

## Example – Machine repair scheduling (revisited)

Same as in the previous case, we have a machine that we use to print money. The condition of this machine can be in one of five states: {new, good, normal, bad, broken}, which naturally deteriorate over time. The amount of money the machine prints depends on its condition. If the machine is not in perfect condition (new), we can schedule a repair, that should put the machine into a better state, or we can buy a new machine. Our task is to come up with a plan of making repairs and buying new machines to maximize our profit, this time over an infinite time period.

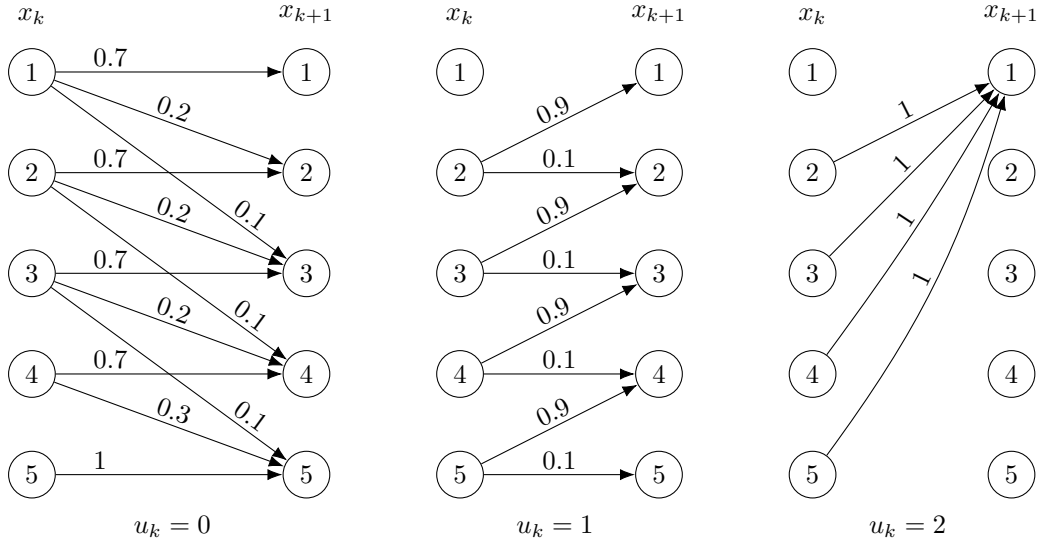
$x_0$ : Initial machine state,  $x_0 \in \{\text{new (1), good (2), normal (3), bad (4), broken (5)}\}$ ,

$\alpha$ : Discount factor,

$x_k$ : State of the machine at time  $k = 1, \dots, N$ ,

$u_k$ : Chosen action at time  $k = 0, \dots, N - 1$ ,  $u_k \in \{\text{do nothing (0), repair (1), buy new (2)}\}$

$w_k$ : Machine deterioration at time  $k$ , depends on  $x_k$  and  $u_k$ .



Amount of money printed ( $g^p$ ) and cost of actions ( $g^a$ ) at  $k$ :

$$g^p(x_k) = \begin{cases} 1, & \text{for } x_k = 1, \\ 0.9, & \text{for } x_k = 2, \\ 0.7, & \text{for } x_k = 3, \\ 0.5, & \text{for } x_k = 4, \\ 0, & \text{for } x_k = 5, \end{cases} \quad g^a(u_k) = \begin{cases} 0, & \text{for } u_k = 0, \\ -0.4, & \text{for } u_k = 1, \\ -1, & \text{for } u_k = 2. \end{cases}$$

Profit at time  $k$ :  $g_k(x_k, u_k) = g^p(x_k) + g^a(u_k)$

**Assignment:** Compute the optimal control for  $x_0 = 1, \alpha = 0.9$ , i.e., the one that minimizes

$$J_\pi(x_0) = \lim_{N \rightarrow \infty} E_{w_0, w_1, \dots} \left\{ \sum_{k=0}^{N-1} \alpha^k g(x_k, \mu_k(x_k), w_k) \right\}$$

by

- using the value iteration algorithm
- using the policy iteration algorithm