Statistics with R: a hands-on approach

Myriam Luce

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## Chapter 1

## Data review

### 1.1 Possibly interesting extra tidbits

In the making of this tutorial, I used several tools that you might like to access as well. Being the tedium-averse programmer I am, I use a reference manager program, in my case Zotero. You can find the full bibliography for this project, including a few entries that did not make it into the references section here because I did not cite them, at the Zotero project page.

I also want to point out a wesome-public-datasets, where I foraged for the examples in this tutorial. It has several interesting datasets in the public health domain.

Finally, this tutorial is not necessarily intended to be done in order. In particular, section 2.6 should be read as needed, rather than all the beginning. Not only the section on tidying up data might be boring as a first subject on R, but it's also unlikely to make much sense without some hands-on experience using the software. However, it seemed to make sense to keep all things R together, to make it easier to find again later, when the reader encounters the unavoidable data QA issue.

#### 1.2 Variables

When "doing science", you will be taking measurements, usually in the hopes of understanding a phenomena often in the shape of a relationship between things you are measuring. When working with this data, the nature of the things you measure (variables) will influence the presentation and analysis that are appropriate.

A qualitative variable refers to categories, or a variable recorded with words, as opposed to a quantitative variable, which is measured with numbers. Examples of qualitative variables would include US state, restaurant chains and college major. Quantitative variables could be time to execute a task, waist circumference, disease rate or spending amounts.

R refers to **qualitative variables** as *factors*. **Qualitative variables** can further be divided into non ordinal and **ordinal variables**, depending on whether there is a natural order among the categories. For example, dog breed (chihuahua, husky, labrador) is a non ordinal variable, whereas level of satisfaction (dissatisfied, neutral, satisfied) is ordinal.

Quantitative variables are either discrete variables, where measurements are done in integers, or continuous variables, where they come in real numbers (you could get an infinity of decimals with a theoretical instrument of infinite precision). Discrete variables could be number of children, cancer deaths, or wedding age. Continuous variables include temperature, blood sugar level, and weight.

Furthermore, when studying variables in relationship with one another, changes in a **dependent variable** are driven or explained by an **independent variable**. Typically, this means the "x" axis of a graph will be the **independent variable**, while the "y" axis will be the **dependent variable**.

#### 1.3 Gotchas

#### 1.3.1 Tidy data

When working with data in R, analysis will be easier if your data is *tidy*, that is, each column in your data set contains one and only one variable. Or, more completely:

- 1. Each variable is in its own column
- 2. Each observation is in its own row
- 3. Each value is in its own cell

(Garrett Grolemund gives an excellent introduction to the subject [4].)

For example, in a cancer dataset that we will use later, the original data is presented as in table 1.1. Here, we have four variables: cancer type, sex, number of cases, and number of deaths. While the first column is one and only one variable, the other columns mix sex with number of cases or sex with number of deaths. If you would like to analyze deaths by sex or cases per cancer type, some data manipulation will be necessary to combine the relevant columns.

| Cancon Tymo | C    | ases   | Deaths |        |  |
|-------------|------|--------|--------|--------|--|
| Cancer Type | Male | Female | Male   | Female |  |
| •••         |      |        |        |        |  |

Table 1.1: Cancer data set format.

If you keep your data tidy, R can usually do the combining for you, if you know how to ask nicely. As such, it is recommended that the first thing you do after successfully importing data into R is to verify it is tidy. Tools to divide or merge columns will be discussed in section 2.6.

# 1.3.2 Correlation is not causation, or of the importance of DoE

DoE refers to design of experiments. The common trope that "correlation is not causation" refers to the fact that because two variables vary together does not necessarily mean that one causes the other to change; for instance, they might both be responding to a common cause, when it's not just plain old coincidence. My personal favorite exemplification of "correlation is not causation" is that the divorce rate in Maine correlates with the per capita consumption of margarine [17].

To distinguish between correlation and causation with certainty, a controlled experiment must be run. Depending on the phenomena studied, this might mean using a control group, a placebo, or directly controlling environmental conditions. For example, to determine the effect of low oxygen concentration in water on cod growth, several tanks can be set up where individual cods are randomly distributed and where oxygen levels are controlled. If you were to simply measure oxygen levels in water and cod growth at different locations and subsequently find a correlation between the two, you couldn't tell for certain whether the difference is due to oxygen levels, or another factor like water temperature, or even the fact that cod compete with one another and that the runts, who would grow slower anyway, end up pushed into less desirable lowoxygen environments. Of course, sometimes running a controlled experiment is not feasible for practical reasons (one can't control amount of natural sunlight, for example) or ethical reasons (having an untreated control group of people with a serious condition, when a potentially life-saving treatment might exist, is questionable).

When dealing with humans, to determine whether medication has a positive effect on an health issue, the health issue can be measured for a group who took the medication (treatment group), a group who took a placebo, and a group who took no medication at all (control group). In humans, particular effort must be placed on controlling or measuring the placebo effect, for the test subjects as well as the professionals. A recent spectacular example is the recommendation to abandon arthroscopic surgeries for knee pain because it did not show better results than physical therapy in randomized trials, despite it being the most common orthopaedic procedure in several countries [15].

Where experimental design is concerned, key factors are randomization, blocking, and replication. If terms like Completely Randomized Design, Latin Squares or Factorial Design are not familiar, I would recommend investing some time into learning the basics of experimental design before embarking in an experiment, in the interest of avoiding some common and easily remedied mistakes ([7] appears to be a well-rounded textbook).

# Chapter 2

# Unavoidable R before we begin

Despite the title, this chapter is not meant to be read from start to finish before you get to the other chapters. First, a long text about programming quirks can get pretty sleep-inducing. Second, the concerns addressed will probably not resonate much with you unless you've personally encountered this problem before, so the information retention is likely to be low.

That being said, the three first sections (2.1, 2.2, 2.3) should probably be read right now if you are not familiar with R at all. The other ones are referenced later in the text when they are relevant and can be read at that time.

## 2.1 Packages

R [13] should be relatively straightforward to install: download and execute, follow the wizard instructions.

Where things get a bit more complicated is when it comes to packages. While the basic R program has a lot of functions built-in, there will come a time when you will need something that is not offered out of the box. Thankfully, R has a very dynamic community with a ton of packages. For instance, a very popular package to produce figures is ggplot2. Let's install it to see how packages are managed in R.

First off, to install packages in R, you will need to launch it as an administrator. If you don't, you will get the rather unhelpful message shown in figure 2.1. To launch with administrator rights, right-click on your R launcher and find the option "Run as administrator". How to do so from the Windows 10 start menu is shown in figure 2.2. (As a note, you should launch as administrator only when installing packages, as opposed to modifying your shortcut to always launch as administrator.)

Now that R is launched as administrator, you can install ggplot2 using either the convenient Packages menu or the command line if you're that hard-



Figure 2.1: Error message displayed by R if trying to install packages without administrator rights.



Figure 2.2: How to launch R with administrative rights.

core. Personally I use the menu; after choosing a mirror (different mirrors offer different packages; Canada NS has a wide selection and is vaguely geographically close), you can select your desired package and hit "install", as shown in figure 2.3. Then you only need to wait until R is done doing its thing. If all the lines say "successfully unpacked", all good; otherwise, an error has occurred and you will have to decipher the message to figure out how to remedy the situation. (If you run into any trouble, I would first recommend updating to the latest release of R.)

Note that installing a package is not enough to use it; you must also load it. Again this can be done either from the menu or with the command line, as shown in figure 2.4. This operation must be repeated *every time* you restart R.

Now let's say that ggplot2 becomes your favoritest package in the whole world and you end up using it every day. After a week or so you will probably be very annoyed having to reload the package every time you open R. You can add packages to be loaded automatically in either of two files: Rprofile.site or .Rprofile. Rprofile.site is located in your R installation folder in the etc folder and is always executed. .Rprofile is located in the user home folder and is applied after the changes made by Rprofile.site. As the appropriate location to put .Rprofile seems to change from R version to version, I will showcase the Rprofile.site here. At the bottom of the file, add the following:

```
.First <- function(){
    library('ggplot2')
    # other libraries go here
}</pre>
```

## 2.2 Types

While relatively accessible as far as programming languages go, R is still a programming language. As such, it has a few concerns that, while painful for the non-programmers among us, are useful tools to diagnose problems, typically when importing data that has not been properly QA'd or when a function refuses to compute because the input is in a form it refuses.

Let's talk about types. Types refer to the nature of a variable in a computer

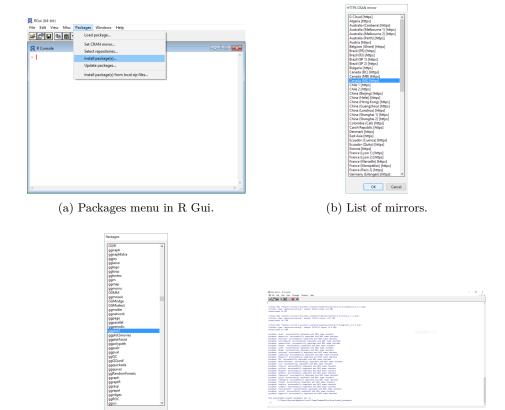


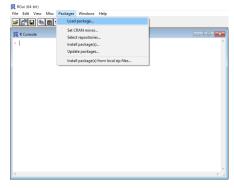
Figure 2.3: Package installation process.

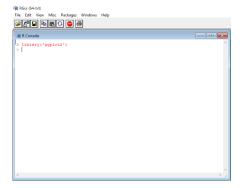
installation.

(c) List of packages.

(d) All successfully unpacked: successful

program; is it text, a number, etc.? If it's a number, can it be any number, or integers only? This is important because computing the means of grades in a class makes sense, while computing the means of the name of the students doesn't. Further, since R is a statistical program, it also includes types not typically seen in programming languages, like factors and ordinal variables. The following table gives an overview of variable types in R.





- (a) Packages menu in R Gui.
- (b) Command to load a package in R Gui.

Figure 2.4: Loading packages in R.

Logical: TRUE or FALSE

Numeric: real, by the math definition (ex. 12.3). Double is a numeric

with better precision.

**Integer:** integer, by the math definition (ex. 12).

**Character:** text of any length; defined by typing "text" or 'text'

Factor: a type that represents a qualitative variable

Ordered: a type that represents an ordinal variable

List: a 1D collection of "things" (may be strings, numbers, or a

mix of them)

Vector: a 1D collection of things of one type

Matrix: a 2D collection of things of one type

Array: a nD collection of things of one type

Data Frame: a (mostly) 2D collection of things, where each column can

be of a different type

For future reference, Quick R gives an excellent introduction on the subject [12]. You can convert a variable to anything reasonable (R will turn "2" into an integer, but not "abc") using the host of as.xyz functions.

The data frame is of particular interest, since it allows the use of a specific syntax we will use later. A data frame is closest to a "table" you would have in your spreadsheet software: it holds values for several variables, where each column is a variable, and the headers hold sensible names.

To see which type a variable has, class and str (structure) are most informative. class will return the type of the variable (for example, "data frame"), while str will make a summary of the variable and its components, if any (for example, the various columns of a data frame).

## 2.3 Accessing collection elements

Some of the types presented in the previous section group several values. At some point, you'll want to access one or many of the elements, but not all. Let's say you have a data frame, for example ebola deaths by country [9]:

#### > ebola

#### Country Deaths

| 1 |                |        |      | Guinea   | 2543 |
|---|----------------|--------|------|----------|------|
| 2 |                |        |      | Liberia  | 4809 |
| 3 |                | S      | ierı | ra Leone | 3956 |
| 4 |                |        |      | Mali     | 6    |
| 5 |                |        |      | Nigeria  | 8    |
| 6 | ${\tt United}$ | States | of   | America  | 1    |

Notice how the line with "Country" and "Deaths" is not numbered in the output? It means R is aware it's a header and not data. *Data frame columns* (not matrices) can be accessed by their name using the \$ operator, like so:

#### > ebola\$Country

| [1]               | Guinea | a              |         | ]    | Liberia |                    | Si     | ierra |
|-------------------|--------|----------------|---------|------|---------|--------------------|--------|-------|
| $\hookrightarrow$ | Leone  |                |         |      |         |                    |        |       |
| [4]               | Mali   |                |         | 1    | Nigeria |                    | Ur     | nited |
| $\hookrightarrow$ | States | s of Ame       | erica   |      |         |                    |        |       |
| 6 L               | evels: | ${\tt Guinea}$ | Liberia | Mali | Nigeria | <br>${\tt United}$ | States | of    |
|                   | Americ | <b>-</b> 2     |         |      |         |                    |        |       |

If you want to access lines, elements or columns, you can use the [row, column] operator, like so:

```
> ebola[1,]
Country Deaths
1   Guinea   2543
> ebola[1,2]
[1]   2543
> ebola[,2]
Deaths
[1]   2543
[2]   4809
[3]   3956
[4]   6
[5]   8
[6]   1
```

While the \$ operator is exclusive to data frames, the [] is used for all collections. Vectors, lists, matrices and arrays can be accessed with the [index] operator for 1D structure, [row, column] operator for 2D structures, and [i, j, k...] for nD structures.

In the case you want to access several items at once, you can use a colon inside the brackets, i.e. [begin:end] like so:

```
> ebola[1:3,]
Country Deaths
1    Guinea   2543
2    Liberia   4809
3 Sierra Leone   3956
```

#### 2.4 Misc

#### 2.4.1 c is for concatenate

Sometimes, a function in R will use an argument that is actually a list of things; for example, the limits of the x axis are two values: the minimum and maximum values to display on the graph. Referring back to the types we just saw, R requires a vector of values. Since it's such a common usage, R offers a quick way to create a vector with the function c().

```
> ... xlim = c(0, 100), color = c(255, 0, 0) ...
```

#### 2.4.2 # is for comments

If you use # in R, it will consider anything to its right to be a *comment*, that is, not code, and it will be ignored. You can start a line with it or use it in the middle of a line. It can be useful to leave notes to yourself in long-ish scripts.

#### 2.4.3 Use argument names

When you use a function, for example barplot, there are a certain number of unavoidable parameters, followed by several optional parameters. The optional parameters typically have a default value, so if you don't specify them, the function works as expected, using the default values. For example, let's consult the help page for barplot by typing ?barplot at the R prompt.

```
inside = TRUE, plot = TRUE, axis.lty = 0, offset = 0,
add = FALSE, args.legend = NULL, ...)
```

In this example, the parameter height, which is not followed by an "=" is a necessary parameter; you can't compute a bar plot without giving it some values to put in the graph! All the other parameters are optional, and the help page lists their default value.

If you decide you want your bars to be beside one another rather than stacked, you will have to set the parameter beside, which is the fifth optional parameter. To avoid really strange and unfortunate guesswork on R's part when it tries to figure out which parameter you set among the gazillion optional parameters, always use the optional parameter names, for example:

```
> heights = c(15, 5, 1, 12, 28)
> # barplot(heights, TRUE)
> # BAD!
> # Don't make R guess!
> # It's bad at it!
> barplot(heights, beside = TRUE) # Good
```

#### 2.4.4 Dates

As I may have mentioned, dates in programming are their very own Pandora box. R internally saves its dates as the number of days since January 1st, 1970.

In real life, you will likely encounter dates in a file in one of various text formats, for example something like "mm/dd/yyyy" (and since not all languages list their dates in the same order, you should pay close attention when dealing with international data), or as three different columns for the day, the month and the year. If you want R to do nice things for you like calculating the number of days between two dates, you need to transform these eminently unstandard formats into R's own format. So let's see how this is done for an arbitrary text format and for the three numeric columns cases.

#### Text to Date

For this, let's use the traffic data from the city of Chicago [1]. After downloading the csv, in your spreadsheet software, assign appropriate types to the date, vehicle volume, latitude and longitude columns, then tweak header names, save as csv and load into R. You should obtain the following:

```
> traffic = read.csv("C:/.../r-tutorial/traffic.csv")
> str(traffic)
'data.frame': 1279 obs. of 9 variables:
$ ID : Factor w/ 1279 levels "1","1,000","1,001",..: 453...
$ Address : Factor w/ 1203 levels "1 West","10 East",..: 212 ...
$ Street : Factor w/ 251 levels "100th St","101st St",..: 40 ...
```

So your date has been read as a factor; dates are a kind of category, I suppose, but R doesn't make computations on factors. You can't subtract blue eyes from green eyes, but you definitely can subtract 2010/01/08 from 2010/02/07 to compute how many days have passed between them.

Thankfully, R offers the function as.Date to convert text to Date. It uses a series of codes that you can see in the details of the help page for strptime. For instance, %m, %d and %Y stand for decimal month, decimal day and decimal year including century, respectively. It is used in the following manner:

```
> traffic$Date = as.Date(traffic$Date, format="%m/%d/%Y")
> str(traffic)
'data.frame':
                1279 obs. of 9 variables:
           : Factor w/ 1279 levels "1","1,000","1,001",...
$ Address
          : Factor w/ 1203 levels "1 West", "10 East", ...: 212 ...
           : Factor w/ 251 levels "100th St", "101st St", ...
$ Street
           : Date, format: "2006-03-09" "2006-02-28" ...
$ Volume
           : int 14600 16500 18200 21600 18300 8600 10000 ...
$ Direction: Factor w/ 1223 levels "East Bound: 1000 / West
→ Bound: 3400",...: 397 442 484 20 495 257 939 936 981 909 ...
$ Latitude : num 41.8 41.8 41.8 41.8 41.8 ...
$ Longitude: num -87.7 -87.7 -87.6 -87.6 -87.6 ...
$ Location : Factor w/ 1276 levels "(41.651861, -87.54501)",...
```

#### Three numbers to Date

While R does not offer a specific function that takes three numbers and returns a date, it is easy enough to build a date string from three numbers, and then feed that to as.Date. For example, if the dates in the traffic data were in three columns, you could proceed this way:

```
> dateStrings[1:10]
[1] "2006/3/9" "2006/2/28" "2006/2/28" "2006/2/28"
[5] "2006/2/28" "2006/3/9" "2006/3/7" "2006/3/7"
[9] "2006/3/7" "2006/3/7"
> traffic2$Date = as.Date(dateStrings, format="%Y/%m/%d")
> str(traffic2)
'data.frame': 1279 obs. of 12 variables:
#...
         : Date, format: "2006-03-09" ...
$ Date
$ Month
       : int 3 2 2 2 2 3 3 3 3 3 ...
        : int 9 28 28 28 28 9 7 7 7 7 ...
         $ Year
→ 2006 ...
#...
```

#### Date to text

Converting a date to text is straightforward enough and allows you to specify the format you want. By default, R prints dates following the ISO convention of YYYY-MM-DD [2]. If you really want your heretic US format, you could use format (which, by the way, also allows you to format numbers by defining leading zeros or number of decimals).

```
> today = Sys.Date()
> format(today, format="%m/%d/%y")
[1] "09/27/18"
```

#### Date computations

You can make calculations on dates. The following examples should tell you the gist of it.

```
> lastyear = Sys.Date()-365
> lastyear
[1] "2017-09-27"
> today-lastyear
Time difference of 365 days
> nextmonth=today+30
> nextmonth
[1] "2018-10-27"
```

## 2.5 Saving, a.k.a scripts

As long as you're doing simple things fitting on two or three lines, you probably won't feel the need to "save your file". However, as you start doing more elaborate data treatment or need to document a process used, you will want to save your progress.

One way to save is to use R's built-in workspace. A workspace is a .RData file that contains all the variables (used here in the computer science sense: a value that you attached a name to) you have defined since you started R. For example, if you typed the following:

```
> 1+2
[1] 3
> a = "I am text"
> x = 5+3
> y = x-8
> x
[1] 8
```

In this case, a, x and y would be saved in your workspace. Next time you started R, you could load the workspace and R would know that x is worth 8.

Another useful feature of R is the history, that is, the 250 (by default) last commands you typed in the window. You can access them by pressing the up arrow, which can be pretty handy when you want to tweak a command to fix a typo. You can save it in a .Rhistory file that you can also load the next time you start R.

Finally, if there is a small routine that you need to save, you can save it in a simple text file that you can load and execute. In the File menu, choose New script and type some text in the window, for instance:

```
x = c(1, 2, 3, 4, 5, 6, 7, 8, 9, 10)
y = 2*x
x
y
plot(x, y)
```

As you type the commands and press enter, nothing happens, as opposed to using the main window. To run these commands, you need to select what you want to run (for example, everything: select with ctrl+a), then press F5. If you do, you should see the outputs appearing in the main window. Once you're reassured that your basic algorithm is running, you might want to tweak the plot function to add axes and labels before re-rerunning the script. Once you're done, you can save this simple text file and have an easily viewable record of what you did.

## 2.6 Data: import, export, tidy

#### 2.6.1 Import

Delimited data: read.csv is your friend

A typical workflow to get data from wherever into R would be as follows:

1. Copy-paste the data into your favorite spreadsheet software (Microsoft Excel, LibreOffice Calc, Google Sheets, etc.).

- 2. If necessary, transpose your data so that variables are in columns (rather than rows).
- 3. Tweak column names so they have no spaces and no special characters (é, \$, etc).
- 4. Assign a reasonable format (text, number, thousand separators, etc.) to all columns.
- 5. With your operating systems using an English locale, save as csv.
- 6. Use read.csv in R with the *full path* using *forward slashes*, and the appropriate options.

As a case study, let's import the data for infant mortality [6]. Data is already in columns and country names contain no special characters. So let's just change the first column header to "Country". Next, let's set the columns B and up (excluding the header for practical reasons seen later) to format "number". You might note that the decimal separator used in this file is a comma rather than a dot. However, setting the number format should be enough for your Spreadsheet software to convert them properly. Where to set number format will vary depending on your spreadsheet program; how to apply number formatting in LibreOffice is shown in figure 2.5. In LibreOffice in particular, make sure your number format locale is English. Save the modified file in csv format.

Once in R, import the data using read.csv. Once that is done, however, you should always doubt that everything went well. Just to prove my point, let's examine the imported data a little more closely (see section 2.2 about data frames and section 2.3 about the \$ operator):

```
> infant = read.csv('C:/.../r-tutorial/infant.csv', header=TRUE)
> class(infant)
[1] "data.frame"
> str(infant)
'data.frame':
                260 obs. of 217 variables:
$ Country: Factor w/ 260 levels "Abkhazia", "Afghanistan", ...: 1
$ X1800
        : int NA ...
$ X1801
        : int NA ...
        : int NA NA NA NA NA NA NA NA NA ...
$ X1861
        : Factor w/ 11 levels "",".","110","131",..: 1 1 1 1 ...
$ X1862
        : Factor w/ 13 levels "",".","106","113",..: 1 1 1 1 ...
$ X1863
```

Wait, what? The country is of type factor, we all agree on that, but infant mortality rate for 1862 is a factor? Let's pick 1862 and see if we can't just eyeball the problem:

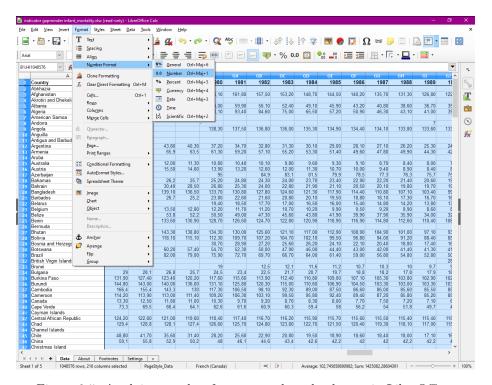


Figure 2.5: Applying number format to selected columns in LibreOffice.

```
> infant$X1862
[1]
          250.00
[16]
                                     150.00
[31]
[46]
                 131.00
[61]
[76] 163.00
[91]
[106]
[121]
[136]
[151]
             193.00
                                     81.00
[166]
                                                              110.00
[181]
[196]
                                                    139.00
[211]
                      175.00
[226]
[241]
[256]
```

```
Levels: . 110.00 131.00 139.00 150.00 163.00 175.00 193.00 

→ 250.00 81.00
```

I don't know if you can see it, or if you think it's a speck of dust on your screen, but there's a lonely dot there somewhere between lines 226 and 241. I am going to assume it means it's a missing data point, since nothing else makes sense.

(In other languages, like French for instance, the decimal "point" is a comma, and therefore the "comma-separated" part of comma-separated value leads to some issues, not to mention the English thousand separator. This is why you set your data format in your spreadsheet: once the cell are properly formatted, your spreadsheet will export them sensibly into the csv.)

Let's try again, this time telling read.csv that dots are missing data:

This looks better, however the last line displayed is for 1897. If you're a trusting person (and you should never trust a computer), you might think everything is okay now. However, I cheated and skipped ahead and tried to use this data before and encountered another QA gem. So let's make sure to display all the variables with a trick we will see in detail later (section 8.1.1; for now let's just say it applies class to every part of infant.

```
> sapply(infant, class)
Country
            X1800
                       X1801
                                  X1802
                                             X1803
                                                       X1804
\,\hookrightarrow\,\quad X1805
              X1806
                         X1807
                                    X1808
                                               X1809
"factor" "numeric" "numeric" "numeric" "numeric" "numeric"
    "numeric" "numeric" "numeric" "numeric"
# ...
X1953
          X1954
                     X1955
                                X1956
                                          X1957
                                                     X1958
                                                                X1959
\rightarrow X1960
              X1961
                         X1962
                                    X1963
"numeric" "numeric" "numeric" "numeric" "numeric" "numeric"
  "numeric" "factor" "numeric" "numeric" "numeric"
# See that pesky 1960?
> infant$X1960
[1]
           245.00
                          115.40 148.20
                                                         208.00
  59.87
                          20.30 37.30
```

```
# ...
[256] 88.00 123.20 92.60
146 Levels: - 100.60 101.60 102.00 102.10 102.20 105.00 106.70

→ 107.40 107.50 110.60 112.00 115.40 115.50 ... 94.00
```

So, apparently "-" also means missing data? Gods forbid the authors hit a snag while importing data and their software didn't warn them something foul was afoot (like R just did to us, thank you R) and they just pasted it in the global csv without noticing. (This is why science should be in databases. Real databases. They don't let you put a dash in a number field, they just don't.)

Now, finally, we get:

```
> infant = read.csv('C:/.../r-tutorial/infant.csv', header=TRUE,

¬ na.strings=c('-', '.'))

> sapply(infant, class)
Country
            X1800
                       X1801
                                 X1802
                                            X1803
                                                       X1804
  X1805
              X1806
                         X1807
                                   X1808
                                              X1809
"factor" "numeric" "numeric" "numeric" "numeric" "numeric"
   "numeric" "numeric" "numeric" "numeric"
# ...
X2008
          X2009
                     X2010
                               X2011
                                          X2012
                                                    X2013
                                                               X2014
\,\hookrightarrow\,\quad X2015
"numeric" "numeric" "numeric" "numeric" "numeric" "numeric"
    "numeric" "numeric"
```

#### Fixed-width data: read.fwf

In some few cases, most often when importing data from government websites who offer them up publicly in .txt format, you will encounter fixed-width data. Delimited data uses a character (most often a comma) to signify the boundary between cells of data. Fixed-width, however, always has the same number of characters for a given field. To demonstrate, figure 2.6 shows what csv (delimited) and fixed-width data look like side by side.

Figure 2.6: Delimited data (left) and fixed-width data (right).

As a case study, let's use historic water levels for a river in Canada [11]. Data looks like this:

- 1 Ministère du Développement durable, de l'Environnement et de la Lutte contre les changements climatiques
- 2 Données validées jusqu'au 1994-09-30
- 3 Station: 070401 Portneuf à l'amont des chutes Philias
- 4 Bassin versant: 3085 km2 Régime: Naturel
- 5 Coordonnées: (NAD83) 48 38' 54" // -69 10' 55"

6

- 7 Date de création du fichier: 2012-06-30 02:40
- 8 Particularité(s):
- 9 -
- 10 -
- 11 -

21

- 12 Lexique: E: La donnée est estimée.
- 13 (Remarque) J: Un jaugeage a été exécuté %\*à cette date.
- 14 MC: La donnée représente un débit moyen converti.
- $15\,$  MJ: La donnée est une moyenne journalière.
- 16 P: La donnée est provisoire.
- 17 PL: La donnée correspond %\*à la premi\ère lecture de niveau d'eau de la journée.
- $18\ \mbox{R:}\ \mbox{Le débit est corrigé pour tenir compte de l'effet de refoulement.}$
- 19 S: La donnée est saisie manuellement.
- 20 Z: La donnée provient d'une redistribution temporelle des données enregistrées en raison d'une dé fectuosité de l'appareil de mesure.

| 41 |          |            |              |    |
|----|----------|------------|--------------|----|
| 22 | Station  | Date       | Débit (m3/s) |    |
|    | Remarque |            |              |    |
| 23 | 070401   | 1973/08/17 | 86.60        | J  |
| 24 | 070401   | 1973/08/18 | 79.90        | MC |
| 25 | 070401   | 1973/08/19 | 73.30        | MC |
| 26 | 070401   | 1973/08/20 | 68.80        | MC |
| 27 | 070401   | 1973/08/21 | 65.10        | MC |
| 28 | 070401   | 1973/08/22 | 63.70        | MC |
| 29 | 070401   | 1973/08/23 | 63.70        | MC |
| 30 | 070401   | 1973/08/24 | 62.00        | MC |
| 31 |          |            |              |    |
| 32 | 070401   | 1994/09/25 | 47.55        | MC |
| 33 | 070401   | 1994/09/26 | 46.74        | MC |
| 34 | 070401   | 1994/09/27 | 45.95        | MC |
| 35 | 070401   | 1994/09/28 | 46.26        | MC |
| 36 | 070401   | 1994/09/29 | 54.98        | MC |
| 37 | 070401   | 1994/09/30 | 80.23        | MC |
|    |          |            |              |    |

Save it as a text file on your computer as is. To read fixed-width data, you need to explicitly tell R the widths of each column. The popular Windows text editor Notepad++ shows column index, which allows to calculate them quickly: 6, 20, 15 and 12 (column starts with whitespace and ends with data). Furthermore, the "table" part of the file starts on line 23.

(Since there are accents in the file, if you were interested in the comments, you might want to take an extracurricular dive into encodings. Since this is an English document, I will not add another painful tangent, but as a quick note, if you ever encounter trouble importing European documents, try CP-1252 (Windows default) or ISO-8859-1 (Latin extended, covers French, German and Spanish, for instance).)

(Another note, there is a function to read Fortran files, which I never needed to use but might be useful to you. My condolences on dealing with Fortran.) read.fwf is used this way:

```
> debit = read.fwf("C:/.../r-tutorial/debit.txt", widths=c(6, 20,
   15, 12), header=FALSE, skip=22, strip.white=TRUE,
   col.names=c('Station', 'Date', 'Debit', 'Remarque'))
> str(debit)
'data.frame':
                7715 obs. of 4 variables:
$ Station : int 70401 70401 70401 70401 70401 70401 70401 ...
          : Factor w/ 7715 levels "1973/08/17", "1973/08/18", ...: 1
$ Date
    2 3 4 5 6 7 8 9 10 ...
          : num 86.6 79.9 73.3 68.8 65.1 63.7 63.7 62 59.2 ...
$ Remarque: Factor w/ 5 levels "E","J","MC","R",..: 2 3 3 3 3 ...
> debit[1:5,]
Station
              Date Debit Remarque
                      86.6
    70401 1973/08/17
   70401 1973/08/18
2
                      79.9
                                 MC
3
   70401 1973/08/19
                                 MC
                      73.3
4
    70401 1973/08/20
                      68.8
                                 MC
   70401 1973/08/21
                      65.1
                                 MC
```

As opposed to read.csv, I used the argument header=FALSE with read.fwf. This is due to read.fwf being pickier about the header format: it wants the header to be *delimited* with a character that is not present in the rest of the file (to practice, type in ?read.fwf in R and *attentively* read the help about the header argument). Since this was not the case, I manually set the column names with col.names. strip.white = TRUE automatically strips the whitespace within the columns, so your date is '1973/08/17' and not ' 1973/08/17'.

The structure of the data frame informs us that the date as been read as a factor. Since dates are their own Pandora boxes in computer science, we will not deal with them here, but you can look at section 2.4.4 if you're a masochist.

#### 2.6.2 Export

Exporting data is useful to save it for later use or send to a spreadsheet software. Despite some internationalization issues, I would recommend using csv for the output file, since it is easy to import into spreadsheet software. In that simple case, the write.csv function works quite well:

```
> demo
[,1] [,2] [,3] [,4] [,5]
[1,] 82.94 115.94 89.48 101.06 91.23
[2,] 111.22 117.65 94.64 115.79 103.91
[3,] 82.10 95.96 101.11 82.44 98.84
> write.csv(demo, file='path.../demo.csv', row.names=FALSE)
```

With data frames, the column headers will make sense and, should your object have row names, you can remove the row.names argument.

#### 2.6.3 Tidy

This section is quite heavy on R programmy-like stuff, so you may want to skip it until you are more familiar with R or actually need to disentangle a data set, whichever comes first.

Since their help pages are, in my opinion, easier to understand, I use the functions in the tidyr package, so you might want to install and load it to follow along.

#### $n \rightarrow 1 \text{ rows: spread}$

When the data is placed in a table where the name of a variable is used as a value in cells, you need to make them into columns. In other words, your table has a column of *keys* followed by a column of *values*. You can do so with the spread function, the result of which is represented in figure 2.7.

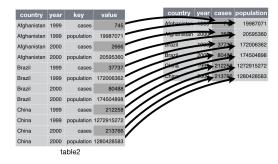


Figure 2.7: Putting variables in their own columns with spread (taken from [4]).

#### 1 ->n rows: gather

When the data is placed in a table where the column headers are values of a variable, you need to put them into one column, as shown in figure 2.8. You can do so with the gather function.

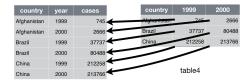


Figure 2.8: Putting a variable into only one column with gather (taken from [4]).

#### 1 ->n columns: separate

If one of the columns contain more than one variable, for example it is a rate written as cases/population, since number of cases and population are two separate variables, you will need to split this column into several others. You can use the separate function for this, as shown in figure 2.9.

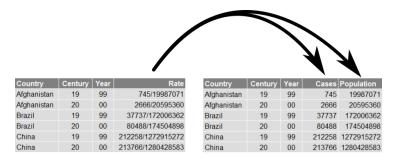


Figure 2.9: Separate one column into two with separate (inspired by [4]).

#### n ->1 columns: unite

If one variable is spread across multiple columns, for example a date split in year, month and day, while the date is a single variable, you will need to combine them into a single column. This can be done with the unite function, as pictured in figure 2.10.

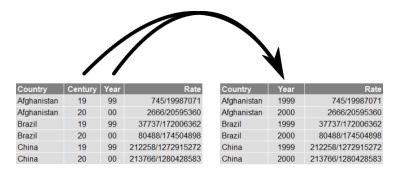


Figure 2.10: Merge two columns into one with unite (inspired by from [4]).

#### Example

The cancer data mentioned as an example in section 1.3.1 will be used as a case study for these functions. Data can most easily be copy-pasted into a Spreadsheet software from Table 1 of the peer-reviewed article version of the report online [14]. As a first step, remove sum lines and columns, remove the thousand separator and tweak header names (also, the hyphen is not a real hyphen, so retype it).

Let's identify the variables: cancer type, sex of patient, number of cases, and number of deaths. Here, we need to make sex its own column; and since there are two columns with female data, we will proceed in several steps: first, make all four columns one "variable" with gather. Arguments key and value are simply the name to give to the new columns that gather will create. The last argument is the columns to "gather", while the columns not listed will be duplicated as necessary.

```
> cancer = read.csv('C:/.../r-tutorial/cancer.csv')
> str(cancer)
'data.frame':
                47 obs. of 5 variables:
$ cancer
               : Factor w/ 47 levels "Acute lymphocytic
    leukemia",...
$ cases_male
               : int
                      12490 7980 14250 2440 13480 16520 ...
 cases_female : int
                      4620 5600 3340 820 3810 9720 5040 ...
                      1750 1770 2480 1280 12850 6510 810 ...
$ deaths_male : int
$ deaths_female: int 760 880 750 360 3000 4290 640 23240 ...
 cancer = gather(cancer, key="tmpvar", value="n", 2:5)
> str(cancer)
'data.frame':
                188 obs. of 3 variables:
$ cancer: Factor w/ 47 levels "Acute lymphocytic leukemia",...
$ tmpvar: chr "cases_male" "cases_male" "cases_male" ...
              12490 7980 14250 2440 13480 16520 5430 49690 ...
$ n
> cancer
    cancer
                  tmpvar
                              n
              cases_male
                         12490
    Tongue
```

```
2
     Mouth
               cases_male
                             7980
#...
48
    Tongue
             cases female
                             4620
49
     Mouth
             cases_female
                             5600
#...
95
   Tongue
              deaths_male
                             1750
     Mouth
96
              deaths_male
                             1770
142 Tongue deaths female
                              760
143 Mouth deaths_female
                              880
#...
```

Now, we need to separate the two words in the "tmpvar" column into two columns with separate. Arguments should be self-explanatory.

```
> cancer = separate(cancer, col="tmpvar", into=c("category",
   "sex"), sep="_")
> cancer
cancer category
                    sex
                              n
     Tongue
                        male
                              12490
                cases
2
      Mouth
                cases
                        male
                                7980
#...
                                4620
48
     Tongue
                cases female
49
      Mouth
                cases female
                                5600
#...
95
     Tongue
               deaths
                        male
                                1750
96
      Mouth
               deaths
                        male
                                1770
#...
142
     Tongue
                                 760
               deaths female
143
      Mouth
               deaths female
                                 880
#...
```

Finally, we need to bring "cases" and "deaths" back as their own column with spread. The argument key is the name of the column containing the variable names that you want to make into their own column. The argument value is the name of the column whose values you want to show under the new columns to be created. Other columns will be arranged accordingly.

```
#...
37
                   5600
                           880
    Mouth female
38 Mouth male
                  7980
                          1770
                   4620
81 Tongue female
                           760
82 Tongue
            {\tt male}
                  12490
                           1750
#...
```

Finally, let's correctly specify that "sex" is a **qualitative variable** rather than just text.

```
> cancer$sex = as.factor(cancer$sex)
> str(cancer)
'data.frame': 94 obs. of 4 variables:
$ cancer: Factor w/ 47 levels "Acute lymphocytic leukemia",....
$ sex : Factor w/ 2 levels "female", "male": 1 2 1 2 1 2 1 2 1 2 ...
$ cases : int 2670 3290 9140 10380 5620 2960 1510 1940 10160 ...
$ deaths: int 640 830 4490 6180 680 480 660 930 7340 9490 ...
```

There we go! Tidy data set!

# Chapter 3

# Data presentation

# 3.1 Frequency table (1D) or contingency table (2D)

For qualitative, discrete and continuous variables

If you feel the need to make a table with your data, use a spreadsheet software. ;) R is superior in statistics and (arguably) in figures, but spreadsheets definitely have their uses when it comes to tables.

#### 3.2 Pie chart

For qualitative and discrete variables, max 2 values

A pie chart is a graph that can be used to visually represent proportions of a **qualitative variable** or **discrete variable**. Note that they have their critics, who recommend never using them, as our brain is bad at comparing the size of slices [10].

As an example data set, let's use ebola deaths by country [9]. An excerpt giving the source data is shown in figure 3.1. Enter the data in your favorite spreadsheet software and save it as a csv. You should get the following:

Country, Deaths Guinea, 2543 Liberia, 4809 Sierra Leone, 3956 Mali, 6 Nigeria, 8 United States of America, 1

Go ahead and load your small csv into R with read.csv. You can then use the function pie to produce a pie chart. However, as shown below, a naive approach might disappoint.

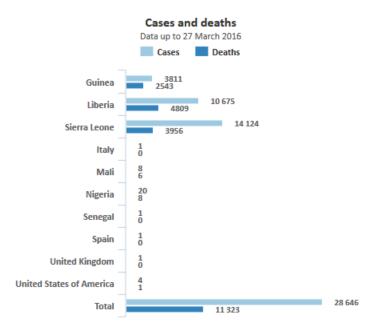


Figure 3.1: Excerpt from [9].

```
> ebola = read.csv('C:/.../r-tutorial/ebola.csv', header=TRUE)
> ebola
                   Country Deaths
1
                     Guinea
                              2543
2
                   Liberia
                              4809
3
              Sierra Leone
                              3956
4
                                 6
                       Mali
5
                   Nigeria
                                 8
6 United States of America
                                 1
> pie(ebola)
Error in pie(ebola) : 'x' values must be positive.
```

You might be scratching your head and wondering which part of 2543 or 6 is not positive, and you'd be justified to do so. Here, one must dive into computer programming concerns to understand what is going on. The "not positive" message hints at a problem with the format or the type of the input data (see section 2.2). Let's demonstrate:

```
> class(values)
[1] "numeric"
> class(labels)
[1] "character"
> class(ebola)
[1] "data.frame"
> class(ebola$Country)
[1] "factor"
> class(ebola$Deaths)
[1] "integer"
> pie(ebola$Deaths, labels=ebola$Country) # works too now!
```

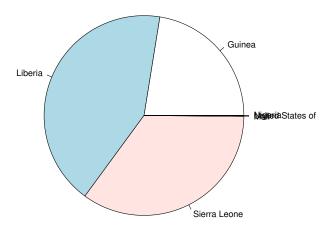


Figure 3.2: Ebola deaths in 2015-2016 by country.

Technically, read.csv returns a data.frame, while pie only accepts numbers. Accessing the columns of the data frame (see section 2.3) to feed pie the right types of arguments allows it to produce the expected figure.

Now that we have our basic pie chart, you might be thinking, "That squiggle on the right with the tiny pie slices is quite unseemly". In addition, you might want to tweak other aspects of the graph, like adding a title or choosing colors. We will discuss common graph properties in a following section, to keep it all

in the same place. As a note, all options are always listed in the function's help page.

Let's just deal with the pie-chart specific problem of small slices here (I reiterate, you should run away, run away into the arms of a bar chart.), and add a percent annotation, as that is a common occurrence. R does not offer an option to deal with small slices out of the box (probably because it tells you in its own manual to use bar charts instead), so let's just manually tweak the labels:

```
> labels = as.character(ebola$Country)
> labels[4]='Others'
> labels[5:6]=''
> labels
[1] "Guinea"
                                  "Sierra Leone" "Others"
                   "Liberia"
   0.00
[6] ""
> percents = ebola$Deaths/sum(ebola$Deaths)*100
> percents
[1] 22.458712355 42.471076570 34.937737349 0.052989490
→ 0.070652654
[6] 0.008831582
> percents[4] = sum(percents[4:6])
> percents
[1] 22.458712355 42.471076570 34.937737349 0.132473726
→ 0.070652654
[6] 0.008831582
> percents = round(percents, 2)
> percents
[1] 22.46 42.47 34.94 0.13 0.07 0.01
> labels[1:4] = paste(labels[1:4], percents[1:4], '%')
> labels
[1] "Guinea 22.46 %"
                           "Liberia 42.47 %"
                                                  "Sierra Leone

→ 34.94 %"

[4] "Others 0.13 %"
> pie(ebola$Deaths, labels)
```

Hacky, but it works, and no more time should be dedicated to pie charts, so let's move on.

#### 3.3 Bar chart

#### For qualitative and discrete variables

A bar chart, sometimes called a line graph, is used to represent a **qualitative** variable or a **discrete variable**, and the bars *do not touch*. As an example, data on infant mortality by country can be found at Gapminder [6]. The import process is detailed in section 2.6.1.

A barplot is relatively straightforward to produce with R, but we will see all "common" (imho) plot options here, so tie your winter hat down with wire, you'll be sitting here a while. Let's start by simply plotting infant mortality rate by country. To keep the plot readable, let's choose a subset of G8 countries: Canada, France, Germany, Italy, Japan, Russia, United Kingdom and United States of America. Let's also start by studying the mortality rate in 2000. First, we will select each of the countries by its row number, then we will stitch the G8 back together with a function called rbind, which binds data frames together by row, as long as all data frames have the same columns.

Producing a barplot now is easy:

```
> barplot(g8$X2000, names.arg=g8$Country)
```

Several things are wrong with this graph. Glaringly, a bar should not extend beyond its axis. Axes are set as plot options with xlim and ylim. Also, should you want a box around the graph, bty takes care of that. Usually. Bar plots are special and you need to all an extra function after your plot appears. See all graph options with ?par, which we will use a lot more as we customize our graphs.

You probably also want all country names to show up. Easiest way to do that is to tilt the axis label text. Here we will learn about par, used before your graph function to specify general plotting settings. For this next iteration, let's do a few things at once. First, let's make all labels perpendicular to their axis with par and las. Let's also demonstrate color manipulation by making each country's bar the dominant color on their flag (I may have made some arbitrary choices) with col.

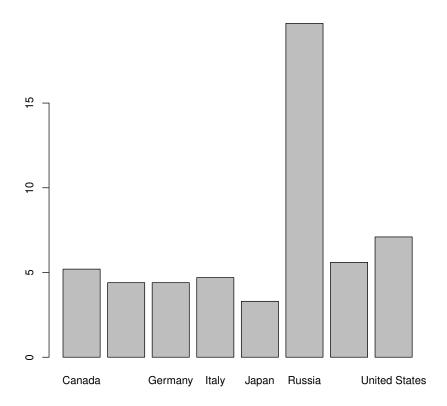


Figure 3.3: Simplest bar plot: infant mortality rate per country.

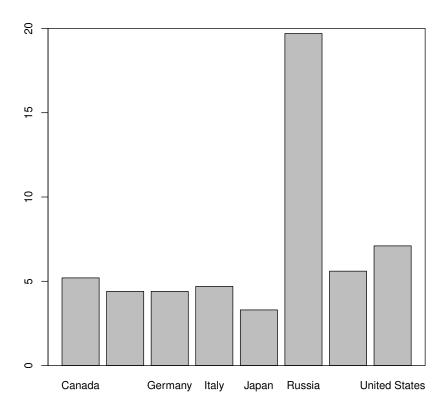


Figure 3.4: Simple bar plot: infant mortality rate per country, axis set.

#### Colors in R

Colors in R can be specified by their names, if they are among R's list of predefined colors, which you can see by calling colors().

A more visually helpful version can be found at Color Chart [3] which, incidentally, has other fascinating references about the use of color in science (good vs. bad color ramps, color blindness, etc).

Additionally, colors can be specified in other formats like #RRGGBB. These values can be found with graphics software or off a color generator on the internet.

Finally, if color space is a concern, additional functions exist: rgb, hsv, hcl, gray and rainbow.

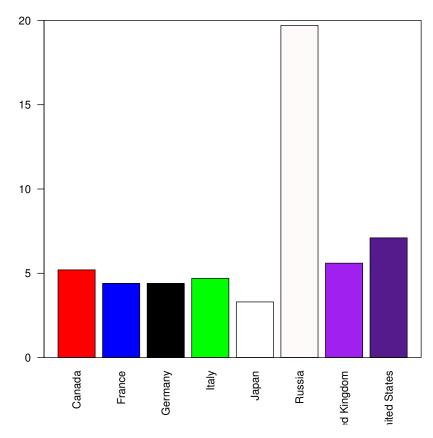


Figure 3.5: Psychedelic bar plot: infant mortality rate per country, axis set, labels perpendicular, colors.

With the country names printed at the vertical, they are running out of space at the bottom of the graph. More margin is needed there. Figures have two types of margins in R: outer and inner. The inner margin is used to draw the figure title and the axis ticks and labels and can be set in inches with mai=c(bottom, left, top, right) or in lines with mar=c(bottom, left, top, right). The outer margin is outside the figure; it makes more sense when several plots are displayed together, as we will do a few exercises down the line. The outer margin as well can be set in inches with omi=c(bottom, left, top, right) or in lines with oma=c(bottom, left, top, right). As for the appropriate margin necessary to display the full country name, that's a matter of trial and error. Starting with the current parameters' value of inner margin, I found that a value of 8 worked well.

Now, bar charts often use stacked bars. For example, let's use cancer rates [16]. This data includes number of cases and number of deaths by sex and cancer type. If the thing you would most like to compare is the number of cancer by type, you would stack the sexes into one bar. Let's use the tidy version of the data set produced in section 2.6.3.

```
> str(cancer)
'data.frame': 94 obs. of 4 variables:
$ cancer: Factor w/ 47 levels "Acute lymphocytic leukemia",....
$ sex : Factor w/ 2 levels "female", "male": 1 2 1 2 1 2 1 2 1 2 ...
$ cases : int  2670 3290 9140 10380 5620 2960 1510 1940 10160 ...
$ deaths: int  640 830 4490 6180 680 480 660 930 7340 9490 ...
```

The help page of barplot tells you that the first argument can be either a vector or matrix. If height is a vector, for example the single column cancer\$deaths, then the barplot shows what one would expect. If height is a matrix, then each *column* must be either the values to stack (beside=FALSE) or the values for a group of bars (beside=TRUE). To visualize, let's plot data for five short-named cancers in the list. And since this is a perfect occasion, let's learn about a few more figure options: the legend argument and how to plot several figures into one plot window.

```
> subset=rbind(cancer[11:12,], cancer[17:18,], cancer[35:36,],
    cancer[63:64,], cancer[79:80,])
> subset = subset[, 1:3]
> subset
     cancer
               sex cases deaths
     Breast female 266120
                           40920
11
12
     Breast
              male
                     2550
                              480
17
      Colon female
                   47530
                           23240
18
      Colon
              male
                   49690
                           27390
35 Melanoma female
                   36120
                             3330
36 Melanoma
                    55150
              male
                             5990
63
   Pharynx female
                     3340
                             750
64
   Pharynx
              male
                    14250
                             2480
   Thyroid female
                    40900
                             1100
79
    Thyroid
              male
                    13090
                             960
> fordemo = spread(subset[, 1:3], cancer, cases) # let's just use
    cases for now
```

```
> fordemo
sex Breast Colon Melanoma Pharynx Thyroid
1 female 266120 47530
           2550 49690
                         55150
                                  14250
                                          13090
 # each column of the matrix is one cancer to stack or group
> str(fordemo)
'data.frame':
                2 obs. of 6 variables:
          : Factor w/ 2 levels "female", "male": 1 2
$ sex
          : int 266120 2550
$ Breast
$ Colon
         : int 47530 49690
$ Melanoma: int 36120 55150
$ Pharynx : int
                3340 14250
$ Thyroid : int 40900 13090
> # but you want an actual matrix, not a data frame
> # with row and column names
> # and cells containing numbers only
> fordemo = as.matrix(fordemo[,2:6])
> fordemo
Breast Colon Melanoma Pharynx Thyroid
[1,] 266120 47530
                     36120
                              3340
                                      40900
       2550 49690
                     55150
                             14250
                                      13090
> rownames(fordemo) = c("female", "male")
> fordemo
       Breast Colon Melanoma Pharynx Thyroid
female 266120 47530
                       36120
                                3340
                                        40900
male
         2550 49690
                       55150
                               14250
                                        13090
```

At this point, your data is ready in the shape that barplot wants it: it's a matrix with each column representing a stack or group. It's also in the shape you want it because the row and column names are readable. Now, let's use mfrow to plot the results of beside=TRUE and beside=FALSE side by side, as seen in figure 3.6.

```
> par(mfrow=c(1,2)) # 1 row, 2 columns, fill by row
> # par(mfcol=c(1,2)) # 1 row, 2 columns, fill by column
> # a plot window opens, ready with 1x2 plot regions
> barplot(fordemo, beside=FALSE, legend=TRUE, main="Parameter

    beside=FALSE")
> # first plot appears on the left
> barplot(fordemo, beside=TRUE, legend=TRUE, main="Parameter

    beside=TRUE")
> # second plot appears on the right
```

Note that setting the legend argument automatically produces a human-readable result from the row names of the "fordemo" matrix.

Now, if you want to stack sexes and group cases and deaths per cancer, this is where barplot would fail you and you would have to resort to a package, for

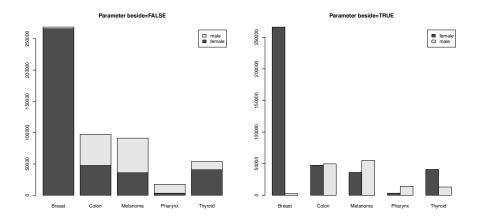


Figure 3.6: Comparing the effect of the beside parameter for a matrix fed to barplot, using mfrow.

example ggplot2. According to discussions in the R mailing lists, the basic bar plot function does not support this option because the developers felt it was too much information to fit on one figure, so keep that in mind and ask yourself whether it's a good idea. However, as shown by the pie chart section, I'm not here to judge, so here's a way to do that.

ggplot2 is so ubiquitously used to produce peer-review quality graphics in R, while being so different from the basic graphics we have used so far that it warrants a bit of an introduction.

ggplot2 works by sequentially adding *layers* from a *data frame*. So first, you say, "I want to make a new ggplot". An empty graphics window opens. Then you say, "I want to add points to this blank canvas". Then you can say, "I want to add a line in addition to the points already there", and then "I also want a main title", and so on. So you will add new function calls separated by a plus sign.

With our cancer study case, our situation is that we want to stack sexes, as well as group cases and deaths (which we will call effect) per cancer. You need each of these in their own column, and you need a data frame since that's what ggplot uses. Our data must be transformed this way:

```
> forgg = gather(subset, "effect", "n", 3:4)
> forgg
cancer
          sex effect
                            n
1
     Breast female
                     cases 266120
2
     Breast
              male
                              2550
                     cases
3
      Colon female
                     cases
                             47530
      Colon
                             49690
4
               male
                     cases
5
   Melanoma female
                     cases
                             36120
   Melanoma
               male
                     cases
                             55150
```

```
7
    Pharynx female
                              3340
                     cases
8
    Pharynx
               male
                             14250
                     cases
9
    Thyroid female
                             40900
                     cases
10
    Thyroid
               male
                     cases
                             13090
11
     Breast female deaths
                             40920
     Breast
               male deaths
                               480
12
13
      Colon female deaths
                            23240
      Colon
              male deaths
14
                             27390
15 Melanoma female deaths
                              3330
16 Melanoma
              male deaths
                              5990
17
    Pharynx female deaths
                              750
18
    Pharynx
               male deaths
                              2480
19
    Thyroid female deaths
                              1100
20
   Thyroid
               male deaths
                               960
```

As for the plotting part of the work, ggplot loves to use scientific notation, so we'll turn that off. ggplot comes with several "themes", which control a series of layout options like background color, presence of grids, etc. We'll use the classic theme since it looks most like the basic graphics package we have been using.

```
options(scipen=999)
theme_set(theme_classic())
```

ggplot's first argument is the source data frame. Then, you will need to specify what it calls an *aesthetic*: what do you want to show in x and y? We want our variable "n" to be shown as y, and we want "effect" and "cancer" on x.

This leads me to talk of *facets* and *formulas*. Facets are a ggplot2 thing, while formulas are used throughout R. So basically, we want to divide our graph into several smaller graphs, one for each type of cancer, and show them side by side. So each "subgraph" is a facet. Therefore, we will use "cancer" in the facet function, and it leaves "effect" as the x in the ggplot's aesthetic.

As for formulas, they define a more "talkative" way for you to specify which relationship you want R to study for you. The most basic form is  $y \sim x$ , which reads "y as a function of x". More elaborate forms include  $y + z \sim x$ , which is "y and z as a function of x" (note, the plus sign means "and", not a literal addition), and  $y \sim x \mid a$ , which is "y as a function of x, per value of a".

With this preliminary knowledge, we are ready to look at the code, which produces figure 3.7.

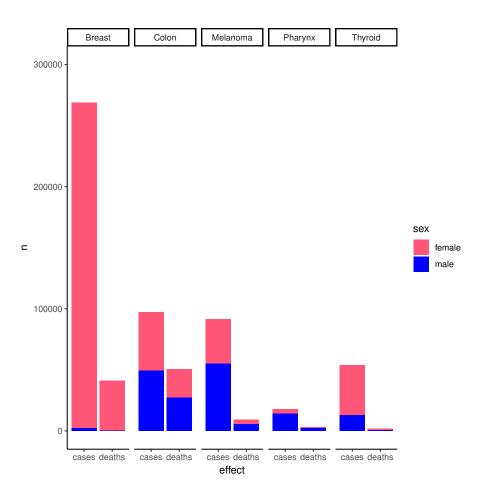


Figure 3.7: Number of cases and deaths by sex for five cancers, with the help of ggplot.

Your options of types of plots include: geom\_point for points, geom\_col for bars showing heights, geom\_bar for bars showing counts.

You can control color and size of points, as well as fill of bars, by setting the appropriate options in the aesthetic, for example:

```
geom_point(aes(size=population, col=state))
geom_col(aes(fill=sex))
```

As you may have noted when we made our figure, the legend appears automatically, with the colors and sizes (if relevant) used.

You can use facet\_wrap to make your "subgraphs" follow one after the other, or facet\_grid to have them form a grid, for instance, see the code below, which produces figure 3.8. As for layout options regarding colors, titles, annotations, etc, they are so numerous that I can't detail them here. Digging into the help pages and asking the internet how to do things is the way to go.

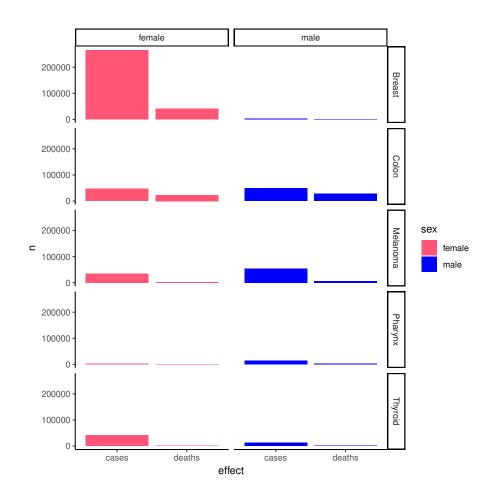


Figure 3.8: Grid presentation of number of cases and deaths per cancer per sex.

#### 3.4 Histogram

#### For continuous variables

A histogram is a representation of a **continuous variable**, and *the bars touch*. It is used to visually present the shape of the distribution by compiling counts for "bins", ranges of values. Bins are typically, but not necessarily, of equal width.

For our example, let's use traffic data in the city of Chicago, with the import process described in section 2.4.4. A simple call to hist, will produce the figure 3.9.

```
> str(traffic)
'data.frame':
                1279 obs. of 9 variables:
           : Factor w/ 1279 levels "1", "1,000", "1,001",...
          : Factor w/ 1203 levels "1 West", "10 East", ...: 212 ...
           : Factor w/ 251 levels "100th St", "101st St",...
$ Date
           : Date, format: "2006-03-09" "2006-02-28" ...
           : int 14600 16500 18200 21600 18300 8600 10000 ...
$ Volume
$ Direction: Factor w/ 1223 levels "East Bound: 1000 ..." ...
$ Latitude : num 41.8 41.8 41.8 41.8 41.8 ...
$ Longitude: num -87.7 -87.7 -87.6 -87.6 -87.6 ...
$ Location : Factor w/ 1276 levels "(41.651861, -87.54501)",...
> hist(traffic$Volume, xlab="Car volume", ylab="Count", main="",
   ylim=c(0, 600))
> box()
```

You will note that we fed hist the list of car volumes, and the function automatically computed the bins and counted how many observations were in each bin before plotting the resulting histogram.

There are several ways to compute bins for histograms, but the most used is the Sturges method, used by default in R, which outputs more bins the greater the range of the data (more or less) [5].

As you may have noted, there are several outliers at the right of the graph, with such small numbers that their bar is barely visible. I don't necessarily recommend this course of action, since you change the representativity of your figure, but you could decide to group together the small bins at the end so they are visible. Let's say you wanted to group together the bins at the right with five or less observations. Here, let's point out a neat feature of R. In order to produce a plot, hist must compute bins, counts, etc., and it actually gives you access to them if you save the output of hist. You can then make use those to produce your personalized histogram, producing figure 3.10.

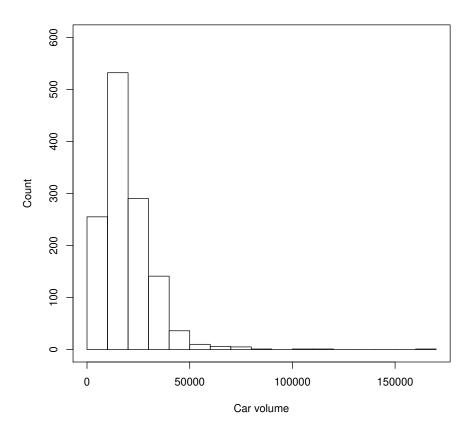


Figure 3.9: Histogram of car volumes in the city of Chicago.

[9] 80000 90000 100000 110000 120000 130000 140000 150000 [17] 160000 170000

#### \$counts

[1] 255 532 290 141 36 10 6 5 1 0 1 1 0 0 [15] 0 0 1

#### \$density

- [1] 0.00001993745113 0.00004159499609 0.00002267396403
- [4] 0.00001102423769 0.00000281469898 0.00000078186083
- [7] 0.00000046911650 0.00000039093041 0.00000007818608
- [10] 0.0000000000000 0.00000007818608 0.00000007818608

```
[16] 0.0000000000000 0.0000007818608
$mids
[1]
      5000 15000 25000 35000 45000 55000 65000 75000
           95000 105000 115000 125000 135000 145000 155000
[17] 165000
$xname
[1] "traffic$Volume"
$equidist
[1] TRUE
attr(,"class")
[1] "histogram"
> h$breaks
[1]
         \cap
           10000 20000 30000 40000 50000 60000 70000
[9]
    80000 90000 100000 110000 120000 130000 140000 150000
[17] 160000 170000
> h$counts
[1] 255 532 290 141 36 10
                             6
                                 5
                                         \cap
                                             1
                                                         0
> mybreaks = c(h$breaks[1:7], 170000)
> mybreaks
[1]
         0 10000 20000 30000 40000 50000 60000 170000
> h2 = hist(traffic$Volume, breaks=mybreaks, xlab="Car volume",
   main="")
> h2
$`breaks
[1]
                        30000
                                40000 50000 60000 170000
          10000 20000
$counts
[1] 255 532 290 141 36 10 15
```

This figure has density as its y axis, meaning that the area (width\*height) of all the bars sum to 1. This is the default behavior when using bins of different sizes. Note that your last bin, [60000, 170000[, contains 15 observations, more than the previous bin, while appearing lower in the figure; this is due to the density calculations. The area of the bar is representative of its data, not the height.

#### 3.5 Scatter graph

For continuous variables

This figure is used to illustrate the relationship between two **continuous** variables. As an incendiary correlation-is-not-causation example, let's use the

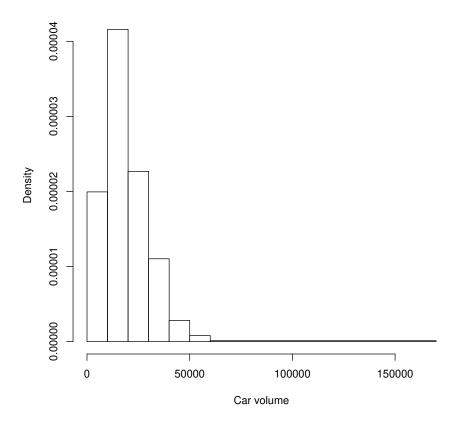


Figure 3.10: Density histogram of car volumes in the city of Chicago.

National Health Interview Survey data to study the relationship between diabetes and body mass index [8]. The Sample Adult file has the information we'll use. The Variable summary file will inform you that the column labels that interest you are DIBEV1 (diagnosis of diabetes), DIBTYPE (diabetes type) and BMI (body mass index). The variable layout will inform you of the meaning of the values in the file.

#### For diabetes diagnosis:

- 1 Yes
- 2 No
- 3 Borderline or prediabetes
- 7 Refused
- 8 Not ascertained
- 9 Don''t know

```
Type of diabetes

1 Type 1
2 Type 2
3 Other
7 Refused
8 Not ascertained
9 Don''t know
```

And BMI is the number you'd expect multiplied by 100.

For once, simply loading the csv into R gives the expected results. I will spare you the sanity check on import integrity, given the number of variables in the file. Let's just remove all the columns we're not interested with at the moment, divide BMI, and correctly create factors from the integer codes for the other two. Then let's take a quick look at sample data:

```
> nhis=read.csv("C:/.../r-tutorial/samadult.csv")
> nhis$BMI = nhis$BMI/100
> nhis = as.data.frame(cbind(nhis$BMI, nhis$DIBTYPE,
    nhis$DIBEV1))
> colnames(nhis)=c("BMI", "Type", "Diagnosis")
> nhis$Type = factor(nhis$Type,
   levels=c(1, 2, 3, 7, 8, 9),
   labels=c("Type I", "Type II", "Other", "Refused", "Not
  Ascertained", "Don't know"))
> nhis$Diagnosis = factor(nhis$Diagnosis,
  levels=c(1, 2, 3, 7, 8, 9),
  labels=c("Yes", "No", "Borderline or prediabetes", "Refused",
   "Not Ascertained", "Don't know"))
> str(nhis)
'data.frame':
                26742 obs. of 3 variables:
$ BMI
          : num 29.3 23.1 35.4 43.1 32.3 ...
           : Factor w/ 6 levels "Type I", "Type II", ...: NA NA NA
$ Type
\hookrightarrow NA NA NA NA 2 1 NA ...
$ Diagnosis: Factor w/ 6 levels "Yes", "No", "Borderline or
→ prediabetes",..: 2 2 2 2 2 2 1 1 2 ...
> nhis[1:20,]
     BMI
            Type Diagnosis
  29.30
            <NA>
2 23.09
                        No
            <NA>
  35.44
            <NA>
                        No
4 43.13
            <NA>
                        No
5 32.27
            <NA>
                        No
6 23.25
            <NA>
                        No
   24.67
            <NA>
                        No
8 41.97 Type II
                       Yes
9 33.51 Type I
                       Yes
10 26.62
            <NA>
                        No
```

```
11 22.61
             <NA>
                           No
12 28.72
             <NA>
                           No
13 28.17
             <NA>
                           No
14 27.83
             <NA>
                           No
15 36.58 Type II
                          Yes
16 21.81
             <NA>
                           No
17 27.41
             <NA>
                          No
18 27.80
            Other
                         Yes
19 27.36
                          Yes
            Other
20 20.81
             <NA>
                           No
```

Now, to simplify our analysis and our figure, let's just concern ourselves with the diagnosis values of yes or no and diabetes types 1 or 2. To do this, I will use the filter function. Since R has two filter functions, one in the stats and the other in the dplyr package, I will manually specify which one I want. filter works by giving it some data, then specifying a condition, and it returns the rows where the condition is verified.

In our case, we want all the cases where the diagnosis is "No" (in that case, diabetes type is NA). We also want rows where diagnosis is "Yes", but only if their value of type is I or II. Verbally, it is:

Note that the parenthesis are important, even though it would not appear to make a difference with our data. Instead, to demonstrate, let's consider this table:

| Name     | Sex    | Eyes  |
|----------|--------|-------|
| Sarah    | Female | Green |
| James    | Male   | Blue  |
| Nicholas | Male   | Brown |

Now, let's compare the following parentheses placement:

This kind of statement is called boolean algebra, and it definitely needs some getting used to. Moreover, in R, when using "=" to mean a comparison rather than the assignment of a value to a variable, you must actually type "==". I means "or" and & means "and". This leads to the following code:

| I Ty  | ype   | Diagnosis  |       |
|-------|---|--|-------|
| 29.30 |   | <NA $>$  | No    |
| 23.09 |   | <NA $>$  | No    |
| 35.44 |   | <NA $>$  | No    |
| 43.13 |   | <NA $>$  | No    |
| 32.27 |   | <NA $>$  | No    |
| 23.25 |   | <NA $>$  | No    |
| 24.67 |   | <NA $>$  | No    |
| 41.97 | Тур   | pe II  | Yes   |
| 33.51 | Ty  | ype I  | Yes   |
| 26.62 |   | <NA $>$  | No    |
| 22.61 |   | <NA $>$  | No    |
| 28.72 |   | <NA $>$  | No    |
| 28.17 |   | <NA $>$  | No    |
| 27.83 |   | <NA $>$  | No    |
| 36.58 | Тур   | pe II  | Yes   |
| 21.81 |   | <NA $>$  | No    |
| 27.41 |   | <NA $>$  | No    |
| 20.81 |   | <na></na>  | No    |
| 23.72 |   | <NA $>$  | No    |
| 22.33 |   | <na></na>  | No    |
|       | 29.30<br>23.09<br>35.44<br>43.13<br>32.27<br>23.25<br>24.67<br>41.97<br>33.51<br>26.62<br>22.61<br>28.72<br>28.17<br>27.83<br>36.58<br>21.81<br>27.41<br>20.81<br>23.72 | 29.30<br>23.09<br>35.44<br>43.13<br>32.27<br>23.25<br>24.67<br>41.97 Typ<br>33.51 Ty<br>26.62<br>22.61<br>28.72<br>28.17<br>27.83<br>36.58 Typ<br>21.81<br>27.41<br>20.81<br>23.72 | 29.30 |

#### 3.6 Box and whiskers graph

# Data description

- 4.1 Center tendency measurements
- 4.1.1 Mean
- 4.1.2 Median
- 4.1.3 Mode
- 4.2 Dispersion measurements
- 4.2.1 Range
- 4.2.2 Variance
- 4.2.3 Standard deviation
- 4.2.4 Coefficient of variation
- 4.2.5 Quartiles and percentiles
- 4.3 Shape measurements
- 4.3.1 Skewness
- 4.3.2 Kurtosis
- 4.3.3 L-moments

## **Probabilities**

- 5.1 Factorial
- 5.2 Combinations
- 5.3 Permutations
- 5.4 Probability Mass/Density Function

### **Statistics**

- 6.1 Binomial distribution
- 6.2 Multinomial distribution
- 6.3 Poisson distribution
- 6.4 Inverse binomial distribution
- 6.5 Hypergeometric distribution
- 6.6 Normal distribution
- 6.7 Exponential distribution
- 6.8 Gamma distribution
- 6.9 c2 distribution
- 6.10 Fisher-Snedecor distribution
- 6.11 Student's law

#### Inferential statistics

- 7.1 Student's test
- 7.2 Student's paired test
- 7.3 Bartlett's test
- 7.4 Single-factor ANOVA
- 7.5 c2 test
- 7.6 Wilcoxon-Mann-Whitney test
- 7.7 Kolmogorov-Smirnov test
- 7.8 Kruskal-Wallis test
- 7.9 Pearson's test
- 7.10 Spearman's test
- 7.11 Kendall's test
- 7.12 Simple linear regression
- 7.13 Multiple linear regression

# Programming

- 8.1 Sequence, iteration, branching
- 8.1.1 Iteration
- 8.1.2 Branching
- 8.2 Functions
- 8.3 Misc

### Cheat sheet

#### 9.1 Plumbing

? ?exact\_function\_name ?? ??keyword class class(R\_variable) str(R\_variable)  $\operatorname{str}$  $colnames(R_variable)$ colnames as.integer as.integer(R\_variable) rbindrbind(var, var...) cbind cbind(var, var...)

#### 9.2 Data import and export

```
read.csv read.csv('delimited_data.csv', header=TRUE, sep=",", dec=":")
read.fwf read.fwf('fixed_width_data.txt', widths=c(10, 5, 4), header=FALSE, skip=2, strip.white=TRUE, of write.csv (R_variable, file='desired_file_name.csv', row.names=FALSE, append=FALSE)
```

## Bibliography

- [1] Average Daily Traffic Counts | City of Chicago | Data Portal. URL: https://data.cityofchicago.org/Transportation/Average-Daily-Traffic-Counts/pfsx-4n4m (visited on 09/26/2018).
- [2] Calendar date. en. Page Version ID: 856764544. Aug. 2018. URL: https://en.wikipedia.org/w/index.php?title=Calendar\_date&oldid=856764544 (visited on 09/27/2018).
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## Glossary

- continuous variable A variable that refers to continuous data, i.e. that can take on an infinite number of values (ex. height in mm), as opposed to categorical data (ex. color of eyes). 5, 42, 44
- **dependent variable** The "explained" variable in a relationship, the one we try to understand as a consequence of another factor. For example, when studying the effect of smoking on lung cancer, lung cancer is the dependent variable.. 5
- discrete variable A variable that refers to categorical data (ex. color of eyes), as opposed to continuous data (ex. height in mm). 5, 28, 31
- independent variable The "explaining" variable in a relationship, the one that drives a phenomena. For example, when trying to understand the causes of diabetes, body mass index would be an independent variable.. 5
- **ordinal variable** A qualitative variable where the values can be ordered (ex. small, medium, large). 5, 10
- qualitative variable A variable that is recorded with words rather than numbers (ex. color of eyes, state of mind). 4, 5, 10, 27, 28, 31
- **quantitative variable** A variable that is measured with numbers (ex. number of cases, height in mm). 4, 5