

金氧半電容元件 作業 - 112, 9, 19 學號: 1070759 姓名: 蔡明軒

S_i 參數: electron affinity = 4.15 eV, $E_g = 1.12$ eV, $\epsilon_{Si} = 11.9\epsilon_0$, $\epsilon_0 = 8.85 \times 10^{-14}$ F/cm,
常溫下 $kT/q = 0.0259$ V, $n_i = 1.5 \times 10^{10} \text{ cm}^{-3}$, 假設 $E_i = \frac{1}{2}(E_c + E_v)$ 成立

金屬 Al: $\phi_m = 4.1$ eV

SiO_2 參數: $\epsilon_{\text{SiO}_2} = 3.9\epsilon_0$, 厚度 d_{ox} , 假設 $Q_m = Q_{ox} = Q_f = Q_{it} = 0$

給予偏壓 V_G 時 $V_G = V_{FB} + V_{ox} + \psi_s = V_{FB} - \frac{Q_s}{C_{ox}} + \psi_s$

1. MOS(n) 元件 $N_D = 1 \times 10^{14} \text{ cm}^{-3}$, 其 $V_{FB} = -0.382$ (V); $N_D = 1 \times 10^{16} \text{ cm}^{-3}$, 其
 $V_{FB} = -0.263$ (V); MOS(p) 元件, $N_A = 1 \times 10^{14} \text{ cm}^{-3}$, 其 $V_{FB} = -0.838$ (V),
若 $N_A = 1 \times 10^{16} \text{ cm}^{-3}$, 其 $V_{FB} = -0.957$ (V)。

2. MOS(p) 元件, 對於 $N_A = 1 \times 10^{14}$ 及 $N_A = 1 \times 10^{16} \text{ cm}^{-3}$ 兩種情形, 假設
設理論公式在 E_F 接近 E_v 及 E_c 時仍照常引用, 請在同一圖
中繪出 ψ_s 由 $-(0.56 - |\phi_B|)$ 至 $+(0.56 + |\phi_B|)$ 範圍內之 $\log|Q_s|$
對 ψ_s 分布曲線 (六小題計)

3. MOS(p) 元件, $N_A = 1 \times 10^{14} \text{ cm}^{-3}$, 對於 $d_{ox} = 500 \text{ \AA}$ 及 800 \AA 兩種
情形請在同一圖中繪出 ψ_s 由 $-(0.56 - |\phi_B|)$ 至 $+(0.56 + |\phi_B|)$
範圍內之 V_G 對 ψ_s 分布曲線 (六小題計)

4. MOS(p) 元件, $N_A = 1 \times 10^{14} \text{ cm}^{-3}$, $d_{ox} = 800 \text{ \AA}$, 當偏壓使得 S_i
表面達 intrinsic 時, $\psi_s = 0.228$, 此時之 $V_G = -0.5496$ 。

5. MOS(n) 元件, $N_D = 1 \times 10^{14} \text{ cm}^{-3}$, $d_{ox} = 800 \text{ \AA}$, 當偏壓使得 S_i
表面達 intrinsic 時, $\psi_s = -0.228$, 此時之 $V_G = -0.6704$ 。

(請於 112, 9, 26 前將 pdf 檔上傳 NTU COOL 繳交,
逾期不取! 演算過程請一併附上, 標
請填寫答案!)

1.

$$Q_m = Q_{ot} = Q_f = Q_{it} = 0$$

$$\Rightarrow \phi_{ms} = V_{FB}$$

$$\phi_m = 4.1 \text{ (eV)}$$

$$\phi_s = \chi_{si} + \frac{1}{2} E_g - kT \ln \frac{N_D}{n_i}$$

$$\Rightarrow \phi_s = 4.15 + 0.56 - 0.0259 \ln \frac{10^{14}}{1.5 \times 10^{10}}$$

$$\Rightarrow \phi_s = 4.482 \text{ (eV)}$$

$$V_{FB} = \phi_{ms} = \phi_m - \phi_s = -0.382 \text{ (V)}$$

$$N_D = 10^{16} \text{ (cm}^{-3}\text{)}$$

$$\phi_s = 4.15 + 0.56 - 0.0259 \ln \frac{10^{16}}{1.5 \times 10^{10}}$$

$$\Rightarrow \phi_s = 4.363 \text{ (eV)}$$

$$V_{FB} = 4.1 - 4.363 = -0.263 \text{ (V)}$$

$$N_A = 10^{14} \text{ (cm}^{-3}\text{)}$$

$$\phi_s = 4.15 + 0.56 + 0.0259 \ln \frac{10^{14}}{1.5 \times 10^{10}}$$

$$\Rightarrow \phi_s = 4.938 \text{ (eV)}$$

$$V_{FB} = 4.1 - 4.938 = -0.838 \text{ (V)}$$

$$N_A = 10^{16} \text{ (cm}^{-3}\text{)}$$

$$\phi_s = 4.15 + 0.56 + 0.0259 \ln \frac{10^{16}}{1.5 \times 10^{10}}$$

$$\Rightarrow \phi_s = 5.057 \text{ (eV)}$$

$$V_{FB} = 4.1 - 5.057 = -0.957 \text{ (V)}$$

2.

$$N_A = 10^{14}$$

$$\phi_B = E_F - E_i = 0.0259 \ln \frac{N_A}{n_i}$$

$$\Rightarrow \phi_B = -0.228 \text{ (V)}$$

$$N_A = 10^{16}$$

$$\phi_B = 0.0259 \ln \frac{N_A}{n_i} = -0.3474 \text{ (V)}$$

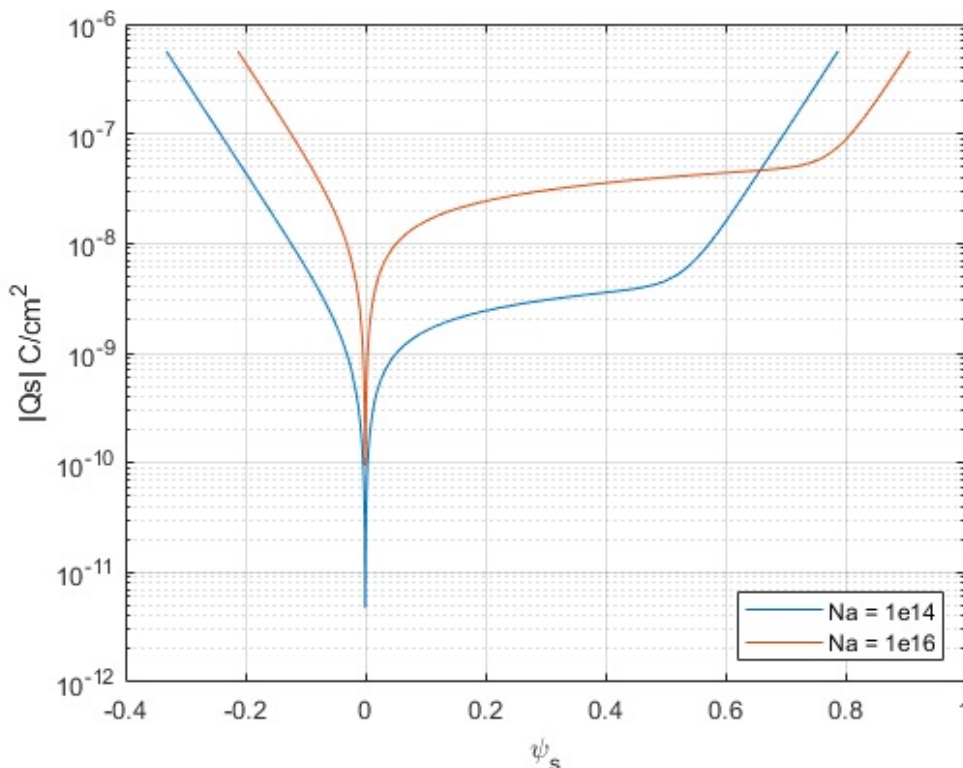
$$\lambda_i = \left[\frac{\epsilon_s kT}{2q n_i} \right]^{0.5} = 0.0024 \text{ (cm)}$$

$$F_s = \text{sign}(u_b - u_s) \frac{kT}{q \lambda_i} F(u_s, u_b)$$

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clear all
% Parameter
eps_si = 11.9 * 8.85 * 10^-14;
eps_sio2 = 3.9 * 8.85 * 10^-14;
ni = 1.5 * 10^10;
K = 1.38 * 10^-23;
T = 300;
KT = 0.0259;
q = 1.6 * 10^-19;
q_phi_m = 4.1;
q_x_si = 4.15;
eg_si = 1.12;
phi_B1 = -log(10^14 / (1.5*10^10)) * 0.0259;
phi_B2 = -log(10^16 / (1.5*10^10)) * 0.0259;
% Set x domain for na1 condition
x1_max = 0.56 + abs(phi_B1);
x1_min = -(0.56 - abs(phi_B1));
x1 = x1_min : x1_max / 1000 : x1_max;
% Formula reference for na2 condition
x2_max = 0.56 + abs(phi_B2);
x2_min = -(0.56 - abs(phi_B2));
x2 = x2_min : x2_max / 1000 : x2_max;
% Formula reference for na1 condition
phi_s1=x1+phi_B1;
us1=phi_s1/KT;
ub1=phi_B1/KT;
% Formula reference for na2 condition
phi_s2=x2+phi_B2;
us2=phi_s2/KT;
ub2=phi_B2/KT;
% Calculate na1 condition
na1 = 1e14;
lambda_p1 = (eps_si * KT / (2 * q * ni))^0.5;
Fs1= sign(ub1-us1) .* (2^0.5) * KT / lambda_p1 .* ((ub1 - us1) * sinh(ub1) - (cosh(ub1) - cosh(us1))).^0.5;
Qs1 = eps_si * Fs1;
% Calculate na2 condition
na2 = 1e16;
lambda_p2 = (eps_si * KT / (2 * q * ni))^0.5;
Fs2 = sign(ub2-us2) .* (2^0.5) * KT / lambda_p2 .* ((ub2 - us2) * sinh(ub2) - (cosh(ub2) - cosh(us2))).^0.5;
Qs2 = eps_si * Fs2;
% Draw plot
semilogy(x1 , abs(Qs1) , x2 , abs(Qs2))
% Plot tag
legend({'Na = 1e14','Na = 1e16'},'Location','southeast')
xlabel('\psi_s');
ylabel('|Qs| C/cm^2');

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3.

```
clear all
% Parameter
eps_si = 11.9 * 8.85 * 10^-14;
eps_sio2 = 3.9 * 8.85 * 10^-14;
ni = 1.5 * 10^10;
K = 1.38 * 10^-23;
T = 300;
KT = 0.0259;
q = 1.6 * 10^-19;
q_phi_m = 4.1;
q_x_si = 4.15;
eg_si = 1.12;
phi_B = -log(10^14 / ni) * 0.0259;
na = 1e14;
% Calculate Vfb
q_phi_s = q_x_si + eg_si/2 + KT * log(na / ni);
Vfb = q_phi_m - q_phi_s;
% Set x domain
x_max = 0.56 + abs(phi_B);
x_min = - (0.56 - abs(phi_B));
x = x_min : x_max / 1000 : x_max;
% Formula reference
phi_s = x + phi_B;
us = phi_s / KT;
ub = phi_B / KT;
% Calculate dox1 condition
dox1 = 5e-6;
Cox1 = eps_sio2 / dox1;
lambda_p1 = (eps_si * KT / (2 * q * ni))^0.5;
Fs1 = sign(ub-us) * (2^0.5) * KT / lambda_p1 * ((ub - us) * sinh(ub) - (cosh(ub) - cosh(us)))^0.5;
Qs1 = eps_si * Fs1;
Vg1 = Vfb - Qs1 / Cox1 + x;
% Calculate dox2 condition
dox2 = 8e-6;
Cox2 = eps_sio2 / dox2;
lambda_p1 = (eps_si * KT / (2 * q * ni))^0.5;
Fs2 = sign(ub-us) * (2^0.5) * KT / lambda_p1 * ((ub - us) * sinh(ub) - (cosh(ub) - cosh(us)))^0.5;
Qs2 = eps_si * Fs2;
Vg2 = Vfb - Qs2 / Cox2 + x;
% Draw plot
hold on
plot(x , Vg1)
plot(x , Vg2)
hold off
legend({'dox = 500 Å', 'dox = 800 Å'}, 'Location', 'southwest')
xlabel('\psi_s');
ylabel('Vg');
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$$\phi_m = 4.1$$

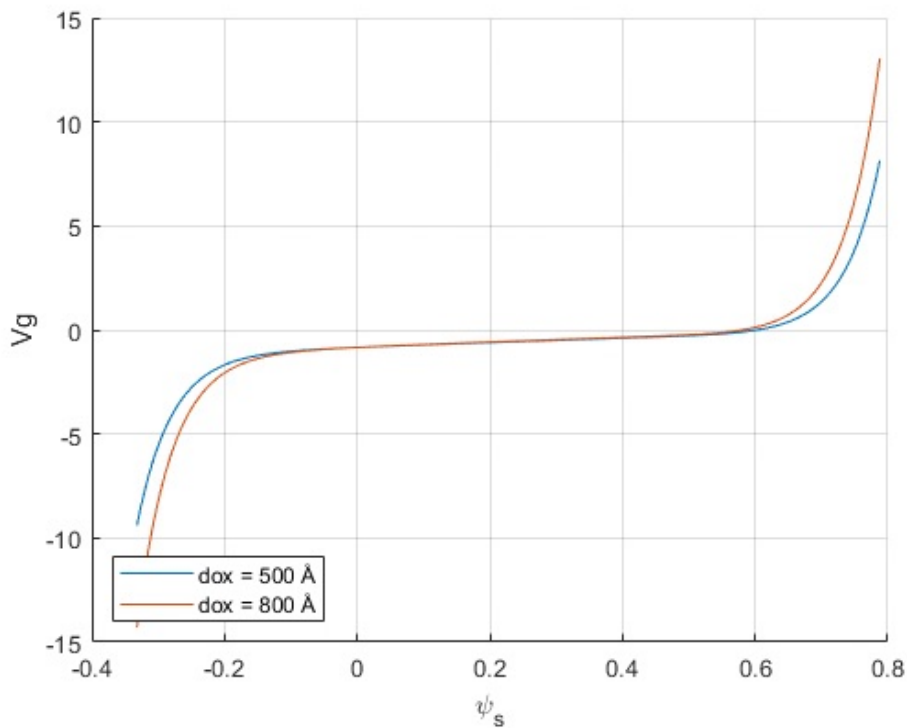
$$\phi_s = 4.15 + 0.56 + kT \ln \frac{N_a}{n_i}$$

$$= 4.9380$$

$$V_{FB} = \phi_m - \phi_s = -0.838$$

$$C_{ox} = \frac{\epsilon_{sio_2}}{d_{ox}} = 6.9 \times 10^{-8} \text{ (dox = 500 Å)}$$

$$4.3 \times 10^{-8} \text{ (dox = 800 Å)}$$



4.

$$C_{ox} = 800 \text{ \AA}$$

$$N_A = 10^{14} \text{ cm}^{-3}$$

$$\text{intrinsic} \Rightarrow \psi_s = |\phi_B|$$

$$\Rightarrow \phi_B = -0.228 \text{ (V)}$$

$$\Rightarrow \psi_s = 0.228 \text{ (V)}$$

$$V_{FB} = -0.838 \text{ (V)}$$

$$\psi_s = \phi_s - \phi_B \Rightarrow \phi_s = 0$$

$$C_{ox} = \frac{\epsilon}{d_{ox}} = \frac{3.9 \times 8.85 \times 10^{-14}}{8 \times 10^{-6}}$$

$$= 4.314 \times 10^{-8}$$

$$U_s = \frac{\phi_s}{kT} = 0$$

$$U_B = \frac{\phi_B}{kT} = -8.031$$

$$F_s = -2.476 \times 10^3$$

$$Q_s = E_s F_s = -2.608 \times 10^{-9}$$

$$V_g = V_{FB} - \frac{Q_s}{C_{ox}} + \psi_s$$

$$= -0.382 + \frac{2.608 \times 10^{-9}}{4.314 \times 10^{-8}} + 0.228$$

$$= -0.5496$$

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5.

$$N_D = 10^{14}$$

$$C_{ox} = 800 \text{ \AA}$$

$$V_{FB} = -0.382$$

$$\psi_s = |\phi_B|$$

$$\phi_B = E_F - E_i = kT \ln \frac{N_D}{n_i}$$

$$\Rightarrow \phi_B = 0.228$$

$$\Rightarrow \psi_s = -0.228$$

$$\phi_B - \phi_s = \psi_s$$

$$\Rightarrow \phi_s = 0$$

$$C_{ox} = 4.314 \times 10^{-8}$$

$$U_s = \frac{\phi_s}{kT} = 0$$

$$U_B = \frac{\phi_B}{kT} = 8.031$$

$$F_s = 2.4759 \times 10^3$$

$$Q_s = E_s F_s = 2.6075 \times 10^{-9}$$

$$V_g = V_{FB} - \frac{Q_s}{C_{ox}} + \psi_s$$

$$\Rightarrow V_g = -0.6704 \text{ (V)}$$

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