## **CMPT 423/820**

# **Assignment 1 Question 4**

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In this question, we'll do a little more work with Numpy, and we'll combine this with a bit of review from Lecture 02 -- Probability. Numpy can do the calculations here, but you the programmer have to manage really tiny details about the NDArray data structure. It's not ideal for convenient work with discrete probability distributions, but it is a little instructive on the use of Numpy.

#### **Tasks**

On Slide 18 of Lecture 02, there is a Joint Probability Distribution on 2 random variables A and W. This JPD will be the basis for some Numpy calculations. In parts 4 and following, below, the exercises create a new JPD \$P 2(AW); this is not supposed to be equal to the JPD from part 1.

1. Define a NDArray to store the numeric values of the JPD.

```
In [10]: import numpy as np

# based on Lecture 02, page 16
    jpd = np.array([[0.144, 0.02, 0.016, 0.02], [0.576, 0.08, 0.064, 0.08]])
    print('P_1(AW):\n', jpd)

P_1(AW):
    [[0.144 0.02 0.016 0.02]
    [0.576 0.08 0.064 0.08]]
```

- 1. Using the Numpy method sum(), do the following:
  - A. Display the sum of all the values in the JPD. It should be (very close to) 1.
  - B. Display the marginal P(W) as an NDArray obtained from the JPD using sum().
  - C. Display the marginal P(A) as an NDArray obtained from the JPD using sum().

1. Using Numpy methods, show that A and W are in fact independent, that is  $P_1(AW) = P(A)P(W)$ 

```
In [12]: # matrix multiplication of P(A)*P(W)
product_aw_1 = np.matmul(pa.reshape(2,1), pw.reshape(1,4))
print('The product of P(A)P(B) is: \n', product_aw_1)

print()

# checking equality to original JPD
print('Does JPD P(AW) equals to P(A)P(W)?', np.array_equal(jpd, product_aw_1))

The product of P(A)P(B) is:
   [[0.144 0.02 0.016 0.02 ]
   [0.576 0.08 0.064 0.08 ]]

Does JPD P(AW) equals to P(A)P(W)? True
```

1. Define a NDArray for a new conditional  $P(A|W) \neq P(A)$ . Choose your own values here.

```
In [13]: # considering keeping old marginal on W
         my jpd = np.array([[0.15, 0.03, 0.02, 0.05], [0.57, 0.07, 0.06, 0.05]])
         # checking my array to sum to 1
         print('Sum of all the values in my JPD=', np.sum(my_jpd))
         # checking P(A|W) != P(A) by P(AW)!=P(A)P(W)
         my pw = np.sum(my jpd, axis = 0)
         my_pa = np.sum(my_jpd, axis = 1)
         my product aw = np.matmul(my pa.reshape(2,1), my pw.reshape(1,4))
         print('Does P1(AW) equals to P(A)P(W) for my JPD?', np.array equal(my jp
         d, my product aw))
         # checking P(A|W) != P(A) by comparing P(A|W) and P(A)
         # P(A|W) by dividing each row of my jpd to P(W) value columnwise
         pw = pw.reshape(1,4)
         paw conditional = np.true divide(my jpd, pw)
         # calculating whether P(A|W)-P(A) is all zeros
         independence difference = (paw conditional - pa.reshape(2,1))
         print('Does P1(A|W) equals to P(A) for my JPD?', np.count_nonzero(indepe
         ndence difference) == 0)
```

1. Using Numpy methods, calculate the new JPD  $P_2(AW) = P(A|W)P(W)$  (keep the old marginal on W). Note: we'll use this new JPD in some of the parts that follow.

```
In [14]: # P(A/W) by dividing each row of my_jpd to P(W) value columnwise
    pw = pw.reshape(1,4)
    paw_conditional = np.true_divide(my_jpd, pw)

# P2(AW) = P(A/W)P(W)
    p2_aw = paw_conditional * pw
    print('The new JPD P2(AW):\n', p2_aw)

print()

# checking equality to original JPD
    print('Does JPD P2(AW) equals to P(A|W)P(W)?', np.array_equal(my_jpd, p2_aw))

The new JPD P2(AW):
    [[0.15 0.03 0.02 0.05]
    [0.57 0.07 0.06 0.05]]

Does JPD P2(AW) equals to P(A|W)P(W)? True
```

1. Using Numpy methods, calculate the conditional P(W|A) from the new JPD.

1. Using Numpy methods, show that Bayes' Rule is true (for the new JPD):

$$P(W|A) = \frac{P(A|W)P(W)}{P(A)}$$

```
In [16]: # P(A/W) by dividing each row of my_jpd to P(W) value columnwise
    paw_conditional = np.true_divide(my_jpd, pw)

# calculating Bayes' rule right side
    bayes_right = (paw_conditional * pw)/my_pa

print('Is Bayes Rule true?', np.array_equal(pwa_conditional, bayes_right
))
```

Is Bayes Rule true? True

1. Produce a Boolean NDArray showing which values of the new JPD are greater than the old JPD  $P_1(AW)$ .

1. Using Numpy methods, calculate the number of values in the new JPD that are smaller than the old JPD  $P_1(AW)$ .

```
In [18]: small_count = np.sum(np.less(jpd,p2_aw))
    print('The number of values in the new JPD that are smaller than the old
    JPD is', small_count)
```

The number of values in the new JPD that are smaller than the old JPD i s  $4\,$ 

#### What to hand in

Your version of this notebook named A1Q4.pdf, containing completed work above, and your name and student number at the top.

### **Evaluation:**

• 10 marks: Your answers show that you have basic mastery of Numpy.