

110.2

(2)  $(x^2 + y^2 - x) \in \mathbb{R}, x^2 - y^2 \geq 0 \text{ and } 2x - x^2 - y^2 \neq 0$

$\therefore D(f) = \{(x, y) \mid \cancel{x - \frac{1}{2} + y^2} > \frac{1}{4} \text{ and } x - \frac{1}{2} + y^2 < 1\}$

(4)  $\frac{x}{y} \in [-1, 1], 1 - y \in [-1, 1] \therefore D(f) = \{(x, y) \mid 0 \leq y \leq 2, -y^2 \leq x \leq y^2\}$

(5)  $x \ln(y-x) > 0, y-x > 0 \therefore D(f) = \{(x, y) \mid x > 0 \text{ and } y > 1+x \text{ or } x < 0, 0 < y-x \leq 1\}$

110.3

(2)  $x^2 \leq y \leq \sqrt{x} \quad x \in [0, 1]$

110.4

(2)  $\begin{cases} x+y=u, & x-y=v \end{cases} \Rightarrow \begin{cases} x=u+v \\ y=u-v \end{cases} \therefore f(x, y, z) = (u+v)^{uv} + uv^{2u}$   
 $\Rightarrow \begin{cases} x = \frac{1}{2}(u+v) \\ y = \frac{1}{2}(u-v) \end{cases} \quad z = uv \quad = f(u+v, u-v, uv)$   
 $\therefore f(x+y, x-y, xy) = (x+y)^{xy} + xy^{2x}$

(3)  $\begin{cases} x+y=u \\ \frac{y}{x}=v \end{cases} \Rightarrow \begin{cases} x = \frac{u}{1+v} \\ y = \frac{uv}{1+v} \end{cases} \therefore f(u, v) = \left(\frac{u}{1+v}\right)^2 - \frac{u^2 v^2}{(1+v)^2}$

$\therefore f(x, y) = \frac{u^2(1-v)(1+v)}{(1+v)^2} = \frac{u^2(1-v)}{1+v} = \frac{1-y}{1+y} x^2$

110.5

$f(tx, ty) = t^k f(x, y) \quad \forall t$

$f(x \cdot 1, x \cdot \frac{y}{x}) = x^k f(1, \frac{y}{x}) = x^k F(\frac{y}{x})$