Quick Sort

Divide And Conquer

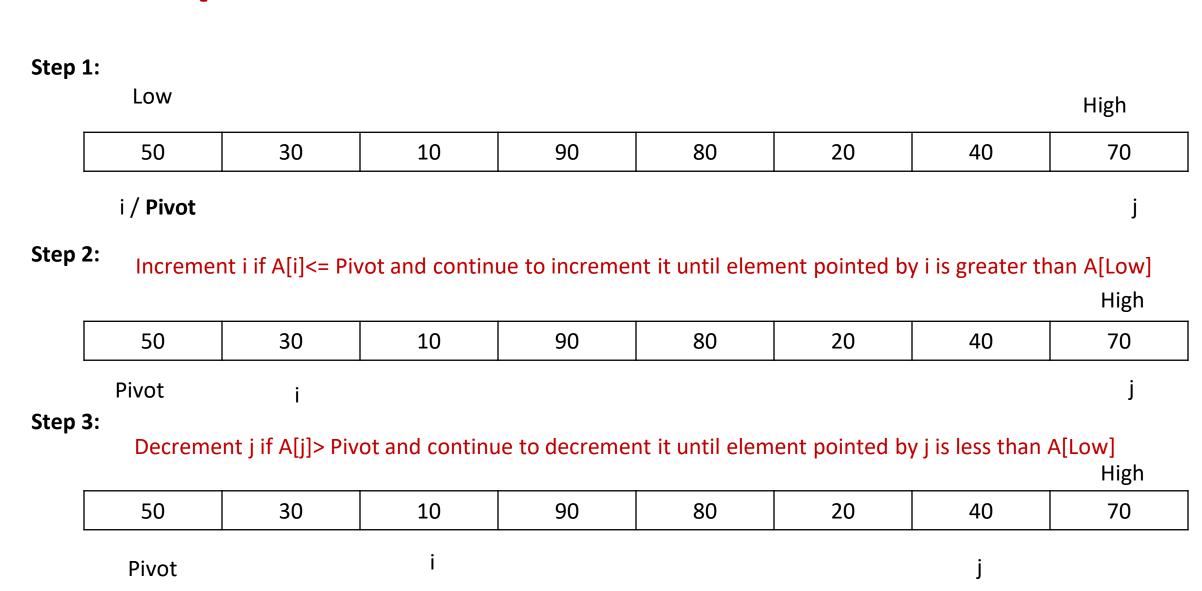
Module 2

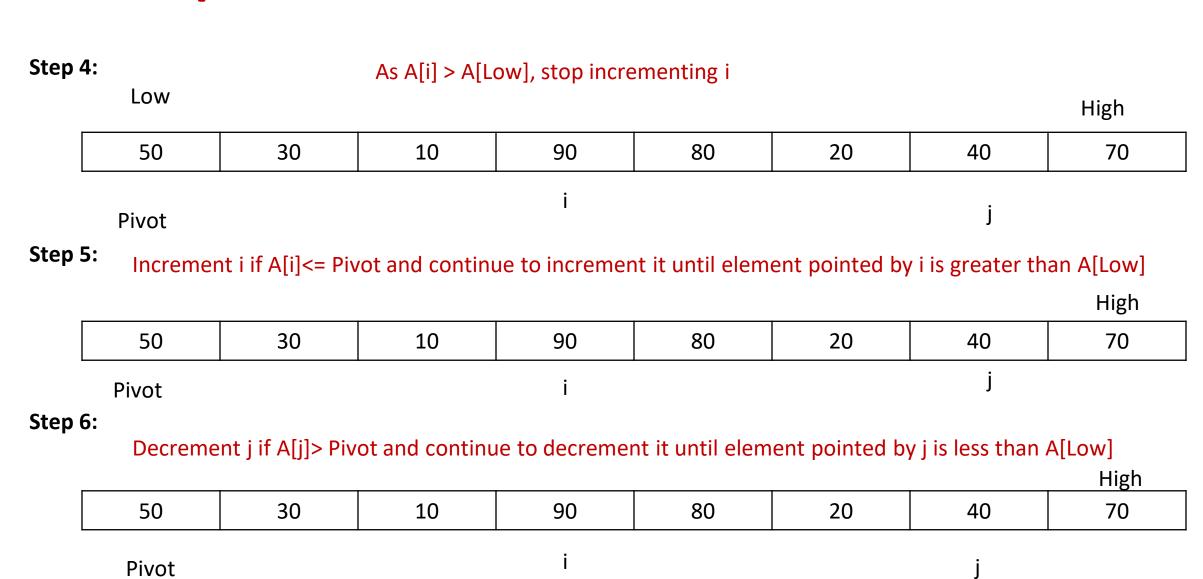
Quick Sort

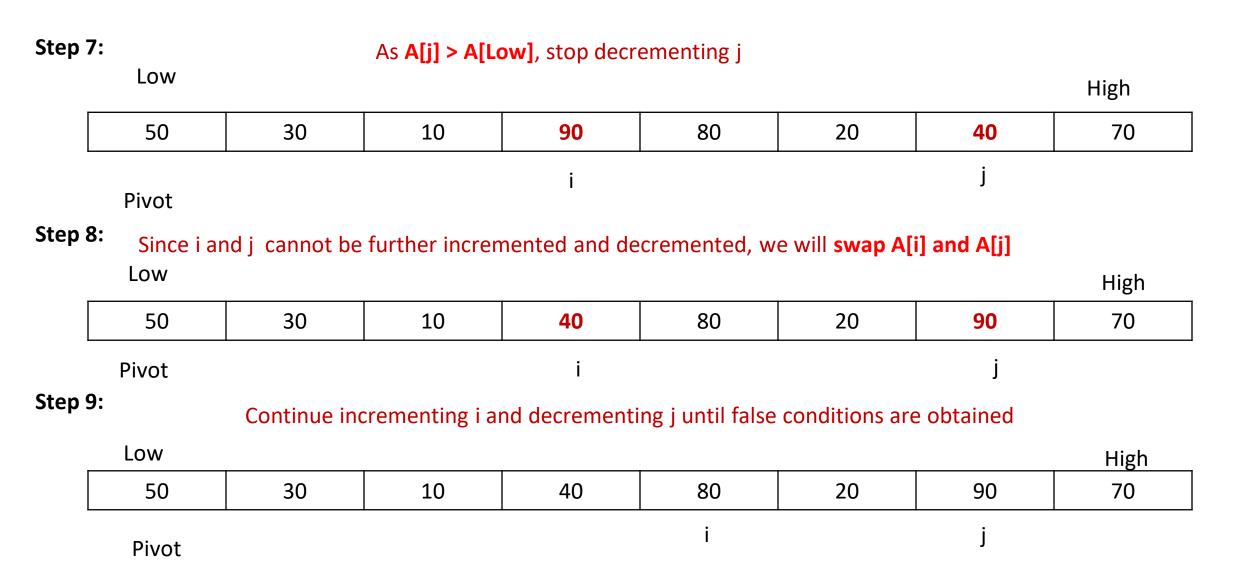
- Quick Sort uses Divide and Conquer Strategy.
- There are three steps:

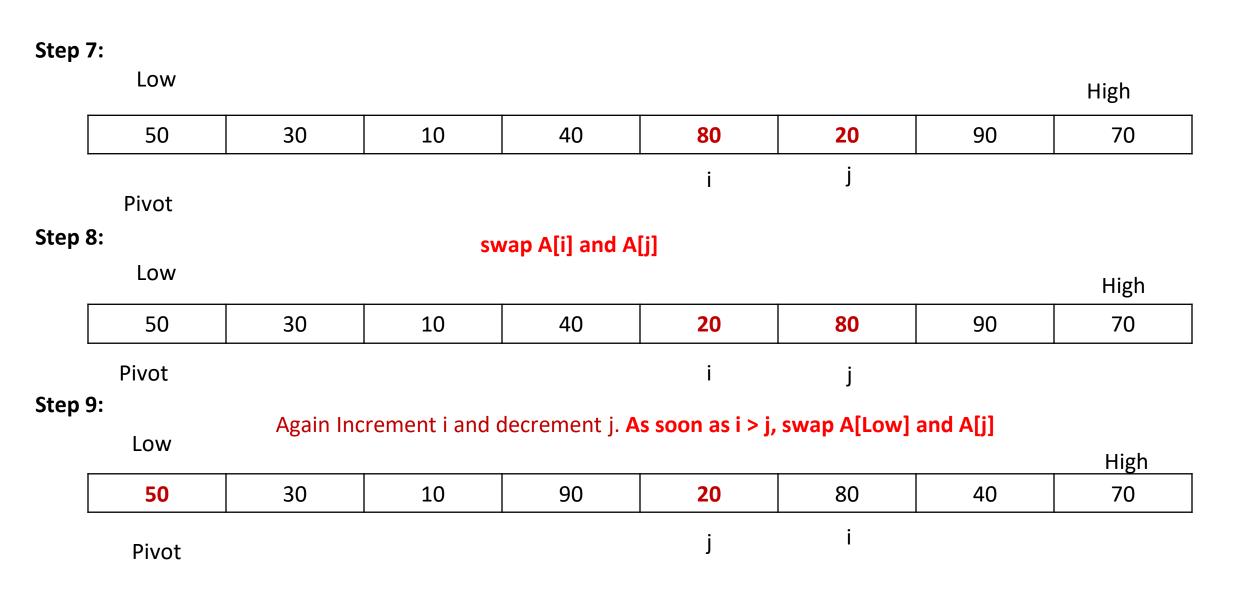
1. Divide:

- Splits the array into sub arrays.
- Splitting of array is based on pivot element.
- Each element in left sub array is less than and equal to middle (pivot) element.
- Each element in right sub array is greater than the middle (pivot) element.
- 2. Conquer: Recursively sort the two sub arrays
- **3. Combine:** Combine all sorted elements in a group to form a list of sorted elements.







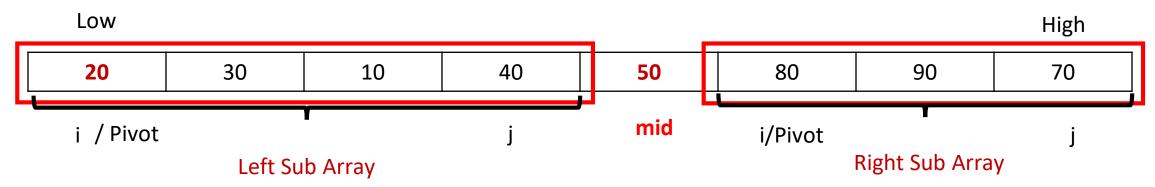


swap A[Low] and A[j]

| Low | | | | Pivot | | | High |
|-----|----|----|----|-------|----|----|------|
| 20 | 30 | 10 | 40 | 50 | 80 | 90 | 70 |
| | | | | i | i | | |

Step 11:

Step 10:



Algorithm

```
Algorithm QuickSort(A[0...n], low, high)
{
    if(low<high) then
    mid ← partition(A[low...high])
    QuickSort(A[low...mid-1])
    QuickSort(A[mid+1...high])
}</pre>
```

```
Algorithm Partition(A[0...n], low, high)
        pivot←A[low];
        i ← low;
        j ← high+1;
       while(i ≤ j)do
                while(A[i] ≤ pivot)do
                { i++;}
                while(A[j] ≥ pivot)do
                { j--;}
                if(i \le j) then
                        swap(A[i],A[j])
        swap(A[low],A[j])
        return j;
```

1. Best Case:

- If array is partitioned at the mid
- The Recurrence relation for quick sort for obtaining best case time complexity.

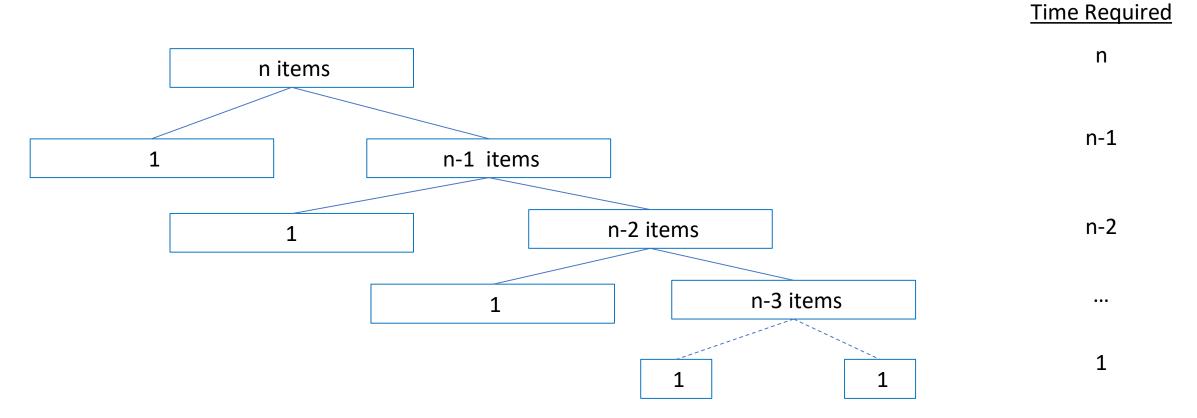
Using Master Theorem:

$$T(n) = 2 * T(n/2) + cn$$

$$T(n) = \Theta(nlogn)$$

2. Worst Case:

- If pivot is a maximum or minimum of all the elements in the sorted list.
- This can be graphically represented as follows



2. Worst Case:

- If pivot is a maximum and minimum of all the elements in the sorted list.
- The Recurrence relation for quick sort for obtaining best case time complexity.

Average Case:

- For any pivot position i; where $i \in \{0,1,2,3...n-1\}$
 - Time for partition an array: cn
 - Head and Tail sub-arrays contain i and n-1-i items.
 - So,

$$T(n) = T(i) + T(n-1-i) + cn$$

Average running time for sorting:

$$T(n) = \frac{1}{n} \sum_{i=0}^{n-1} (T(i) + T(n-1-i)) + cn$$

Proof & Calculation