



# Today's Class

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- Chomsky Hierarchy and Grammar
- Parsing Approaches for Context-Free Grammar (CFG)
  - Top-down Approach
  - Bottom-up Approach
- Parsing Algorithms
  - Shift-reduce Parsing
  - CYK Parsing

# Syntactic Analysis

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Computer and Natural Languages are very **productive**. They are also highly **regular** in character. Hence, any grammar which is generated to accept all structurally correct strings must account for this productivity and regularity.

- To describe the regularity and productivity of languages, we provide rules of **syntax**
- Our rules of syntax should specify the syntactic structure of a string in our language.

# Syntactic Analysis

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- To provide a syntactic analysis for a string, we must have:
- **A Grammar:** the formal specification of allowable structures.
- **A Parsing Algorithm:** a method of analyzing the sentence to determine its structure.
- **Generative grammars** can be thought of as a set of rules that generate valid phrases in a particular language. Noam Chomsky defined four classes of "complexity" for generative grammars, that are commonly organized into the **Chomsky Hierarchy**.

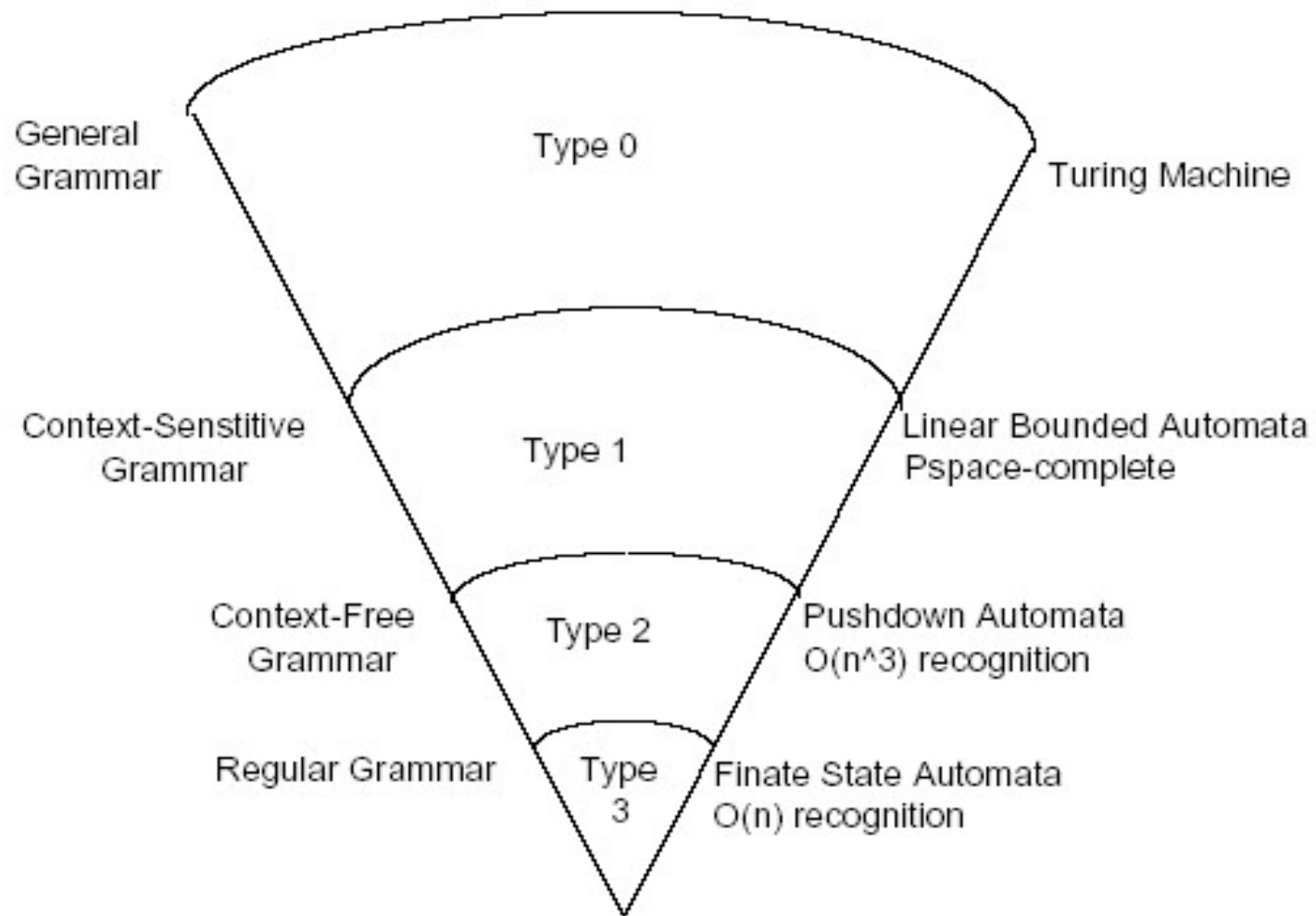
# Generative Grammar

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- A generative grammar  $G$  is expressed as  $G=(V, T, P, S)$ , where:
  - $V$  is a **finite** set of non-terminals or variables (use capital letters to designate them).
  - $T$  is a **finite** set of terminals or tokens (use small letters to designate them).
  - $P$  is a finite set of productions or rules of the form  $\alpha \rightarrow \beta$ .
  - $S$  is a special non-terminal called the start symbol,  $S \in V$ .
- Normally  $V \cap T = \emptyset$ .
- A grammatical symbol is an element of  $V \cup T$ .

# Chomsky Hierarchy

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# Regular Grammar (Type 3)

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- A Regular Grammar is denoted as  $G=(V, T, P, S)$ 
  - $V$  are finite set of non-terminal variables
  - $T$  are finite set of terminal variables
  - $S$  are start symbol
  - $P$  is a finite set of productions. Consist of productions like  $A \rightarrow \beta$
- Left linear grammar for  $ab$ 
  - $B \rightarrow Ab \quad A \rightarrow a$
  - Left hand side: one non-terminal symbol*
  - Right hand side: empty string / a terminal symbol/a non-terminal symbol following a terminal symbol*
- Right linear grammar
  - $A \rightarrow aB \quad B \rightarrow b$

# Context-free Grammars (Type 2)

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- A Context-free Grammar is denoted as  $G=(V, T, P, S)$ 
  - $V$  are finite set of non-terminal variables
  - $T$  are finite set of terminal variables
  - $S$  are start symbol
  - $P$  is a finite set of productions. Consist of productions like  $A \rightarrow \alpha$
  - Only one non-terminal symbol on the left hand side
- Push down Automata



# Example

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- Example Grammar, G:

$V = \{S, VP, NP, \text{Name}, \text{Det}, \text{Noun}, \text{Pro}, \text{Verb}\}$

$T = \{\text{Nyssa}, \text{chases}, \text{cat}, \text{cats}, \text{the}, \text{he}, \text{she}\}$

$S = \{S\}$

$P = \{$   
     $S \rightarrow NP VP$   
     $VP \rightarrow \text{Verb } NP$   
     $NP \rightarrow \text{Name} \mid \text{Det Noun} \mid \text{Pro}$   
     $\text{Name} \rightarrow \text{Nyssa}$   
     $\text{Det} \rightarrow \text{the}$   
     $\text{Noun} \rightarrow \text{cat} \mid \text{cats}$   
     $\text{Pro} \rightarrow \text{he} \mid \text{she}$   
     $\text{Verb} \rightarrow \text{chases}\}$

- 
- To generate phrases in the language of grammar  $G$ , repeatedly apply productions to non-terminals beginning with the start symbol.
  - If we apply  $A \rightarrow \beta$  to the string  $\alpha A \gamma$ , we obtain  $\alpha \beta \gamma$ , obtaining a string in the language generated by  $G$ ,  $L(G)$ .
  - $L(G)$  is the set of strings such that:
    1. Each string consists **solely** of terminals.
    2. Each string is derived from  $S$  by applying the productions in  $P$ . Below is a string of derivations:
$$\alpha_1 \rightarrow \alpha_2 \rightarrow \alpha_3 \rightarrow \dots \rightarrow \alpha_n$$

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- An important aspect of the CFGs is that the derivations involve variables that are independent of what surrounds them; hence, they are context independent.
  - Importance of CFGs:
    1. They are powerful enough to handle much of the productivity of computer and natural languages.
    2. They are restrictive enough to construct efficient parsers,  $O(n^3)$  generally,  $O(n)$  for deterministic grammars (generally true for computer languages).

# Context-Sensitive Grammars (Type 1)

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- A Context-Sensitive Grammar is denoted as  $G=(V, T, P, S)$ 
  - $V$  are finite set of non-terminal variables
  - $T$  are finite set of terminal variables
  - $S$  are start symbol
  - $P$  is a finite set of productions. Consist of productions like  $\alpha \rightarrow \beta$
  - $\alpha$  and  $\beta$  are strings of symbol in  $(VUT)^*$  and  $\beta$  is at least as long as  $\alpha$
  - NO productions of  $AB \rightarrow C$  or  $AB \rightarrow \text{empty}$
  - $\alpha_1 A \alpha_2 \rightarrow \alpha_1 \beta \alpha_2$  where  $\beta$  can't be empty "A becomes  $\beta$  in the context of  $\alpha_1$  and  $\alpha_2$ "

# General Grammar (Type 0)

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- A General Grammar is denoted as  $G=(V, T, P, S)$ 
  - $V$  are finite set of non-terminal variables
  - $T$  are finite set of terminal variables
  - $S$  are start symbol
  - $P$  is a finite set of productions WITHOUT RESTRICTIONS
- Type 0 grammar are recursively enumerable and are accepted by a Turing Machine.
- Too complex a specification for computer languages.

# Parsing

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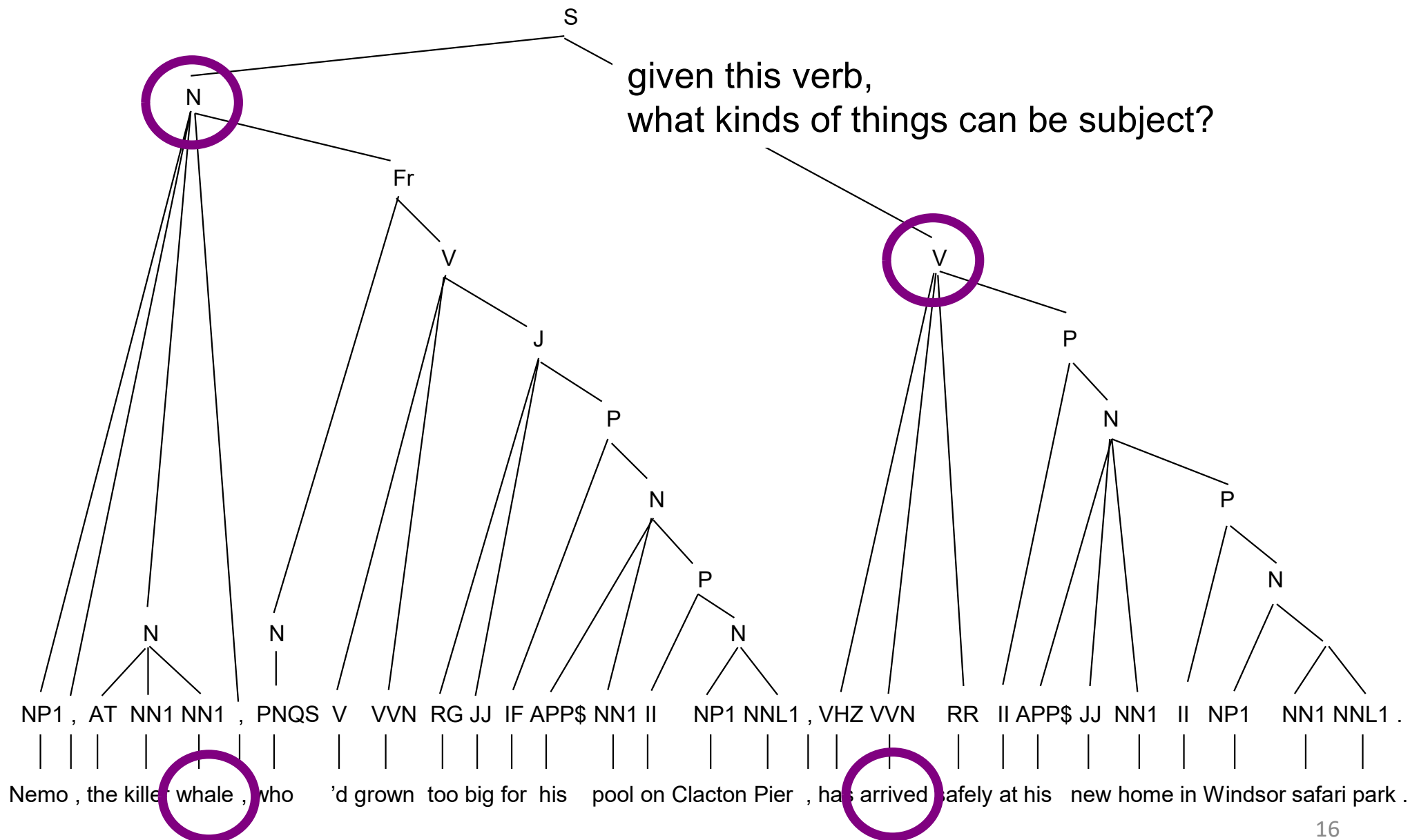
- Parsing is the process of determining whether a string is in a grammar  $G$ .
- Without context, ambiguities occurs in natural language frequently. With more contextual information, most ambiguities can be removed
- The core of parsing natural language is to resolve the ambiguities in the syntactic structures.
- The goal of sentence processing is to understand the representations people form as they understand a sentence (syntax, meaning...).

# Parsing

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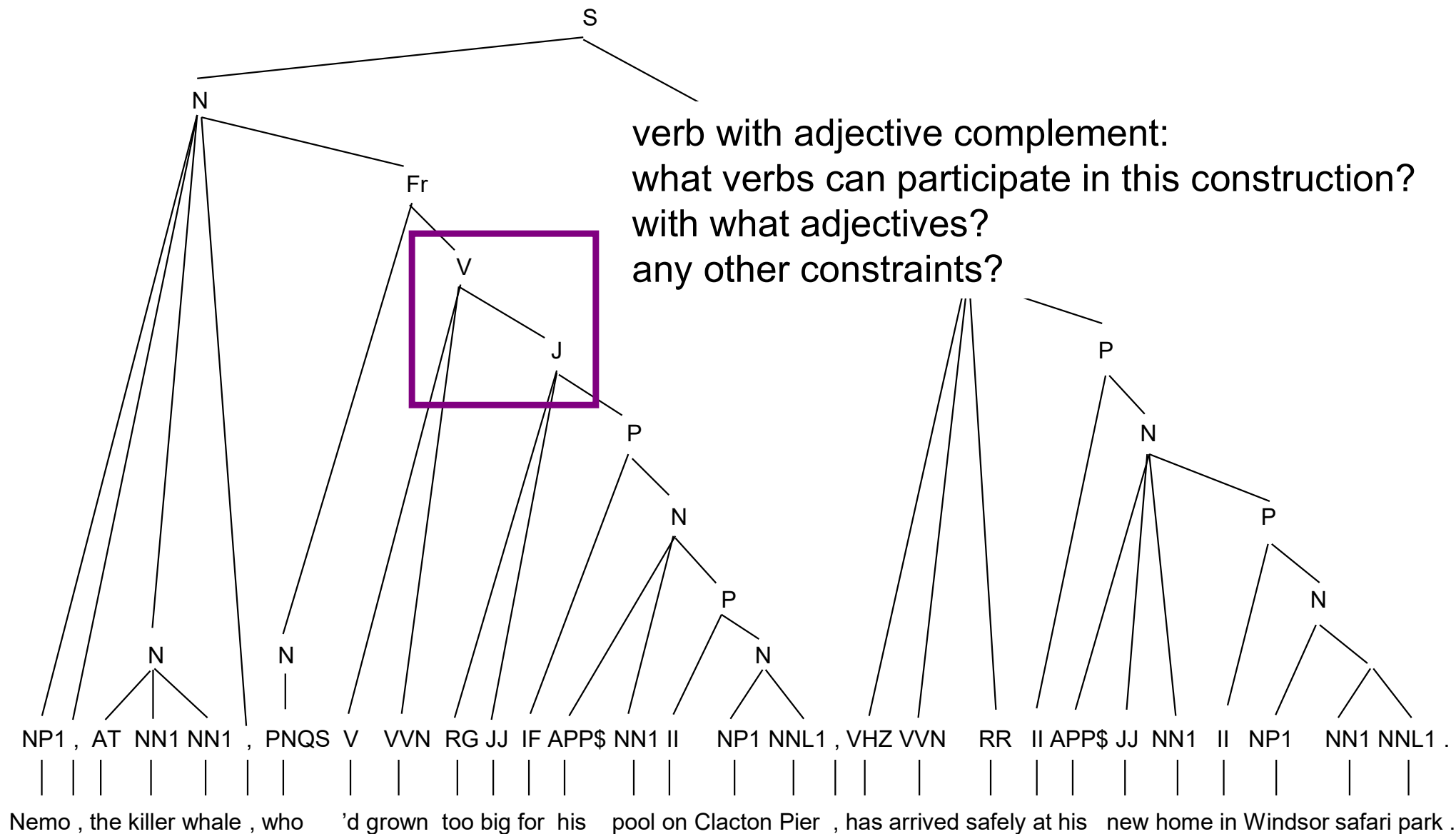
- Parsing adds information about sentence structure and constituents
- Allows us to see what constructions words enter into
  - eg, transitivity, passivization, argument structure for verbs
- Allows us to see how words function relative to each other
  - eg, what words can modify / be modified by other words

[S[N Nemo\_NP1 ,\_, [N the\_AT killer\_NN1 whale\_NN1 N] ,\_, [Fr[N who\_PNQS N][V 'd\_VHD grown\_VVN [J too\_RG big\_JJ [P for\_IF [N his\_APP\$ pool\_NN1 [P on\_II [N Clacton\_NP1 Pier\_NNL1 N]P]N]P]J]V]Fr[N] ,\_, [V has\_VHZ arrived\_VVN safely\_RR [P at\_II [N his\_APP\$ new\_JJ home\_NN1 [P in\_II [N Windsor\_NP1 [ safari\_NN1 park\_NNL1 ]N]P]N]P]V] .\_. S]

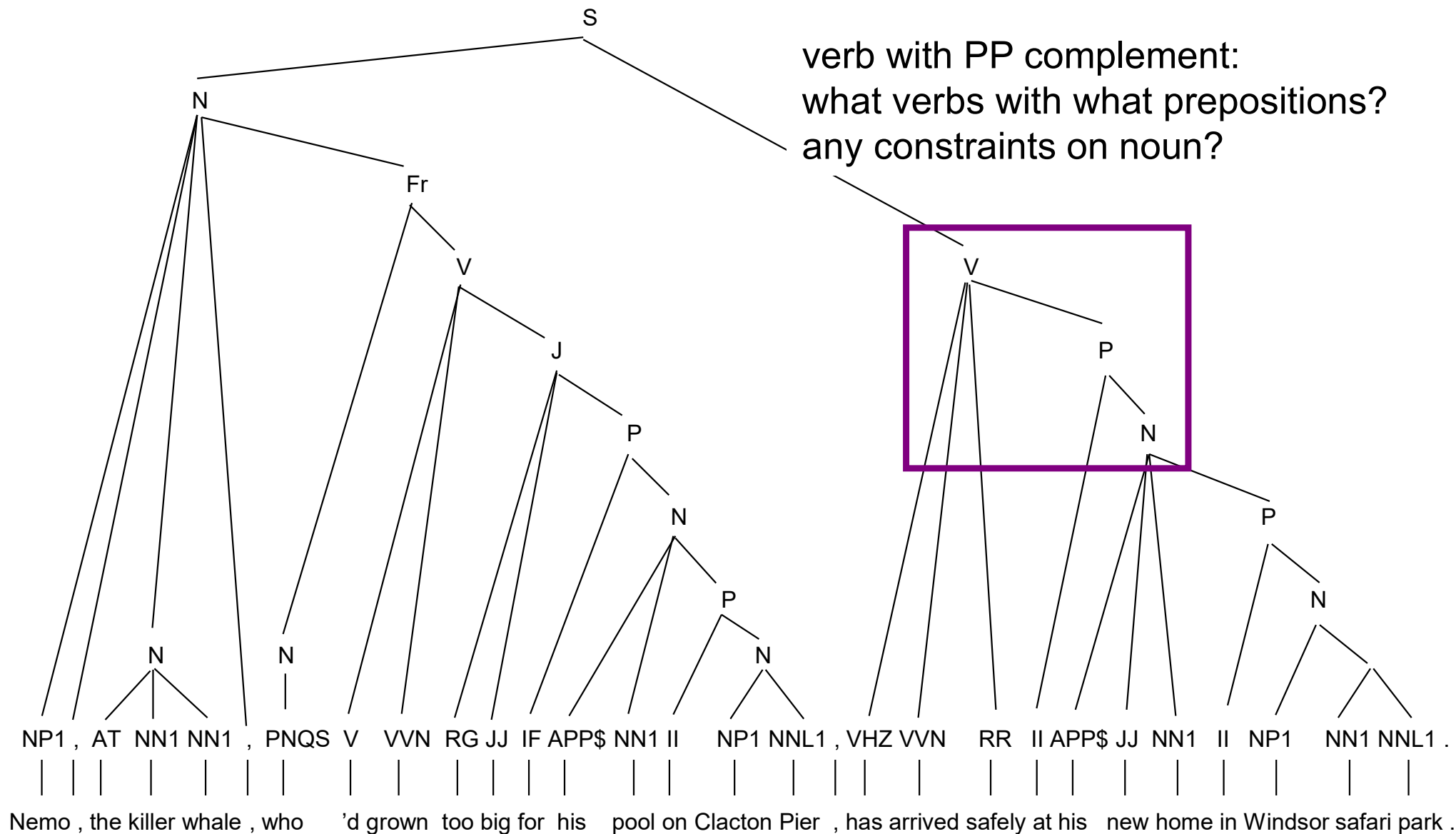




[S[N Nemo\_NP1 ,\_, [N the\_AT killer\_NN1 whale\_NN1 N] ,\_, [Fr[N who\_PNQS N][V 'd\_VHD grown\_VVN [J too\_RG big\_JJ [P for\_IF [N his\_APP\$ pool\_NN1 [P on\_II [N Clacton\_NP1 Pier\_NNL1 N]P]N]P]J]V]Fr[N] ,\_, [V has\_VHZ arrived\_VVN safely\_RR [P at\_II [N his\_APP\$ new\_JJ home\_NN1 [P in\_II [N Windsor\_NP1 [ safari\_NN1 park\_NNL1 ]N]P]N]P]V] .\_. S]



[S[N Nemo\_NP1 ,\_, [N the\_AT killer\_NN1 whale\_NN1 N] ,\_, [Fr[N who\_PNQS N][V 'd\_VHD grown\_VVN [J too\_RG big\_JJ [P for\_IF [N his\_APP\$ pool\_NN1 [P on\_II [N Clacton\_NP1 Pier\_NNL1 N]P]N]P]J]V]Fr[N] ,\_, [V has\_VHZ arrived\_VVN safely\_RR [P at\_II [N his\_APP\$ new\_JJ home\_NN1 [P in\_II [N Windsor\_NP1 [ safari\_NN1 park\_NNL1 ]N]P]N]P]V] .\_. S]



# Parsing: difficulties

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- Besides lexical ambiguities (usually resolved by tagger), language can be structurally ambiguous
  - global ambiguities due to ambiguous words and/or alternative possible combinations
  - local ambiguities, especially due to attachment ambiguities, and other combinatorial possibilities
  - sheer weight of alternatives available in the absence of (much) knowledge

# Parsing: difficulties

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- Broad coverage necessary for parsing corpora of real text
- Long sentences:
  - structures are very complex
  - ambiguities proliferate
- Difficulty (even for human) to verify if parse is correct
  - because it is complex
  - because it may be genuinely ambiguous

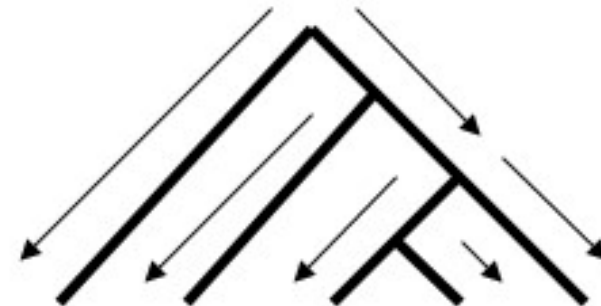
# Parsing

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- Parsing Approaches
  - Top down parsers
  - Bottom up parsers
  - Left corner parsers

# Top-down Parsing

- Begin with the start symbol  $S$  and produce the right hand side (RHS) of the rule
- Match the left-hand side (LHS) of CFG rules to the non-terminals in the string, replacing them with the right-hand side of the rule.
- Continue until all the non-terminals are replaced by terminals, such that they correspond to the symbols in the sentence.
- The parse succeeds when all words in the sentence are generated.

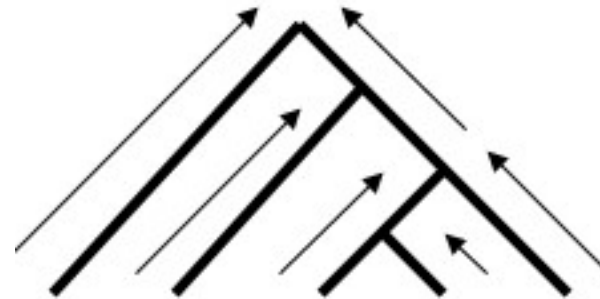


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- This is a left-most derivation for the sentence; each production is applied to the left-most non-terminals
  - Based on Prediction
    - Produce the prediction for following component, then verify the prediction by matching words
    - If the prediction is verified, the target string will be parsed according to the prediction
    - If not verified, use other predictions (backtracking)
    - If all predictions are rejected, the sentence is not valid  
→ parser fails

# Bottom-up Parsing

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- Begin with Words.
- Apply the right-hand side RHS of the rules to the words to generate non-terminals from the LHS.
- The parse succeeds when the start non-terminal is generated.



- Based on Reduction
  - Match the words in the sentence
  - Generate possible non-terminal symbols iteratively
  - If S is generated, Parse succeeds
  - If S is not generated , use other symbols (backtracking)



# Rule Set

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Rule	Dictionary
(7) $NP \rightarrow R$	(1) $R \rightarrow$ 我
(8) $NP \rightarrow N$	(2) $N \rightarrow$ 县长
(9) $NP \rightarrow S\phi\ de$	(3) $V \rightarrow$ 是
(10) $VP\phi \rightarrow V\ V$	(4) $V \rightarrow$ 派
(11) $VP \rightarrow V\ NP$	(5) $V \rightarrow$ 来
(12) $S\phi \rightarrow NP\ VP\phi$	(6) $de \rightarrow$ 的
(13) $S \rightarrow NP\ VP$	

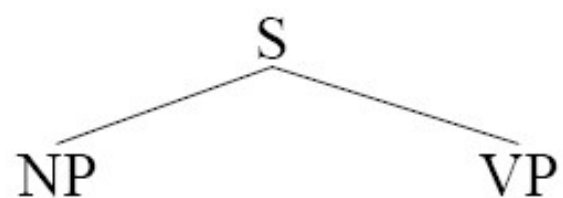
# Top-Down Parsing Illustration -1

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R	V	N	V	V	de
我	是	县长	派	来	的

2

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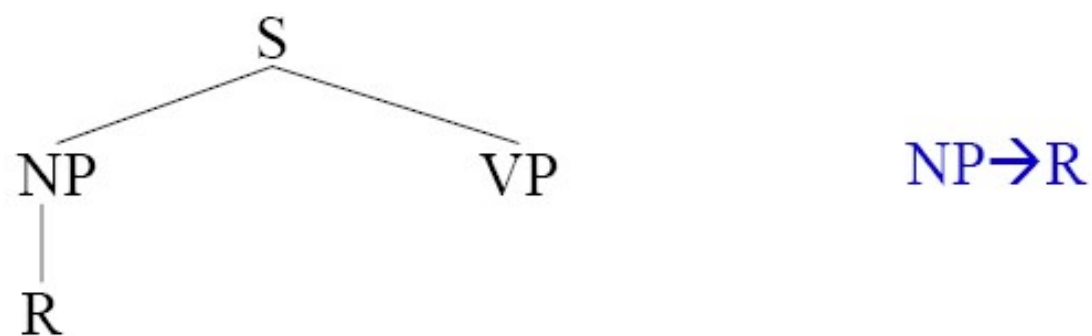


$S \rightarrow NP VP$

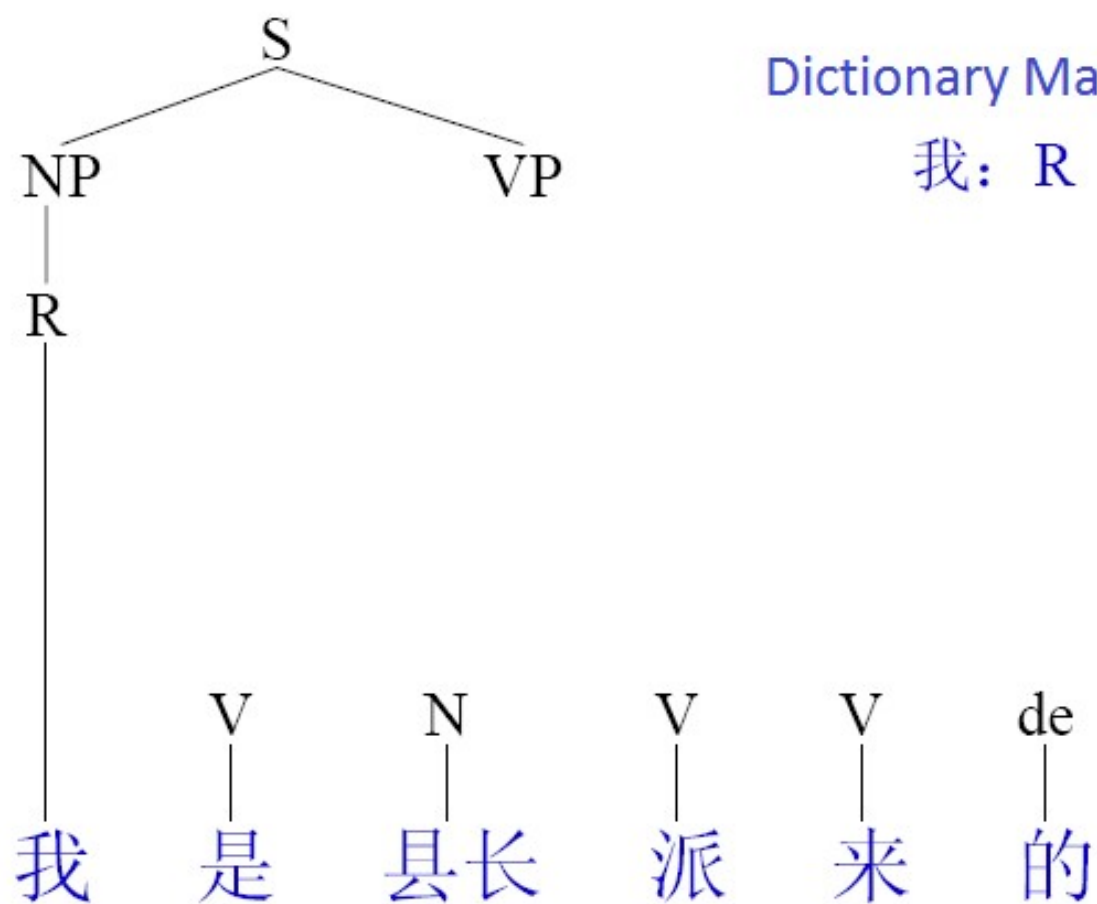
R	V	N	V	V	de
我	是	县长	派	来	的

# 3

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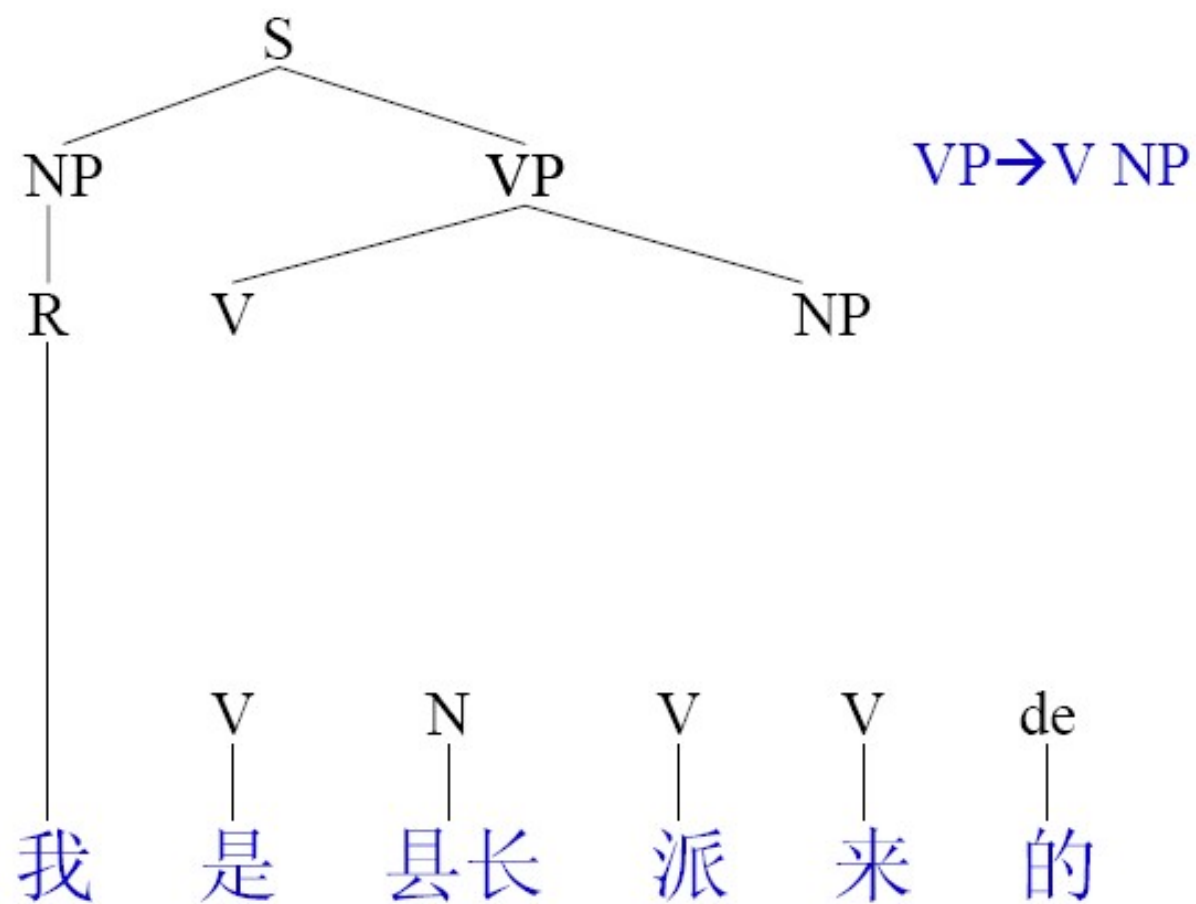


R	V	N	V	V	de
我	是	县长	派	来	的



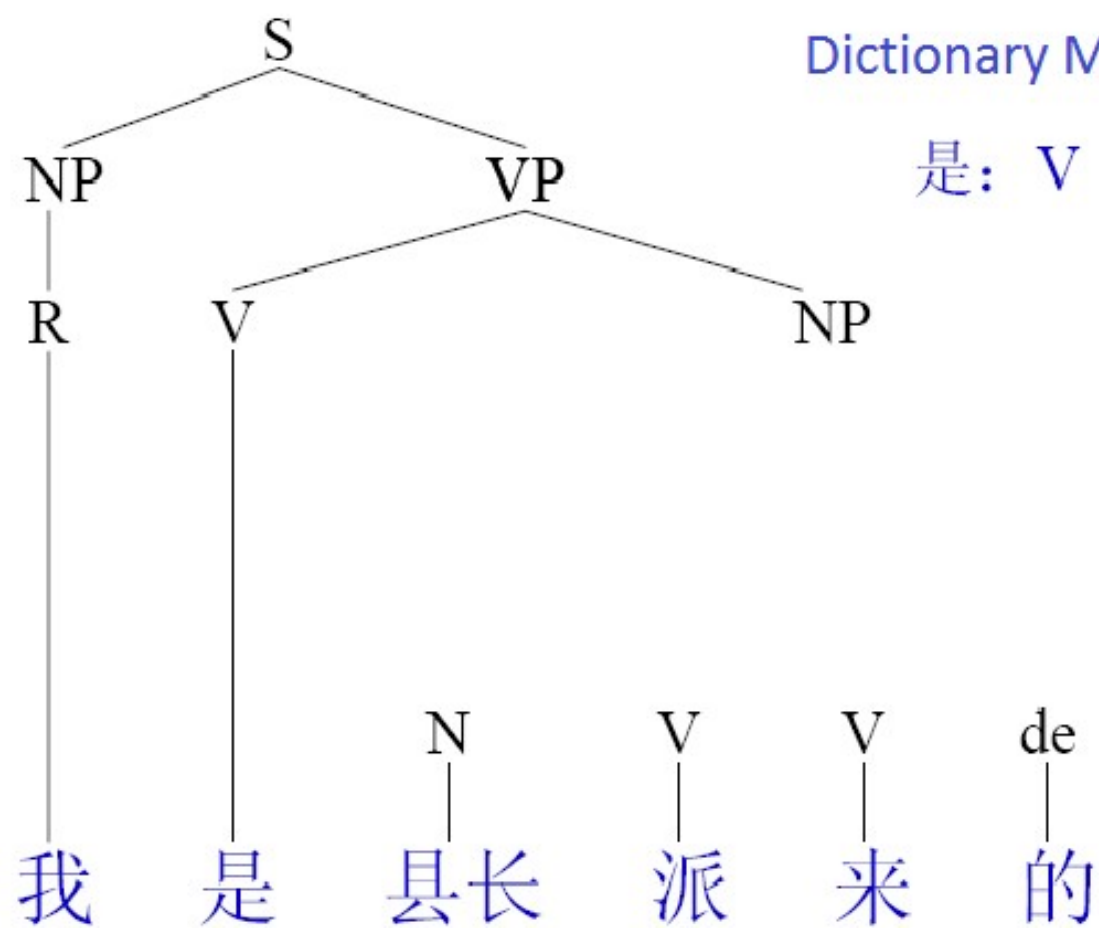
# 5

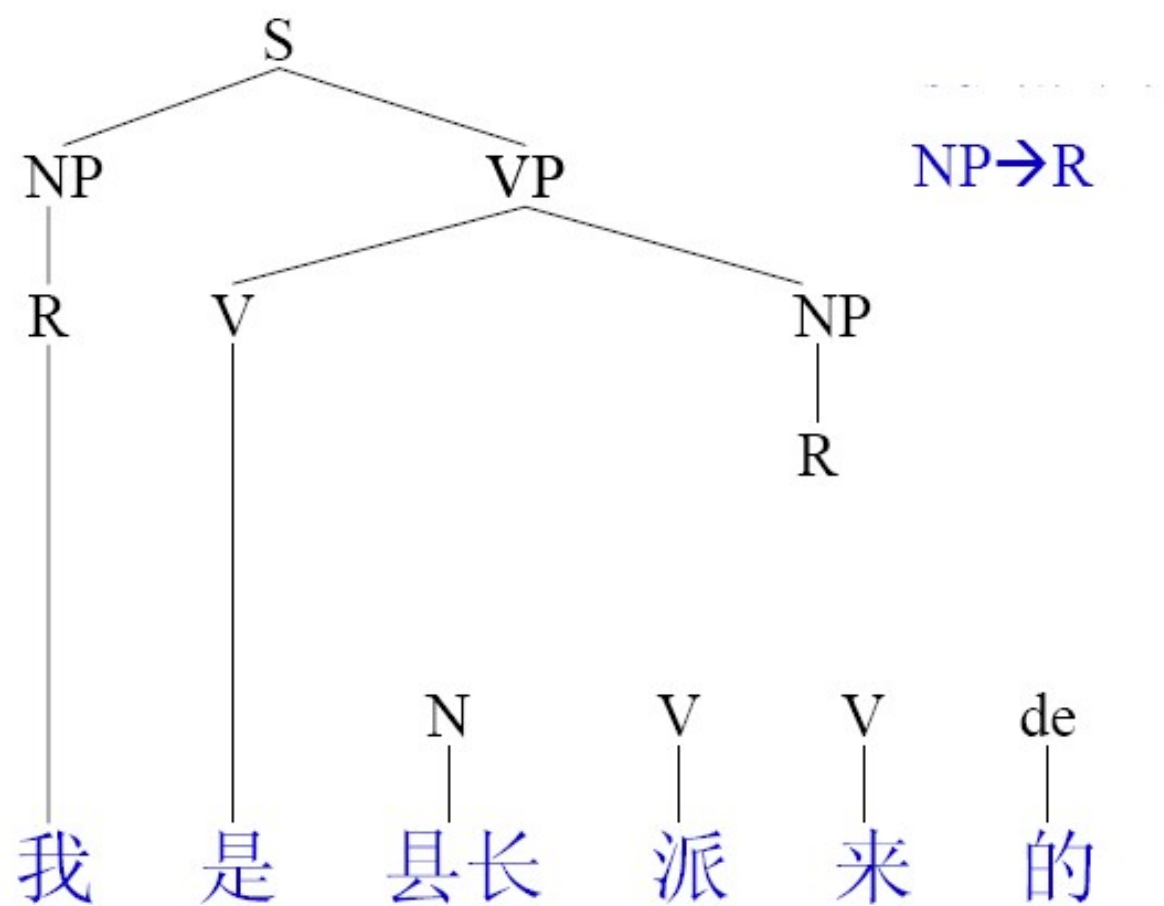
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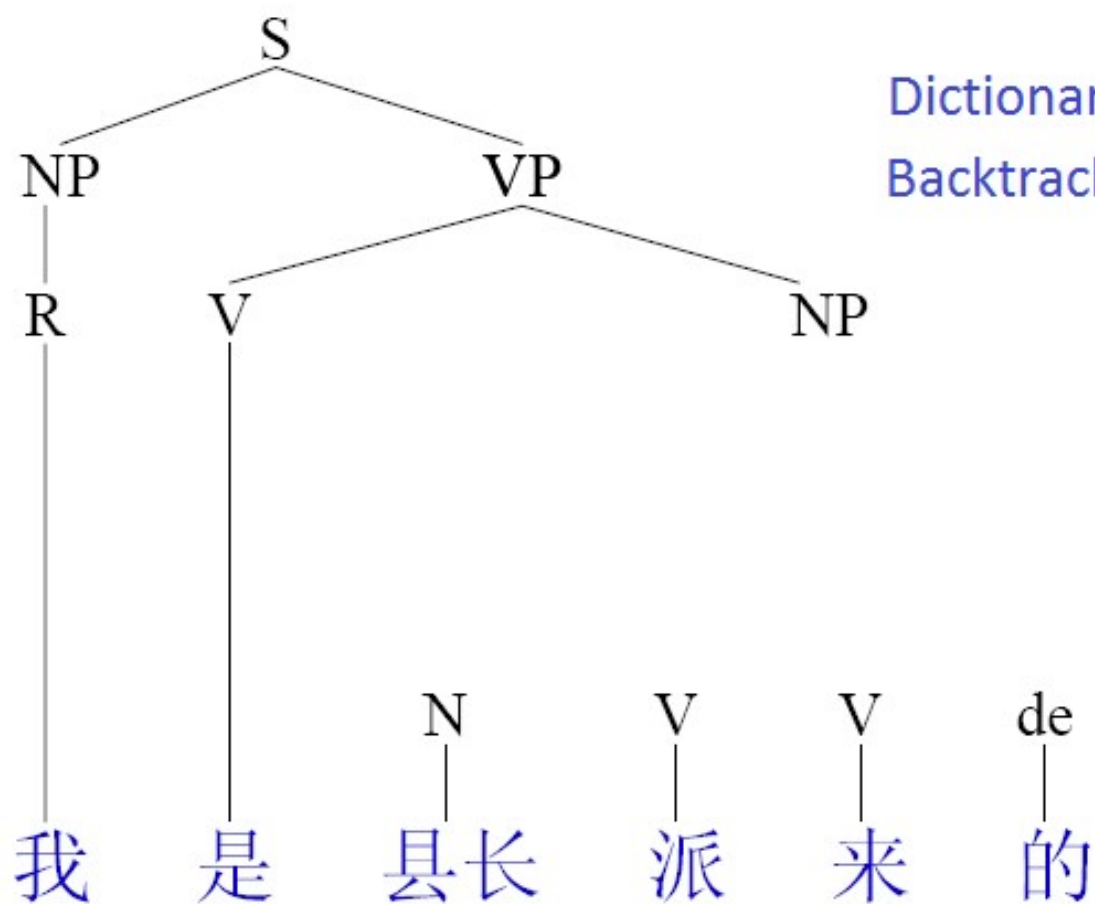
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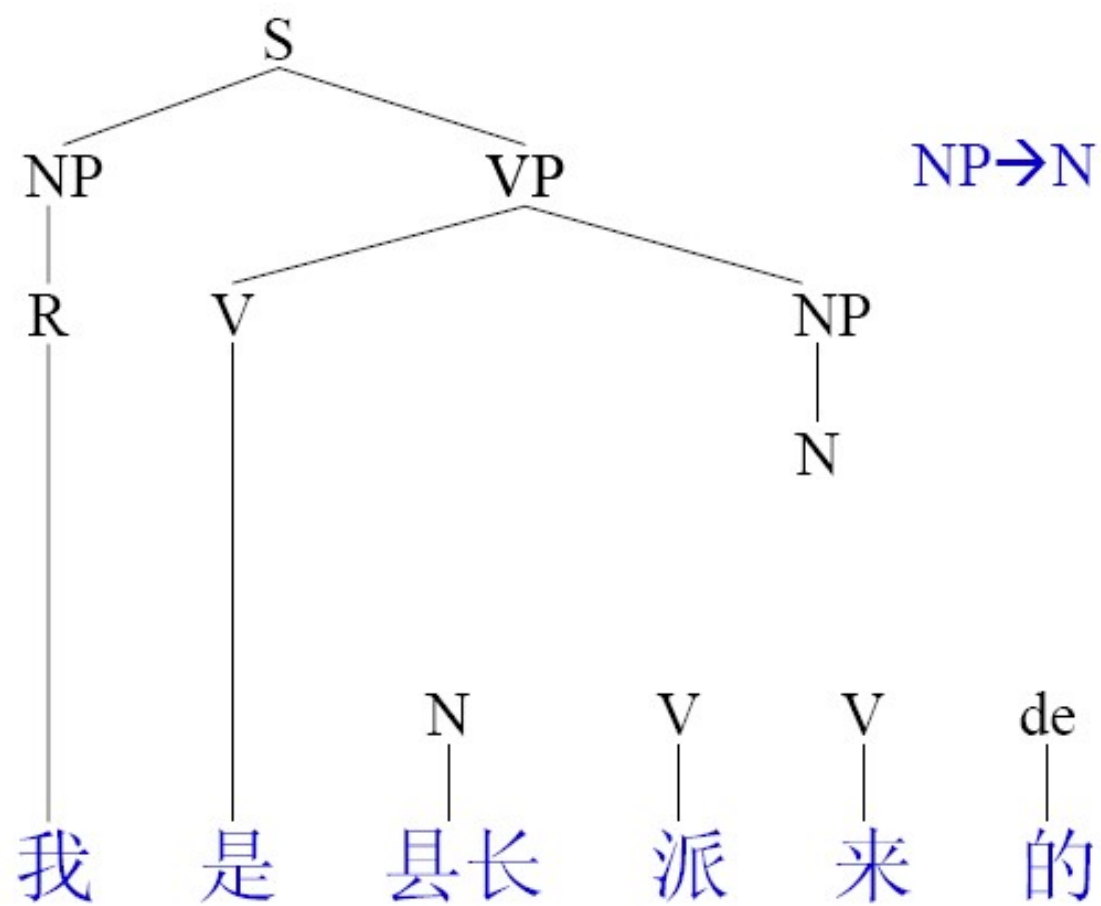






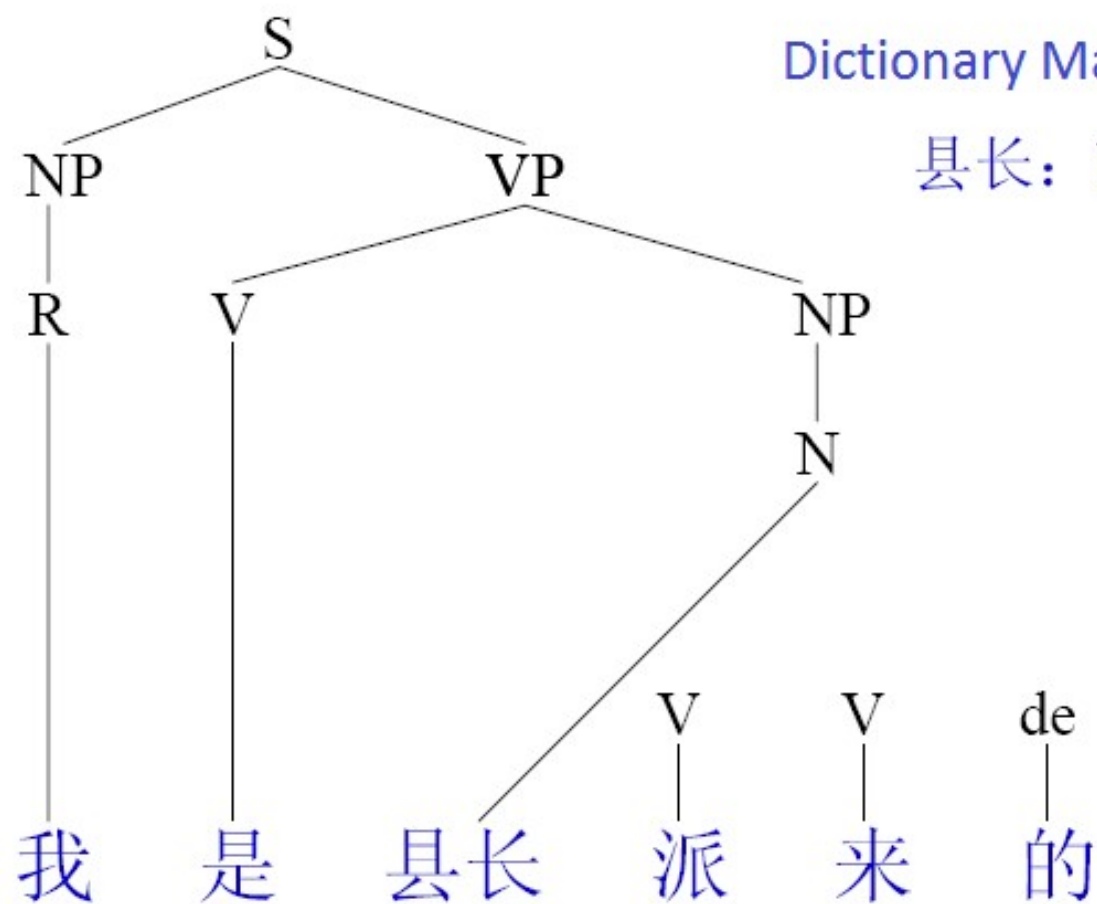


Dictionary Match Fails  
Backtracking



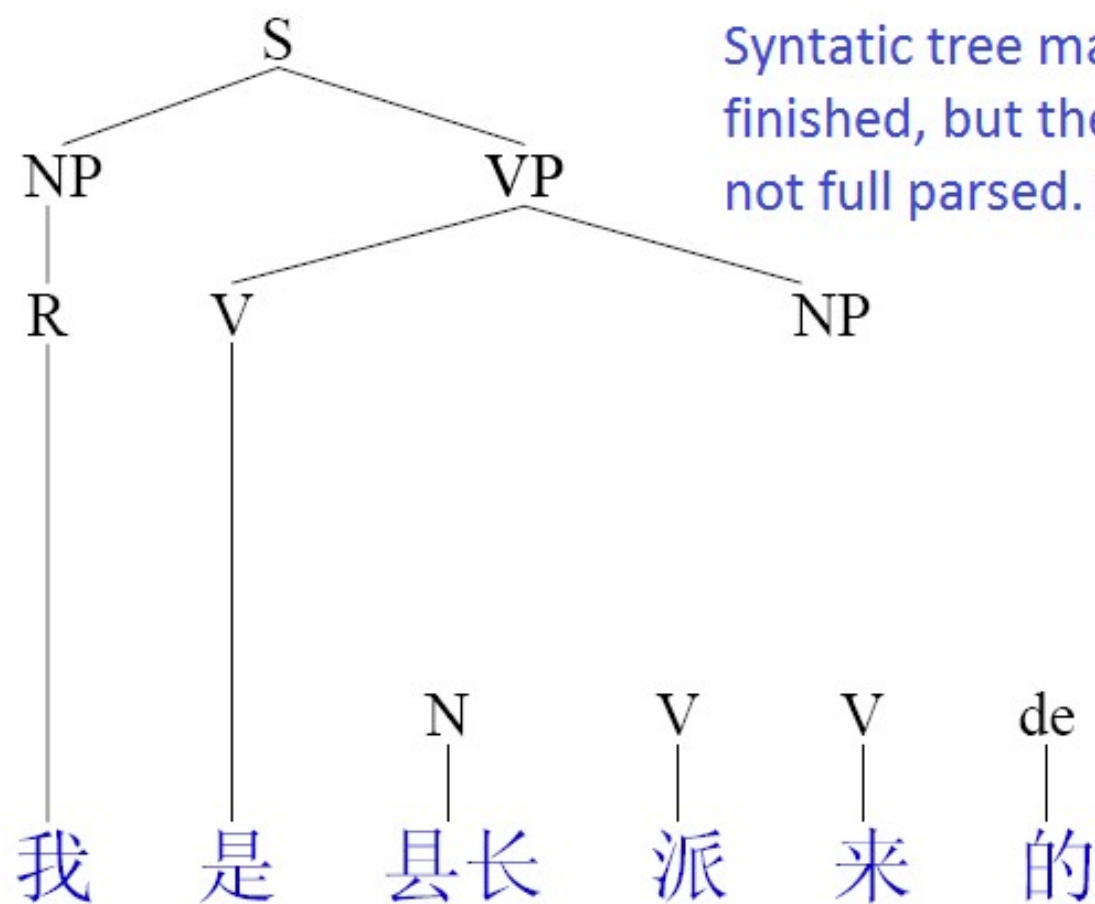
# 10

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Dictionary Match Succeeds

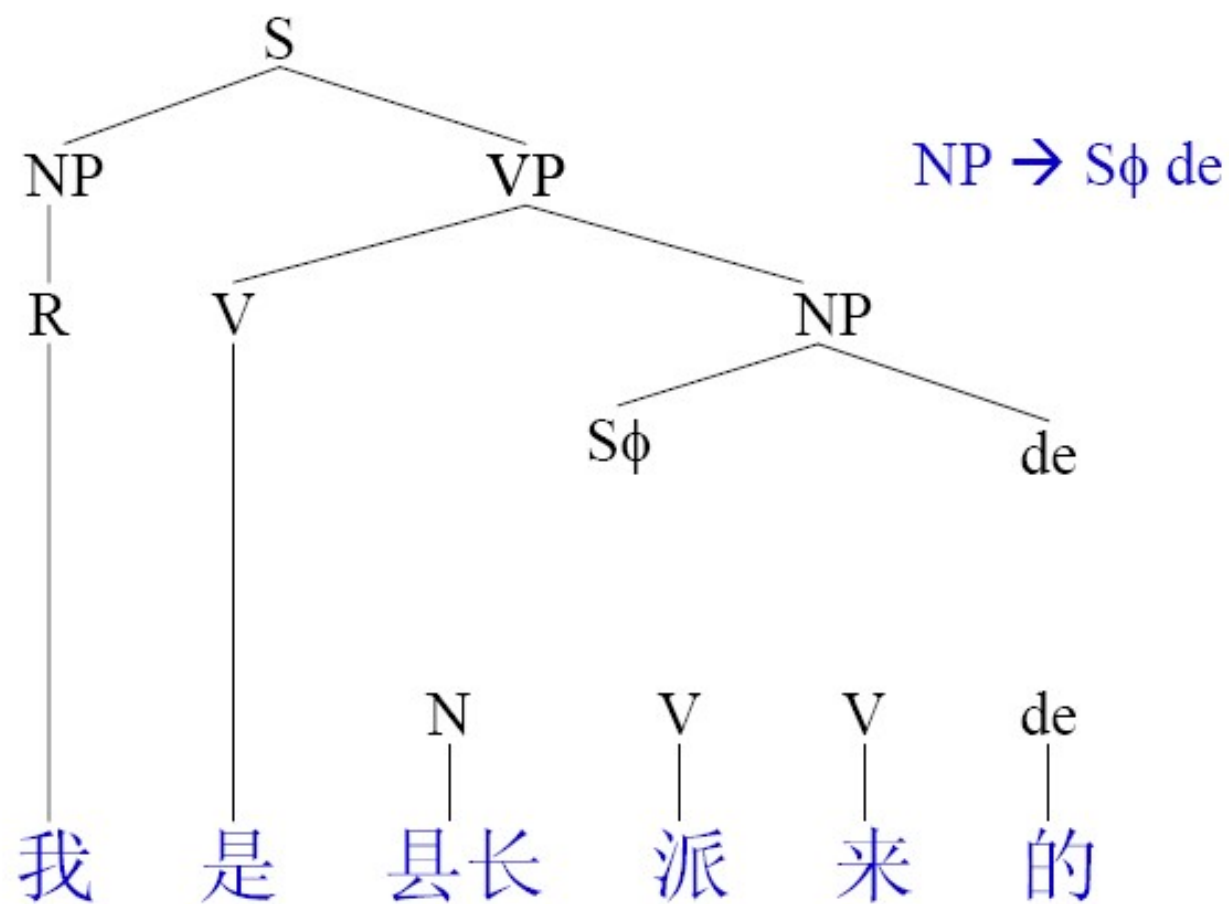
县长: N

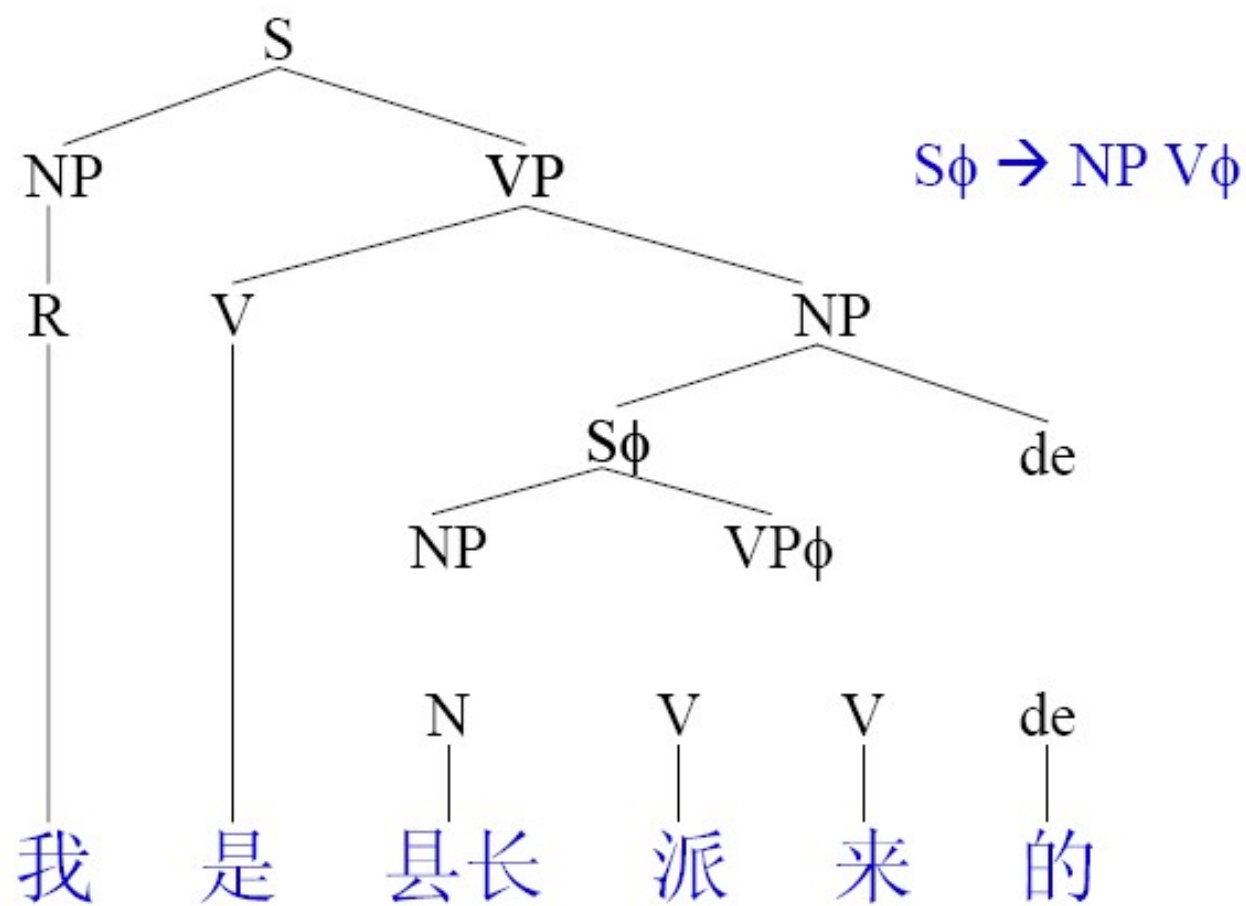


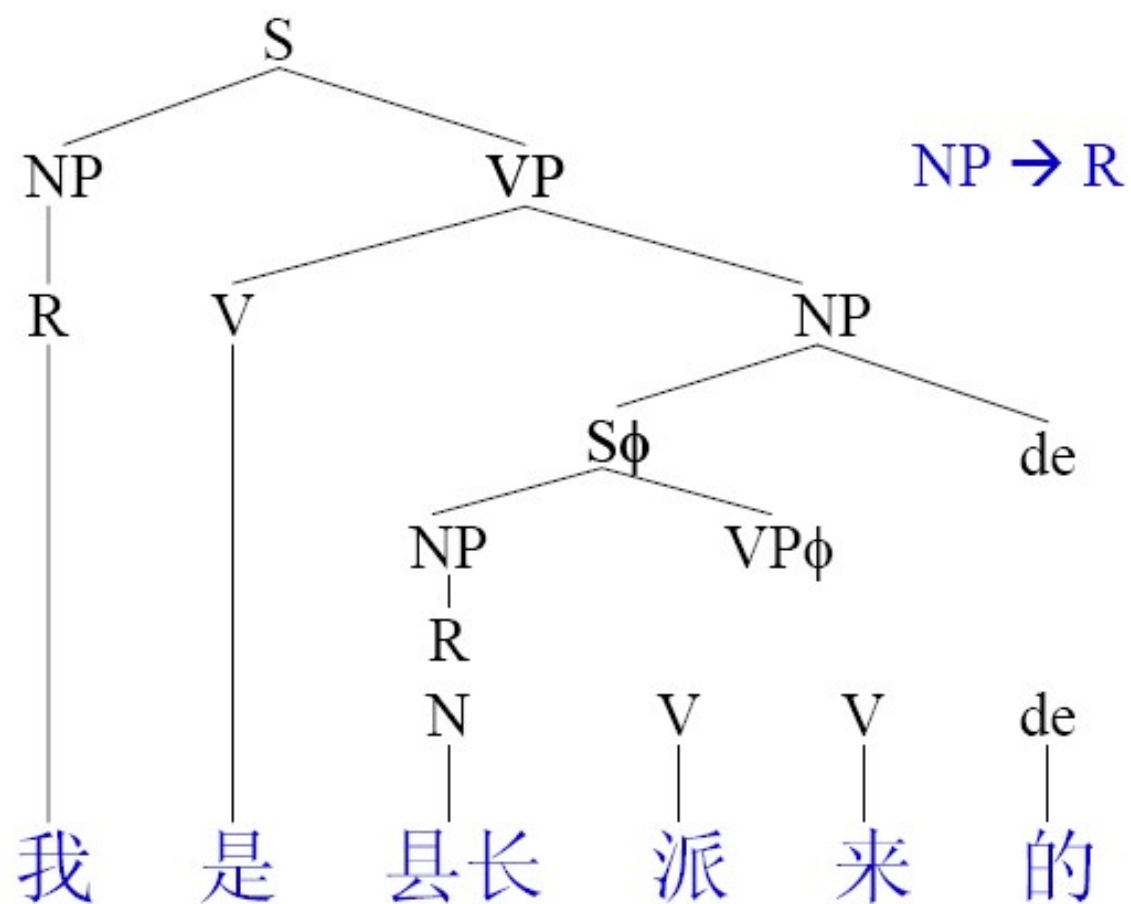
Syntactic tree matching  
finished, but the sentence is  
not full parsed. Backtracking

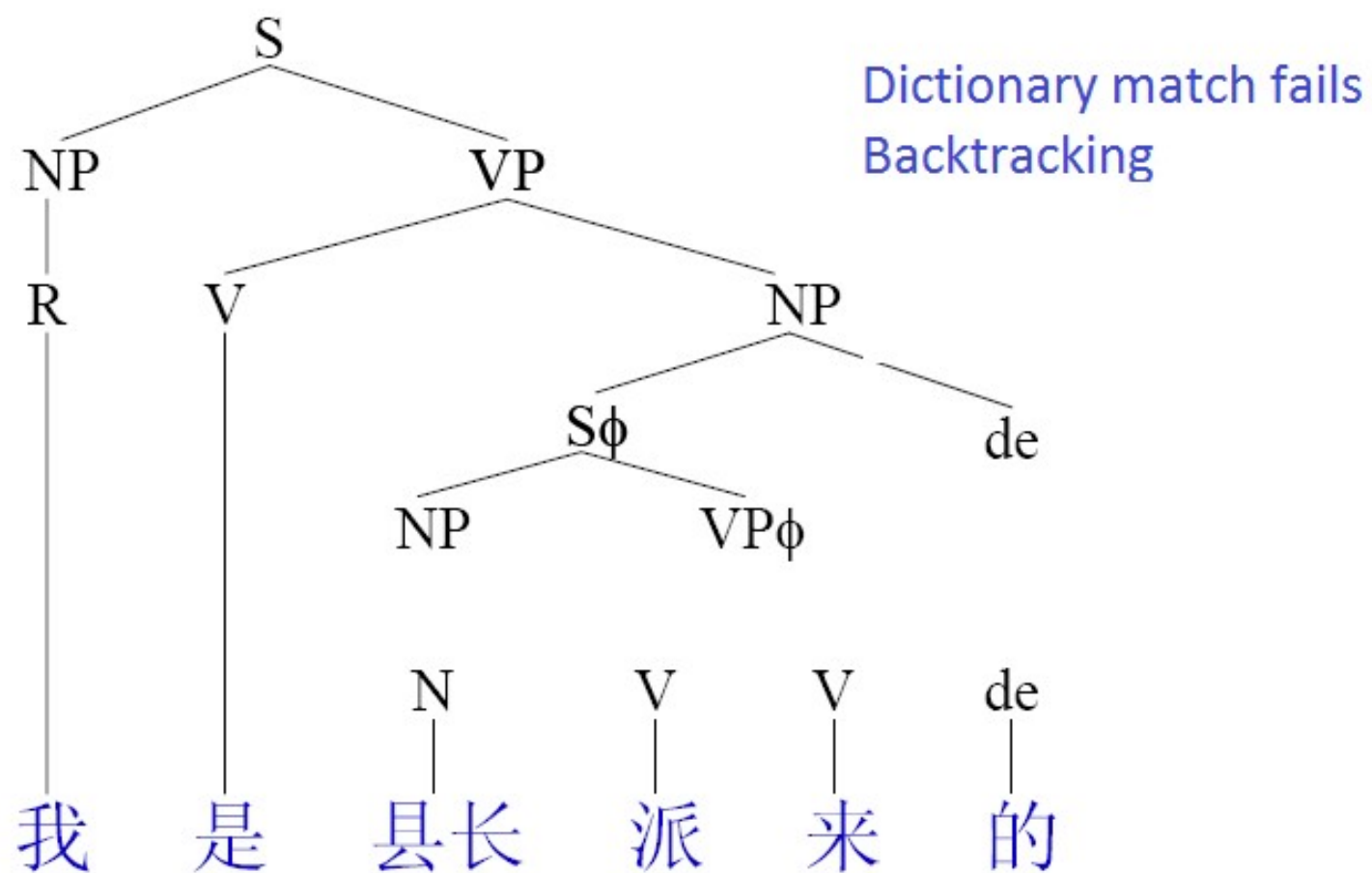
# 12

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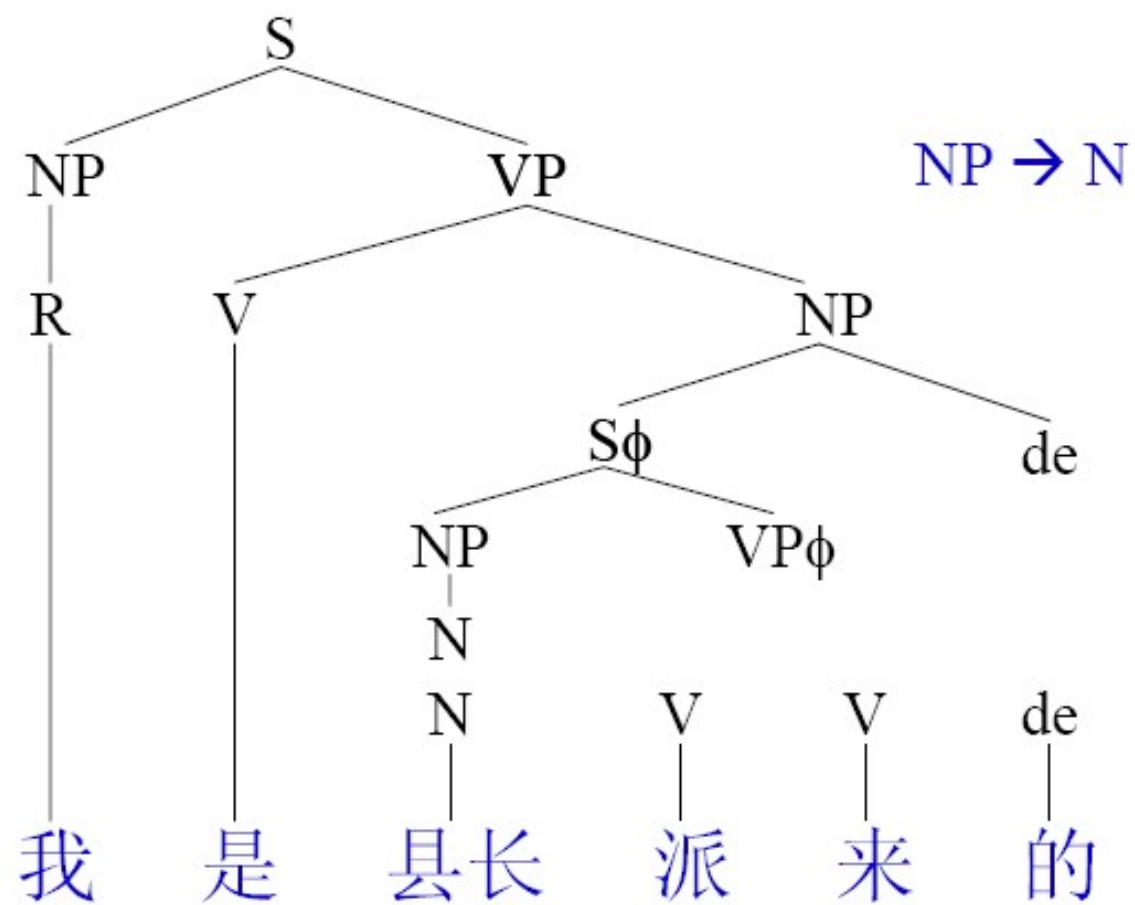


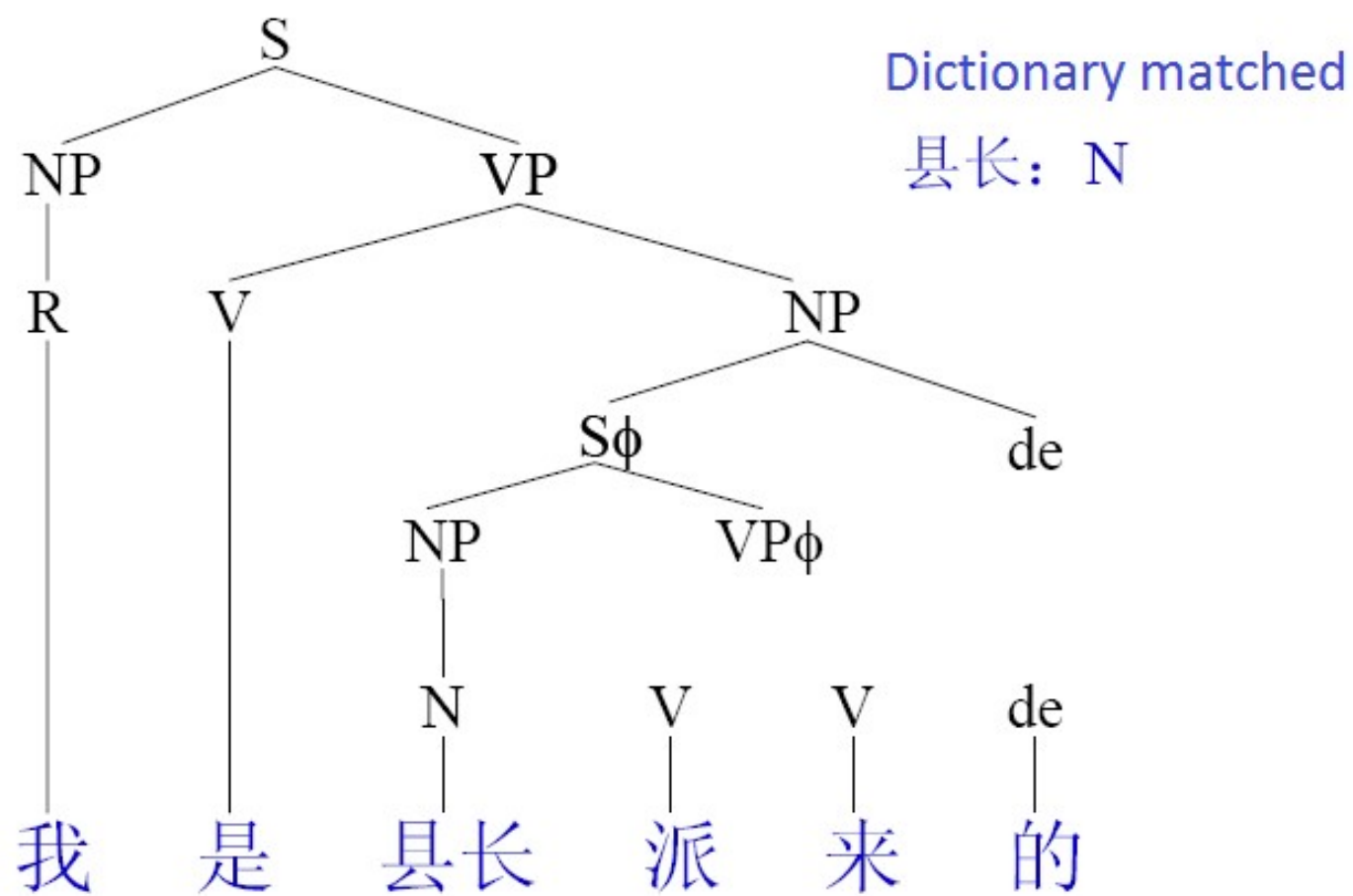


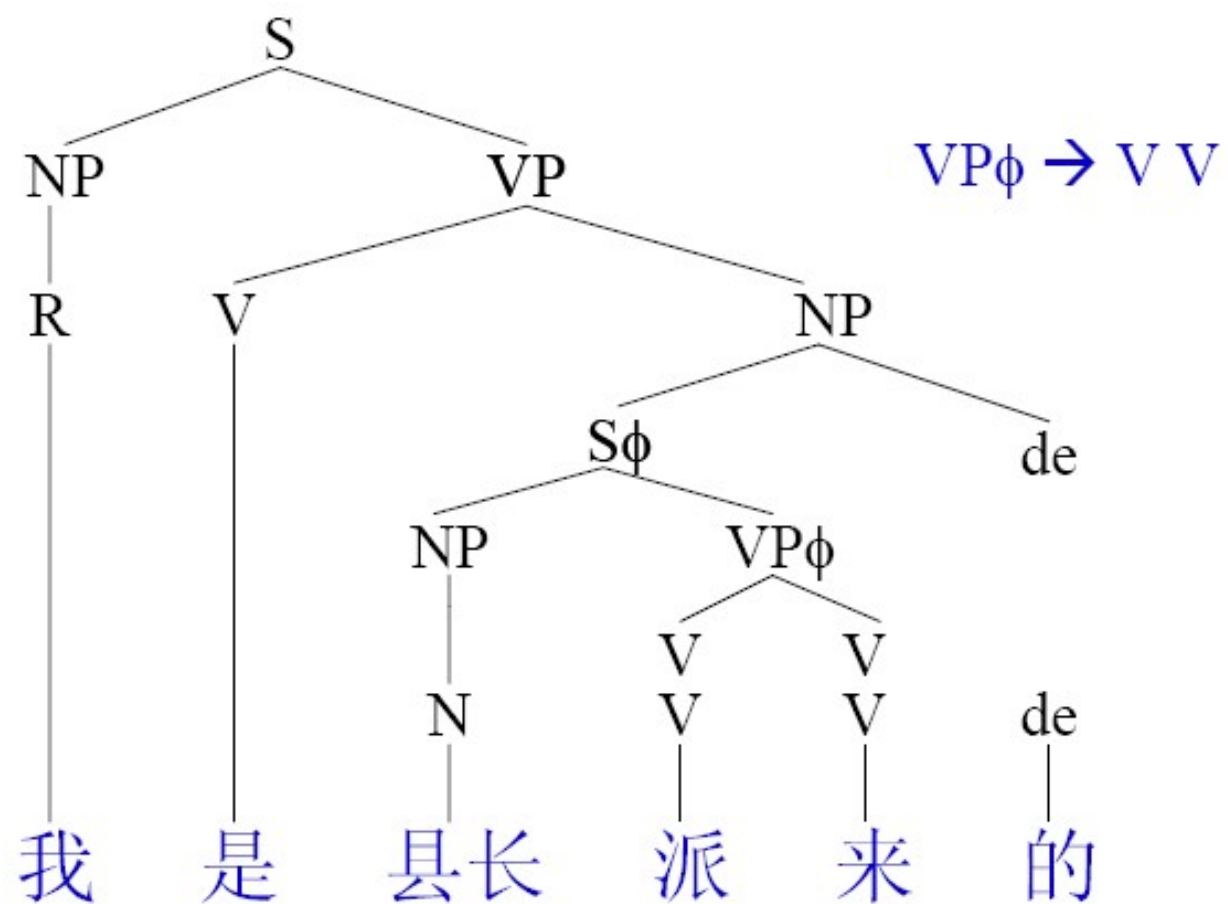


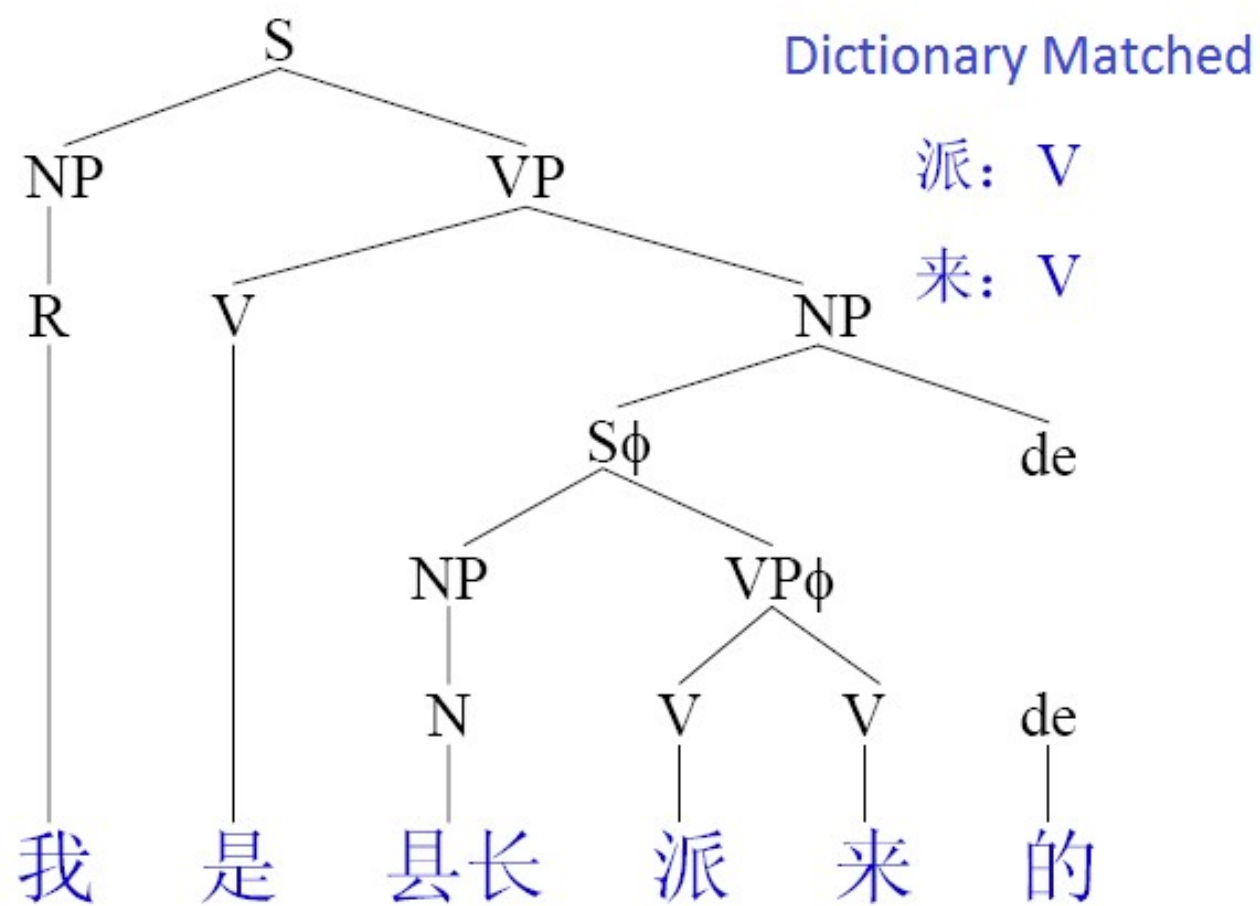


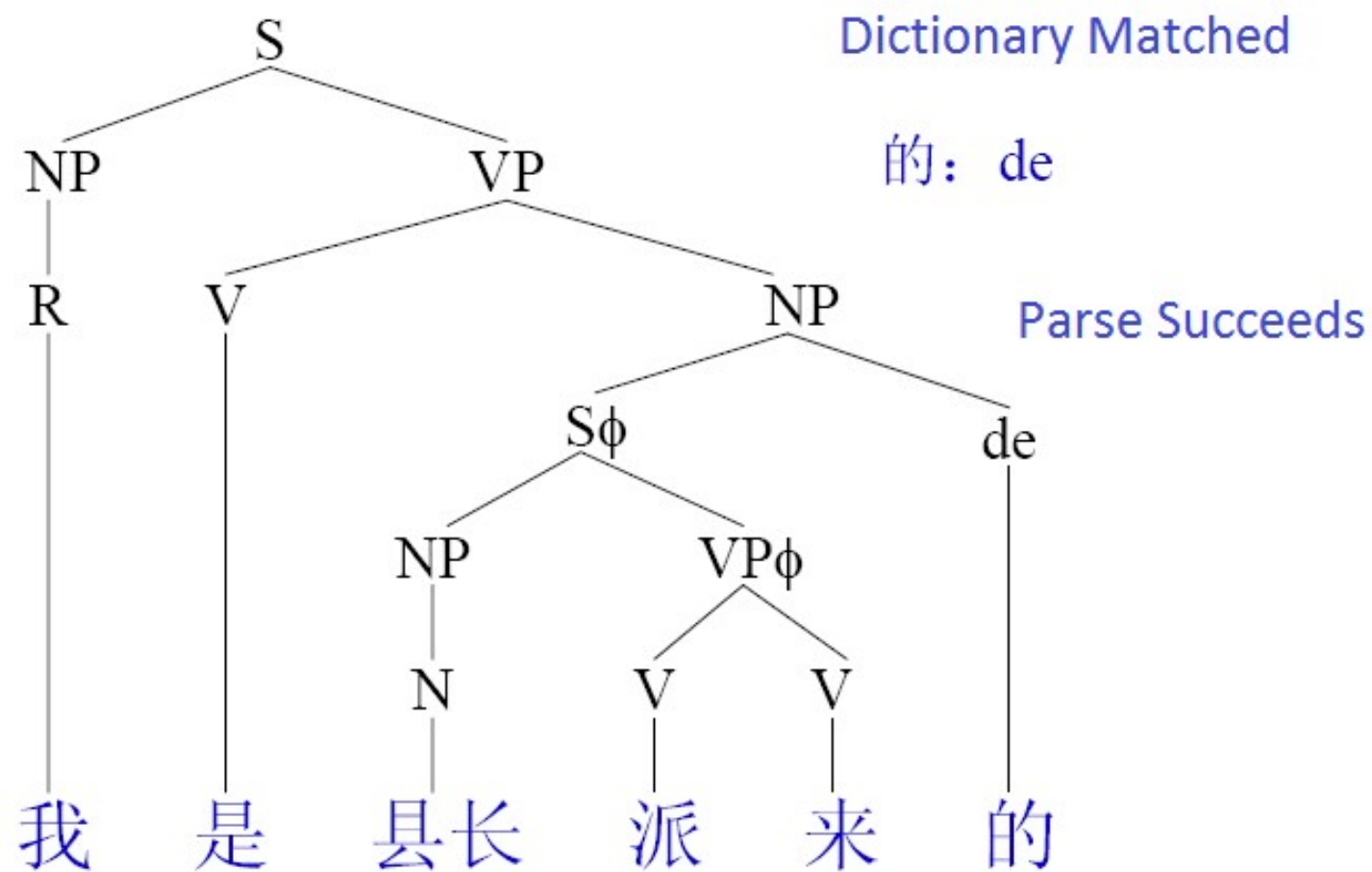












# Bottom-Up Parsing Illustration -1

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R	V	N	V	V	de
我	是	县长	派	来	的

# 2

---

NP→R

NP					
R	V	N	V	V	de
我	是	县长	派	来	的

# 3

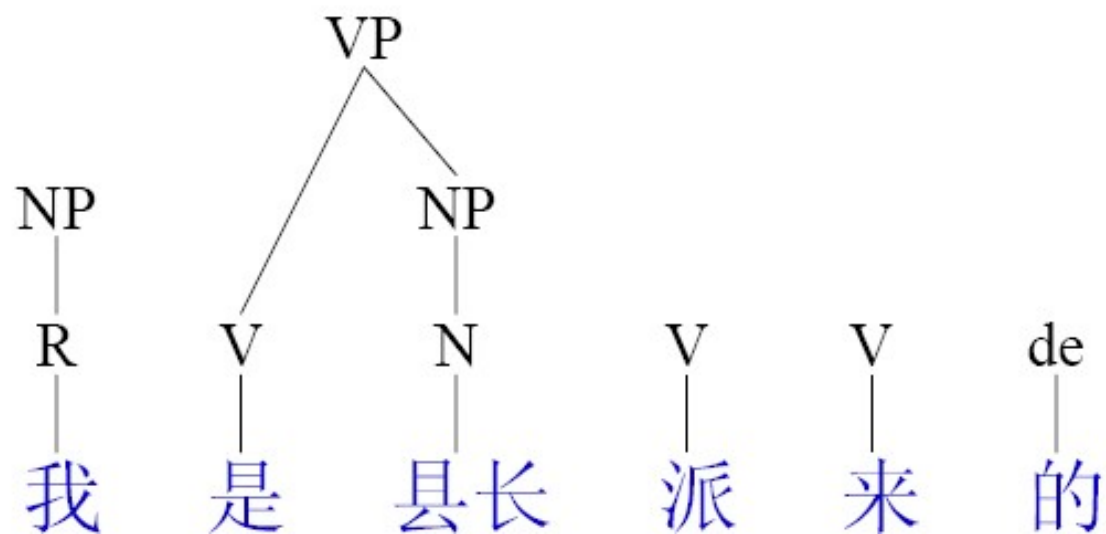
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NP→N

NP		NP			
R	V	N	V	V	de
我	是	县长	派	来	的

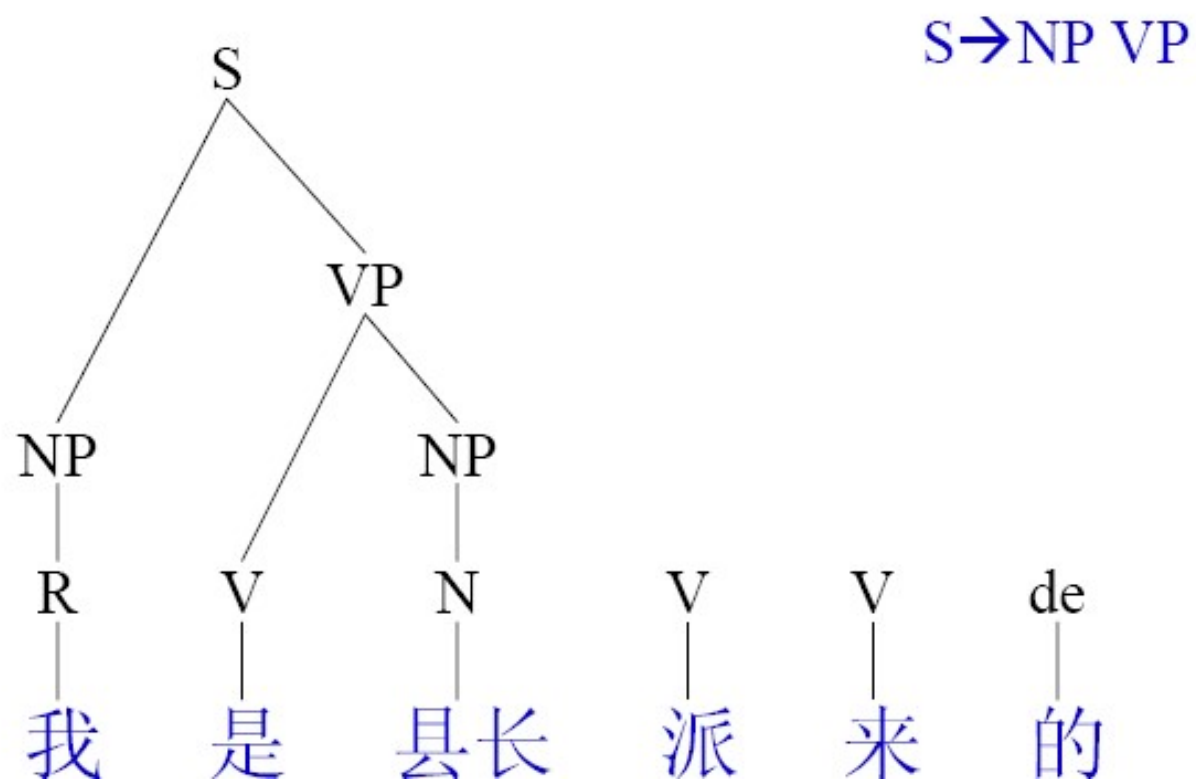


VP → V NP



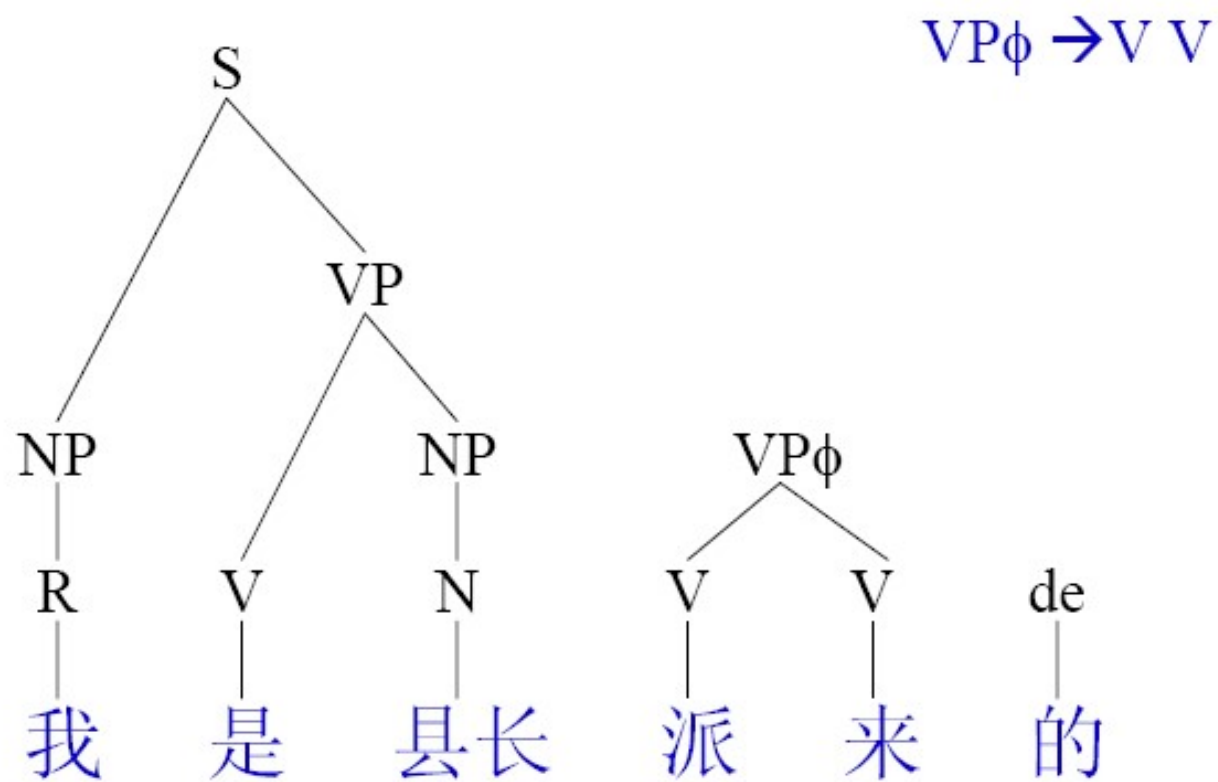
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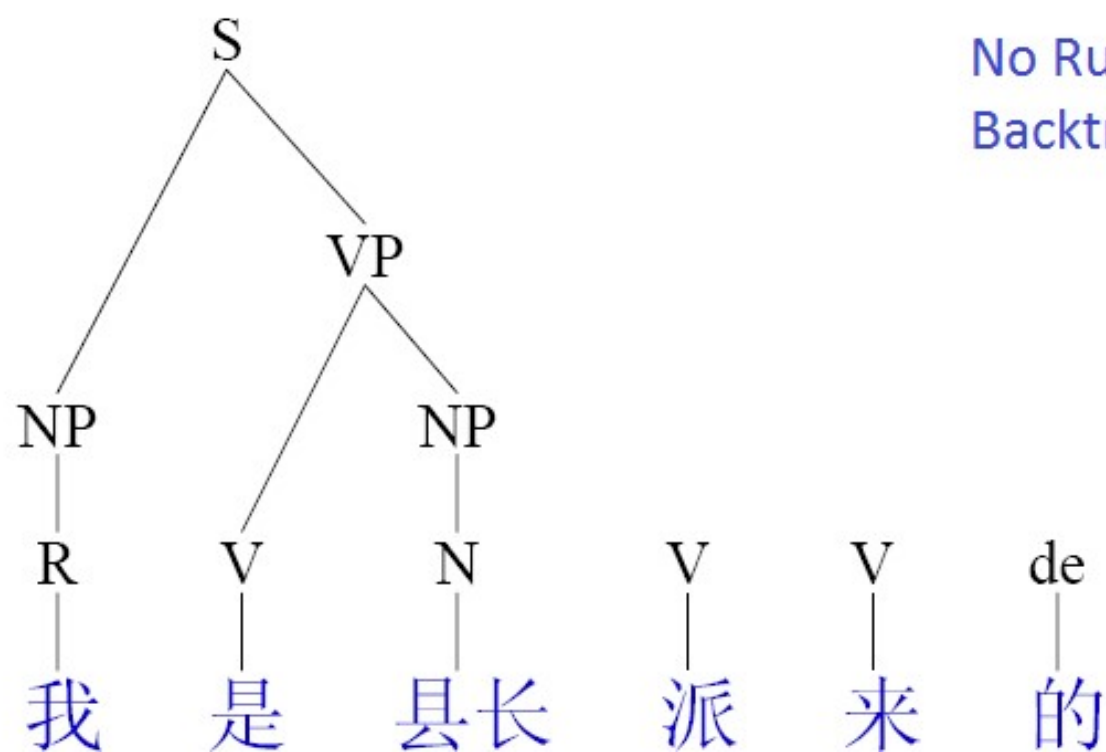
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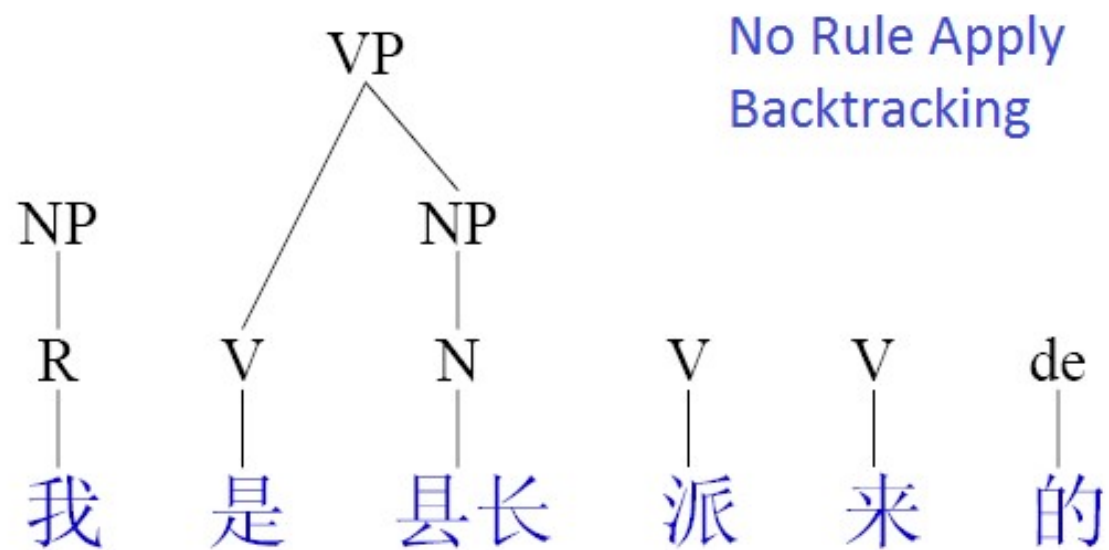


# 6

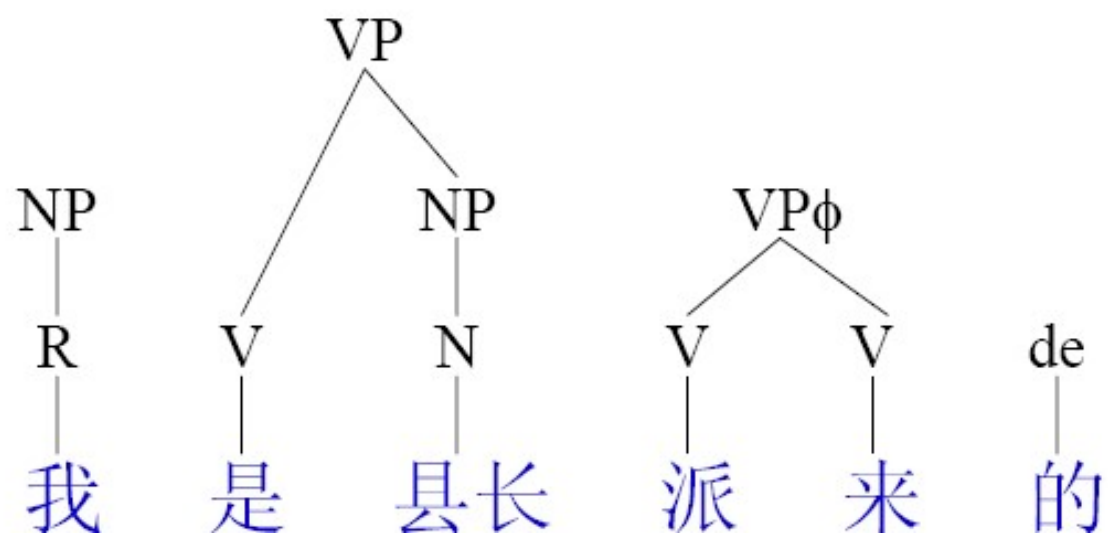
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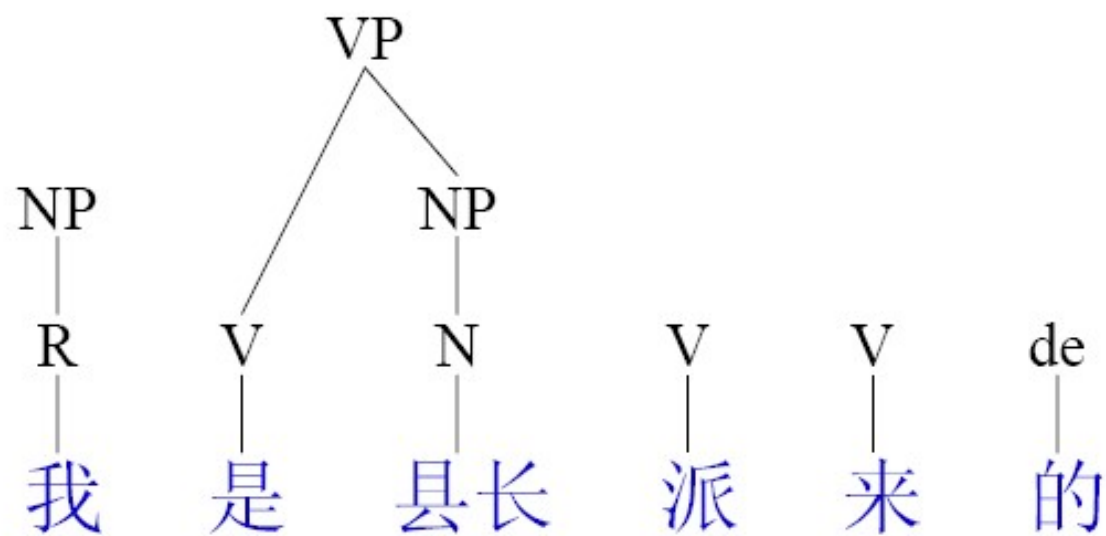
$VP\phi \rightarrow V V$



# 10

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No Rule Apply  
Backtracking



# 11

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No Rule Apply  
Backtracking

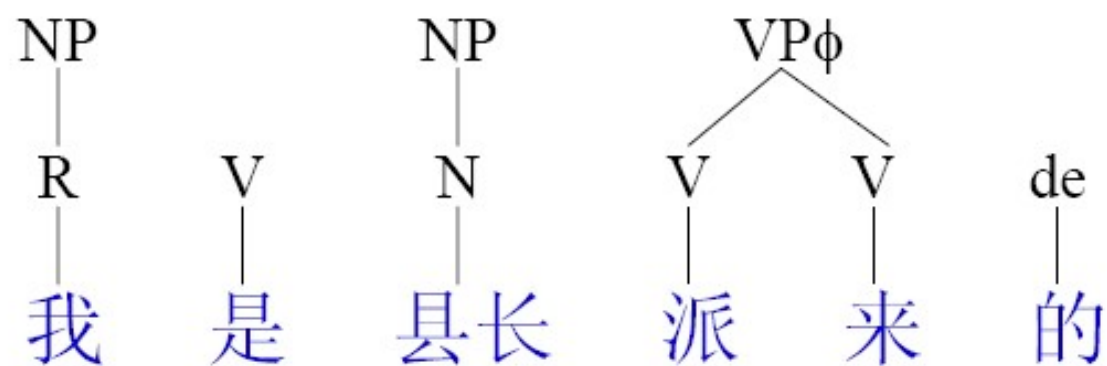
NP		NP			
R	V	N	V	V	de
我	是	县长	派	来	的

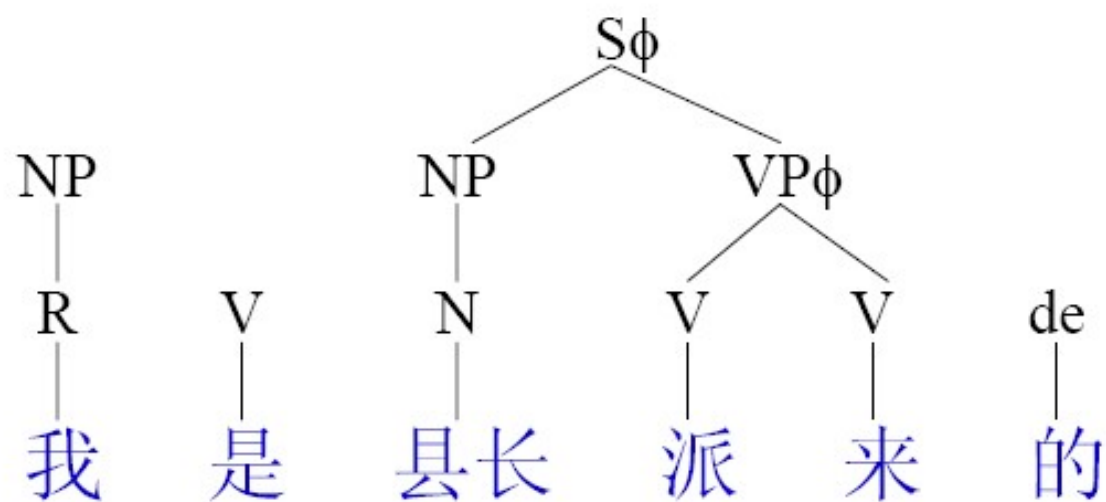


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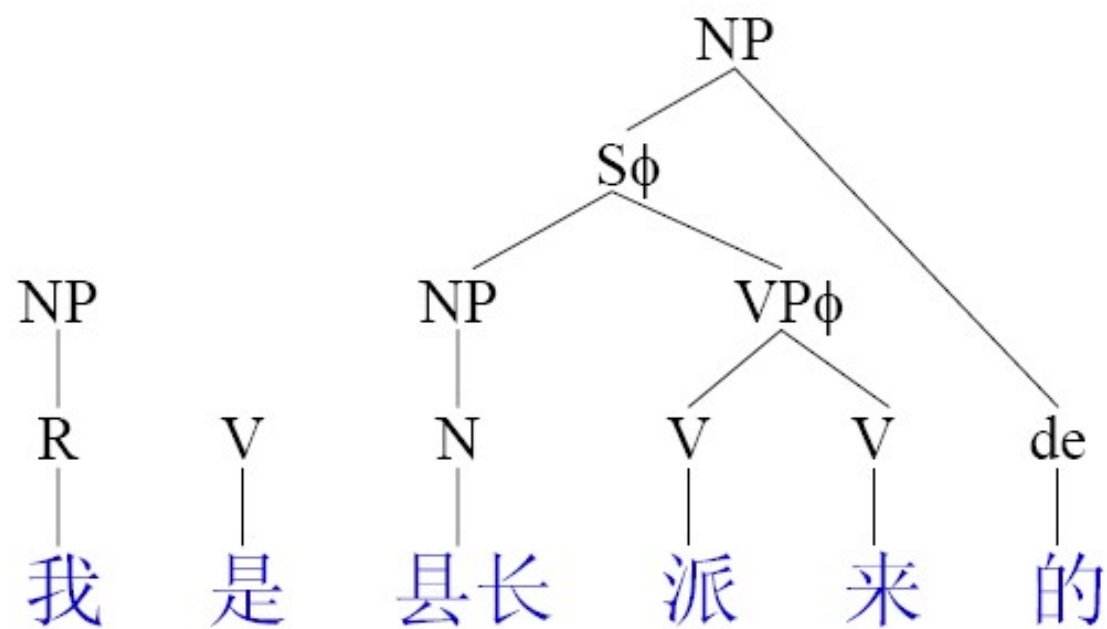
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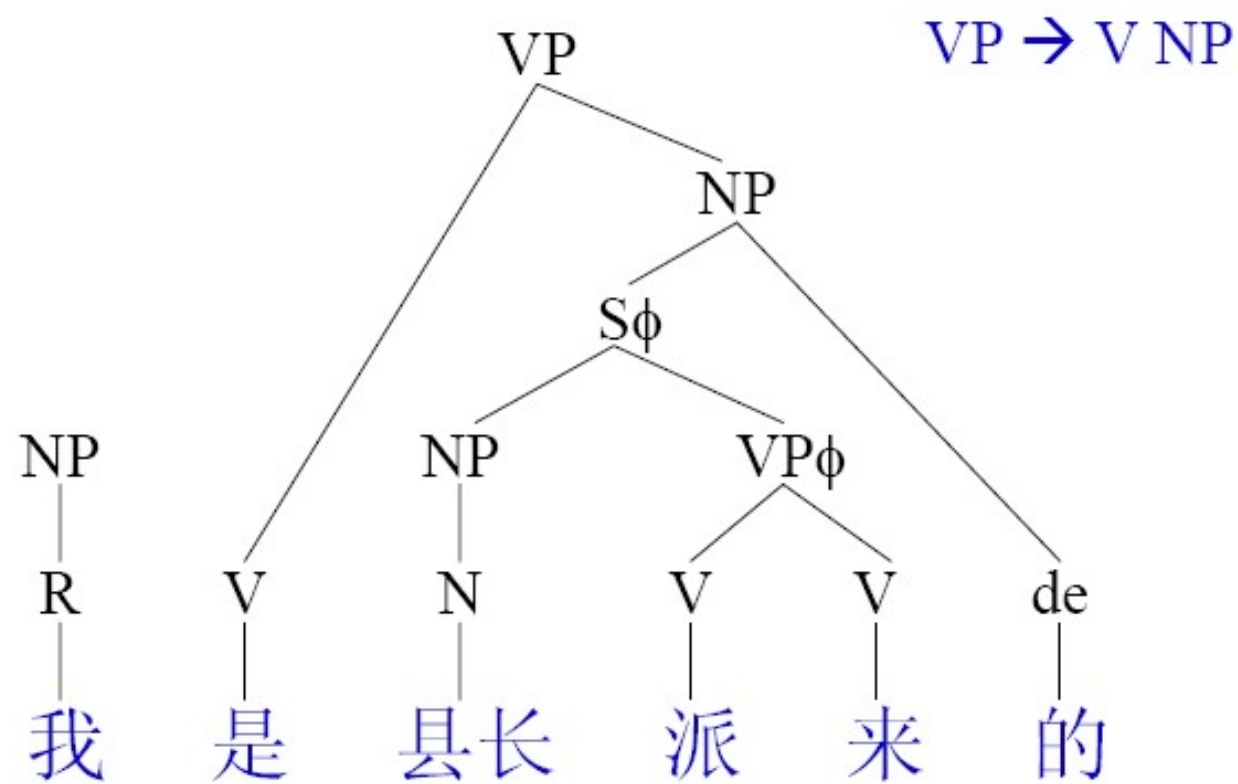
$VP\phi \rightarrow V V$

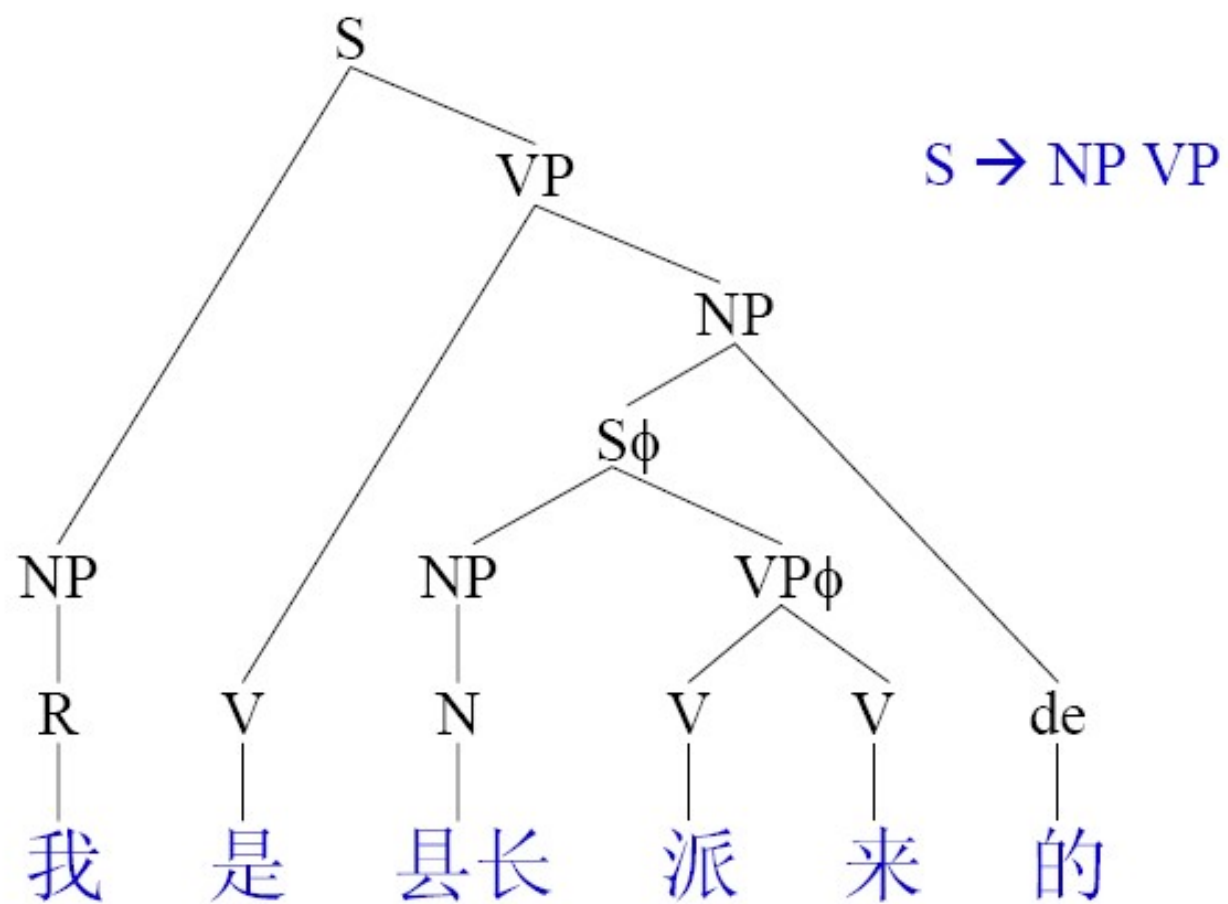


$S\phi \rightarrow NP VP\phi$ 

NP  $\rightarrow$  S $\phi$  de







# Top Down Parsing - Remarks

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- Top-down parsers do well if there is useful *grammar driven control*: search can be directed by the grammar.
- Not too many different rules for the same category
- Not too much distance between non terminal and terminal categories.
- Top-down is unsuitable for rewriting parts of speech (preterminals) with words (terminals). In practice that is always done bottom-up as lexical lookup.

# Bottom Up Parsing - Remarks

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- It is data-directed: it attempts to parse the words that are there.
- Does well, e.g. for lexical lookup.
- Does badly if there are many rules with similar RHS categories.
- Insufficient when there is great lexical ambiguity (grammar driven control might be helpful here)
- Empty categories: termination problem unless rewriting of empty constituents is somehow restricted (but it's generally incomplete)

# CFG Parsing Algorithms

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- Shift-Reduce Algorithm
- CYK Algorithm
- Marcus Analysis Algorithm
- Earley Algorithm (Top-down)
- Tomita Algorithm
- Chart Algorithm



# Shift-Reduce Algorithm

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- Similar to Push Down Automata
- Basic Data structure: Stack
- Four Operations in Shift-Reduced Algorithm
  - Shift 移进:
    - push next input on to top of stack
    - = Shift a terminator to top of stack from left of sentence
  - Reduce 归约 R:
    - top of stack should match RHS of rule
    - replace top of stack with LHS of rule
    - = replace several symbols on the top of stack to one symbol
  - Accept (shift EOF & can reduce what remains on stack to start symbol)
  - Error (shift all words to the stack, but stack have symbols more than S and cannot be reduced)

# Shift-Reduce Algorithm

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	Stack	Input	Operation	Rule
1	#	我是县长	Shift	
2	# 我	是县长	Reduce	$R \rightarrow \text{我}$
3	# R	是县长	Reduce	$NP \rightarrow R$
4	# NP	是县长	Shift	
5	# NP 是	县长	Reduce	$V \rightarrow \text{是}$
6	# NP V	县长	Shift	
7	# NP V 县长		Reduce	$N \rightarrow \text{县长}$
8	# NP V N		Reduce	$NP \rightarrow N$
9	# NP V NP		Reduce	$VP \rightarrow V NP$
10	# NP VP		Reduce	$S \rightarrow NP VP$
11	# S		Accept	

# Ambiguities in Shift-Reduce Algorithm

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- Two kinds of Ambiguities
  - Shift-Reduce ambiguity: The word can be both shifted and reduced
  - Reduce-Reduce ambiguity: The word can be reduced by different rules.
- Backtracking
  - For the ambiguous operations, give a selection order
  - Breakpoint Information: Maintain the non-terminator in stack and breakpoint information including the stack information and optional operations on the breakpoint.

# Backtracking

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- Backtracking Strategy
  - Shift-Reduce Ambiguity: Reduce first, Shift second
  - Reduce-Reduce Ambiguity: Sort the rules according to their priority. Apply the high priority rule first.
- Breakpoint Information
  - Current Applied Rule
  - Candidate Rules
  - Substituted node during reduce operation

# Shift-Reduce Algorithm: Illustration

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- Sort the rule set

Rule	Dictionary
(7) $NP \rightarrow R$	(1) $R \rightarrow$ 我
(8) $NP \rightarrow N$	(2) $N \rightarrow$ 县长
(9) $NP \rightarrow S\phi\ de$	(3) $V \rightarrow$ 是
(10) $VP\phi \rightarrow V\ V$	(4) $V \rightarrow$ 派
(11) $VP \rightarrow V\ NP$	(5) $V \rightarrow$ 来
(12) $S\phi \rightarrow NP\ VP\phi$	(6) $de \rightarrow$ 的
(13) $S \rightarrow NP\ VP$	

# 2

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	Stack	Input	Opr	Rule
1	#	我是县长派来的	Shift	
2	# 我	是县长派来的	Reduce	(1) $R \rightarrow 我$
3	# R (1)	是县长派来的	Reduce	(7) $NP \rightarrow R$
4	# NP (7)	是县长派来的	Shift	
5	# NP (7) 是	县长派来的	Reduce	(3) $V \rightarrow 是$
6	# NP (7) V (3)	县长派来的	Shift	
7	# NP (7) V (3) 县长	派来的	Reduce	(2) $N \rightarrow 县长$
8	# NP (7) V (3) N (2)	派来的	Reduce	(8) $NP \rightarrow N$
9	# NP (7) V (3) NP (8)	派来的	Reduce	(11) $VP \rightarrow V NP$
10	# NP (7) VP (11)	派来的	Reduce	(13) $S \rightarrow NP VP$
11	# S (13)	派来的	Shift	

# 3

---

	Stack	Input	Opr	Rule
12	# S (13) 派	来的	Reduce	(4) $V \rightarrow \text{派}$
13	# S (13) V(4)	来的	Shift	
14	# S (13) V(4) 来	的	Reduce	(5) $V \rightarrow \text{来}$
15	# S (13) V(4) V(5)	的	Reduce	(10) $VP_\phi \rightarrow V V$
16	# S (13) $VP_\phi$ (10)	的	Shift	
17	# S (13) $VP_\phi$ (10) 的		Reduce	(6) $de \rightarrow \text{的}$
18	# S (13) $VP_\phi$ (10) de(6)		Back	
19	# S (13) $VP_\phi$ (10) 的		Back	
20	# S (13) $VP_\phi$ (10)	的	Back	
21	# S (13) V(4) V (5)	的	Back	
22	# S (13) V(4) 来	的	Back	

# 4

---

	Stack	Input	Opr	Rule
23	# S (13) V(4)	来的	Back	
24	# S (13) 派	来的	Back	
25	# S (13)	派来的	Back	
26	# NP (7) VP (11)	派来的	Shift	(13) $S \rightarrow NP VP$
27	# NP (7) VP (11) 派	来的	Reduce	(4) $V \rightarrow 派$
28	# NP (7) VP (11) V(4)	来的	Shift	
29	# NP (7) VP (11) V(4) 来	的	Reduce	(5) $V \rightarrow 来$
30	# NP (7) VP (11) V(4) V(5)	的	Reduce	(10) $VP_{\phi} \rightarrow V V$
31	# NP (7) VP (11) $VP_{\phi}$ (10)	的	Shift	
32	# NP (7) VP (11) $VP_{\phi}$ (10) 的		Reduce	(6) $de \rightarrow 的$
33	# NP (7) VP (11) $VP_{\phi}$ (10) de(6)		Back	



# 5

---

	Stack	Input	Opr	Rule
34	# NP (7) VP (11) VP $\phi$ (10) 的		Back	
35	# NP (7) VP (11) VP $\phi$ (10)	的	Back	
36	# NP (7) VP (11) V(4) V(5)	的	Back	
37	# NP (7) VP (11) V(4) 来	的	Back	
38	# NP (7) VP (11) V(4)	来的	Back	
39	# NP (7) VP (11) 派	来的	Back	
40	# NP (7) VP (11)	派来的	Back	
41	# NP (7) VP (11)	派来的	Back	
42	# NP (7) V (3) NP (8)	派来的	Shift	
43	# NP (7) V (3) NP (8) 派	来的	Reduce	(4) V $\rightarrow$ 派
44	# NP (7) V (3) NP (8) V(4)	来的	Shift	

# 6

---

	Stack	Input	Opr	Rule
45	# NP (7) V (3) NP (8) V(4)来	的	Reduce	(5) $V \rightarrow 来$
46	# NP (7) V (3) NP (8) V(4) V(5)	的	Reduce	(10) $VP_{\phi} \rightarrow V V$
47	# NP (7) V (3) NP (8) $VP_{\phi}$ (10)	的	Reduce	(12) $S_{\phi} \rightarrow NP VP_{\phi}$
48	# NP (7) V (3) $S_{\phi}$ (12)	的	Shift	
49	# NP (7) V (3) $S_{\phi}$ (12) 的		Reduce	(6) $de \rightarrow 的$
50	# NP (7) V (3) $S_{\phi}$ (12) de (6)		Reduce	(9) $NP \rightarrow S_{\phi} de$
51	# NP (7) V (3) NP (9)		Reduce	(11) $VP \rightarrow V NP$
52	# NP (7) VP (11)		Reduce	(13) $S \rightarrow NP VP$
53	# S (13)		Accept	

# Summary of Shift-Reduce Algorithm

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- Shift-Reduce algorithm is a bottom-up analysis
- In order to obtain all possible parsing results, force backtracking is conducted for each success analysis, which leads to lots of redundant operations
- Revisions:
  - Introduce conditional operation rule
  - Introduce contextual operation rule
  - Introduce Cache (Marcus Algorithm)

# CKY Parsing

---

- CKY (Cocke-Kasami-Younger) algorithm
- Bottom-Up Parsing
- The productive rules must be formalized
- Dynamic Parsing ( $O(n^3)$ )
- The rules must be formalized to Chomsky normal form (CNF), where the RHS of this rule must be 2 non-terminal or 1 terminal
- Parsing from Bottom in a table.
- The Parsing for a string depends on the parsing for its sub-strings

# CYK Parsing: Rule Formalization

## Original Grammar

$S \rightarrow NP VP$

$S \rightarrow Aux NP VP$

$S \rightarrow VP$

$NP \rightarrow \text{Pronoun}$

$NP \rightarrow \text{Proper-Noun}$

$NP \rightarrow \text{Det Nominal}$

$\text{Nominal} \rightarrow \text{Noun}$

$\text{Nominal} \rightarrow \text{Nominal Noun}$

$\text{Nominal} \rightarrow \text{Nominal PP}$

$VP \rightarrow \text{Verb}$

$VP \rightarrow \text{Verb NP}$

$VP \rightarrow VP PP$

$PP \rightarrow \text{Prep NP}$

## Chomsky Normal Form

$S \rightarrow NP VP$

$S \rightarrow X1 VP$

$X1 \rightarrow Aux NP$

$S \rightarrow \text{book} \mid \text{include} \mid \text{prefer}$

$S \rightarrow \text{Verb NP}$

$S \rightarrow VP PP$

$NP \rightarrow I \mid \text{he} \mid \text{she} \mid \text{me}$

$NP \rightarrow \text{Houston} \mid \text{NWA}$

$NP \rightarrow \text{Det Nominal}$

$\text{Nominal} \rightarrow \text{book} \mid \text{flight} \mid \text{meal} \mid \text{money}$

$\text{Nominal} \rightarrow \text{Nominal Noun}$

$\text{Nominal} \rightarrow \text{Nominal PP}$

$VP \rightarrow \text{book} \mid \text{include} \mid \text{prefer}$

$VP \rightarrow \text{Verb NP}$

$VP \rightarrow VP PP$

$PP \rightarrow \text{Prep NP}$

*Det*  $\rightarrow \text{that} \mid \text{this} \mid a$

*Noun*  $\rightarrow \text{book} \mid \text{flight} \mid \text{meal} \mid \text{money}$

*Verb*  $\rightarrow \text{book} \mid \text{include} \mid \text{prefer}$

*Pronoun*  $\rightarrow I \mid \text{she} \mid \text{me}$

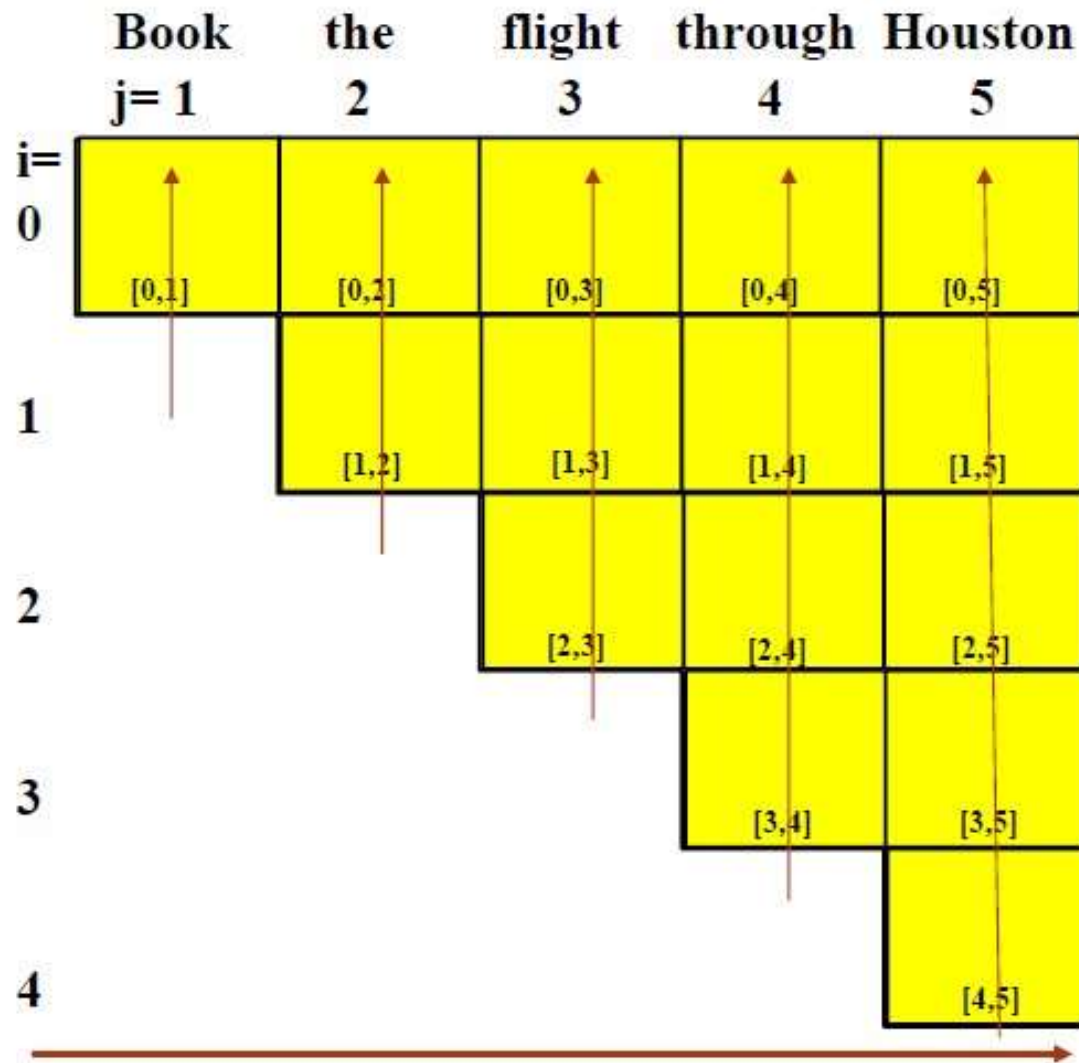
*Proper-Noun*  $\rightarrow \text{Houston} \mid \text{TWA}$

*Aux*  $\rightarrow \text{does}$

*Preposition*  $\rightarrow \text{from} \mid \text{to} \mid \text{on} \mid \text{near} \mid \text{through}$

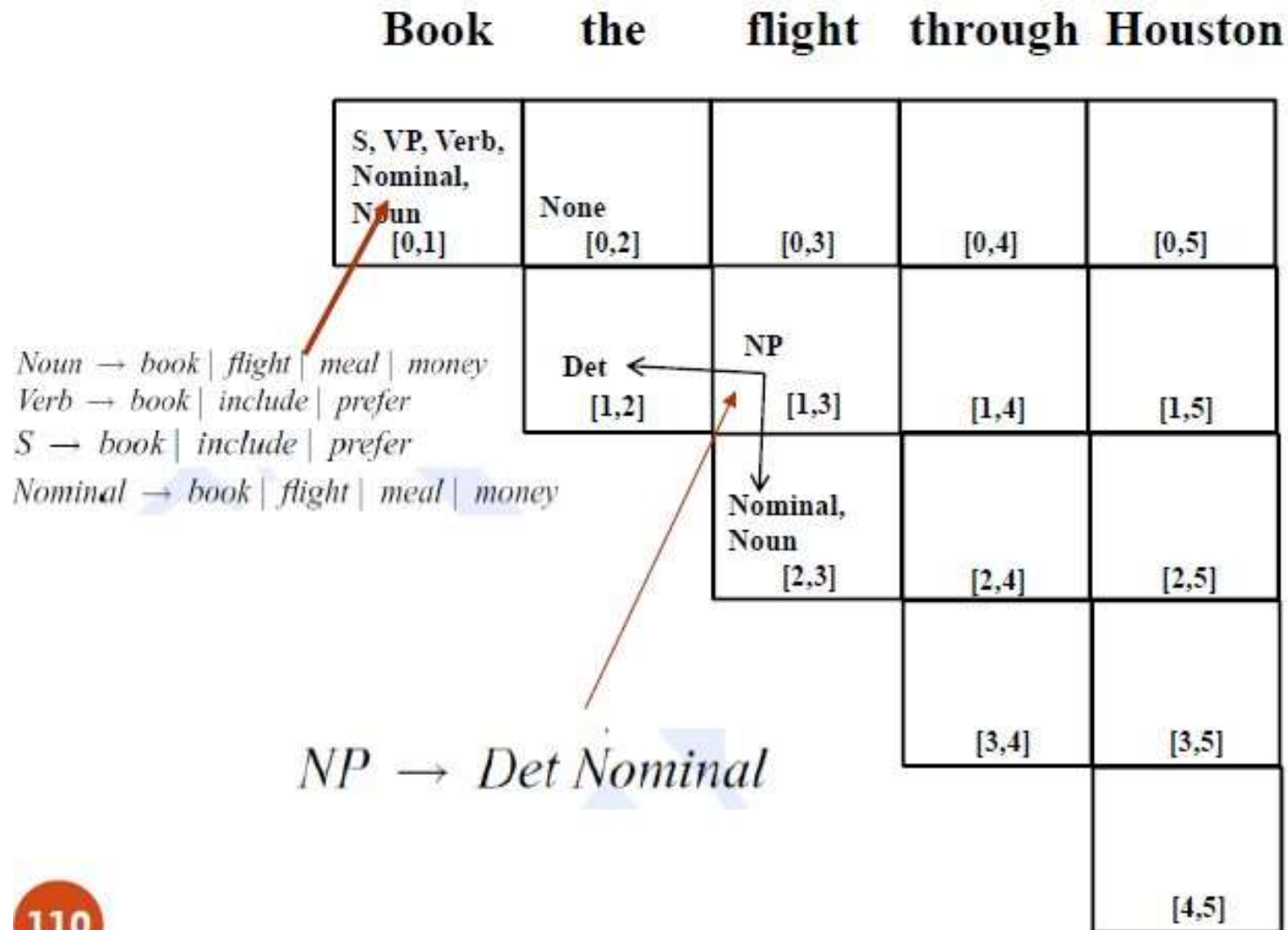
# CYK Parsing

---



**Cell[i,j] contains all of  
Non-terminals which  
covers  
Word<sub>i+1</sub> to Word<sub>j</sub>**

# CYK Parsing



# CYK Parsing

Book the flight through Houston

S, VP, Verb Nominal, Noun [0,1]	None [0,2]	VP [0,3]	[0,4]	[0,5]
	Det [1,2]	NP [1,3]	[1,4]	[1,5]
		Nominal, Noun [2,3]	[2,4]	[2,5]
			[3,4]	[3,5]
				[4,5]

$VP \rightarrow \text{Verb NP}$



# CYK Parsing

---

**Book    the    flight    through    Houston**

S, VP, Verb Nominal, Noun [0,1]	None [0,2]	S VP [0,3]	[0,4]	[0,5]
	Det [1,2]	NP [1,3]	[1,4]	[1,5]
		Nominal, Noun [2,3]	[2,4]	[2,5]
			[3,4]	[3,5]
				[4,5]

$S \rightarrow Verb\ NP$

# CYK Parsing

---

**Book      the      flight      through      Houston**

S, VP, Verb, Nominal, Noun [0,1]	None [0,2]	S VP [0,3]	[0,4]	[0,5]
	Det [1,2]	NP [1,3]	[1,4]	[1,5]
		Nominal, Noun [2,3]	[2,4]	[2,5]
			[3,4]	[3,5]
				[4,5]

# CYK Parsing

---

**Book      the      flight      through      Houston**

S, VP, Verb, Nominal, Noun [0,1]	None [0,2]	S VP [0,3]	None [0,4]	[0,5]
	Det [1,2]	NP [1,3]	None [1,4]	[1,5]
		Nominal, Noun [2,3]	None [2,4]	[2,5]
			Prep [3,4]	[3,5]
				[4,5]

# CYK Parsing

---

Book      the      flight      through      Houston				
S, VP, Verb, Nominal, Noun [0,1]	None [0,2]	S VP [0,3]	None [0,4]	[0,5]
	Det [1,2]	NP [1,3]	None [1,4]	[1,5]
		Nominal, Noun [2,3]	None [2,4]	[2,5]
			Prep [3,4]	PP [3,5]
				NP ProperNoun [4,5]

*PP* → *Preposition NP*

# CYK Parsing

- 

**Book    the    flight    through    Houston**

S, VP, Verb, Nominal, Noun [0,1]	None [0,2]	S VP [0,3]	None [0,4]	[0,5]
	Det [1,2]	NP [1,3]	None [1,4]	[1,5]
		Nominal, Noun [2,3]	None [2,4]	Nominal [2,5]
			Prep [3,4]	PP [3,5]
				NP ProperNoun [4,5]

*Nominal* → *Nominal PP*

# CYK Parsing

**Book the flight through Houston**

S, VP, Verb, Nominal, Noun [0,1]	None [0,2]	S VP [0,3]	None [0,4]	[0,5]
	Det [1,2]	NP [1,3]	None [1,4]	NP [1,5]
		Nominal, Noun [2,3]	None [2,4]	Nominal [2,5]
			Prep [3,4]	PP [3,5]
				NP ProperNoun [4,5]

*NP* → *Det Nominal*

# CYK Parsing

**Book the flight through Houston**

S, VP, Verb, Nominal, Noun [0,1]	None [0,2]	S VP [0,3]	None [0,4]	VP [0,5]
	Det [1,2]	NP [1,3]	None [1,4]	NP [1,5]
		Nominal, Noun [2,3]	None [2,4]	Nominal [2,5]
			Prep [3,4]	PP [3,5]
				NP ProperNoun [4,5]

$VP \rightarrow Verb\ NP$

# CYK Parsing

**Book the flight through Houston**

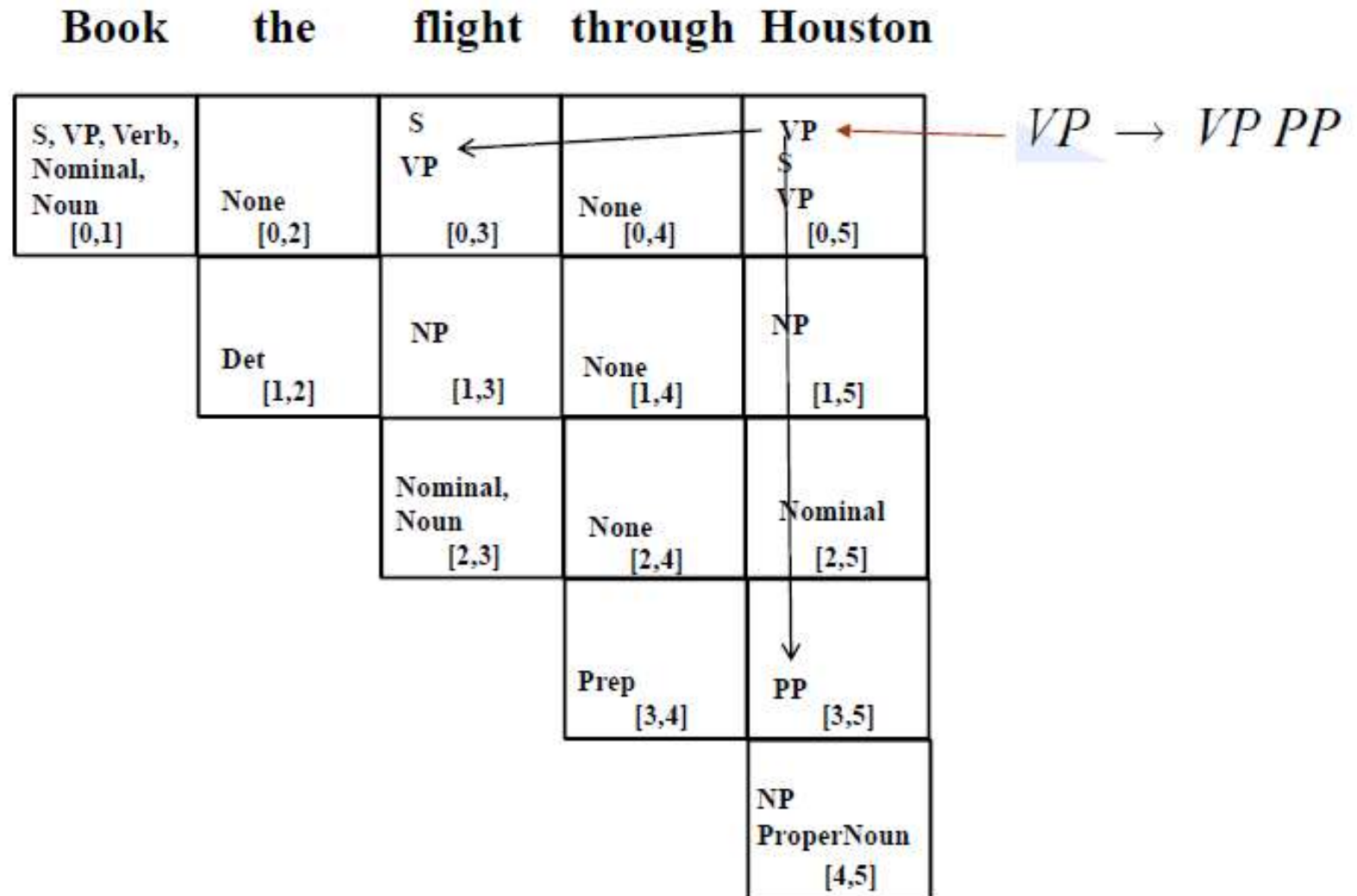
$S \rightarrow Verb NP$

S, VP, Verb, Nominal, Noun [0,1]		S VP [0,3]		S VP [0,5]
	None [0,2]		None [0,4]	
	Det [1,2]	NP [1,3]	None [1,4]	NP [1,5]
		Nominal, Noun [2,3]	None [2,4]	Nominal [2,5]
			Prep [3,4]	PP [3,5]
				NP ProperNoun [4,5]



# CYK Parsing

- 



# CYK Parsing

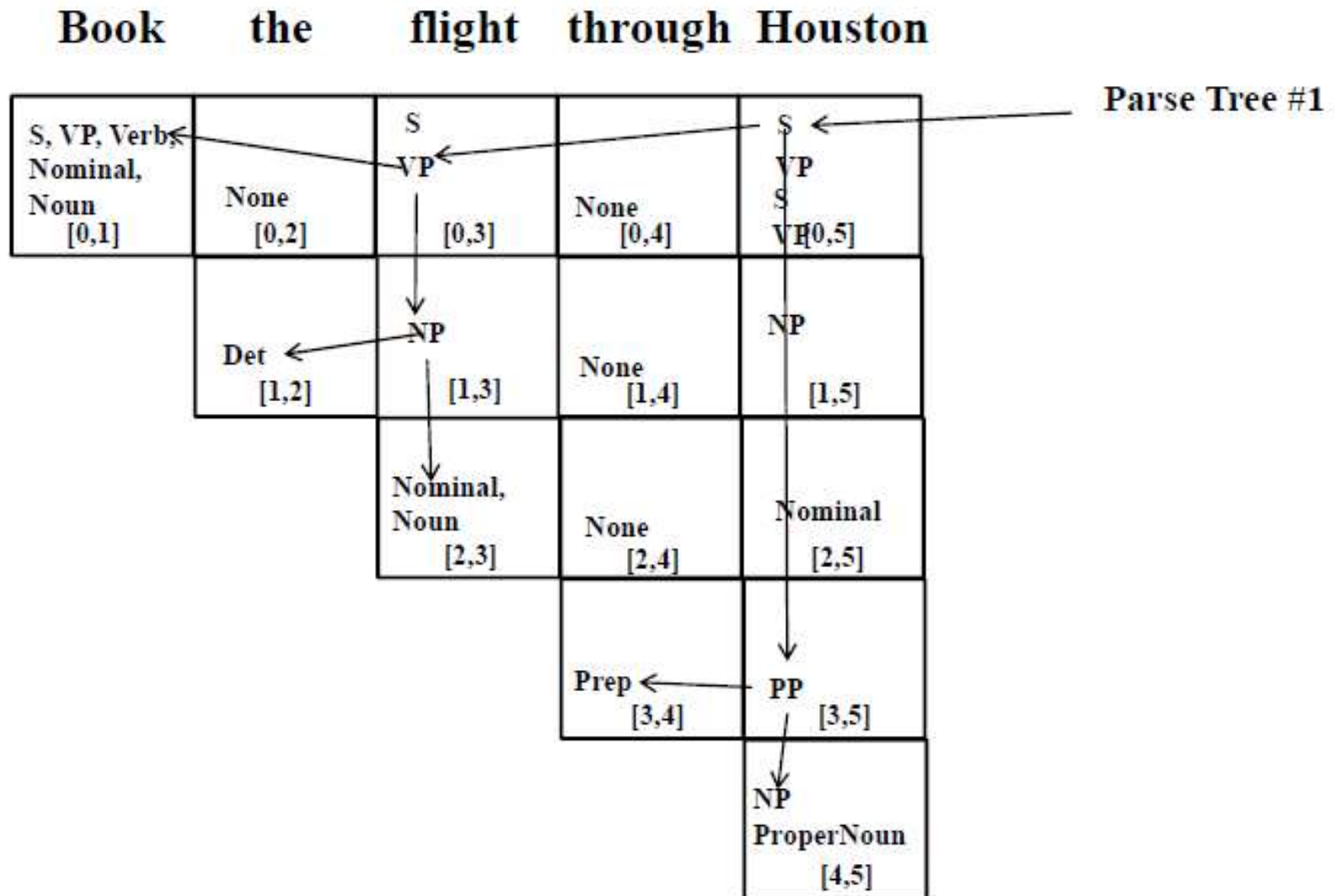
**Book      the      flight      through      Houston**

$S \rightarrow VP PP$

S, VP, Verb, Nominal, Noun [0,1]	None [0,2]	S VP [0,3]	None [0,4]	S VP S VP [0,5]
	Det [1,2]	NP [1,3]	None [1,4]	NP [1,5]
		Nominal, Noun [2,3]	None [2,4]	Nominal [2,5]
			Prep [3,4]	PP [3,5]
				NP ProperNoun [4,5]

# CYK Parsing

- 



# CYK Parsing

- 

**Book the flight through Houston**

S, VP, Verb, Nominal, Noun [0,1]	None [0,2]	S VP [0,3]	None [0,4]	S VP S VH[0,5]
	Det [1,2]	NP [1,3]	None [1,4]	NP [1,5]
		Nominal, Noun [2,3]	None [2,4]	Nominal [2,5]
			Prep [3,4]	PP [3,5]
				NP ProperNoun [4,5]

Parse Tree #2

# CYK Parsing

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- Generate all possible parsing tree
- Complexity:  $O(n^3)$
- Dynamic Parsing
- No disambiguation capability

# The Next Lecture

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- Lecture 11  
Parsing II