



# Particle size dependence of ethylene epoxidation rates on Ag/ $\alpha$ -Al<sub>2</sub>O<sub>3</sub> catalysts: Why particle size distributions matter

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## ABSTRACT

The post-reaction Ag surface area distribution of 16 Ag/ $\alpha$ -Al<sub>2</sub>O<sub>3</sub> ethylene epoxidation catalysts with varying Ag weight loadings (6.9 – 35 wt%) containing different distributions of Ag particle sizes was correlated with measured ethylene oxide (EO) rates in presence of 3.5 ppm ethyl chloride via a particle size dependent Gaussian rate function. The Gaussian rate function model differs from a description based on average particle size as it accounts for the effects of the breadth of particle size distribution as well as the population of different particle sizes that constitute the Ag particle distribution on measured EO rates. This description of particle size effects in ethylene epoxidation catalysis facilitates accurate prediction of EO rates over a wide range of particle sizes (5–400 nm) and suggests that very small (5–50 nm) and very large Ag particles (>250 nm) have low EO rates (<3  $\mu\text{mol g}_{\text{Ag}}^{-1} \text{s}^{-1}$ ). A narrow Ag particle size distribution centered around ~130–150 nm would enable operation of ethylene epoxidation with high EO rates and EO selectivity.

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## 1. Introduction

Identification and quantification of active sites relating structure and morphology of a catalyst formulation to its rate is a key objective in catalysis. Metal nanoparticles supported on a porous non-metallic support are a class of catalysts wherein typically the exposed metal atoms constitute the active site. Certain reaction systems [1–4] exhibit a particle size effect wherein the rate of the catalytic event sensitively depends on changes in the coordination and electronic environment induced by aggregation and clustering of metal atoms which in turn changes the ability of the catalytic center to adsorb or desorb catalytically relevant species. The two macroscopic observables relevant for developing structure–function correlations in such systems are the metal particle size distribution and the rate. For convenience and by convention, the particle size distribution is only represented by a single number—the average particle size, without explicitly accounting for any other characteristics of the distribution.

Selective chemisorption, scanning and transmission electron microscopy, X-ray diffraction, among other methods are used to measure metal particle sizes however, only an average particle size is reported when in practice there is a broad distribution of particle sizes. We demonstrate for ethylene epoxidation over Ag/ $\alpha$ -Al<sub>2</sub>O<sub>3</sub>

catalysts that this representation of the particle size distribution with an average particle size, while simple and convenient, and almost universally adopted, is insufficient to explain the particle size dependence of measured epoxidation rates. Consider a scenario in which two catalyst samples have the same average particle size albeit resulting from very different particle size distributions. Lumping all description of the particle size distribution into a single average measure masks the contributions from metal clusters of different sizes which may contribute differently to the observed reaction rate.

The effects of Ag particle size on ethylene epoxidation rates and ethylene oxide (EO) selectivity over Ag/ $\alpha$ -Al<sub>2</sub>O<sub>3</sub> catalysts have been extensively investigated previously [5–14]. Van Der Reijen et al. [5] measured ethylene oxidation rates ( $0.1\text{--}1.5 \mu\text{mol C}_2\text{H}_4 \text{g}_{\text{Ag}}^{-1} \text{exposed s}^{-1}$ ) over a series of 18 wt% Ag/ $\alpha$ -Al<sub>2</sub>O<sub>3</sub> catalysts, treated under different gas environments and temperatures, at 473 K and 1 bar pressure (30 mol% C<sub>2</sub>H<sub>4</sub>, 8.5 mol% O<sub>2</sub>) and found that EO rates increase with increasing surface area averaged Ag particle size up to 60 nm and thereafter decrease with Ag particle size. Similarly, an optimum in ethylene oxidation rates with mean Ag crystallite size was observed by Lee et al. [6] over 2–10 wt% Ag/ $\alpha$ -Al<sub>2</sub>O<sub>3</sub> catalysts at 503 K and 13 bar pressure (3 mol% C<sub>2</sub>H<sub>4</sub>, 12 mol% O<sub>2</sub>) and by Goncharova et al. [7] over 0.5–13 wt% Ag/ $\alpha$ -Al<sub>2</sub>O<sub>3</sub> catalysts at 500 K and 1 bar (2 mol% C<sub>2</sub>H<sub>4</sub>, 7 mol% O<sub>2</sub>). Contrary trends were observed by Van hoof et al. [8] wherein EO rates decrease with increasing average particle size until 50 nm before becoming

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constant with size over 1–14 wt% Ag/ $\alpha$ -Al<sub>2</sub>O<sub>3</sub> catalysts at 498 K and 20 bar (5 mol% C<sub>2</sub>H<sub>4</sub>, 10 mol% O<sub>2</sub>) both in presence and in absence of 1 ppm vinyl chloride. Other studies allude to the effects of Ag particle size on EO selectivity. Christopher and Linic [9] measured ethylene epoxidation rates over Ag/ $\alpha$ -Al<sub>2</sub>O<sub>3</sub> catalysts having different shapes (nanospheres, nanocubes, and nanowires) and sizes (75 nm to 350 nm) at 510 K and 1 atm pressure (10 mol% C<sub>2</sub>H<sub>4</sub>, 10 mol% O<sub>2</sub>) and observed that EO selectivity increased with increasing particle size and oxygen partial pressure. At identical reaction conditions, large (350 nm) nanocube-shaped catalysts, terminated by Ag (100) surface facets ascertained using HRTEM imaging, offered the highest EO selectivity among the different shapes and sizes tested. Egelske et al. [10] also tested several 0.3–5 wt% Ag/ $\alpha$ -Al<sub>2</sub>O<sub>3</sub> catalysts at 483 K and 17 bar pressure (25 mol% C<sub>2</sub>H<sub>4</sub>, 8 mol% O<sub>2</sub>) and observed an increase in EO selectivity from 58% for an average particle size of 65 nm to 75% at 350 nm. A summary of the catalyst specifications and the reaction conditions employed in previous studies examining particle size effects in ethylene epoxidation is given in Table 1. The disparity in the observed EO rates with particle size among different studies is plausibly due to some differences in catalyst formulation and differences in some process conditions including use of C<sub>2</sub>H<sub>4</sub> or O<sub>2</sub> rich reactant mixtures, presence/absence of chlorine, total pressure, and temperature. What is noteworthy is that trends in EO rates differ from one study to another when using average size as a descriptor. We inquire whether these distinctions arise because particle sizes are assessed merely by the mean of the distribution not accounting for the broad distribution of Ag particle sizes.

Several authors have noted previously that Ag undergoes restructuring [15,16] and sintering [17,18] during ethylene epoxidation. Van Hoof et al. [15] carried out STEM imaging of an 8.1 wt% Ag/ $\alpha$ -Al<sub>2</sub>O<sub>3</sub> catalyst before and after reaction (20 bar, 498 K, 5 mol% C<sub>2</sub>H<sub>4</sub>, 10 mol% O<sub>2</sub>) and found that the average Ag particle size increased from 107 nm to 119 nm in presence of 1 ppm vinyl chloride in the reactor feed. Particle size distributions measured after reaction thus are likely more representative of the operational state of the epoxidation catalyst and as such these distributions should be correlated with epoxidation rates.

Weber, in a recent publication [19], articulated the limitations of using fractional metal exposure as a measure of active sites in a catalyst because it obscures the distribution of active sites. In making this point, Weber considered 5–30 wt% Pt/C catalysts with mean crystallite sizes between 1 and 4 nm synthesized by Peukert et al. [20] to have a particle size distribution that can be represented by: (i) a Rayleigh distribution with the same mean particle size, with some variance in the distribution, or (ii) a Delta function centered at the mean particle size not accounting for the distribution of particle sizes. Weber assumed that a subset of sites with a specific configuration (C9 sites in this example) are the relevant active sites whose population can be represented by a distribution that varies with particle size in a power law manner. The particle size dependency of measured turnover rates was captured only by expressing the rate as a continuous function of particle size (integral of the population of C9 sites at a particular particle size 'r' multiplied by the population of particles of size 'r') and by considering the distribution of particle sizes (Rayleigh distribution in this example), presenting a hypothetical example of correlating the particle size distribution with measured rates.

In this study, we develop a particle size dependent rate function model that allows us to map changes in the Ag particle size distribution to observed changes in EO rates. We measured ethylene epoxidation rates over 13 different Ag/ $\alpha$ -Al<sub>2</sub>O<sub>3</sub> catalysts with 6.9–35 wt% Ag weight loadings and 3 other formulations obtained by physically mixing two catalyst formulations, such that the 16 samples have a wide range of Ag particle sizes (5–400 nm). The

**Table 1**  
Catalyst specifications and reactions conditions for previous studies on particle size effects in ethylene epoxidation on Ag-based catalysts.

Reference	Catalyst	Average particle size range	CH <sub>4</sub> :O <sub>2</sub> ratio in the reactor feed	Total pressure and temperature	Chlorine promoters	Observations
Wu and Harriott (11)	(1–11 g) 0.5–39.5 wt% Ag/SiO <sub>2</sub>	5–50 nm	1:1	1.3 bar, 493 K	none	EO rates increase until 12 nm and then decrease and EO selectivity increases with Ag crystallite size
Verykios et al. (12)	(1–11 g) 1–14 wt% Ag/ $\alpha$ -Al <sub>2</sub> O <sub>3</sub>	30–180 nm	1.5	1.3 bar, 493 K	none	EO rates decrease from 30 to 50 nm before increasing continuously with size whereas EO selectivity increases until 130 nm before decreasing with Ag crystallite size
Cheng and Clearfield (13)	(0.5 g) 3–55 wt% Ag/Zr <sub>x</sub> (NaPO <sub>4</sub> ) <sub>2</sub>	5–85 nm	1:15	1 bar, 503 K	none	EO rates and EO selectivity increase until 27 nm before decreasing continuously with size
Lee et al. (6)	0.5–10 wt% Ag/ $\alpha$ -Al <sub>2</sub> O <sub>3</sub>	20–100 nm	1:4	0.1 bar, 508 K	none	EO rates increase until 40 nm and then decrease with Ag crystallite size whereas EO selectivity increases until 60 nm, and then becomes invariant with size
Goncharova et al. (7)	(0.5–2 g) 0.5–13 wt% Ag/ $\alpha$ -Al <sub>2</sub> O <sub>3</sub>	20–100 nm	1:3.5	1 bar, 503 K	none	Turnover frequencies for ethylene consumption and EO selectivity increase with size selectivity increases with size
Lu et al. (14)	(0.5 g) 0.5–56 wt% Ag/CaCO <sub>3</sub>	50–370 nm	1:1.7	3 bar, 475 K	none	EO rates increase until 60 nm and then decrease and EO selectivity is invariant with Ag particle size
Van den Reijen et al. (5)	(0.15 g) 18 wt% Ag/ $\alpha$ -Al <sub>2</sub> O <sub>3</sub>	20–500 nm	3.5:1	1 bar, 473 K	none	EO rates decrease with average particle size until 50 nm before becoming constant with size whereas EO selectivity increases with size
Van Hoof et al. (8)	(0.02–0.15 g) 1.3–14.4 wt% Ag/ $\alpha$ -Al <sub>2</sub> O <sub>3</sub>	19–300 nm	1:2	20 bar, 498 K	None or 1 ppm vinyl chloride	Turnover frequencies for ethylene consumption and EO selectivity increase with size
Egelske et al. (10)	0.3–5 wt% Ag/ $\alpha$ -Al <sub>2</sub> O <sub>3</sub>	65–350 nm	3:1:1	17 bar, 483 K	none	Turnover frequencies for ethylene consumption and EO selectivity increase with size

exposed surface area of Ag particles post-reaction for each of the 16 catalyst formulations was observed to follow a lognormal distribution. Epoxidation rates on these 16 samples were measured in presence of an organochloride promoter (3.5 ppm C<sub>2</sub>H<sub>5</sub>Cl) and these samples exhibited nearly invariant EO selectivity (~75–81%). We represent the measured EO rates as a continuum i.e., as an integral of the product of a Gaussian rate function and the log-normal surface area distribution to capture the contributions of different particle sizes to the rate eschewing any assumptions of site ensemble requirements or specificity of a particular Ag crystal facet or site. The rate-function model results in an explicit description of the Ag particle size distribution and the rate dependence on Ag particle size. The model captures the low reactivity of very small Ag particles (5–50 nm) and very large Ag particles (>250 nm) and leads us to postulate that a narrow Ag particle size distribution centered around 130–150 nm will facilitate high EO rates and EO selectivity over Ag/α-Al<sub>2</sub>O<sub>3</sub> catalysts.

## 2. Materials and methods

### 2.1. Catalyst synthesis

The Ag/α-Al<sub>2</sub>O<sub>3</sub> formulations in this report were synthesized by incipient-wetness impregnation of a silver oxalate (Ag<sub>2</sub>C<sub>2</sub>O<sub>4</sub>) precursor over α-Al<sub>2</sub>O<sub>3</sub> following protocols established previously by several authors [5,8,21]. Catalox HPA-150 γ-Al<sub>2</sub>O<sub>3</sub> was heat treated in stagnant air at 1698 K for 4 h with a ramp rate of 0.033 K s<sup>-1</sup> to synthesize the α-Al<sub>2</sub>O<sub>3</sub> support. Ag<sub>2</sub>C<sub>2</sub>O<sub>4</sub> was synthesized as a precipitate by mixing a 0.24 M solution of oxalic acid (oxalic acid dihydrate, Fisher Scientific, 99.6%) in HPLC-grade water with an equimolar amount of silver nitrate (Thermo Scientific, 99.7%) at ambient temperature. The Ag<sub>2</sub>C<sub>2</sub>O<sub>4</sub> precipitate was washed three times in HPLC-grade water before filtration under vacuum for ~12 h at ambient temperature. A solution containing 1:3 M ratio of silver oxalate: ethylene diamine (Sigma-Aldrich, Reagent-Plus, >99%) diluted in 2 cm<sup>3</sup> HPLC-grade water was impregnated onto the α-Al<sub>2</sub>O<sub>3</sub> support before drying in static air at 333 K. The molarity of Ag<sub>2</sub>C<sub>2</sub>O<sub>4</sub> solution was varied between 0.5 M and 2.5 M to obtain Ag/α-Al<sub>2</sub>O<sub>3</sub> catalysts with different Ag weight loadings from 6.9 to 35% as confirmed using SEM-EDX analysis. Upon drying, the Ag-impregnated support was treated in 0.83 cm<sup>3</sup> s<sup>-1</sup> flow of pure He (Research grade) at 498 K for 2 h to breakdown the Ag precursor and form Ag/α-Al<sub>2</sub>O<sub>3</sub>. The catalyst (1 g) was heat treated post synthesis under different gas atmospheres (H<sub>2</sub> (Airgas, UHP 99.999%), He (Matheson, Research grade), zero-grade air, and O<sub>2</sub> (Matheson, 99.9%) at flowrates of 0.8–1.25 cm<sup>3</sup> s<sup>-1</sup> and temperatures between 498 and 943 K to obtain a wide range of Ag particle sizes derived from procedures previously detailed by Van der Reijen et al. [5] The heat treatment conditions used to modify Ag particle sizes are detailed in Table 2 (Section 3.1).

### 2.2. Catalyst characterization

The crystalline phases in Ag/α-Al<sub>2</sub>O<sub>3</sub> samples were determined by powder X-ray diffraction (p-XRD) using Cu K<sub>α</sub> radiation ( $\lambda = 0.154$  nm) on a Bruker-AXS (Siemens) D5005 diffractometer (Supporting Information Section S.1). Ag nanoparticle size was measured after reaction by Scanning Electron Microscopy (SEM, JEOL 6500 Field Emission gun, 10 kV electron beam accelerating voltage). The spent catalyst was prepared for SEM imaging by coating it on a thin film of amorphous carbon. Three SEM images representing different regions over the catalyst and ~1600 Ag particles were analyzed for each catalyst sample using ImageJ to evaluate the Ag particle size distribution (Supporting information Figure S.2). The sampling error made in representing the population

of total Ag particles with a sample of size 1600 was quantified to be <1% (Supporting Information Section S.2).

### 2.3. Measurement of steady state rates of ethylene epoxidation

Rates of ethylene epoxidation were measured in a stainless-steel packed-bed reactor (McMaster-Carr, OD = 6.36 mm, ID = 4.57 mm), containing 25–100 mg of Ag/α-Al<sub>2</sub>O<sub>3</sub> catalyst loaded between two plugs of quartz wool (CE Elantech). The reactor was held between two split-tube copper sleeves and heated by two cartridge heaters (Omega Engineering Inc., CIR-2100, 600 W) with heating controlled using a Watlow temperature controller (96 Series) and pressure maintained at 530 kPa using a backpressure regulator (Tescom). The reaction temperature (513 K) was measured using a K-type thermocouple (Omega Engineering Inc.) placed in the center of the catalyst bed. The reactor feed consisted of 30 mol% C<sub>2</sub>H<sub>4</sub> (Airgas 99.99%), 0.4 mol% C<sub>2</sub>H<sub>6</sub> (Matheson 10% diluted in He), 7.7 mol% O<sub>2</sub> (Matheson 99.99%), 3.5 ppm C<sub>2</sub>H<sub>5</sub>Cl (Airgas 160 ppm diluted in He), and 1 mol% CO<sub>2</sub> (Matheson 10% diluted in He), was unchanged for all ethylene oxidation experiments and the respective gases were supplied to the reactor through mass flow controllers (MKS G-series) at a total flowrate of 2.78 cm<sup>3</sup> s<sup>-1</sup>. At the process conditions, the measured EO rates were free from external heat and mass-transfer limitations as confirmed by the invariance of EO rates with space velocity (Supporting Information Figure S.3) as well as calculations using GradientCheck [22] reported in Section S.3 of the Supporting Information. The reactor effluent composition was analyzed using a gas chromatograph (GC, Agilent 7890A) equipped with an HP-Plot Q column (30 m × 320 μm × 20 μm) and a thermal conductivity detector (TCD) in series with a flame ionization detector (FID) before the effluent was discharged into a bubbler containing 0.5 M H<sub>2</sub>SO<sub>4</sub> (BeanTown Chemical). The gas lines upstream of the reactor were maintained above 393 K using heat tapes (W.W. Grainger) to prevent condensation of the effluent gas stream. Ethylene conversions varied between 0.2 and 0.7% and oxygen conversions were <5% for all data reported, and the carbon mass balance (total carbon moles in/total carbon moles out) closed within 2%. Product selectivities reported in the study are defined as moles of carbon in the product divided by moles of carbon in all products. Major reaction products include EO, CO<sub>2</sub>, and H<sub>2</sub>O with trace amounts of acetaldehyde formed (<1% selectivity). Steady-state rates reported in this study are determined after exposing the catalyst to the reaction mixture for 18 h to allow for the slow evolution of the catalyst with time on-stream (Supporting Information Figure S.5).

## 3. Results and discussion

### 3.1. Analysis of Ag particle size distribution

The Ag particle size distribution of Ag/Al<sub>2</sub>O<sub>3</sub> catalysts with different Ag weight loadings was varied using heat treatments under different gas environments (He/H<sub>2</sub>/O<sub>2</sub>). An increase in the average Ag particle size of the Ag/α-Al<sub>2</sub>O<sub>3</sub> catalyst after attaining steady state rates compared to that of the as-synthesized sample (Supporting information Figure S.6) is consistent with observations made previously by several authors noting Ag undergoes restructuring [15,16] and sintering [17,18] during ethylene epoxidation; therefore, we determined particle size distribution of Ag/α-Al<sub>2</sub>O<sub>3</sub> catalysts after reaction. A summary of total surface area per gram, surface area weighted particle diameter (D<sub>S.A.</sub>), and heat treatment conditions used to modify the particle size distribution of all the catalysts and physical mixtures of catalysts is given in Tables 2 and 3 respectively. A comparison of average diameters and surface

**Table 2**

Surface area weighted particle diameter ( $D_{SA}$ ), total surface area per gram, and heat treatment conditions employed for different  $\text{Ag}/\alpha\text{-Al}_2\text{O}_3$  catalysts. The Ag weight loading of the sample has been mentioned as a prefix in the sample name. All catalysts were initially treated in  $1.25 \text{ cm}^3 \text{ s}^{-1}$  flowing He at 498 K with a ramp rate of  $0.17 \text{ K s}^{-1}$  and dwell time of 2 h except 31S-9 which was treated in  $1.25 \text{ cm}^3 \text{ s}^{-1}$  flowing  $\text{H}_2$  at 498 K. Histograms depicting the surface area per gram as a function of particle size for all catalysts are shown in Supporting Information Section S.9.

Sample name	$D_{SA}$ / nm	Total area per gram / $\text{m}^2 \text{Ag g}^{-1}$	Heat treatment conditions
6.9S-1	$69.4 \pm 23.4$	8.0	$1.25 \text{ cm}^3 \text{ s}^{-1} \text{ H}_2$ , ramp at $0.17 \text{ K s}^{-1}$ , hold at 498 K for 4 h
9.9S-2 <sup>1</sup>	$74.6 \pm 25.4$	6.4	–
16.9S-2 <sup>1</sup>	$93.6 \pm 31.5$	5.4	–
16.9S-1	$101.7 \pm 33.1$	5.8	$1.25 \text{ cm}^3 \text{ s}^{-1} \text{ H}_2$ , ramp at $0.17 \text{ K s}^{-1}$ , hold at 498 K for 4 h
31S-9	$151.5 \pm 47.3$	3.2	$1.10 \text{ cm}^3 \text{ s}^{-1} \text{ H}_2$ , ramp at $0.17 \text{ K s}^{-1}$ , hold at 673 K for 4 h
35S-1	$164.9 \pm 50.7$	3.6	$1.25 \text{ cm}^3 \text{ s}^{-1} \text{ H}_2$ , ramp at $0.17 \text{ K s}^{-1}$ , hold at 498 K for 4 h
35S-2 <sup>1</sup>	$176.1 \pm 54.1$	3.2	–
35S-3	$181.7 \pm 57.4$	2.7	$0.83 \text{ cm}^3 \text{ s}^{-1} \text{ He}$ , ramp at $0.17 \text{ K s}^{-1}$ , hold at 773 K for 4 h
35S-4	$203.4 \pm 70.3$	2.4	$0.83 \text{ cm}^3 \text{ s}^{-1} \text{ air}$ , ramp at $0.17 \text{ K s}^{-1}$ , hold at 598 K for 4 h
35S-5	$257.7 \pm 75.2$	2.0	$0.83 \text{ cm}^3 \text{ s}^{-1} \text{ O}_2$ , ramp at $0.17 \text{ K s}^{-1}$ , hold at 943 K for 4 h
35S-6	$261.6 \pm 82.6$	2.1	$0.83 \text{ cm}^3 \text{ s}^{-1} \text{ air}$ , ramp at $0.17 \text{ K s}^{-1}$ , hold at 848 K for 4 h
35S-7	$268.1 \pm 88.6$	2.1	$0.83 \text{ cm}^3 \text{ s}^{-1} \text{ O}_2$ , ramp at $0.17 \text{ K s}^{-1}$ , hold at 898 K for 4 h
35S-8	$272.5 \pm 89.3$	2.1	$0.83 \text{ cm}^3 \text{ s}^{-1} \text{ O}_2$ , ramp at $0.17 \text{ K s}^{-1}$ , hold at 928 K for 4 h

<sup>1</sup>These samples were not subjected to any additional heat treatment.

area histograms for 35S-1 and 35S-2 (Table 2 and Supporting Information Figures S.10, S.11) shows that  $\text{H}_2$  treatment favors formation of smaller Ag particles whereas treatment in  $\text{O}_2$  flow leads to larger Ag particles (see samples 35S-2 with 35S-7 in Table 2 and Supporting Information Figures S.11, S.16).

A typical SEM image and a histogram depicting the Ag particle size distribution of one of the  $\text{Ag}/\alpha\text{-Al}_2\text{O}_3$  samples are shown in Fig. 1 (a, b).

The particle size distribution can be expressed as a histogram of exposed surface area of Ag particles using Eq. 1 where ‘ $s_i$ ’ is the diameter of particle ‘ $i$ ’,  $n$  is the total number of particles, and ‘ $\rho_{\text{Ag}}$ ’ is the bulk density of silver. The discrete surface area histogram was fitted to a continuous lognormal distribution as it captured the tail of the distribution better compared to the symmetric Gaussian distribution (Fig. 2 (a, b)). The lognormal distributions fitted to the surface area histograms for all 16 catalysts enlisted in Tables 2 and 3 are shown in Supporting Information Section S.8 along with respective SEM images for each sample (Figures S.10–S.25).

$$\text{Surface area per gram (m}^2\text{g}^{-1}\text{)} = \frac{\sum_{i=1}^{n(\text{size interval})} 2\pi(\frac{s_i}{2})^2}{\sum_{i=1}^n \frac{2\pi}{3}(\frac{s_i}{2})^3 * \rho_{\text{Ag}}} \quad (1)$$

### 3.2. Ethylene epoxidation rates and EO selectivity as a function of average particle size

EO rates measured at identical process conditions over 13 different  $\text{Ag}/\alpha\text{-Al}_2\text{O}_3$  catalyst formulations and 3 physical mixtures are shown in Fig. 3 (a). The measured rates of ethylene consumption ( $0.8\text{--}8 \mu\text{mol g}_{\text{Ag}}^{-1} \text{ s}^{-1}$ ) are comparable to rates measured by Van der Reijen et al. [5] over 18%  $\text{Ag}/\alpha\text{-Al}_2\text{O}_3$  at 473 K and 1 bar total pressure while they are lower than 50–100 ethylene  $\mu\text{mol converted g}_{\text{Ag}}^{-1} \text{ s}^{-1}$  measured by Van Hoof et al. [8] over 2–10%  $\text{Ag}/\alpha\text{-Al}_2\text{O}_3$  at 498 K and 20 bar total pressure plausibly because of higher total pressure. EO rates increase with increasing surface area averaged Ag particle ( $D_{SA}$ ) size up to  $\sim 110 \text{ nm}$  before starting to decrease with Ag particle size. EO selectivity, on the other hand, varied between 75 and 81% and showed no trends with average particle size (Fig. 3 (b)).

First, we considered the possibility that all Ag particles of different sizes have equal reactivity and Ag particles of different sizes contribute to rate differently only because of a difference in the surface area per gram of silver exposed by these particles. EO rates normalized by the total surface area per gram for different catalysts should collapse to a constant value if all Ag particles of different sizes have equal reactivity. Surface area normalized EO rates (EO rate / total Ag surface area per gram), calculated using rates from Fig. 3.1 (a) and the total surface area per gram from Tables 2 and 3, for all catalysts tested show  $\sim 4\times$  variation (Fig. 4) suggesting that particles of different sizes have inherently different reactivity and thus uniquely contribute to cumulative EO rate.

We then examined the possibility that there exists a functional relationship between EO rate and average Ag particle size and this relationship is robust to describe particle size effects in ethylene epoxidation. The dependence of EO rates on the surface area-averaged particle size ( $D_{SA}$ ) for the 16 samples tested can be fitted using a lognormal equation (Eq. (2)) as shown in Fig. 5. This model, if appropriate, should be able to predict the rate of a physical mixture (mix-1 in Table 3) of 16.9S-2 and 35S-2 with a  $D_{SA} = 144.4 \text{ nm}$ . EO rate predicted for mix-1 by Eq. (2) is  $4.17 \mu\text{mol g}_{\text{Ag}}^{-1} \text{ s}^{-1}$  which is  $\sim 1.5\times$  higher than the experimentally measured rate of  $2.97 \mu\text{mol g}_{\text{Ag}}^{-1} \text{ s}^{-1}$  suggesting that average particle size may not be adequate as a descriptor of the size distribution of the  $\text{Ag}/\alpha\text{-Al}_2\text{O}_3$  catalyst. Subsequently, we attempted to map changes in Ag particle size distribution to epoxidation rates instead of using the average diameter which does not capture the variance of the distribution.

$$\text{rate}(\mu\text{mol g}_{\text{Ag}}^{-1} \text{ s}^{-1}) = 0.39 + \frac{518.87}{\sqrt{2\pi} \times 0.36 \times D_{SA}} \times e^{-\frac{(\ln(\frac{D_{SA}}{129.68}))^2}{2 \times 0.36^2}} \quad (2)$$

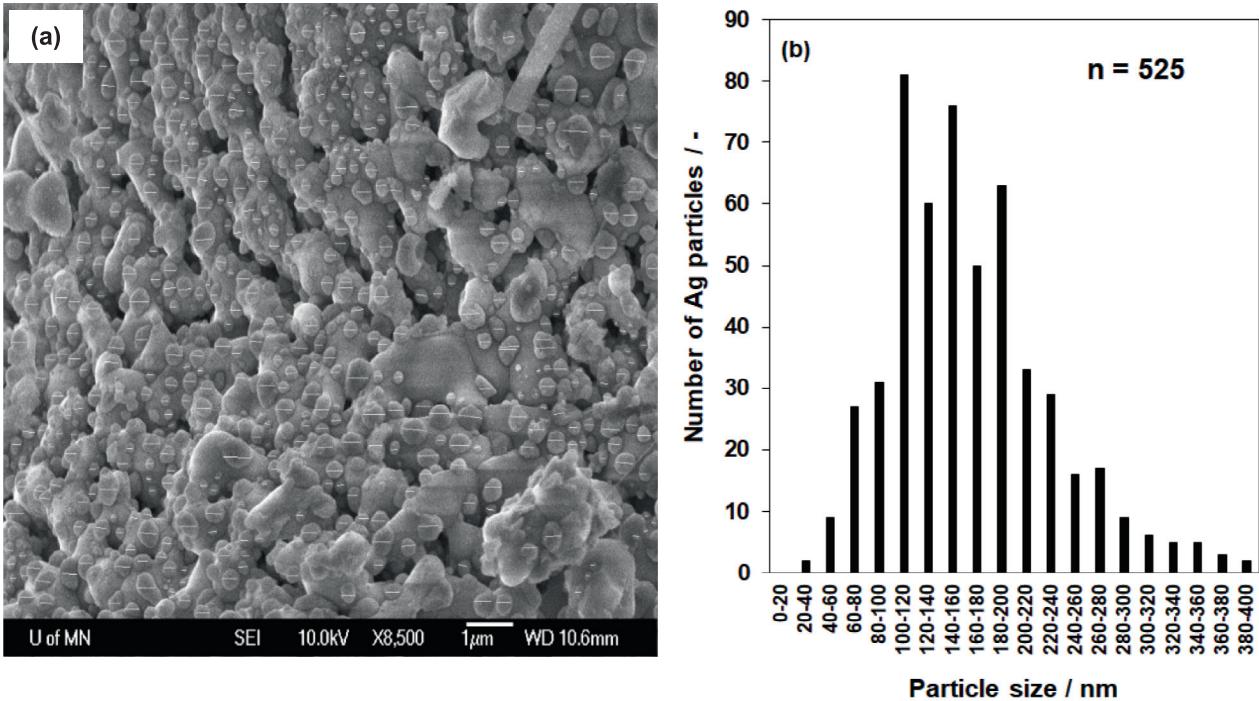
### 3.3. Mapping the particle size distribution to EO rates using rate functions

To incorporate the Ag particle size dependence of epoxidation rates we formulated a model based on the concept proposed by Weber [19] wherein the observed rate is a cumulative quantity that reflects accrual of contributions from Ag particles of different size. Mathematically, rate is described as an integral (Eq. (3)) of the product of two terms: (i) a rate function  $r(s)$  that gives the contribution of a particle of size ‘ $s$ ’ to the EO rate and (ii)  $A(s)$  which is the surface area exposed per gram (Eq. (1)) of particles of diameter ‘ $s$ ’, evaluated across the particle size range ( $R_{\min}$  to  $R_{\max}$ ). The surface area exposed per gram,  $A(s)$ , for all catalysts is fitted by a lognor-

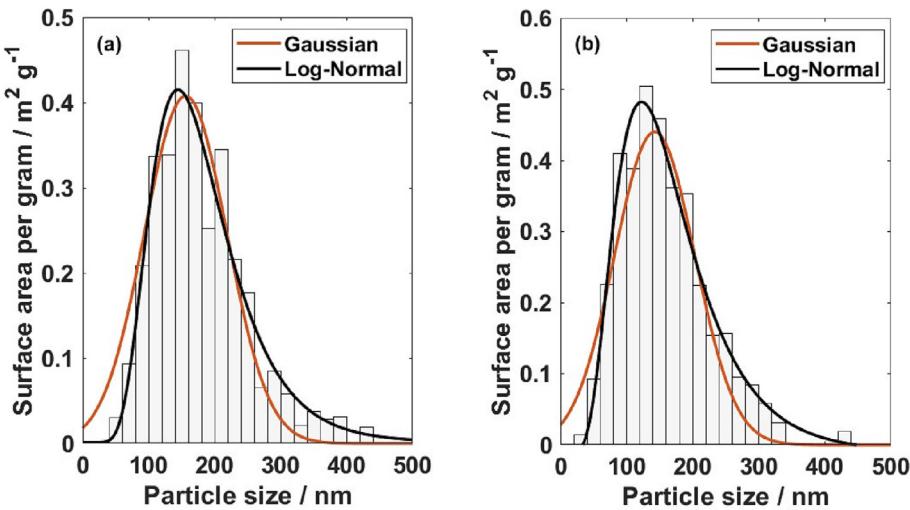
**Table 3**

Surface area weighted particle diameter ( $D_{SA}$ ), total surface area per gram, and mixture composition for physical mixtures of  $\text{Ag}/\alpha\text{-Al}_2\text{O}_3$  catalysts.

Sample name	$D_{SA}$ / nm	Total area per gram / $\text{m}^2 \text{Ag g}^{-1}$	Mixture composition
mix-1	$144.4 \pm 47.8$	3.9	30 wt% 35S-2 and 70 wt% 16.9S-2
mix-2	$181.6 \pm 59.4$	2.7	40 wt% 35S-4 and 60 wt% 9.9S-2
mix-3	$209.4 \pm 67.4$	2.3	30 wt% 35S-2 and 70 wt% 35S-5



**Fig. 1.** (a) Representative SEM image of sample 35S-4 (refer to Table 2). (b) Measured particle diameter count distribution for a sample of 525 Ag particles. 18 h steady state reaction conditions: 30 mol% C<sub>2</sub>H<sub>4</sub>, 7.7 mol% O<sub>2</sub>, 1 mol% CO<sub>2</sub>, 3.5 ppm C<sub>2</sub>H<sub>5</sub>Cl, 0.4 mol% C<sub>2</sub>H<sub>6</sub>, balance He; 5.3 bar; 513 K; catalyst mass = 0.034 g 35S-4.



**Fig. 2.** A histogram of exposed surface area per gram as a function of particle size for two catalyst samples (a) 35S-2 (refer to Table 2) and (b) 35S-1 (refer to Table 2) fitted to Gaussian and lognormal distributions.

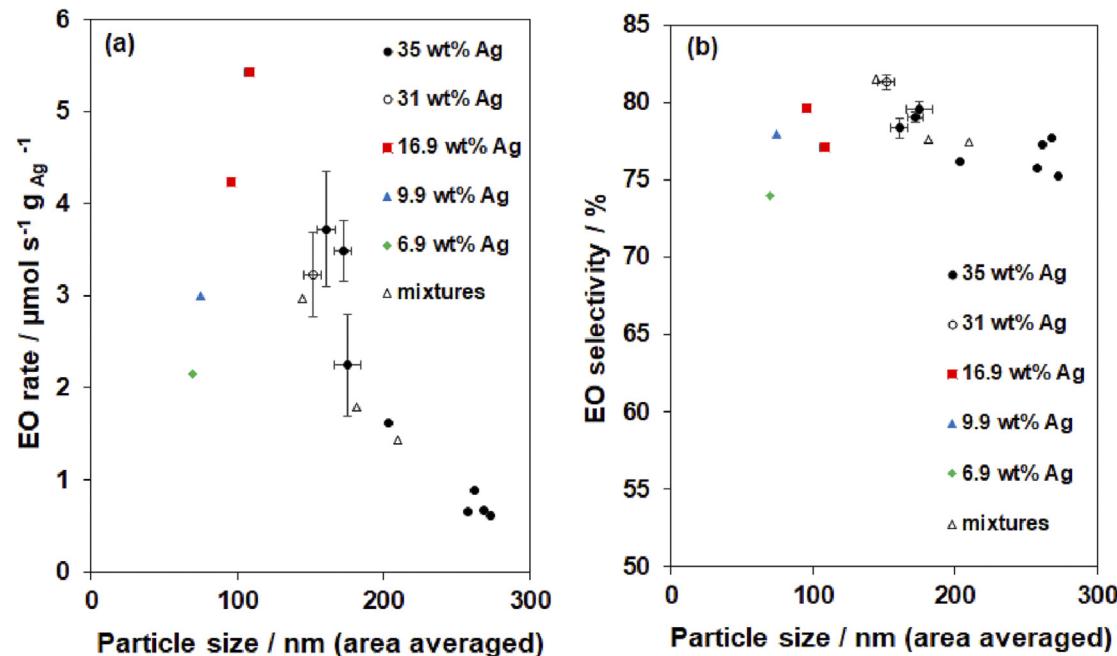
mal distribution (Eq. (5)) with A,  $\mu$ ,  $\sigma$  as its parameters (Fitted log-normal distribution functions for all catalysts are shown in Supporting Information Section S.9).

$$\text{rate}(\mu\text{mol g}_{\text{Ag}}^{-1} \text{s}^{-1}) = \int_{R_{\min}}^{R_{\max}} r(s) * (A(s)) ds \quad (3)$$

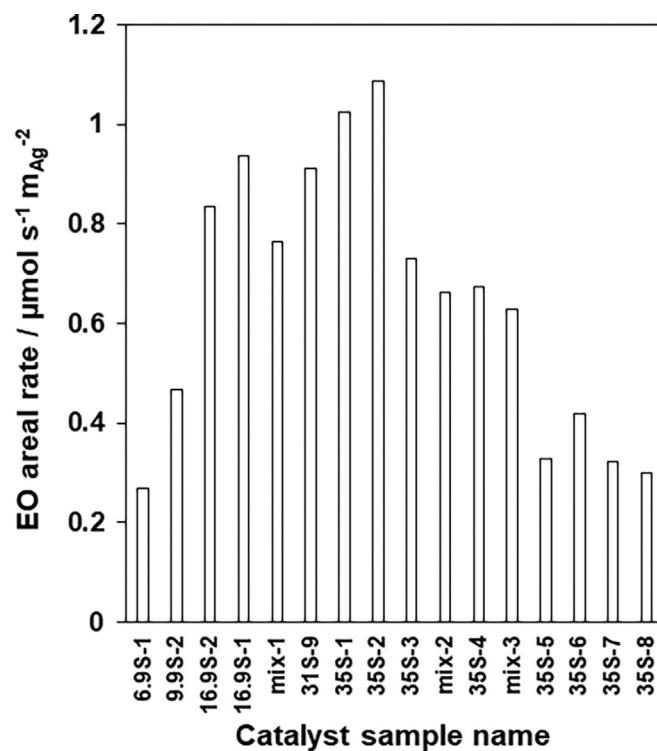
$$r(s) = ae^{-\frac{(s-\mu)^2}{2\sigma^2}} \quad (4)$$

$$A(s) = \frac{A}{\sigma\sqrt{2\pi}} e^{-\frac{(\log(\frac{s}{\mu}))^2}{2\sigma^2}} \quad (5)$$

The epoxidation rates and the surface area per gram fitted with a lognormal distribution (Eq. (5)) across 23 data points (includes replicates and physical mixtures of catalysts) were fitted to Eq. (3) using Athena Visual Studio to find the optimal rate function parameters for r(s). The function r(s) is unknown therefore, we evaluated different functional forms: power law, polynomials, and Gaussian for the rate function r(s) and used model discrimination statistics to obtain the best fit model (detailed statistics in Supporting Information Section S.6). A Gaussian rate function model (Eq. (4)) correlates the lognormal surface area distribution to measured epoxidation rates (Fig. 6 (a)) across a wide range of Ag particle sizes (5–400 nm) evidenced by the close agreement between the measured rates and the rates predicted by the Gaus-



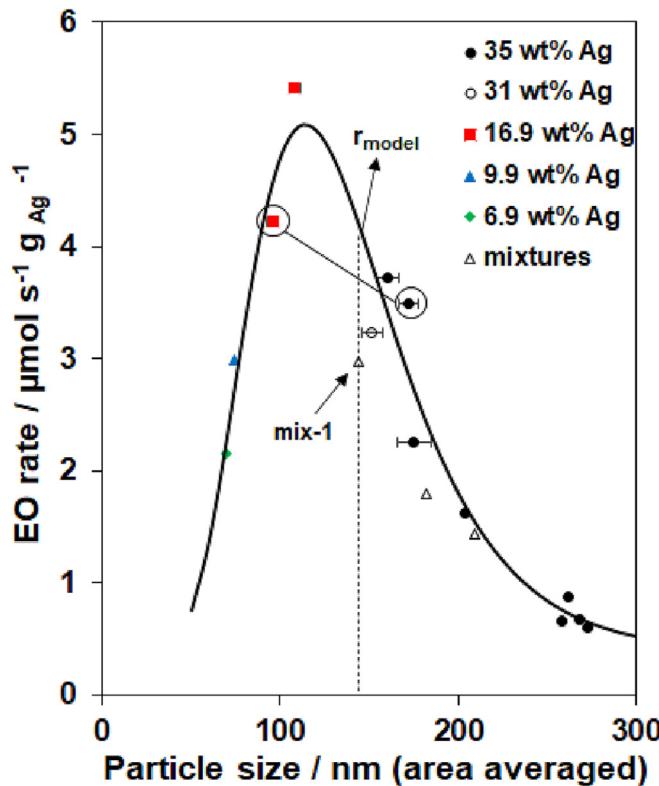
**Fig. 3.** (a) EO rates (b) EO selectivity measured as a function of surface area averaged particle size. Reaction conditions: 30 mol% C<sub>2</sub>H<sub>4</sub>, 7.7 mol% O<sub>2</sub>, 1 mol% CO<sub>2</sub>, 3.5 ppm C<sub>2</sub>H<sub>5</sub>Cl, 0.4 mol% C<sub>2</sub>H<sub>6</sub>, balance He; 5.3 bar; 513 K; catalyst mass = 0.027–0.082 g 6.9–35 wt% unpromoted Ag/ $\alpha$ -Al<sub>2</sub>O<sub>3</sub>. Data acquired at 18 h on-stream after steady state rates were obtained.



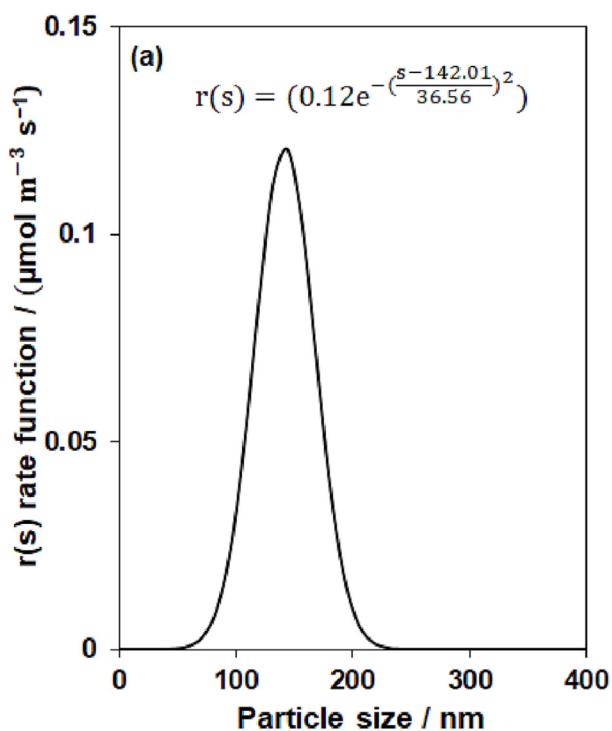
**Fig. 4.** Surface area normalized EO rates plotted for all the catalysts tested. Catalyst nomenclature follows the presentation in Tables 2 and 3.

sian rate function model (Fig. 6 (b)). The optimal rate function parameters for the Gaussian rate function are listed in Table 4. A more detailed discussion on the magnitude of errors in the measured EO rates and particle size distributions as well as model

parameter uncertainties is given in the Supporting Information Section S.7. A residual plot displaying the deviation of the EO rate predicted by the Gaussian model from the experimental value (% residual) for all catalysts (Supporting Information Figure S.9)



**Fig. 5.** EO rates measured as a function of surface area averaged particle size. The solid line is a lognormal fit according to Eq.2. Reaction conditions: 30 mol%  $\text{C}_2\text{H}_4$ , 7.7 mol%  $\text{O}_2$ , 1 mol%  $\text{CO}_2$ , 3.5 ppm  $\text{C}_2\text{H}_5\text{Cl}$ , 0.4 mol%  $\text{C}_2\text{H}_6$ , balance He; 5.3 bar; 513 K; catalyst mass = 0.027–0.082 g 6.9–35 wt% unpromoted Ag/ $\alpha$ - $\text{Al}_2\text{O}_3$ . Data acquired at 18 h on-stream after steady state rates were obtained.

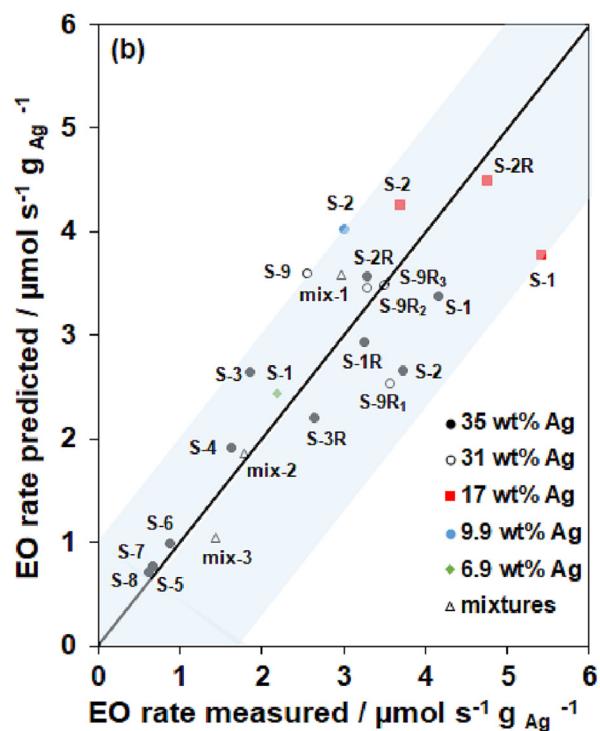


shows that three catalysts (35S-3, 16.9S-1, and 31S-9) primarily containing Ag particles of sizes <100 nm have residuals >30% and thus deviate slightly from the parity line in Fig. 6 (b). Catalysts (35S-5, 35S-6, 35S-7, 35S-8) containing a large fraction of Ag particles with sizes >180 nm have much smaller residuals (<15%) implying that Gaussian model captures rate contributions from large particles better compared to the ones <100 nm.

Consider two catalysts: 35S-2 (Table 2) and mix-2 (Table 3) that have similar average particle sizes of 176.1 nm and 181.6 nm respectively but exhibit almost 2× differences in EO rates (35S-2 – 3.49  $\mu\text{mol g}^{-1} \text{s}^{-1}$ , mix-2 – 1.79  $\mu\text{mol g}^{-1} \text{s}^{-1}$ ). A description based on average particle size (Eq. (2)) would predict similar rates (35S-2 – 2.66  $\mu\text{mol g}^{-1} \text{s}^{-1}$ , mix-2 – 2.46  $\mu\text{mol g}^{-1} \text{s}^{-1}$ ) for the two samples as it lacks information about the breadth of the distribution as well as the population of different particle sizes that constitute the distribution. The distribution of surface area per gram for the two catalysts (Fig. 7) not only reveals the broader span of particle sizes in mix-2 but also the higher fraction of particles between 140 nm and 180 nm in 35S-2 that contributes to its higher observed EO rate which is captured by the Gaussian rate-function model (Fig. 6 (a, b)).

We can classify the samples listed in Table 2 in three categories based on the measured EO rates and Ag particle size distribution: (i) 6.9 wt% and 9.9 wt% catalysts containing small particle sizes between 40 and 80 nm that have intermediate EO rates  $\sim$ 2–3  $\mu\text{mol g}^{-1} \text{s}^{-1}$  (ii) 16.9 wt% and 35 wt% catalysts with intermediate particle sizes between 80 and 140 nm that have high EO rates  $\sim$ 4–5  $\mu\text{mol g}^{-1} \text{s}^{-1}$  (iii) 35 wt% catalysts with large particle sizes between 180 and 300 nm that have low EO rates  $\sim$ 0.5–1  $\mu\text{mol g}^{-1} \text{s}^{-1}$ . The surface area histograms for two or three catalysts in each of these three categories, are overlayed in Fig. 8 (a, b, c).

The Gaussian rate function model (Fig. 6 (a)) suggests that very small (5–50 nm) and very large Ag particles (>250 nm) have low

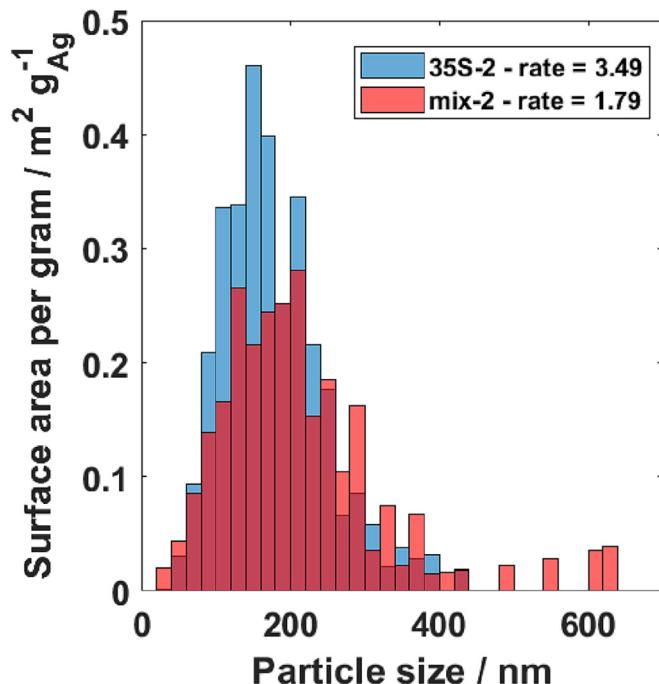


**Fig. 6.** (a) Variation of the fitted rate function model with particle size (b) Parity plot comparing the measured EO rates with rates predicted by the Gaussian rate function model (Eq.4). Each data point is associated with a catalyst having Ag weight loading as mentioned in the legend and the catalyst nomenclature from Tables 2 and 3 was used here with an additional letter 'R' to represent a replicate experiment.

**Table 4**

Fitted values for the parameters of the Gaussian rate function model described by Eq. (4). Uncertainties represent the 95% confidence intervals generated by Athena Visual studio.

Parameter	Value
a	$1.21 \times 10^{-1} \pm 1.33 \times 10^{-1} \mu\text{mol m}^{-3} \text{g}_{\text{Ag}}^{-1} \text{s}^{-1}$
b	$-1.42 \times 10^2 \pm 2.34 \times 10^1 \text{ nm}$
c	$3.66 \times 10^1 \pm 4.81 \times 10^1 \text{ nm}$



**Fig. 7.** A histogram of exposed surface area per gram as a function of particle size for two catalysts 35S-2 and mix-2 (Tables 2 and 3). The unit for rates of two catalysts mentioned in the legend is  $\mu\text{mol g}_{\text{Ag}}^{-1} \text{s}^{-1}$ .

reactivity whereas Ag particles  $\sim 130\text{--}150 \text{ nm}$  have optimal reactivity. Particle size dependent rates in ethylene epoxidation catalysis have been rationalized variously as arising due to:

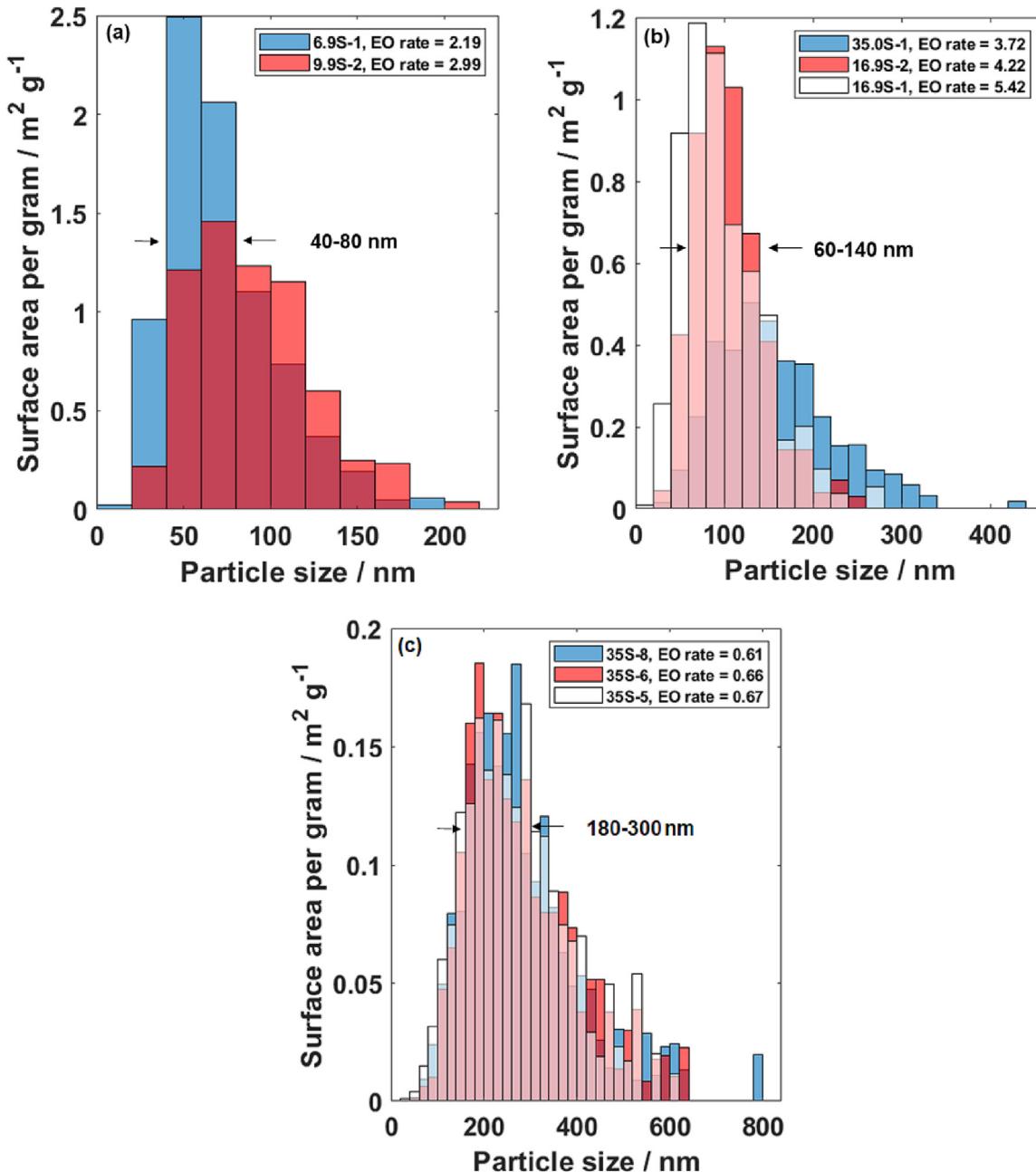
- (i) Geometric factors such as exposed crystal facets (e.g., Ag (110), Ag(111)) or different coordination environment of sites exposed by metal clusters: Steady state turnover rates for EO and  $\text{CO}_2$  production measured by Campbell [23] over Ag (111) and Ag (110) single crystal surfaces at 20 torr  $\text{C}_2\text{H}_4$  and 150 torr  $\text{O}_2$  at 490 K varied  $<2\times$  implying that variation in epoxidation rates of  $\sim 10\times$  that we observe (Fig. 3(a)) cannot be solely explained by differences in exposed facets with particle size.
- (ii) Electronic factors like metal work function/ binding energy or charge transfer between metal and support: Bukthiyarov et al. [24] have correlated the changes in ethylene consumption rates ( $0.2$  to  $5 \mu\text{mol m}^{-2} \text{catalyst (BET)} \text{s}^{-1}$ ) with Ag particle size (20 to 100 nm) to corresponding changes in Ag 3d<sub>5/2</sub> binding energies from 368.4 eV to 367.9 eV thus revealing electronic changes in Ag particles with increasing size.

- (iii) Particle morphology: Christopher and Linic [9] measured different ethylene epoxidation rates over  $\text{Ag}/\alpha\text{-Al}_2\text{O}_3$  catalysts having different shapes (100 nm nanospheres –  $1.9 \times 10^{-2} \text{ mmol g}_{\text{Ag}}^{-1} \text{ min}^{-1}$ , 90 nm nanocubes –  $2.3 \times 10^{-3} \text{ mmol g}_{\text{Ag}}^{-1} \text{ min}^{-1}$ , and 75 nm nanowires –  $1.2 \times 10^{-2} \text{ mmol g}_{\text{Ag}}^{-1} \text{ min}^{-1}$ ) at 510 K and 1 atm pressure suggesting a possible role of Ag particle morphology in inducing particle size effects.

Particle size effects manifest as changes in rate/equilibrium constants for elementary steps involved in ethylene epoxidation. Two plausible rate limiting steps have been proposed by Stegelmann et al. [25] based on microkinetic modeling studies: (i) adsorption of oxygen over silver and (ii) surface reaction between adsorbed ethylene and adsorbed oxygen. Lamothe et al. [26] treated a 5 wt%  $\text{Ag}/\text{SiO}_2$  catalyst containing sub-30 nm Ag particles and a 13.7 wt%  $\text{Ag}/\alpha\text{-Al}_2\text{O}_3$  catalyst containing Ag particles between 20 and 250 nm under  $1.67 \text{ cm}^3 \text{ s}^{-1}$  of 25%  $\text{O}_2/\text{Ar}$  at 1 bar and 483 K for 12 h prior to thermal desorption (heating rate of  $25 \text{ K min}^{-1}$  up to 973 K) under vacuum and found that the amount of oxygen desorbed was  $\sim 17\times$  higher in case of 5 wt%  $\text{Ag}/\text{SiO}_2$  ( $293 \mu\text{mol 'O' g}_{\text{Ag}}^{-1}$ ) compared to the 13.7 wt%  $\text{Ag}/\alpha\text{-Al}_2\text{O}_3$  ( $17 \mu\text{mol 'O' g}_{\text{Ag}}^{-1}$ ) catalyst. Moreover, the temperature of the maximum in oxygen desorption was 638 K for 5 wt%  $\text{Ag}/\text{SiO}_2$  compared to 440 K for 13.7 wt%  $\text{Ag}/\alpha\text{-Al}_2\text{O}_3$  which the authors attributed to stronger Ag-O interactions in smaller Ag particles. Li et al. [27] used DFT calculations and scaling relations to show that high O-binding energy ( $>1 \text{ eV}$ ) can increase activation barriers for the surface reaction of oxygen with ethylene despite facile  $\text{O}_2$  adsorption which is a plausible explanation for low rates over small Ag particles. Other factors such as changes in chlorine coverage or coverages of other surface intermediates with particle size could also play a role in inducing particle size effects. An extremum in epoxidation rate with particle size ( $\sim 130\text{--}150 \text{ nm}$ ) is likely caused by a combination of such factors. While the underlying cause to the observed particle size effect remains a topic of study, what is evident from the work we report is that the electronic and geometric attributes that contribute to these size effects should be associated with the Ag particle size distribution in ethylene epoxidation catalysis and these attributes are not captured by models that correlate measured rates to average particle size.

#### 3.4. Determination of optimal Ag particle size for ethylene epoxidation

The rate function model, that defines rate as the product of the rate function and exposed surface area per gram (Eq. (3)), can be used to determine the optimal Ag particle size that maximizes epoxidation rates. This is different from the size corresponding to the peak in the Gaussian rate function (142 nm) as shown in Fig. 6 (a). Hypothetically, we could generate catalyst samples containing Ag particles of identical sizes between 5 and 400 nm in intervals of 1 nm. At a given particle size  $s = D$ , the epoxidation rate is given by the product of the rate function  $r(D)$  and the exposed surface area per gram ( $A(D)$ ) calculated using Eq. (3) that varies with particle size as shown in Fig. 9. Expressing the rate as a continuous function of particle size in the form of a Gaussian function allows us to calculate  $\sim 140 \text{ nm}$  as the optimal size that maximizes epoxidation rate with EO selectivities  $>76\%$ . An  $\text{Ag}/\text{Al}_2\text{O}_3$  sample with a narrow size distribution centered around 140 nm would thus yield  $\sim 10\times$  higher rates per gram compared to distributions centered around very small ( $\sim 30 \text{ nm}$ ) or very large Ag particle sizes



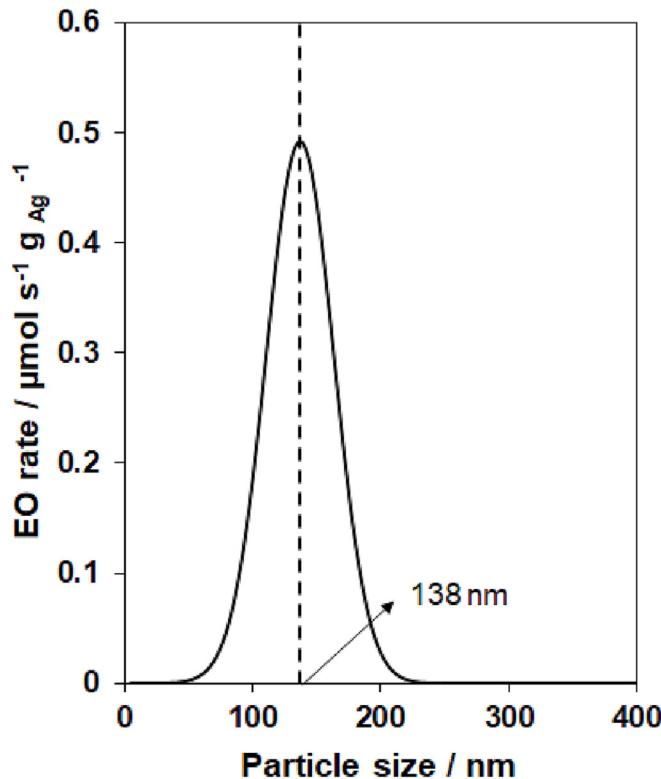
**Fig. 8.** A histogram of exposed surface area per gram as a function of particle size for (a) 6.9S-1, 9.9S-2 (b) 35S-1, 16.9S-1, 16.9S-2 (c) 35S-5, 35S-6, 35S-8 (refer to Table 2). The unit for rates for all catalysts mentioned in the legend is  $\mu\text{mol g}^{-1}\text{s}^{-1}$ .

(~250 nm) under the conditions of our study. Notably, a recent study from Egelske et al. [10] showed that Ag particles <100 nm exhibit a significantly lower EO selectivity of 58% compared to Ag particles >100 nm (EO selectivity ~ 73%) which the authors correlated with increased Ag sintering and carbon fouling over small Ag particles which reaffirms why large Ag particles (~130–150 nm) are beneficial in ethylene epoxidation catalysis under differential ethylene conversions as they exhibit high EO rates and EO selectivity. Under integral ethylene conversions effects such as gradients in chlorine coverage and changes in ethylene and oxygen reaction orders for EO formation along the reactor bed can impact

ethylene epoxidation rates and selectivity [28] which may result in a different optimal Ag particle size distribution.

#### 4. Conclusions

The effects of Ag particle size on ethylene epoxidation rates were studied over 6.9–35 wt% Ag/ $\alpha$ -Al<sub>2</sub>O<sub>3</sub> catalysts with varying particle size distributions. EO rates increase with average particle size until ~110 nm before decreasing with size. Particle size effects were better described when the Ag surface area (per gram)



**Fig. 9.** EO rates as a function of particle size calculated using the product of the rate function and exposed surface area per gram (Eq. (3)) at each particle size between 5 and 400 nm.

distributions of spent  $\text{Ag}/\alpha\text{-Al}_2\text{O}_3$  catalysts were correlated to the observed EO rates via a Gaussian particle size-dependent rate function over a wide range of particle sizes (5–400 nm) than a description based on average particle size as the latter omits details related to the breadth of the distribution and the population of particles of different sizes. The Gaussian rate function model reveals that very small Ag particles (5–50 nm) and large Ag particles (>250 nm) exhibit low EO rates which can plausibly be explained based on changes in the binding energy of oxygen and other surface intermediates with silver particle size. The model also suggests optimal particle size distributions of  $\text{Ag}/\alpha\text{-Al}_2\text{O}_3$  centered around (~140 nm) will facilitate high EO rates ( $>4 \mu\text{mol g}_{\text{Ag}}^{-1} \text{s}^{-1}$ ).

## Data availability

Data will be made available on request.

## Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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## Appendix A. Supplementary data

Supplementary data to this article can be found online at <https://doi.org/10.1016/j.jcat.2023.02.008>.

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