

1.)

1.) It is *lossy* compression. No you could not recover the original image from the compressed one. You have lost information.

2.) My image has  $N = 46800$  vectors of length  $D=3$ , and number of bits per scalar  $C = 8$ .

This image takes up some function of  $(N \cdot D \cdot C)$  space.  $\rightarrow O(NDC) \rightarrow 46,800 \cdot 3 \cdot 8 = 1.1$  mega bits

The compressed image has  $N=46,800$  vectors of length  $D=3$ , and number of bits per scalar  $C=8$  and number of clusters  $K=8$ .

Compressed image takes up  $O(N \log_2 K + KDC)$  bits.  $\rightarrow 46,800 \cdot 3 + 8 \cdot 8 \cdot 3 \rightarrow 140592$  bits  $\rightarrow .14$  mega bits

$1.1/.14 = 8$  compression factor!

2.)

As we increase the degree of the polynomial basis function we are better able to fit the test data and thus we see a reduction in the Root Mean Square Error. However, we are getting farther away from the true relationship of chirps and temperature, and therefore, when we present new data we have a poor fit (RMSE goes up). When training for the ideal parameters it's as if we are fitting the noise more than the signal. We have *overfit* the data.

3.)

As we increase the gamma value, the training RMSE raises a bit. This is because we aren't able to fit every point perfectly when we start limiting the parameter size of our OLS fit and decrease the model complexity. However, the testing RMSE drops precipitously when penalizing complex models. This is because we are penalizing high order basis functions (incidentally by penalizing large parameter values) and are less likely to overfit to the training data. If we are going to assume a ninth order polynomial is a good basis function for the chirp data, we better make sure we are using high gamma values to lessen the impact of the higher order bases.

