Searching

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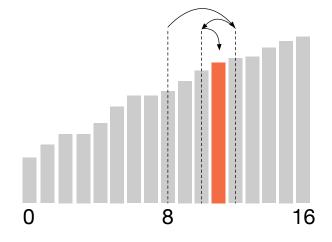
Common searching/membership strategies

- linear: scan data structure looking for element(s)
- binary search: if array and sorted, split recursively in half
- binary search tree: subtree to left has elements less than current node and subtree to the right has elements greater than
- hash table: function maps key to bucket, linear search in bucket; recall search index project from MSDS692; for word search, not arbitrary string search in document(s)
- state machines (graphs)

Binary search (review sort of)

- If we know data is sorted, we can search much faster than linearly
- Means we don't have to examine every element even worst-case

```
def binsearch(a,x):
    left = 0; right = len(a)-1
    while left<=right:
        mid = int((left + right)/2)
        if a[mid]==x: return mid
        if x < a[mid]: right = mid-1
        else: left = mid+1
    return -1</pre>
```





Compare to (tail-)recursive version

```
def binsearch(a,x,left,right):
    if left > right: return -1
    mid = (left + right)//2
    if a[mid]==x: return mid
    if x < a[mid]:
        return binsearch(a,x,left,mid-1)
    else:
        return binsearch(a,x,mid+1,right)</pre>
```

```
left = 0; right = len(a)-1
while left<=right:
    mid = (left + right)//2
    if a[mid]==x: return mid
    if x < a[mid]: right = mid-1
    else: left = mid+1</pre>
Bracket region with element

Bracket region with
```

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String matching

- **Problem**: Given a document of length n characters and a string of length m, find an occurrence or all occurrences
- Brute force algorithm is O(nm), but theoretical best case algorithm exists for O(n + m)
- Exercise: Describe brute force algorithm

Hash searches

- First, note that two equal strings have same hash code so we can compare int codes quickly even for huge strings
- Rabin-Karp* algorithm uses hash function to speed up but still O(nm) worst-case; works for any substring not just words
- Idea: h = hash search string s; compute hash for doc[i:i+m] and compare to h; if same, compare s to doc[i:i+m], return if found; move i from 0 to n-m
- Key is to avoid comparing strings unless the hash codes match

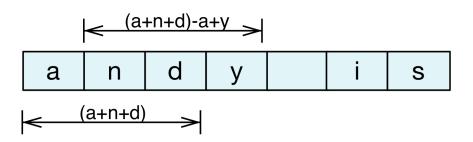
Rabin-Karp (almost)

```
def hash(s:str)->int:
    return sum(ord(c) for c in s)
```

See searching notebook



Issues

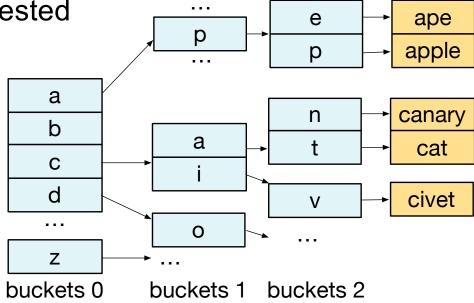


- Naïve hash(doc[i:i+m]) is O(m) so use rolling hash:
 - next hash is old hash minus doc[i] plus doc[i+m]
 - drop old one off, add in new char (see improved search() in notebook):
 hdoc = hdoc ord(doc[i]) + next # roll it!
- What about finding all occurrences?
- What if search string s is very long? Could get expensive.
- Can we do better than O(nm) or even O(n+m) algorithms?
- Yes. I claim we can search for strings in doc in O(m) if we prepare a proper side data structure and you let me search for words instead of arbitrary strings
- How is this possible?!

Revisit recursive bucket sort

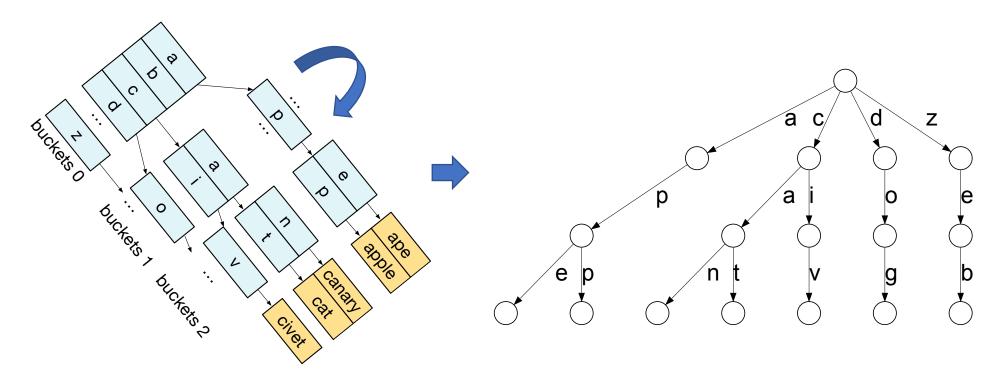
 Break up doc into words, make nested bucket structure as before

- To find a word, use s[i] to navigate and find final "leaf" with list of words with same prefix, linearly search leaf
- The key tells us how to navigate
- How long does it take to find s for n=len(doc), m=len(s)?
 T(n,m) = m





"Tries" or Prefix Trees



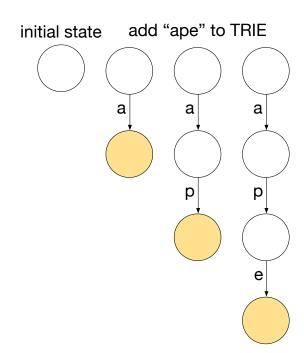
Convert buckets to nodes and rotate: we get a tree!



Adding string s to TRIE

- TRIE can hold a big set of words and we can search for a word superfast
- Note: Now that we're not sorting, order of edges is not important; can use dict()
- Starting at the root, add edge labeled with s[0] pointing to new node
- Traverse edge to child root.child[s[0]] and add subtree for s[1:] to that child
- Recurse until out of chars in string s

class TrieNode:
 def __init__(self):
 self.edges = {}



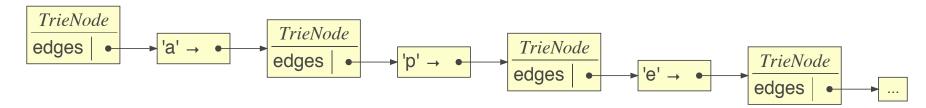


Construction

```
class TrieNode:
   def __init__(self):
       self.edges = {}
```

add(root, "ape")

```
def add(p:TrieNode, s:str, i=0) -> None:
    if i>=len(s): return
    if s[i] not in p.edges:
        p.edges[s[i]] = TrieNode()
    add(p.edges[s[i]], s, i+1)
```



Note that nodes have no values, edges contain the letters

Searching a Trie

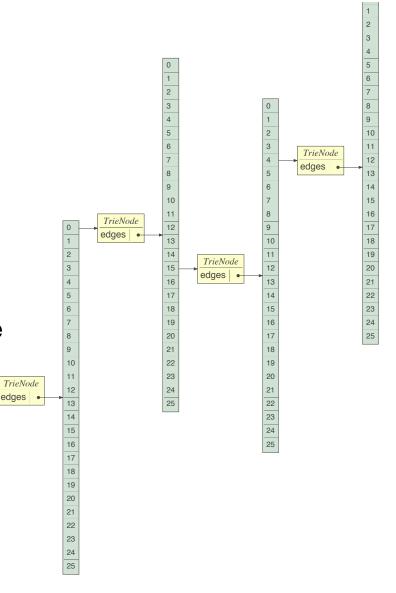
(was in a "big internet company" interview)

- Return true if s is prefix of word in Trie or full word in Trie
- Note that the search depends on <u>len(s)</u> NOT num words n in the vocabulary!!!

```
def search(root:TrieNode, s:str, i=0) -> bool:
    p = root
    while p is not None:
        if i>=len(s): return True
        if s[i] not in p.edges: return False
        p = p.edges[s[i]]
        i += 1
    return True
```

Dictionaries are O(1) but...

- ...slower than array access via perfect hash function f(c) = ord(c) - ord('a')
- But we use 26 slots even for one edge
- How can we reduce memory costs?
 - Many nodes will have just one outgoing edge so we can optimize for that case with single pointer instead of an array
 - Switch to 26-element edge array if we need more than one edge



Exercise: Brute force dictionary search

- Load words from /usr/share/dict/words file (one per line) into list
- Search for each word in list of words; what is complexity?
- This takes almost 5 minutes on my fast computer. ugh

Exercise: Build Trie from dictionary of words

- From searching notebook, get Trie implementation
- Add each word to a trie, which takes about 6s on my machine
- Search the trie for each of 235,886 words; takes 0.75s for me!!
- Rejoice in your new super powers
- Cool interview question/task: How can you do fast spell checking on big documents?

Exercise: find all words starting with prefix

- Create a trie again from the word list
- Write a function that prints all words in trie that begin with a specific prefix like "app"; it should get "apple", "application", ...
- Idea: trace prefix into trie, reaching specific non-leaf node p; find all reachable leaves; track string as recursion parameter for each path; print the string when you reach a leaf

Exercise: Build a suffix tree

 Simple: create trie from reversed strings or modify add() method to walk backwards through string

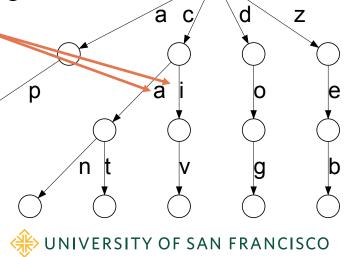
Exercise: Given misspelled words off by 1 letter only, find all possible words

- Trace word into trie until no edge exists for s[i]; this is node p
- Get list of words reachable from each node targeted by p starting with s[i+1]

• E.g., "cxt" would get to p=root.edges['c'] target and fail

• Find "t" from p.edges['a'] and p.edges['i']

• We only find "t" matches via 'a' to get "cat"



Summary

- Lots of ways to search beyond linear and binary search
- String searching has some really efficient solutions such as Rabin-Karp; idea is to compare hash codes before doing string comparisons and do a rolling hash for the document substrings
- If we are willing to build a graph data structure, the TRIE is pretty hard to beat complexity and performance; looking up a word in the TRIE is O(m) for m character string!
- TRIE is just a nested pigeonhole sort turned into a graph
- Useful as prefix and suffix trees; can find even misspelled words