STAT5303HW10

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11/20/2020

```
library(cfcdae)

## Registered S3 method overwritten by 'DoE.base':

## method from

## factorize.factor conf.design

library(car)

## Loading required package: carData

## Registered S3 methods overwritten by 'car':
```

from

lme4

1me4

1me4

dfbetas.influence.merMod library(knitr)

method

influence.merMod

dfbeta.influence.merMod

E15.1, E15.3, P15.1(a-e), P15.2(a-e), P15.3, P15.4

cooks.distance.influence.merMod lme4

E15.1

##

##

##

I will consider to use the even odd method with two defining contrasts BCD and ACD to get four blocks of eight.

Table 1: Blocks

Treatments	ACD	BCD
(1)	e	е
a	O	e
b	e	O
\mathbf{c}	O	O
d	O	O
ab	O	O
ac	e	O
ad	e	O
bc	O	e
bd	O	e
cd	e	e
abc	e	e
abd	e	e
acd	O	e
bcd	e	O
abcd	О	0

e_e	e_o	o_e	0_0
$\overline{(1)}$	b	a	c
cd	ac	bc	d
abc	ab	$_{\mathrm{bd}}$	ab
abd	bcd	acd	abcd

Table 3: 15 Confunded Effects

Generators	TwoWay	ThreeWay	FourWay
ABCF ABDE ACDE BCDH	CDEF BDEF ADFH BC ACEF ABEF	AF BEFH CEFH DH	ABCDEFH

P15.1

- (a) In the experiment, the treatment is different spatial scales and I will specifically set the levels of treatment are a meter of each other, two meters of each other, three meters, four meters and five meters of each other. For each level, there are 10 measurement. Besides, 10 blocks of 5 units each can be used. Thus, we can do a randomized complete design.
- (b) In this experiment, we have three factors with 2 levels so that it is a two series factorial design. So, we have 8 combinations of treatments in total and each combination has 2 measurments. Besides, we treat the variable day as a block. So, we have 4 blocks with 4 units in each block. Thus, we can do an incomplete block design.
- (c) In this experiment, we have four different designs of arterial stints and three major coronary arteries so that we have 12 combinations. And, we can let animal be the block. It follow that we have 12 blocks with 3 units in each block. This is an incomplete block design.
- (d) In this experiment, we have three factors and all them has 2 levels so it is a two series factorial design. In total, we have 8 combinations and each combination has 6 measurements. Because we can only make eight measurements before the equipment needs to be cleaned and recalibrated, we can treat the equipment as blocks. Thus, we have 6 blocks and each block has 8 units. It is an incomplete block design.
- (e) In this experiment, we have three factors A,B and C, and, all factors has 2 levels. If we do not think there is large differences between devices, we can use these three factors to do ANOVA test. However, if we expect large device to device differences, we should let the device be block. Further, the block design is better.

P 15.2

(a) This is an incomplete block design. We have 2 blocks. One of them contains a low rigor/pharma abstract and a high rigor/NIH abstract combinations. Another one contains a low rigor/NIH abstract and a high rigor/pharma abstract.

Source DF

Block 2

Attribution 1

Rigor 1

Attribution.Rigor 1

(b) This is an incomplete block design. The treatment is the brand of booties with 6 different brands. The vraiable day is viewd as block. So, we have 15 blocks and each block has 4 units.

Source DF

Day 14

Brand 5

Error 39

(c) In this experiment, we have 2 factors with 2 level, which is a two series factorial design. Four combinations of treatment and each combination has 10 measurements. Bacause the warmer is not uniformly warm and differs slightly in temperature from back to front, there is a diffrence in dishes. Thus, the dishes should be blocks in this experiment because it might cause variability. This is an incomplete block design with four blocks. For each row, the two dishes are in a block.

Source DF

Dishes 3

Choline 1

Protein 1

Choline.Protein 1

Error 32

(d) Sessions and drugs are treatments with 2 levels. When we expect there exits diffrence in subjects, it is appropriate to treat subjects as blocks. Each block contains 2 combinations of session and drug. This is an incomplete block design.

Source DF

Subjects 29

Sessions 1

Drugs 1

Sessions.Drugs 1

Error 26

(e) In this experiment, we have fifteen level combinations. Each combination has 2 replications. Apparently, the day is the block. Each block has 10 units which is 10 combinations of two levels of the charge and all levels additive.

Source DF

Day 2

Charge 2

Additive 4

Charge. Additive 8

Error 13

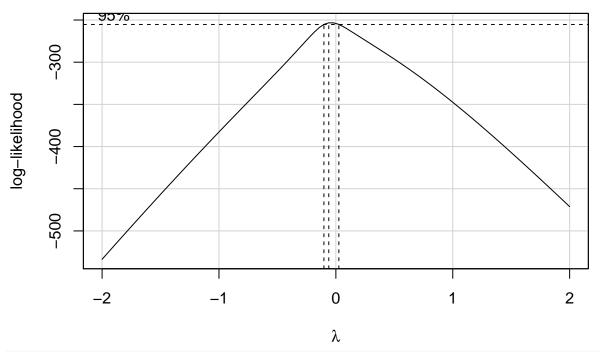
P15.3

```
data(OdorIntensity)
attach(OdorIntensity)
head(OdorIntensity)
```

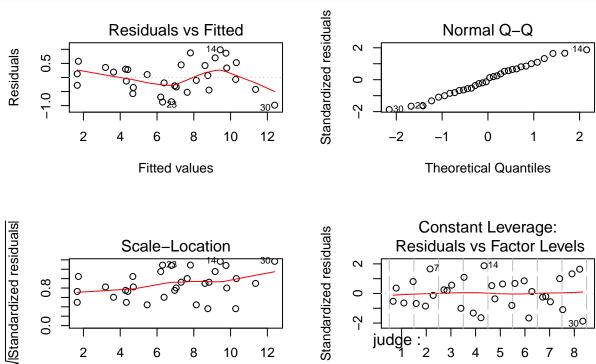
```
В
                         С
                              D concentration
     judge
              Α
## 1
                                         8389
            low
                low
                      low
                           low
## 2
         1 low high high low
                                          816
## 3
                                            4
         1 high high low high
## 4
         1 high low high high
                                           46
```

```
## 5
          2 high low low low
                                               4351
## 6
          2 high high low
                                                 78
judge<-as.factor(judge)</pre>
##First fitting a full model with judge:
mod<-lm(concentration~judge+A*B*C*D,data=OdorIntensity )</pre>
##Checking assumptions:
par(mfrow=c(2,2))
plot(mod)
                                                     Standardized residuals
                                                                         Normal Q-Q
                 Residuals vs Fitted
                                                                  00 0 <sup>270</sup>
      20000
                           270
Residuals
                                                          0
      -20000
                                  0
                                                          7
                     20000
                                    60000
                                                                -2
                                                                                0
                                                                                        1
                                                                                               2
                 0
                      Fitted values
                                                                      Theoretical Quantiles
                                                                     Constant Leverage:
/|Standardized residuals
                                                     Standardized residuals
                   Scale-Location
                                                                 Residuals vs Factor Levels
                      0 011270
                                0 0
                                                                                  170
                                                                                                0
      0.8
                                                                       0 000
                                                                             0
                                                                                  ၀ ၀၀
                                                          0
                                                                  000
                                                                               0 0
                                                                                        000
      0.0
                                                          ۲
                                                                            011
                                    60000
                                                                          3
                 0
                     20000
                                                                                  5
                                                                                       6
                                                                                              8
                      Fitted values
                                                                    Factor Level Combinations
##Apparently, the constant variance is not good since it has a curve.
par(mfrow=c(1,1))
```

boxCox(mod)







Factor Level Combinations

Fitted values

```
mod 1$coefficients
##
    (Intercept)
                      judge1
                                   judge2
                                                judge3
                                                             judge4
                                                                          judge5
   6.845578696 -1.607072018 1.062719503 -2.080618471 -0.806662546
                                                                    1.141405457
##
         judge6
                      judge7
                                      A1
                                                   B1
                                                                 C1
                                                                             D1
A1:D1
##
          A1:B1
                       A1:C1
                                   B1:C1
                                                             B1:D1
                                                                          C1:D1
##
  -0.270995112 -0.187488653
                             0.143915100
                                                   NA -0.008112085 -0.260149961
##
       A1:B1:C1
                   A1:B1:D1
                                 A1:C1:D1
                                             B1:C1:D1
                                                       A1:B1:C1:D1
                0.191649287 -0.013750007
                                                   NA 0.112794774
##
anova (mod 1)
## Analysis of Variance Table
##
## Response: log(concentration)
            Df Sum Sq Mean Sq F value
##
                                          Pr(>F)
              7 60.710
                        8.673 11.7590 0.0001586 ***
## judge
## A
              1 98.026
                       98.026 132.9079 7.548e-08 ***
## B
              1 74.362
                       74.362 100.8229 3.426e-07 ***
## C
              1 0.862
                        0.862
                                1.1686 0.3009266
## D
              1 10.788
                       10.788
                              14.6273 0.0024193 **
                2.350
                        2.350
                                3.1863 0.0995380
## A:B
              1
## A:C
              1
                1.125
                        1.125
                                1.5251 0.2404777
                        0.663
                                0.8986 0.3618536
## B:C
              1
                0.663
## B:D
              1
                0.002
                        0.002
                                0.0029 0.9582659
## C:D
              1
                2.166
                        2.166
                                2.9364 0.1122962
## A:B:D
                        1.175
                                 1.5936 0.2307968
              1
                1.175
## A:C:D
              1
                0.006
                        0.006
                                0.0082 0.9293287
## A:B:C:D
              1
                0.407
                        0.407
                                 0.5520 0.4717972
## Residuals 12
                8.851
                        0.738
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
This is a two series factorial design with four factors and judge is as block. The ANOVA table shows the
terms A,B,D and judge have significant difference so there is no significant interaction term.
P15.3
data("Milfoil")
attach(Milfoil)
## The following objects are masked from OdorIntensity:
##
##
       A, B, C
head(Milfoil)
     tank
             Α
                 В
                       C biomass
## 1
        1 low low
                    low
                            10.4
## 2
        1 high high low
                            17.5
## 3
        1 high low high
                            22.2
## 4
                            27.7
          low high high
## 5
        2 high low
                    low
                            4.8
## 6
       2 low high low
                            8.9
```

##It is abvious that the constant variance and normality are improved.

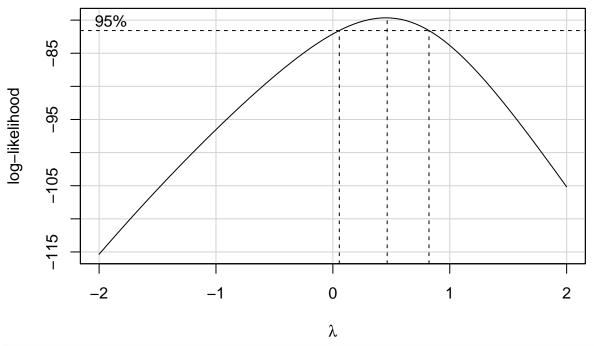
par(mfrow=c(1,1))

```
tank<-as.factor(tank)</pre>
##First fitting a full model with judge:
lmod<-lm(biomass~tank+A*B*C,data=Milfoil )</pre>
##Checking assumptions:
par(mfrow=c(2,2))
plot(lmod)
                                                       Standardized residuals
                  Residuals vs Fitted
                                                                             Normal Q-Q
                                                                    O31
                                                                                                   310
Residuals
                       00
                               0
                                             ٥٥
      0
      4
                               <sub>20</sub>060
            5
                              20
                                   25
                                         30
                                               35
                                                                   -2
                                                                                    0
                                                                                                    2
                  10
                        15
                                                                           -1
                       Fitted values
                                                                          Theoretical Quantiles
                                                                        Constant Leverage:
/|Standardized residuals
                                                       Standardized residuals
                    Scale-Location
                                                                     Residuals vs Factor Levels
                             0 0 0
                                             00
      0.8
                        00
                                             0
                                                             0
                                        0
                 0
      0.0
                                                             7
                                               35
            5
                  10
                        15
                              20
                                   25
                                         30
                                                                             3
                                                                                  4
                                                                                      5
                                                                                           6
                                                                                                   8
```

The constant variance and normality is not bad but the boxCox suggest 0.5 power better.
par(mfrow=c(1,1))
boxCox(lmod)

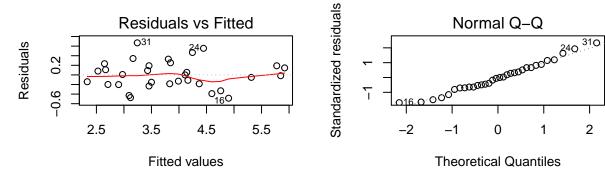
Factor Level Combinations

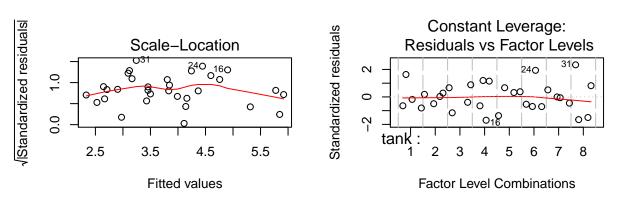
Fitted values



```
##Refitting the model:
lmod_1<-lm(biomass^(0.5) ~tank+A*B*C,data=Milfoil )</pre>
##Checking assumptions again:
par(mfrow=c(2,2))
plot(lmod_1)
```

2





The constant variance and normality have been improved. par(mfrow=c(1,1))

anova(lmod_1) ## Analysis of Variance Table ## ## Response: biomass^(0.5) ## Df Sum Sq Mean Sq F value Pr(>F) ## tank 7 15.3510 2.1930 14.2064 5.597e-06 *** 0.3323 0.3323 2.1527 ## A 0.16057 ## B 8.9774 8.9774 58.1561 6.961e-07 *** 4.7941 ## C 4.7941 31.0566 3.367e-05 *** 1 ## A:B 0.0522 0.0522 0.3380 0.56863 1 ## A:C 1 0.0280 0.0280 0.1815 0.67543 ## B:C 1 0.4796 0.4796 3.1070 0.09593 . ## A:B:C 1 0.0687 0.0687 0.4448 0.51376 ## Residuals 17 2.6242 0.1544 ## ---0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1 ## Signif. codes: lmod_1\$coefficientsc

NULL

This is a two series factorial design with 3 factors and tank is as block. The ANOVA table shows only the terms B,C and tank have significant difference and none of the interaction terms is significant.