

The 2020 ICPC Vietnam Southern Provincial Programming Contest University of Science, VNU-HCM October 25, 2020



Problem G Exotic Convolution

Time Limit: 1 seconds

Memory Limit: 512 megabytes

You are given a binary three-dimensional array t[n][3][3], where t[i][a][b] = t[i][b][a], and two integers u and v where $0 \le u, v < 3^n$.

In base 3, u and v are represented as:

$$u = a_0 + a_1 \cdot 3^1 + \dots + a_{n-1} \cdot 3^{n-1}$$
$$v = b_0 + b_1 \cdot 3^1 + \dots + b_{n-1} \cdot 3^{n-1}$$

where $0 \le a_i, b_i < 3$.

Let define the function f as follows:

$$f(u, v) = t[0][a_0][b_0] + t[1][a_1][b_1] \cdot 2^1 + \dots + t[n-1][a_{n-1}][b_{n-1}] \cdot 2^{n-1}$$

It is straight-forward to show that $0 \le f(u, v) < 2^n$.

Your task is to calculate the array c, defined as follows:

$$c_i = \sum_{f(u,v)=i} a_u \cdot b_v$$

Input

The first line contains n ($0 \le n \le 11$).

The next n lines of the input represents the binary array t. The i^{th} line contains 9 integers:

$$t[i-1][0][0], t[i-1][0][1], t[i-1][0][2], t[i-1][1][0], t[i-1][1][1],$$

$$t[i-1][1][2]$$
, $t[i-1][2][0]$, $t[i-1][2][1]$, $t[i-1][2][2]$, separated by spaces.

It is guaranteed that all elements of t are either 0 or 1, and t[i][x][y] = t[i][y][x].

The next line contains 3^n space-separated integers: $a_0, a_1, \ldots, a_{3^{n-1}}$. It is guaranteed that $0 \le a_i \le 10^9$.

The next line contains 3^n space-separated integers: $b_0, b_1, \ldots, b_{3^{n-1}}$. It is guaranteed that $0 \le b_i \le 10^9$.

Output

Print 2^n space-separated integers on a single line: $c_0, c_1, \ldots, c_{2^n-1}$ modulo $10^9 + 7$.



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Sample Input

Sample Output

1	72 24
0 0 0 0 0 0 0 1	
0 0 6	
4 8 4	