

Stereo Calibration in Opencv

유용길

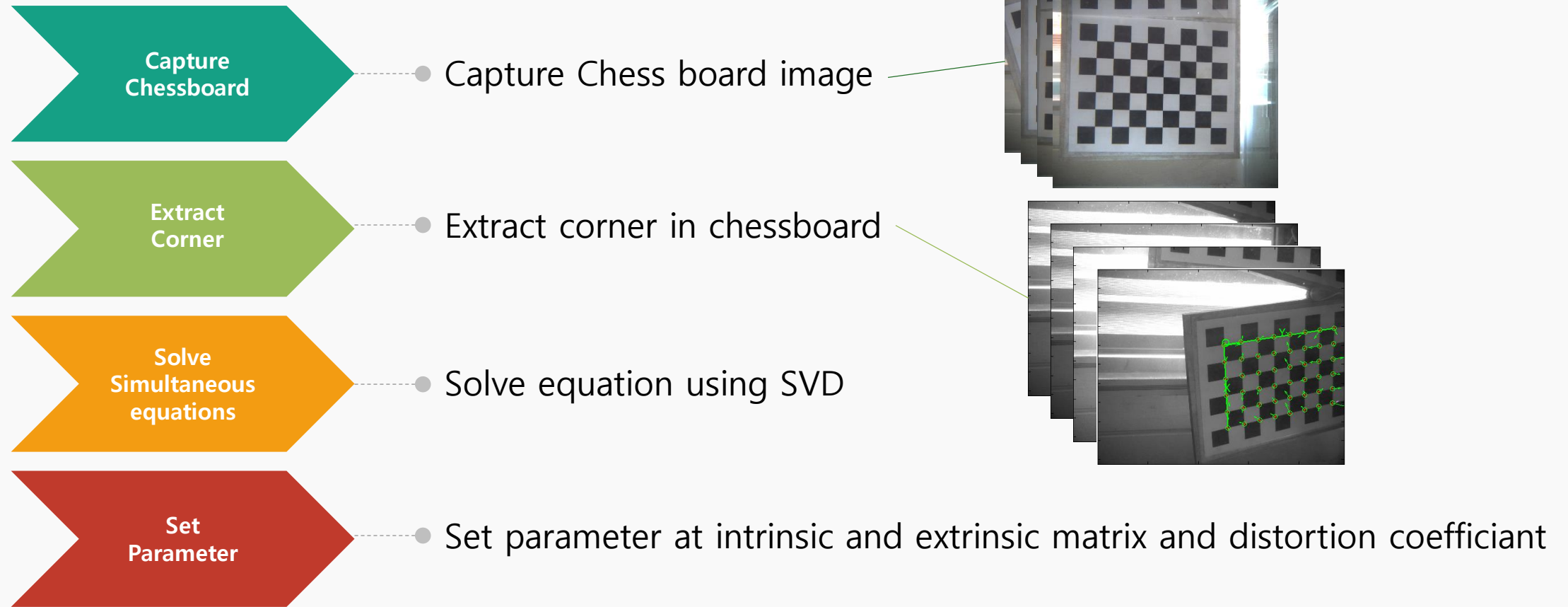
ISL Image System Laboratory

CONTENTS



- Stereo Calibration
- Singular Value Decomposition
- Solve simultaneous equations
- Stereo Calibration in OpenCV
- Another consideration

Stereo Calibration



Singular Value Decomposition

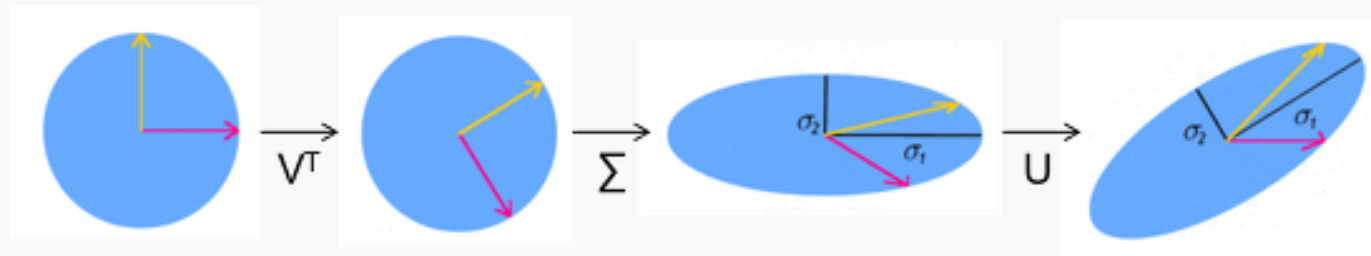
Orthogonal matrix

Diagonal matrix

Orthogonal matrix

$$A = U \Sigma V^T = \begin{bmatrix} u_1 & u_2 & \cdots & u_m \end{bmatrix} \begin{bmatrix} \sigma_1 & 0 & \cdots & 0 \\ 0 & \sigma_2 & \ddots & 0 \\ 0 & \ddots & \ddots & 0 \\ 0 & 0 & \cdots & \sigma_k \end{bmatrix} \begin{bmatrix} v_1^T \\ v_2^T \\ \vdots \\ v_{n1}^T \end{bmatrix}$$

Singular Value of A



Solve Simultaneous equations

$$By = c$$

$$\begin{bmatrix} B & | & c \\ 0 & 1 \end{bmatrix} \begin{bmatrix} y \\ - \\ 1 \end{bmatrix} = Ax = 0$$

02

$$V^T = \begin{bmatrix} v_1^T \\ v_2^T \\ \vdots \\ v_n^T \end{bmatrix}$$

04

Convert Homogeneous
Format

Singular Value
Decomposition

Extract V column

Solve equations

01

$$A = U \Sigma V^T$$

03

$$x = v_n^T$$

Solve Simultaneous equations

$$Ax = 0 = U \Sigma V^T x$$

$$Q = \text{Orthogonal Matrix}$$

$$\|Qa\| = \|a\|$$

$$\|x\| = 1$$

$$\|U \Sigma V^T x\| = \|\Sigma V^T x\|$$

$$\|x\| = \|V^T x\|$$

$$y = V^T x$$

$$\left\{ \begin{array}{l} \|\Sigma y\| = 0 \\ \|y\| = 1 \end{array} \right.$$

$$\left\{ \begin{array}{l} \|\Sigma y\| \approx 0 \\ \|y\| = 1 \end{array} \right.$$

$$\Sigma = \text{Diagonal Matrix}$$

$$\Sigma = \begin{bmatrix} \sigma_1 & 0 & \cdots & 0 \\ 0 & \sigma_2 & \ddots & 0 \\ \vdots & \ddots & \ddots & \vdots \\ 0 & 0 & \cdots & \sigma_k \end{bmatrix}$$

$$\sigma_1 > \sigma_2 > \cdots > \sigma_k$$

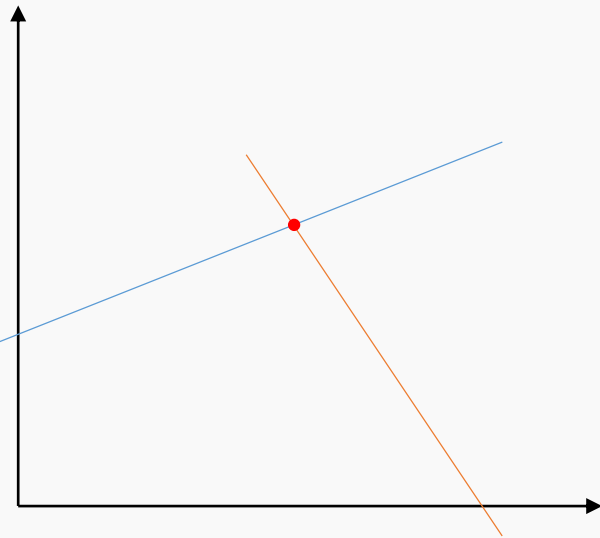
$$y = (0, 0, \dots, 1)^T$$

$$Vy = x$$

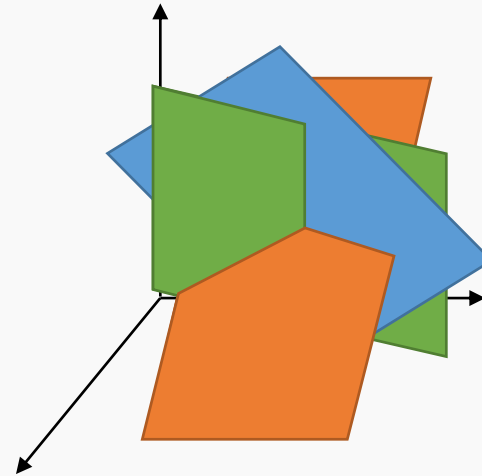
$$x = v_n^T$$

Solve Simultaneous equations

2-dimensional



3-dimensional



Stereo Calibration in OpenCV

```
stereoCalibrate(vObjectPoints,  
               vImagePoints[0], vImagePoints[1],  
               MCameraMatrix[0], MDistortionCoef[0],  
               MCameraMatrix[1], MDistortionCoef[1],  
               SImageSize, MR, MT, ME, MF,  
               CALIB_RATIONAL_MODEL,  
               TermCriteria(TermCriteria::COUNT+TermCriteria::EPS, 100, 1e-5));
```

Corner information

Image size

Extrinsic Matrix

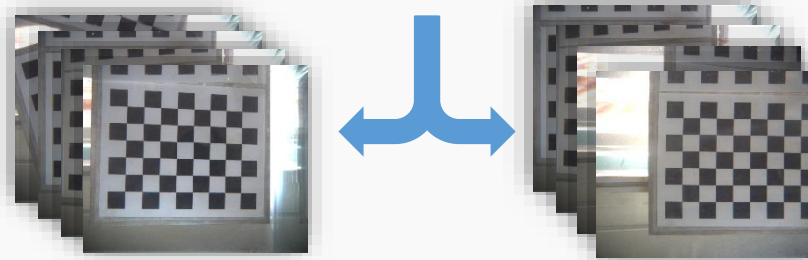
Intrinsic Matrix

Besides the stereo-related information, the function can also perform a full calibration of each of two cameras. However, due to the high dimensionality of the parameter space and noise in the input data, the function can diverge from the correct solution. If the intrinsic parameters can be estimated with high accuracy for each of the cameras individually (for example, using `calibrateCamera`), you are recommended to do so and then pass `CV_CALIB_FIX_INTRINSIC` flag to the function along with the computed intrinsic parameters. Otherwise, if all the parameters are estimated at once, it makes sense to restrict some parameters, for example, pass `CV_CALIB_SAME_FOCAL_LENGTH` and `CV_CALIB_ZERO_TANGENT_DIST` flags, which is usually a reasonable assumption.

Stereo Calibration in OpenCV

01

Capture stereo chessboard image.



02

Calibrate each camera and estimate two intrinsic matrix.

MCameraMatirx[0]
Mdistortcoef[0]

MCameraMatirx[1]
Mdistortcoef[1]

03

Stereo Calibrate using intrinsic matrix estimated step1 with fix intrinsic option.

Another consideration

01

Mask size

- Mask size unit is pixel.
- Mask size adjustment consider image size

02

Find chessboard corner option

- Don't use **CV_CALIB_CB_ADAPTIVE_THRESH** option.
- Process can fall into infinite loop.

03

Reduce parameter

- First, estimate intrinsic matrix each camera.
- Then, estimate extrinsic matrix using fix intrinsic matrix option.