

Stat3032HW1

Mingming Xu

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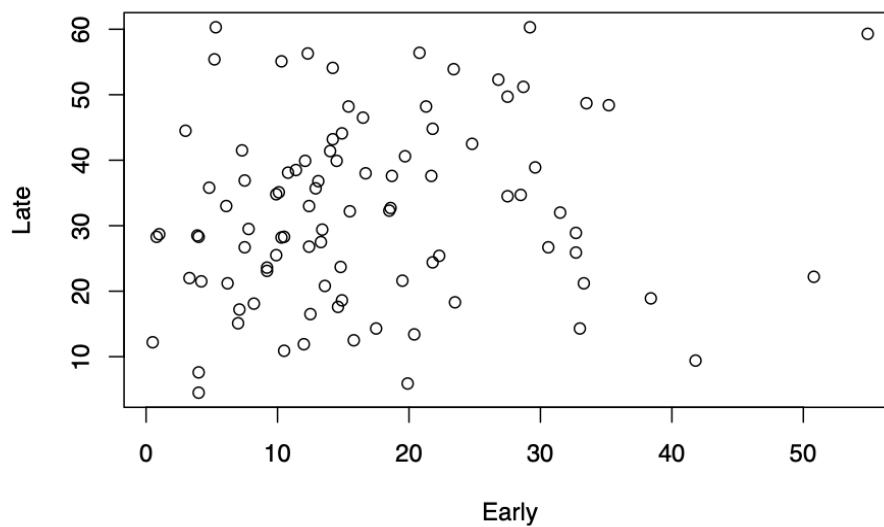
Problem 1

```
library(alr4)
```

```
## Loading required package: car
## Loading required package: carData
## Loading required package: effects
## lattice theme set by effectsTheme()
## See ?effectsTheme for details.
data(ftcollinssnow)
```

Part a

```
plot(Late~Early,data=ftcollinssnow )
```



Part b

```
model=lm(Late~Early,data = ftcollinssnow)
summary(model)

##
## Call:
## lm(formula = Late ~ Early, data = ftcollinssnow)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -27.7416  -9.3898  -0.1393   8.8177  30.5857
```

```
##
## Coefficients:
##           Estimate Std. Error t value Pr(>|t|)
## (Intercept)  28.6358     2.6149  10.951  <2e-16 ***
## Early        0.2035     0.1310   1.553   0.124
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 13.72 on 91 degrees of freedom
## Multiple R-squared:  0.02581,    Adjusted R-squared:  0.01511
## F-statistic: 2.411 on 1 and 91 DF,  p-value: 0.1239
```

Part c

Test statistic: t=10.951

P-value:<2e-16

Conclusion:p value<0.05, reject the null hypothesis.

Part d

Test statistic:t=0.2035

P-value=0.124

Conclusion:p value>0.05, refuse to reject the null hypothesis.

Part e

I believe that we cannot use it.Because in the part c, we refuse to reject the hypothesis $\beta_1 = 0$.Hence, we cannot use the coefficient β_1 value to predict late season snowfall.

Problem 2

```
xbar=mean(ftcollinssnow$Early)
ybar=mean(ftcollinssnow$Late)
SXY=sum((ftcollinssnow$Early-xbar)*(ftcollinssnow$Late-ybar))
SXX=sum((ftcollinssnow$Early-xbar)^2)
RSS=sum((ftcollinssnow$Late-28.6358-0.2035*ftcollinssnow$Early)^2)
Betahat1=SXY/SXX
Betahat0=ybar-Betahat1*xbar
sigmahatsq=RSS/91
```

xbar=16.7440860215054

ybar=32.0430107526882

SXY=2229.01365591398

SXX=10954.0692473118

RSS=17118.83205735

Betahat1=0.203487270856991

Betahat0=28.6358023861774

sigmahatsq=188.119033597253

Problem 3

$$SXX = \sum_{i=1}^n (x_i - \bar{x})^2 = \sum_{i=1}^n (x_i^2 - 2 * x_i * \bar{x} + \bar{x}^2) = \sum_{i=1}^n x_i^2 - 2 \sum_{i=1}^n x_i * \bar{x} + \sum_{i=1}^n \bar{x}^2 = \sum_{i=1}^n x_i^2 - 2 * n * \bar{x} * \bar{x} + n * \bar{x}^2 = \sum_{i=1}^n x_i^2 - n * \bar{x} * \bar{x} = \sum_{i=1}^n x_i^2 - \sum_{i=1}^n x_i * \bar{x} = \sum_{i=1}^n x_i * (x_i - \bar{x})$$

Problem 4

(a)

```
tcrit=qt(0.975,28)
0.6417099+c(-1,1)*tcrit*0.1222707
```

```
## [1] 0.3912497 0.8921701
```

(b)

Test statistic:

```
t=(0.0112916-0.01)/0.0008184
```

P-value:

```
2*(1-pt(t,28))
```

```
## [1] 0.1257517
```

Conclusion:

P-value is larger than 0.05, the value of alpha, so refuse to reject the null hypothesis. There is no sufficient evidence that processing time has a relationship with the number of invoices.

(c)

For 130 invoices, $\hat{Time} = 0.6417099 + 0.0112916 * Invoices$, the point estimate is $0.6417099 + 0.0112916 * 130 = 15.32079$

```
xbar=130
tcrit=qt(0.975,28)
sxx=(0.3928/0.0008184)^2
sepred=0.3298*sqrt(1+1/30+((130-xbar)^2)/sxx)
(0.6417099+0.0112916*130)+c(-1,1)*tcrit*sepred
```

```
## [1] 1.422886 2.796350
```