# Project 3A: Lil' Trie Adventure (alternative node definitions for smaller memory footprints)

## Introduction

We have studied *tries*, a specialized tree designed for the quick search of sequenced data such as words or IP addresses. Our lecture and 3P version of lowercase word tries allocated 26 pointers (208 bytes!) to store the .children[] of **each node**.

This project has you consider more specialized node structures designed to reduce the overall memory footprint of the 3P word trie and investigates the run-time trade-off in doing so.

For this assignment, please provide responses for the "deliverables" in this prompt. These will primarily consist of text in complete sentences, along with tables, charts, diagrams, and equations as needed or directed by the write-up. Your answers should be concise but complete. Diagrams or charts must be clearly labeled and readable; use of a software plotting tool (Excel, matplotlib, gnuplot, tikz, etc.) is required. Equations must be properly typeset (e.g., using the equation editor in your word processing software or an equation environment in LTEX). The rubric for each deliverable is at the end of the write-up.

# Part 1 — tooling up with child histograms

Clone the LilTrieAdventure repo according to the Canvas assignment instructions. Drop in your trie header and source file from the Trie programming project and follow the README.md instructions to make sure you can build run-main.

**Take Note 1**: The CMakeLists.txt expects your header and source to be trie.h and trie.cpp, but you can change these names if you choose.

Additionally, this write-up assumes you've used a nested class structure for your trie class, with the "internal" node structure named node. (This approach wasn't a requirement of 3P, you may have opted to use to a single object definition that was itself a node.) You aren't required to use the former but you'll need to make some mental translations for clean compiles. You're permitted to change any of the functions provided in liltrie.h — we are interested in your results, not so much the code gymnastics to get them.<sup>a</sup>

 $^{a}$ This would be a wonderful project to learn about C++ polymorphism, user-defined iterators and virtual base class design — but these are beyond the scope of this course and assignment. It makes me sad :/

The first thing we will do is add some statistics collecting member functions to your trie and node classes. We'll refer to the base 3P trie node structure as node, you may have called it something else, not a big deal. The trie:: versions of these functions are used by the provided code, they should all initiate a recursive chain of calls on the root's node:: children to "get the ball rolling."

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- void trie::finalize() {} and void node::finalize() {}: for now these function can do nothing, you may choose to use them in Part 4 of this analysis to reduce the amount of new code you have to write. (But these need to be implemented for compilations.)
- size\_t trie::size() should report the total number of words (*W*) stored in the trie (recall a word exists where node::is\_terminal is true). You may want to implement a size\_t node::size() helper function as well, which could return the number of words at or below the current node.

trie::size() will be used to help verify correct changes of your 3P trie node.

We will refer to the result of .size() as the variable W in this project.

Once you have these node member functions implemented and compiling cleanly, change the zero in main-test.cpp's #if line to a 1 and rebuild (make run-test). The test\_node\_functions<Y> parameterized function in main() will make sure your implementations compile cleanly. You will probably want to populate the string of vectors with data from the wordlists files for a more thorough test.

Expected values for the various word dictionaries used in this project are in the test\_node\_functions directory of the repo.

**Take Note 2**: If test\_node\_functions<Y> is called with a dictionary less than 2000 words or with sample=false, it will put all the dictionary vector's words into the trie. If the dictionary has more than 2000 words and sample=true, it will put a random number of words into the trie and test .contains() for both included and un-included words. The default value for the function is sample=false.

test\_node\_functions<Y> always **randomizes** the order in which words go into your trie and the order in which they are tested for appropriate .contains() results.

Now we want to collect some statistics about the structure of our project 3P trie after it has stored a dictionary of words. We will build a discrete count (or "cardinal") histogram of the number of children each node has in a trie.

A discrete data histogram records either the absolute number or the population percentage of a set of distinct attributes in a population. In this case the population is all the nodes in a trie, the attribute is the number of children the trie nodes have for a particular dictionary. For this task you will implement one or two more member functions:

- size\_t node::node\_children() reports the number of children a node has. You'll need to iterate through .children[] and return the count of non-nullptrs in the array.
- void trie::children\_histogram( vector<size\_t>& histo ) does two things:
  - i. it calls void node::children\_histogram( vector<size\_t>& histo ) for all of the trie's children (do this recursively!),
  - ii. node::children\_histogram also increments the node\_children() valued index in histo by one:

histo[this->node\_children()]++;

and recursively call children\_histogram on its children with the same histoparameter.

(You could choose to simply calculate the number of children in a node within children\_histogram, in which case you won't need node\_children for this project.)

Test these newly added functions with something like:

```
yourTrie trie;
vector<size_t> histo(LETTERS+1);
test_child_histogram( trie, words, histo );
```

Where words is a vector of words from one of the project dictionaries in the wordlists/directory of the repository (you've done similar word reading in 2A).

Compare the output results with the appropriately named files in child\_histogram/directory.

The value at histo[i] is the number of nodes in the trie that have i children (or the fraction of nodes in the trie with i children, if you are looking at the frequency histogram results). For instance, from the child\_histogram/words8.txt file, we see none of the eight words have sub-word prefixes because there are eight nodes with zero children (nodes without children are always terminal nodes, and there are eight words in the dictionary generating the histogram). There are 53 nodes with only one child, two nodes with two children and one node with six children.

## The "3P node" footprint

Let's now use our histogram tool to calculate the total memory footprint of the trie node structure presented in lecture and used in 3P as well as two other alternative trie designs.

**Take Note 3**: We'll use the following constants (conveniently defined in liltrie.h) to avoid inconsistent alignment and word sizes of each student's individual machines: INTBYTES, PTRBYTES, CHARBYTES and BOOLBYTES which are the sizes of (you guessed it) a signed or unsigned integer, a pointer, a char data type and a bool. **Don't** generate analysis data using sizeof() and don't worry about uncounted bytes due to alignment issues. Just pretend you're targeting an ARM Cortex-M like processor:)

The 3P trie node has a Boolean flag is\_terminal and LETTERS=26<sup>1</sup> pointers in a static array. Regardless of the number of children stored in a 3P trie node, its size is always

$$LnodeSize = BOOLBYTES + LETTERS \times PTRBYTES \tag{1}$$

If **N** is the number of nodes in the trie (the result of calling liltrie.h's nodecount() on the trie or its histogram):

$$LnodeFootprint(N) = N \times LnodeSize()$$
 (2)

<sup>&</sup>lt;sup>1</sup>Conveniently defined in liltrie.h.

# Part 2 — smaller footprints

We now consider two other node structures we expect will generate smaller memory footprints than the 3P trie node.

## Using a char→ node mapping, implemented as a chained hash table

We like to think of generic containers and data structures in computer science. We have LIFOs (implemented as stacks), FIFOs (implemented as queues), sequences (implemented as lists or vectors) and "priority queues" typically implemented with min or max heaps. A **map** or a **key-value pair container**<sup>2</sup> in CS is modeled after mathematical functions (which are also called "maps"). Maps connect elements in a domain ("keys") to values in a range.

C++ provides the std::unordered\_map container, and tries could be implemented by replacing the children array with a std::unordered\_map that associates char values to trie nodes. We'll call this alternative node implementation a trie\_Cnode, where the C stands for a **chained** hash table. We've studied these in lecture and will use our understanding of them to motivate our analysis. Conveniently, since chained and open-addressed hash tables have the same expected **performance**, we can use C++'s std::unordered\_map (which C++ implements as some form of hash table), to assess trie performance using nodes based on these data structures.

The trie\_Cnode structure could be:

```
struct trie_Cnode {
   struct C_link {
      char letter;
      trie_Cnode* edge;
      struct C_link* next;
   };
   bool is_terminal;
   trie_Clink* table[];
   size_t table_size;
   size_t count;
};
```

Where the table data member replaces the children array of the 3P trie as the container for character and edge pointer associations. The struct C\_link is an individual node of the hash table slots' singly linked lists. table\_size is the number of struct C\_link pointers allocated to the hash table array, and count is the number of character-edge pairs stored in the table chains.

Each trie node child will be held in a C\_link object which is a constant size, namely:

$$ClinkSize = CHARBYTES + 2 \times PTRBYTES$$
 (3)

<sup>&</sup>lt;sup>2</sup>also called **associative array**s

The size of the table[] array also depends on C, as we should keep the hash table load factor  $\leq 0.75$ . We'll think of this as a "doubling" hash table, so the number of table[] elements is the smallest power of 2 greater than or equal to  $\frac{C}{0.75}$ :

CtableSize(C) = 
$$2^{\left\lceil \log_2\left(\frac{C}{0.75}\right)\right\rceil}$$
 given  $C > 0$ , 0 otherwise (4)

The memory consumed by one trie\_Cnode, given **C** (the number of children it has), can be calculated as:

$$CnodeSize(C) = BOOLBYTES + 2 \times INTBYTES + (CtableSize(C) + 1) \times PTRBTYES + C \times ClinkSize (5)$$

Where the first two terms come from the simpler data members of trie\_Cnode and CtableSize and ClinkSize are from eqns 4 and 3 respectively. It may appear that we over count the number of PTRBYTES by one, but don't forget that the table[] data member needs PTRBYTES to store a pointer to the block of memory holding a table\_size array of pointers!

The total footprint of a C node trie can be calculated from its histogram of child counts, H:

$$CnodeFootprint(H) = \sum_{c \in H} CnodeSize(c) \times H[c]$$
 (6)

#### The smallest trie node structure

The 3P trie node definition and most other alternative node definitions over-allocate space for children. We can minimize the size of a trie node with some bit-twiddling and allocating a children[] array for only the number of children needed at each node.

We'll call this final node structure a trie\_Mnode, where M stands for "mask" or more accurately "bitmask". A bitmask uses a standard integer data type but treats each bit as a Boolean value. We'll assume *INTBYTES*  $\geq$  4 and thus we have at least 32 bits. We'll use *LETTERS* = 26 of the Booleans to track if a particular letter has an edge in the node and one more bit to store the is\_terminal property of the node.

The trie\_Mnode data declaration would be:

```
struct trie_Mnode {
  int mask;
  typedef trie_Mnode* trie_Mnode_ptr;
  trie_Mnode_ptr* children;
};
```

The memory footprint of the trie\_Mnode depends on the absolute number of children a node has, *C*. The memory footprint of a trie\_Mnode is simply:

$$MnodeSize(C) = INTBYTES + (C + 1) \times PTRBYTES$$
 (7)

Recall that the structure has a "built-in" pointer (children), and it will point to C trie\_Mnode\_ptrs in memory, hence the C+1 number of pointers, not just C.

The total footprint of an M node trie can be calculated from its histogram of child counts, H:

$$MnodeFootprint(H) = \sum_{c \in H} MnodeSize(c) \times H[c]$$
 (8)

# Part 3 — empirical evidence

## **Footprint data collection**

We want to investigate how the footprints of the 3P node, the Cnode and the Mnode compare for variously sized word sets.

Change your code in main.cpp to run collect\_child\_histogram with all the words from dictionary.txt at least 100 times.

```
for( size_t i=0; i<AT_LEAST_100; ++i ) {
   yourTrie trie;
   vector<size_t> H(LETTERS+1);
   collect_child_histogram( trie, dict, H);
   // calculate three data points
}
```

A random sample of the dictionary words will be used for each invocation. The result will be a wide range of word counts over all the runs. For each run of collect\_child\_histogram, determine the number of words stored in the trie (**W**) with trie::size(), and show in a scatterplot the three coordinate pairs:

Where:

- The dependent values are from equations (2,6,8) respectively
- H is the child histogram of the trie, valued by collect\_child\_histogram
- N = nodecount(H) /\*\* defined in liltrie.h \*/

## Deliverable 1

Show a properly labeled **scatterplot** of these coordinate pairs (9). Use three distinct symbols in your plot, treating each trie node definition as a plot series.

# Part 4 — the adventure

We have investigated how the overall memory footprint of a trie depends on the core trie node data structure. Your results should provide convincing evidence that substantial memory savings can be had. But are these savings in memory for free? We shouldn't think so, as both of the proposed alternative node structures will require more complicated algorithms for word insertion and tree traversals (eg: contains(), prefix finding and trie::size(), to name a few).

Consider this: with 3P node tries there is immediate access to the child pointer of a letter. It is simply .children[letter-'a'] (or  $\mathcal{O}(1)$  for those of you who are counting:)

With the trie\_Cnode, the **expected** cost of checking if an edge exists is **O(1)** (that's pretty good!), but there is arguably more work done compared to the 3P node implementation. Consider

```
if( this->children[letter-'a'] != nullptr ) // 3P node edge test
compared to

// trie_Cnode edge test
size_t slot = hash(letter) % this->table_size;
C_link* link = this->table[slot]
while( link != nullptr ) {
   if( link->letter == letter ) break;
   link = link->next;
}
if( link != nullptr ) // link->edge contains child pointer
```

Futhermore, the 3P implementation is a **gauranteed** O(1), whereas the trie\_Cnode is an **expected** measure of performance — is this really a big deal? You may well choose to investigate this as part of this project!

With the trie\_Mnode, we must first examine the bits in mask to determine if an appropriate letter edge exists. When new letter edges are added to a node we have to allocate and delete memory as well as shuffle pointer values to keep letter edges in alphabetical order.

Your task for the last part of this analysis is to implement **just one** of the two alternative node structures and compare its runtime performance against the 3P trie.

**Take Note 4**: **First**, don't trash your 3P trie! You'll need it for the runtime tests later in the project..

**Second**, if you add new header or source files to the project (alternatively you could just keep stickin' everything in trie.h and trie.cpp) you'll need to add their filenames alongside the trie.h and trie.cpp entries in CMakeLists.txt and possibly re-initialize your build directory with the cmake command.

**Lastly**, once you have your lil'trie class compiling cleanly and working with the time\_trials<Y,0> function (described below) — you should be ready for generating data. time\_trials<Y,0> does a very thorough job of making sure each trie is returning the anticipated results from contains tests. You shouldn't have to implement trie::size, trie::node\_children or trie::children\_histogram for the time trials.

You have **four choices**, which seems strange because there are only two node structures to choose from, let us explain:

## Choice: an on the fly node

You can write a brand new trie class and manage the node structure from start to finish. This means implementing the constructor, destructor, .insert() and .contains() (at least).

There may be more memory management required for this scheme (it depends on the alternative node you are implementing), but it's not too much to ask from students in this course. We call this "on the fly" because you are maintaining trie nodes while the whole trie structure is changing — your 3P was "on the fly" as well.

If you're just itchin' to implement one more data structure from scratch, follow the appropriate link:

Cnode "on the fly" instructions Mnode "on the fly" instructions

## Choice: nodes using .finalize()

You can also copy your current trie class definition<sup>3</sup> and only have to implement or rework the .finalize() and .contains() logic of your new class. The advantage to this approach is that it may not require any new memory management and you won't have to debug .insert(), constructor or destructor logic for a brand new class.

If this sounds more to your liking, follow the appropriate link: Cnode "finalize" instructions Mnode "finalize" instructions

# Part 5 — runtime performance

When you have your lil'trie class compiling cleanly, you're ready for the last bit of data generation in CSCI220!

Use the time\_trials<Y,0> function defined in liltrie.h to generate a pair of std::chrono::duration<double> values. The returned pair's .first is the runtime for the Y trie class, its .second is the runtime for the O trie class. The function should be provided with empty tries for comparison (the Y trie being your 3P trie, the O trie being your other lil'trie class implementation), a dictionary of words and an optional Boolean finalize parameter. The default value for finalize is true.

time\_trials<Y, 0> will take a random number of words from the dictionary, half will go into a trie, .finalize() is called on the trie, and then the trie is searched for all the words (half the queries will fail, half must succeed). The elapsed time is measured during the searching phase of the experiment (post .finalize()).

**Take Note 5**: If you have implemented an "on the fly" node, you can provide finalize=false and the timing results will reflect the total "load time" as well (all the .insert() calls). If you have implemented a "finalized" trie, you should use the default value for the finalize argument.

Your invocation might look like:

<sup>&</sup>lt;sup>3</sup>Or, if you're into the whole class hierarchy approach, you could inherit from your original trie class.

```
size_t W = trie3P.size();
cout << W << " " << secs.second.count() << endl;</pre>
```

**Take Note 6**: **Help! My machine is a beast!** If your machine is so fast that time\_trials<Y,0> doesn't generate reliable, repeatable run times, take a look inside liltrie.h. Increment the MY\_MACHINE\_IS\_A\_BEAST counter until you get reliable, repeatable timing results.

You will provide a scatterplot of these timing results for your submitted write-up to this project. Of course this could be a simple two series plot with **W** on the horizontal access and runtime on the vertical axis. However care has been taken in time\_trials<Y,0> to make sure that each trie sees the same order of words for both .insert()'ions and .contain()s tests — so it is legitimate to compare these values directly within one experiment.

Consider the following four styles of scatterplot graphs to show your results, if  $t_{3P}$  and  $t_0$  are the .first and .second values for one experiment:

a. You could plot the difference in time vs trie size:

$$(W, t_0 - t_{3P})$$

b. The percentage increase in runtime by the lil'trie class:

$$(W,(t_0-t_{3P})/t_{3P})$$

c. The difference in time normalized by the number of words in the trie:

$$(W,(t_0-t_{3P})/W)$$

d. Or you could plot the coordinate pair  $(t_{3P}, t_0)$  along with the line of identity (y = x). If these points lie on or near the line of identity it means the runtime performance is nearly identical. If the points lie above y = x, then  $t_0$  is consistently  $> t_{3P}$ .

#### Deliverable 2

Choose your preferred graphic presentation(s), make sure the axis, title and labels are accurate and provide a plot of your runtime results. **Also**, be sure to state whether you have coded an "on-the-fly" or .finalize() solution.

#### Deliverable 3

Among the implementations you've provided runtime results for (which includes the original 3P trie), which would you prefer to use in a real world application? What development or runtime factors might influence your choice?

Consider, for instance, the following scenarios:

- a. A desktop editor that uses a trie to provide word completion hints.
- b. A small resource-constrained (memory, storage space) customer service kiosk that uses a trie, populated by customer input, for completion hints to many different types of information: street addresses, ZIP codes, nine digit phone numbers, email addresses, ....

# Deliverable 4

Finally, copy and paste a nicely formatted version of the .contains() logic of your lil'trie class implementation and any other functions it may call. Use a fixed width font, single line spacing and consistent block indentation for this in your report.

## **Rubrics**

#### Rubric for Deliverable 1

- S Scatterplot has a title, correctly labeled axes. Plot shows results over a wide range of words. Data points **may be connected with lines** (it is reasonable to extrapolate between two points). Different symbols for each of the three trie node types must be used to denote actual data points.
- N Plot does not meet S criteria, has missing data, is poorly formatted or has poorly chosen axis ranges or scales.
- U No plot

#### Rubric for Deliverable 2

- S Scatterplot has a title, correctly labeled axes. Plot shows results for a wide range of independent axis values. Data points **should not be connected with lines**.
- N Plot does not meet S criteria, has missing data, does not support conclusions, is poorly formatted or has poorly chosen axis ranges or scales.
- U No plot

## **Rubric for Deliverable 3**

- S Response addresses the question, is correct and supported by features of the data or scatterplot(s).
- N Same as S, but there are errors/misunderstandings in the discussion.
- U No discussion

#### Rubric for Deliverable 4

- S Response is the student's Cnode or Mnode .contains() function and any helper functions it might call. Indentation of programming blocks and the use of {}s is consistent throughout. A fixed with font is used.
- N Insufficient, incorrect, or too much source provided. Formatting does not meet S standards. A variable width or difficult to read font is used.
- U No source provided.

# **Appendix: Cnode tries "on the fly"**

For "on the fly" implementations, you will need to implement the following for your node class:

- i. Constructor and destructor
- ii. .insert()
- iii. .contains()
- iv. If you run into development issues and wish to use test\_node\_functions for testing, you'll need to implement the .size() member function.
- v. If you wish to use collect\_child\_histogram for testing or debug, you'll need both .size() and child\_histogram member functions.
- vi. For "on the fly" implementations, you want to avoid memory leaks and corrupted data. Fortunately our runtime needs for your chosen lil'trie class are simple: allocate memory as needed in .insert() and make sure the destructor frees all memory for a node. You **really** want to avoid the stray typo or synapse misfire and accidentally copy construct or assign a node, because without these procedures properly implemented you will likely have very hard to debug issues when testing large tries. Recall that C++ will provide default (aka, dumb, wrong) versions of these "big 3" functions for you. You can prevent this by providing "delete" at the end of these declarations for in your class definition. So (for example) your node class called trie\_Xnode should have the following prototypes:

```
trie_Xnode( const trie_Xnode& trie ) = delete;
trie_Xnode& operator=( const trie_Xnode& rhs ) = delete;
```

Providing these will prevent C++ from using its default versions. You should do the same for your on the fly implementations.

**Take Note 7**: There are many online resources documenting the std::unordered\_map API and you will quickly notice there are several different ways to accomplish the general idea behind the operations "insert" and "query" or "find". We suggest looking at the documentation **examples** first, as these tend to demonstrate the easier to understand interfaces into the data structure.

**Take Note 8**: Furthermore keep in mind that the struct trie\_Cnode initially presented for "footprint" calculations is different than the one below. **Don't let this confuse you.** The former was a thought exercise for calculating the minimum memory required for a Cnode trie.

Now we want to investigate the runtime effects of using a O(1) hash table instead of the 3P trie's O(1) structure. To this end we hijack std::unordered\_map from the standard library.

In a professional environment, if our experimental results suggested the space  $\times$  time tradeoff would be beneficial in our application's tries, we would only then invest the time in implementing the initial, theorized, small footprint trie structure.

Your "on the fly" trie structure can be as simple as:

```
#include <unordered_map>
struct trie_Cnode {
  bool is_terminal;
  std::unordered_map<char,trie_Cnode*> childmap;
};
```

- 1. On any insertion of a new letter edge, the childmap should be queried for the appropriate letter (std::unordered\_map::find). If the letter edge exists, its "value" will be a pointer to that letter edge node. If it doesn't exist, a new trie\_Cnode should be allocated and std::unordered\_map::insert'd into the childmap keyed by the appropriate letter (char).
- 2. For .contains(), query the childmap for the appropriate letter (std::unordered\_map::find). If the "key" letter is found, its "value" will be a pointer to that letter edge node. If the query fails, the search fails.
- 3. The destructor can be tricky. Be sure to do a **post order** traversal of your trie nodes, deleting a parent node only after all its children (the values in the childmap key-value container) have been deleted.

# Appendix: Mnode tries "on the fly"

For "on the fly" implementations, you will need to implement the following for your node class:

- i. Constructor and destructor
- ii. .insert()
  iii. .contains()
- iv. If you run into development issues and wish to use test\_node\_functions for testing, you'll need to implement the .size() member function.
- v. If you wish to use collect\_child\_histogram for testing or debug, you'll need both .size() and child\_histogram member functions.
- vi. For "on the fly" implementations, you want to avoid memory leaks and corrupted data. Fortunately our runtime needs for your chosen lil'trie class are simple: allocate memory as needed in .insert() and make sure the destructor frees all memory for a node. You **really** want to avoid the stray typo or synapse misfire and accidentally copy construct or assign a node, because without these procedures properly implemented you will likely have very hard to debug issues when testing large tries. Recall that C++ will provide default (aka, dumb, wrong) versions of these "big 3" functions for you. You can prevent this by providing "delete" at the end of these declarations for in your class definition. So (for example) your node class called trie\_Xnode should have the following prototypes:

```
trie_Xnode( const trie_Xnode& trie ) = delete;
trie_Xnode& operator=( const trie_Xnode& rhs ) = delete;
```

Providing these will prevent C++ from using its default versions. You should do the same for your on the fly implementations.

Here is a quick synopsis of the trie\_Mnode structure and its workings. You should be familar with the terminology and concepts in the bitmask primer before embarking on this part of the project.

```
struct trie_Mnode {
  int mask;
  typedef trie_Mnode* trie_Mnode_ptr;
  trie_Mnode_ptr* children;
};
```

- 1. Bits 0–25 will be "up" or "on" if the cooresponding letter 'a'-'z' has an edge out of the node. The edge pointers are kept in children.
- 2. Bit 31 is used to store the is\_terminal property of the node.
- 3. The Mnode goal is to minimize a trie footprint, so children will always be perfectly sized for

$$\alpha = \sum_{i=0}^{i < LETTERS} bit\_on(mask,i)$$
 (10)

children at a node.

4. Letter  $\epsilon$ 's edge pointer in children depends on how many alphabetical order letters precede  $\epsilon$  in the node:

$$\delta = \epsilon \text{ index} = \sum_{i=0}^{i < \epsilon - 'a'} \text{bit\_on(mask,i)}$$
 (11)

where 'a' is the ASCII code for letter a.

For example: if  $\epsilon$  = 's' is the smallest letter with an edge in the node, its edge pointer index in children is 0. The letter edge index of  $\epsilon$  = 's' in a node also containing edges for 'g', 'q', 'u' and 'w' is 2, the edge for 'w' is 3.

- 5. On any insertion of a new letter edge, the children array must be grown by one (we suppose the letter value is again  $\epsilon$ :
  - i. Determine the initial number of children in the node ( $\alpha$ , eqn 10) and allocate a new trie\_Mnode\_ptr type array of size  $\alpha + 1$ .
  - ii. Turn the appropriate bit for  $\epsilon$  on in the mask (set\_bit\_on) and find  $\epsilon$ 's index in the newly allocated array (12).
  - iii. If  $\alpha > 0$ , copy any pre-existing edge pointers for indices  $< \delta$  from children to the same index in the newly allocated array.
  - iv. Allocate a new trie\_Mnode at index  $\delta$  in the new array.
  - v. If  $\delta < \alpha$ , copy any pre-existing edge pointers for indices  $\delta \leq i < \alpha$  to index i + 1 in the new array
  - vi. delete children, and store the new array at children.

# Appendix: Cnode tries using finalize

For finalize implementations, you should make a copy of your 3P trie class as a starting point. Here are the changes you should expect to make to your lil'trie class:

- i. You will add some data members to the class, they won't be used until the testing harness loads all the words into the trie and calls finalize.
- ii. Of course, you'll need to implement a finalize function (more details soon).
- iii. You'll need to change contains function logic.
- iv. If you run into development issues and wish to use test\_node\_functions for testing, you'll need to implement the .size() member function.
- v. If you wish to use collect\_child\_histogram for testing or debug, you'll need both .size() and child\_histogram member functions.

**Take Note 9**: There are many online resources documenting the std::unordered\_map API and you will quickly notice there are several different ways to accomplish the general idea behind the operations "insert" and "query" or "find". We suggest looking at the documentation **examples** first, as these tend to demonstrate the easier to understand interfaces into the data structure.

**Take Note 10**: Furthermore keep in mind that the struct trie\_Cnode initially presented for "footprint" calculations is different than the one below. **Don't let this confuse you.** The former was a thought exercise for calculating the minimum memory required for a Cnode trie.

Now we want to investigate the runtime effects of using a O(1) hash table instead of the 3P trie's O(1) structure. To this end we hijack std::unordered\_map from the standard library.

In a professional environment, if our experimental results suggested the space  $\times$  time tradeoff would be beneficial in our application's tries, we would only then invest the time in implementing the initial, theorized, small footprint trie structure.

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We need add only one new data member to our trie class from 3P: a std::unordered\_map.

```
#include <unordered_map>
struct trie_Cnode {
  bool is_terminal;
  trie_Cnode* children[LETTERS];
  std::unordered_map<char,trie_Cnode*> childmap;
};
```

#### The finalize method

In the finalize method, you'll need to iterate through the children array, std::unordered\_map::insert'ing any non-nullptr entry into childmap with the appropriate letter edge char value.

#### The contains method

For .contains(), query the childmap for the appropriate letter (std::unordered\_map::find). If the "key" letter is found, its "value" will be a pointer to that letter edge node. If the query fails, the search fails.

The existing destructor for your 3P trie should be sufficient even though the pointer values are aliased inside of a node's childmap.

# Appendix: Mnode tries using finalize

For finalize implementations, you should make a copy of your 3P trie class as a starting point. Here are the changes you should expect to make to your lil'trie class:

- i. You will add some data members to the class, they won't be used until the testing harness loads all the words into the trie and calls finalize.
- ii. Of course, you'll need to implement a finalize function (more details soon).
- iii. You'll need to change contains function logic.
- iv. If you run into development issues and wish to use test\_node\_functions for testing, you'll need to implement the .size() member function.
- v. If you wish to use collect\_child\_histogram for testing or debug, you'll need both .size() and child\_histogram member functions.

You should be familar with the terminology and concepts in the bitmask primer before embarking on this part of the project.

First, a quick recap of the memory saving strategy of this trie. An Mnode trie uses the minimum amount of memory for a trie node. An integer mask member variable uses bits as Boolean values to keep track of letters associated with child edges and whether or not the node is "terminal" (ends a word). We'll mimick the use of a minimally sized children array by packing all the edge pointers created during "word loading" to the front of children in the finalize logic.

- 1. Bits 0–25 will be "up" or "on" if the cooresponding letter 'a'-'z' has an edge out of the node. The edge pointers are kept in children.
- 2. Bit 31 is used to store the is\_terminal property of the node.
- 3. Letter  $\epsilon$ 's edge pointer in children depends on how many alphabetical order letters precede  $\epsilon$  in the node:

$$\delta = \epsilon \text{ index} = \sum_{i=0}^{i < \epsilon - 'a'} \text{bit\_on(mask,i)}$$
 (12)

where 'a' is the ASCII code for letter a.

For example: if  $\epsilon$  = 's' is the smallest letter with an edge in the node, its edge pointer index in children is 0. The letter edge index of  $\epsilon$  = 's' in a node also containing edges for 'g', 'q', 'u' and 'w' is 2, the edge for 'w' is 3.

We need to add only one new data member to our 3P trie class: an integer mask. It should be initialized to zero in the constructor.

#### The finalize method

In the finalize method, you'll need to:

- a. Set bit index 31 "on" or "up" in the node's mask if is\_terminal is true.
- b. Compress the non-nullptr values in children to the front of children, and record the ones that exist in mask:

```
if( is_terminal ) set_bit_on(mask,31);
unsigned c=0;
for( unsigned i=0; i<LETTERS; ++i ) {
    if( children[i] != nullptr ) {
        set_bit_on(mask,i);
        children[c++] = children[i];
    }
}
while( c < LETTERS ) children[c++] = nullptr;</pre>
```

### The contains method

The contains method should first check if the  $\epsilon$  – 'a' bit of mask is "on" or "up" (where  $\epsilon$  is the letter value of the next character in the word). If the flag is up, a child edge exists and is at the  $\delta$  index of chidren (equation 12).

## Appendix: A quick primer on bitmasks and their manipulation

We often refer to the bits in a bitmask as "flags": a 1 represents an "up" flag, representing true, whereas 0 represents false. In this project, an "up" flag for some character tells us the children array will have a pointer for this character edge. The mask layout (labeling the bits with indices 0–31) would be

bit index	0	1	2	3	4	5	 23	24	25		31
associated with	'a'	'b'	'c'	'd'	'e'	'f'	 'x'	'y'	'z'	(unused)	is_terminal

A bitmask in an Mnode that terminated a word and had child edges for the letters 'b', 'f' and 'p' would have a mask value of 0x80008022 in a debugger print out, the leftmost 0x8 nibble is the "up" is\_terminal flag, the last 0x2 nibble is the flag for character 'b'. The children data member would hold three trie\_Mnode pointers, the first for the 'b' edge, the second for the 'f' edge, the last for the 'p' edge.

To manipulate the bit values of an integer mask, you can use the following functions found in bitwiseops.h:

```
// bit is 0 to 31, returns true if bit in mask is "on"
static inline bool bit_on( unsigned mask, unsigned bit )
{ return mask & (1<<bit); }

// bit is 0 to 31, sets the bit to "on"
static inline void set_bit_on( unsigned & mask, unsigned bit )
{ mask |= (1<<bit); }

// bit is 0 to 31, sets the bit to "off"
static inline void set_bit_off( unsigned& mask, unsigned bit )
{ mask &= (1<<bit); }</pre>
```