

1e

$$M_2 = \begin{bmatrix} -3 & 1 \\ 0 & 1 \end{bmatrix}$$

$$R = \begin{bmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{bmatrix}$$

$$A = M_2 R$$

$$B = R M_2$$

$$\begin{bmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{bmatrix}$$

$$B = \begin{bmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{bmatrix} \begin{bmatrix} -3 & 1 \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} -3\cos \theta & \cos \theta + \sin \theta \\ 3\sin \theta & -\sin \theta + \cos \theta \end{bmatrix}$$

$$A = \begin{bmatrix} -3 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} -3\cos \theta - \sin \theta & -3\sin \theta + \cos \theta \\ -\sin \theta & \cos \theta \end{bmatrix}$$

$$A \neq B$$

1g

$$M_3 = \begin{bmatrix} 0.5 & 0 \\ 0 & 2 \end{bmatrix}$$

$$V_3 = \begin{bmatrix} 1/\sqrt{2} & -1/\sqrt{2} \\ -1/\sqrt{2} & 1/\sqrt{2} \end{bmatrix}$$

$$C = M_3 V_3$$

$$\begin{bmatrix} 1/\sqrt{2} & -1/\sqrt{2} \\ -1/\sqrt{2} & 1/\sqrt{2} \end{bmatrix}$$

$$D = V_3 C \begin{bmatrix} 1/2\sqrt{2} & -1/2\sqrt{2} \\ -2/\sqrt{2} & 2/\sqrt{2} \end{bmatrix}$$

$$C = \begin{bmatrix} 0.5 & 0 \\ 0 & 2 \end{bmatrix}$$

$$\begin{bmatrix} 1/2\sqrt{2} & -1/2\sqrt{2} \\ -2/\sqrt{2} & 2/\sqrt{2} \end{bmatrix}$$

$$D = \begin{bmatrix} 1/\sqrt{2} & -1/\sqrt{2} \\ -1/\sqrt{2} & 1/\sqrt{2} \end{bmatrix} \begin{bmatrix} 1/4 + 1 & -1/2 + 1 \\ -1/2 + 1 & 1/4 + 1 \end{bmatrix}$$

$$D = \begin{bmatrix} 1.25 & 0.75 \\ 0.75 & 1.25 \end{bmatrix} = M_4$$

$$H = V_3 M_3$$

$$\begin{bmatrix} 0.5 & 0 \\ 0 & 2 \end{bmatrix}$$

$$\begin{bmatrix} 1/\sqrt{2} & -1/\sqrt{2} \\ -1/\sqrt{2} & 1/\sqrt{2} \end{bmatrix} \begin{bmatrix} 1/2\sqrt{2} & -2/\sqrt{2} \\ -1/2\sqrt{2} & 2/\sqrt{2} \end{bmatrix}$$

CI in halved

CII in doubled