involved in relationship
  - ▣ Only way to represent certain constraints!

- Bank jobs example:



- ▣ Each (*employee*, *branch*) pair can have only one job
- ▣ Simply cannot construct the same constraint using only binary relationships
  - (Reason is related to issue identified on slide 8)

# E-R Model and Real Databases

14

- For E-R model to be useful, need to be able to convert diagrams into an implementation schema
- Turns out to be very easy to do this!
  - ▣ Big overlaps between E-R model and relational model
  - ▣ Biggest difference is E-R composite/multivalued attributes, vs. relational model atomic attributes
- Three components of conversion process:
  - ▣ Specify schema of the relation itself
  - ▣ Specify primary key on the relation
  - ▣ Specify any foreign key references to other relations

# Strong Entity-Sets

15

- Strong entity-set  $E$  with attributes  $a_1, a_2, \dots, a_n$ 
  - ▣ Assume simple, single-valued attributes for now
- Create a relation schema with same name  $E$ , and same attributes  $a_1, a_2, \dots, a_n$
- Primary key of relation schema is same as primary key of entity-set
  - ▣ Strong entity-sets require no foreign keys to other things
- Every entity in  $E$  is represented by a tuple in the corresponding relation

# Entity-Set Examples

16

- Geocache location E-R diagram:

- ▣ Entity-set named *location*

<i>location</i>
<u><i>latitude</i></u>
<u><i>longitude</i></u>
<i>description</i>
<i>last_visited</i>

- Convert to relation schema:

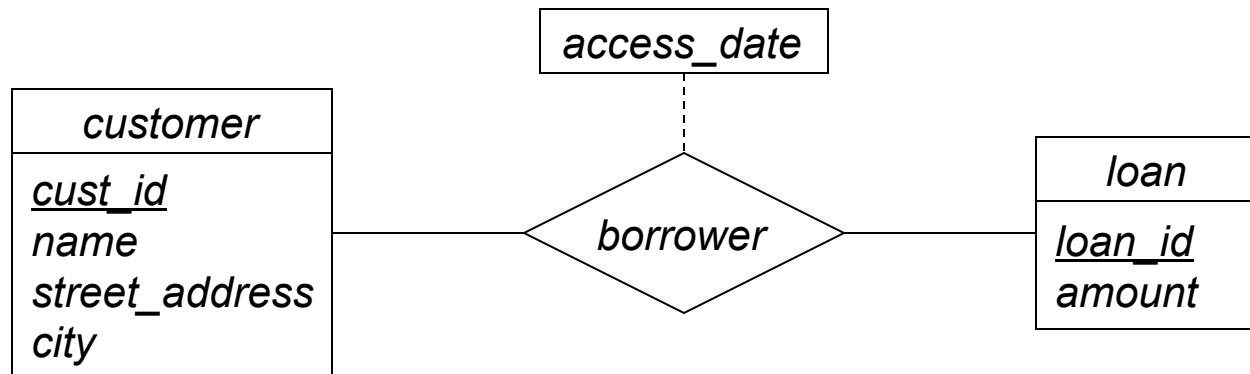
*location*(*latitude*, *longitude*, *description*, *last\_visited*)



# Entity-Set Examples (2)

17

- E-R diagram for customers and loans:



- Convert *customer* and *loan* entity-sets:  
*customer*(*cust\_id*, *name*, *street\_address*, *city*)  
*loan*(*loan\_id*, *amount*)

# Relationship-Sets

18

- Relationship-set  $R$ 
  - ▣ For now, assume that all participating entity-sets are strong entity-sets
  - ▣  $a_1, a_2, \dots, a_m$  is the union of all participating entity-sets' primary key attributes
  - ▣  $b_1, b_2, \dots, b_n$  are descriptive attributes on  $R$  (if any)
- Relational model schema for  $R$  is:
  - ▣  $\{a_1, a_2, \dots, a_m\} \cup \{b_1, b_2, \dots, b_n\}$
- $\{a_1, a_2, \dots, a_m\}$  is a superkey, but not necessarily a candidate key
  - ▣ Primary key of  $R$  depends on  $R$ 's mapping cardinality

# Relationship-Sets: Primary Keys

19

- For binary relationship-sets:
  - ▣ e.g. between strong entity-sets  $A$  and  $B$
  - ▣ If many-to-many mapping:
    - Primary key of relationship-set is union of all entity-set primary keys
    - $primary\_key(A) \cup primary\_key(B)$
  - ▣ If one-to-one mapping:
    - Either entity-set's primary key is acceptable
    - $primary\_key(A)$ , or  $primary\_key(B)$
    - Enforce both candidate keys in DB schema!

# Relationship-Sets: Primary Keys (2)

20

- For many-to-one or one-to-many mappings:
  - ▣ e.g. between strong entity-sets  $A$  and  $B$
  - ▣ Primary key of entity-set on “many” side is primary key of relationship
- Example: relationship  $R$  between  $A$  and  $B$ 
  - ▣ One-to-many mapping, with  $B$  on “many” side
  - ▣ Schema contains  $primary\_key(A) \cup primary\_key(B)$ , plus any descriptive attributes on  $R$
  - ▣  $primary\_key(B)$  is primary key of  $R$ 
    - Each  $a \in A$  can map to many  $b \in B$
    - Each value for  $primary\_key(B)$  can appear only once in  $R$

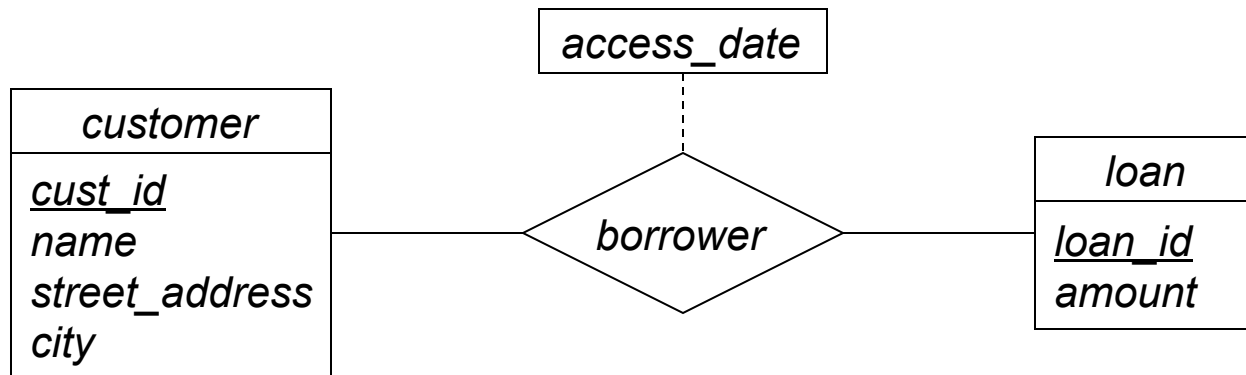
# Relationship-Set Foreign Keys

21

- Relationship-sets associate entities in entity-sets
  - ▣ We need foreign-key constraints on relation schema for  $R$  !
- For each entity-set  $E_i$  participating in  $R$  :
  - ▣ Relation schema for  $R$  has a foreign-key constraint on  $E_i$  relation, for *primary\_key*( $E_i$ ) attributes
- Relation schema notation doesn't provide mechanism for indicating foreign key constraints
  - ▣ Don't forget about foreign keys and candidate keys!
    - Making notes on your relational model schema is a very good idea
  - ▣ Can specify both foreign key constraints and candidate keys in the SQL DDL

# Relationship-Set Example

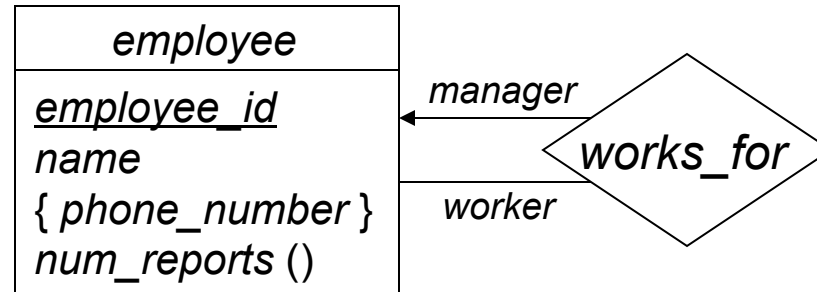
22



- Relation schema for *borrower*:
  - ▣ Primary key of *customer* is *cust\_id*
  - ▣ Primary key of *loan* is *loan\_id*
  - ▣ Descriptive attribute *access\_date*
  - ▣ *borrower* mapping cardinality is many-to-many
  - ▣ Result: *borrower*(*cust\_id*, *loan\_id*, *access\_date*)

# Relationship-Set Example (2)

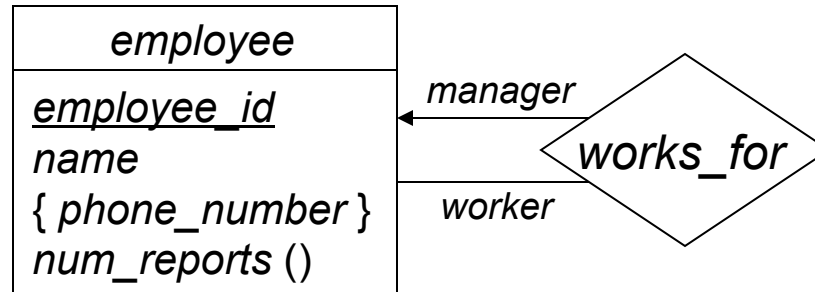
23



- In cases like this, must use roles to distinguish between the entities involved in the relationship-set
  - ▣ *employee* participates in *works\_for* relationship-set twice
  - ▣ Can't create a schema (*employee\_id*, *employee\_id*) !
- Change names of key-attributes to distinguish roles
  - ▣ e.g. (*manager\_employee\_id*, *worker\_employee\_id*)
  - ▣ e.g. (*manager\_id*, *employee\_id*)

# Relationship-Set Example (2)

24



- Relation schema for *employee* entity-set:
  - ▣ (For now, ignore *phone\_number* and *num\_reports*...)  
*employee*(*employee\_id*, *name*)
- Relation schema for *works\_for*:
  - ▣ One-to-many mapping from *manager* to *worker*
  - ▣ “Many” side is used for primary key
  - ▣ Result: *works\_for*(*employee\_id*, *manager\_id*)



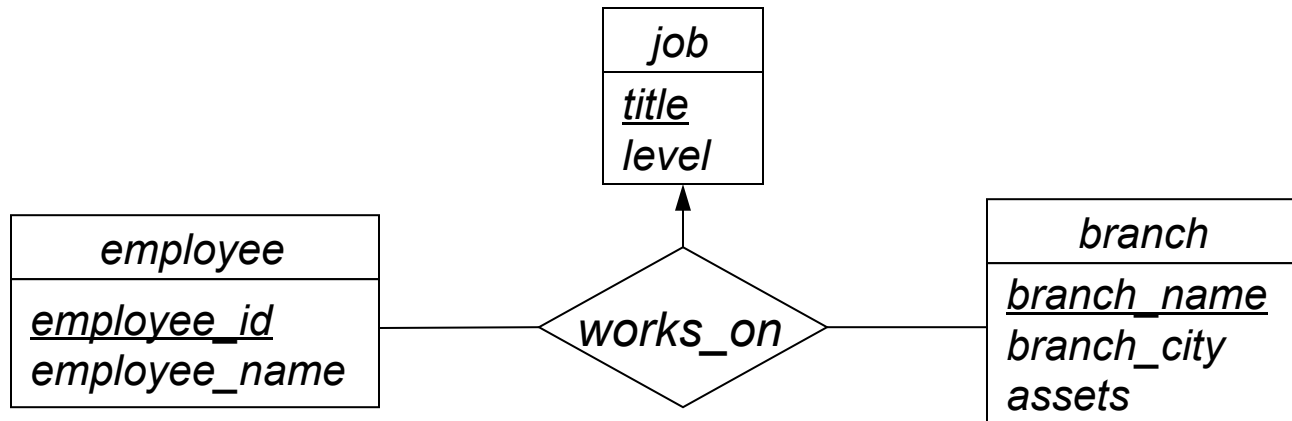
# N-ary Relationship Primary Keys

25

- For degree  $> 2$  relationship-sets:
  - ▣ If no arrows (“many-to-many” mapping), relationship-set primary key is union of all participating entity-sets’ primary keys
  - ▣ If one arrow (“one-to-many” mapping), relationship-set primary key is union of primary keys of entity-sets without an arrow
  - ▣ Don’t allow more than one arrow for relationship-sets with degree  $> 2$

# N-ary Relationship-Set Example

26



## □ Entity-set schemas:

*job*(title, level)

*employee*(employee\_id, employee\_name)

*branch*(branch\_name, branch\_city, assets)

## □ Relationship-set schema:

- ▣ Primary key includes entity-sets on non-arrow links

*works\_on*(employee\_id, branch\_name, title)

# Weak Entity-Sets

27

- Weak entity-sets depend on at least one strong entity-set
  - ▣ The identifying entity-set, or owner entity-set
  - ▣ Relationship between the two is called the identifying relationship
- Weak entity-set  $A$  owned by strong entity-set  $B$ 
  - ▣ Attributes of  $A$  are  $\{a_1, a_2, \dots, a_m\}$ 
    - Some subset of these attributes comprises the discriminator of  $A$
  - ▣  $primary\_key(B) = \{b_1, b_2, \dots, b_n\}$
  - ▣ Relation schema for  $A$ :  $\{a_1, a_2, \dots, a_m\} \cup \{b_1, b_2, \dots, b_n\}$
  - ▣ Primary key of  $A$  is  $discriminator(A) \cup primary\_key(B)$
  - ▣  $A$  has a foreign key constraint on  $primary\_key(B)$ , to  $B$

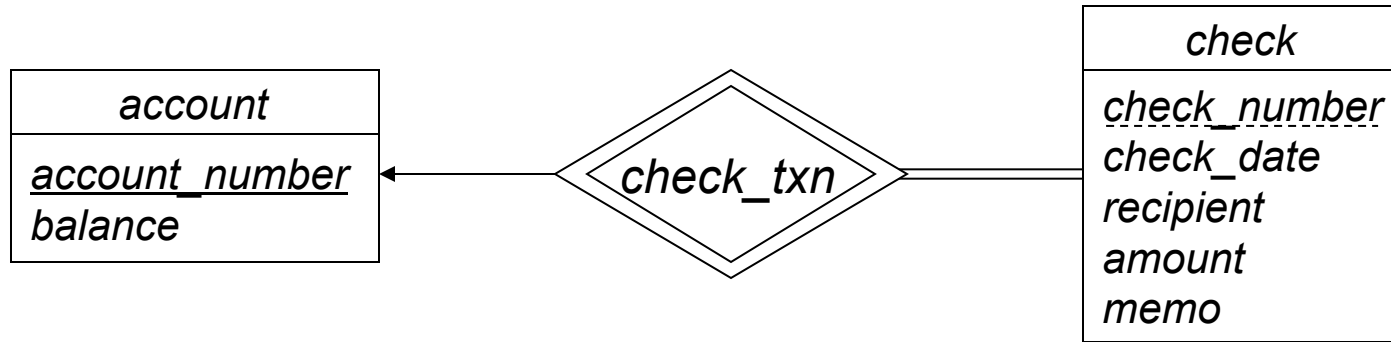
# Identifying Relationship?

28

- The identifying relationship is many-to-one, with no descriptive attributes
- Relation schema for weak entity-set already includes primary key for strong entity-set
  - ▣ Foreign key constraint is imposed, too
- No need to create relational model schema for the identifying relationship
  - ▣ Would be redundant to the weak entity-set's relational model schema!

# Weak Entity-Set Example

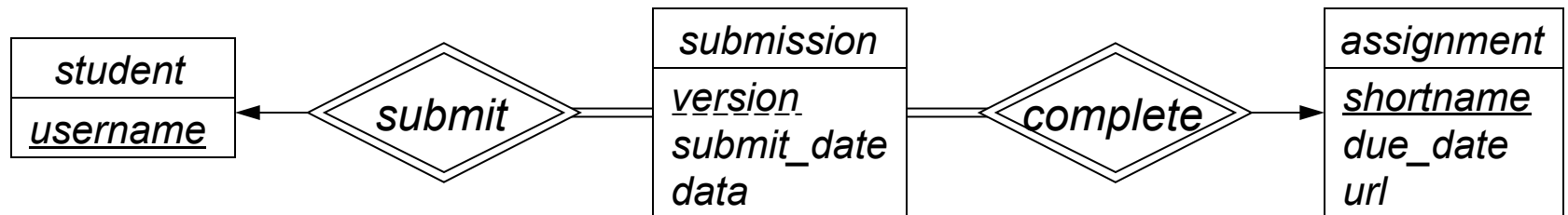
29



- *account* schema:  
*account*(*account\_number*, *balance*)
- *check* schema:
  - ▣ Discriminator is *check\_number*
  - ▣ Primary key for *check* is: (*account\_number*, *check\_number*)*check*(*account\_number*, *check\_number*, *check\_date*,  
*recipient*, *amount*, *memo*)

# Weak Entity-Set Example (2)

30



- Schemas for strong entity-sets:  
*student*(username)  
*assignment*(shortname, due\_date, *url*)
- Schema for *submission* weak entity-set:
  - ▣ Discriminator is *version*
  - ▣ Both *student* and *assignment* are owners!*submission*(username, shortname, version, submit\_date, *data*)
  - Two foreign keys in this relation as well

# Composite Attributes

31

- Relational model simply doesn't handle composite attributes
  - ▣ All attribute domains are *atomic* in the relational model
- When mapping E-R composite attributes to relation schema: simply flatten the composite
  - ▣ Each component attribute maps to a separate attribute in relation schema
  - ▣ In relation schema, simply can't refer to the composite as a whole
  - ▣ (Can adjust this mapping for databases that support composite types)

# Composite Attribute Example

32

- Customers with addresses:

<i>customer</i>
<u><i>cust_id</i></u>
<i>name</i>
<i>address</i>
<i>street</i>
<i>city</i>
<i>state</i>
<i>zip_code</i>

- Each component of *address* becomes a separate attribute

*customer*(*cust\_id*, *name*, *street*, *city*, *state*, *zip\_code*)



# Multivalued Attributes

33

- Multivalued attributes require a separate relation
  - ▣ Again, no such thing as a multivalued attribute in the relational model
  - ▣ E-R constraint on multivalued attributes: in a specific entity's multivalued attribute, each value may only appear once
- For a multivalued attribute  $M$  in entity-set  $E$ 
  - ▣ Create a relation schema  $R$  to store  $M$ , with attribute(s)  $A$  corresponding to the single-valued version of  $M$
  - ▣ Attributes of  $R$  are:  $primary\_key(E) \cup A$
  - ▣ Primary key of  $R$  includes all attributes of  $R$ 
    - Each value in  $M$  for an entity  $e$  must be unique
  - ▣ Foreign key from  $R$  to  $E$ , on  $primary\_key(E)$  attributes

# Multivalued Attribute Example

34

- Change our E-R diagram to allow customers to have multiple addresses:

<i>customer</i>
<u><i>cust_id</i></u>
<i>name</i>
{ <i>address</i>
<i>street</i>
<i>city</i>
<i>state</i>
<i>zip_code</i> }

- Now, must create a separate relation to store the addresses

*customer*(*cust\_id*, *name*)

*cust\_addrs*(*cust\_id*, *street*, *city*, *state*, *zipcode*)

- ▣ Large primary keys aren't ideal – tend to be costly