

P31. 1

$$(1) U = \{2, 3, 4, 5, 6, 7\}$$

$$(2) U = \{4, 5, 6, 7, 8, 9, 10\}$$

$$(3) U = \{(t_1, t_2) | 0 \leq t_1 \leq 24h, 0 \leq t_2 \leq 24h\}$$

$$(4) U = \{0, 1, 2, \dots, n\}$$

$$(5) U = \{1000X | X = 0, 1, \dots, 10000\}$$

P32. 4

$$(1) \overline{A} \overline{B} \cup B = A \cup B \quad \checkmark$$

$$(1) \overline{A} \overline{B} \cup B = (B \cup A)(B \cup \overline{B}) = B \cup A = A \cup B \quad \checkmark$$

$$(2) \overline{A} \overline{B} = \text{不成立} \quad \times$$

$$(3) (AB)(A\overline{B}) = AB\overline{B} = \emptyset \quad \checkmark$$

$$(4) BC = B(A \cup \overline{C}) = AB \cup B\overline{C} = B \cup A\overline{C} = \emptyset \quad \checkmark$$

$$(5) A \cup B = B \quad \checkmark \quad (B \supset A)$$

$$(6) AB = B\overline{A} \cup B\overline{A} = B\overline{A} = A \quad \checkmark$$

$$(7) \overline{B} = U - B, \overline{A} = U - A \quad (A \supset B) \quad \checkmark$$

$$(8) (\overline{A} \cup B)C = \overline{A}BC \neq \overline{A}\overline{B}C \quad \times$$

P32. 6

$$P(A \cup B) = P(A) + P(B) - P(AB) = 0.625$$

$$P(\overline{A}B) = P(\overline{A} \cup B) - P(A \cup B) = P(B) - P(AB) = 0.375$$

$$P(\overline{A}\overline{B}) = P(\overline{A} \cup \overline{B}) - P(A \cup B) = 1 - P(A) + 1 - P(B) - (1 - P(A \cup B)) = 0.875 = 1 - P(AB)$$

$$P((A \cup B)(\overline{A}\overline{B})) = (A \cup B)(\overline{A}\overline{B}) = (A \cup B)(\overline{A} \cup \overline{B}) = A\overline{A} \cup B\overline{A} \cup A\overline{B} \cup B\overline{B}$$

$$\therefore = P(B\overline{A}) + P(A\overline{B}) = P(A) + P(B) - 2P(AB) = 0.5$$

P33. 9

$$(1) \quad S = 36, \quad a = 4 \quad \therefore P(A) = \frac{1}{9}$$

$$(2) \quad S = 216, \quad a = 25 \quad \therefore P(A) = \frac{25}{216}$$

P33. 10

$$(1) \quad \sum_{k=0}^n n^k, \quad P(A) = \frac{C_n^k \cdot k!}{n^k}$$

$$(2) \quad P(B) = \frac{(n-1)^{k-r} \cdot C_k^r}{n^k}$$

$$(3) \quad P(C) = \frac{\sum_{k=r}^n C_k^r \cdot (n-1)^{k-r}}{n^k}$$