

# Machine Learning

## Lecture 16: Policy-Based Deep Reinforcement Learning

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This set of notes is based on the references listed at the end and internet resources.

# Outline

## 1 Policy Gradients

## 2 Actor-Critic Algorithms

# Value-Based RL vs Policy-Based RL

## ■ Value-based RL:

$$\{(s, a, r, s')\} \Rightarrow Q(s, a : \theta) \Rightarrow \pi^*(s) = \arg \max_a Q(s, a : \theta)$$

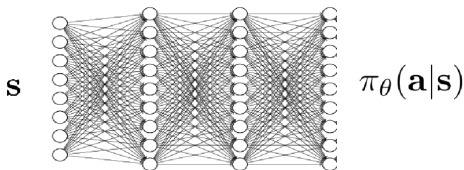
where  $\pi^*$  is a **deterministic policy**.

## ■ Policy-based RL

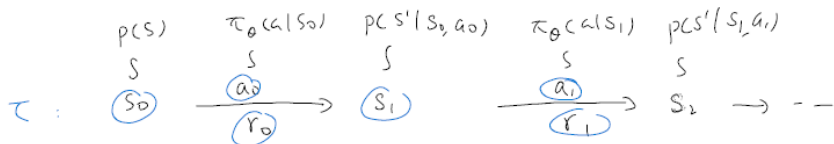
$$\{(s, a, r, s')\} \Rightarrow \pi(a|s)$$

where  $\pi(a|s)$  is a **stochastic policy**.

- For a given  $s$ ,  $\pi(a|s)$  is a distribution over actions, and is represented as a neural network:



# Acting according to Stochastic Policy



Trajectory

prob of  $\tau$ : 
$$\begin{aligned} \pi_\theta(\tau) &= p(s_0) \pi_\theta(a_0|s_0) p(s_1|s_0, a_0) \\ &\quad \pi_\theta(a_1|s_1) p(s_2|s_1, a_1) \\ &\quad \dots \\ &= p(s_0) \prod_t \pi_\theta(a_t|s_t) p(s_{t+1}|s_t, a_t) \end{aligned}$$

Reward: 
$$r(\tau) = r_0 + \gamma r_1 + \gamma^2 r_2 + \dots$$

$$J(\theta) = \mathbb{E}_{\tau \sim \pi_\theta(\tau)} [r(\tau)]$$

Learning: 
$$\max_{\theta} J(\theta)$$

Expected cumulative reward  
for following  $\pi_\theta(a|s)$

$$\theta \leftarrow \theta + \alpha \nabla_{\theta} J(\theta)$$

# Acting according to Stochastic Policy

- Suppose an agent interacts with its environment by following a stochastic policy  $\pi_\theta(a|s)$  until an episode ends:
  - Experience trajectory  $\tau$ :  $s_0, a_0, r_0, \dots, s_T, a_T, r_T$
  - At each time point  $t$ , an action  $a_t$  is sampled from the distribution  $\pi_\theta(a|s_t)$
  - The probability of an experience trajectory is:

$$\pi_\theta(\tau) = p(s_0) \prod_{t=0}^T \pi_\theta(a_t|s_t) p(s_{t+1}|s_t, a_t) \quad (1)$$

# Objective of the Policy Gradient Method

- Because of stochasticity in environment  $p(s_{t+1}|s_t)$  and in action selection  $\pi_\theta(a_t|s_t)$ , the trajectory, and hence the total reward, will be different in different runs of the process.
- The expected total reward is:

$$J(\theta) = E_{\tau \sim \pi_\theta(\tau)}[r(\tau)] = E_{\tau \sim \pi_\theta(\tau)}\left[\sum_t \gamma^t r_t\right]$$

- The objective of policy gradient is to maximize  $J(\theta)$ :

$$\theta^* = \arg \max_{\theta} J(\theta)$$

- This is done via gradient ascent, and the output is (an approximation of) the optimal policy  $\pi_{\theta^*}(a|s)$ :

$$\theta \leftarrow \theta + \alpha \nabla_{\theta} J(\theta)$$

# Policy Gradients

$$\begin{aligned}\nabla_{\theta} J(\theta) &= \nabla_{\theta} E_{\tau \sim \pi_{\theta}(\tau)}[r(\tau)] \\ &= \nabla_{\theta} \int r(\tau) \pi_{\theta}(\tau) d\tau \\ &= \int r(\tau) \nabla_{\theta} \pi_{\theta}(\tau) d\tau \\ &= \int r(\tau) \pi_{\theta}(\tau) \nabla_{\theta} \log \pi_{\theta}(\tau) d\tau \quad (\text{the log-gradient trick}) \\ &= E_{\tau \sim \pi_{\theta}(\tau)}[\nabla_{\theta} \log \pi_{\theta}(\tau) r(\tau)]\end{aligned}$$

# Policy Gradients

- Because of Equation (1), we have

$$\log \pi_{\theta}(\tau) = \log p(s_0) + \sum_t \log \pi_{\theta}(a_t|s_t) + \sum_t \log p(s_{t+1}|s_t)$$

- Hence,

$$\begin{aligned} & E_{\tau \sim \pi_{\theta}(\tau)} [\nabla_{\theta} \log \pi_{\theta}(\tau) r(\tau)] \\ &= E_{\tau \sim \pi_{\theta}(\tau)} [\nabla_{\theta} (\log p(s_0) + \sum_t \log \pi_{\theta}(a_t|s_t) + \sum_t \log p(s_{t+1}|s_t)) r(\tau)] \\ &= E_{\tau \sim \pi_{\theta}(\tau)} [\sum_t \nabla_{\theta} \log \pi_{\theta}(a_t|s_t) r(\tau)] \\ &\approx \frac{1}{N} \sum_{i=1}^N \sum_t \nabla_{\theta} \log \pi_{\theta}(a_t^i|s_t^i) r(\tau^i) \end{aligned}$$

where  $\{\tau^i = \{s_0^i, a_0^i, r_0^i, s_1^i, a_1^i, r_1^i, \dots\}_{i=1}^N$  is a collection of  $N$  sample trajectories.



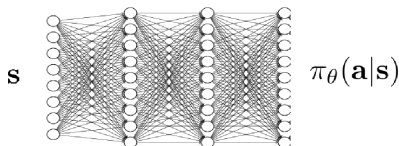
# The REINFORCE Algorithm

- REINFORCE algorithm (Williams 1992):

**Repeat:**

- 1 sample  $\{\tau^i\}_{i=1}^N$  from  $\pi_\theta(a_t|s_t)$  (run the current policy)
- 2  $\nabla_\theta J(\theta) \approx \frac{1}{N} \sum_i \sum_t \nabla_\theta \log \pi_\theta(a_t^i|s_t^i) r(\tau^i)$
- 3  $\theta \leftarrow \theta + \alpha \nabla_\theta J(\theta)$

- The term  $\nabla_\theta \log \pi_\theta(a_t|s_t)$  is calculated on the policy network:



## Supervised Learning, Imitation Learning, and RL (REINFORCE)

supervised learning  $\{x_i, y_i\}_{i=1}^N \Rightarrow P(Y|X, \theta)$

$$\theta \leftarrow \theta + \alpha \frac{1}{N} \sum_{i=1}^N \nabla_{\theta} \log P(y_i | x_i, \theta)$$

max likelihood of model / prob of data

current settings:  $\{(s_t^i, a_t^i) \mid i=1, \dots, N, t=1, \dots, T\}$

$$\theta \leftarrow \theta + \alpha \frac{1}{N} \sum_i \sum_t \nabla_{\theta} \log P(a_t^i | s_t^i)$$

max prob of data / prob of actions

Imitation learning: learn from expert demo

REINFORCE

$$\theta \leftarrow \theta + \alpha \frac{1}{N} \sum_i \sum_t \nabla_{\theta} \log P(a_t^i | s_t^i) r(I^i)$$

$r(I^i) > 0$ , increase the prob of action in  $\tau^i$

$r(I^i) < 0$  decrease the prob of actions in  $\tau^i$

# Interpretation of the REINFORCE Update Rule


$$\theta \leftarrow \theta + \alpha \sum_i \sum_t \nabla_{\theta} \log \pi_{\theta}(a_t^i | s_t^i) r(\tau^i)$$

- Changing  $\theta$  in the direction of  $\nabla_{\theta} \log \pi_{\theta}(a_t^i | s_t^i)$  would increase the probability of the action  $a_t^i$ .
- If  $r(\tau^i) < 0$ , we change  $\theta$  in the opposite direction and hence reduce the probability of  $a_t^i$ 
  - So, the update rule makes bad experiences less likely.
- If  $r(\tau^i) > 0$ , we change  $\theta$  so as to increase the probability of  $a_t^i$ 
  - So, the update rule makes good experiences more likely
- So, the REINFORCE update formalizes the notion of “trial and error”.

# On-Policy vs Off-Policy

- REINFORCE is an **on-policy** algorithm because all the data used to improve the current policy are collected using the policy itself.

REINFORCE algorithm:

- 
1. sample  $\{\tau^i\}$  from  $\pi_\theta(\mathbf{a}_t|\mathbf{s}_t)$  (run the policy)
  2.  $\nabla_\theta J(\theta) \approx \sum_i (\sum_t \nabla_\theta \log \pi_\theta(\mathbf{a}_t^i|\mathbf{s}_t^i)) (\sum_t r(\mathbf{s}_t^i, \mathbf{a}_t^i))$
  3.  $\theta \leftarrow \theta + \alpha \nabla_\theta J(\theta)$

# On-Policy vs Off-Policy

- DQN is an **off-policy** algorithm because some of the data used to improve the current policy are **collected using other policies**.

Repeat:

- Take action  $a$  in current state  $s$ , observe  $r$  and  $s'$ ; add experience tuple  $(s, a, s', r)$  to a buffer  $D$ ;  $s \leftarrow s'$
- Sample a minibatch  $B = \{s_j, a_j, s'_j, r_j\}$  from  $D$ .
- Update the parameters

$$\theta \leftarrow \theta - \alpha \nabla_{\theta} \sum_j ([r(s_j, a_j) + \gamma \max_{a'_j} Q(s'_j, a'_j; \theta^-)] - Q(s_j, a_j; \theta))^2$$

- $\theta^- \leftarrow \theta$  in every  $C$  steps.

# On-Policy vs Off-Policy

- Q-learning is off-policy even without experience replay because the agent does not necessarily take the action  $a' = \arg \max_{a'} Q(s', a')$  in the next step
  - The action  $a'$  used for update is chosen using the current  $Q$ , but
  - The next action is chosen using the updated  $Q$ .
- Initialize  $Q(s, a)$  arbitrarily.
- Repeat (for each episode)
  - Pick initial state  $s$ .
  - Repeat
    - Choose  $a$  for the state  $s$  ( $\epsilon$ -greedy with  $\arg \max_a Q(s, a)$ )
    - Take action  $a$ , observe  $r$  and  $s'$
    - Update:
 
$$Q(s, a) \leftarrow Q(s, a) + \alpha[r + \gamma \max_{a'} Q(s', a') - Q(s, a)]$$

$$s \leftarrow s'$$
  - until  $s$  is terminal

# Policy Gradient has High Variance

$$\nabla_{\theta} J(\theta) \approx \frac{1}{N} \sum_{i=1}^N \sum_t \nabla_{\theta} \log \pi_{\theta}(a_t^i | s_t^i) r(\tau^i)$$

- The policy gradient is estimated using  $N$  trajectory samples.
- $N$  cannot be large because running a policy is costly.
- Because we can use only a small number of trajectory samples, the variance is high.

# Reducing Variance using Causality

$$\begin{aligned}\nabla_{\theta} J(\theta) &\approx \frac{1}{N} \sum_{i=1}^N \sum_{t=0}^T \nabla_{\theta} \log \pi_{\theta}(a_t^i | s_t^i) r(\tau^i) \\ &\approx \frac{1}{N} \sum_{i=1}^N \sum_{t=0}^T [\nabla_{\theta} \log \pi_{\theta}(a_t^i | s_t^i) \sum_{t'=0}^T \gamma^{t'} r_{t'}^i]\end{aligned}$$

- An action  $a_t^i$  taken at time point  $t$  does not affect only rewards at earlier time points.
- Hence, rewards before time  $t$  should not be considered when optimizing  $a_t$ .
- So, we use the following gradient instead:

$$\frac{1}{N} \sum_{i=1}^N \sum_{t=0}^T [\nabla_{\theta} \log \pi_{\theta}(a_t^i | s_t^i) \sum_{t'=t}^T \gamma^{t'} r_{t'}^i]$$

- The variance of  $\sum_{t'=t}^T \gamma^{t'} r_{t'}^i$  is smaller than that of  $\sum_{t'=0}^T \gamma^{t'} r_{t'}^i$  because it is influenced by less stochasticity.



# Reducing Variance using Baselines

$$\nabla_{\theta} J(\theta) \approx \frac{1}{N} \sum_{i=1}^N \sum_{t=0}^T \nabla_{\theta} \log \pi_{\theta}(a_t^i | s_t^i) r(\tau^i)$$

- Another way to reduce the variance is to use

$$\nabla_{\theta} J(\theta) \approx \frac{1}{N} \sum_{i=1}^N \sum_{t=0}^T \nabla_{\theta} \log \pi_{\theta}(a_t^i | s_t^i) (r(\tau^i) - b)$$

where the **baseline**  $b$  is given by:

$$b = \frac{1}{N} \sum_{i=1}^N r(\tau^i).$$

# Reducing Variance using Baselines: Analogy

- Let  $x_1, x_2, \dots, x_n$  be i.i.d random variables and  $b$  be another random variable.

$$\begin{aligned}
 V\left(\sum_{i=1}^n (x_i - b)\right) &\approx \sum_{i=1}^n V(x_i - b) \quad (\text{strictly true if independent}) \\
 &= \sum_{i=1}^n (E[(x_i - b)^2] - (E[x_i - b])^2) \\
 &= \sum_{i=1}^n E[(x_i - b)^2] - \sum_{i=1}^n (E[x_i - b])^2
 \end{aligned}$$

- The first term is minimized when  $b = \frac{1}{n} \sum_{i=1}^n x_i$
- The second term is also minimized when  $b = \frac{1}{n} \sum_{i=1}^n x_i$ .

# Baseline does not Make the Estimation Unbiased

- This is the policy gradient

$$\nabla_{\theta} J(\theta) = E_{\tau \sim \pi_{\theta}(\tau)} [\nabla_{\theta} \log \pi_{\theta}(\tau) r(\tau)]$$

- Subtracting a baseline  $b = E_{\tau \sim \pi_{\theta}(\tau)} [r(\tau)]$ , we get

$$\nabla_{\theta} J(\theta) = E_{\tau \sim \pi_{\theta}(\tau)} [\nabla_{\theta} \log \pi_{\theta}(\tau) (r(\tau) - b)]$$

- This does not introduce bias because

$$\begin{aligned} E_{\tau \sim \pi_{\theta}(\tau)} [\nabla_{\theta} \log \pi_{\theta}(\tau) b] &= \int \pi_{\theta}(\tau) \nabla_{\theta} \log \pi_{\theta}(\tau) b d\tau \\ &= \int \nabla_{\theta} \pi_{\theta}(\tau) b d\tau \\ &= b \nabla_{\theta} \int \pi_{\theta}(\tau) d\tau \\ &= 0 \end{aligned}$$

# Advanced Policy Gradient Methods

- Problems with policy gradient:
  - The parameters  $\theta$  are changed only a little bit at each gradient step because it does not make efficient use of the sampled trajectories  $\{\tau^i\}$ .
  - Large learning rate can lead to performance collapse, while small learning rate implies slow learning.
- Advanced policy gradient methods:
  - Purpose: Make efficient use of data and find an update rule that is just right.
  - Methods: Natural policy gradient (Peters and Schall 2008); Trusted region policy optimization (Schulman et al. 2015); Proximal policy optimization (Schulman et al. 2017).

# Outline

1 Policy Gradients

2 Actor-Critic Algorithms

# Optimal Value Functions and Value Functions of Policy

## ■ Optimal value functions:

- $V^*(s)$ : Total reward for acting optimally from state  $s$ .
- $Q^*(s, a)$ : total reward for, starting from  $s$ , taking action  $a$  and acting optimally after that.

$$V^*(s) = \max_a Q^*(s, a).$$

## ■ Value functions of a policy $\pi$ :

- $V^\pi(s)$ : Total reward for following  $\pi$  from state  $s$ .
- $Q^\pi(s, a)$ : total reward for, starting from  $s$ , taking action  $a$  and then following  $\pi$ .

$$V^\pi(s) = E_{a \sim \pi(a|s)}[Q^\pi(s, a)].$$

- Actor-Critic Algorithms: Policy gradient with policy evaluation, i.e.,  $Q^\pi(s, a)$ .

# Key Idea of Actor-Critic Algorithms

- The **advantage function**:

$$A^\pi(s_t, a_t) = Q^\pi(s_t, a_t) - V^\pi(s_t)$$

tells us how good the action  $a_t$  is relative to the average.

- Using the advantage function, we can write our policy gradient estimate as follows:

$$\nabla_\theta J(\theta) \approx \frac{1}{N} \sum_{i=1}^N \sum_{t=0}^T [\gamma^t \nabla_\theta \log \pi_\theta(a_t^i | s_t^i) A^\pi(s_t^i, a_t^i)],$$

- Increase probabilities of actions that are better than average,
- Decrease probabilities of actions worse than average.

## Key Idea of Actor-Critic Algorithms

REINFORCEActor:  $s \rightarrow [\theta] \rightarrow \pi_{\theta}(a|s)$ 

$$\theta \leftarrow \theta + \alpha \sum_i \sum_t \nabla_{\theta} \log \pi_{\theta}(a_t^i | s_t^i) \underline{r(\tau^i)}$$

Actor-Critic

$$\theta \leftarrow \theta + \alpha \sum_i \sum_t \nabla_{\theta} \log \pi_{\theta}(a_t^i | s_t^i) \underline{A^{\pi}(s_t^i, a_t^i)}$$

$A^{\pi}(s_t^i, a_t^i) > 0$ ,  $a_t^i$  better than average,  
prob of  $a_t^i$  increased

$A^{\pi}(s_t^i, a_t^i) < 0$ ,  $a_t^i$  worse than average,  
prob of  $a_t^i$  decreased

$$A^{\pi}(s_t^i, a_t^i) \approx \underbrace{r_t^i + \gamma V^{\pi}(s_{t+1}^i) - V^{\pi}(s_t^i)}_{\text{TD error}}$$



# How to Estimate the Advantage Function?

- In general, we have

$$Q^\pi(s, a) = r(s, a) + \gamma \sum_{s'} V^\pi(s') P(s'|s, a).$$

- Estimating  $Q^\pi(s_t, a_t)$  using one sample  $(s_{t+1})$  of  $s'$ ,

$$Q^\pi(s_t, a_t) \approx r(s_t, a_t) + \gamma V^\pi(s_{t+1}).$$

- Hence we can estimate  $A^\pi(s_t, a_t)$  using

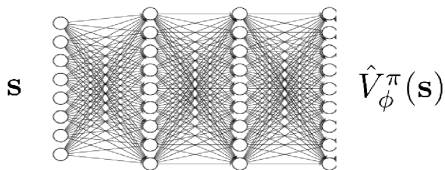
$$A^\pi(s_t, a_t) \approx r(s_t, a_t) + \gamma V^\pi(s_{t+1}) - V^\pi(s_t)$$

where  $s_{t+1} \sim P(s_{t+1}|s_t, a_t)$ , which can be obtained by letting agent act for one step.

- If we can estimate  $V^\pi(s_t)$ , then we can get  $A^\pi(s_t, a_t)$  and perform gradient ascent.

# How to Estimate the Value Function $V^\pi(s_t)$ ?

- This is called the **policy evaluation** problem.
- To learn the function from data, we use a neural network with parameters  $\phi$  to represent it. The output for input  $s$  is denoted by  $\hat{V}_\phi^\pi(s)$ .



- After obtaining a collection of experience tuples  $\{(s_i, a_i, s'_i, r_i)\}$ , we update  $\phi$  via backprop based on the following training set:

$$\{(s_i, r_i + \gamma \hat{V}_\phi^\pi(s'_i))\}$$

# Online Actor-Critic algorithm

## Repeat:

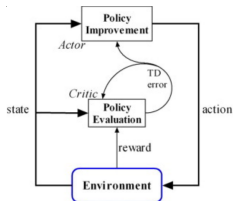
- 1 Take action  $a \sim \pi_\theta(a|s)$ , get  $(s, a, s', r)$ .
- 2 Update Critic parameters  $\phi$  using L2 loss and training data:

$$\{(s, r + \gamma \hat{V}_\phi^\pi(s'))\}$$

- 3  $\hat{A}^\pi(s, a) \leftarrow r + \gamma \hat{V}_\phi^\pi(s') - \hat{V}_\phi^\pi(s)$

- 4 Update actor parameters:

$$\theta \leftarrow \theta + \alpha \nabla_\theta \log \pi_\theta(a|s) \hat{A}^\pi(s, a)$$



# Batch Actor-Critic algorithm

## Repeat:

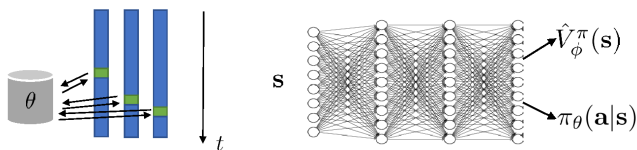
- 1 Sample experiences  $\{(s_i, a_i, s'_i, r_i)\}$  by following  $\pi_\theta$  for multiple steps.
- 2 Update Critic parameters  $\phi$  using L2 loss and training data

$$\{(s_i, r_i + \gamma \hat{V}_\phi^\pi(s'_i))\}$$

- 3  $\hat{A}^\pi(s_i, a_i) \leftarrow r_i + \gamma \hat{V}_\phi^\pi(s'_i) - \hat{V}_\phi^\pi(s_i) \quad \forall i$
- 4 Update actor parameters:

$$\theta \leftarrow \theta + \alpha \sum_i \nabla_\theta \log \pi_\theta(a_i | s_i) \hat{A}^\pi(s_i, a_i)$$

# Asynchronous Advantage Actor-Critic (A3C)

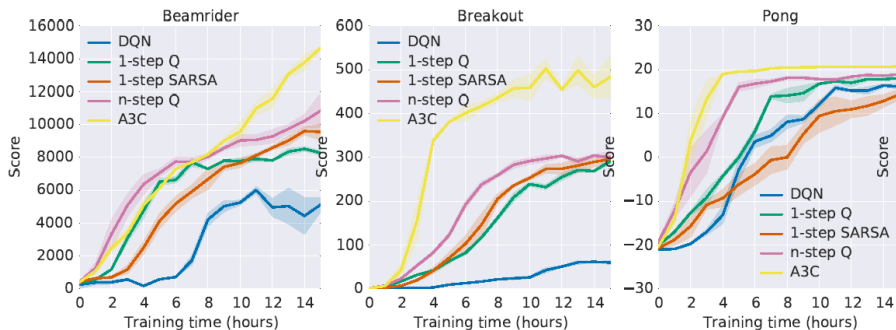


- Run multiple learners in parallel and let them take turns to update parameters .
- Decorrelates data used in learning. (Alternative to experience relay).
- Different learners explore different parts of environment.
- Actor and Critic share the same network

<https://www.youtube.com/watch?v=Ajjc08-iPx8&sns=tw&>

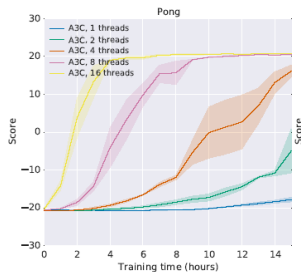
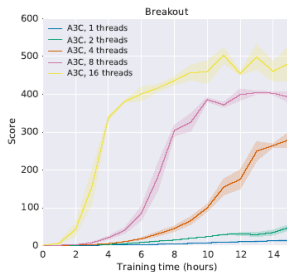
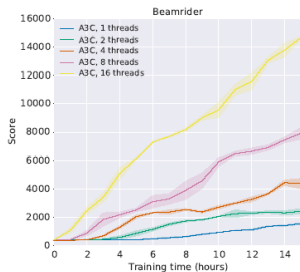
# Comparisons on Atari Games: Learning Speed

- DQN on single GPU
- Asynchronous methods use 16 CPU cores



# Comparisons on Atari Games: Learning Speed

## ■ More cores mean faster learning



# Comparisons on Atari Games: Performance <sup>1</sup>

Method	Training Time	Mean	Median
DQN	8 days on GPU	121.9%	47.5%
Gorila	4 days, 100 machines	215.2%	71.3%
D-DQN	8 days on GPU	332.9%	110.9%
Dueling D-DQN	8 days on GPU	343.8%	117.1%
Prioritized DQN	8 days on GPU	463.6%	127.6%
A3C, FF	1 day on CPU	344.1%	68.2%
A3C, FF	4 days on CPU	496.8%	116.6%
A3C, LSTM	4 days on CPU	623.0%	112.6%

*Table 1.* Mean and median human-normalized scores on 57 Atari games using the human starts evaluation metric.

<sup>1</sup> [github.com/vmayoral/basic\\_reinforcement\\_learning/blob/master/tutorial12/README.md](https://github.com/vmayoral/basic_reinforcement_learning/blob/master/tutorial12/README.md)



# Proximal Policy Optimization Algorithms (PPO) <sup>2</sup>

- Recall Actor-Critic Algorithm:

$$\begin{aligned}\nabla_{\theta} J(\theta) &\approx \frac{1}{N} \sum_{i=1}^N \sum_{t=0}^T [\gamma^t \nabla_{\theta} \log \pi_{\theta}(a_t^i | s_t^i) A^{\pi}(s_t^i, a_t^i)] \\ &= \frac{1}{N} \sum_{i=1}^N \sum_{t=0}^T [\gamma^t \frac{\nabla_{\theta} \pi_{\theta}(a_t^i | s_t^i)}{\pi_{\theta}(a_t^i | s_t^i)} A^{\pi}(s_t^i, a_t^i)]\end{aligned}$$

- To get PPO, replace  $\pi_{\theta}$  in the denominator with an old policy

$$\nabla_{\theta} J(\theta) \approx \frac{1}{N} \sum_{i=1}^N \sum_{t=0}^T [\gamma^t \nabla_{\theta} \frac{\pi_{\theta}(a_t^i | s_t^i)}{\pi_{old}(a_t^i | s_t^i)} A^{\pi}(s_t^i, a_t^i)]$$

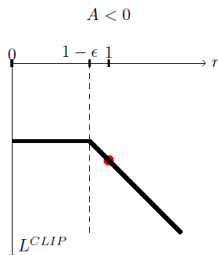
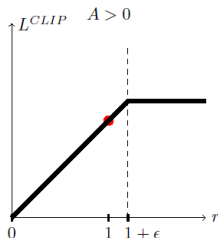
- The idea of PPO is keep  $r_t^i = \frac{\pi_{\theta}(a_t^i | s_t^i)}{\pi_{old}(a_t^i | s_t^i)}$  close to 1 so that the gradient update step does not introduce too much change in the policy, and hence make the training more **stable**. Often used.

<sup>2</sup>Schulman et al. "Proximal policy optimization algorithms." arXiv preprint arXiv:1707.06347 (2017).

# Proximal Policy Optimization Algorithms (PPO)

- PPO uses a lower bound of  $r_t^i A^\pi(s_t^i, a_t^i)$ , i.e.,  
 $L_t^{CLIP}(\theta) = \min(r_t^i A^\pi(s_t^i, a_t^i), \text{clip}(r_t^i, 1 - \epsilon, 1 + \epsilon) A^\pi(s_t^i, a_t^i))$ :

$$\nabla_{\theta} J(\theta) \approx \frac{1}{N} \sum_{i=1}^N \sum_{t=0}^T [\gamma^t \nabla_{\theta} L_t^{CLIP}(\theta)]$$



The clipped surrogate objective function limits the deviation from the previous policy. This avoids large policy updates that may harm the performance.

# Soft Actor-Critic <sup>3</sup>

- Policy gradient and Actor-Critic:

$$\pi^* = \arg \max_{\pi} E_{\tau \sim \pi} \left[ \sum_{t=0}^{\infty} \gamma^t r(s_t, a_t, s_{t+1}) \right]$$

- **Soft Actor-Critic (SAC):**

$$\pi^* = \arg \max_{\pi} E_{\tau \sim \pi} \left[ \sum_{t=0}^{\infty} \gamma^t (r(s_t, a_t, s_{t+1}) + \alpha H(\pi(\cdot | s_t))) \right]$$

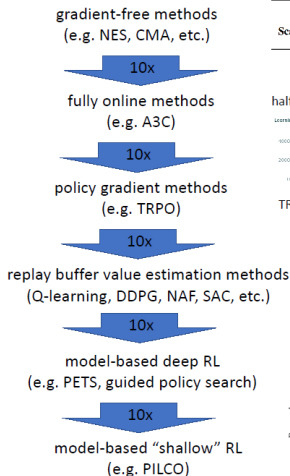
where  $H(\pi(\cdot | s_t))$  is the entropy of the policy, and  $\alpha$  is the temperature parameter.

- SAC prefers policies with high entropy, which results in better exploration performance.
- Consequently, SAC is more stable and more sample efficient than others algorithms such as DDPG and A3C.

<sup>3</sup> <https://spinningup.openai.com/en/latest/algorithms/sac.html>

Haarnoja *et al*, 2018. Soft Actor-Critic: Off-Policy Maximum Entropy Deep Reinforcement Learning with a Stochastic Actor

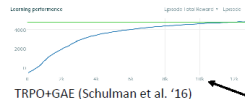
# Sample Complexity (Sergey Levine)



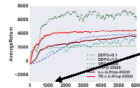
## Evolution Strategies as a Scalable Alternative to Reinforcement Learning

Tin Saikkumäki<sup>1</sup> Jonathan Ho<sup>1</sup> Xi Chen<sup>1</sup> Rya Sutskever<sup>1</sup>

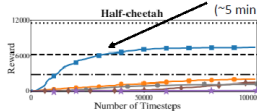
half-cheetah (slightly different version)



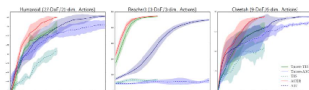
half-cheetah



Gu et al. '16



Chua et al. '18: Deep Reinforcement Learning in a Handful of Trials



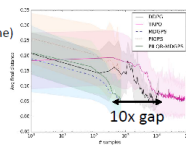
Wang et al. '17

10,000,000 steps  
(10,000 episodes)  
(~ 1.5 days real time)

1,000,000 steps  
(1,000 episodes)  
(~3 hours real time)



100,000,000 steps  
(100,000 episodes)  
(~ 15 days real time)



Chebotar et al. '17 (note log scale)

about 20 minutes of experience on a real robot

# Value-Based RLvs Policy-Based RL

## ■ Value-based RL:

- Pros: Can be off-policy, can use experience replay, more sample efficient
- Cons: Indirect, accuracy estimation of  $Q$  is difficult, might lead to unstable policy.

## ■ Policy-based RL:

- Pros: Directly optimize policy, more stable.
- Cons: It is on-policy, not sample efficient.

## ■ Recent Trends: Combine the best of two worlds.