

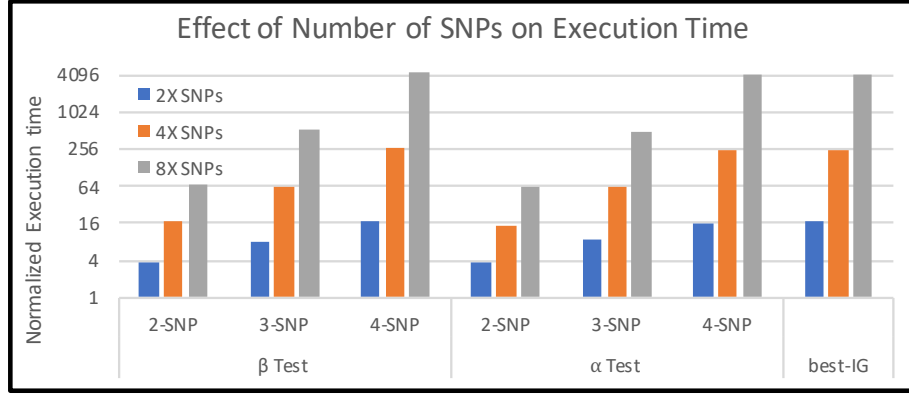
BitEpi: A Fast and Accurate  
Exhaustive Higher-Order Epistasis Search

**Supplementary Data**

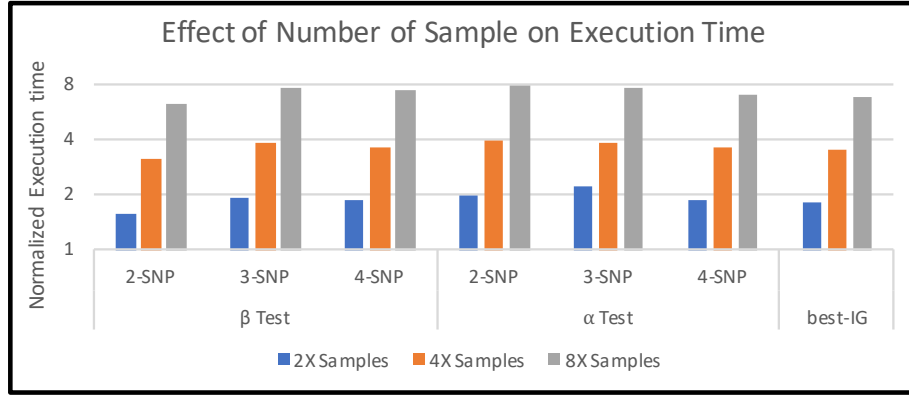
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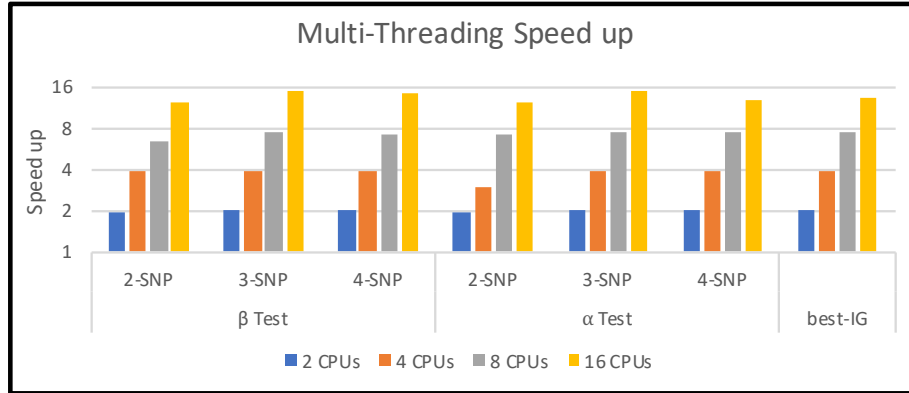
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(a) The effect of number of SNPs on BitEpi execution time.



(b) The effect of number of samples on BitEpi execution time.



(c) The effect of number of threads on BitEpi execution time.

Figure 1: The effect of number of SNPs, samples and threads on BitEpi execution time.

Table 1: BitEpi execution time when the number of SNPs varies in the dataset. The number of samples is 4,000 (2,000 cases and 2,000 controls) in all cases.

| Test                   | Number of SNP | Execution Time (sec) |
|------------------------|---------------|----------------------|
| best<br>test           | 50            | 0.82                 |
|                        | 100           | 13.65                |
|                        | 200           | 207.58               |
|                        | 400           | 3320.27              |
| $\alpha$ Test<br>2-SNP | 5000          | 40.19                |
|                        | 10000         | 155.33               |
|                        | 20000         | 611.36               |
|                        | 40000         | 2423.67              |
| $\alpha$ Test<br>3-SNP | 250           | 8.04                 |
|                        | 500           | 72.97                |
|                        | 1000          | 506.50               |
|                        | 2000          | 4047.00              |
| $\alpha$ Test<br>4-SNP | 50            | 0.82                 |
|                        | 100           | 12.91                |
|                        | 200           | 207.16               |
|                        | 400           | 3327.03              |
| $\beta$ Test<br>2-SNP  | 5000          | 40.19                |
|                        | 10000         | 155.27               |
|                        | 20000         | 688.16               |
|                        | 40000         | 2711.73              |
| $\beta$ Test<br>3-SNP  | 250           | 7.94                 |
|                        | 500           | 63.11                |
|                        | 1000          | 504.49               |
|                        | 2000          | 4034.00              |
| $\beta$ Test<br>4-SNP  | 50            | 0.75                 |
|                        | 100           | 12.59                |
|                        | 200           | 202.91               |
|                        | 400           | 3281.52              |

Table 2: BitEpi execution time when the number of samples varies in the dataset.

| Test                   | Number of SNP | Number of Sample | Execution Time (sec) |
|------------------------|---------------|------------------|----------------------|
| best test              | 200           | 2000             | 115.90               |
|                        | 200           | 4000             | 207.77               |
|                        | 200           | 8000             | 400.76               |
|                        | 200           | 16000            | 785.50               |
| $\alpha$ Test<br>2-SNP | 10000         | 2000             | 79.07                |
|                        | 10000         | 4000             | 155.62               |
|                        | 10000         | 8000             | 310.64               |
|                        | 10000         | 16000            | 618.94               |
| $\alpha$ Test<br>3-SNP | 500           | 2000             | 33.07                |
|                        | 500           | 4000             | 73.08                |
|                        | 500           | 8000             | 125.68               |
|                        | 500           | 16000            | 249.03               |
| $\alpha$ Test<br>4-SNP | 200           | 2000             | 111.88               |
|                        | 200           | 4000             | 207.26               |
|                        | 200           | 8000             | 408.13               |
|                        | 200           | 16000            | 785.06               |
| $\beta$ Test<br>2-SNP  | 10000         | 2000             | 100.42               |
|                        | 10000         | 4000             | 155.53               |
|                        | 10000         | 8000             | 310.31               |
|                        | 10000         | 16000            | 618.24               |
| $\beta$ Test<br>3-SNP  | 500           | 2000             | 32.83                |
|                        | 500           | 4000             | 63.09                |
|                        | 500           | 8000             | 124.77               |
|                        | 500           | 16000            | 247.52               |
| $\beta$ Test<br>4-SNP  | 200           | 2000             | 109.28               |
|                        | 200           | 4000             | 203.11               |
|                        | 200           | 8000             | 392.05               |
|                        | 200           | 16000            | 814.35               |

Table 3: BitEpi execution time when the number of threads varies. The number of samples is 4,000 (2,000 cases and 2,000 controls) in all cases.

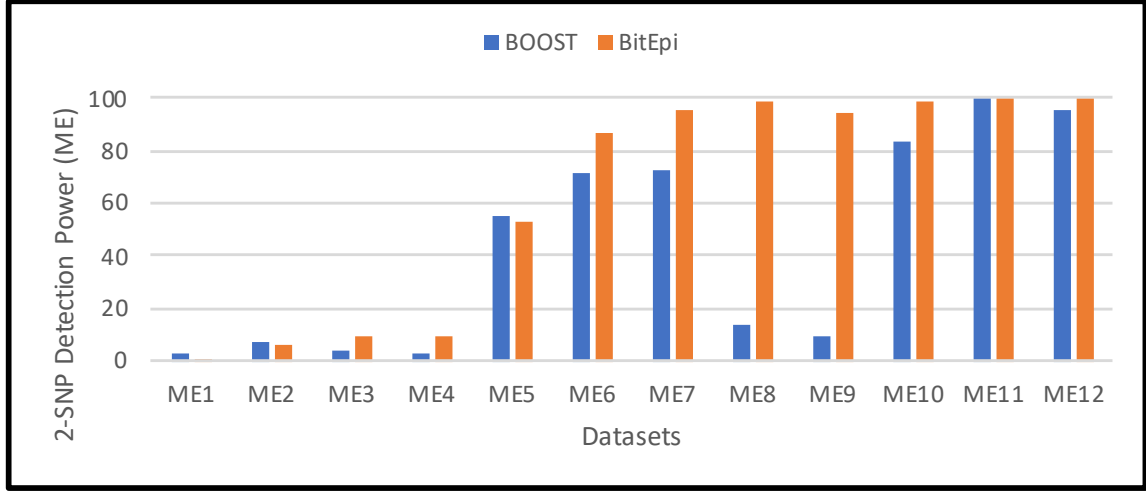
| Test                | Number of SNP | Number of Threads | Execution Time (sec) |
|---------------------|---------------|-------------------|----------------------|
| best Test           | 400           | 1                 | 3158.39              |
|                     | 400           | 2                 | 1589.64              |
|                     | 400           | 4                 | 811.48               |
|                     | 400           | 8                 | 425.12               |
|                     | 400           | 16                | 236.35               |
| $\alpha$ Test 2-SNP | 40000         | 1                 | 2370.38              |
|                     | 40000         | 2                 | 1200.37              |
|                     | 40000         | 4                 | 781.90               |
|                     | 40000         | 8                 | 323.10               |
|                     | 40000         | 16                | 188.89               |
| $\alpha$ Test 3-SNP | 2000          | 1                 | 3844.00              |
|                     | 2000          | 2                 | 1927.50              |
|                     | 2000          | 4                 | 973.27               |
|                     | 2000          | 8                 | 503.19               |
|                     | 2000          | 16                | 255.58               |
| $\alpha$ Test 4-SNP | 400           | 1                 | 3154.43              |
|                     | 400           | 2                 | 1586.92              |
|                     | 400           | 4                 | 806.27               |
|                     | 400           | 8                 | 423.24               |
|                     | 400           | 16                | 244.00               |
| $\beta$ Test 2-SNP  | 40000         | 1                 | 2653.23              |
|                     | 40000         | 2                 | 1341.05              |
|                     | 40000         | 4                 | 685.57               |
|                     | 40000         | 8                 | 405.74               |
|                     | 40000         | 16                | 214.14               |
| $\beta$ Test 3-SNP  | 2000          | 1                 | 3840.00              |
|                     | 2000          | 2                 | 1917.02              |
|                     | 2000          | 4                 | 970.26               |
|                     | 2000          | 8                 | 504.73               |
|                     | 2000          | 16                | 255.69               |
| $\beta$ Test 4-SNP  | 400           | 1                 | 3125.74              |
|                     | 400           | 2                 | 1571.14              |
|                     | 400           | 4                 | 801.53               |
|                     | 400           | 8                 | 425.05               |
|                     | 400           | 16                | 219.61               |

Table 4: Description of epistasis model-simulated with GAMETES and 2-SNP detection power of BOOST and BitEpi for each model. For each model, 100 datasets are generated each with 100 SNPs and 2,000 samples (1,000 case and 1,000 controls). The minor allele frequency of SNPs in each dataset varies between 0.01 and 0.5. MAF1 and MAF2 are the minor allele frequency of the first and second interactive SNPs. Detection power is the number of datasets (out of 100) where the interactive pair is ranked first by the analysis metod.

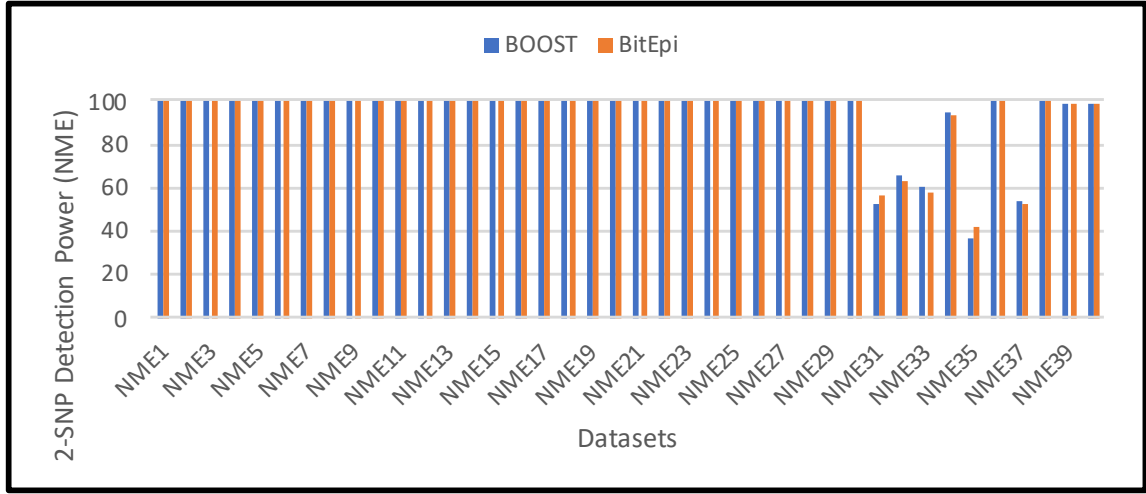
| Model | Model Characteristics |       |       | Detection Power |        |
|-------|-----------------------|-------|-------|-----------------|--------|
|       | Heritability          | MAF1  | MAF2  | BOOST           | BitEpi |
| PM1   | 0.005                 | 0.050 | 0.050 | 10              | 6      |
| PM2   | 0.005                 | 0.050 | 0.250 | 66              | 81     |
| PM3   | 0.005                 | 0.050 | 0.500 | 45              | 55     |
| PM4   | 0.005                 | 0.250 | 0.250 | 68              | 88     |
| PM5   | 0.005                 | 0.250 | 0.500 | 55              | 79     |
| PM6   | 0.005                 | 0.500 | 0.500 | 64              | 82     |
| PM7   | 0.050                 | 0.050 | 0.050 | 70              | 100    |
| PM8   | 0.050                 | 0.050 | 0.250 | 75              | 100    |
| PM9   | 0.050                 | 0.250 | 0.250 | 71              | 100    |
| PM10  | 0.200                 | 0.500 | 0.500 | 75              | 100    |

Table 5: Description of epistasis model-simulated with GAMETES and 3-SNP detection power of MPI3SNP and BitEpi for each model. For each model, 100 datasets are generated each with 100 SNPs and 2,000 samples (1,000 cases and 1,000 controls). The minor allele frequency of SNPs in each dataset varies between 0.01 and 0.5. MAF1, MAF2, and MAF3 are the minor allele frequency of the first, second and third interactive SNPs. Detection power is the number of datasets (out of 100) where the interactive 3-SNP is ranked first by the analysis method.

| Model | Model Characteristics |       |       |       | Detection Power |        |
|-------|-----------------------|-------|-------|-------|-----------------|--------|
|       | Heritability          | MAF 1 | MAF 2 | MAF 3 | MPI3SNP         | BitEpi |
| TM1   | 0.005                 | 0.050 | 0.050 | 0.050 | 0               | 0      |
| TM2   | 0.005                 | 0.050 | 0.250 | 0.500 | 16              | 25     |
| TM3   | 0.005                 | 0.050 | 0.500 | 0.500 | 9               | 16     |
| TM4   | 0.005                 | 0.250 | 0.250 | 0.250 | 13              | 36     |
| TM5   | 0.005                 | 0.250 | 0.250 | 0.500 | 15              | 36     |
| TM6   | 0.005                 | 0.500 | 0.500 | 0.500 | 27              | 52     |
| TM7   | 0.050                 | 0.250 | 0.250 | 0.250 | 100             | 100    |
| TM8   | 0.050                 | 0.250 | 0.250 | 0.500 | 100             | 100    |
| TM9   | 0.050                 | 0.500 | 0.500 | 0.500 | 100             | 100    |



(a) The effect of number of SNPs on BitEpi execution time.



(b) The effect of number of samples on BitEpi execution time.

Figure 2: The effect of number of SNPs, samples and threads on BitEpi execution time.



Table 6: Description of ME epistasis models simulated with GAMETES in [1] and 2-SNP detection power of BOOST and BitEpi for each model. For each model, 100 datasets are generated each with 100 SNPs and 1,600 samples (800 cases and 800 controls). Detection power is the number of datasets (out of 100) where the interactive pair is ranked first by the analysis method.

| Model Identifier<br>(Downloaded Data) | Model | Detection Power |        |
|---------------------------------------|-------|-----------------|--------|
|                                       |       | BOOST           | BitEpi |
| 70                                    | ME1   | 3               | 1      |
| 71                                    | ME2   | 7               | 6      |
| 72                                    | ME3   | 4               | 9      |
| 73                                    | ME4   | 3               | 9      |
| 74                                    | ME5   | 55              | 53     |
| 75                                    | ME6   | 72              | 87     |
| 76                                    | ME7   | 73              | 96     |
| 77                                    | ME8   | 14              | 99     |
| 78                                    | ME9   | 10              | 94     |
| 79                                    | ME10  | 84              | 99     |
| 80                                    | ME11  | 100             | 100    |
| 81                                    | ME12  | 96              | 100    |

Table 7: Description of NME epistasis models simulated with GAMETES in and 2-SNP detection power of BOOST and BitEpi for each model. For each model, 100 datasets are generated each with 100 SNPs and 1,600 samples (800 cases and 800 controls). Detection power is the number of datasets (out of 100) where the interactive pair is ranked first by the analysis method.

| Model Identifier<br>(Downloaded Data) | Model | Detection Power |        |
|---------------------------------------|-------|-----------------|--------|
|                                       |       | BOOST           | BitEpi |
| 0                                     | NME1  | 100             | 100    |
| 1                                     | NME2  | 100             | 100    |
| 2                                     | NME3  | 100             | 100    |
| 3                                     | NME4  | 100             | 100    |
| 4                                     | NME5  | 100             | 100    |
| 5                                     | NME6  | 100             | 100    |
| 6                                     | NME7  | 100             | 100    |
| 7                                     | NME8  | 100             | 100    |
| 8                                     | NME9  | 100             | 100    |
| 9                                     | NME10 | 100             | 100    |
| 15                                    | NME11 | 100             | 100    |
| 16                                    | NME12 | 100             | 100    |
| 17                                    | NME13 | 100             | 100    |
| 18                                    | NME14 | 100             | 100    |
| 19                                    | NME15 | 100             | 100    |
| 25                                    | NME16 | 100             | 100    |
| 26                                    | NME17 | 100             | 100    |
| 27                                    | NME18 | 100             | 100    |
| 28                                    | NME19 | 100             | 100    |
| 29                                    | NME20 | 100             | 100    |

| Model Identifier<br>(Downloaded Data) | Model | Detection Power |        |
|---------------------------------------|-------|-----------------|--------|
|                                       |       | BOOST           | BitEpi |
| 30                                    | NME21 | 100             | 100    |
| 31                                    | NME22 | 100             | 100    |
| 32                                    | NME23 | 100             | 100    |
| 33                                    | NME24 | 100             | 100    |
| 34                                    | NME25 | 100             | 100    |
| 40                                    | NME26 | 100             | 100    |
| 41                                    | NME27 | 100             | 100    |
| 42                                    | NME28 | 100             | 100    |
| 43                                    | NME29 | 100             | 100    |
| 44                                    | NME30 | 100             | 100    |
| 55                                    | NME31 | 52              | 57     |
| 56                                    | NME32 | 66              | 63     |
| 57                                    | NME33 | 60              | 58     |
| 58                                    | NME34 | 95              | 93     |
| 59                                    | NME35 | 37              | 42     |
| 65                                    | NME36 | 100             | 100    |
| 66                                    | NME37 | 54              | 53     |
| 67                                    | NME38 | 100             | 100    |
| 68                                    | NME39 | 99              | 99     |
| 69                                    | NME40 | 99              | 99     |

## References

- [1] Peng-Jie Jing and Hong-Bin Shen. Macoed: a multi-objective ant colony optimization algorithm for snp epistasis detection in genome-wide association studies. *Bioinformatics*, 31(5):634–641, 2014.