Number Theory - Prime numbers

Prime Numbers

- p is prime if 1 and p are its only divisors e.g 3, 5, 7, 11 ...
- p and q are relatively prime (a.k.a. coprime) if gcd(p,q) = 1e.g gcd(4,5) = 1
- There are infinitely many primes

Euler-Fermat Theorem

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If n = p \cdot q and z = (p-1) \cdot (q-1)
and a such that a and n are relative primes
Then a^z \equiv 1 \pmod{n}
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Computational Complexity

Easy problems with prime numbers

- Generating a prime number p
- Addition, multiplication, exponentiation
- Inversion, solving linear equations

Hard problem with prime numbers

• Factoring primes e.g. given n find p and q such that $n = p \cdot q$