

Classic Crypto

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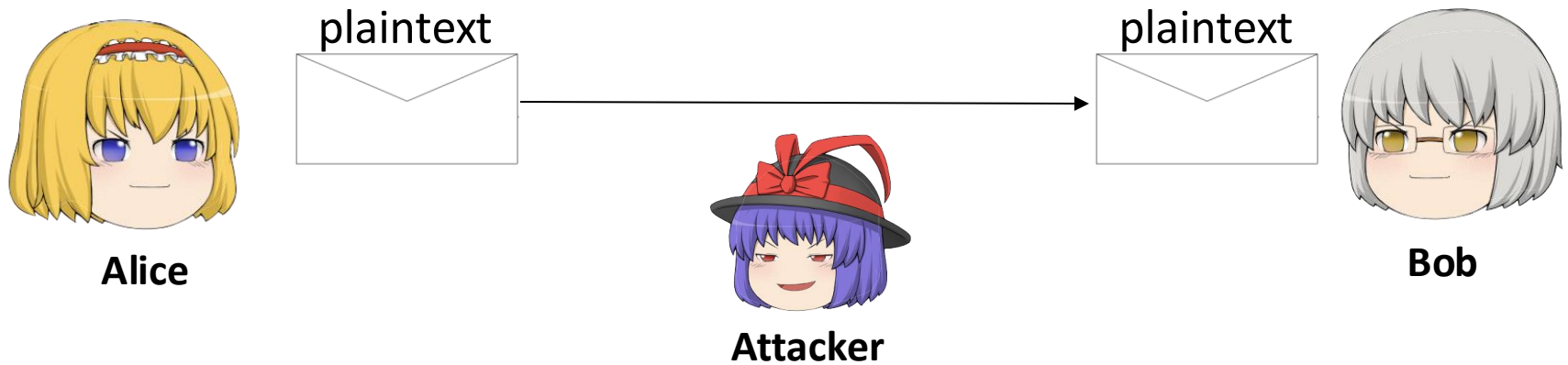


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Some slides are written by Mark Stamp.

Communication could be unsafe



Cryptography

Cryptography is the science (and art?) of **secret writing**

A cryptosystem consists of:



- Key(s)



- Encryption mechanism



- Decryption mechanism

Again, How to Speak Crypto

- A *cipher* or *cryptosystem* is used to *encrypt* the *plaintext*
- The result of encryption is *ciphertext*
- We *decrypt* ciphertext to recover plaintext
- A *key* is used to configure a cryptosystem
- A *symmetric key* cryptosystem uses the same key to encrypt as to decrypt
- A *public key* cryptosystem uses a *public key* to encrypt and a *private key* to decrypt → talk about that later
- Computing plaintext from ciphertext → **hard**
- Computing plaintext from ciphertext with key → **easy**

$E(\text{plaintext}, \text{key}) = \text{ciphertext}$

$D(\text{ciphertext}, \text{key}) = \text{plaintext}$

Basic Assumption in Crypto

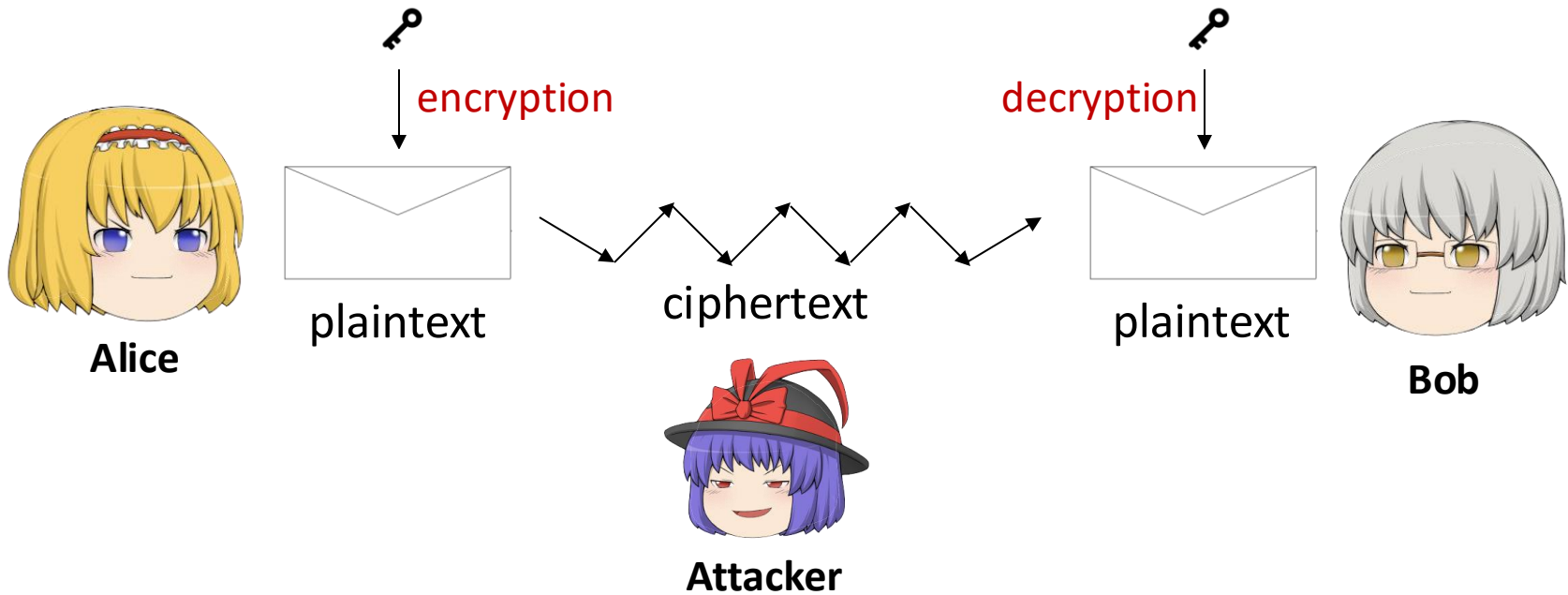
- **Kerckhoffs' Principle:**

The key(s) of a cryptosystem should be hidden,
but the mechanisms should be public.

- Why do we make such an assumption?
 - Experience has shown that secret algorithms tend to be weak when exposed
 - Secret algorithms never remain secret
 - Better to find weaknesses beforehand

Crypto as Black Box

A generic view of symmetric key crypto



What does the attacker know in this scenario?

Alice and Bob both already know some key K

Symmetric Key Cryptography

- Symmetric keys, where a **single key** (**k**) is used for **E** and **D**

$$D(E(p, k), k) = P$$

- All (intended) receivers have access to key
- Management of keys determines who has access to encrypted data
 - But how to do that? A chicken and egg problem?
- Examples:
 - Simple substitution; codebook ← **classic crypto (can be done by hand)**
 - One-time pad (OTP) ← **classic crypto (can be done by hand)**
 - Stream ciphers ← talk later
 - Block ciphers ← talk later
- Of course, we will talk about **public key crypto** later.

Simple Substitution

- Plaintext: **fourscoreandsevenyearsago**
- Key: **3**

Plaintext	a	b	c	d	e	f	g	h	i	j	k	l	m	n	o	p	q	r	s	t	u	v	w	x	y	z
Ciphertext	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C

❑ Ciphertext:

IRXUVFRUHDQGVHYHQBHDUVDJR

❑ Shift by 3 is “Caesar’s cipher”

Ceasar's Cipher Decryption

- Suppose we know a Caesar's cipher is being used:

Plaintext	a	b	c	d	e	f	g	h	i	j	k	l	m	n	o	p	q	r	s	t	u	v	w	x	y	z
Ciphertext	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C

- Given ciphertext:

VSRQJHEREVTXDUHSDQWV

- Plaintext: **spongebobsquarepants**

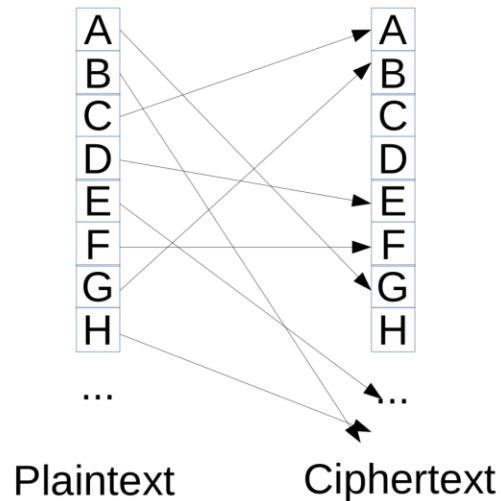


Attack I: Try Them All

- A simple substitution (shift by n) is used
 - But the key is unknown
- Given ciphertext: **CSYEVIXIVQMREXIH**
- How to find the key?
- Only 25 possible keys — try them all!
- **Exhaustive key search**

Simple Substitution: General Case

- any **permutation** of letters?

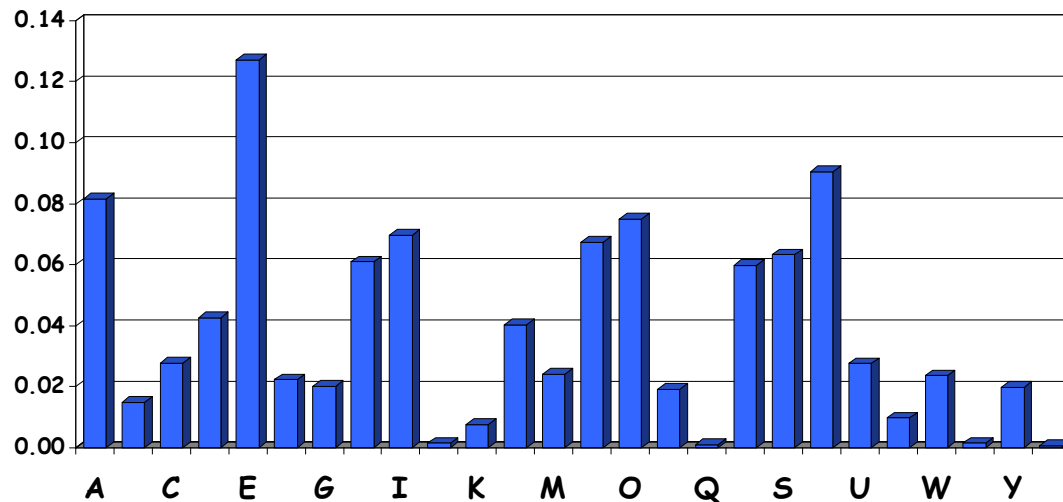


□ How many variations?

□ $26! = 403291461126605635584000000 > 2^{88}$

Crypto Attack II

- Cannot try all 2^{88} simple substitution keys
- Can we be more clever?
- English letter frequency counts...

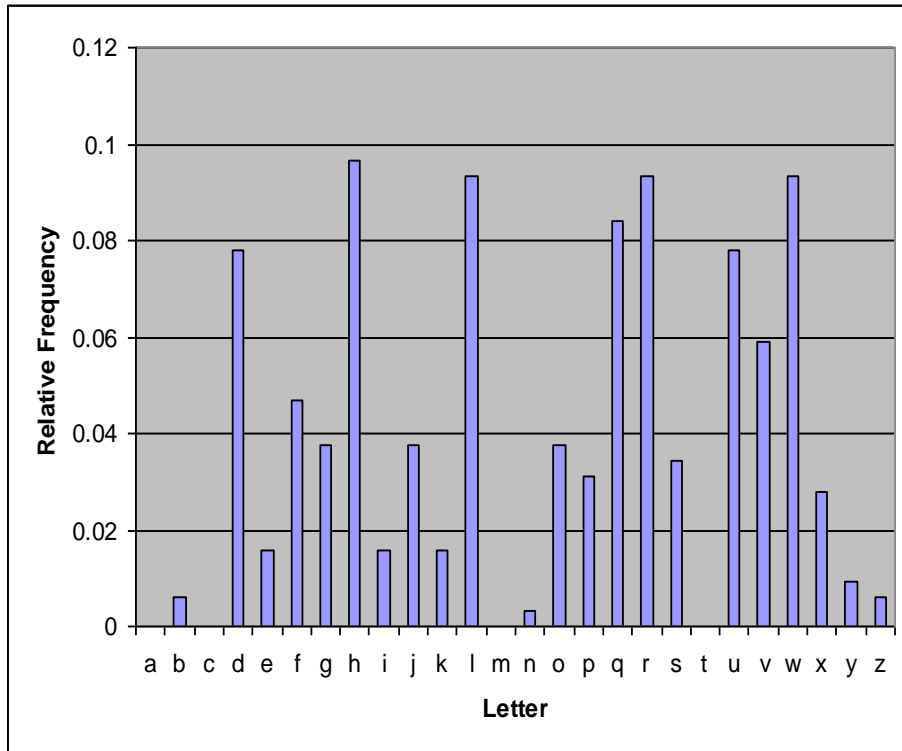


Let's see an example...

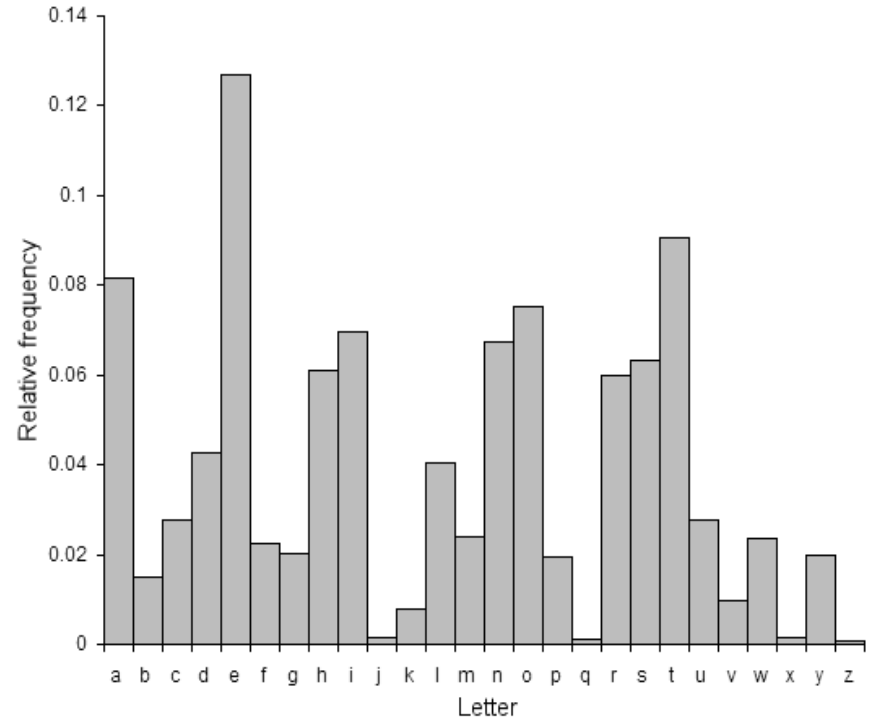
Crypto Attack II

- Vg gbbx n ybg bs oybbq,
fjrng naq grnef gb trg
gb jurer jr ner gbqnl,
ohg jr unir whfg ortha.
Gbqnl jr ortva va
rnearfg gur jbex bs
znxvat fher gung gur
jbeyq jr yrnir bhe
puvyqera vf whfg n
yvggyr ovg orggre guna
gur bar jr vaunovg
gbqnl.

Crypto Attack II



Ciphertext distribution



English distribution

$\{h, l, r\} \rightarrow \{t, a, e\}?$

Crypto Attack II

- Vg gbbx n ybg bs oybbq,
fj**r**ng naq g**r**nef gb t**r**g
gb ju**r**e**r** j**r** ne**r** gbqnl,
ohg j**r** un**i****r** whfg o**r**tha.
Gbqnl j**r** o**r**tva va
rne**a****r**fg gur j**r**bex bs
znxvat fhe**r** gung gu**r**
jbeyq j**r** y**r**n**i****r** bhe
puvyqe**r**a vf whfg n
yvggy**r** ov**g** o**r**gg**r**e guna
gu**r** ba**r** j**r** vaunovg
gbqnl.

- It took a lot of blood,
swe**a**t and te**a**rs to get
to whe**r**e we a**r**e today,
but we have just be**g**un.
Today we be**g**in in
earne**s**t the **w**ork of
making su**r**e that the
world we le**a**ve our
childre**n** is just a
little bit be**t**te**r** than
the one we inhabit
today.

‘r’ appears very frequently so likely is one of
the top frequency letters (i.e., e).

Crypto Attack II

- Vg gbbx n ybg bs oybbq,
fj**r**ng naq g**r**nef gb t**r**g
gb ju**r**e**r** j**r** ne**r** gbqnl,
ohg j**r** un**i**r whfg o**r**tha.
Gbqnl j**r** o**r**tva va
rne**a**r**f**g gur j**b**ex bs
znxvat fhe**r** gung **g**ur
jbeyq j**r** y**r**n**i**r bhe
puvyqe**r**a vf whfg n
yvggy**r** ov**g** o**r**gg**r**e guna
gur ba**r** j**r** vaunovg
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- It took a lot of blood,
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earne**s**t the**e** work of
making sure**e** that **the**
world we le**a**ve our
children is just a
little**e** bit be**t**ter than
the one we inhabit
today.

Repeat this process, picking out more letters,
then common words, e.g., '**the**'

Again, Principle

- Cryptosystem is **secure** if best known attack is to try all keys
 - i.e., exhaustive key search
- Cryptosystem is **insecure** if *any* shortcut attack is known
 - **Secure**
 - **No exhaustive search is feasible!**

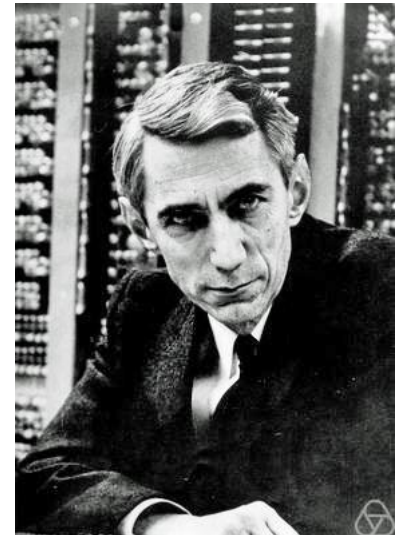
Then, is there an **unbreakable** cipher?

- Yes!
 - Claude Shannon proved it → One-Time Pad (OTP)!
 - The father of of Information Theory

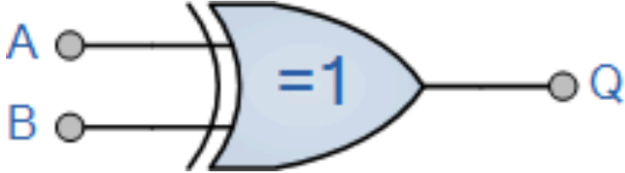
A Mathematical Theory of Communication 1948



The Mathematical Theory of Communication 1949



Exclusive OR

Symbol	Truth Table		
 <p>2-input Ex-OR Gate</p>	B	A	Q
	0	0	0
	0	1	1
	1	0	1
	1	1	0
Boolean Expression $Q = A \oplus B$	A OR B but NOT BOTH gives Q		

You XOR the same thing twice, you get the same thing!

One-Time Pad: Encryption

e=000 h=001 i=010 k=011 l=100 r=101 s=110 t=111

Encryption: Plaintext \oplus Key = Ciphertext

Salute!



h e i l h i t l e r

Plaintext: 001 000 010 100 001 010 111 100 000 101

Key: 111 101 110 101 111 100 000 101 110 000

Ciphertext: 110 101 100 001 110 110 111 001 110 101

s r l h s s t h s r

One-Time Pad: Decryption

e=000 h=001 i=010 k=011 l=100 r=101 s=110 t=111

Decryption: Ciphertext \oplus Key = Plaintext

	s	r	l	h	s	s	t	h	s	r
Ciphertext:	110	101	100	001	110	110	111	001	110	101
Key:	111	101	110	101	111	100	000	101	110	000
Plaintext:	001	000	010	100	001	010	111	100	000	101
	h	e	i	l	h	i	t	l	e	r

One-Time Pad

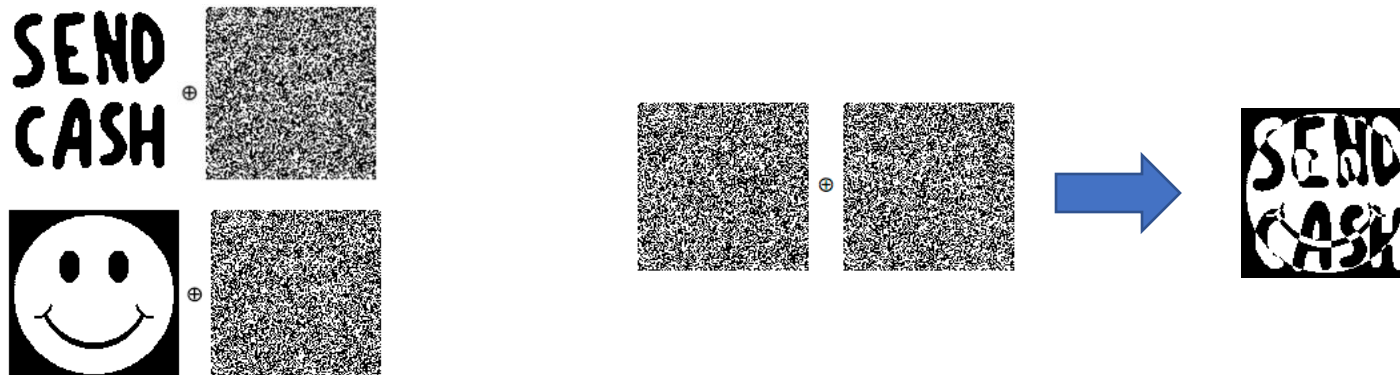
Claim the following “**key**” was used:

	s	r	l	h	s	s	t	h	s	r
Ciphertext:	110	101	100	001	110	110	111	001	110	101
“ key ”:	101	111	000	101	111	100	000	101	110	000
<hr/>										
“Plaintext”:	011	010	100	100	001	010	111	100	000	101
	k	i	l	l	h	i	t	l	e	r

e=000 h=001 i=010 k=011 l=100 r=101 s=110 t=111

One-Time Pad

- **Provably** secure
 - Ciphertext gives **no** useful info about plaintext
 - Assume value of each bit in **k** is equally likely.
 - All ciphertexts are ***equally likely***
- BUT, only when be used correctly
 - Pad must be **random**, used **only once**



Shannon, Claude (1949). "Communication Theory of Secrecy Systems" Bell System Technical Journal 28 (4): 656–715.

One-Time Pad

- **Provably** secure
 - Ciphertext gives **no** useful info about plaintext
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- BUT, only when be used correctly
 - Pad must be **random**, used **only once**
 - Pad (key) is **same size** as message
- So, why not distribute pad instead of msg?

Real-World One-Time Pad

- Project *VENOVA*
 - Russia spies encrypted messages from U.S. to Moscow in 30's, 40's, and 50's
 - Thousands of messages
- Spy carried one-time pad into U.S.
- Spy used pad to encrypt secret messages
- **Repeats** within the “one-time” pads made cryptanalysis possible

Codebook Cipher

- Literally, a book filled with “codewords”
- [Zimmerman Telegram](#) encrypted via codebook

Februar	13605
fest	13732
finanzielle	13850
folgender	13918
Frieden	17142
Friedensschluss	17149
:	:

- Modern block ciphers are codebooks!
- More about this later...

Codebook Cipher: Additive

- Codebooks also (usually) use **additive**
- Additive — book of “random” numbers
 - Encrypt message with codebook
 - Then choose position in additive book
 - Add in additives to get ciphertext
 - Send ciphertext and **additive position** ← **not secret**
 - Recipient subtracts additives before decrypting
- Why use an additive sequence?
 - Same word encodes into different representations.