

NOTE ON DUCROS' BOOK — CHAPTER 4

MINGCHEN XIA

CONTENTS

1. Introduction	1
2. Notes	1
References	3

1. INTRODUCTION

These are a series of notes on the book [\[DucCurve\]](#) [\[Duc24\]](#).

2. NOTES

Let k be a non-Archimedean analytic field. Consider a k -analytic curve X .

Unlike Ducros' book, we assume that X is good.¹

4.1.1. Line 17, $\mathbb{P}_k^{1,\text{an}}$ should be \mathbb{P}_k^1 .

4.2.1. Line 4, $\varphi^{-1}(\varphi((x)))$ should be $\varphi^{-1}(\varphi(x))$.

4.2.3. Line 5, φ should be f .

4.2.4.1. Line 6, $= 0$ should be removed.

Line 8, X' should be X_0 .

4.2.5.1. The existence of function mentioned in the first paragraph is constructed in 3.5.9.

4.2.9. Line 3, $\mathbb{P}_{\mathcal{H}(x)}$ should be $\mathbb{P}_{\mathcal{H}(x)/k}$.

4.2.16.

4.2.16.1. Line 5, the second y should be x .

Line 5, U est une composante connexe de $\varphi^{-1}(x)$ should be V est une composante connexe de $\varphi^{-1}(U)$.

4.2.16.2. Line 26, $\varphi^{-1}U$ should be $\varphi^{-1}(U)$.

4.3.4.1. Line 4, x_i should be x'_i .

4.3.5.2. Line 1, $3)$ should be $1)$.

4.3.6.4. Line 8, $|\mathcal{O}_X(Z)^\times|$ should be $|\mathcal{O}_X(Z)^\times|_b$.

4.3.9.1. Line 18, Y^{an} should be $S^{\text{an}}(Y)$.

Line 19, X^{an} should be $S^{\text{an}}(X)$.

4.3.11.1. Line 7, b should be y .

Line 8, a should be x .

Line 8, **le lemma** should be **la proposition**.

4.4.3.1. Line 8, U should be $X \setminus \{x\}$.

Line 9, U should be Z .

¹This is proved in Ducros' book based on Temkin's goodness criterion. I cannot understand the proof of the latter as explained in my note on graded reductions.

4.4.5. Line 4, $H^1(\kappa(x), \mu_\ell)$ should be $H^1(\kappa(x), \mu_\ell)$.

4.4.5.3. Line 2, $H^1(X, x)_{\text{ét}}, \mu_\ell$ should be $H^1((X, x)_{\text{ét}}, \mu_\ell)$.

4.4.8.3. Line 10, H^1 should be H^1 .

In the displayed formula, $T^\ell - f(x)$ should be $(T^\ell - f(x))$.

4.4.10.4. Line 5, remove the first sentence.

4.4.14. Line 3, Y should be X .

Line 9, the formula should be $H^1((X, x)_{\text{ét}}, \mu_\ell) \sim H^1(\mathcal{H}(x), \mu_\ell)$.

4.4.23. Line 6, t should be T .

4.5.4. Line 6, *coronaire* should be *une couronne virtuelle*.

4.5.12. Line 1, $p: X \rightarrow X_{\widehat{k^a}}$ should be $p: X_{\widehat{k^a}} \rightarrow X$.

The finiteness of the fiber over $x \in X_{[0,2,3]}$ is due to the fact that x is Abhyankar. See 3.2.15.4.

REFERENCES

- [Duc24] A. Ducros. La structure des courbes analytiques. 2024. arXiv: [2405.10619 \[math.AG\]](#).
Mingchen Xia, CHALMERS TEKNISKA HÖGSKOLA AND INSTITUTE OF GEOMETRY AND
PHYSICS, USTC
Email address, xiamingchen2008@gmail.com
Homepage, <https://mingchenxia.github.io/home/>.