

Predicting evolutionary site variability from structure in viral proteins: buriedness, flexibility, and design

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Abstract Several recent works have shown that protein structure can predict site-specific evolutionary sequence variation. In particular, sites that are buried and/or have many contacts with other sites in a structure have been shown to evolve more slowly than surface sites with few contacts. Here, we present a comprehensive study of the extent to which numerous structural properties can predict sequence variation. The structural properties we consider include buriedness (relative solvent accessibility and contact number), measures of structural fluctuations (B factors, root-mean-square fluctuations, and variation in dihedral angles), and variability in designed structures. We obtained structural fluctuation measures both from molecular dynamics simulations performed on 9 non-homologous viral protein structures and from variation in homologous variants of those proteins, where available. We obtained measures of variability in designed structures from flexible-backbone design in the Rosetta software. We found that most of the structural properties correlate with site variation in the majority of structures, though the correlations are generally weak (correlation coefficients of 0.1 to 0.4). Moreover, we found that measures of buriedness tend to be better predictors of evolutionary variation than are measures of structural fluctuations. Finally, variability in designed structures was a weaker predictor of evolutionary variability than were both buriedness and fluctuation measures. We conclude that simple measures of buriedness are better predictors of evolutionary variation than are more complicated predictors obtained from dynamic simulations, ensembles of homologous structures, or computational protein design.

Introduction

Patterns of sequence variation in protein-coding genes are shaped by biophysical structure and function of the expressed proteins (Wilke and Drummond, 2010; Marsh and Teichmann, 2014). As the most basic reflection of this relationship, buried residues in proteins tend to be more evolutionarily conserved than exposed residues (Overington et al, 1992; Goldman et al, 1998; Mirny and Shakhnovich, 1999; Dean et al, 2002). More specifically, when evolutionary variation is plotted as a function of Relative Solvent Accessibility (RSA, a measure of residue buriedness), the relationship falls, on average, onto a straight line with a positive slope (Franzosa and Xia, 2009; Ramsey et al, 2011; Franzosa and Xia, 2012; Scherrer et al, 2012). Importantly, however, this relationship represents an average over many sites and many proteins. At the level of individual sites in individual proteins, RSA is often only weakly correlated with evolutionary variation (Meyer and Wilke, 2013; Meyer et al, 2013; Yeh et al, 2014).

Measures of residue buriedness other than RSA, such as residue contact number (CN) have also been shown to correlate with sequence variability (Liao et al, 2005; Franzosa and Xia, 2009; Yeh et al, 2014), and some have argued that CN predicts evolutionary variation better than RSA (Yeh et al, 2014). Because CN may be a proxy of residue and site-specific backbone flexibility (Halle, 2002), a positive trend between local structural variability and sequence variability may also exist (Yeh et al, 2014). Indeed, several authors have suggested that such protein dynamics may play a role in sequence

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variability (Liu and Bahar, 2012; Nevin Gerek et al, 2013; Marsh and Teichmann, 2014). However, a recent paper argued against **the flexibility model (from SJS perspective, unclear what the flexibility model refers to)**, on the grounds that it could introduce certain non-linearities that are not observed in the data (Huang et al, 2014).

While RSA and CN can be calculated in a straightforward manner from individual crystal structures, measures of structural flexibility, either at the side-chain or the backbone level, are more difficult to obtain. Two strong candidates for measuring structural flexibility are examining existing structural data or simulating protein dynamics. First, NMR ensembles and/or PDB structures may approximate *in vivo* physiologically relevant structural fluctuations well. Indeed, the thermal motion of atoms in a crystal are recorded in B factors, which are available for every atom in every PDB structure. However, it is unclear how accurately B factors reflect structural fluctuations of a protein in solution. It is also possible to align homologous PDB protein structures and subsequently assess the extent of fluctuations. Other than using existing structural information, one could measure protein fluctuations using a simulation approach, either using coarse-grained modeling, e.g. via Elastic Network Models (Sanejouand, 2013), or using atom-level modeling, e.g. via molecular dynamics (MD) (Karplus and McCammon, 2002). Even so, it is not well understood which, if any, of these measures of structural fluctuations provide distinct insight into the evolutionary process, in particular site-specific variation evolutionary variation.

Here, we provide a comprehensive analysis of the extent to which numerous different structural quantities predict evolutionary sequence (amino-acid) variation.

We consider two measures of evolutionary sequence variation: site entropy, as calculated from homologous protein alignments, and evolutionary rate. For structural predictors, we include both measures of buriedness (RSA and CN) and measures of structural fluctuations. The fluctuation measures include B factors, several measures of backbone and side-chain variability obtained from MD simulations, and backbone variability obtained from alignments of homologous crystal structures. We also include site variability, as predicted from computational protein design with Rosetta. We consider site variability to be a structural property since it was derived in an explicit protein design context. On a set of nine viral proteins, we find that measures of buriedness generally perform better at predicting evolutionary site variation than do either measures of structural fluctuations or computational protein design. Among the measures of structural fluctuations, measures of side-chain variability perform better than do measures of backbone variability, possibly because the former are more tightly correlated with residue buriedness. Finally, site variability predicted from computational protein design performs worse than the best-performing measures of structural fluctuations.

Materials and Methods

Sequence data, alignments, and evolutionary rates

All viral sequences except influenza sequences were retrieved from <http://hfv.lanl.gov/components/sequence/HCV/search/searchi.html>. The sequences were truncated to the desired genomic region but not in any other way restricted. Influenza sequences were downloaded from <http://www.fludb.org/brc/home.spkg?decorator=influenza>. We only considered human influenza A, H1N1, excluding H1N1 sequences derived from the 2009 Swine Flu outbreak. We only used sequences from after 1998 but did not place any geographic restrictions.

For all viral sequences, we removed any sequence that was not in reading frame, any sequence which was shorter than 80% of the longest sequence for a given viral protein (so as to remove all partial sequences), and any sequence containing any ambiguous characters. Alignments were constructed using amino-acid sequences with MAFFT (Katoh et al, 2002, 2005), specifying the `--auto` flag to select the optimal algorithm for the given data set, and then back-translated to a codon alignment using the original nucleotide sequence data.

To assess site-specific sequence variability in amino-acid alignments, we calculated the Shannon entropy (H_i) at each alignment column i :

$$H_i = - \sum_j P_{ij} \ln P_{ij}, \quad (1)$$

where P_{ij} is relative frequency of amino acid j at position i in the alignment.

For each alignment, we also calculated evolutionary rates, as described (Spielman and Wilke, 2013). In brief, we generated a phylogeny for each codon alignment in RAxML (Stamatakis, 2006) using the

GTRGAMMA model. Using the codon alignment and phylogeny, we inferred evolutionary rates with a Random Effects Likelihood (REL) model, using the HyPhy software (Kosakovsky Pond et al, 2005). The REL model was a variant of the GY94 evolutionary model (Goldman and Yang, 1994) with five ω rate categories as free parameters. We employed an Empirical Bayes approach (Yang, 2000) to infer ω values for each position in the alignment. These ω values represent the evolutionary-rate ratio dN/dS at each site.

Protein crystal structures

A total of 9 viral protein structures were selected for analysis, as tabulated in Table 1. Sites in the PDB structures were mapped to sites in the viral sequence alignments via a custom-built python script that creates a consensus map between a PDB sequence and all sequences in an alignment.

For each of the viral proteins, homologous structures were identified using the `blast.pdb` function of the R package Bio3D (Grant et al, 2006). BLAST hits were retained if they had $\geq 35\%$ sequence identity and $\geq 90\%$ alignment length. Among the retained hits, we subsequently identified sets of homologous structures with unique sequences and with mutual pairwise sequence divergences of $\geq 2\%$, $\geq 5\%$, and $\geq 10\%$.

Measures of buriedness and of structural flexibility

As measures of residue buriedness, we calculated Relative Solvent Accessibility (RSA), contact number (CN), and weighted contact number (WCN). To calculate RSA, we first calculated the Accessible Surface Area (ASA) for each residue in each protein, using the DSSP software (Kabsch and Sander, 1983). We then normalized ASA values by the theoretical maximum ASA of each residue (Tien et al, 2013) to obtain RSA. We calculated CN for each residue as the total number of C α atoms surrounding the C α atom of the focal residue within a spherical neighborhood of a predefined radius r_0 . Following Yeh et al (2014), we used $r_0 = 13\text{\AA}$. We calculated WCN as the total number of surrounding C α atoms for each focal residue, weighted by the inverse square separation between the C α atoms of the focal residue and the contacting residue, respectively (Shih et al, 2012).

In most analyses, we actually used the inverse of CN and/or WCN, $iCN = 1/CN$ and $iWCN = 1/WCN$. Note that for Spearman correlations, which we use throughout here, replacing a variable by its inverse changes the sign of the correlation coefficient but not the magnitude.

As measures of structural variability, we considered RMSF, variability in backbone and side-chain dihedral angles, and B factors. We calculated RMSF for backbone C α atoms based on both MD trajectories and homologous structures. For MD trajectories, we calculated RMSF as

$$\text{RMSF}_j = \left[\sum_i (\mathbf{r}_i^{(j)} - \mathbf{r}_0^{(j)})^2 \right]^{1/2} \quad (2)$$

where RMSF_j is the root-mean-square fluctuation at site j , $\mathbf{r}_i^{(j)}$ is the position of the C α atom of residue j at MD frame i , and $\mathbf{r}_0^{(j)}$ is the position of the C α atom of residue j in the original crystal structure.

To calculate RMSF from homologous structures, we first aligned the structures using the Bio3D package (Grant et al, 2006), and then we calculated

$$\text{RMSF}_j = \left[\sum_i w_i (\mathbf{r}_i^{(j)} - \langle \mathbf{r}^{(j)} \rangle)^2 \right]^{1/2}, \quad (3)$$

where $\mathbf{r}_i^{(j)}$ now stands for the position of the C α atom of residue j in structure i , $\langle \mathbf{r}^{(j)} \rangle$ is the mean position of that C α atom over all aligned structures, and w_i is a weight to correct for potential phylogenetic relationship among the aligned structures. The weights w_i were calculated using BranchManager (Stone and Sidow, 2007), based on phylogenies built with RAxML as before.

To assess variability in backbone and side-chain dihedral angles, we calculated $\text{Var}(\phi)$, $\text{Var}(\psi)$, and $\text{Var}(\chi_1)$. The variance of a dihedral angle was defined according to the most common definition in directional statistics: First, a unit vector \mathbf{x}_i is assigned to each dihedral angle α_i in the sample. The unit vector is defined as $\mathbf{x}_i = (\cos(\alpha_i), \sin(\alpha_i))$. The variance of the dihedral angle is then defined as

$$\text{Var}(\alpha) = 1 - \|\langle \mathbf{x} \rangle\|, \quad (4)$$

where $||\langle \mathbf{x} \rangle||$ represents the length of the mean $\langle \mathbf{x} \rangle$, calculated as $\langle \mathbf{x} \rangle = \sum_i \mathbf{x}_i / n$. Here, n is the sample size. The variance of a dihedral angle is, by definition, a real number in the range $[0, 1]$, with $\text{Var}(\alpha) = 0$ corresponding to the minimum variability of the dihedral angle and $\text{Var}(\alpha) = 1$ to the maximum, respectively (Berens, 2009). Since the χ_1 angle is undefined for Ala and Gly we excluded all sites with these residues in analyses involving χ_1 .

B factors were extracted from the crystal structures. We only considered the B factors of the Ca atom of each residue.

Molecular Dynamics Simulations

Molecular dynamics (MD) simulations were carried out using the GPU implementation of the *Amber12* simulation package (Salomon-Ferrer et al, 2013) with the most recent release of the Amber fixed-charge force field (ff12SB; c.f., AmberTools13 Manual). Prior to MD production runs, all PDB structures were first solvated in a box of TIP3P water molecules (Jorgensen et al, 1983) such that the structures were at least 10\AA away from the box walls. Each individual system was then energy minimized using the steepest descent method for 1000 steps, followed by conjugate gradient for another 1000 steps. Then, the structures were constantly heated from 0K to 300K for 0.1ns, followed by 0.1ns constant pressure simulations with positional harmonic restraints on all atoms to avoid instabilities during the equilibration process. The systems were then equilibrated for another 5ns without positional restraints, each followed by 15ns of production simulations for subsequent post-processing and analyses. All equilibration and production simulations were run using the SHAKE algorithm (Ryckaert et al, 1977). Langevin dynamics were used for temperature control.

Sequence Entropy from Designed Proteins

Designed entropy was calculated as described (Jackson et al, 2013). In brief, proteins were designed using RosettaDesign (Version 39284) (Leaver-Fay et al, 2011) using a flexible backbone approach. This was done for all PDB structures in Table 1 as initial template structures. For each template, we created a backbone ensemble using the Backrub method (Smith and Kortemme, 2008). The temperature parameter in Backrub was set to 0.6, allowing for an intermediate amount of flexibility. For each of the 9 template structures we designed 100 proteins.

Availability of data and methods

All details of simulations, input/output files, and scripts for subsequent analyses are available to view or download at https://github.com/clauswilke/structural_prediction_of_ER.

Results

Data set and structural variables considered

Our goal in this work is to determine which structural properties best predict amino-acid variability at individual sites in proteins. To this end, we selected 9 viral proteins for which we had both high-quality crystal structures and abundant sequences to assess evolutionary variability (Table 1). We quantified evolutionary variability in two ways: by calculating sequence entropies for each alignment column, and by calculating the evolutionary-rate ratio $\omega = dN/dS$ (see Methods for details). Throughout this paper, we primarily report results obtained for sequence entropy. Results for ω are largely comparable, with some specific caveats detailed below.

As predictors of evolutionary variability, we considered two broad classes of structural properties: residue buriedness and residue fluctuation. We additionally considered the variability seen in computationally designed protein variants. **It is jarring here to bring up ASA when in the intro, only RSA is discussed. Is there a good reason to keep ASA here?** Measures of buriedness quantify the extent to which a residue is protected from solvent. Two commonly used measure of buriedness are solvent-accessible surface area (ASA) and its normalized variant relative solvent accessibility (RSA).

Here, we considered only RSA since it can be compared among residues of different sizes. In addition, we also considered the buriedness measures of contact number (CN) and weighted contact number (WCN). While both CN and WCN assess the number of other residues a focal residue contacts, CN simply counts the number of contacts within a sphere of a given radius around the α -carbon of the focal residue. WCN, on the other hand, weights contacts by the distance between the two residues. Note that residue buriedness decreases as RSA increases, but buriedness increases with increasing CN or WCN. To avoid this difference in directionality, we replaced CN and WCN with their inverse, $iCN = 1/CN$ and $iWCN = 1/WCN$, in most analyses. Importantly, this substitution only changed the sign of correlations but not the magnitude because nearly all analyses we carried out were non-parametric and thus depended only on the variables' rank order.

a lot of fluctuating in this sentence: Measures of fluctuation assess the extent to which a residue fluctuates in space as a protein undergoes thermodynamic fluctuations in solution. We quantified these fluctuations using several different measures. First, we measured RMSF, the root mean-square deviation of the $C\alpha$ atom over time. Second, we considered B factors, which measure the spatial localization of individual atoms in a protein crystal. Third, we measured the variability in side-chain or backbone dihedral angles, including $Var(\chi_1)$, $Var(\phi)$, and $Var(\psi)$.

Isn't this paragraph incomplete? Didn't you also use overlaid crystal structures for some of these? To calculate measures of flexibility, we generated molecular dynamics (MD) trajectories for all crystal structures in Table 1. For each protein, we first equilibrated the structure and then simulated 15ns of chemical time and recorded snapshots of the simulated structure every 10ps (see Methods for details). From these snapshots, we calculated RMSF as well as the variability in dihedral and side-chain angles for each residue. We additionally calculated time-averaged values of the three measures of buriedness, RSA, CN, and WCN. We refer to these time-averaged buriedness measures as MD RSA, MD CN, and MD WCN, respectively.

To assess variability in designed proteins, we used the Rosetta protein-design platform to generate 100 designed variants of each protein structure listed in Table 1. We then calculated the sequence entropy at each position in alignments of the designed variants. We refer to the resulting quantity as the *designed entropy*. We had previously shown that designed entropy captures some but not all of the variation observed in natural alignments (Jackson et al, 2013).

Structural buriedness vs. structural flexibility as predictors of evolutionary variation

We began by comparing the correlations of sequence entropy with six different measures of local structural flexibility, including variations in the backbone and side-chain dihedral angles (ϕ , ψ , and χ_1), B factors, RMSF obtained from MD simulations, and RMSF obtained from crystal structures. For the final quantity, we aligned homologous structures with distinct sequences, obtained from the PDB (see Methods and Table 2 for details). The correlation strengths of these quantities with entropy are shown in Figure 2. Significant correlations ($P < 0.05$) are shown with filled symbols, and non-significant correlations are shown with empty symbols ($P \geq 0.05$).

We found that the variation in backbone dihedral angles, $Var(\phi)$ and $Var(\psi)$, explained the least variation in sequence entropy, while the variation in the side-chain dihedral angle $Var(\chi_1)$ explained, on average, more variation in sequence entropy than did any other measure of structural flexibility. B factors and the two measures of RMSF explained on average approximately the same amount of variation in entropy, even though the results for individual proteins were somewhat discordant (see also next subsection).

Based on results from the above analysis, we proceeded to compare the relative explanatory power between the best-performing structural measures ($Var(\chi_1)$, RMSF, and B factors) and buriedness measures. Figure 1 shows the Spearman correlation between sequence entropy and each of the quantities RSA, $iWCN$, $Var(\chi_1)$, RMSF, and B factors, for each protein. In this figure, several patterns emerge. First, nearly all correlations are positive and most are statistically significant. The main exception is the RNA binding domain of Marburg virus, PDB ID 4GHA, which shows mostly no correlation, with the exception of a negative correlation between sequence entropy and χ_1 angle variability. Second, correlations are generally weak, such that no correlation coefficient exceeds 0.4. Third, on average, the correlation strength decreases as we move from buriedness measures to structural fluctuation measures (left to right in the figure). The two measures of buriedness, RSA and $iWCN$, show the strongest correlations of, on average, $\rho = 0.23$ and $\rho = 0.22$, respectively. The three fluctuation measures $Var(\chi_1)$, RMSF, and B factors exhibit weaker correlations of, on average $\rho = 0.14$, $\rho = 0.11$, and $\rho = 0.12$, respectively.

MD time-averages vs. crystal-structure snapshots

Except for analyses involving B factors or crystal RMSF, we obtained structural measures by averaging quantities over MD trajectories, comprising 15ns of chemical time each. This approach, however, breaks from conventional practice for measuring buriedness quantities. Typically, measures such as RSA or CN are obtained from individual crystal structures. Therefore, we examined whether MD averages differed in any meaningful way from estimates obtained from crystal structures, and whether these estimates differ in their predictive power for sequence variability.

We found that RSA, CN, and WCN from crystal structures were highly correlated with their averages over MD trajectories, for all protein structures we examined (Spearman correlation coefficients of > 0.9 **p-values??** in all cases, Table 3). Furthermore, the correlation coefficients we obtained when comparing the crystal structure buriedness measures to sequence entropy were virtually identical to coefficients obtained from the MC trajectory correlations (Figure 3A-C). Thus, in terms of predicting evolutionary variation, RSA and CN values obtained from static structures performed as well as their MD equivalents averaged over short time scales.

By contrast, we found more **variation (does this mean variation in r? it's an awkward WC given the paper topic)** when we considered backbone flexibility as measured by root mean fluctuations (RMSF). As RMSF cannot be obtained from a single crystal structure, we calculated it from an alignment of multiple crystal structures, when available. When we compared RMSF from MD to RMSF from crystal structures, we found that they were sometimes quite different, with correlation coefficients ranging from 0.218 to 0.723 (Table 3). Consequently, for the two proteins for which MD RMSF was the least correlated with crystal-structure RMSF (hepatitis C protease and Rift Valley fever nucleoprotein), the strength of site entropy and RMSF correlation coefficient depended substantially on whether RMSF was obtained from MD or from crystal structures (Figures 2 and 3D).

I'm really not sure what to do with this paragraph. It seems out of place, but I don't know where to put it. To further investigate the relationship between backbone fluctuations and sequence variability, we also compared the RMSF correlations to the correlations between sequence entropy and B factors. Again, we found that these correlations were generally different from the ones found for either the MD RMSF or the crystal structure RMSF (Figure 4). Thus, B factors, MD RMSF, and crystal RMSF, though all measures of backbone fluctuations, contained distinct information about sequence variability in our data set.

Sequence entropy vs. evolutionary-rate ratio ω

In the previous subsections, we have used sequence entropy as a measure of amino-acid variability at individual sites. While sequence entropy is a simple and straightforward measure of site variability, it has two potential drawbacks. First, while measured from homologous protein alignments, sequence entropy doesn't correct for the phylogenetic relationship of those alignment sequences. Hence, entropy can be biased if some parts of the phylogeny are more densely sampled than others. Second, entropy does not take the actual substitution process into account. As a result, a single substitution near the root of the tree can result in a comparable entropy to a sequence of substitutions toggling back and forth between two amino acids.

To consider an alternative quantity of sequence variability that doesn't suffer from either of these drawbacks, we calculated the evolutionary-rate ratio $\omega = dN/dS$ for all proteins at all sites, and repeated all analyses with ω instead of entropy. We found that results generally carried over, but with somewhat weaker correlations. Figure 5 plots, for each protein, the correlation between ω and the various structural quantities versus the correlation between entropy and the same structural quantities. Most data points fall below the $x = y$ line and are shifted downwards by approximately 0.1. Thus, correlations of structural quantities with ω are, on average, approximately 0.1 smaller than correlations of the same quantities with sequence entropy.

Besides the measures of buriedness and measures of structural flexibility, we included the additional property, designed entropy, in Figure 5. We found that designed entropy performed about as well as the measures of structural flexibility did on average, but worse than the measures of buriedness, in predicting either ω or sequence entropy. Designed entropy is discussed in more detail in the next subsection.

Multi-variate analysis of structural predictors

The various structural quantities we have considered are by no means independent of each other. Measures of buriedness co-vary with each other, as do measures of structural flexibility. Further, the latter co-vary with the former, as does designed entropy. Therefore, we conducted a joint multivariate analysis, which included most structural quantities considered in this work, to determine the extent to which these quantities contain independent information about sequence variability. This analysis additionally assessed whether combining multiple structural quantities yields improved predictive power. We employed a principal component (PC) regression approach, which has previously been used successfully to disentangle genomic predictors of whole-protein evolutionary rates (Drummond et al, 2006; Bloom et al, 2006). For this analysis, we first carry out a PC analysis of the predictor variables (i.e., the structural quantities such as RSA and RMSF), and we subsequently regress the response (sequence entropy or ω) against the individual components.

We pooled all structural quantities for a single PC analysis and then regressed entropy and ω against each PC separately for each protein. This strategy allowed us to analyze all proteins in our data set individually but in such a way that results were comparable from one protein to the next. The results of this analysis are shown in Figure 6. The first component (PC1) explained on average the largest amount of variation in sequence entropy (see Figure 6A). We found the second-highest r^2 values, on average, for PC3, while all other components explained very little variation in sequence entropy. When looking at the composition of the components, we found that RSA, iWCN, RMSF, and $\text{Var}(\chi_1)$ all loaded strongly on PC1, while PC2 and PC3 were primarily represented by designed entropy and B factors (see Figure 6B and C). RMSF also had moderate loadings on PC3. Interestingly, designed entropy and B factors load with equal signs on PC2 but with opposite signs on PC3.

We suspect that PC1 can be considered a buriedness component. By definition, PC1 measures the largest amount of variation among the structural quantities, and all structural quantities reflect to some extent the buriedness of residues. PC2 and PC3 are more difficult to interpret. Since designed entropy and B factors load strongly on both but with two different combinations of signs, we think the most parsimonious interpretation is to consider PC2 as a component representing sites with high designed entropy and high spatial fluctuations (as measured by B factors) and PC3 representing sites with high designed entropy and low spatial fluctuations. Using these interpretations, our PC regression analysis suggests that of all the structural quantities, residue buriedness is the best predictor of evolutionary variation. Designed entropy is a useful predictor as well, but it tends to perform better at sites with low spatial fluctuations.

Clarify - was this a second PCA? When we included RMSF derived from crystal structures in our analysis, we found comparable results. The main differences occurred in PC2 and PC3, where CS RMSF generally loaded in the opposite direction of B factor, and either in the same (PC2) or the opposite (PC3) direction of designed entropy (Figure S1). Finally, results were generally comparable when we considered ω instead of sequence entropy (Figures S2 and S3).

Discussion

We have carried out a comprehensive analysis of how well structural quantities predict evolutionary variation in nine viral proteins. We found that measures of buriedness generally performed better than did measures of structural fluctuations, or flexibility. Further, measures of buriedness also performed better than a computational protein-design approach that employed a sophisticated all-atom force field to determine allowed amino-acid distributions at each site. Finally, averaging structural quantities over 15ns of MD simulations provided no improvement in predictive power relative to taking the same quantities from individual crystal structures.

Our results are broadly in agreement with recent work by Echave and collaborators (Yeh et al, 2014; Huang et al, 2014). These authors found that RSA and contact number showed comparable correlation strengths with evolutionary variation (Yeh et al, 2014). Further, they demonstrated that the observed relationship between evolutionary variation and residue-residue contacts was not consistent with a flexibility model that puts evolutionary variability in proportion to structural flexibility (Huang et al, 2014). Instead, a mechanistic stress model, in which amino-acid substitutions cause physical stress in proportion to the number of residue-residue contacts affected, could explain all the observed data (Huang et al, 2014).

We have found here that correlations between sequence entropy and structural quantities were consistently higher than correlations between the evolutionary-rate ratio ω and structural quantities. This

difference likely reflects the distinct physical processes that entropy and ω measure. Entropy is a measure of the amino-acid diversity allowed at a given site, reflecting how many different amino acids are tolerated. By contrast, ω measures how rapidly amino-acid changes occur at a given site. While entropy and ω are generally correlated, a site can have high entropy and comparatively low ω and vice versa. In particular, if substitutions rapidly toggle back and forth between two different amino acids at a site, then that site will have high ω and low entropy. By contrast, if a site diversified into a number of different alleles deep in the phylogeny but did not experience much subsequent evolution, that site will have comparatively high entropy but low ω . Since structural quantities such as measures of buriedness reflect the biophysical constraints imposed on sites, it makes sense that they would be better predictors of the allowed amino-acid diversity at a site than the speed of substitution at that site. By contrast, biological processes such as immune escape would likely be better predictors of substitution rates than of amino-acid diversity.

The correlation strengths we observed were consistently lower than those observed previously (Jackson et al, 2013; Yeh et al, 2014). We believe that this result was due to our choice of analyzing viral proteins instead of the cellular proteins or enzymes used in prior works. First, while viral sequences are abundant, their alignments may not be as diverged as alignments that can be obtained for sequences from cellular organisms. For example, our influenza sequences spanned only approximately one decade. Despite the high mutation rates observed in RNA viruses, the evolutionary variation that can accumulate over this time span is limited. This relatively lower evolutionary divergence makes resolving differences between more and less conserved sites much more difficult. Second, many viral proteins experience a substantial amount of selection pressure to evade host immune responses. The resulting positive selection on viral sequences may mask evolutionary constraints imposed by structure. For example, influenza hemagglutinin displays positive selection throughout the entire sequence, regardless of the extent of residue burial (Meyer and Wilke, 2013; Meyer et al, 2013; Suzuki, 2006; Bush et al, 1999).

We found that simple measures of buriedness, such as RSA and contact numbers, were better predictors of evolutionary variation than was sequence variability predicted from computational protein design. In other words, simple quantities that can be obtained trivially from PDB structures performed better than a sophisticated protein-design strategy that makes use of an all-atom energy function and requires thousands of CPU-hours to complete. This result highlights that, even though computational protein design has yielded impressive results in specific cases (Kuhlman et al, 2003; Röthlisberger et al, 2008; Fleishman et al, 2011), this approach remains limited in its ability to predict evolutionary variation. Similarly, we have previously found that flexible backbone design with Rosetta produced designs whose surface and core were too similar (Jackson et al, 2013). We attributed this discrepancy to either the solvation model or the model of backbone flexibility we used (Backrub, see Smith and Kortemme 2008). The results we found here suggest that the model of backbone flexibility may indeed be the cause of at least some of the discrepancies between predicted and observed site variability. In particular, in our PC regression analysis, the component in which designed entropy loaded opposite to B factor and MD RMSF generally had the second-highest predictive power for evolutionary variability, after the component representing buriedness. In sum, designed entropy was a better predictor for sequence variability for sites with less structural variability **compared to sites with MORE variability? clarify this..**

This concluding paragraph seems tacked-on, as a plug for developing epistasis models. Similar in concept to collaborator's random "therefore, allergies are a huge problem." conclusion... Even though RSA and contact number remain the best currently known predictors of evolutionary variation, neither quantity has particularly high predictive power. One reason why predictive power may be low is that neither quantity accounts for correlated substitutions at interacting sites. Yet such correlated substitutions happen regularly. For example, covariation among sites encodes information about residue-residue contacts and 3D structure (Halabi et al, 2009; Burger and van Nimwegen, 2010; Marks et al, 2011; Jones et al, 2014), and evolutionary models that incorporate residue-residue interactions tend to perform better than models that do not (Rodrigue et al, 2005; Bordner and Mittelman, 2014). An improved predictor of evolutionary variation would have to correctly predict this covariation from structure. In principle, computational protein design, which takes into consideration the atom-level details of the protein structure, should properly reproduce covariation among sites. However, a recent analysis showed that there are significant limitations to the covariation that is predicted (Ollikainen and Kortemme, 2013). In addition, covariation in designed proteins is quite sensitive to the type of backbone variation modeled during design, and improved models of backbone flexibility may be required for improved prediction of covariation among sites (Ollikainen and Kortemme, 2013).

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Tables

Table 1 PDB structures considered in this study.

Viral Protein	PDB ID	Chain	Sequence Length	Number of Sequences
Hemagglutinin Precursor	1RD8	AB	503	1039
Dengue Protease Helicase	2JLY	A	451	2362
West Nile Protease	2FP7	B	147	237
Japanese Encephalitis Helicase	2Z83	A	426	145
Hepatitis C Protease	3GOL	A	557	1021
Rift Valley Fever Nucleoprotein	3LYF	A	244	95
Crimean Congo Nucleocapsid	4AQF	B	474	69
Marburg RNA Binding Domain	4GHA	A	122	42
Influenza Nucleoprotein	4IRY	A	404	943

Table 2 Availability of homologous crystal structures. Even though most viral proteins have many PDB structures available, the sequence divergence among these structures is low. To calculate RMSF from crystal structures, we here considered all proteins for which we could find at least five homologous structures at 5% pairwise sequence divergence (highlighted in bold).

Viral Protein	BLAST hits ^a	Unique sequences			
		all	$\geq 2\%$ ^b	$\geq 5\%$ ^b	$\geq 10\%$ ^b
Hemagglutinin Precursor	63	17	10	9	7
Dengue Protease Helicase	31	13	7	7	7
West Nile Protease	21	16	10	7	6
Japanese Encephalitis Helicase	31	12	7	7	7
Hepatitis C Protease	302	33	10	5	4
Rift Valley Fever Nucleoprotein	95	9	5	5	5
Crimean Congo Nucleocapsid	7	4	3	2	2
Marburg RNA Binding Domain	63	9	5	3	3
Influenza Nucleoprotein	69	15	4	4	2

^a BLAST hits against all sequences in the PDB, excluding hits with $< 35\%$ sequence identity and $< 90\%$ alignment length

^b Unique sequences at indicated minimum pairwise sequence divergence

Table 3 Correlations between quantities obtained from MD trajectories and from crystal structures. For each quantity and each protein, we calculated the Spearman correlation ρ between the values obtained from MD time averages and the values obtained from nine viral protein crystal structures. We then calculated the minimum, maximum, mean, and standard deviation of these correlations.

Quantity	min ρ	max ρ	$\langle \rho \rangle$	SD(ρ)
RSA	0.937	0.981	0.948	0.012
CN	0.964	0.993	0.976	0.008
WCN	0.973	0.991	0.984	0.006
RMSF	0.218	0.723	0.502	0.181

Figures

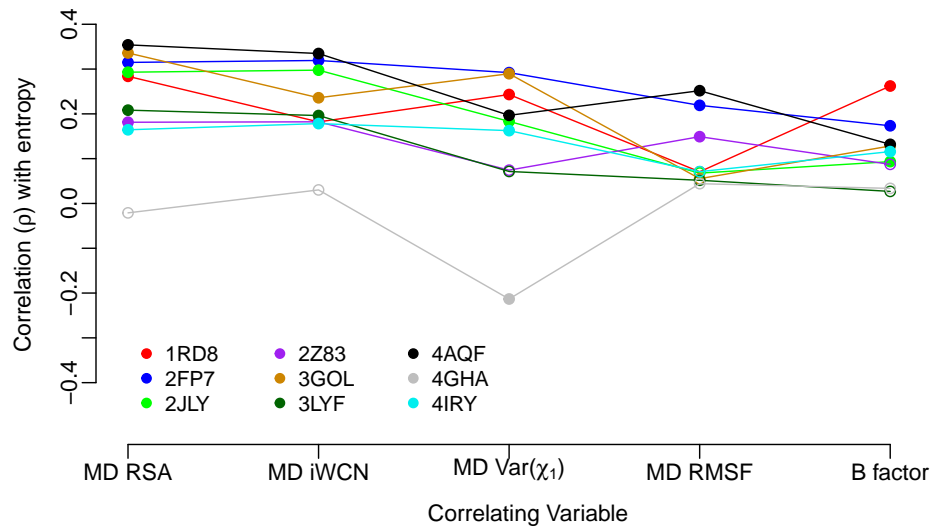


Fig. 1 Spearman correlation of sequence entropy with measures of buriedness and of structural variability. Each symbol represents one correlation coefficient for one protein structure. Significant correlations ($P < 0.05$) are shown as filled symbols, and insignificant correlations ($P \leq 0.05$) are shown as open symbols. The quantities RSA, iWCN, $\text{Var}(\chi_1)$, and RMSF were obtained as time-averages over 15ns of MD simulations. B factors were obtained from crystal structures. Compared to the measures of structural variability, the buriedness measures consistently show stronger correlations with sequence entropy.

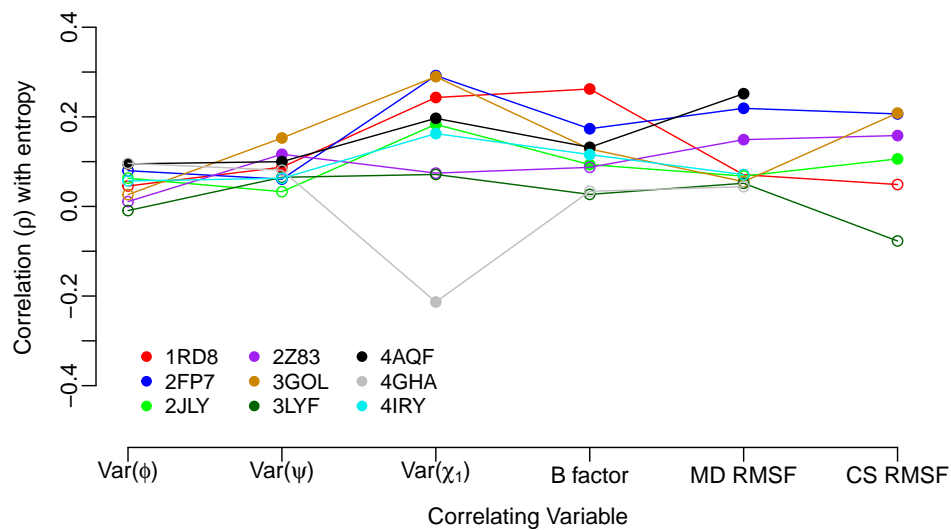


Fig. 2 Spearman correlation of sequence entropy with measures of structural variability. Each symbol represents one correlation coefficient for one protein structure. Significant correlations ($P < 0.05$) are shown as filled symbols, and insignificant correlations ($P \leq 0.05$) are shown as open symbols. The quantities $\text{Var}(\psi)$, $\text{Var}(\phi)$, $\text{Var}(\chi_1)$, and MD RMSF were obtained as time-averages over 15ns of MD simulations. B factors were obtained from crystal structures. CS RMSF values were obtained from alignments of homologous crystal structures. Almost all structural measures of variability correlate weakly but significantly with sequence entropy.

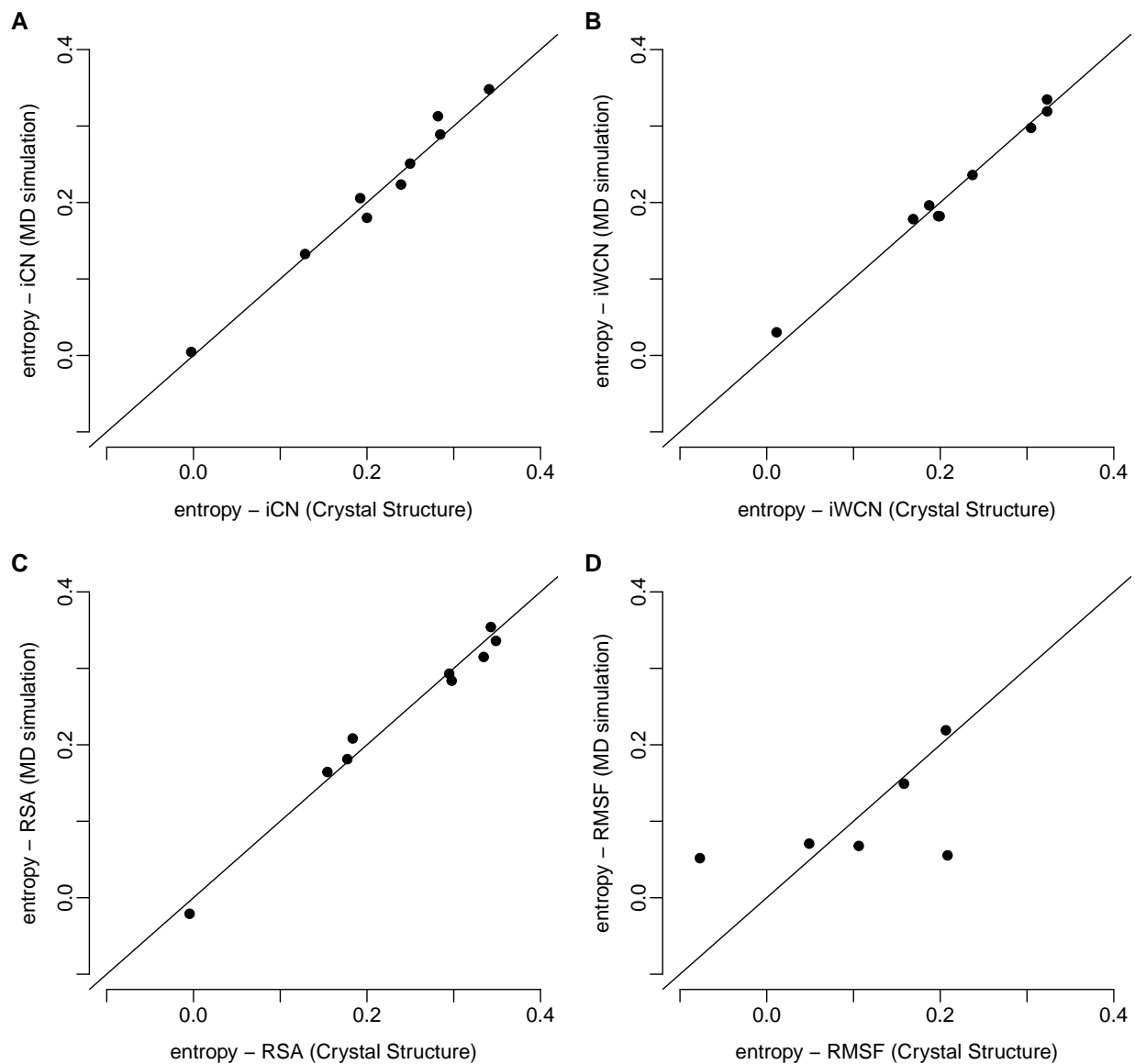


Fig. 3 Spearman correlations of sequence entropy with MD-derived and crystal-structure derived structural measures. The vertical axes in all plots represent the Spearman correlation of sequence entropy with one structural variable obtained from 15ns of molecular dynamics (MD) simulations. The horizontal axes represent the Spearman's rank correlation coefficient of sequence entropy with the same structural variable as in the vertical axes but measured from protein crystal structures. Each dot represents one correlation coefficient for one protein structure. The quantities iCN, iWCN, and RSA have nearly identical predictive power for sequence entropy regardless of whether they are derived from MD simulations or from crystal structures. By contrast, RMSF from MD simulations leads to very different correlations than RMSF from crystal structures does.

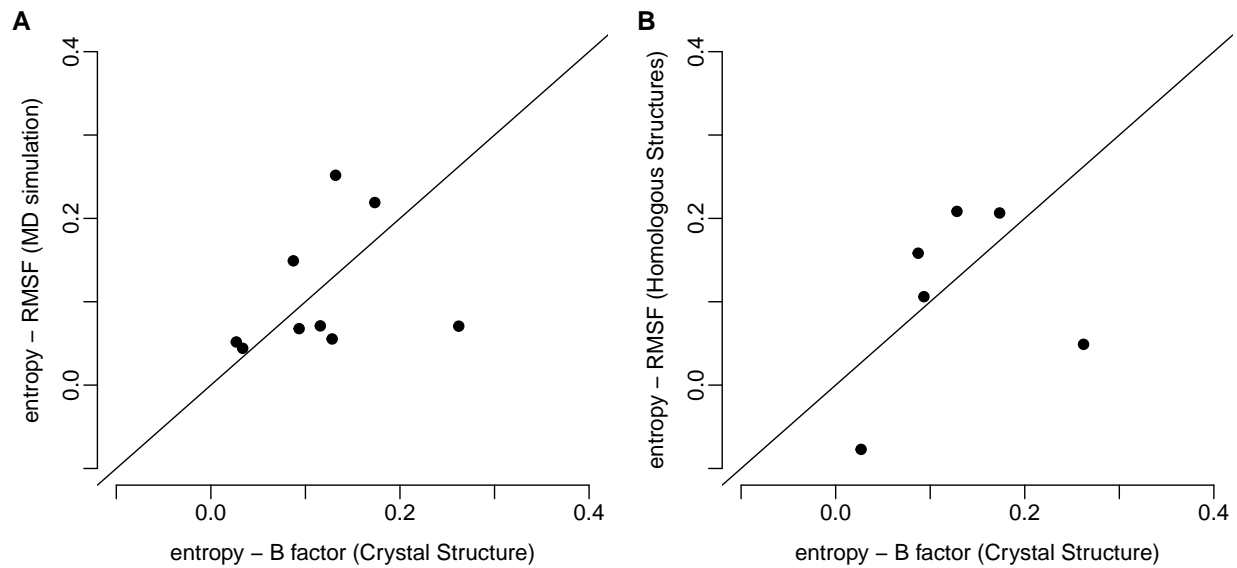


Fig. 4 Spearman correlations of sequence entropy with measures of structural variability. Vertical and horizontal axes represent Spearman correlations of the indicated quantities. Each dot represents one correlation coefficient for one protein structure. MD RMSF, crystal-structure RMSF, and B factors all explain different amounts of variance in sequence entropy for different proteins.

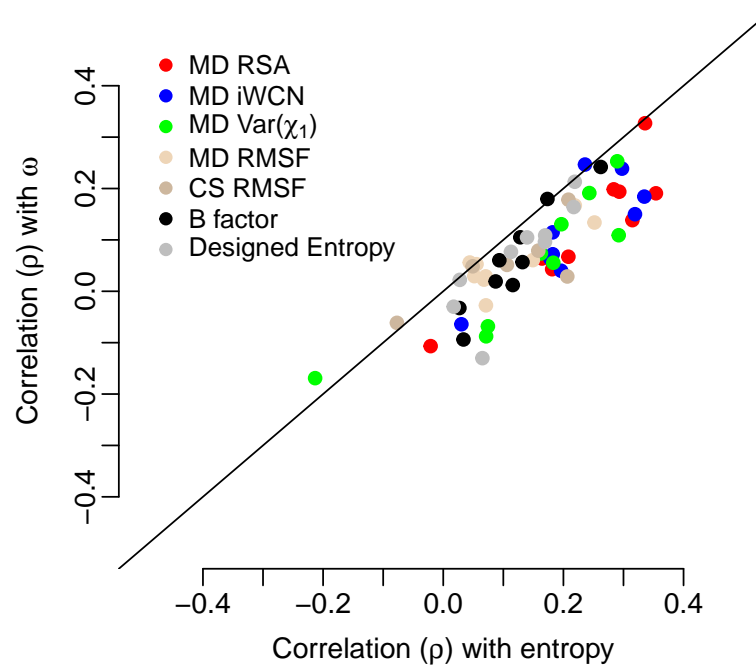


Fig. 5 Spearman correlations of structural quantities with sequence entropy and with the evolutionary rate ratio ω . All structural quantities generally predict as much as or more variation in sequence entropy than in ω .

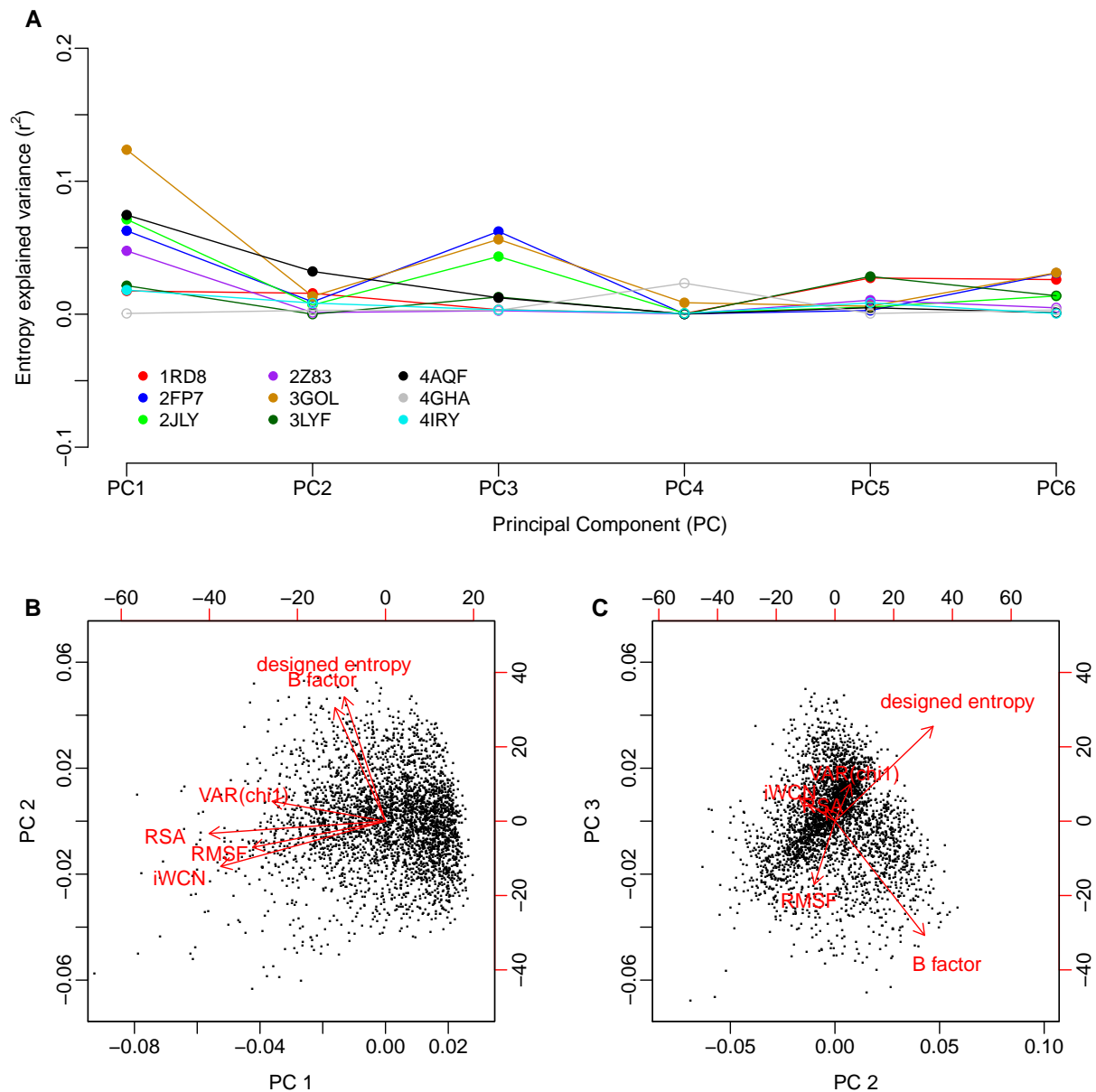


Fig. 6 Principal Component (PC) Regression of sequence entropy against the structural variables. **(A)** Variance in entropy explained by each principal component. For most proteins, PC1 and PC3 show the strongest correlations with sequence entropy. Significant correlations ($P < 0.05$) are shown as filled symbols, and insignificant correlations ($P \geq 0.05$) are shown as open symbols. **(B)** and **(C)** Composition of the three leading components. Red arrows represent the loadings of each of the structural variables on the principal components; black dots represent the amino acid sites in the PC coordinate system. The variables RSA, iWCN, MD RMSF, and Var(χ_1) load strongly on PC1 and weakly on PC2, while B factor and designed entropy load strongly on PC2 and weakly on PC1. Interestingly, B factor and designed entropy also load strongly on PC3, but in opposite directions.

Supplementary Figures

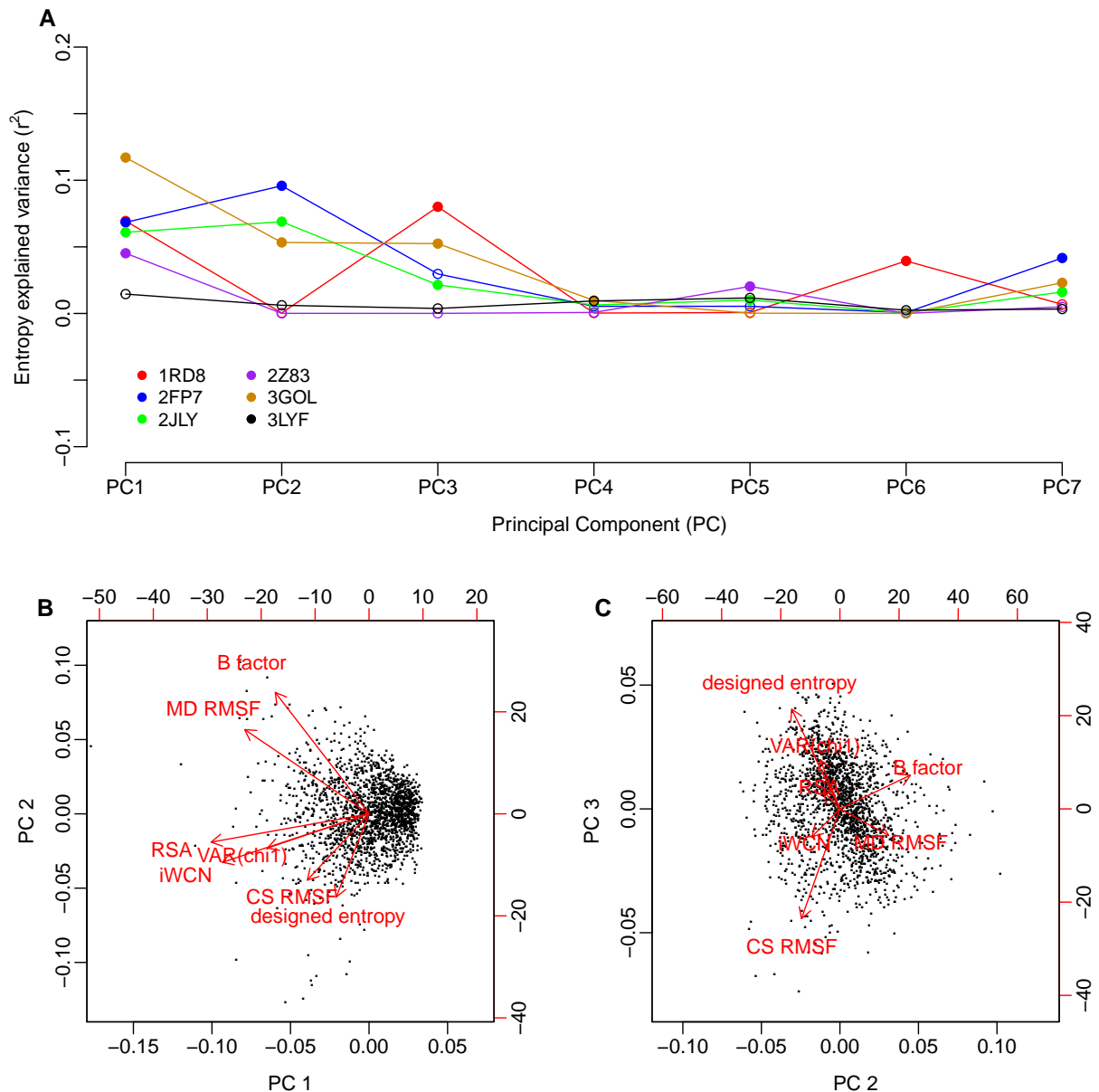


Fig. S1 Principal Component (PC) Regression of sequence entropy against the structural variables, including CS RMSF. **(A)** Variance in entropy explained by each principal component. For most proteins, PC1 and either PC2 or PC3 show the strongest correlations with sequence entropy. Significant correlations ($P < 0.05$) are shown as filled symbols, and insignificant correlations ($P \geq 0.05$) are shown as open symbols. **(B)** and **(C)** Composition of the three leading components. Red arrows represent the loadings of each of the structural variables on the principal components; black dots represent the amino acid sites in the PC coordinate system.

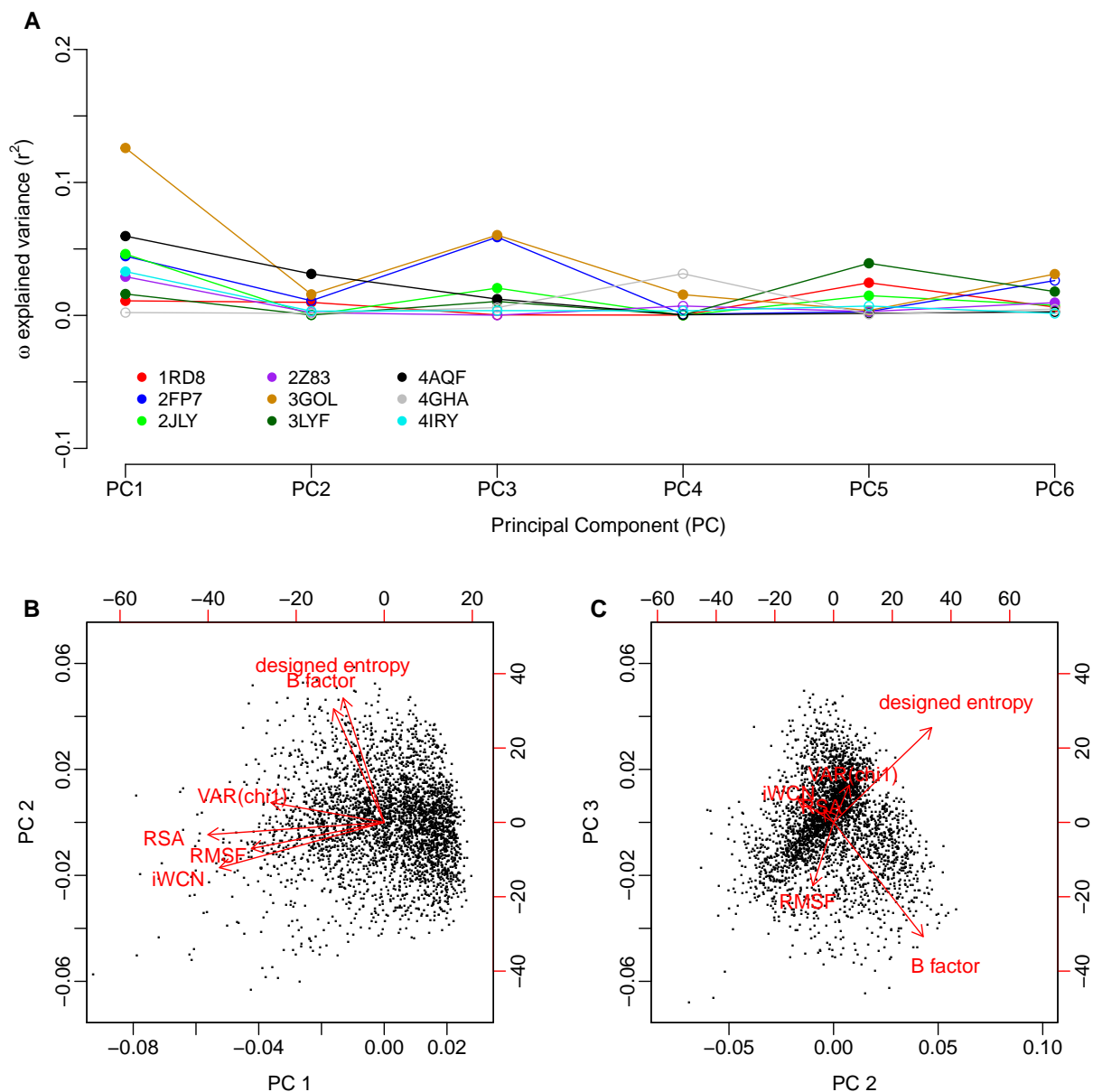


Fig. S2 Principal Component (PC) Regression of ω against the structural variables. **(A)** Variance in ω explained by each principal component. For most proteins, PC1 and PC3 show the strongest correlations with ω . Significant correlations ($P < 0.05$) are shown as filled symbols, and insignificant correlations ($P \leq 0.05$) are shown as open symbols. **(B)** and **(C)** Composition of the three leading components. Red arrows represent the loadings of each of the structural variables on the principal components; black dots represent the amino acid sites in the PC coordinate system. Note that parts B and C are identical to those shown in Figure 6.

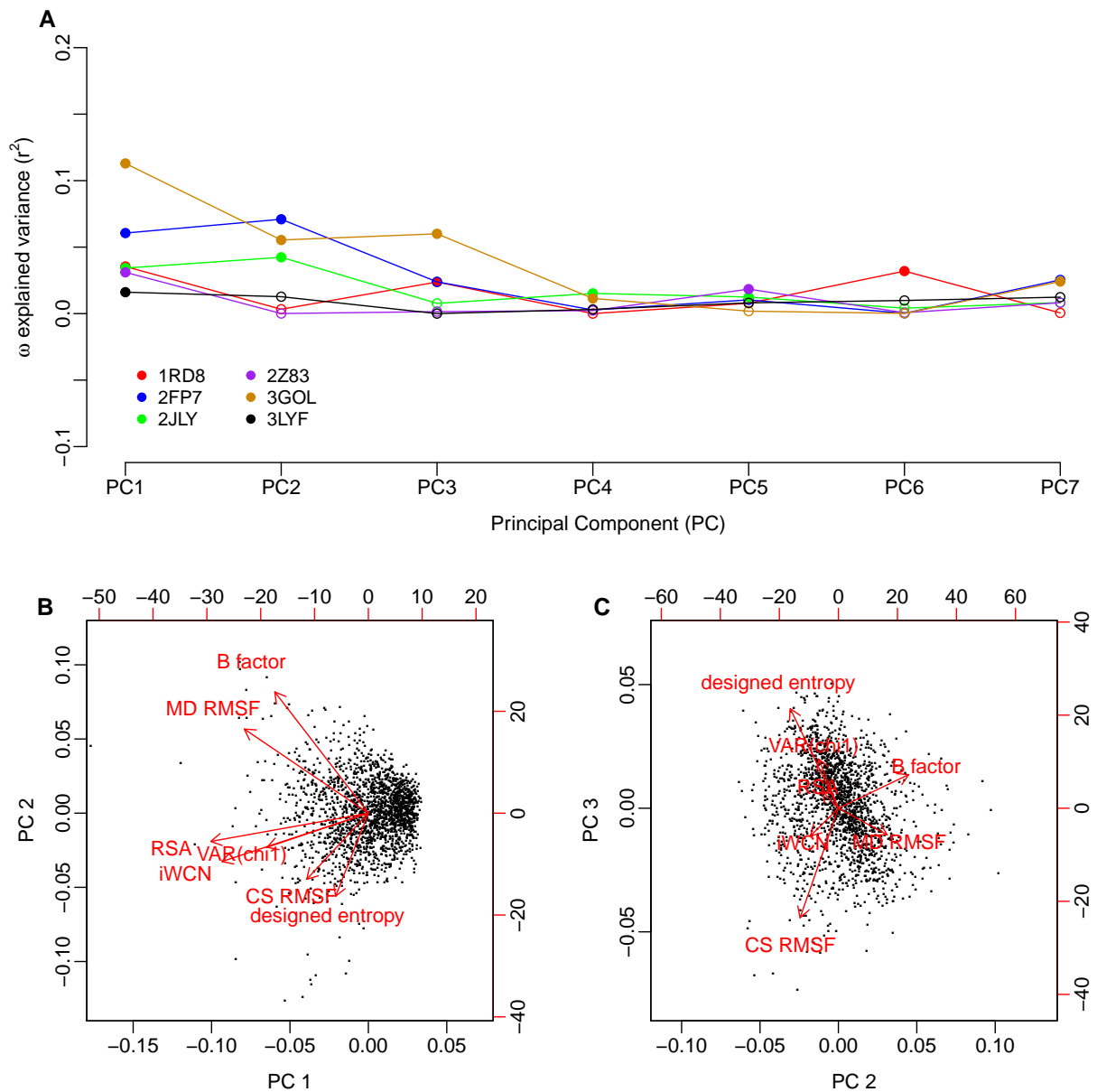


Fig. S3 Principal Component (PC) Regression of ω against the structural variables, including CS RMSF. **(A)** Variance in ω explained by each principal component. For most proteins, PC1 and either PC2 or PC3 show the strongest correlations with ω . Significant correlations ($P < 0.05$) are shown as filled symbols, and insignificant correlations ($P \leq 0.05$) are shown as open symbols. **(B)** and **(C)** Composition of the three leading components. Red arrows represent the loadings of each of the structural variables on the principal components; black dots represent the amino acid sites in the PC coordinate system. Note that parts B and C are identical to those shown in Figure S1.