

Measurement of forward-backward multiplicity correlations in Pb+Pb, p +Pb and pp collisions with the ATLAS detector

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for the ATLAS collaboration

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Stony Brook
University

Motivation: a historical view

- Rapidity correlations is an old story



- Physics goal: understand production mechanism in early stage.
 - More details see Longgang and Jiangyong's talks.

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- Previous methods focused on limited phase space: η and $-\eta$;
 - Short-range correlation and statistical dilution;
 - Few direct comparisons among different systems;

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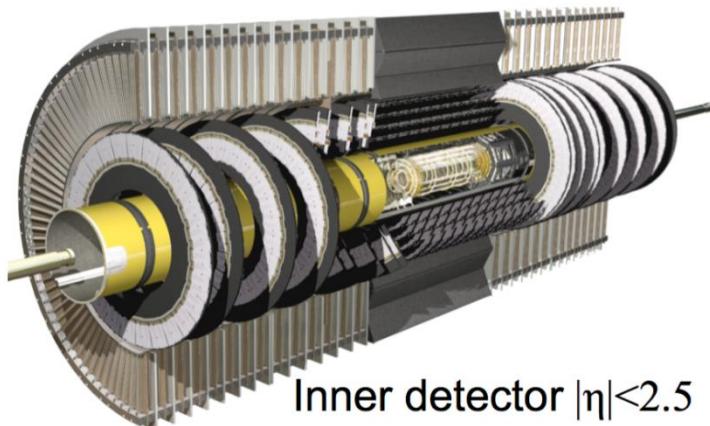
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- Why we come back to this analysis?

- Previous methods focused on limited phase space: η and $-\eta$;
- We used a new observable that covers full η space;
- Short-range correlation and statistical dilution;
- We estimated short-range correlation;
- Few direct comparisons among different systems;
- We compared from large to small systems.

Pb+Pb, p+Pb and pp datasets

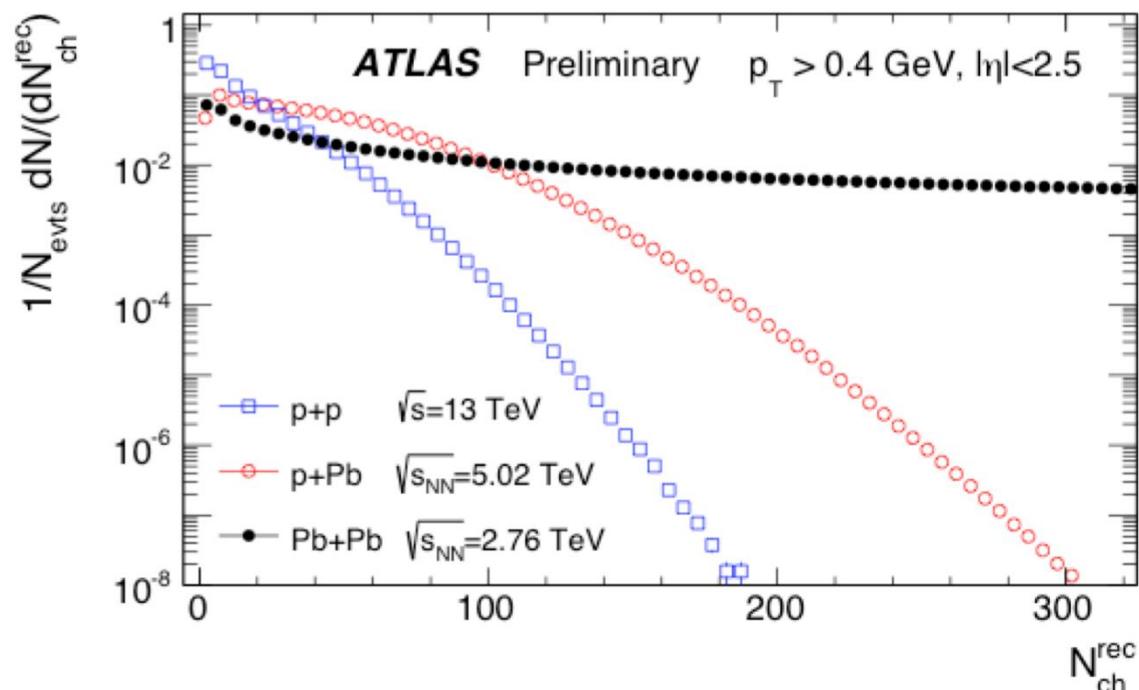
- Correlation functions calculated using charged particles $p_T > 0.2$ GeV;
- **High-multiplicity** track (HMT) trigger used to increase statistics;



Pb+Pb 2.76 TeV, 2010, MB

p+Pb 5.02 TeV, 2013, MB+HMT

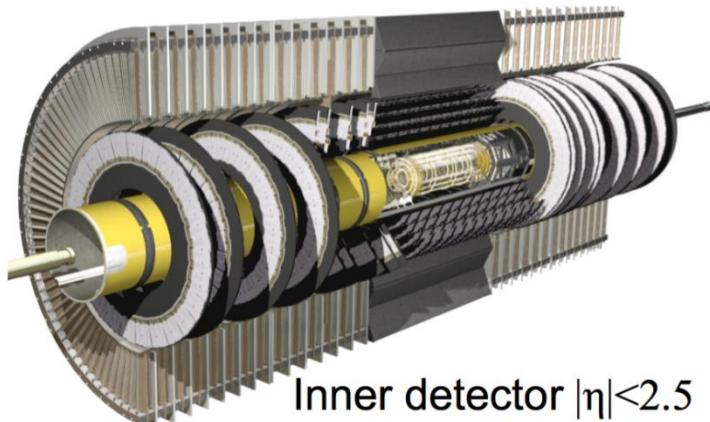
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- Analysis carried out in many bins over $10 \leq N_{\text{ch}}^{\text{rec}} < 300$;
- Results presented as a function efficiency-corrected values N_{ch} .

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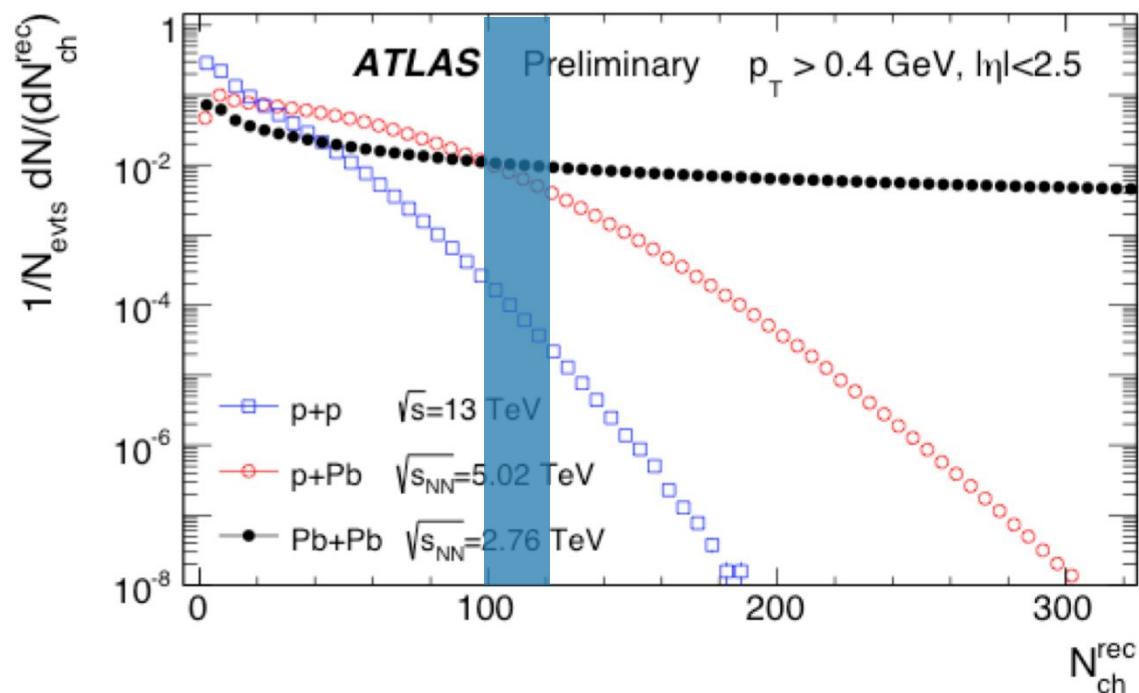
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- Analysis carried out in many bins over $10 \leq N_{ch}^{rec} < 300$;
- Results presented as a function efficiency-corrected values N_{ch} .
 - How long-range correlation compare among three systems, at the same N_{ch} ?

Observable

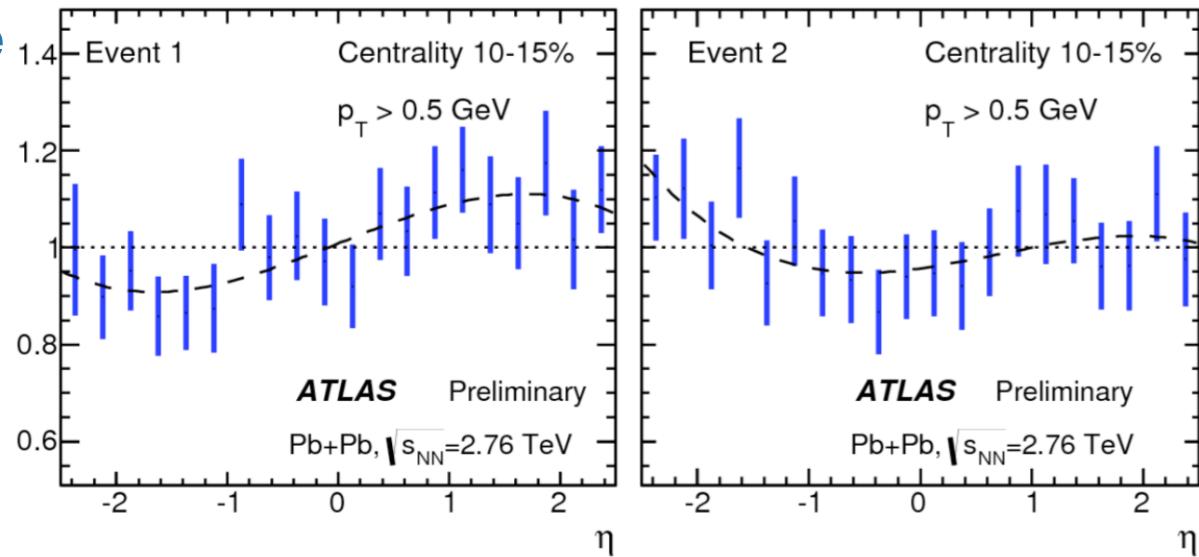
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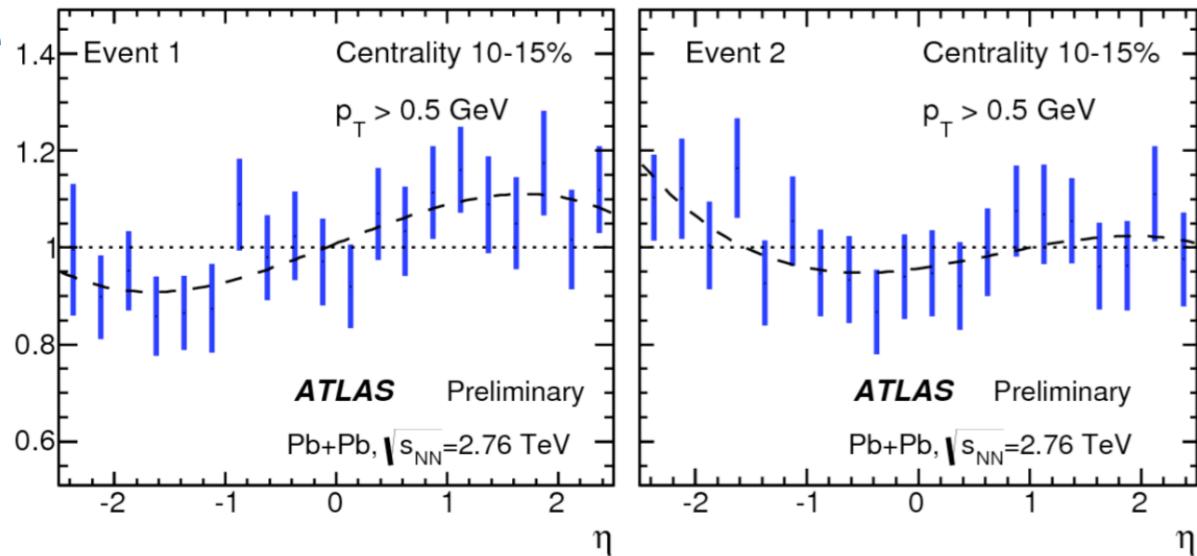


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- Dominated by statistical fluctuations!

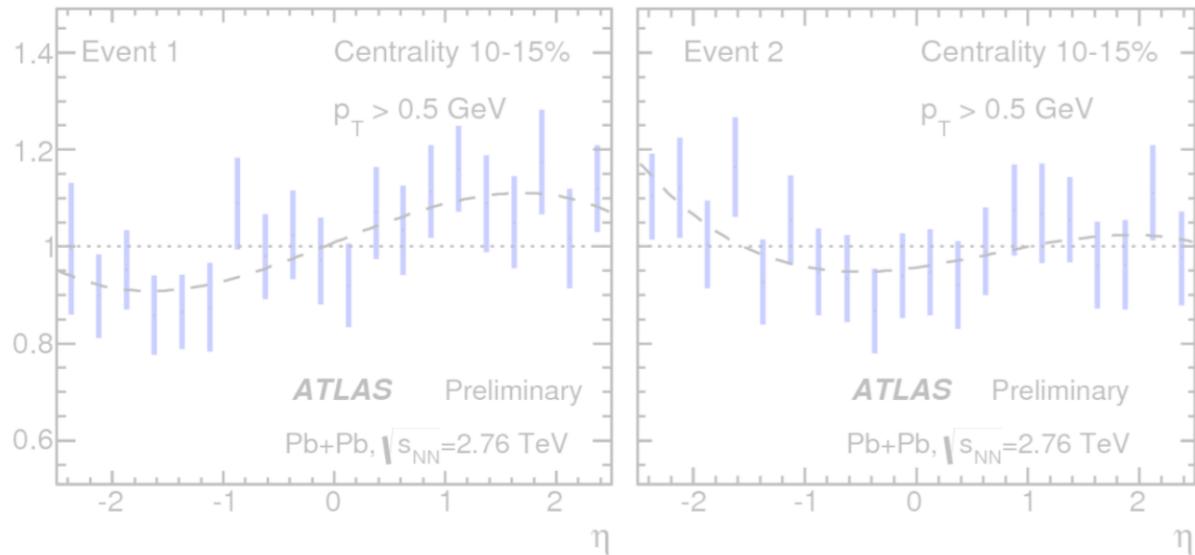


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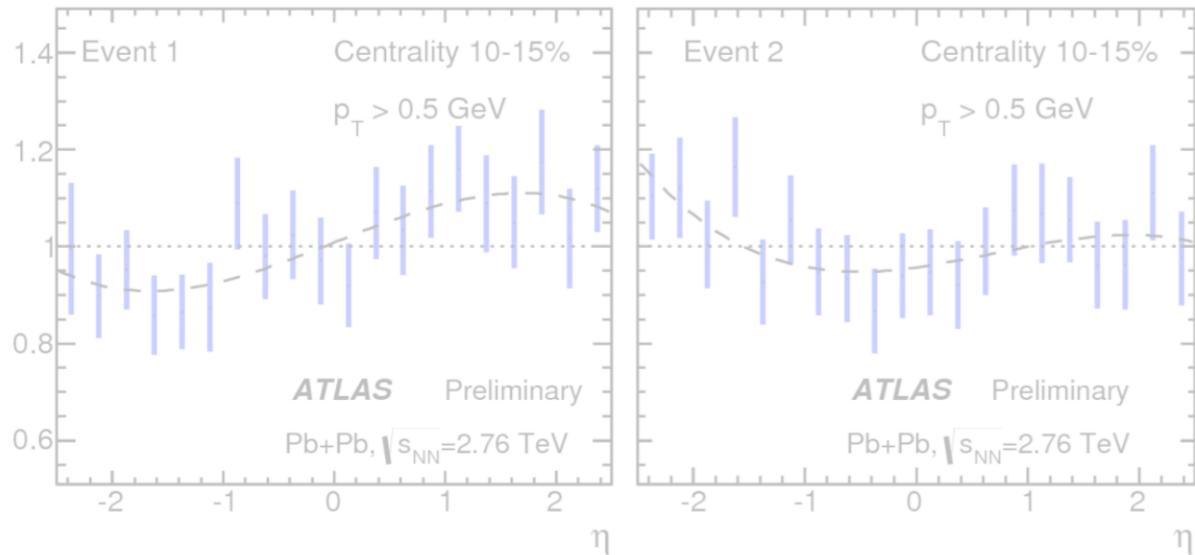
$$C(\eta_1, \eta_2) = \frac{\langle N(\eta_1)N(\eta_2) \rangle}{\langle N(\eta_1) \rangle \langle N(\eta_2) \rangle}$$

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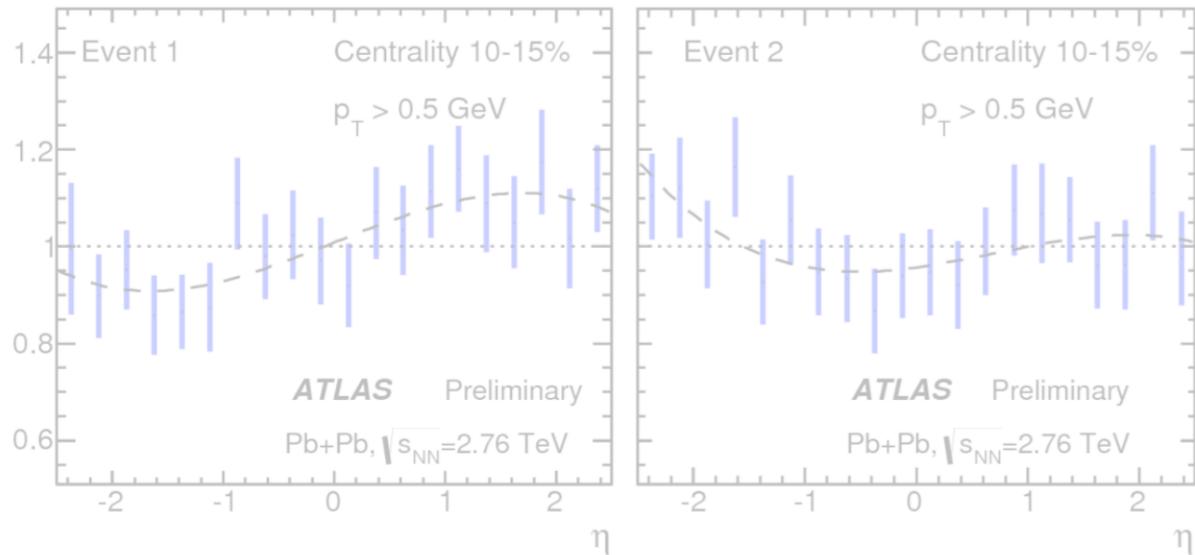
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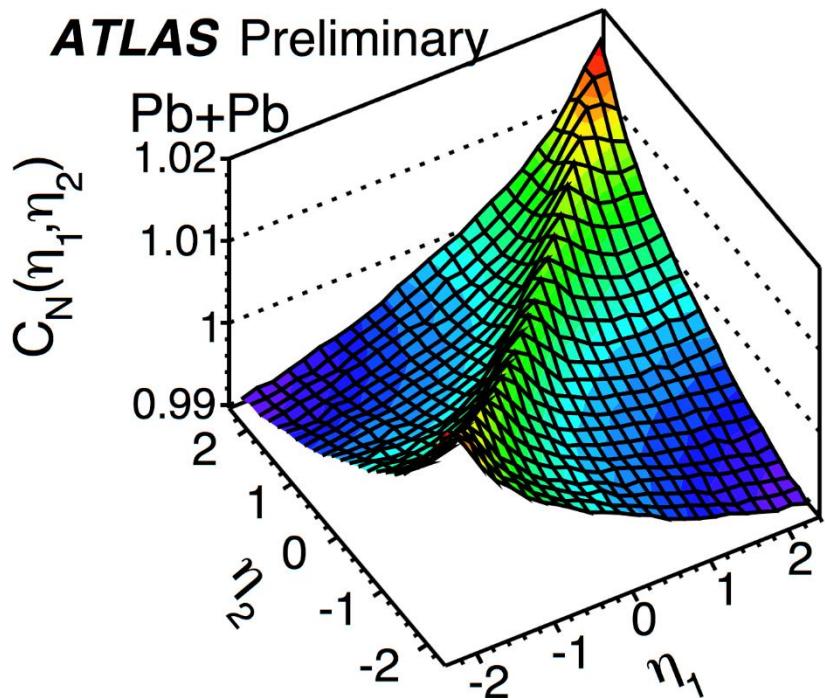
Two-particle correlation is related to single-particle distribution.

- Advantage of correlation function

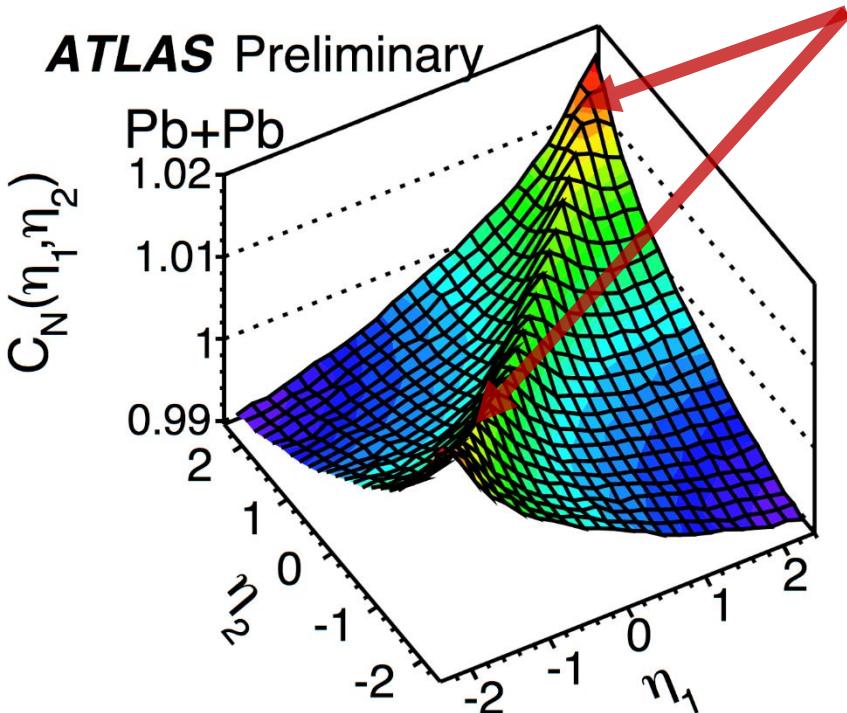
- Disentangles dynamical fluctuation from statistical fluctuation.
- Detector effects removed by mixed events;

FB multiplicity correlation $C(\eta_1, \eta_2)$

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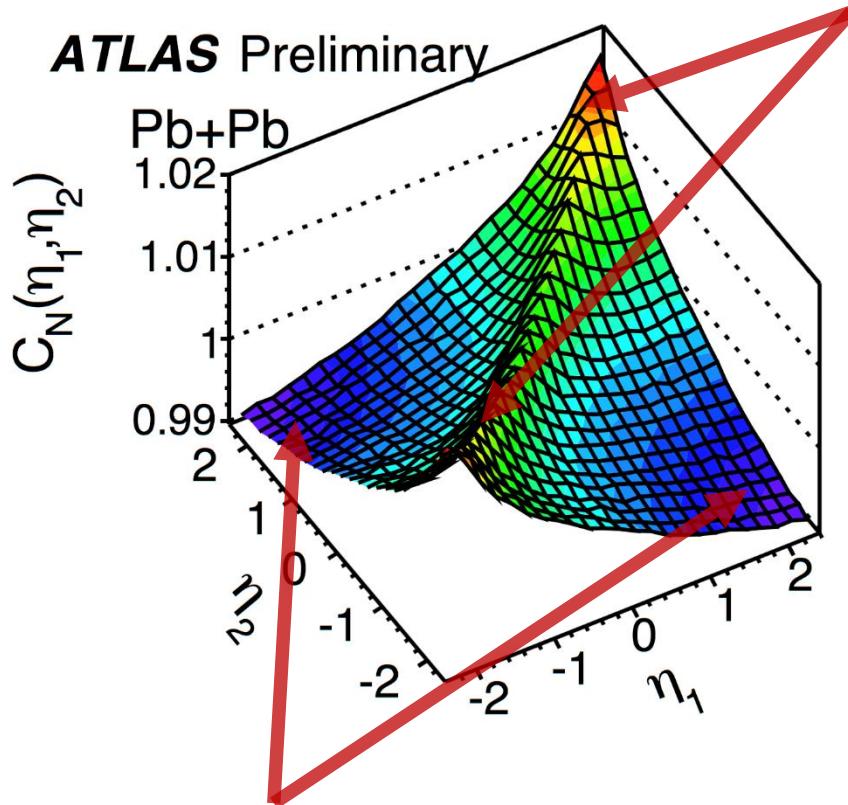


$$|\eta_-| \equiv |\eta_1 - \eta_2| \approx 0$$

Short-range correlation $\delta_{SRC}(\eta_1, \eta_2)$

reflect correlation in the **same source**:
jet fragmentation, resonance decay...

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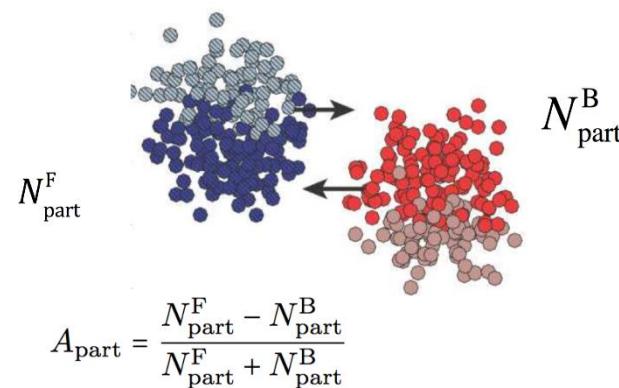
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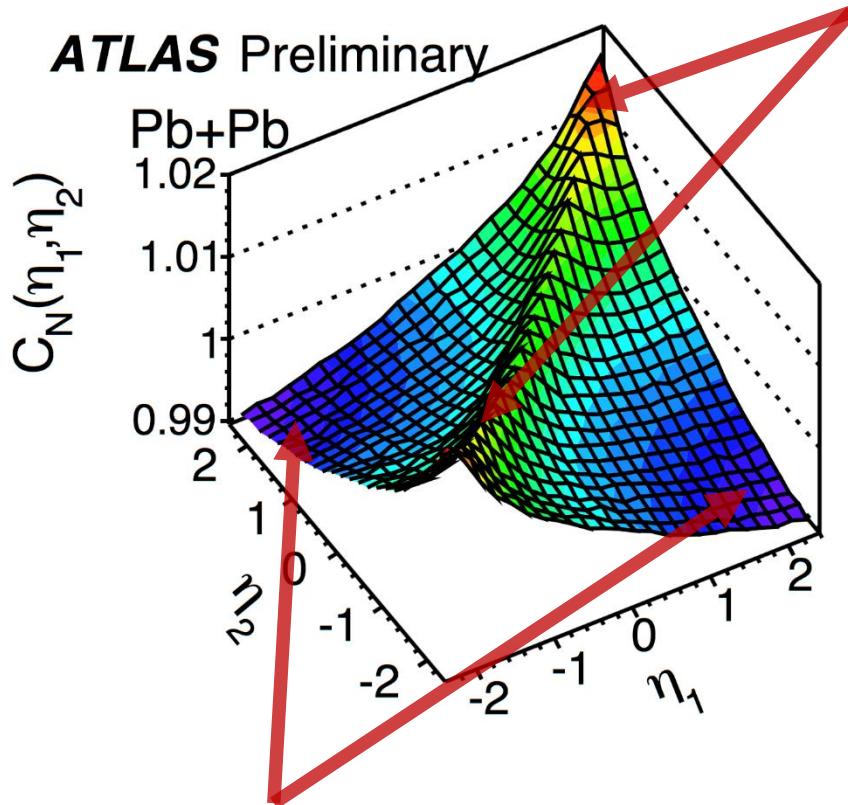
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Long-range correlation $C_{LRC}(\eta_1, \eta_2)$

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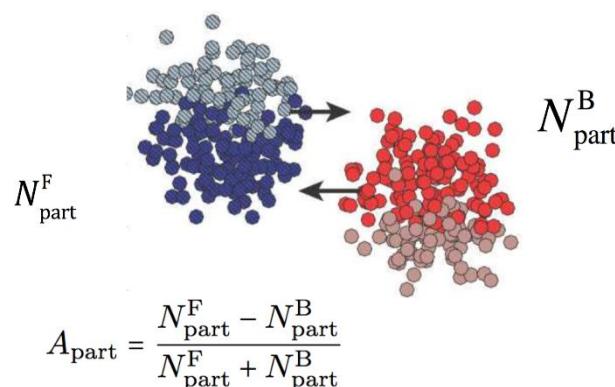
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- **Goal:** study the long-range correlation;
- **Challenge:** hard cut on $|\Delta\eta| < 2$ to suppress SRC will lose information.

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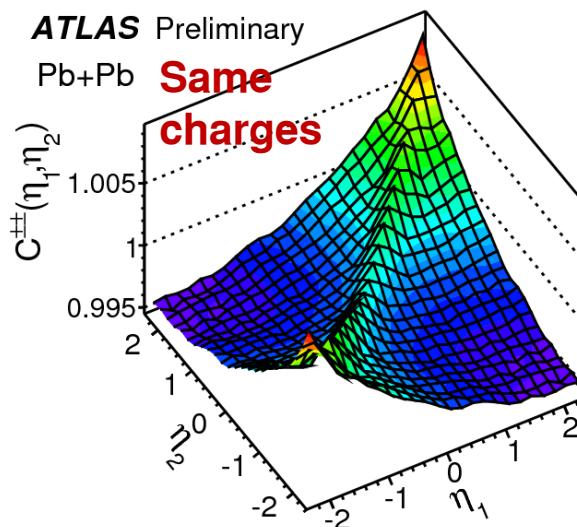
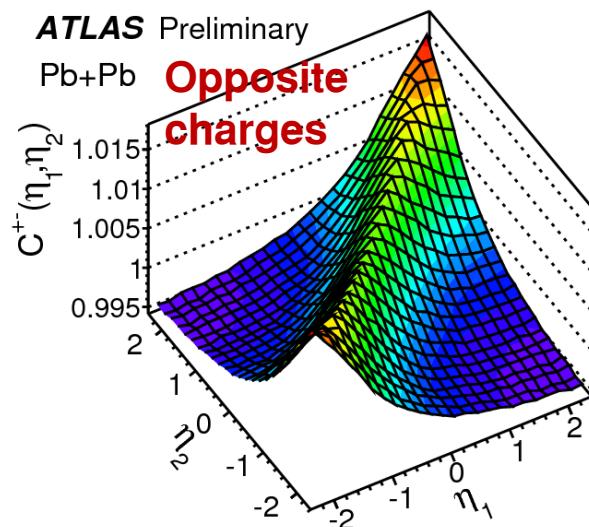
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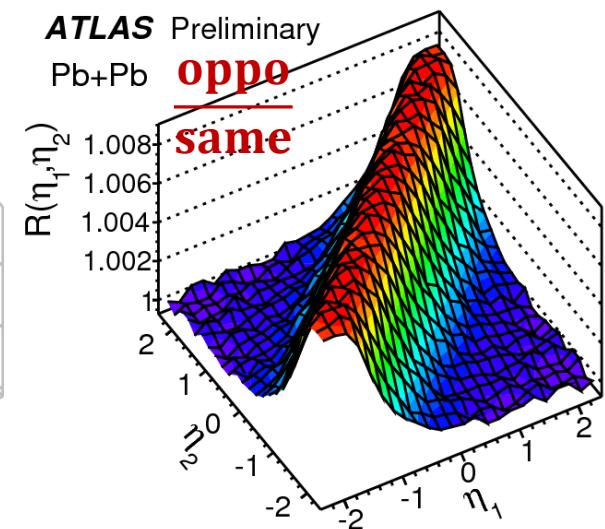
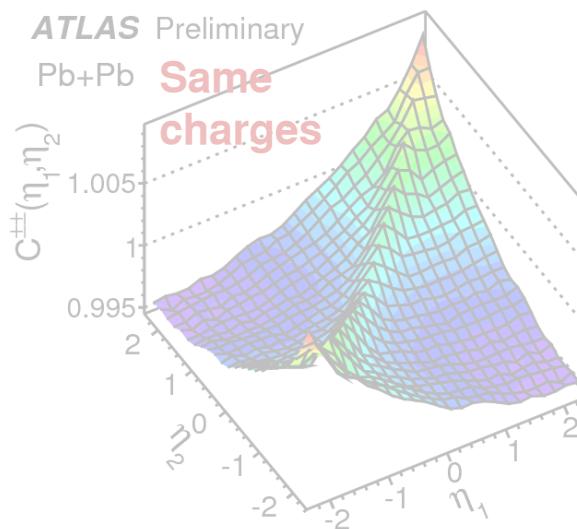
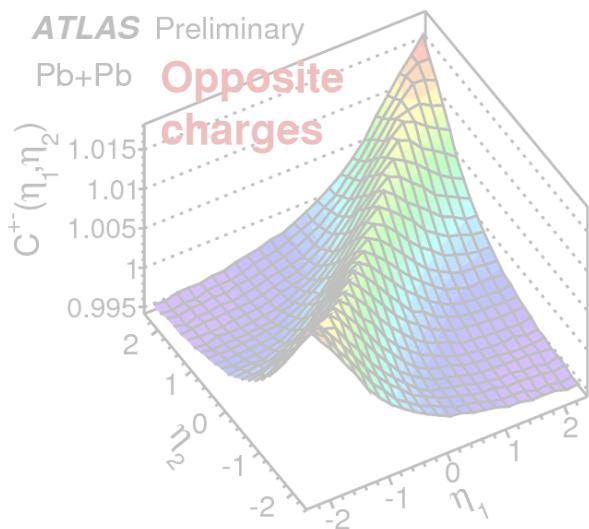
Charge dependence of $C(\eta_1, \eta_2)$

- Particles from the same source (SRC) have strong charge dependence.



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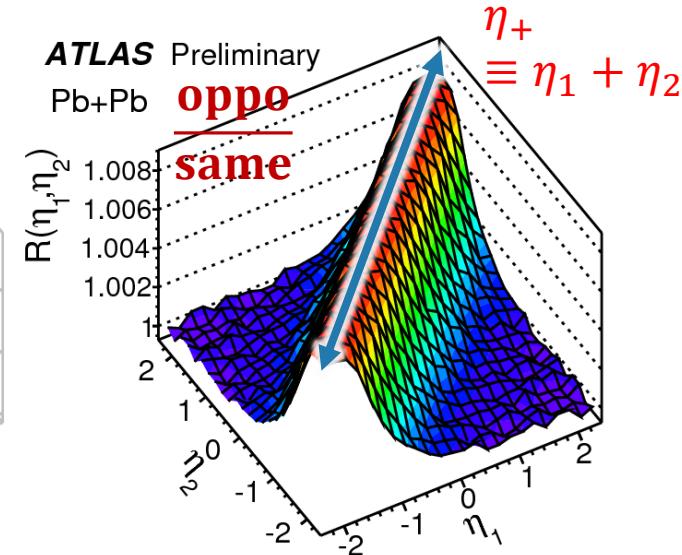
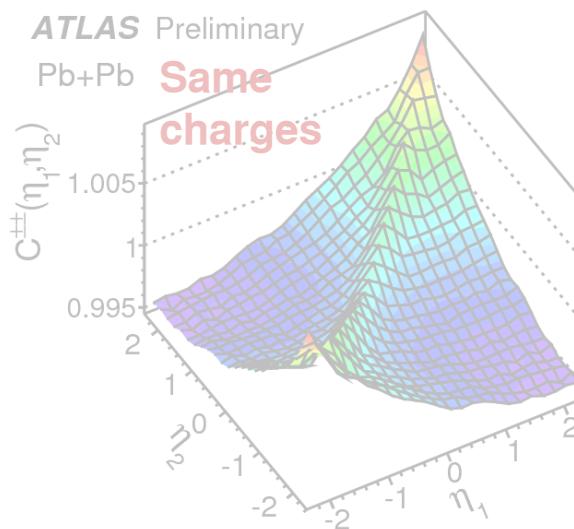
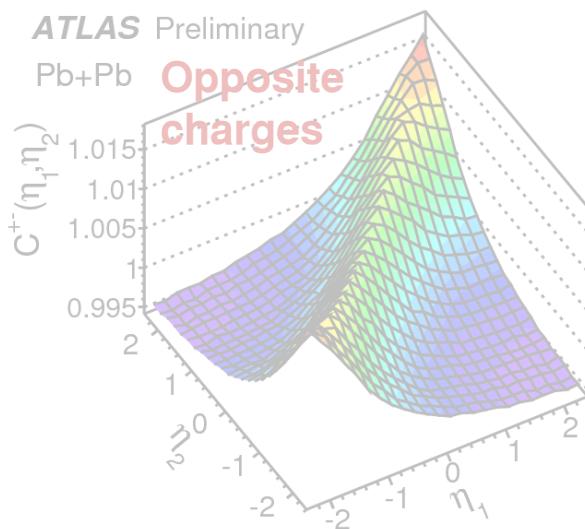
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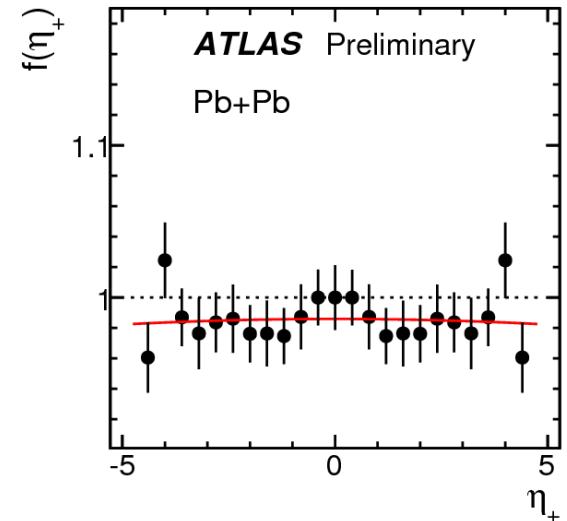
- Ratio of opposite to same charges $R(\eta_1, \eta_2)$
 - Very strong Gaussian-like SRC;
 - Very weak LRC: charge-independent;

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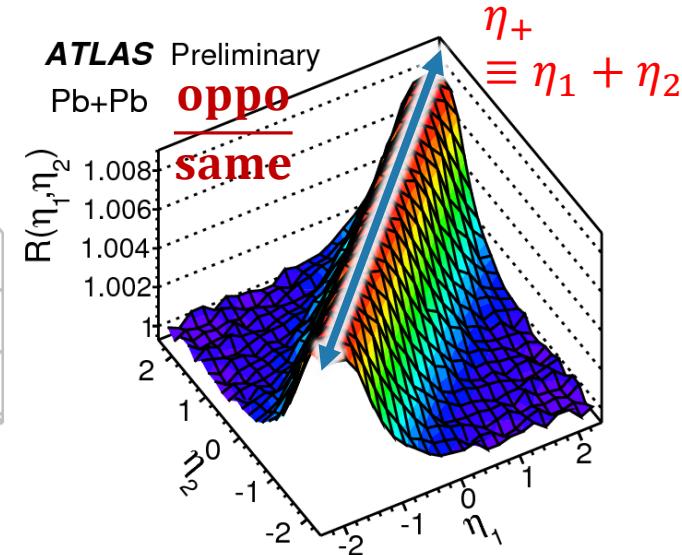
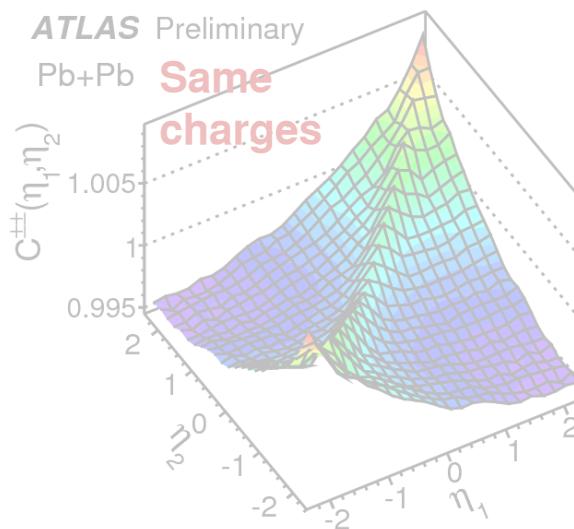
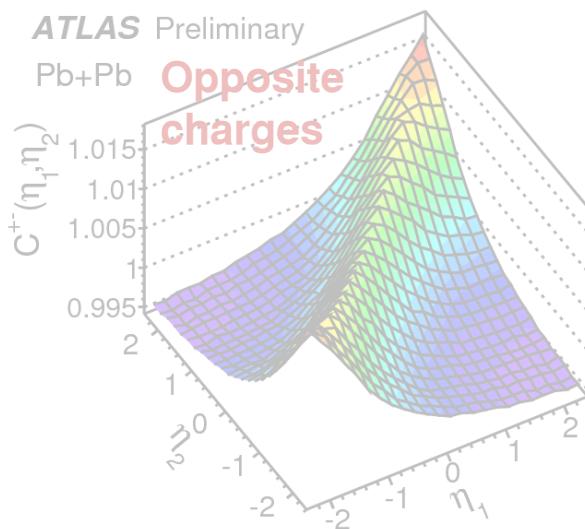


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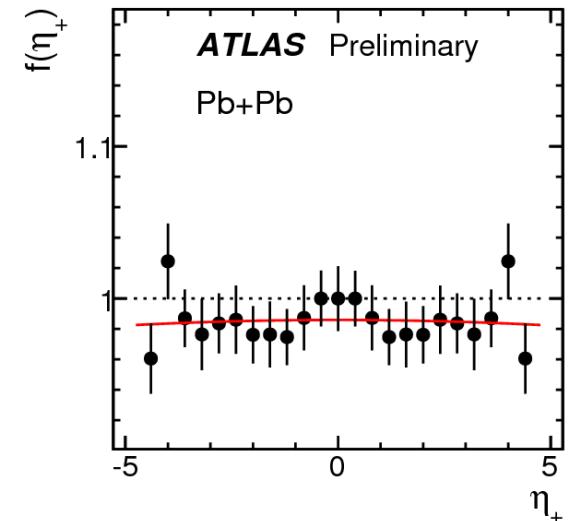


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- Amplitude of $R(\eta_1, \eta_2)$ along η_+ : $f(\eta_+)$, reflects the strength of SRC in the longitudinal direction;
- Assumption: strength of SRC along η_+ is same for same charge and opposite charge.



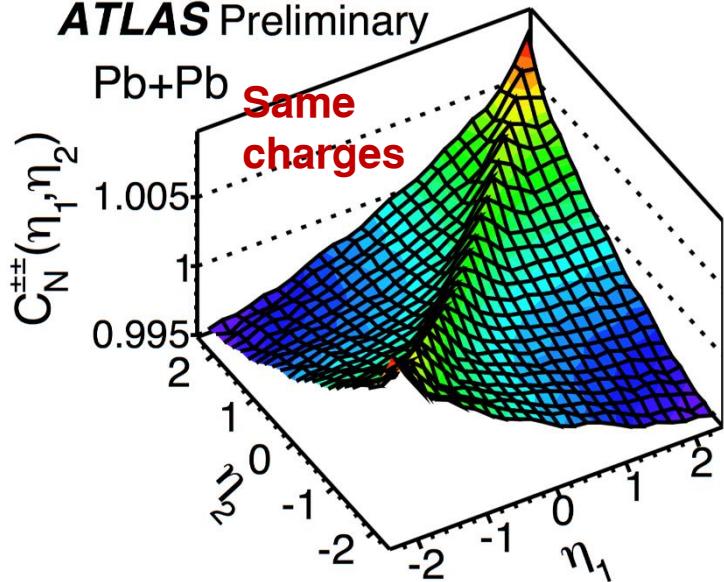
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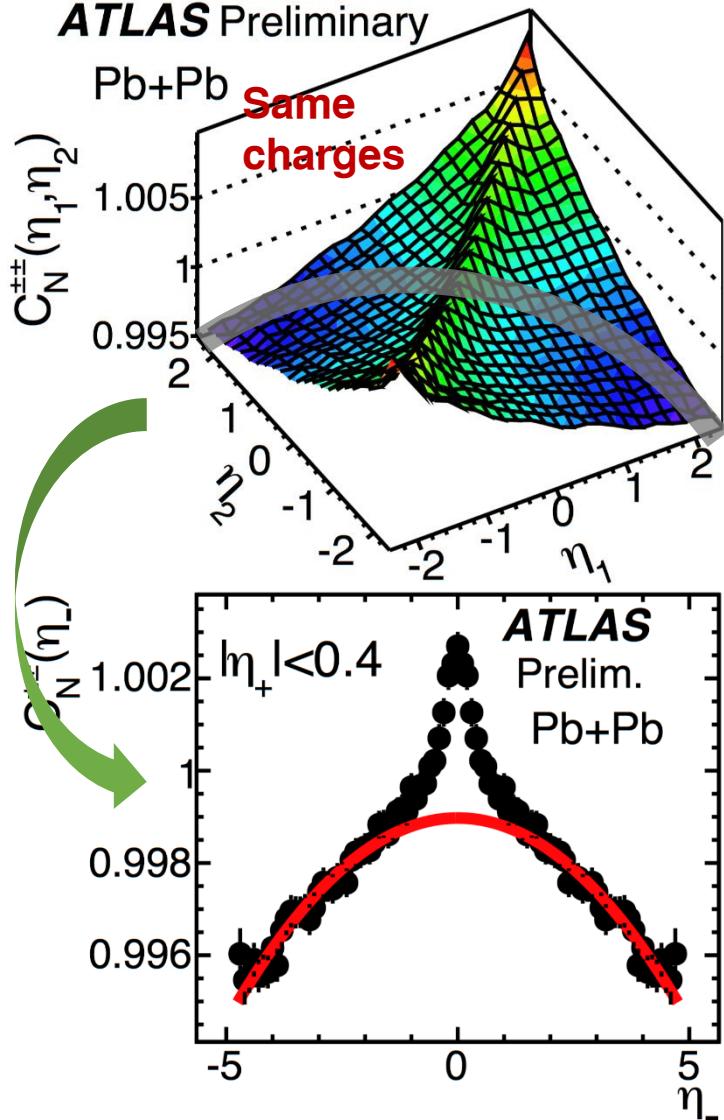
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Pb+Pb

Same
charges

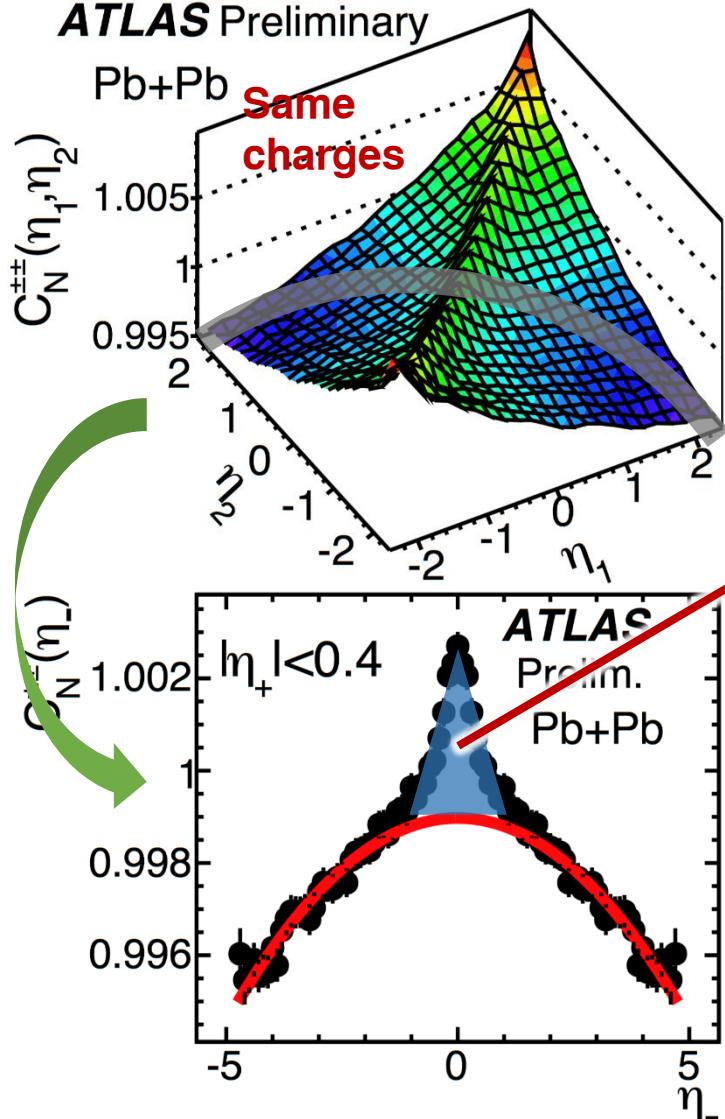


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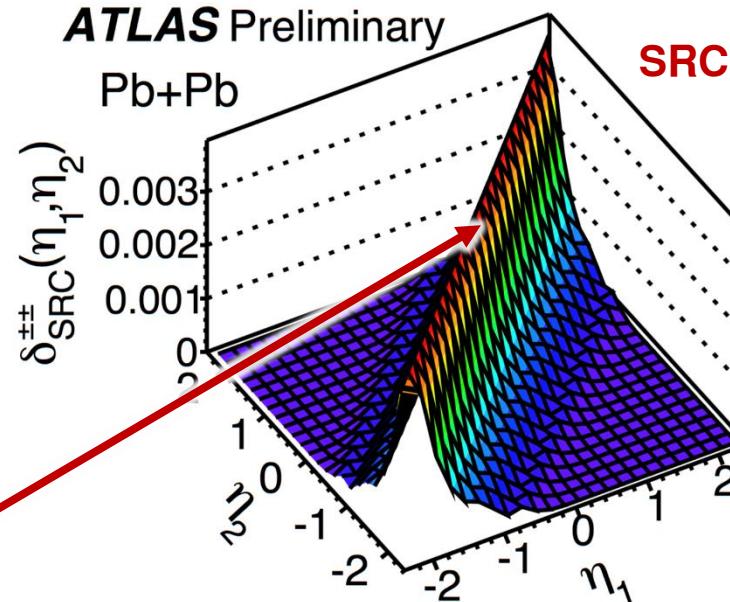
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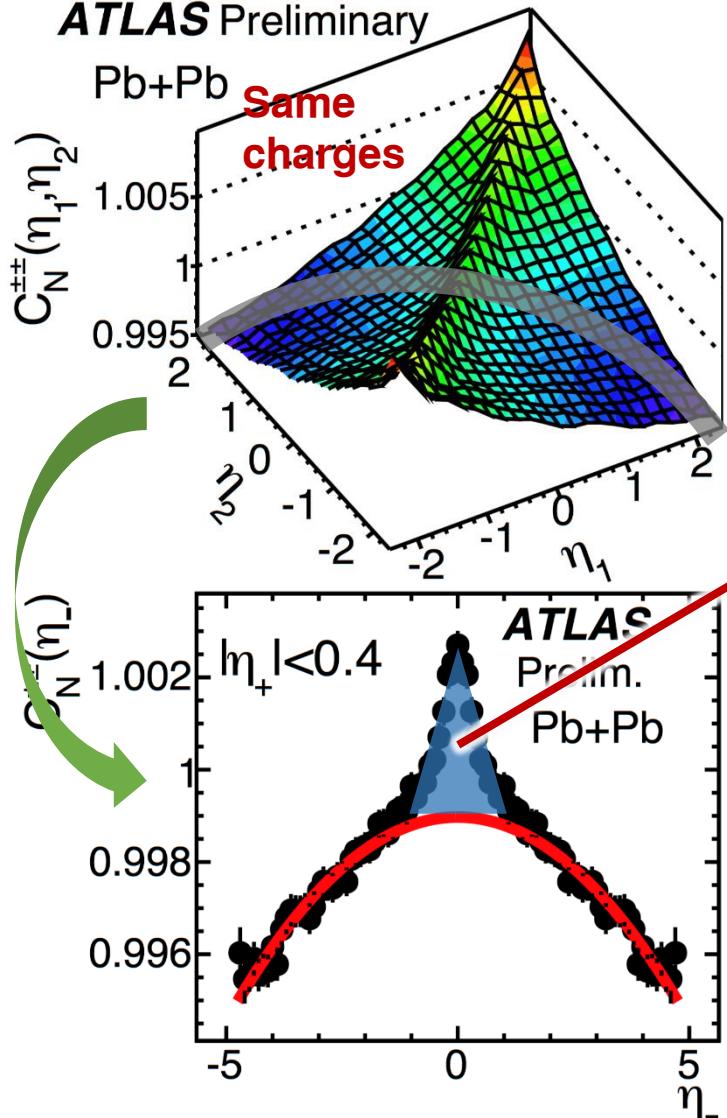


- $C(\eta_1, \eta_2)$ from same charge used to estimate LRC pedestal because of small SRC;
- LRC pedestal is fitted with quadratic function;
- The additional structure upon LRC pedestal determines the shape of SRC;

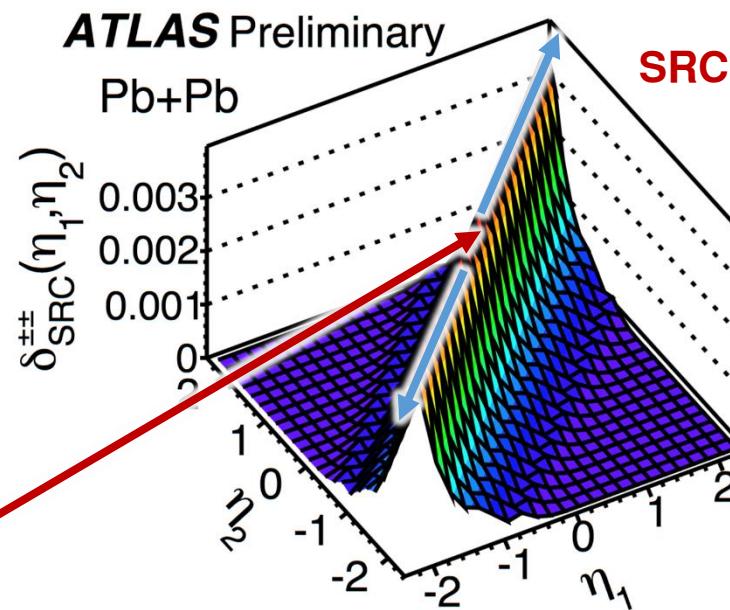
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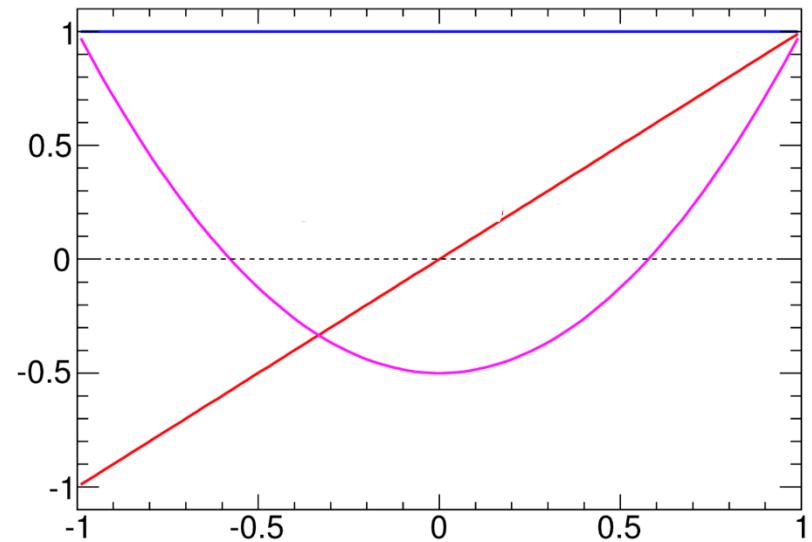


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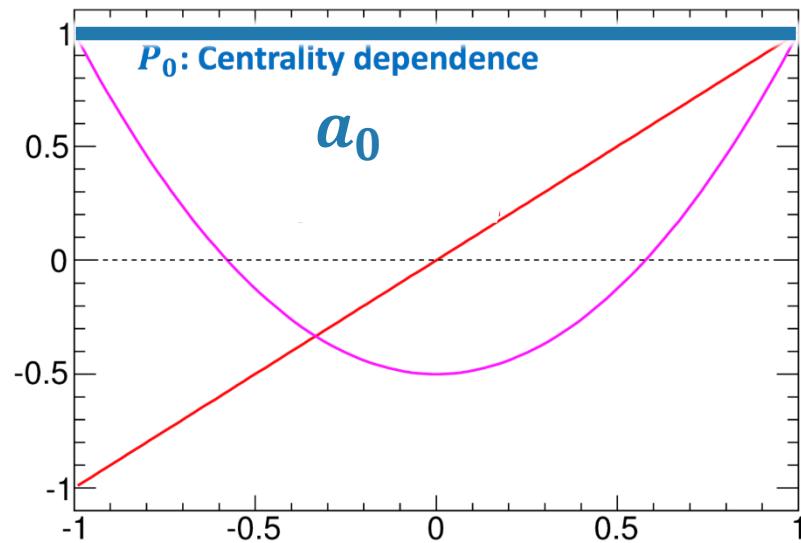


- $C(\eta_1, \eta_2)$ from same charge used to estimate LRC pedestal because of small SRC;
- LRC pedestal is fitted with quadratic function;
- The additional structure upon LRC pedestal determines the shape of SRC;
- The full $\delta_{SRC}(\eta_1, \eta_2)$ is then populated using $f(\eta_+)$ scaling.

Quantify shape fluctuation: Legendre expansion



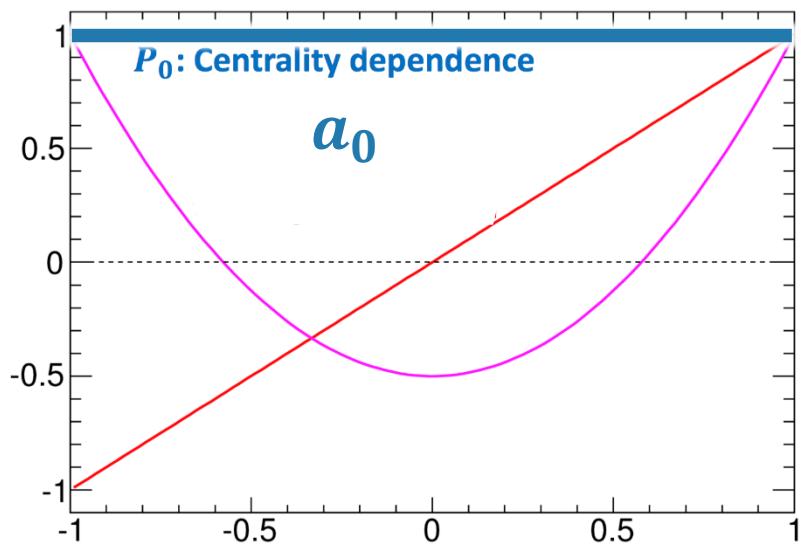
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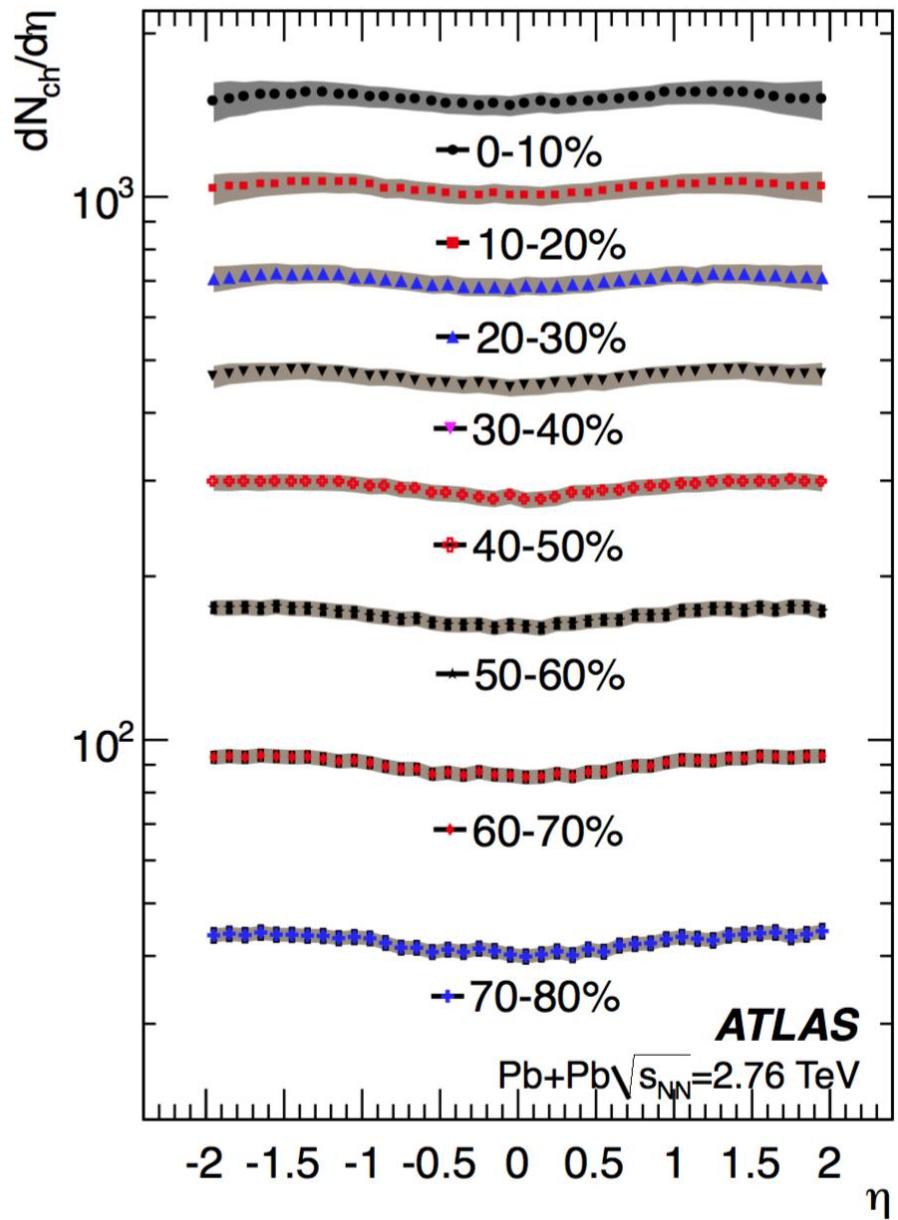
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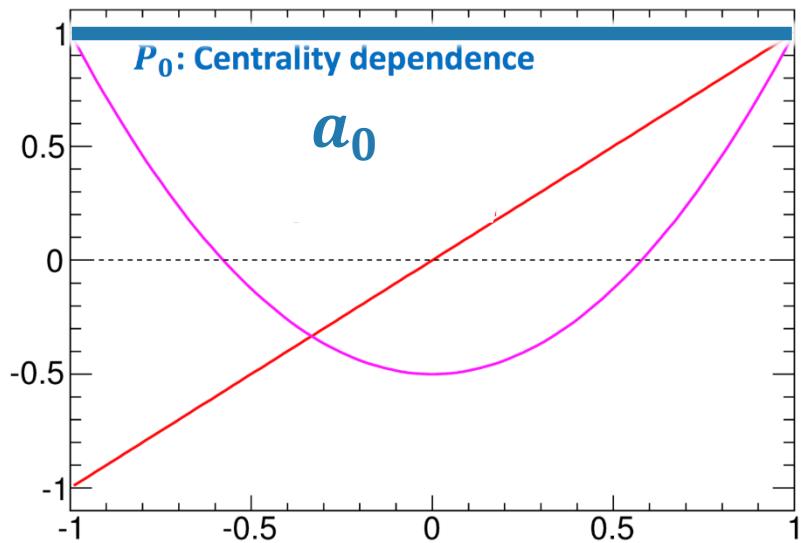
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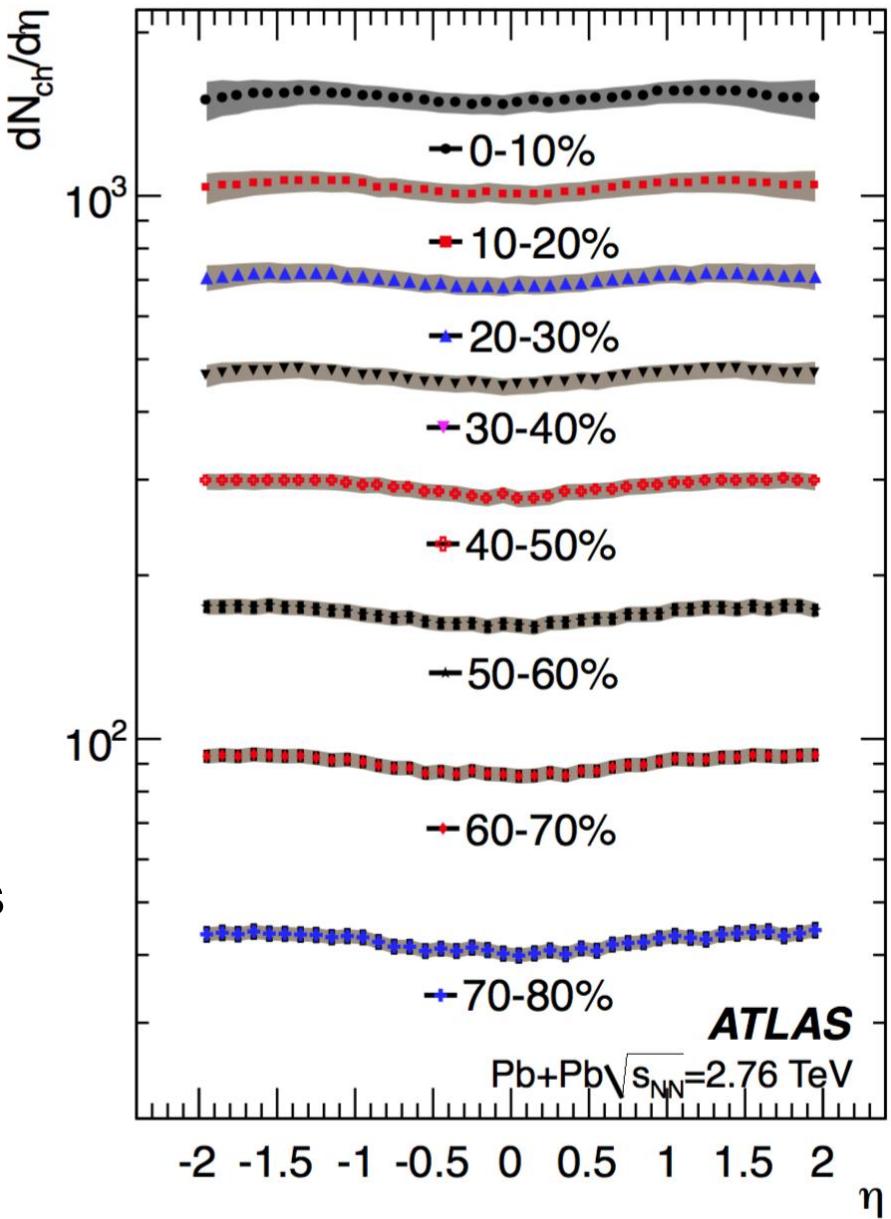


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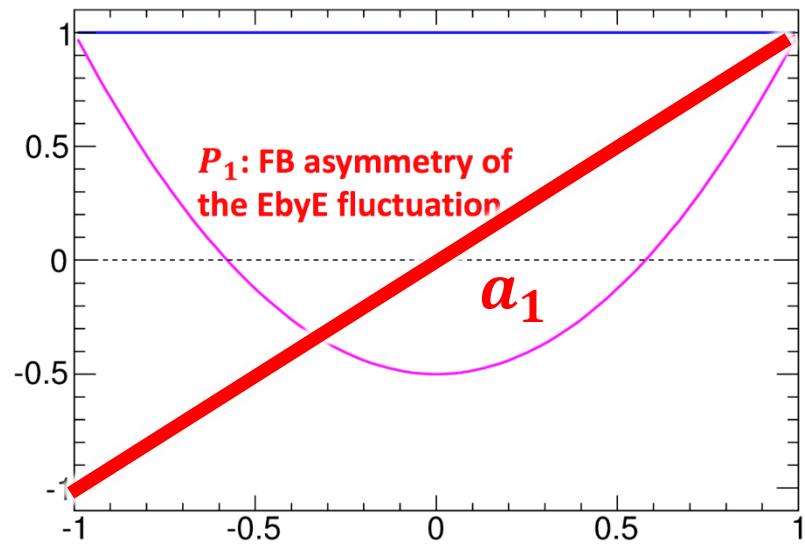


- Analysis focuses on dynamical fluctuation upon average;
- However, average multiplicity changes with centrality;
- The residual centrality dependence is removed by normalizing $C(\eta_1, \eta_2)$

$$C_N(\eta_1, \eta_2) = \frac{C(\eta_1, \eta_2)}{C_p(\eta_1)C_p(\eta_2)}$$

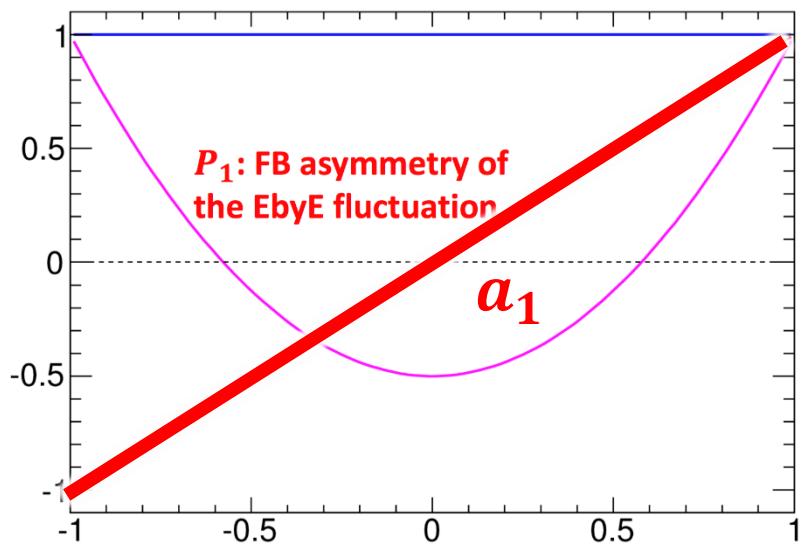


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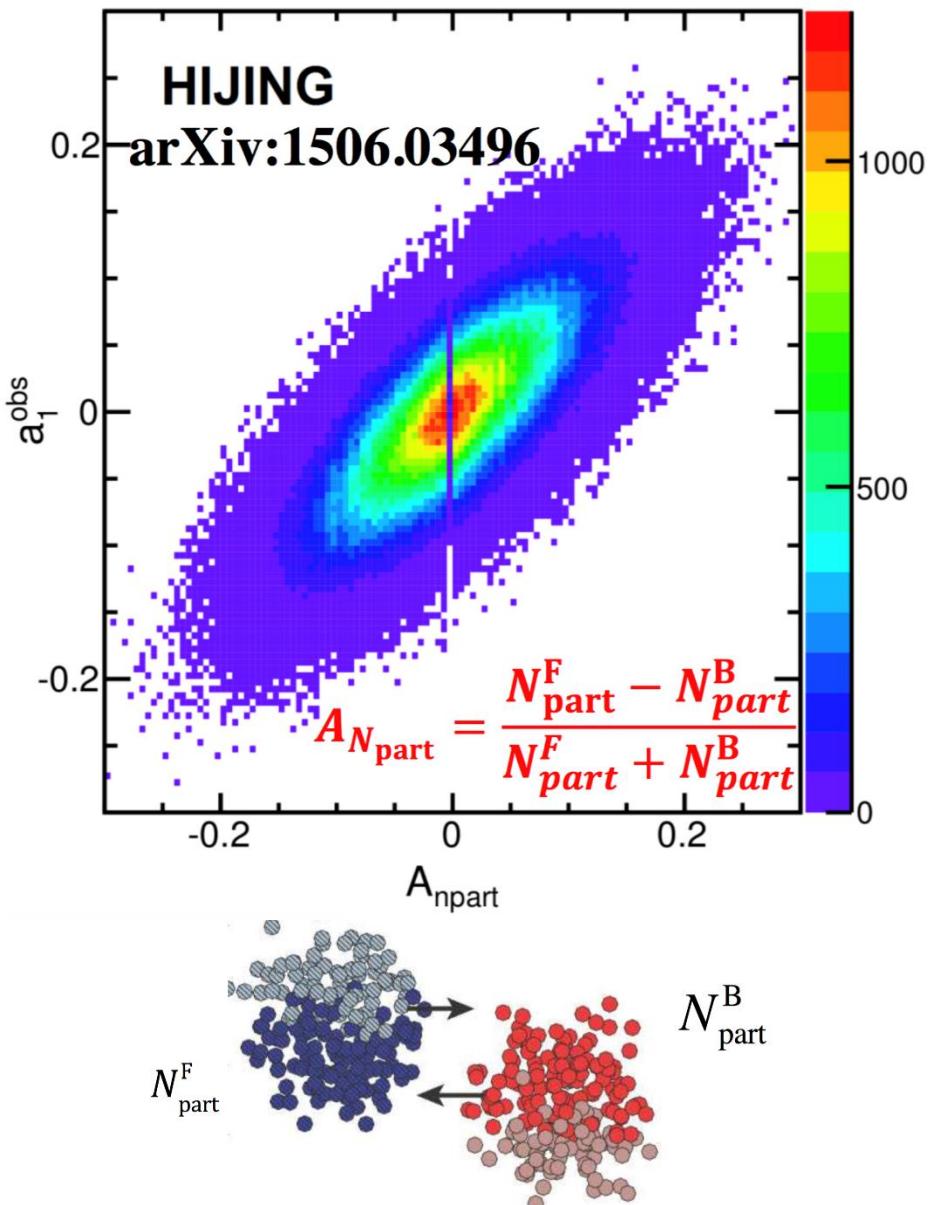


- The linear shape quantifies the FB multiplicity asymmetry;

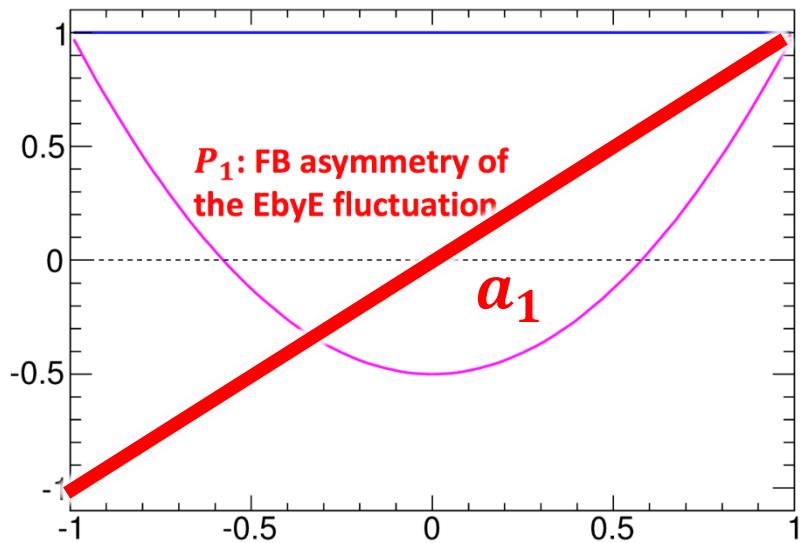
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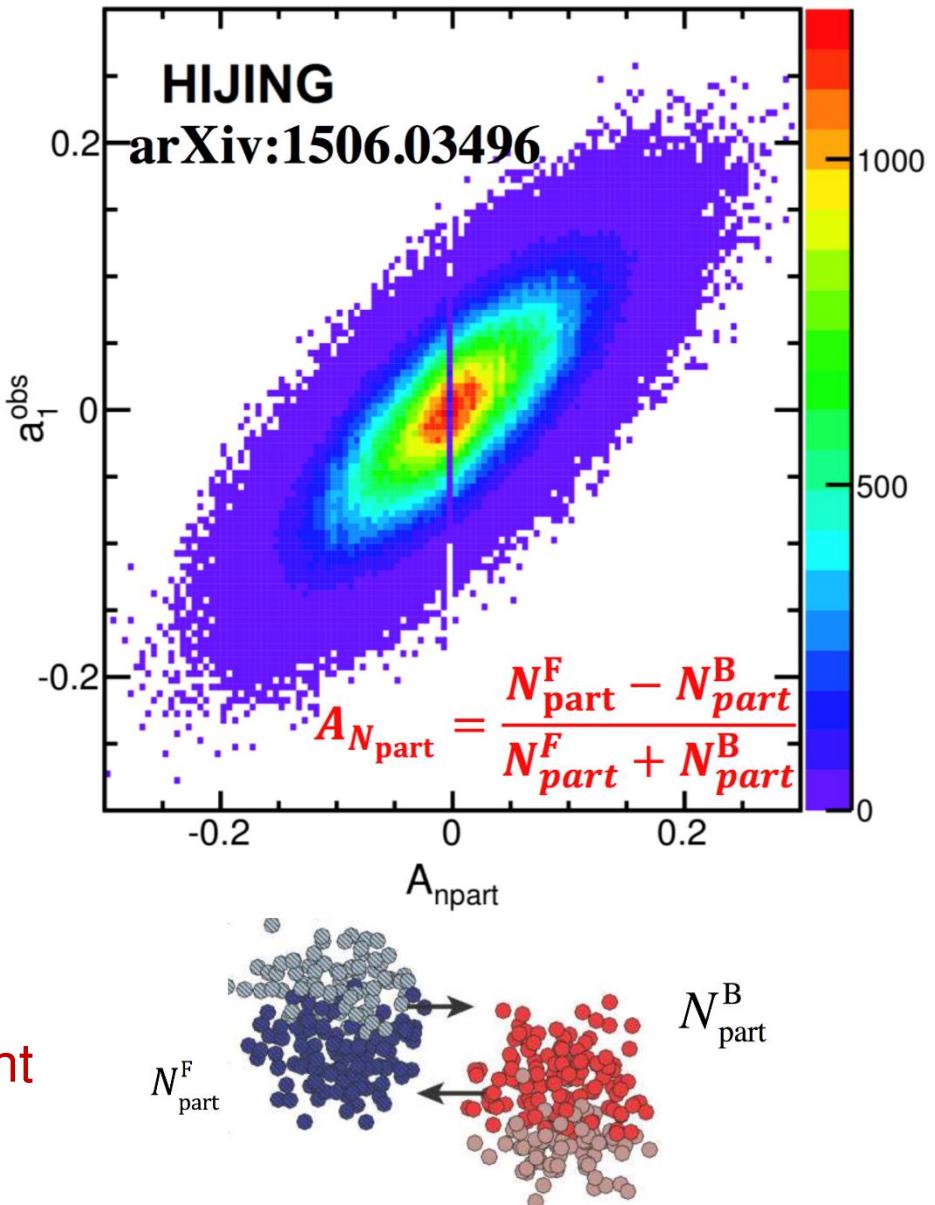
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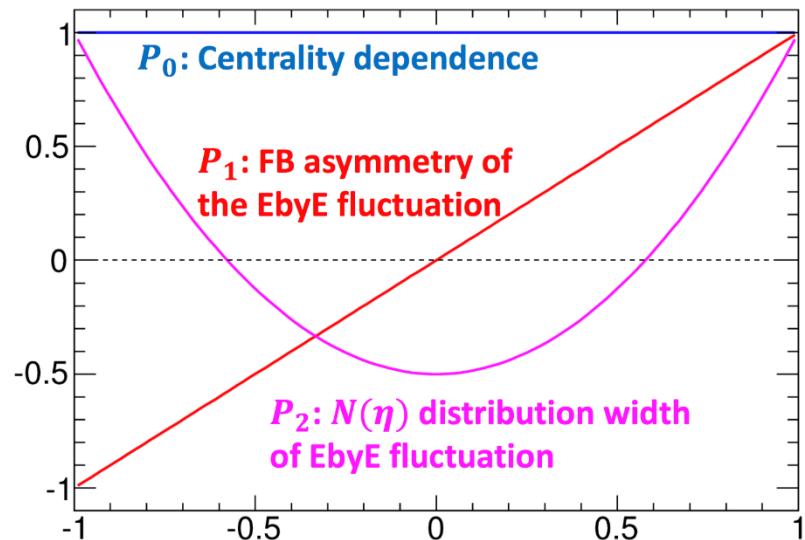
Quantify shape fluctuation: Legendre expansion



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- As will be shown later, this component dominates the shape fluctuation.



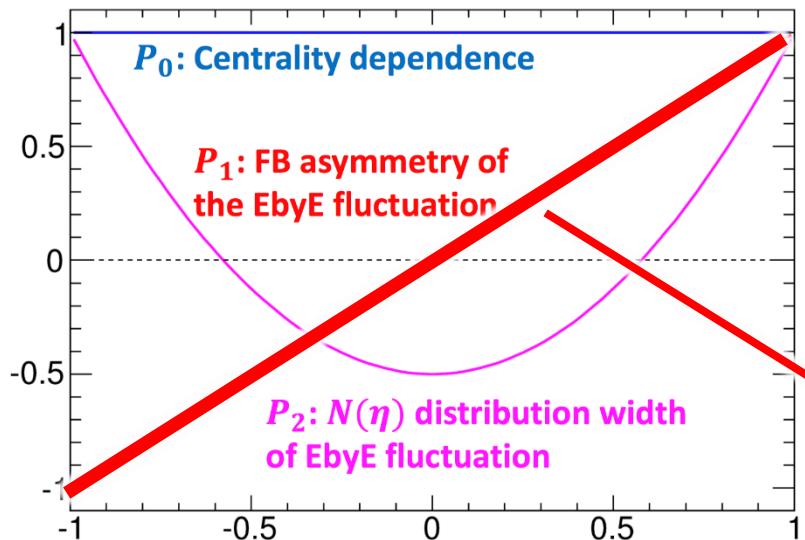
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- Expansion of correlation function $C_N(\eta_1, \eta_2)$

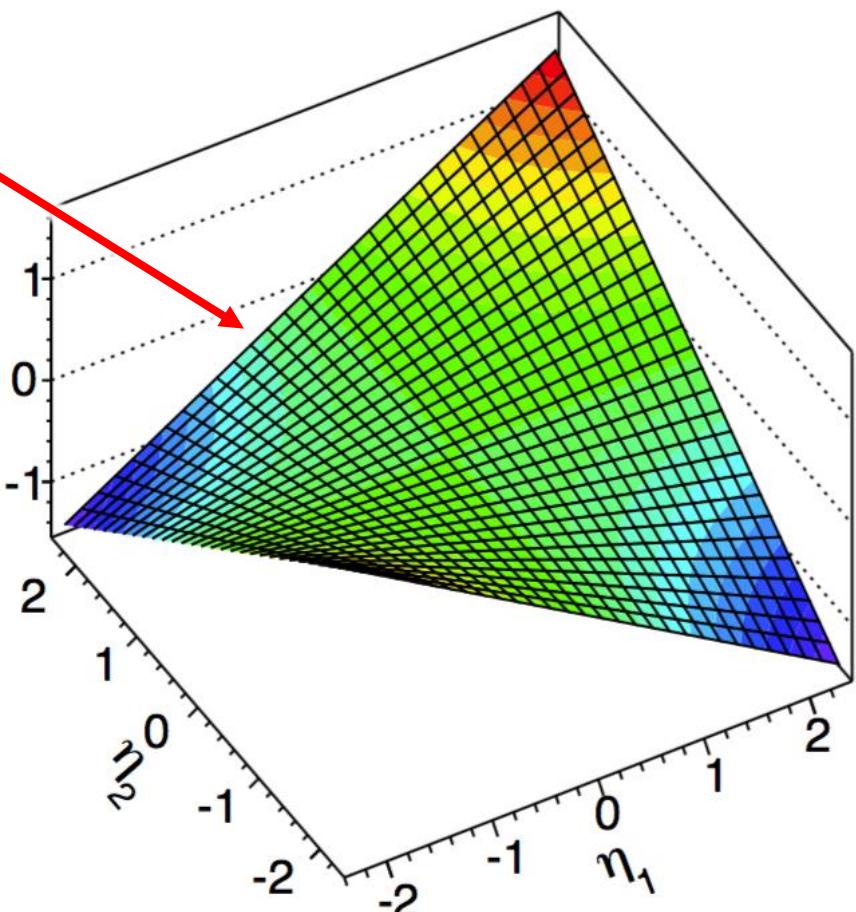
$$1 + \sum_{n,m=1}^{\infty} \langle a_n a_m \rangle \frac{T_n(\eta_1)T_m(\eta_2) + T_n(\eta_2)T_m(\eta_1)}{2}$$

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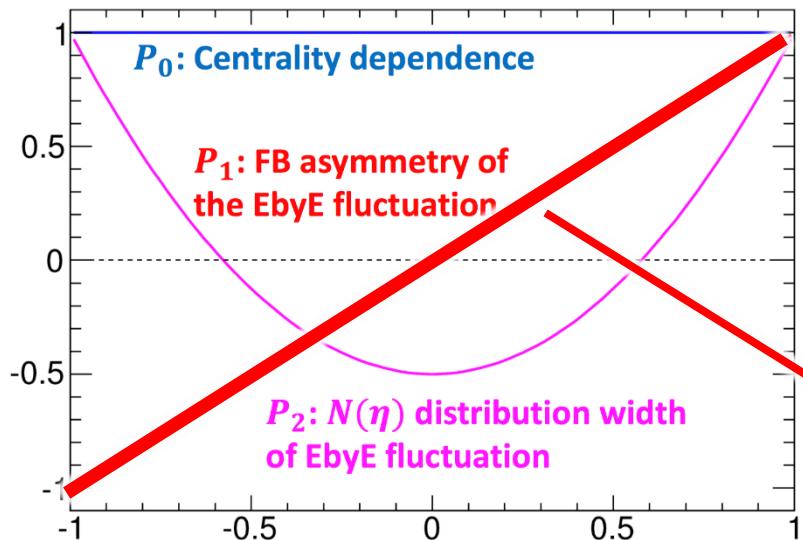
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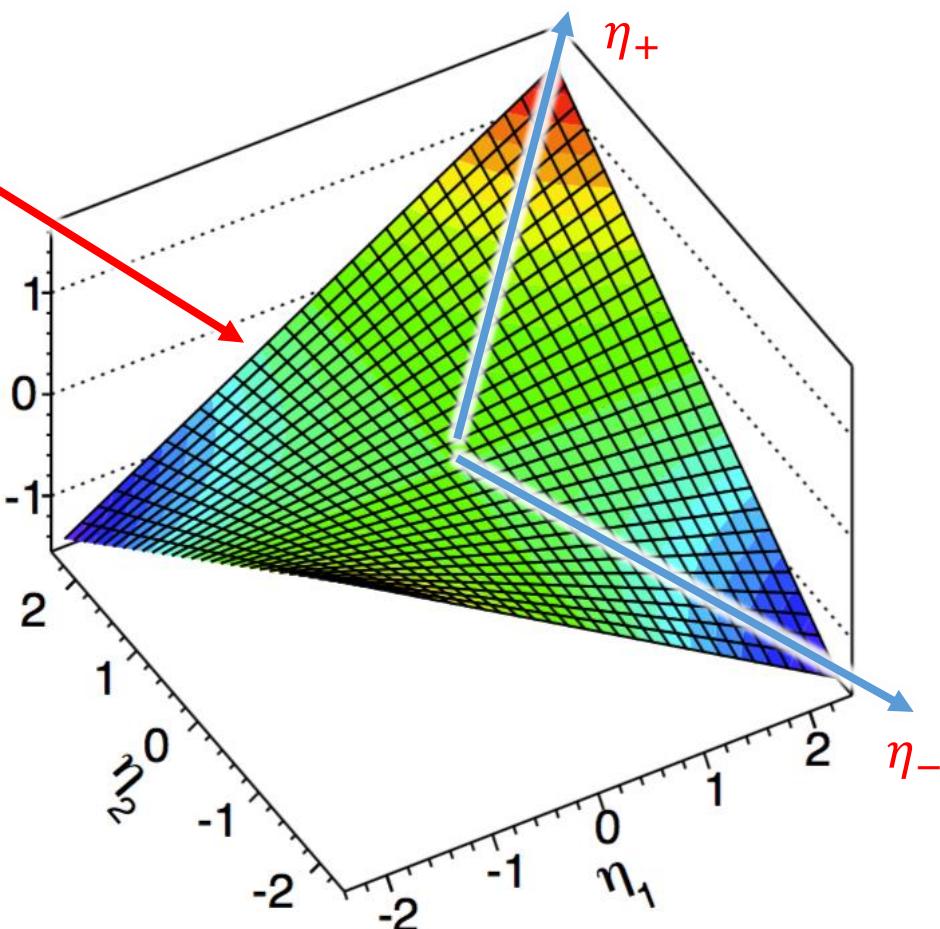
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- Expressed as η_+ and η_- :

$$C_N(\eta_1, \eta_2) = 1 + \frac{\langle a_1^2 \rangle}{4} (\eta_+^2 - \eta_-^2)$$

Results: correlation functions

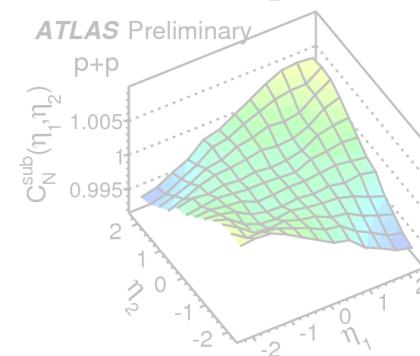
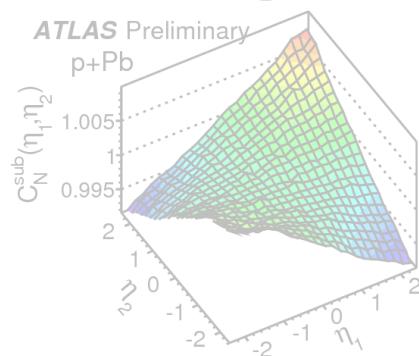
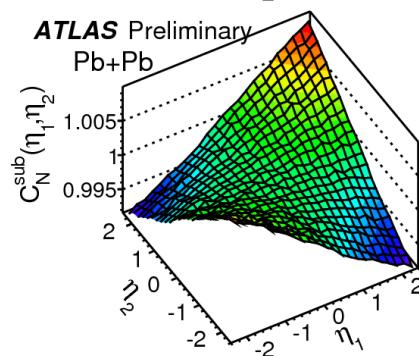
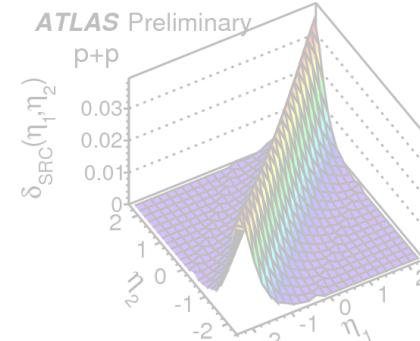
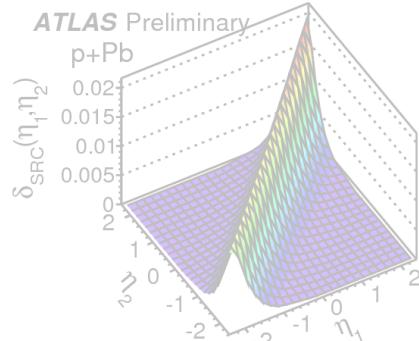
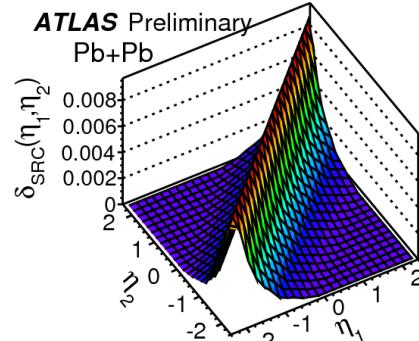
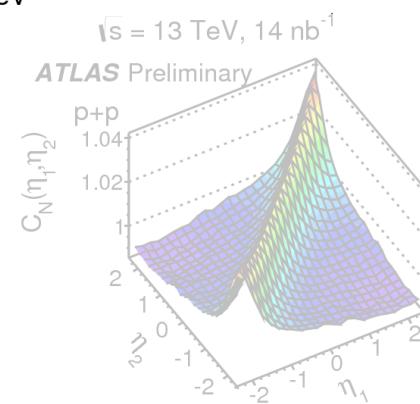
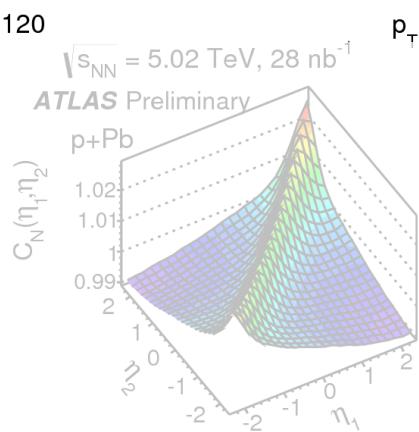
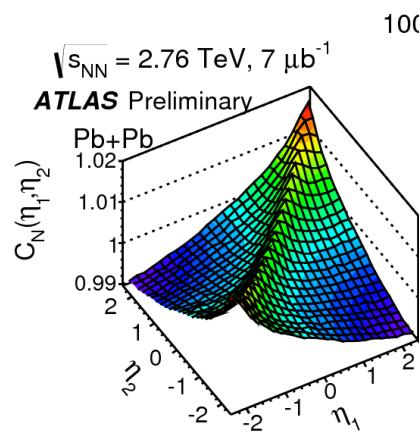
Raw
 $C_N(\eta_1, \eta_2)$

||

Short-range
 $\delta_{SRC}(\eta_1, \eta_2)$

+

Long-range
 $C_N^{sub}(\eta_1, \eta_2)$



Pb+Pb

p+Pb

pp

Initial Stages 2016, Lisbon

Results: correlation functions

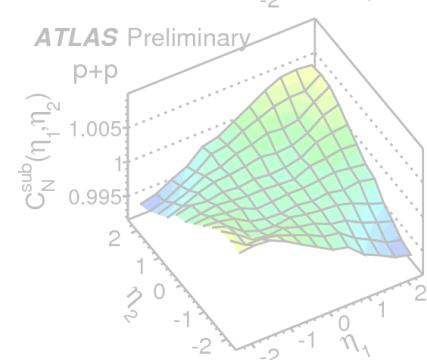
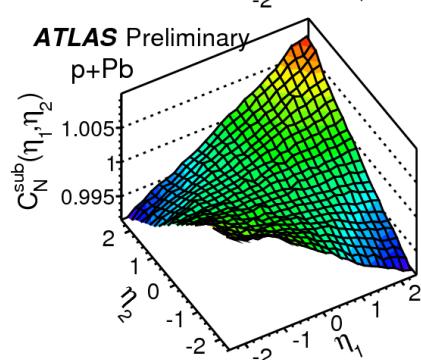
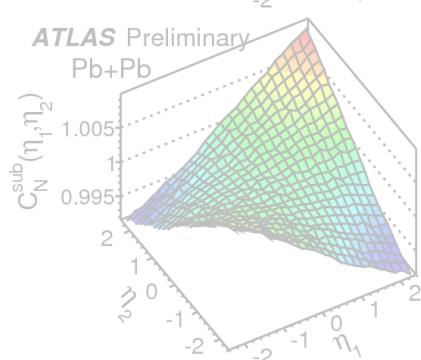
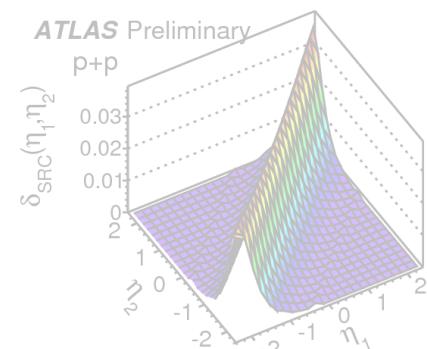
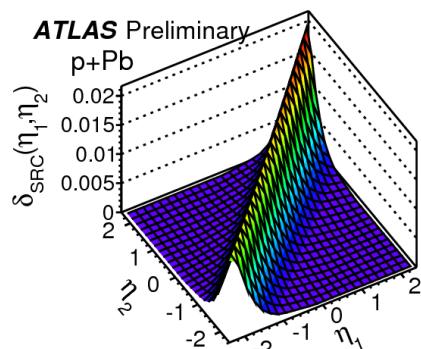
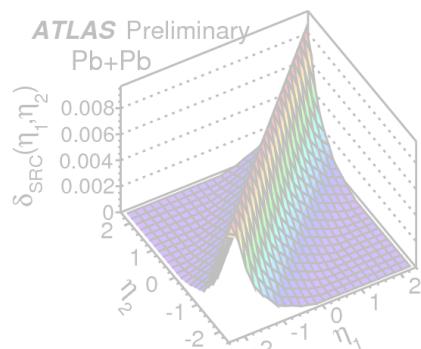
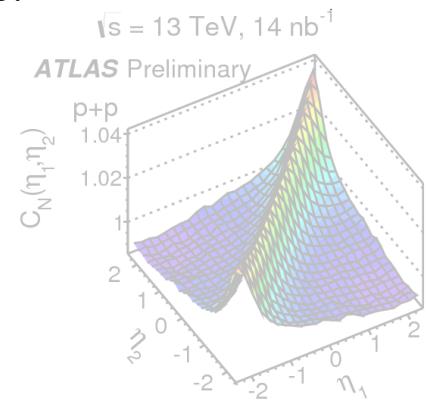
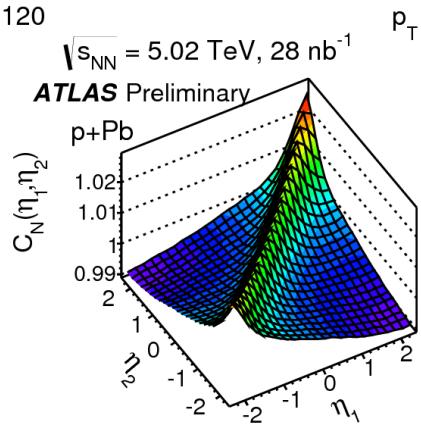
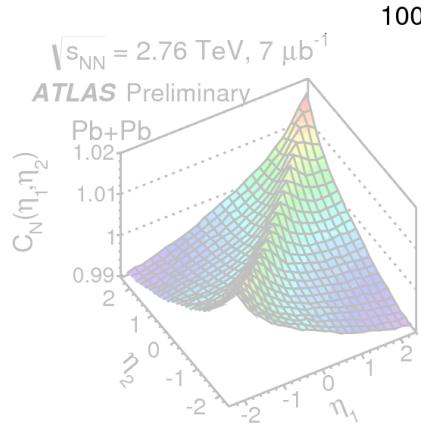
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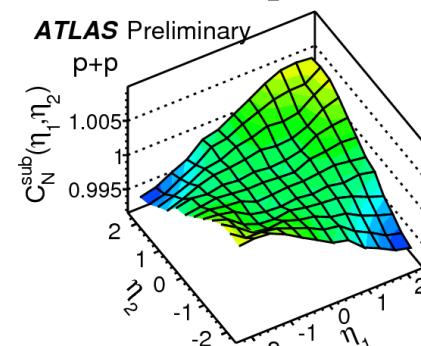
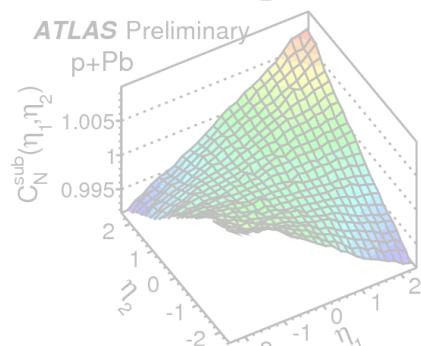
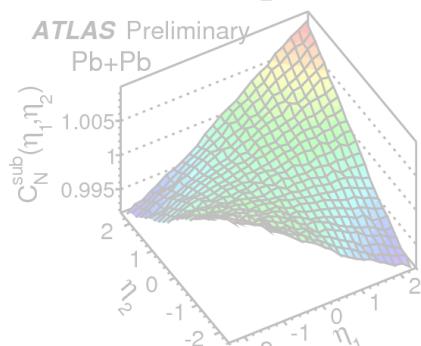
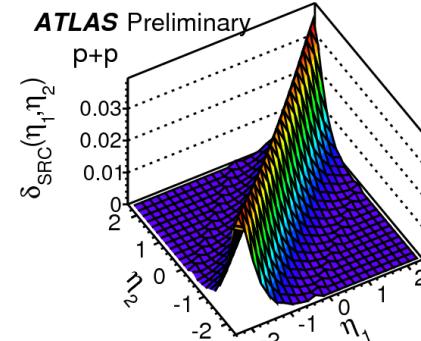
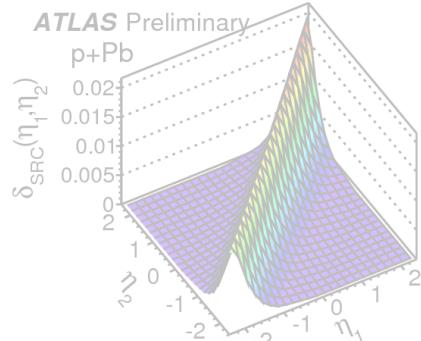
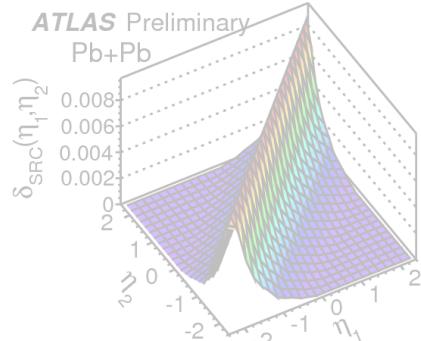
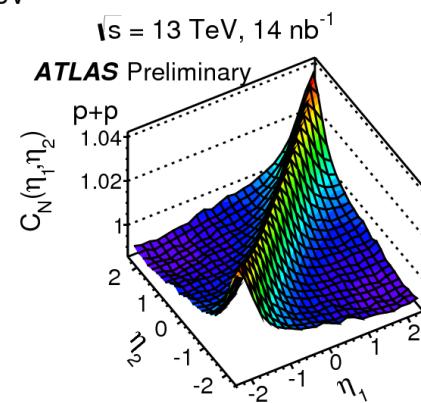
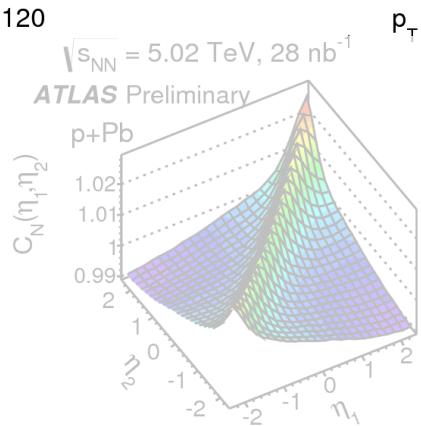
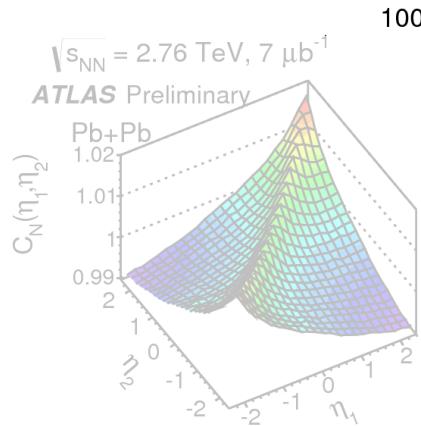
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Initial Stages 2016, Lisbon

Results: correlation functions

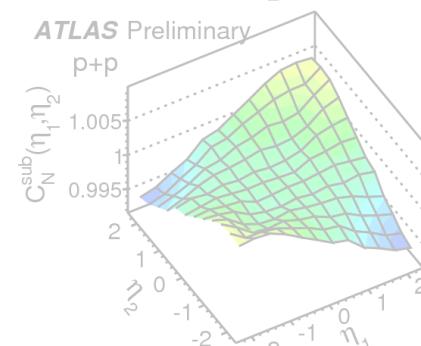
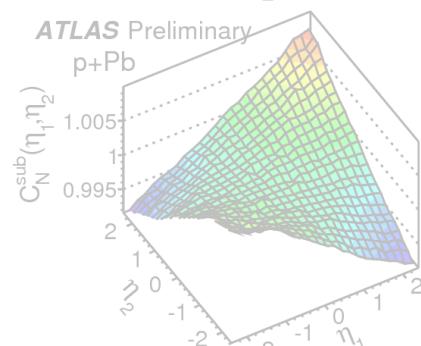
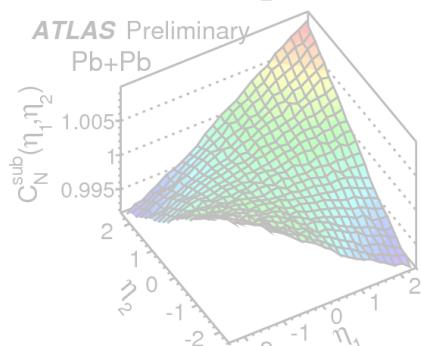
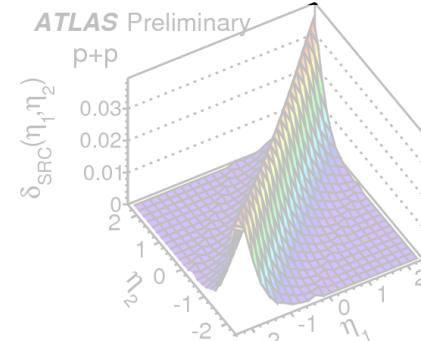
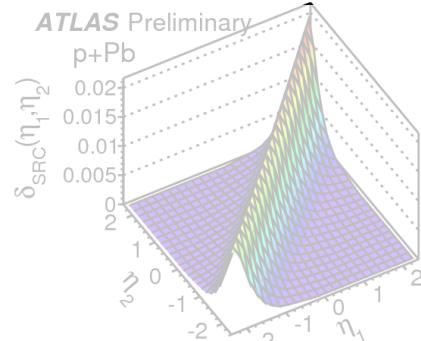
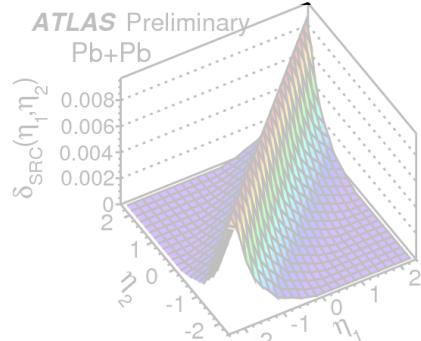
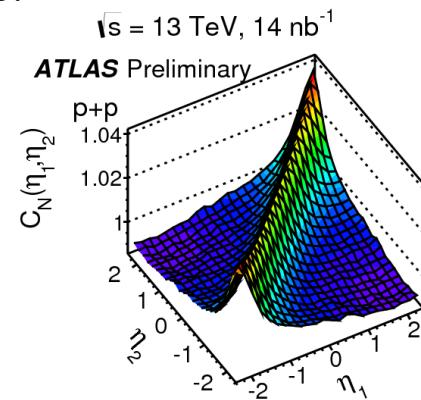
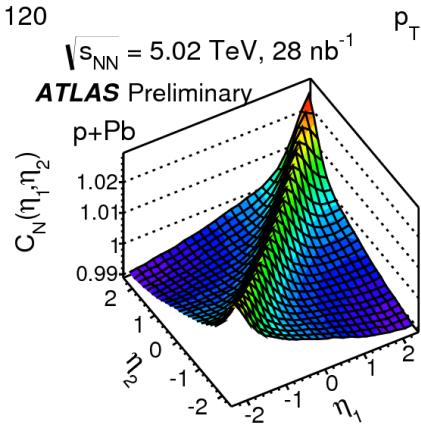
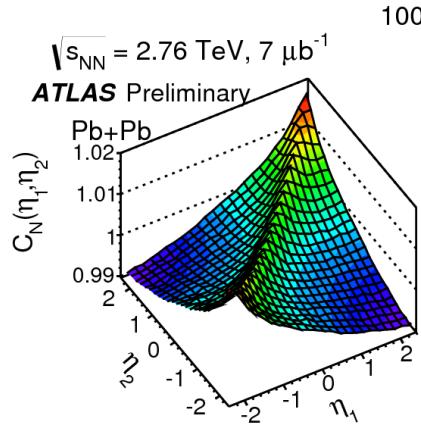
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Results: correlation functions

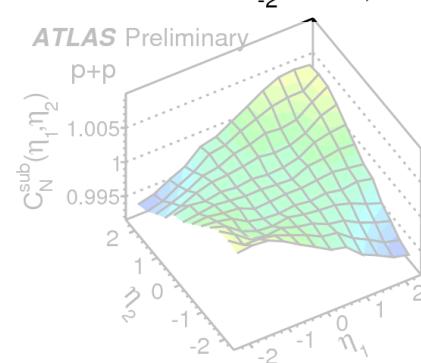
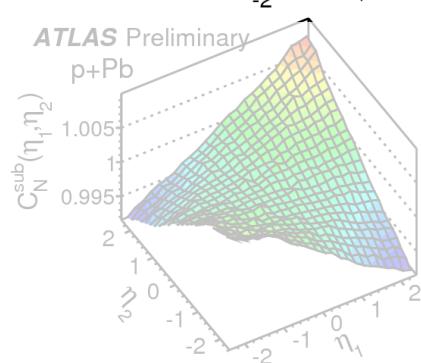
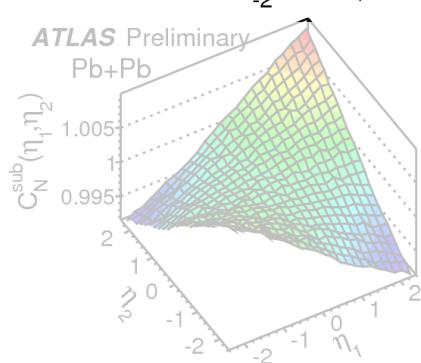
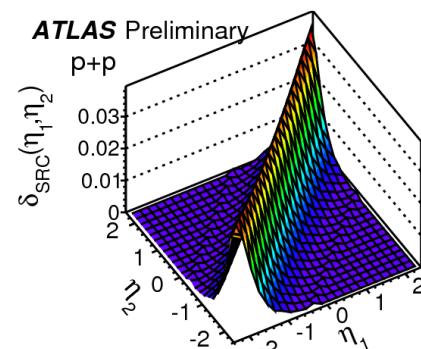
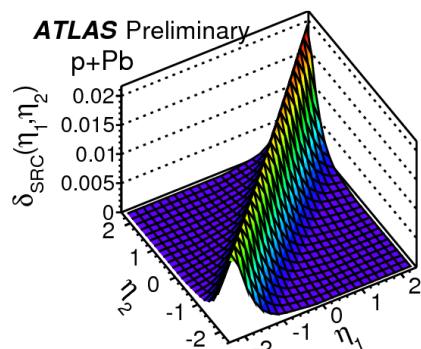
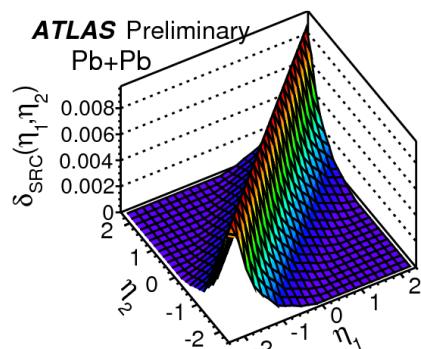
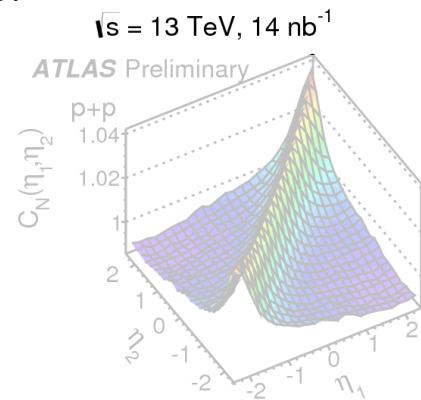
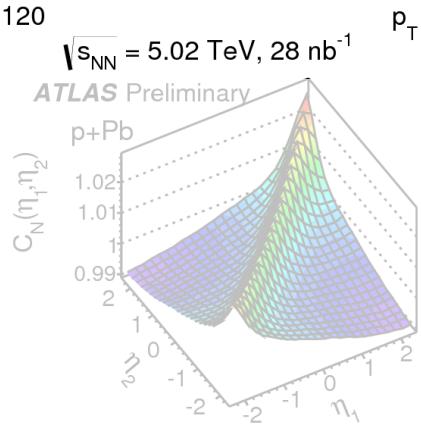
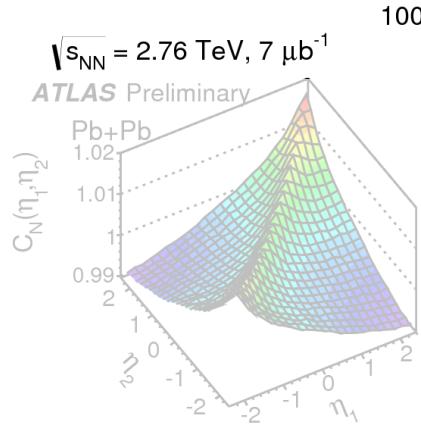
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Pb+Pb

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pp

Initial Stages 2016, Lisbon

Results: correlation functions

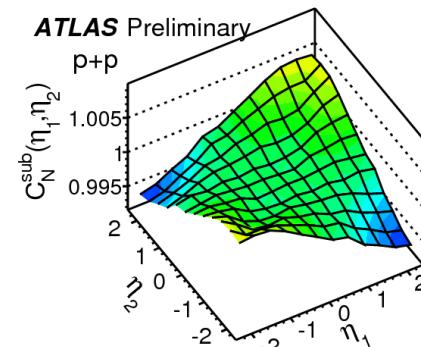
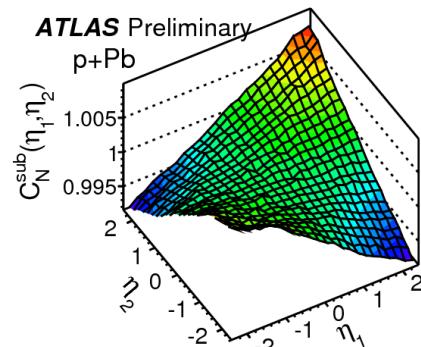
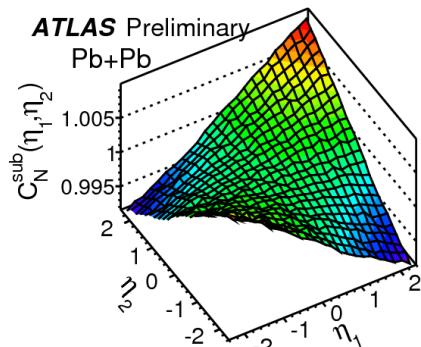
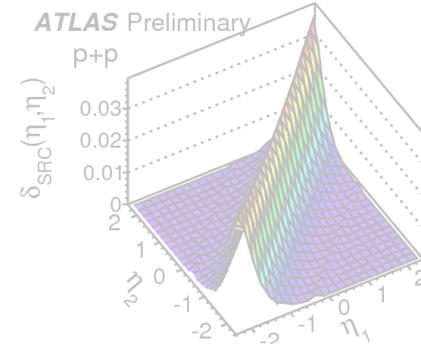
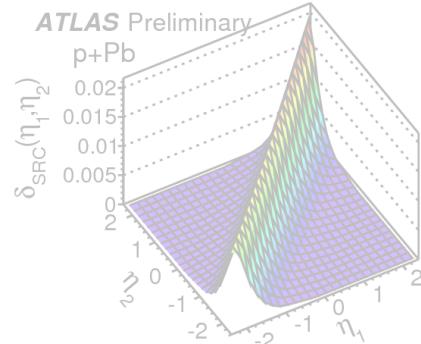
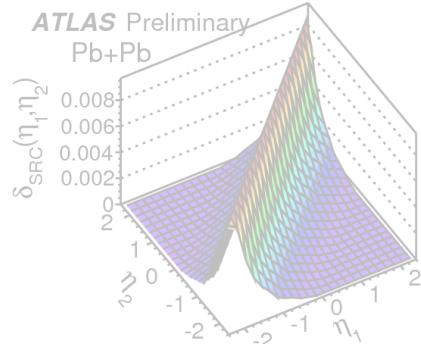
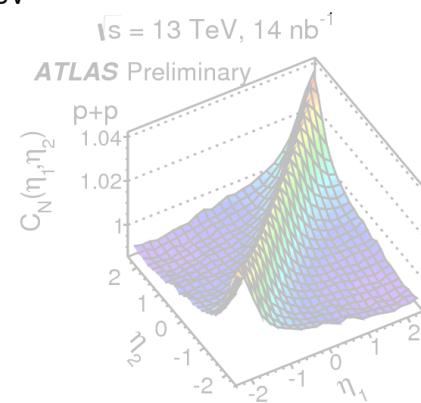
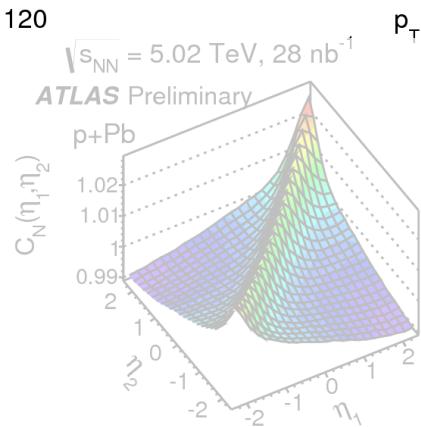
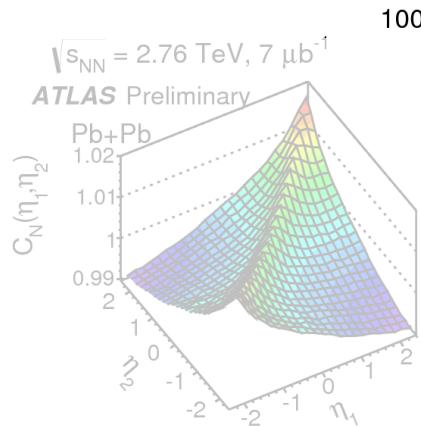
Raw
 $C_N(\eta_1, \eta_2)$

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Short-range
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+

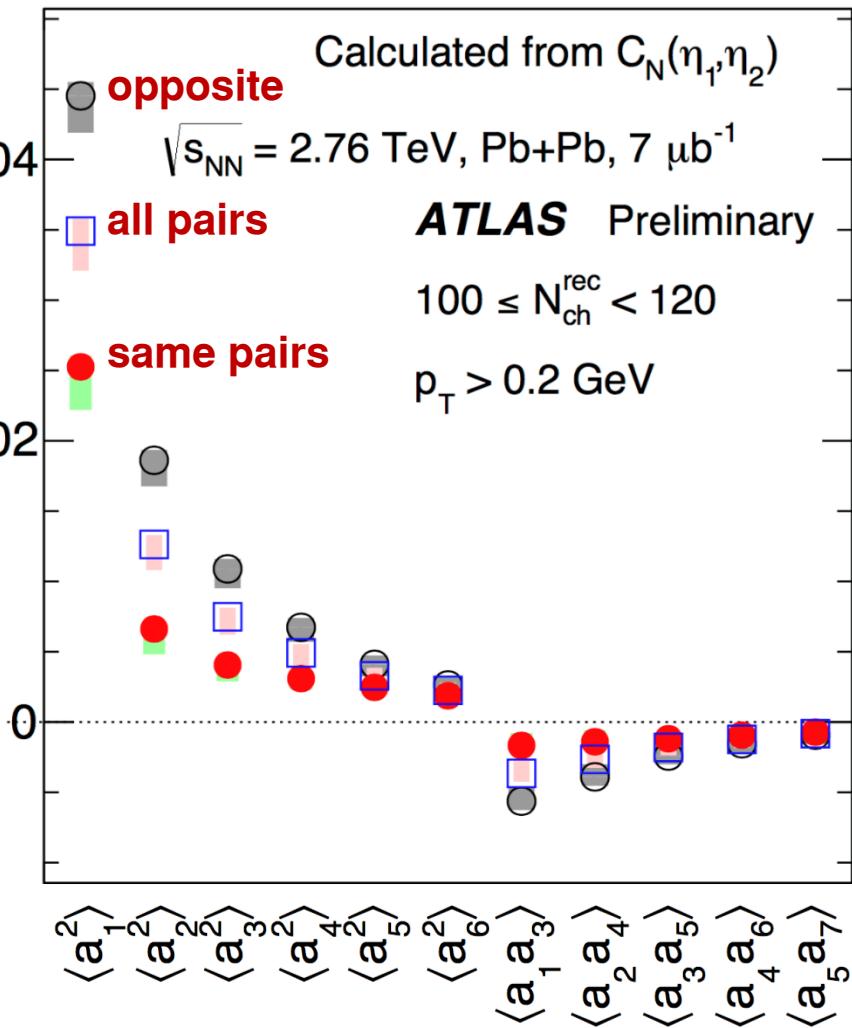
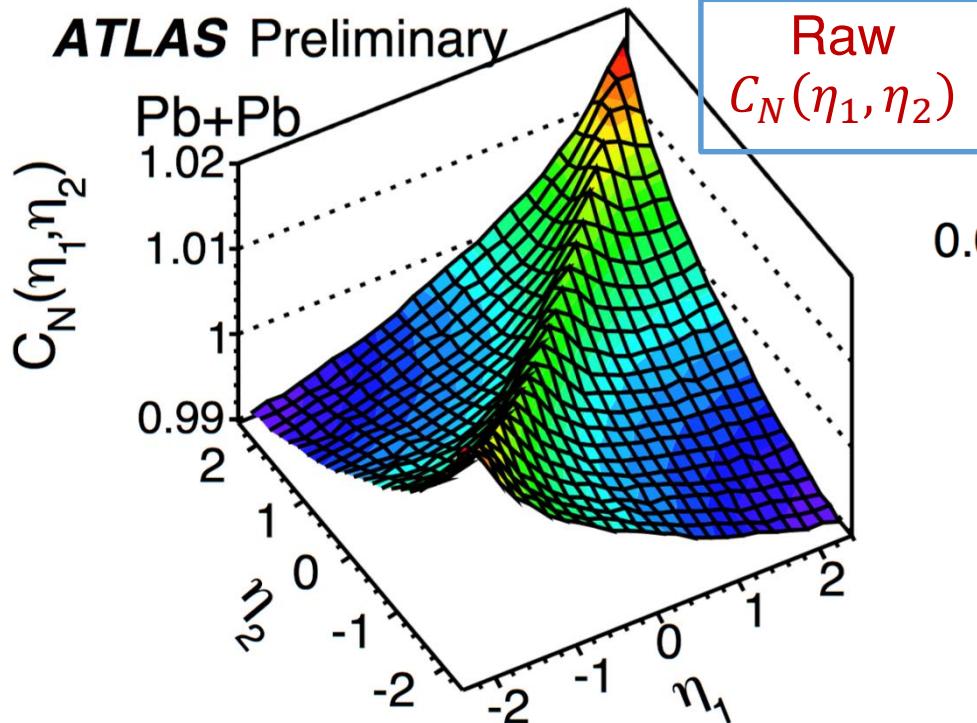
Long-range
 $C_N^{sub}(\eta_1, \eta_2)$



- After SRC subtraction, similar LRC in all three systems!

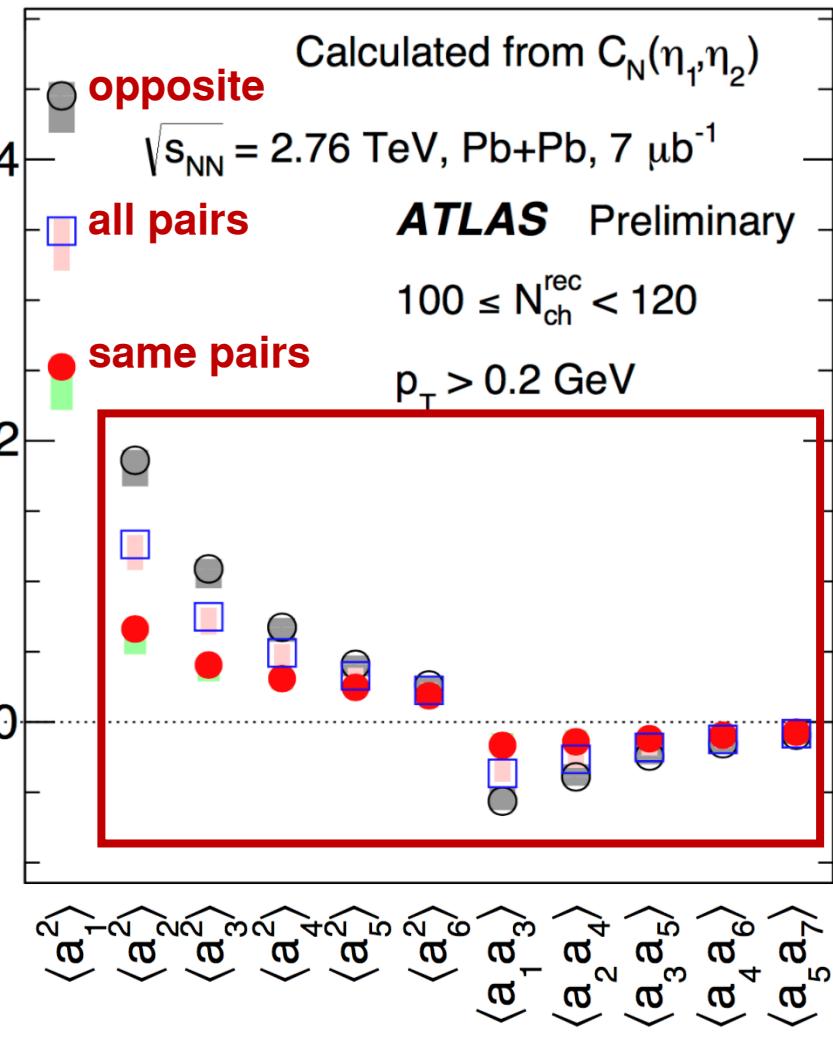
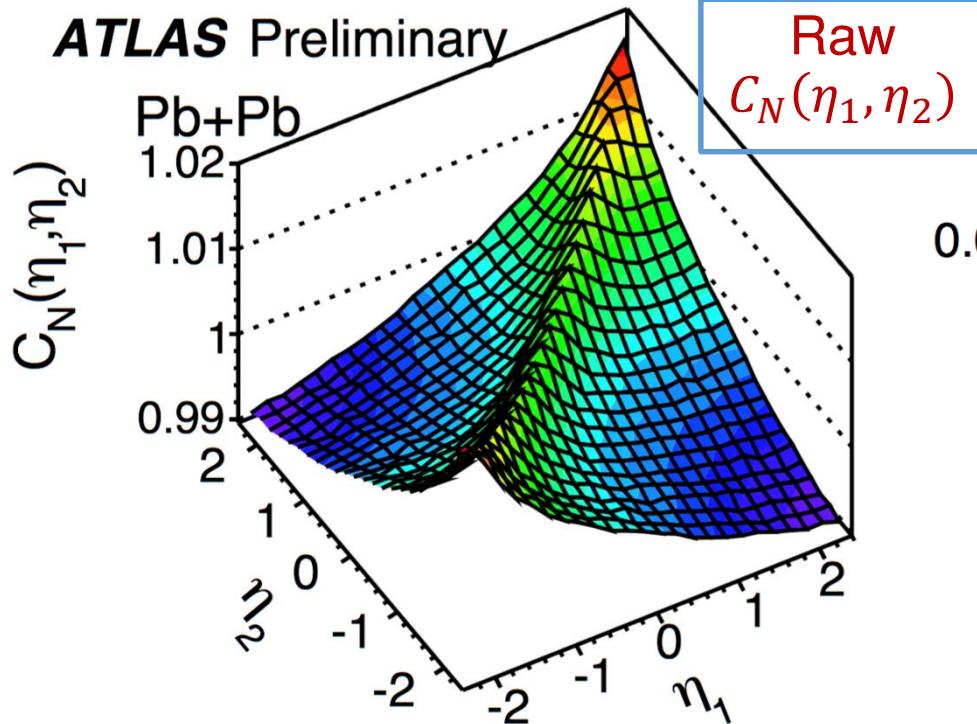
Results: Legendre spectra before SRC removal

$$1 + \sum_{n,m=1}^{\infty} \langle a_n a_m \rangle \frac{T_n(\eta_1)T_m(\eta_2) + T_n(\eta_2)T_m(\eta_1)}{2}$$



Results: Legendre spectra before SRC removal

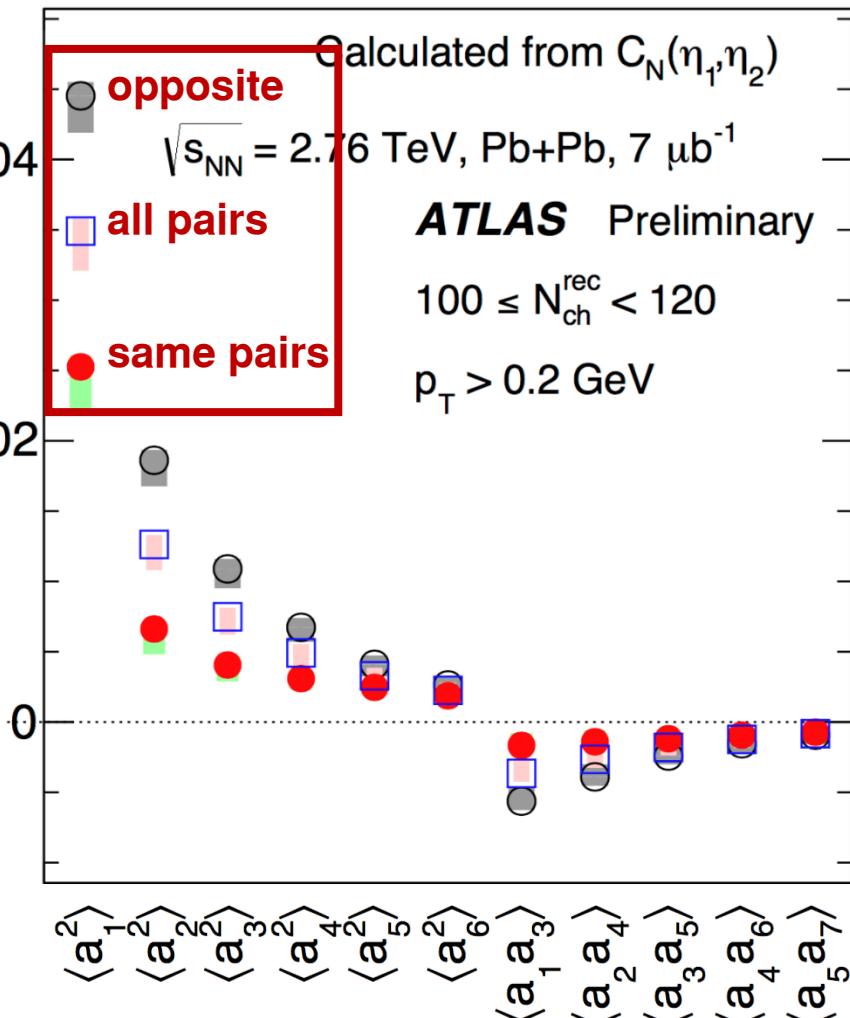
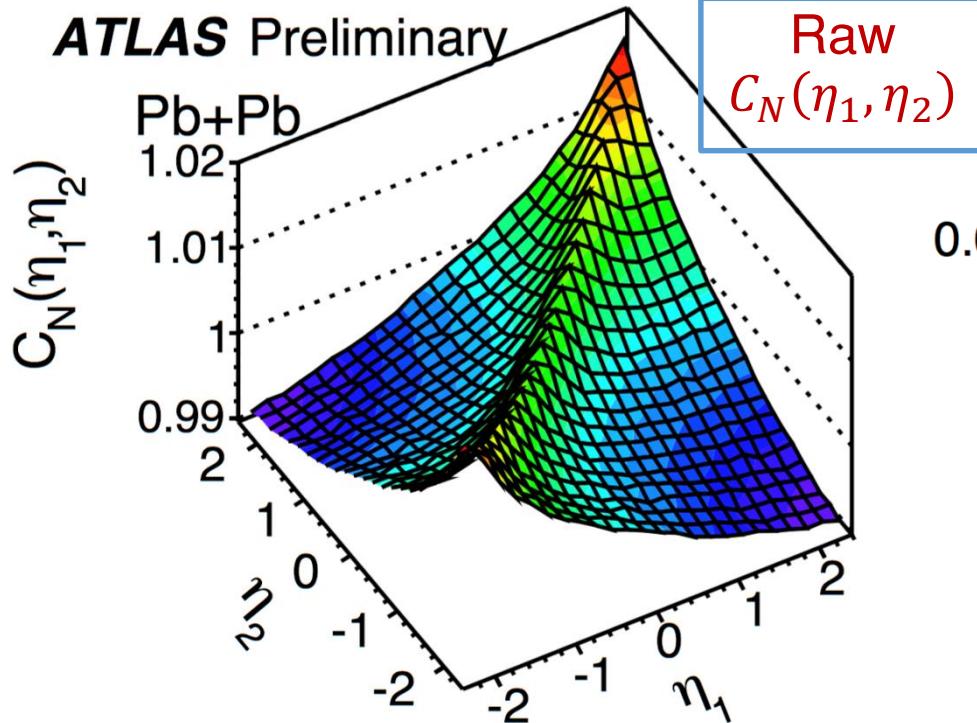
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- Higher order coefficients observed;

Results: Legendre spectra before SRC removal

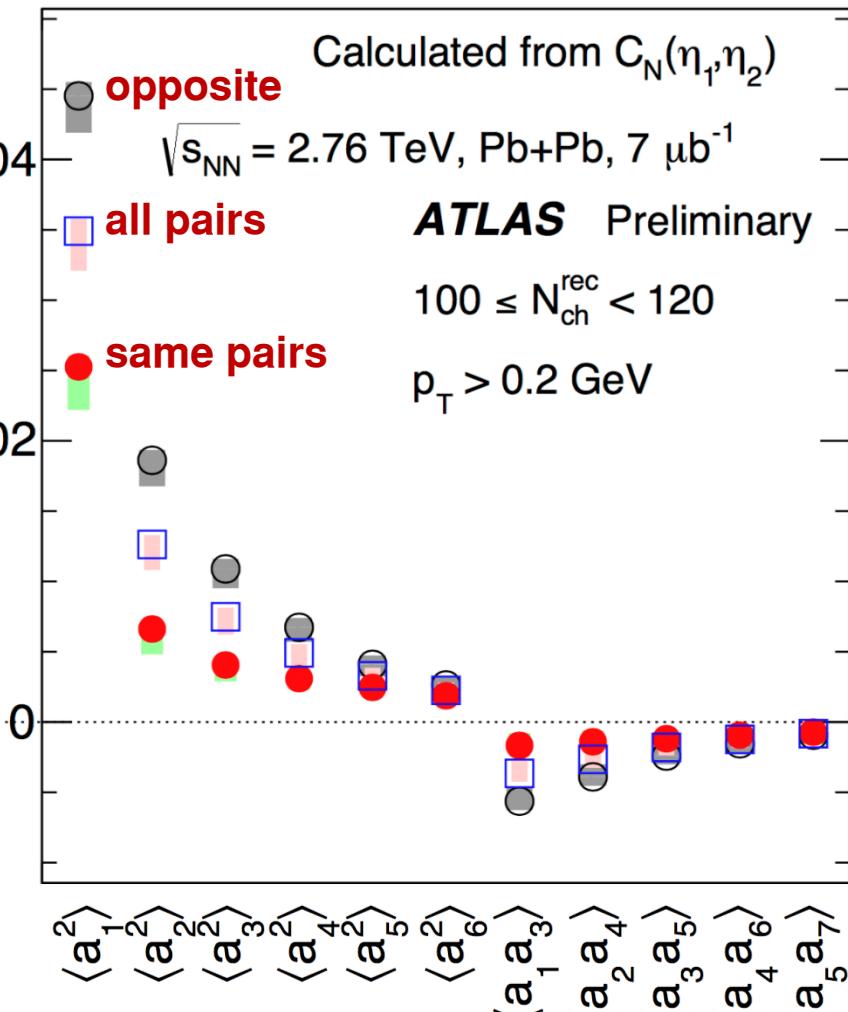
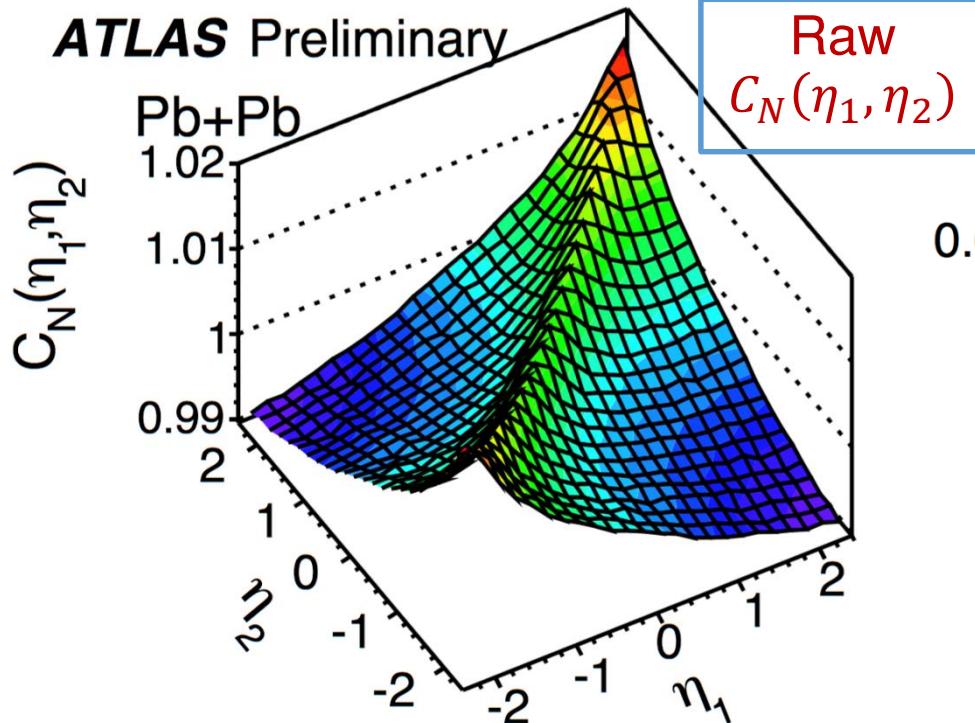
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- Higher order coefficients observed;
- Coefficients depend on charge combinations;

Results: Legendre spectra before SRC removal

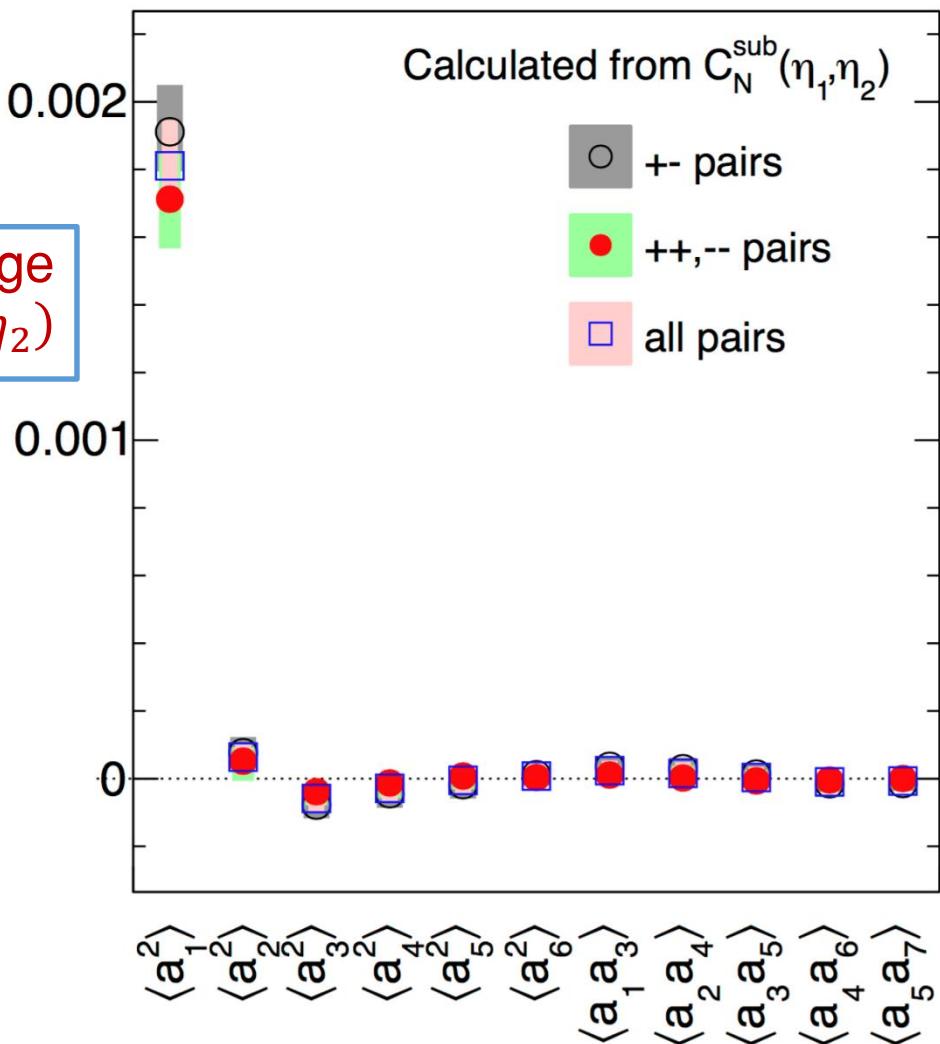
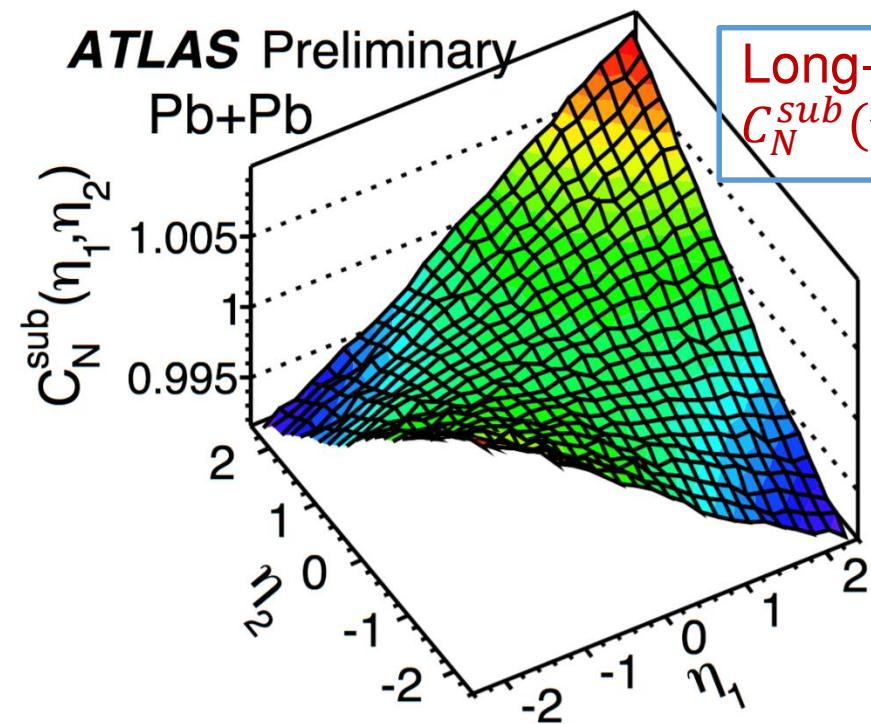
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- Higher order coefficients observed;
- Coefficients depend on charge combinations;
- Complicated and very hard to interpret: due to SRC!

Results: Legendre spectra after SRC removal

$$1 + \sum_{n,m=1}^{\infty} \langle a_n a_m \rangle \frac{T_n(\eta_1)T_m(\eta_2) + T_n(\eta_2)T_m(\eta_1)}{2}$$

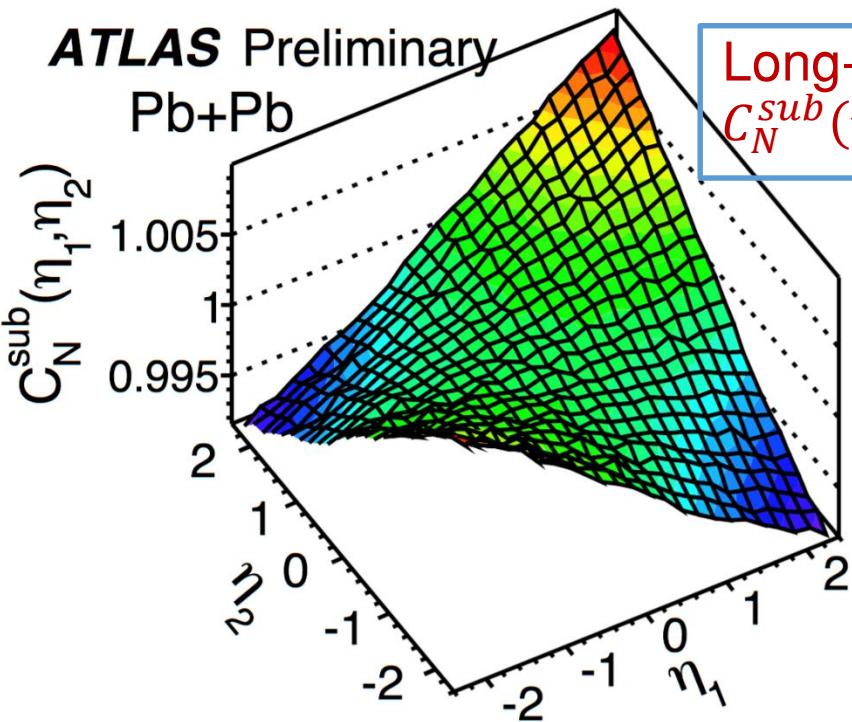


Results: Legendre spectra after SRC removal

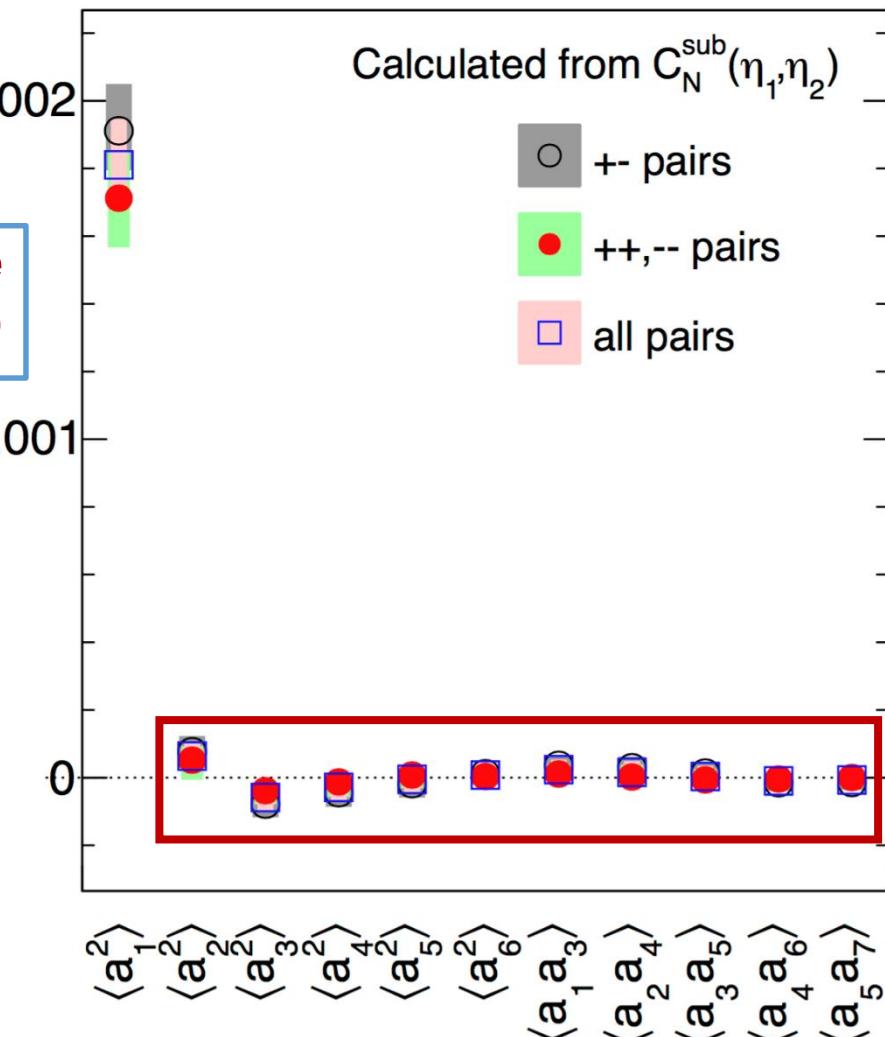
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ATLAS Preliminary

Pb+Pb



Long-range
 $C_N^{sub}(\eta_1, \eta_2)$

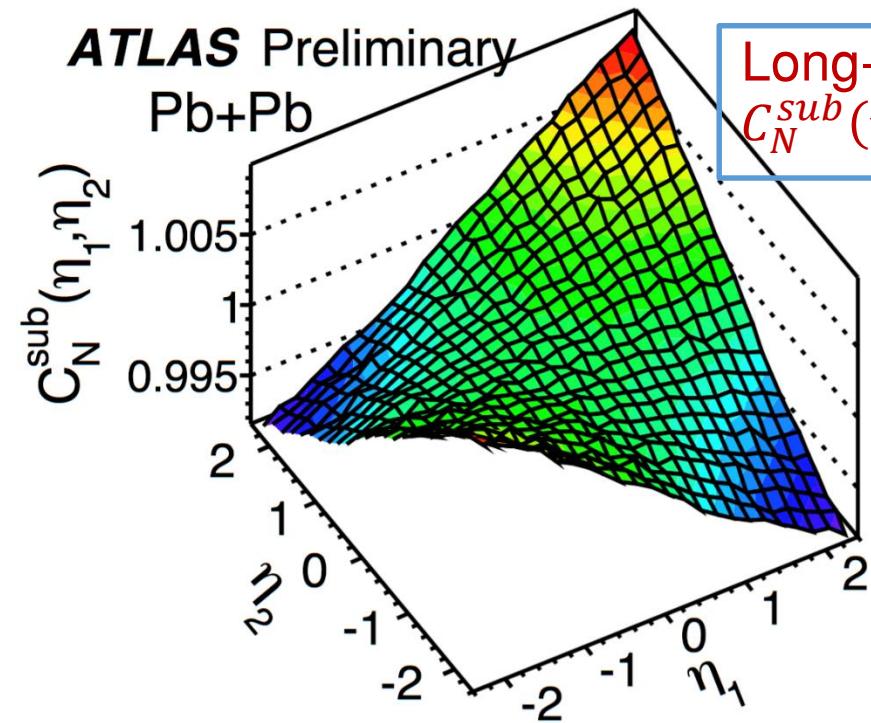


- Higher order coefficients consistent with 0: dominated by a_1 ;

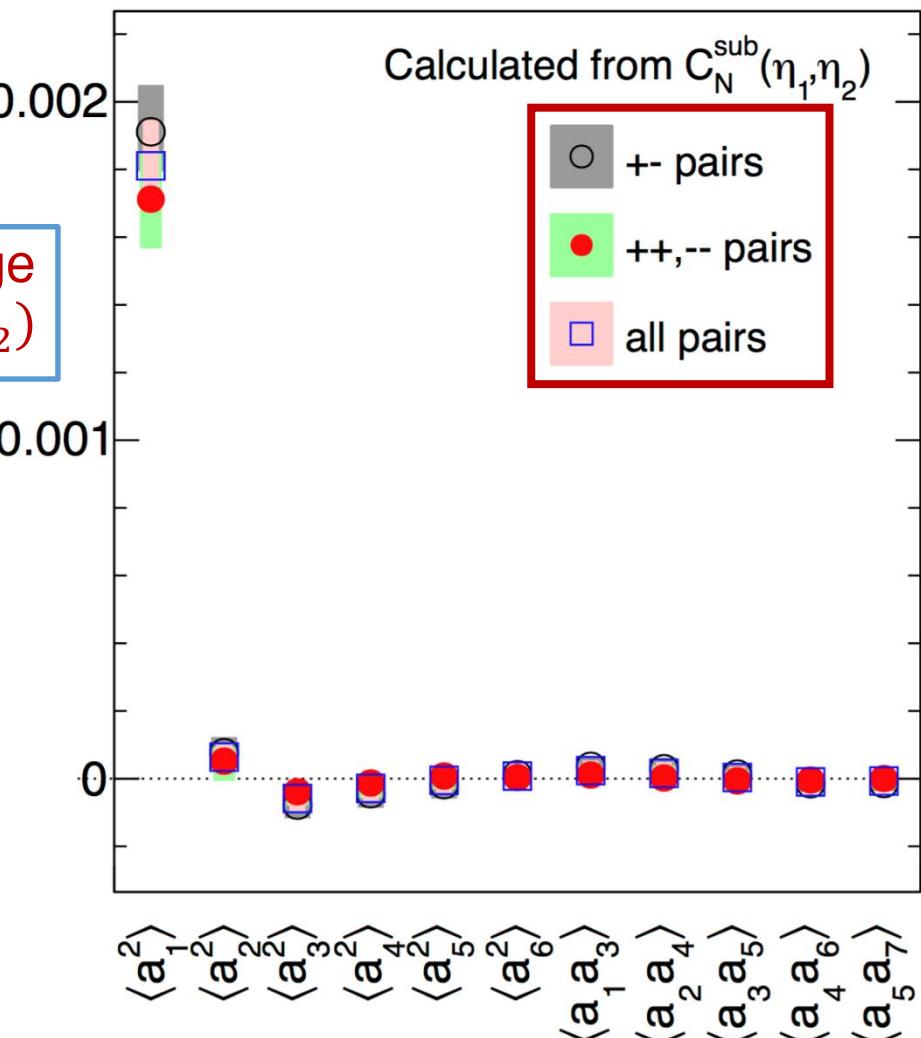
Results: Legendre spectra after SRC removal

$$1 + \sum_{n,m=1}^{\infty} \langle a_n a_m \rangle \frac{T_n(\eta_1)T_m(\eta_2) + T_n(\eta_2)T_m(\eta_1)}{2}$$

ATLAS Preliminary
Pb+Pb



Long-range
 $C_N^{sub}(\eta_1, \eta_2)$



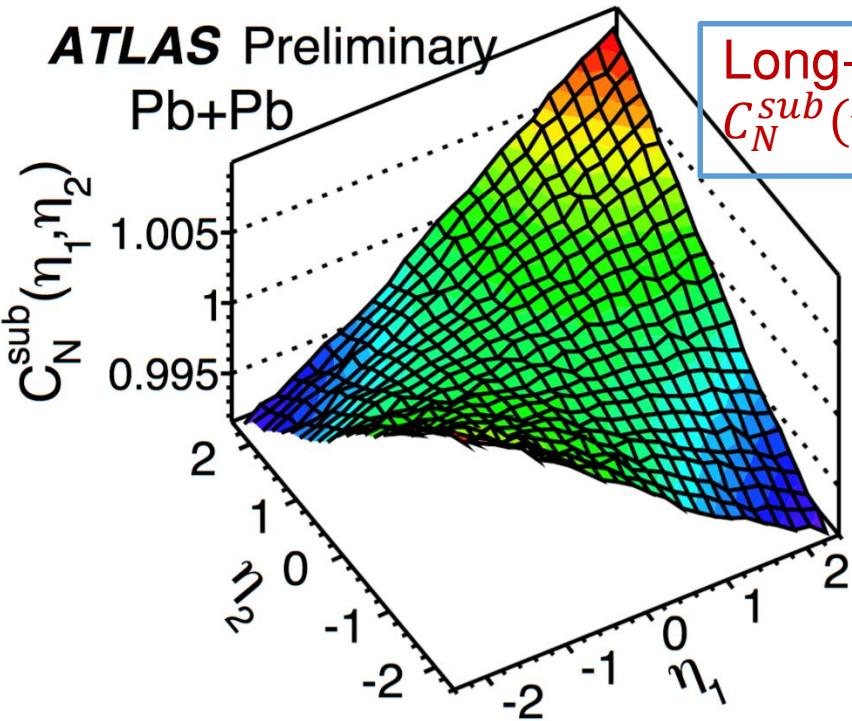
- Higher order coefficients consistent with 0: dominated by a_1 ;
- Coefficients independent of charge combinations;

Results: Legendre spectra after SRC removal

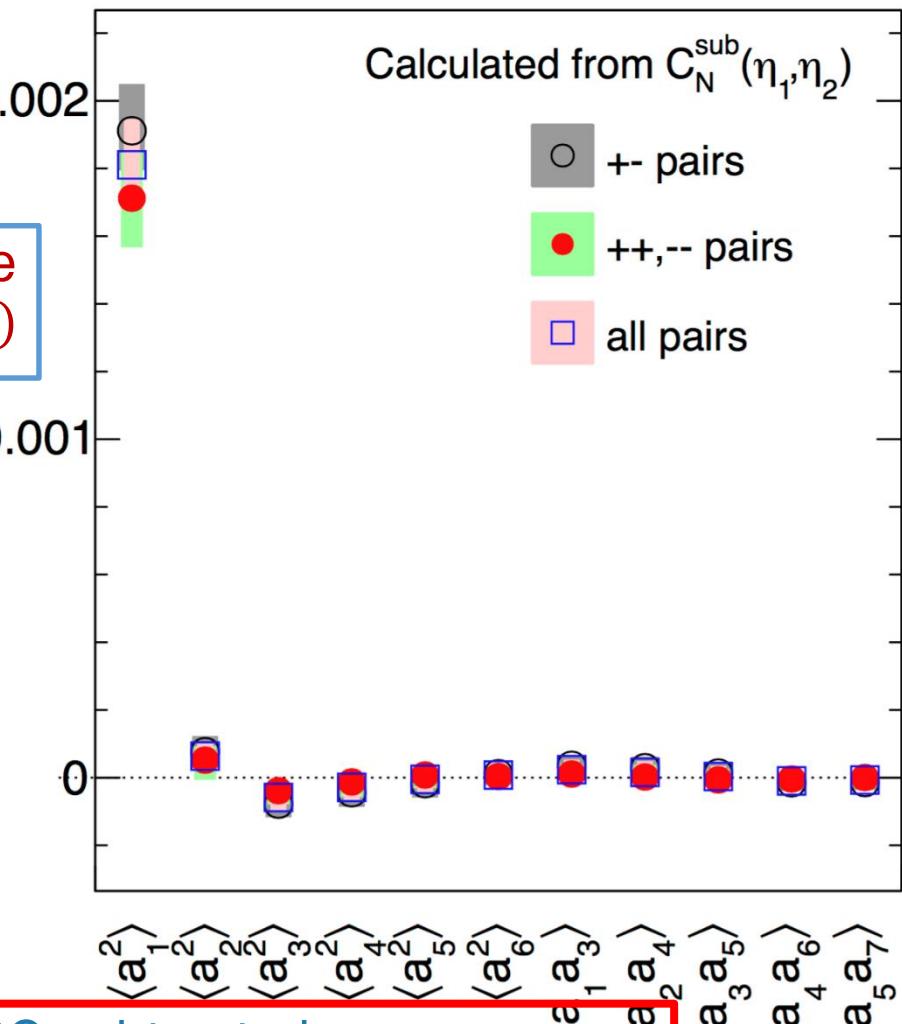
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ATLAS Preliminary

Pb+Pb



Long-range
 $C_N^{sub}(\eta_1, \eta_2)$



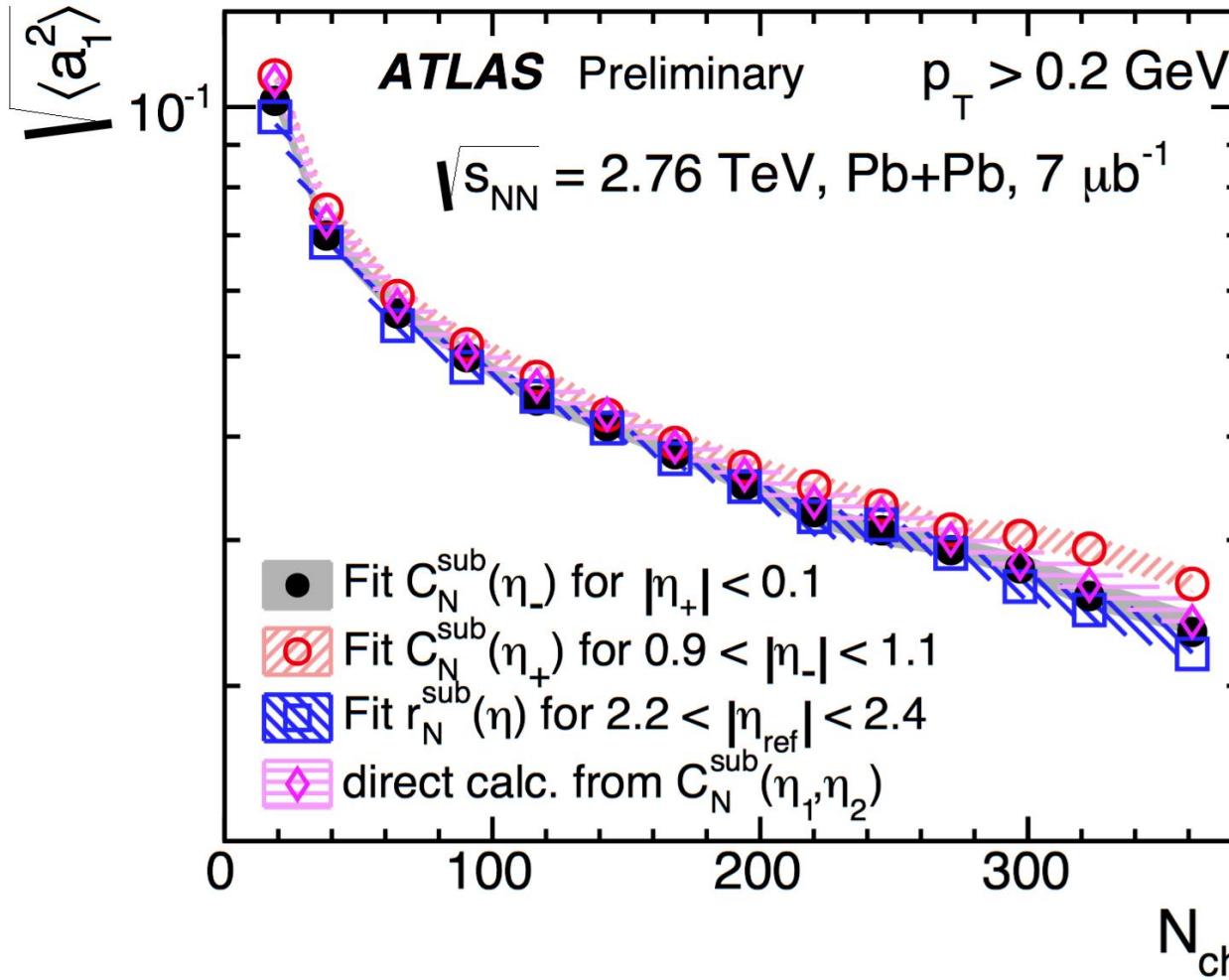
- Much simpler picture after SRC subtracted
 - LRC is dominated by linear multiplicity fluctuation in η ;
 - LRC is independent of charge combination.

How stable are the results?

- Four largely independent methods are applied to determine $\langle a_1^2 \rangle$;
- Different methods have different sensitivity to the analysis procedures;

How stable are the results?

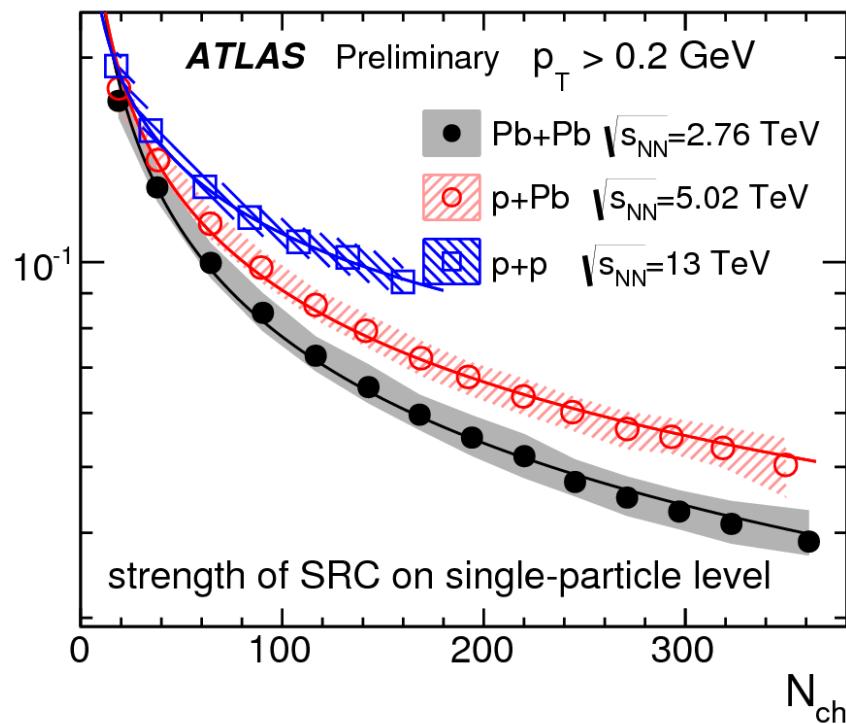
- Four largely independent methods are applied to determine $\langle a_1^2 \rangle$;
- Different methods have different sensitivity to the analysis procedures;



- Four methods give consistent a_1 : conclusions are insensitive to the procedure.

Dependence on N_{ch} and collision systems

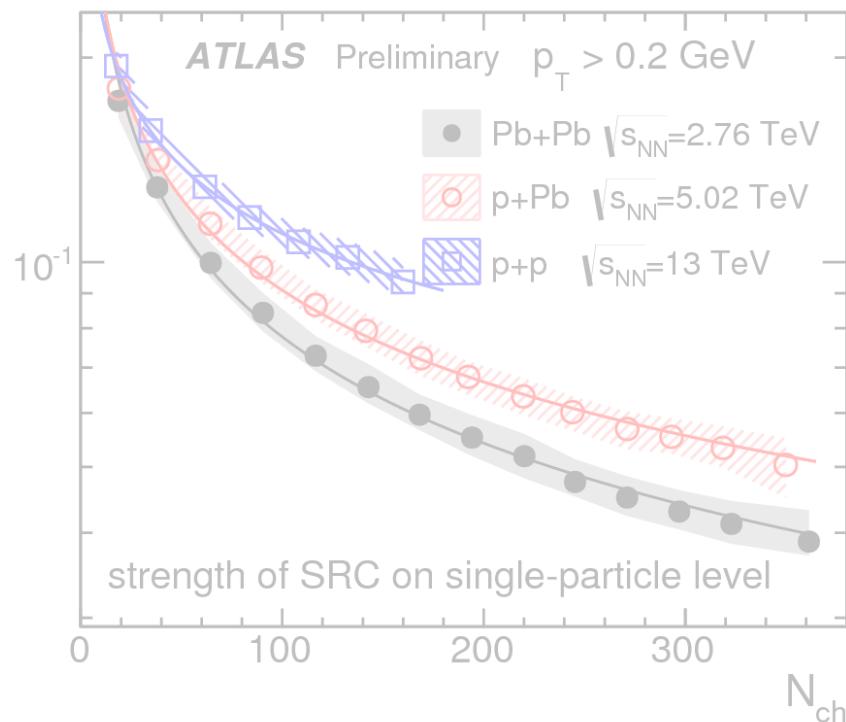
SRC



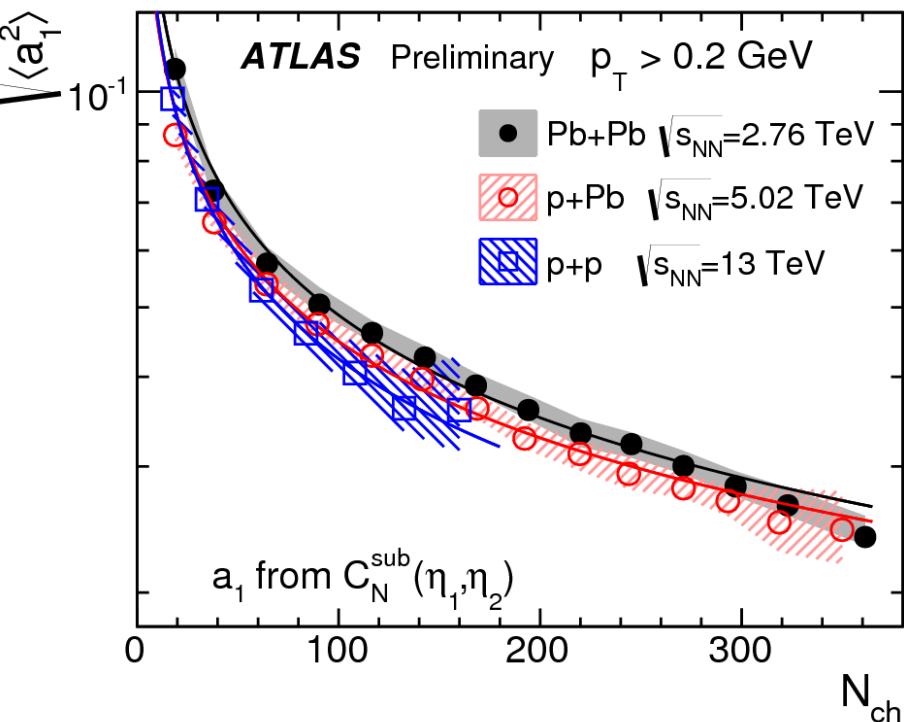
- Strength of SRC defined as: $\sqrt{\Delta_{SRC}} \equiv \sqrt{\frac{\int \delta_{SRC}(\eta_1, \eta_2) d\eta_1 d\eta_2}{4Y^2}}$;
- Depends on N_{ch} : **strength of SRC increases towards peripheral**;
- Depends on system size: **SRC is stronger in small system**.

Dependence on N_{ch} and collision systems

SRC



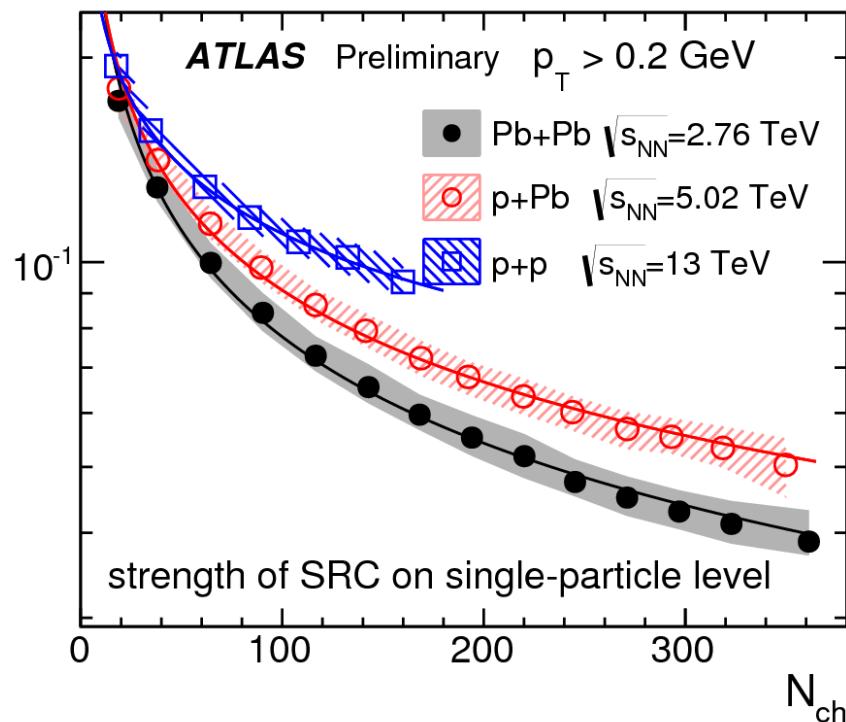
LRC



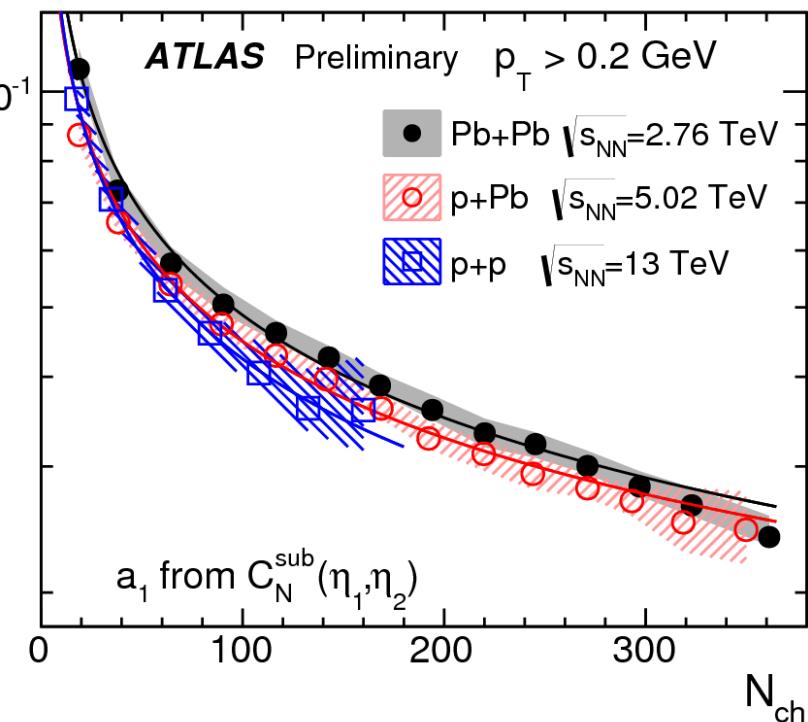
- Strength of LRC is characterized by dominating coefficient $\sqrt{a_1^2}$;
- Depends on N_{ch} : FB multiplicity fluctuation is larger in peripheral;
- Independent of system size: require sources at partonic level!
- Strength of SRC and LRC also follow pow-law function: why?

Dependence on N_{ch} and collision systems

SRC



LRC

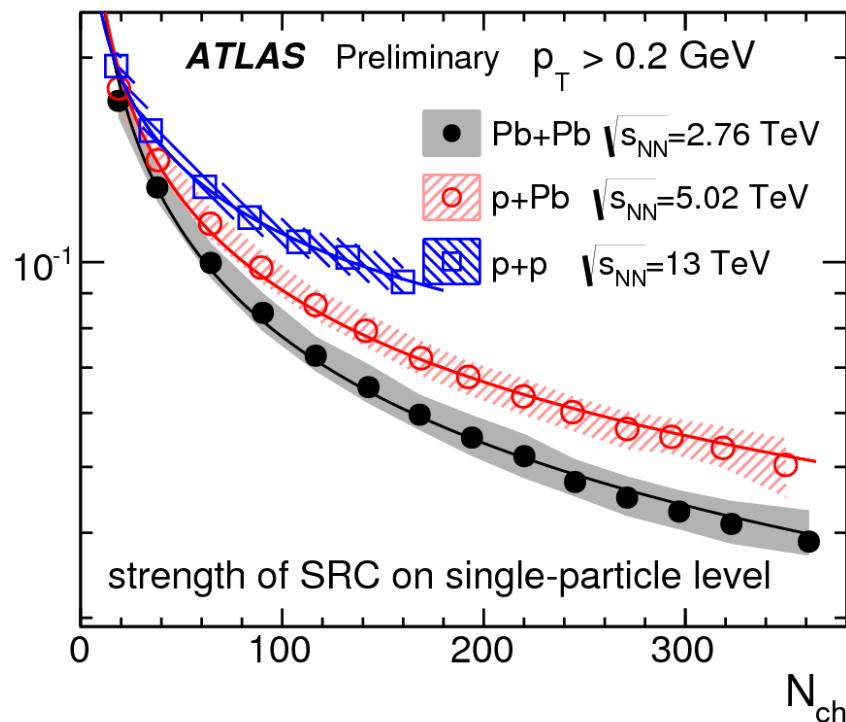


- In an independent cluster model, each cluster emits same number of pairs;
- Both SRC and LRC scale approximately as the inverse of number of clusters n ;

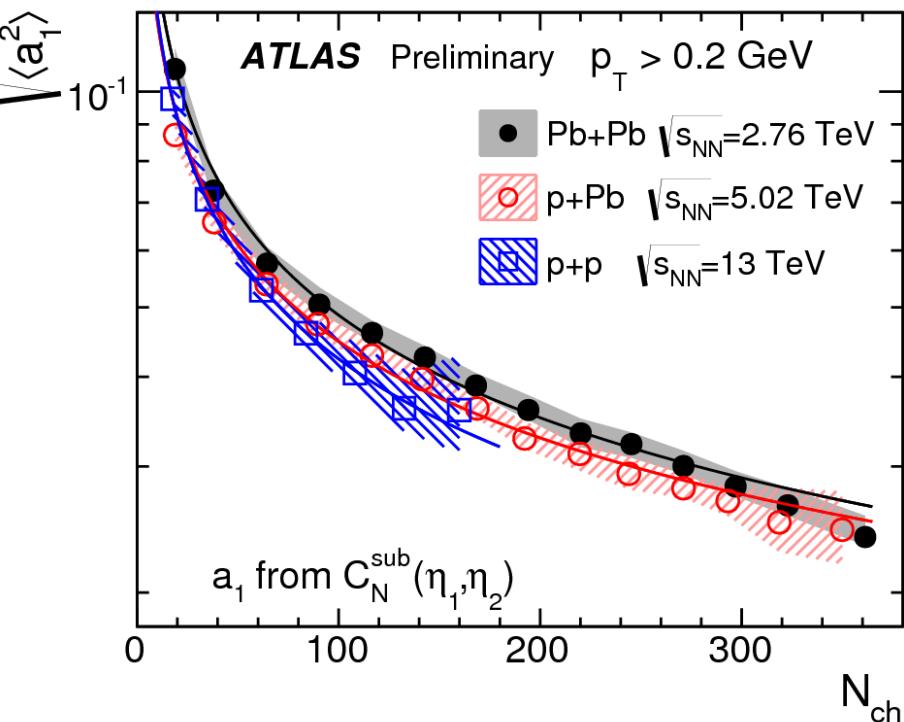
$$\sqrt{\Delta_{SRC}} \sim \sqrt{a_1^2} \sim \frac{1}{n^\alpha}$$

Dependence on N_{ch} and collision systems

SRC



LRC

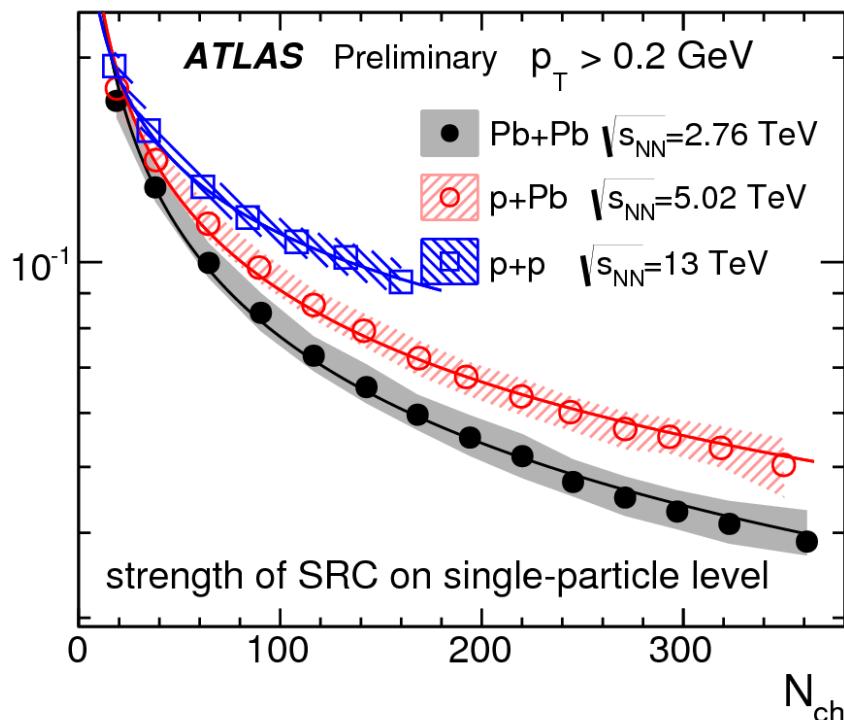


- In an independent cluster model, each cluster emits same number of pairs;
- Both SRC and LRC scale approximately as the inverse of number of clusters n ;
- Assuming n and N_{ch} are directly related, then

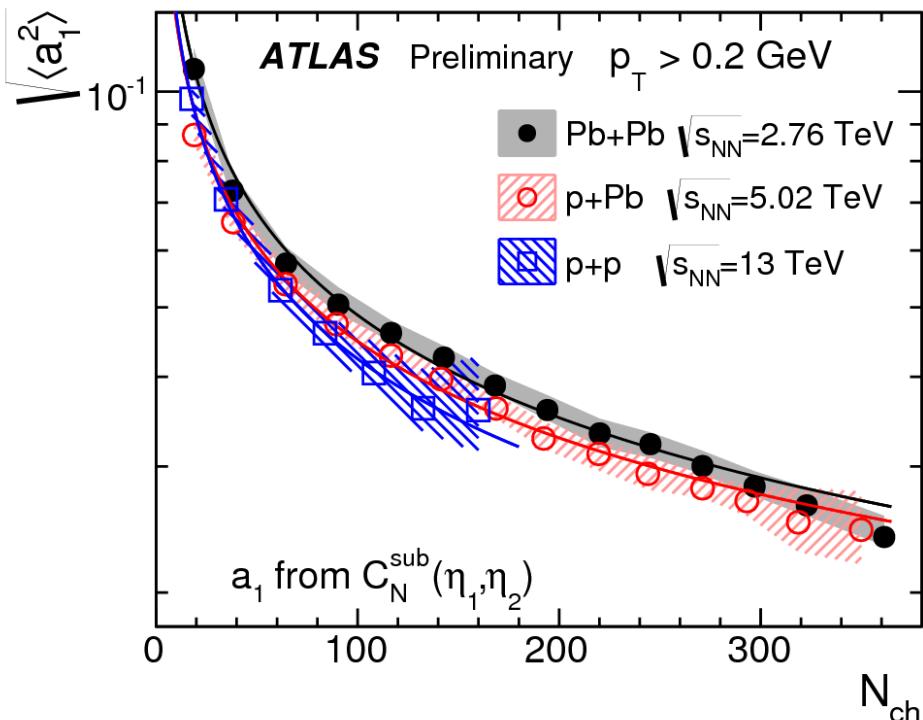
$$\sqrt{\Delta_{SRC}} \sim \sqrt{a_1^2} \sim \frac{1}{n^\alpha} \sim \frac{1}{N_{ch}^\alpha}$$

Dependence on N_{ch} and collision systems

SRC



LRC

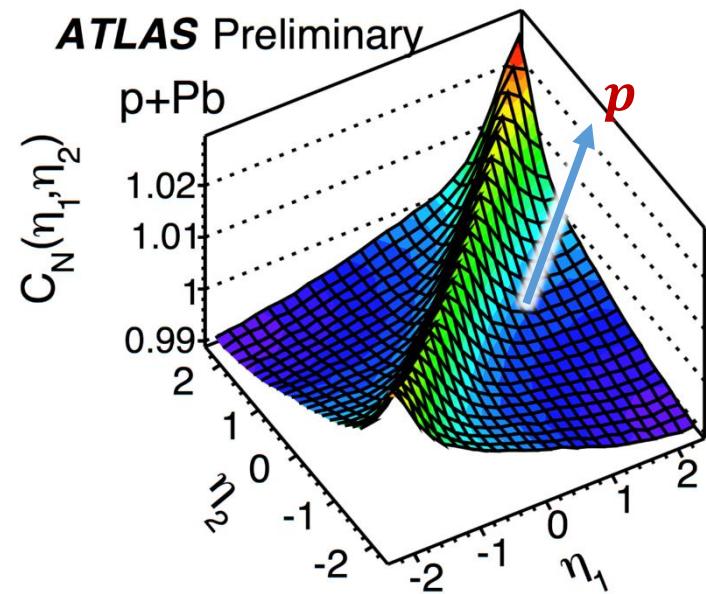


Fit with $\frac{c}{N_{ch}^\alpha}$

	Pb+Pb	$p+Pb$	pp
α for $\sqrt{\Delta_{\text{SRC}}}$	0.505 ± 0.011	0.450 ± 0.010	0.365 ± 0.014
α for $\sqrt{\langle a_1^2 \rangle}$	0.454 ± 0.011	0.433 ± 0.014	0.465 ± 0.018

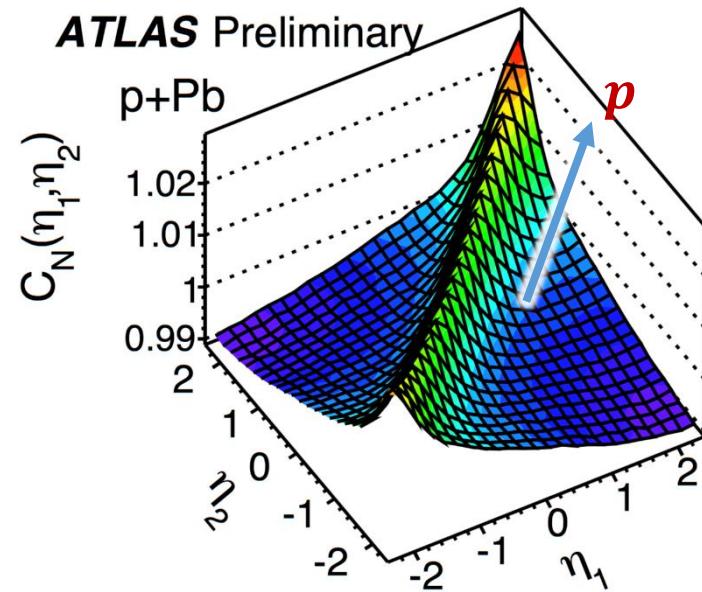
$$\sqrt{\Delta_{\text{SRC}}} \sim \sqrt{a_1^2} \sim \frac{1}{n^\alpha} \sim \frac{1}{N_{ch}^\alpha}, \alpha \sim 0.5$$

Asymmetry in p +Pb collision

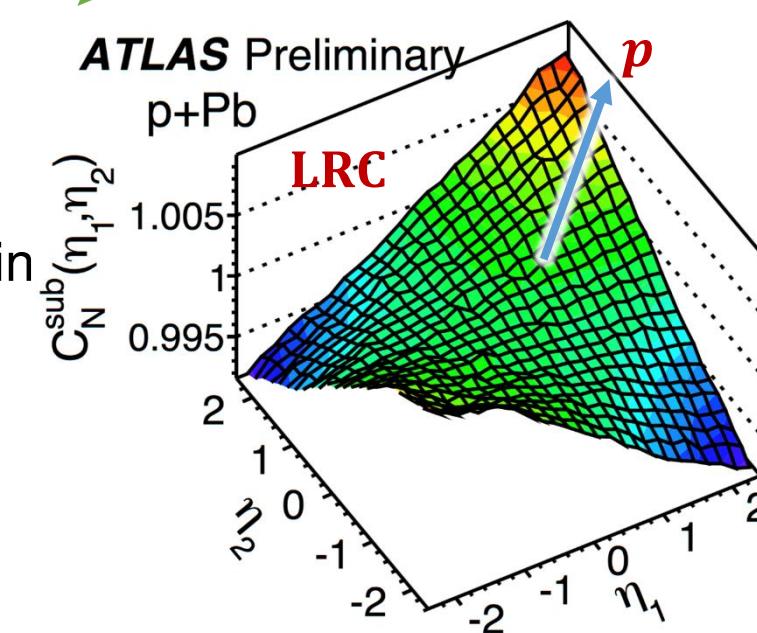


- Asymmetry observed in p +Pb collision: stronger correlation in the proton-going side.

Asymmetry in $p+\text{Pb}$ collision

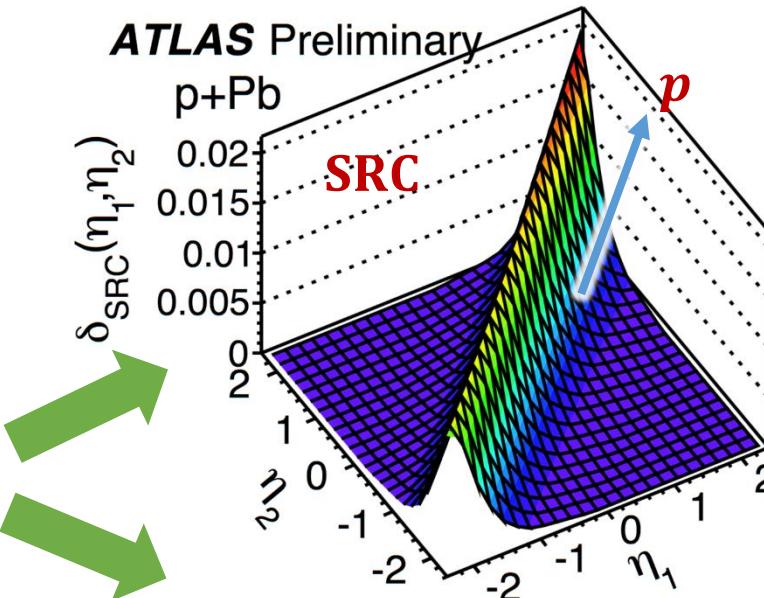
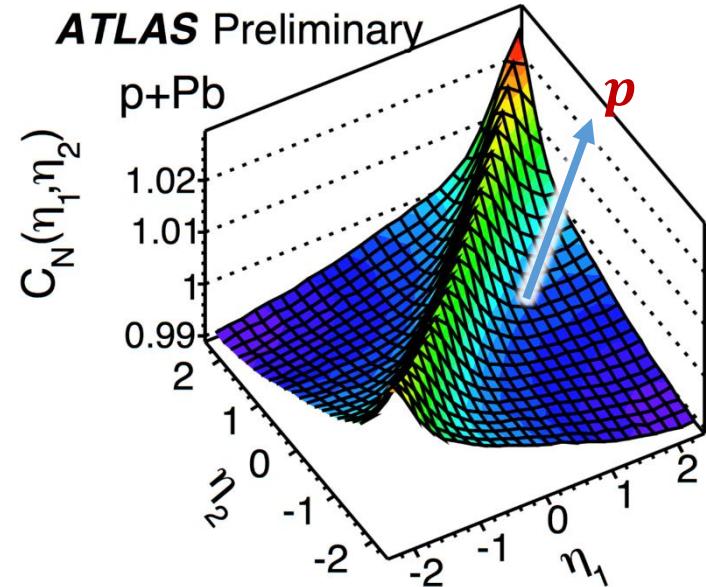


- Asymmetry observed in $p+\text{Pb}$ collision: stronger correlation in the proton-going side.

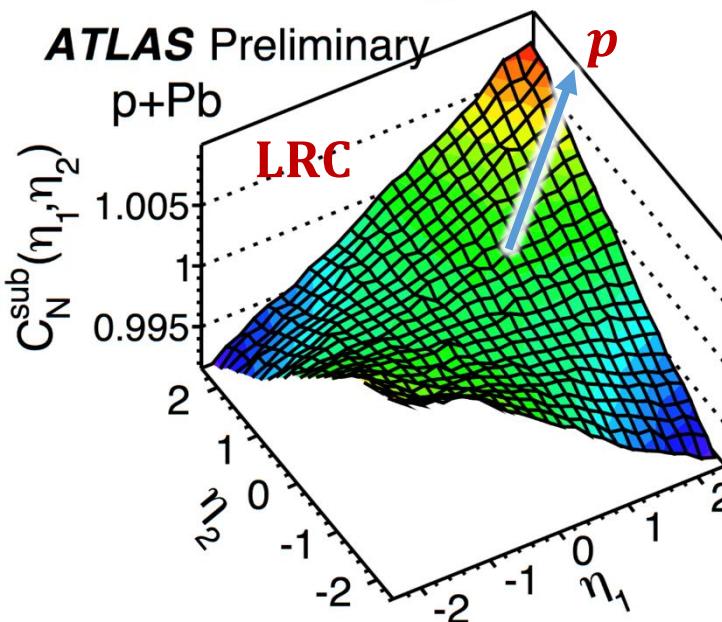


- LRC is symmetric.

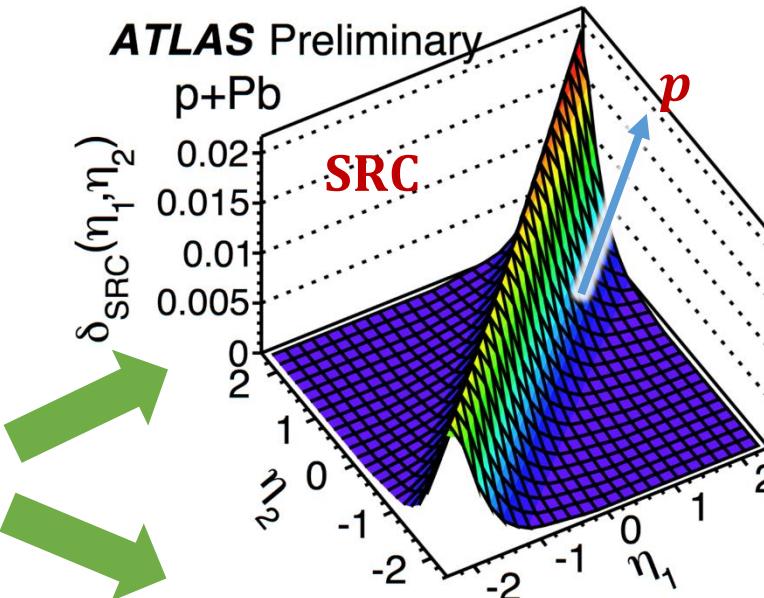
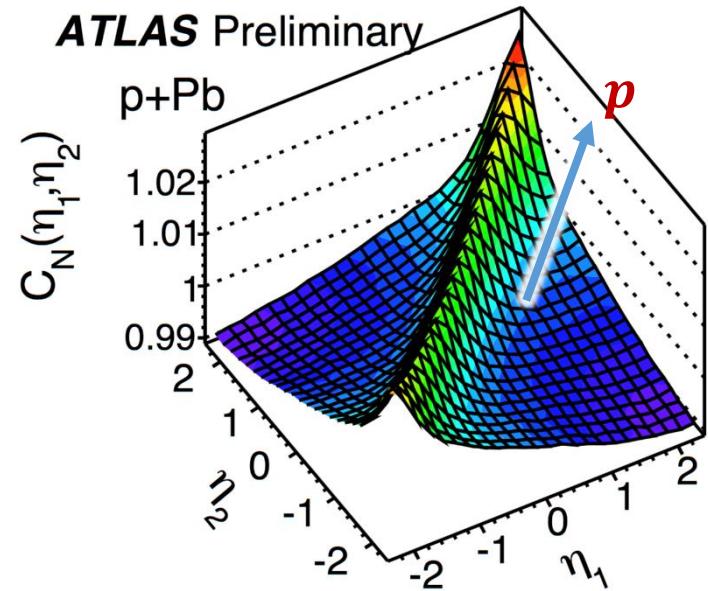
Asymmetry in $p+\text{Pb}$ collision



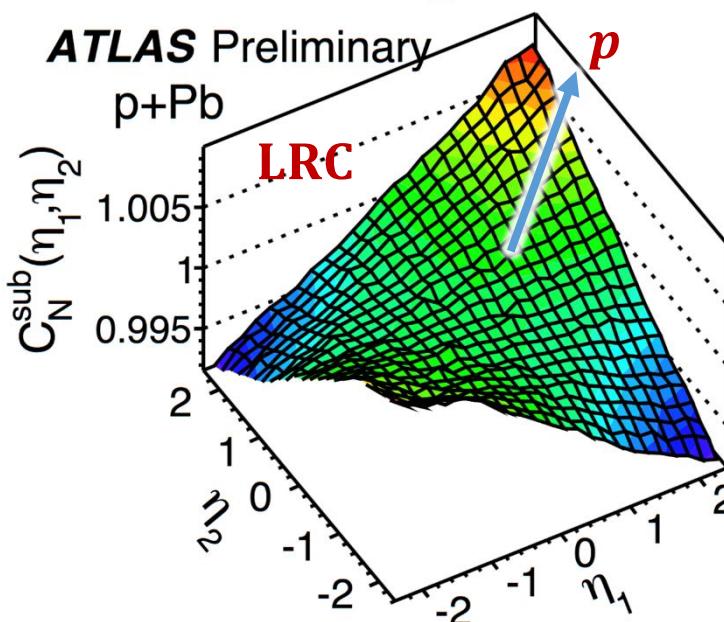
- Asymmetry observed in $p+\text{Pb}$ collision: stronger correlation in the proton-going side.



Asymmetry in $p+\text{Pb}$ collision



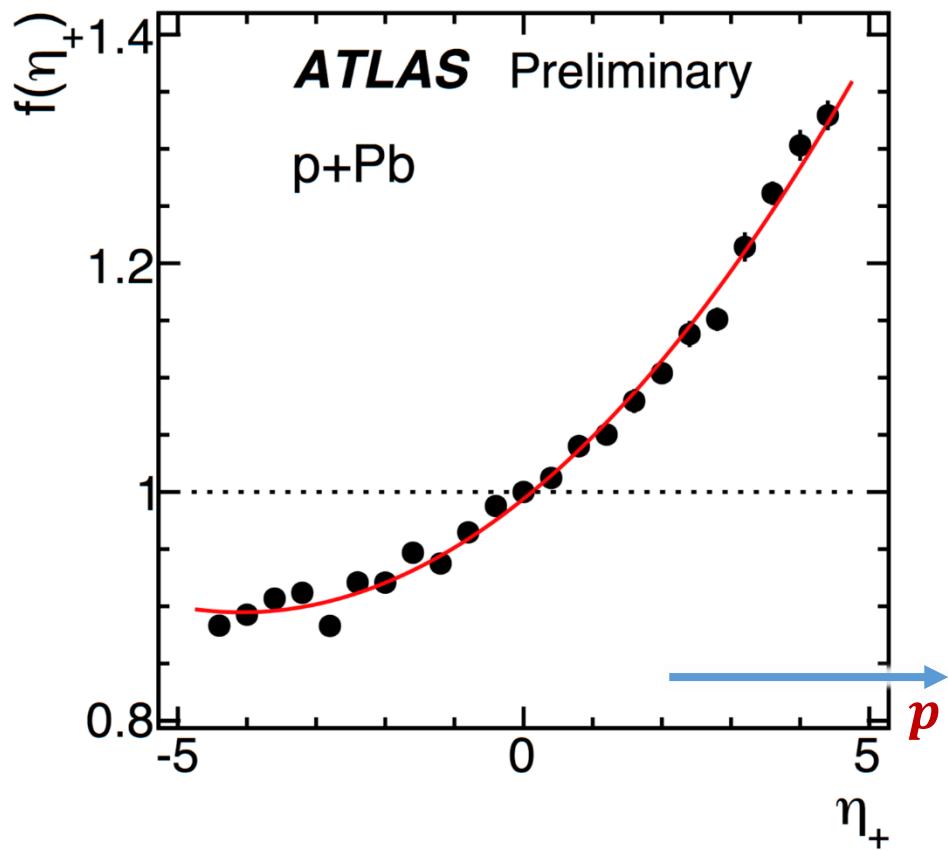
- Asymmetry entirely due to SRC!



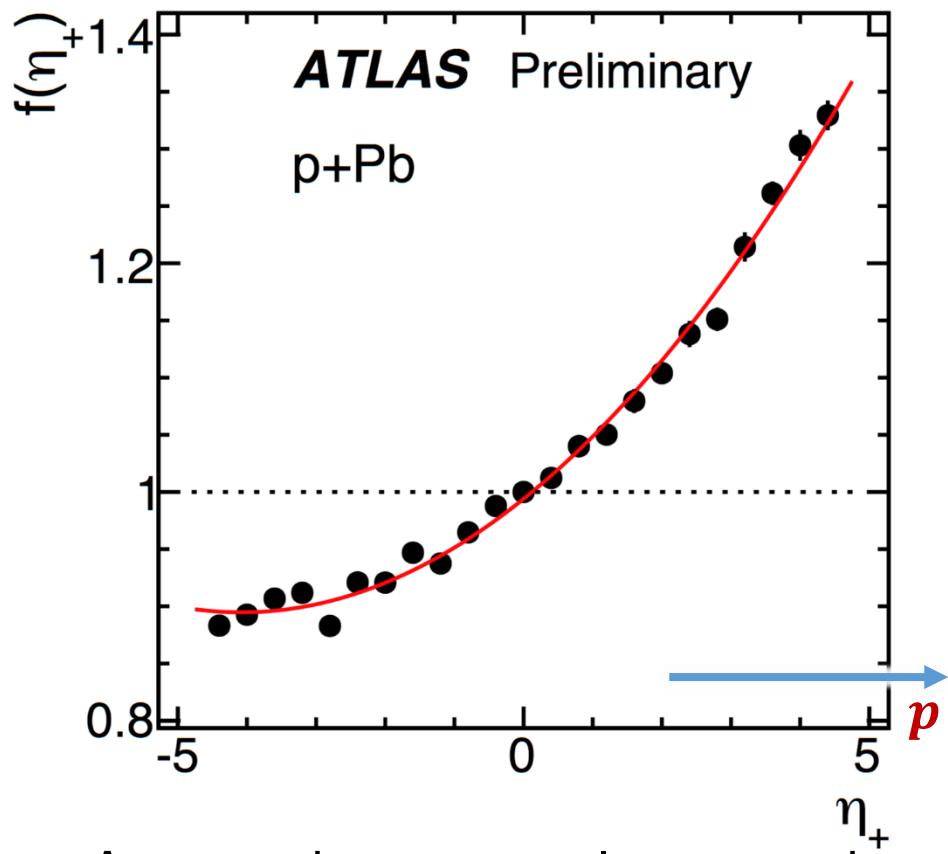
- LRC is symmetric.

- Asymmetry observed in $p+\text{Pb}$ collision: stronger correlation in the proton-going side.
- Why the asymmetric collision causes asymmetric SRC?

SRC asymmetry in $p+\text{Pb}$ collision



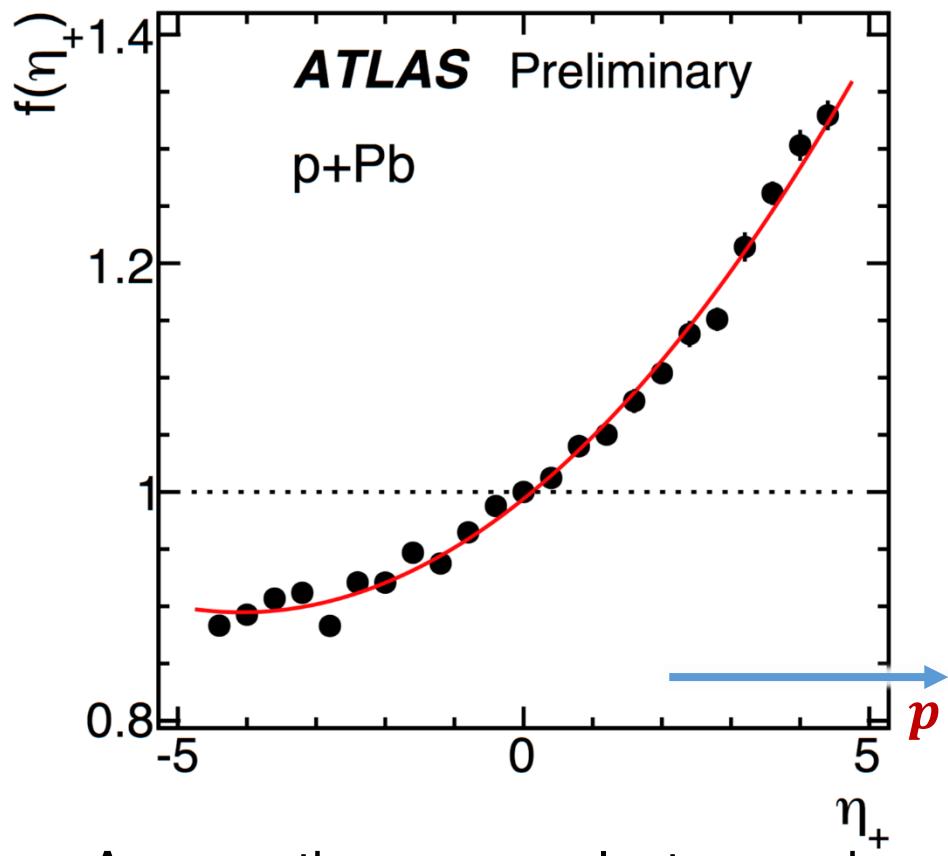
SRC asymmetry in $p+\text{Pb}$ collision



- Assume there are n clusters and each one emits m particles on average;

$$\delta_{SRC} \propto \frac{n\langle m(m-1) \rangle}{(n\langle m \rangle)^2} = \frac{1}{n}$$

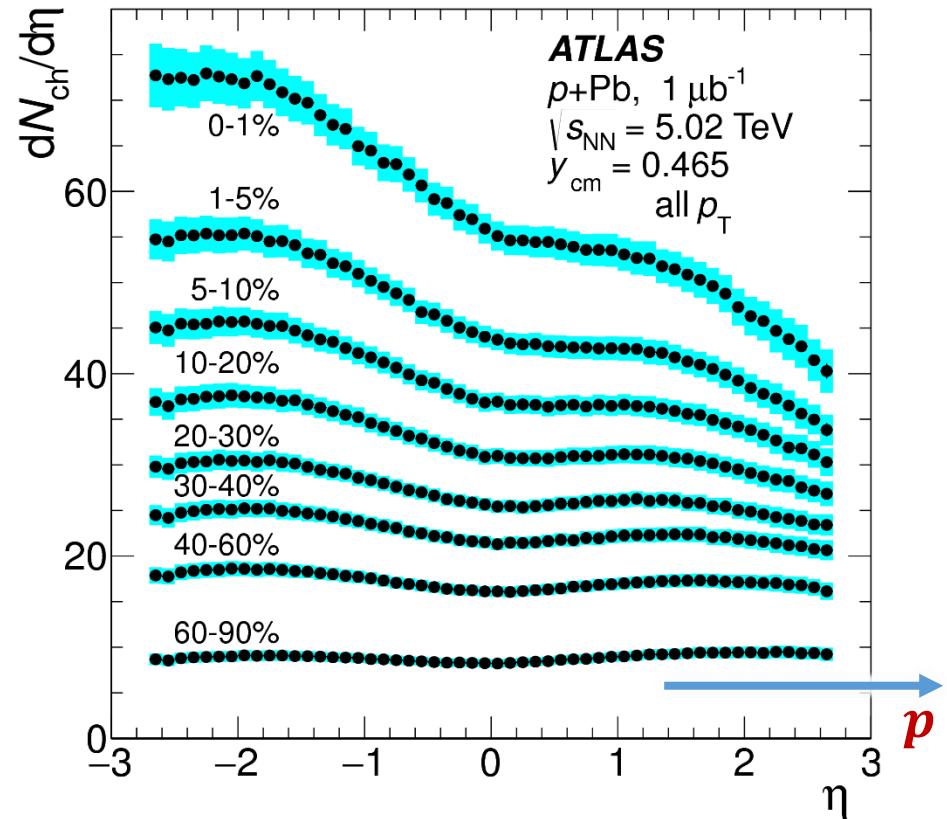
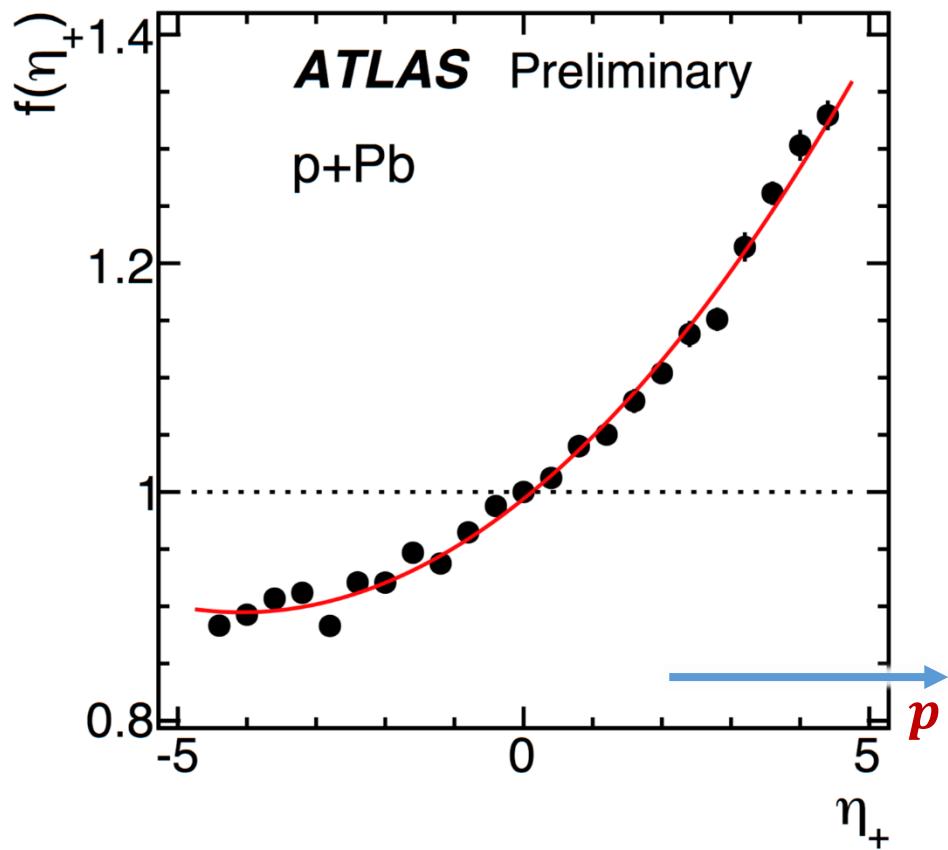
SRC asymmetry in $p+\text{Pb}$ collision



- Assume there are n clusters and each one emits m particles on average;
- Assume n is proportional to local particle density $dN_{ch}/d\eta$;

$$\delta_{SRC} \propto \frac{n \langle m(m-1) \rangle}{(n \langle m \rangle)^2} = \frac{1}{n} \propto \frac{1}{dN_{ch}/d\eta}$$

SRC asymmetry in $p+\text{Pb}$ collision

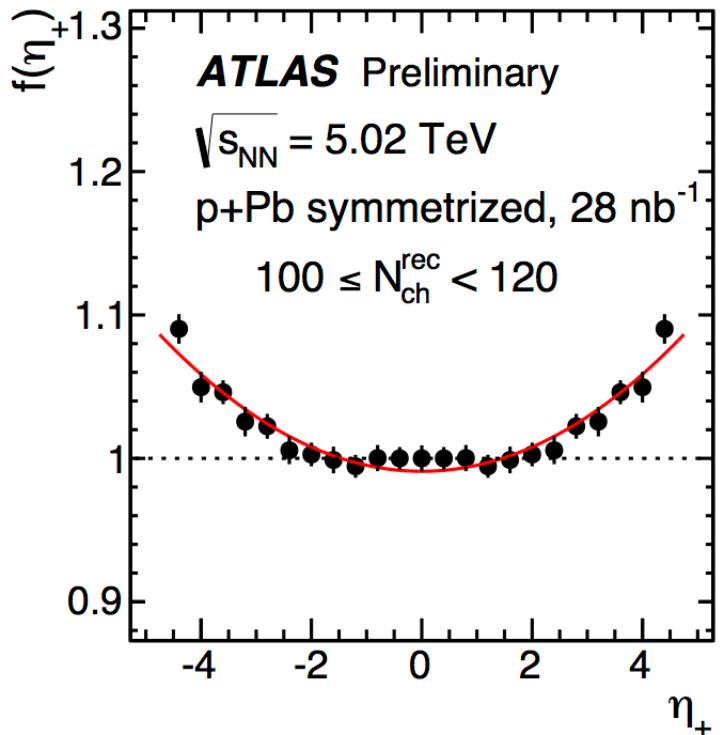


- Assume there are n clusters and each one emits m particles on average;
- Assume n is proportional to local particle density $dN_{ch}/d\eta$;

$$\delta_{SRC} \propto \frac{n \langle m(m-1) \rangle}{(n \langle m \rangle)^2} = \frac{1}{n} \propto \frac{1}{dN_{ch}/d\eta} \quad \text{Inverse to multiplicity distribution}$$

Compare SRC shape in three systems

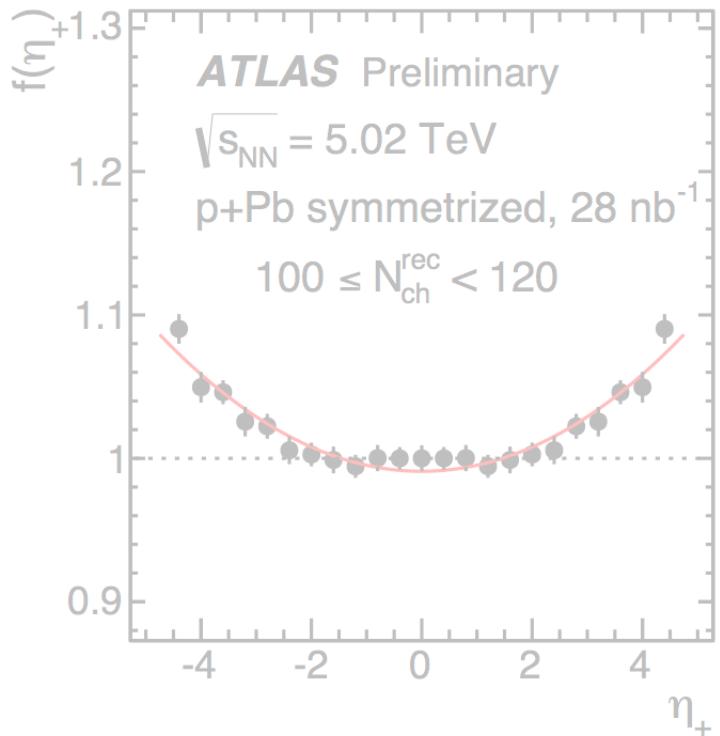
Symmetrized $p+\text{Pb}$



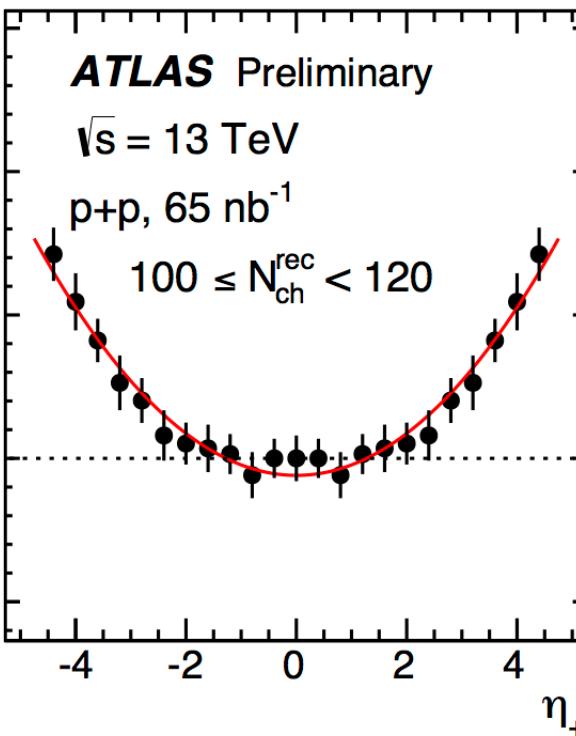
- For better comparison with pp and $\text{Pb}+\text{Pb}$, $p+\text{Pb}$ is symmetrized;

Compare SRC shape in three systems

Symmetrized $p+\text{Pb}$



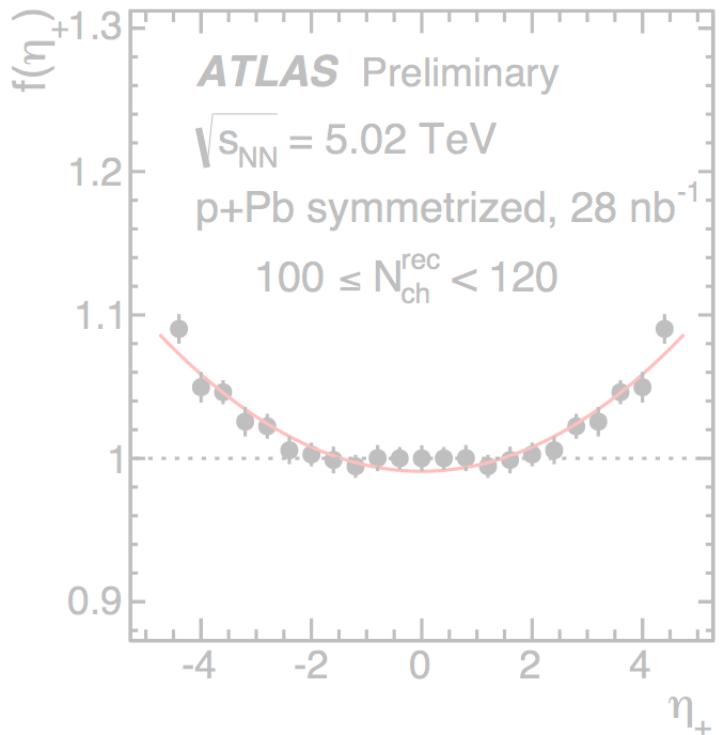
pp



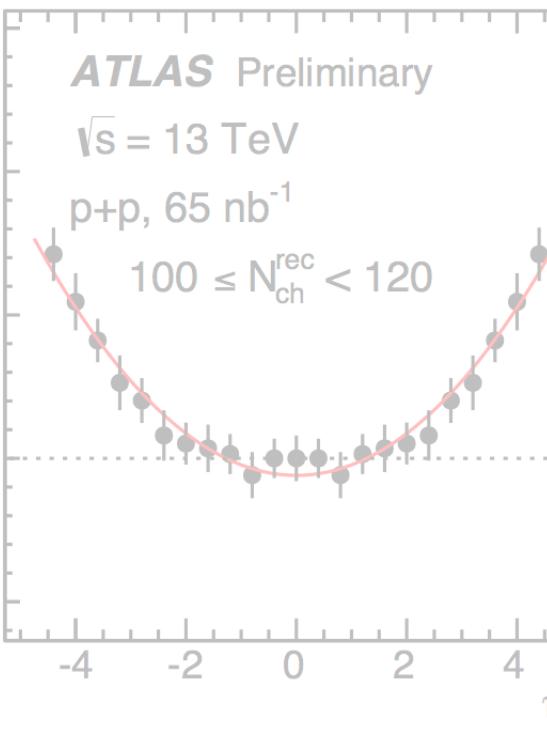
- For better comparison with pp and $\text{Pb}+\text{Pb}$, $p+\text{Pb}$ is symmetrized;
- In high-multiplicity pp , SRC shape is slightly larger than $p+\text{Pb}$;

Compare SRC shape in three systems

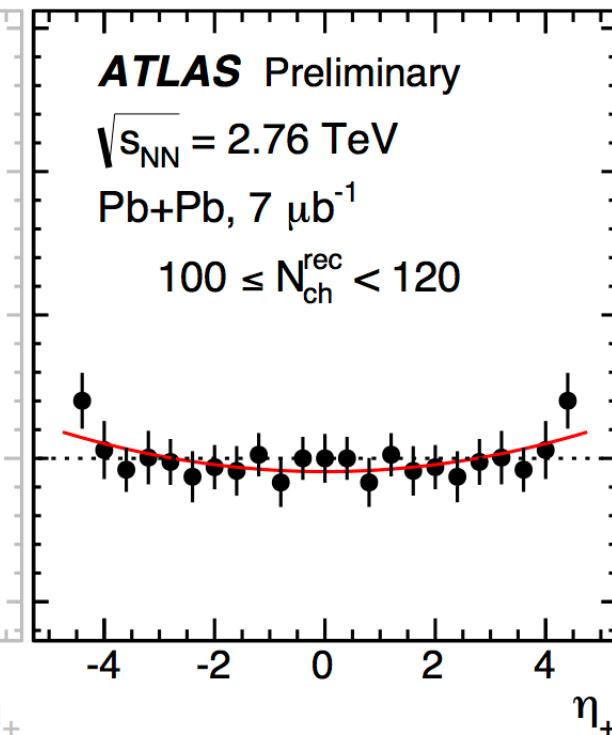
Symmetrized $p+\text{Pb}$



pp



Pb+Pb



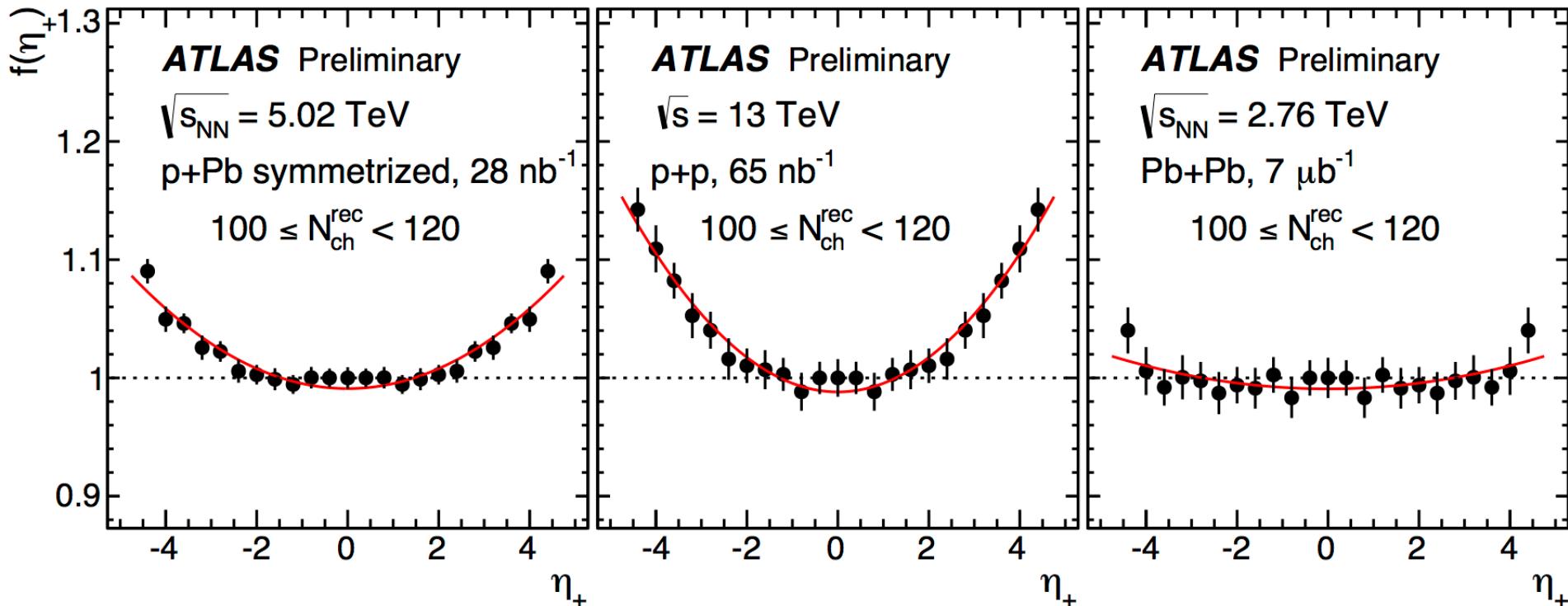
- For better comparison with pp and Pb+Pb , $p+\text{Pb}$ is symmetrized;
- In high-multiplicity pp , SRC shape is slightly larger than $p+\text{Pb}$;
- However in Pb+Pb , SRC shape is more flat.

Compare SRC shape in three systems

Symmetrized $p+\text{Pb}$

pp

$\text{Pb}+\text{Pb}$



- For better comparison with pp and $\text{Pb}+\text{Pb}$, $p+\text{Pb}$ is symmetrized;
- In high-multiplicity pp , SRC shape is slightly larger than $p+\text{Pb}$;
- However in $\text{Pb}+\text{Pb}$, SRC shape is more flat.
- EbyE asymmetry of multiplicity (relative to average multiplicity) in high-multiplicity pp is larger than $p+\text{Pb}$ while $\text{Pb}+\text{Pb}$ collision is more symmetric.

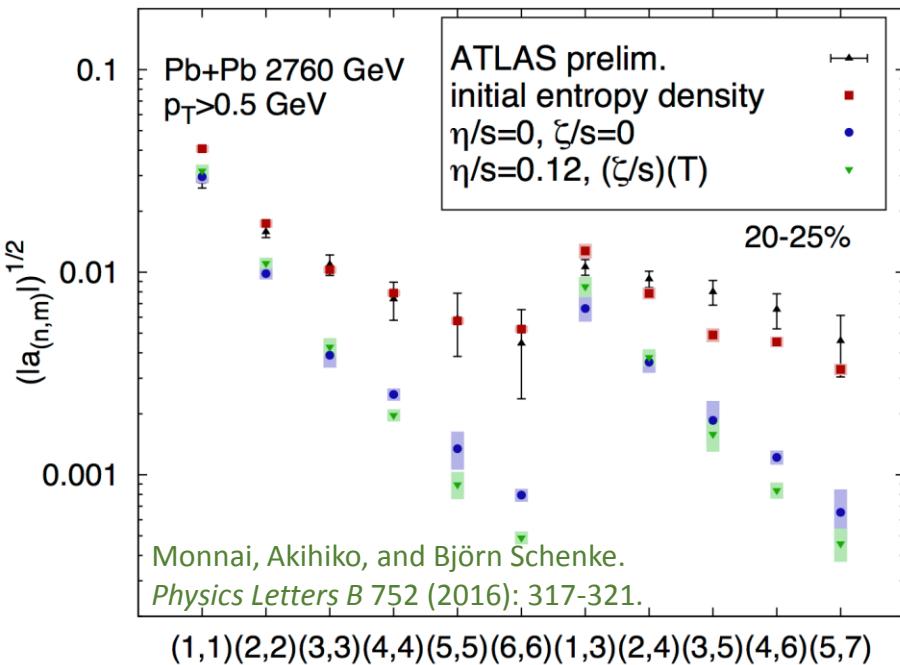
Summary

- Forward-backward multiplicity correlation $C_N(\eta_1, \eta_2)$ is measured in Pb+Pb, $p+\text{Pb}$ and pp collisions at similar event multiplicity.
 - Correlation function consistent of a strong short-range component and a long-range component.
- A data-driven method is used to **estimate SRC** based on the fact that SRC has strong charge dependence, while LRC does not.
- Legendre expansion as well as other three independent methods shows that shape of **LRC** is dominated by leading linear fluctuation $1 + \langle a_1^2 \rangle \eta_1 \eta_2$.
- The N_{ch} -scaling of LRC and SRC across three systems are studied.
 - SRC depends strongly on collision systems and decrease with N_{ch} ;
 - LRC decrease with N_{ch} but independent of system size;
 - Both follows power-law of N_{ch} with an index close to 0.5: information on the number of sources for particle production?
- EbyE asymmetry of multiplicity (relative to the average) in high-multiplicity pp is larger than $p+\text{Pb}$, while Pb+Pb collision is more symmetric.

Summary

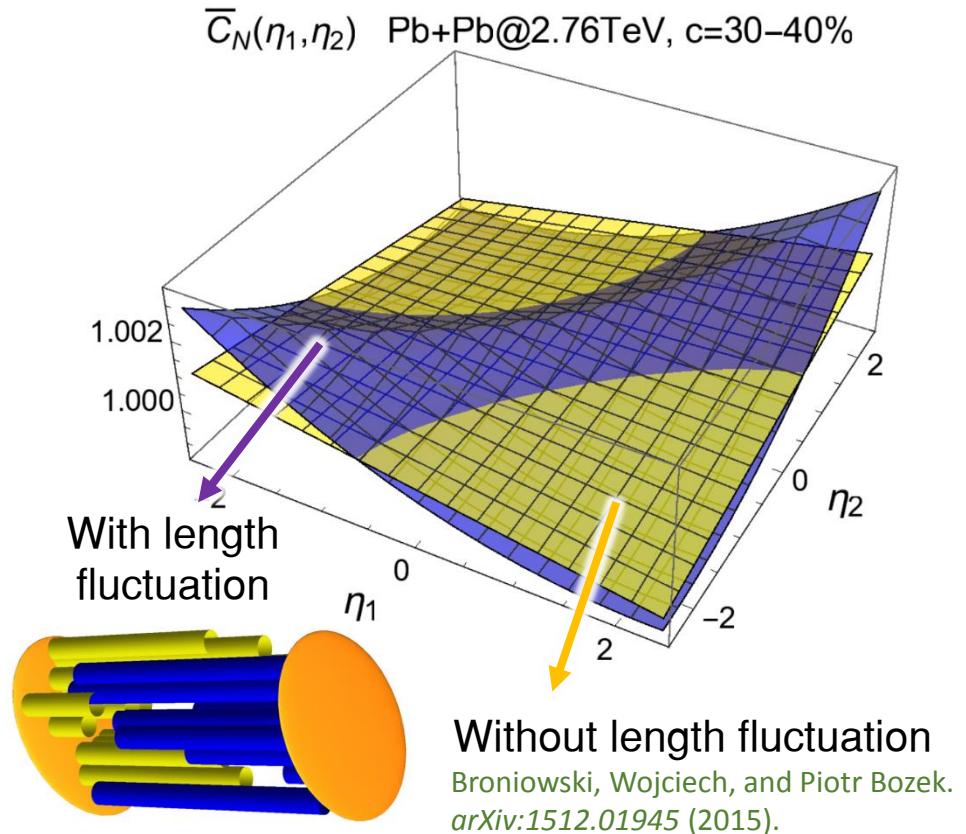
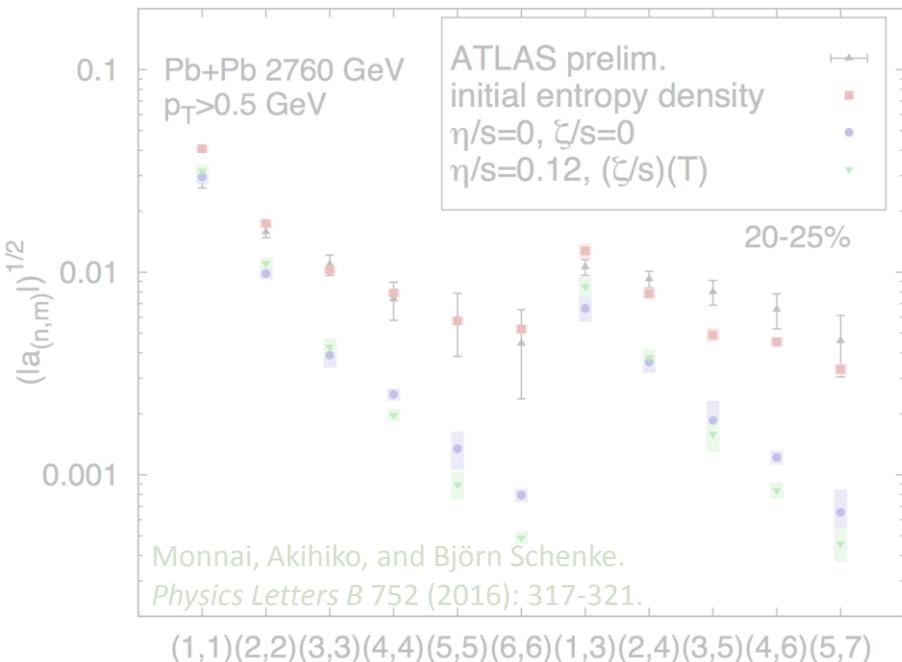
- Forward-backward multiplicity correlation $C_N(\eta_1, \eta_2)$ is measured in Pb+Pb, p+Pb and pp collisions at similar event multiplicity.
 - Correlation function consistent of a strong short range component and a long range component.
- P_1 : FB asymmetry of the EbyE fluctuation
- a_1
- ATLAS Preliminary $p_T > 0.2$ GeV
- $\sigma_{\eta_1}^2$
- N_{ch}
- a_1 from $C_N^{\text{sub}}(\eta_1, \eta_2)$
- Pb+Pb $\sqrt{s_{NN}} = 2.76$ TeV
- p+Pb $\sqrt{s_{NN}} = 5.02$ TeV
- p+p $\sqrt{s} = 13$ TeV
- SRC depends strongly on collision system size;
- LRC decrease with N_{ch} but independent of system size;
- Both follows power-law of N_{ch} with an index close to 0.5: information on the number of sources for particle production?
- EbyE asymmetry of multiplicity (relative to the average) in high-multiplicity pp is larger than p+Pb, while Pb+Pb collision is more symmetric.

Outlook



- Results show the viscous hydro compared with data (LRC+SRC);
- Initial entropy density (modified Glauber) describe the data quite well;
- Hydro-expansion damps the coefficients.

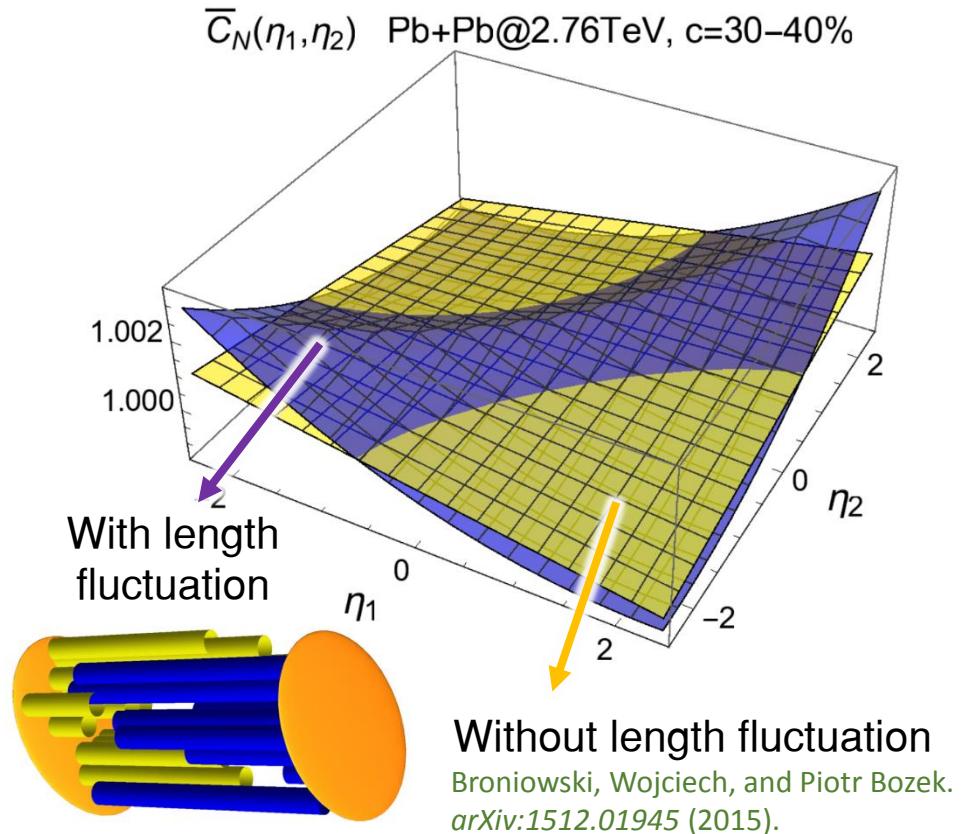
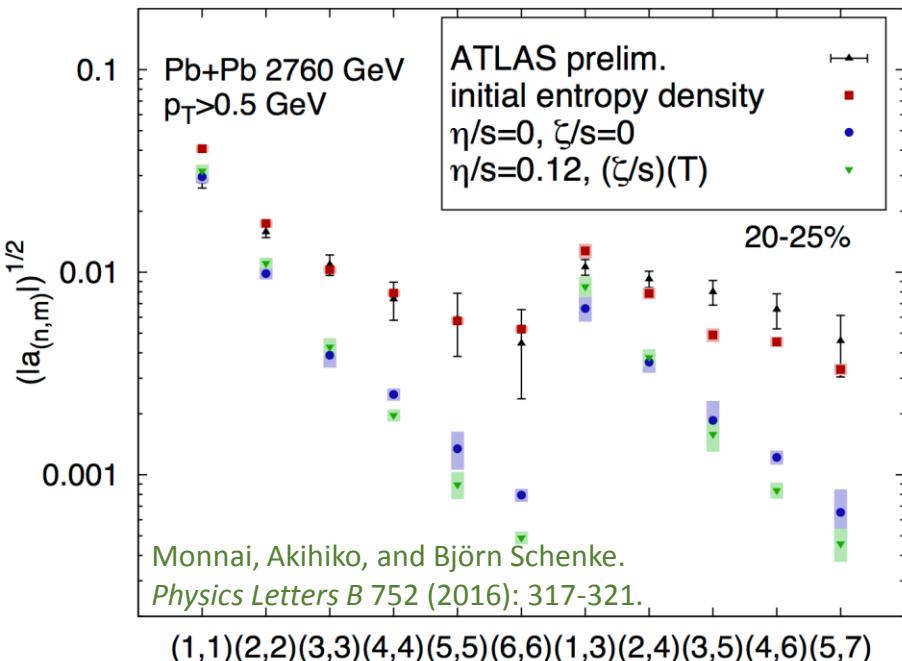
Outlook



- Results show the viscous hydro compared with data (LRC+SRC);
- Initial entropy density (modified Glauber) describe the data quite well;
- Hydro-expansion damps the coefficients.

- Length of sources fluctuation could also explain the shape observed in data.

Outlook

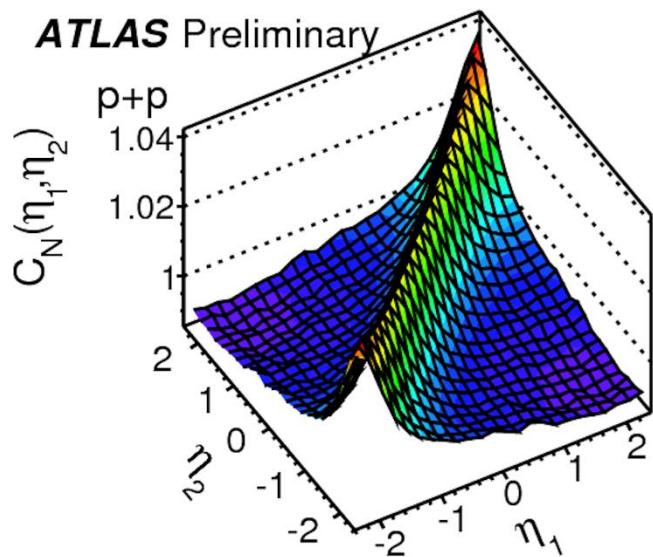


- Results show the viscous hydro compared with data (LRC+SRC);
- Initial entropy density (modified Glauber) describe the data quite well;
- Hydro-expansion damps the coefficients.
- With SRC separated from LRC, these results will provide better constrains to various initial models.

Outlook 2

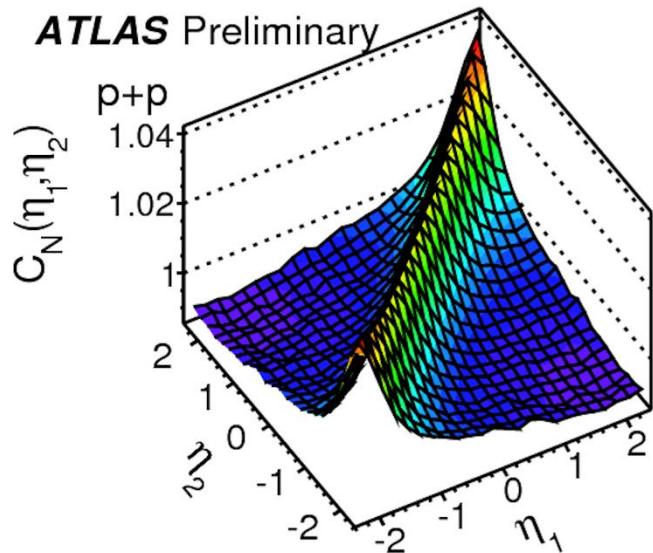
ATLAS Preliminary

- $C(\eta_1, \eta_2)$ is a very comprehensive observable.



Outlook 2

ATLAS Preliminary



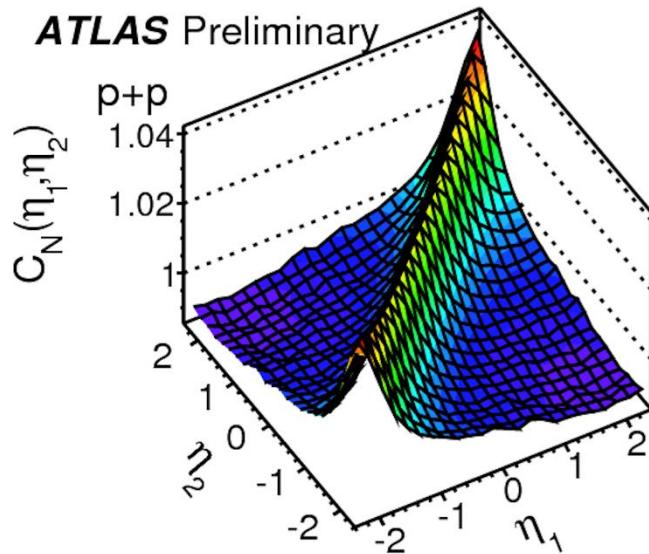
- $C(\eta_1, \eta_2)$ is a very comprehensive observable.

- Reconstruct balance function

$$2B(\Delta\eta) \equiv 2C^{+-}(\Delta\eta) - C^{++}(\Delta\eta) - C^{--}(\Delta\eta)$$

Outlook 2

ATLAS Preliminary



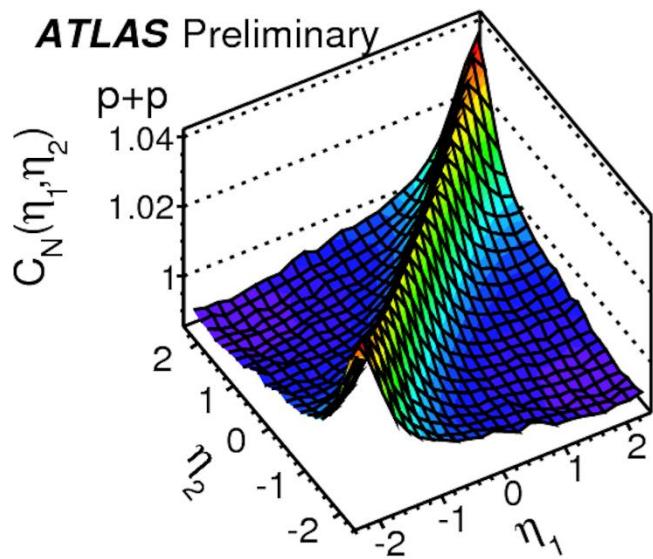
- $C(\eta_1, \eta_2)$ is a very comprehensive observable.
- Reconstruct balance function
- Test factorization: high- p_T a_n^H and low- p_T a_n^L

$$2B(\Delta\eta) \equiv 2C^{+-}(\Delta\eta) - C^{++}(\Delta\eta) - C^{--}(\Delta\eta)$$

$$r_n \equiv \frac{\langle a_n^H a_n^L \rangle}{\sqrt{\langle a_n^H a_n^H \rangle} \sqrt{\langle a_n^L a_n^L \rangle}}$$

Outlook 2

ATLAS Preliminary



- $C(\eta_1, \eta_2)$ is a very comprehensive observable.

- Reconstruct balance function

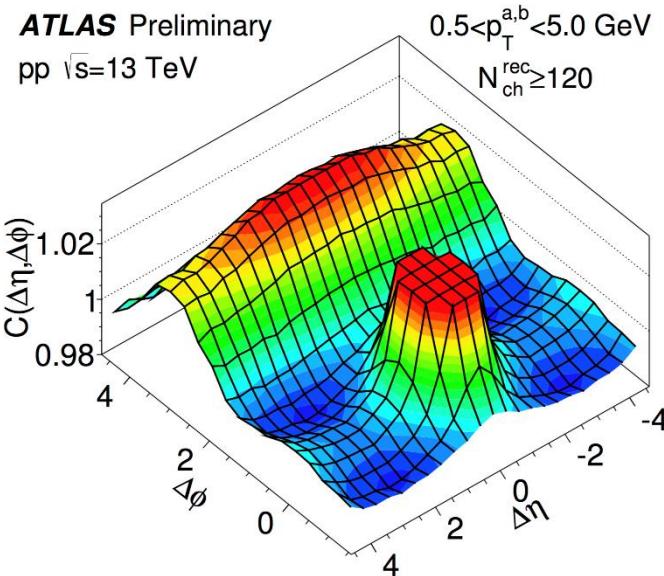
$$2B(\Delta\eta) \equiv 2C^{+-}(\Delta\eta) - C^{++}(\Delta\eta) - C^{--}(\Delta\eta)$$

- Test factorization: high- p_T a_n^H and low- p_T a_n^L

$$r_n \equiv \frac{\langle a_n^H a_n^L \rangle}{\sqrt{\langle a_n^H a_n^H \rangle} \sqrt{\langle a_n^L a_n^L \rangle}}$$

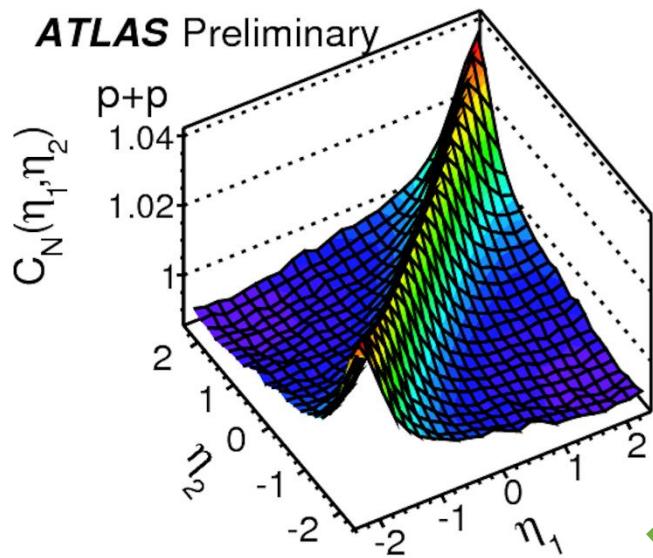
ATLAS Preliminary

pp $\sqrt{s}=13$ TeV



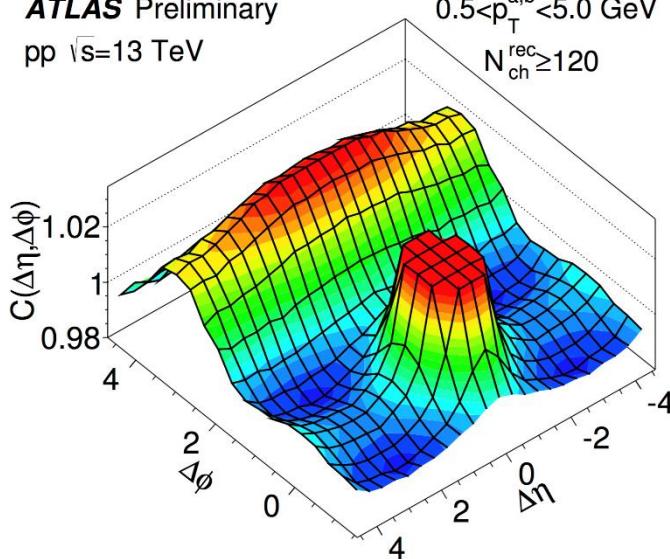
Outlook 2

ATLAS Preliminary



ATLAS Preliminary

pp $\sqrt{s}=13$ TeV



- $C(\eta_1, \eta_2)$ is a very comprehensive observable.

- Reconstruct balance function

$$2B(\Delta\eta) \equiv 2C^{+-}(\Delta\eta) - C^{++}(\Delta\eta) - C^{--}(\Delta\eta)$$

- Test factorization: high- p_T a_n^H and low- p_T a_n^L

$$r_n \equiv \frac{\langle a_n^H a_n^L \rangle}{\sqrt{\langle a_n^H a_n^H \rangle} \sqrt{\langle a_n^L a_n^L \rangle}}$$

$C(\eta_1, \eta_2)$

+

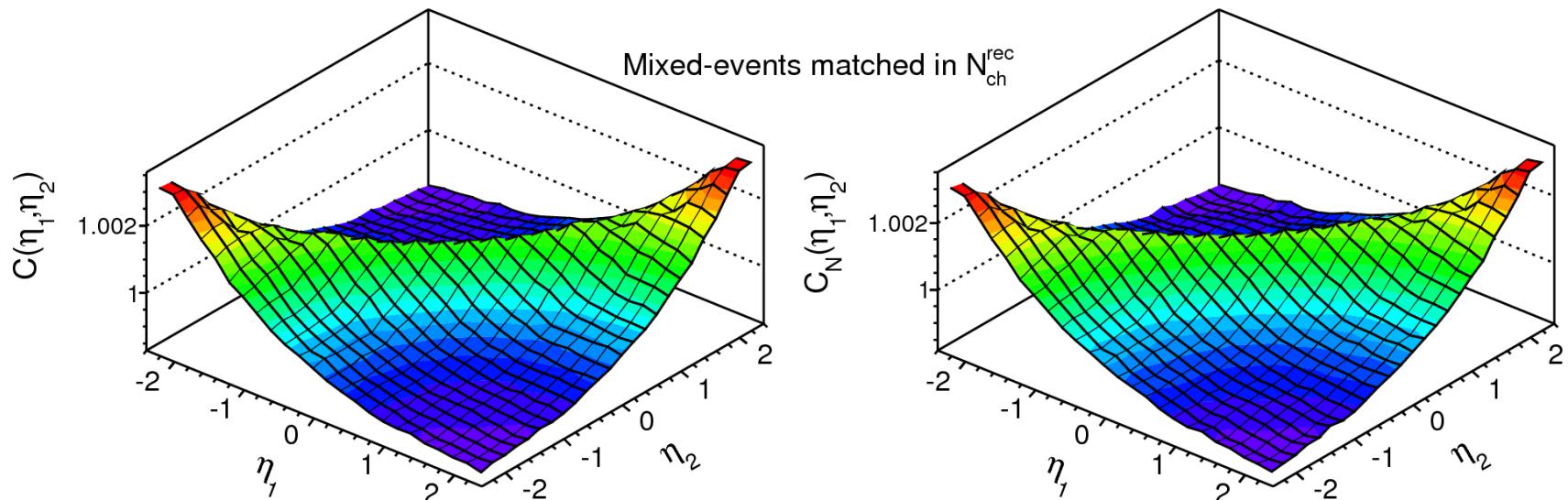
$C(\Delta\eta, \Delta\phi)$

$C(\eta_1, \eta_2, \Delta\phi) !$

Back-up

Initial Stages 2016, Lisbon

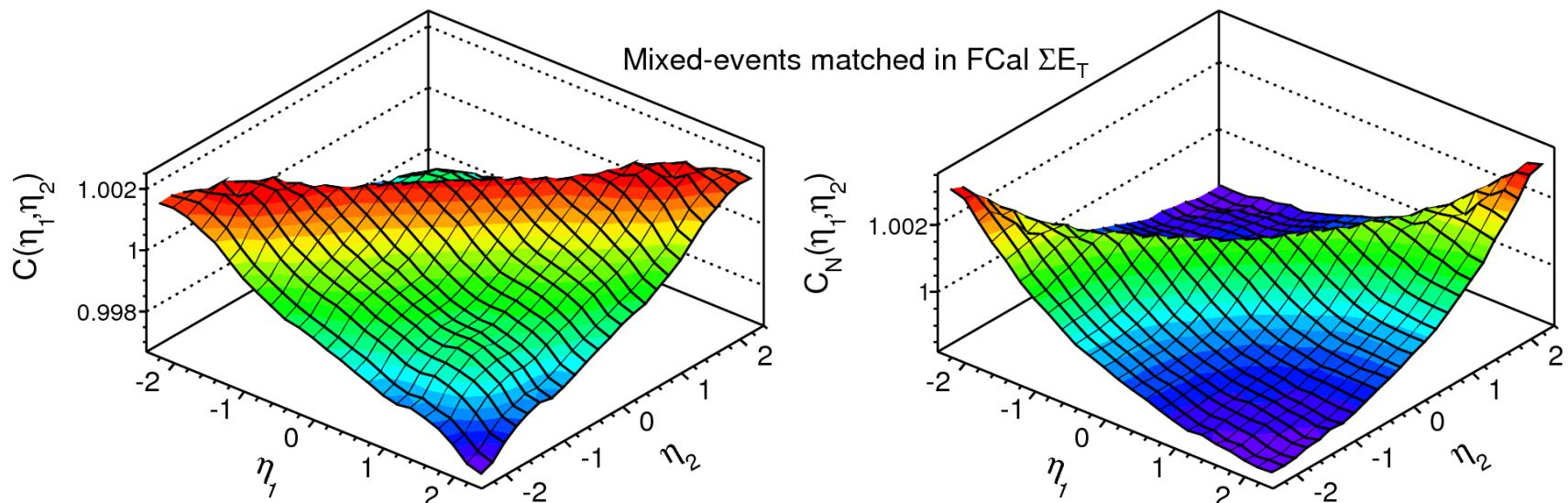
Residual centrality dependence



$p_T > 0.5 \text{ GeV}$

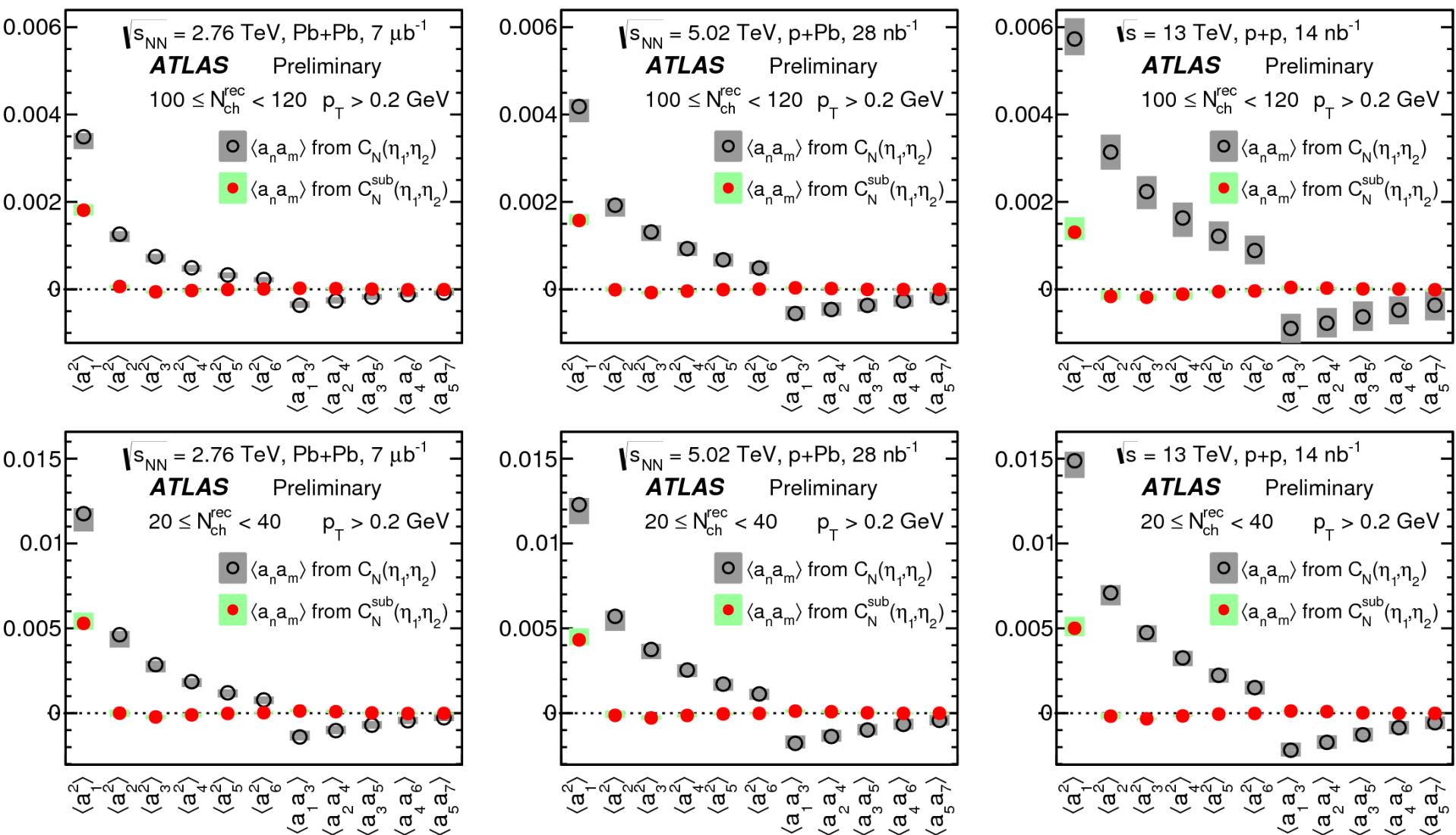
ATLAS Preliminary, Centrality 35-40%

$\sqrt{s_{\text{NN}}} = 2.76 \text{ TeV}, \text{Pb+Pb}, L \approx 7 \mu\text{b}^{-1}$



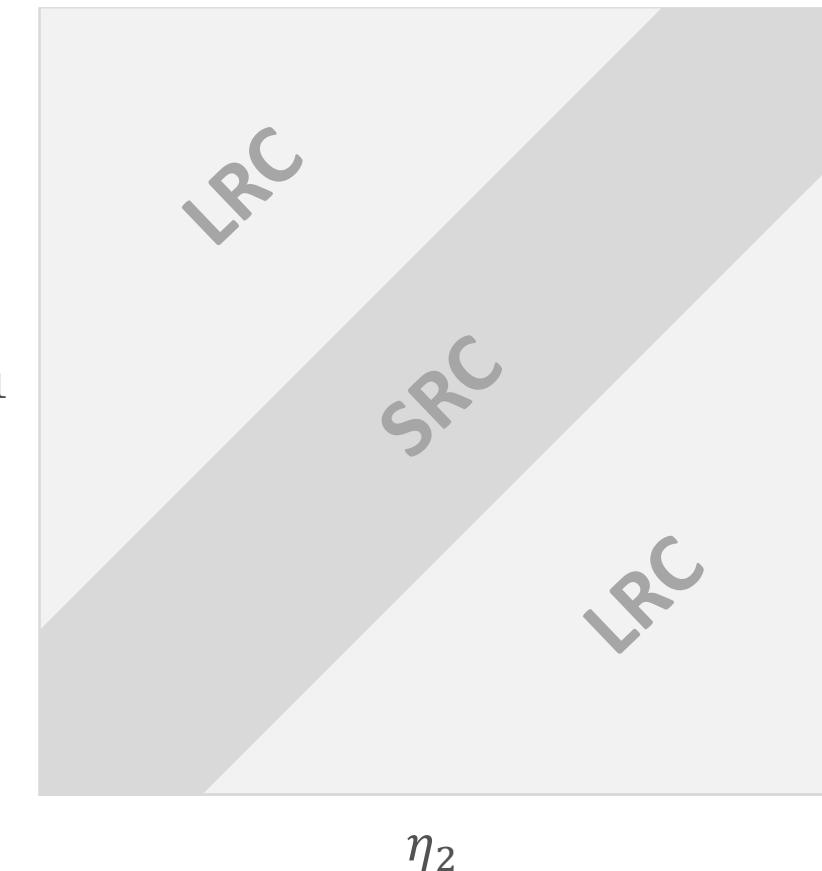
Initial Stages 2016, Lisbon

Spectrum: before and after SRC subtraction



Other methods to measure $\langle a_1^2 \rangle$

$$C_N(\eta_1, \eta_2)$$

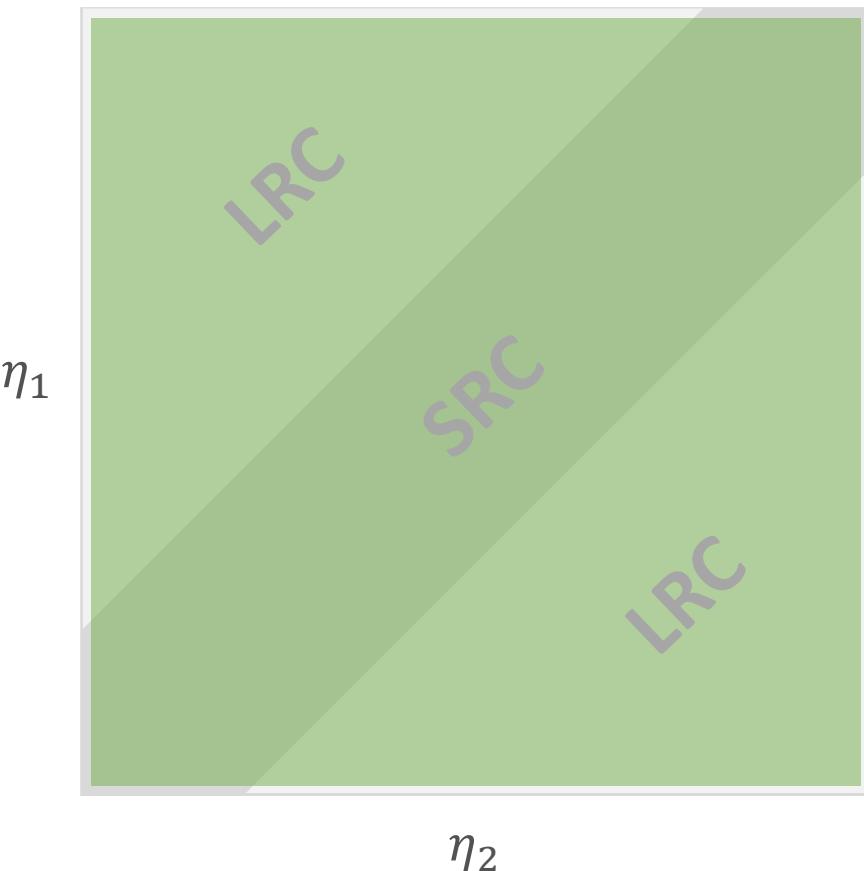


Other methods to measure $\langle a_1^2 \rangle$

$$C_N(\eta_1, \eta_2)$$

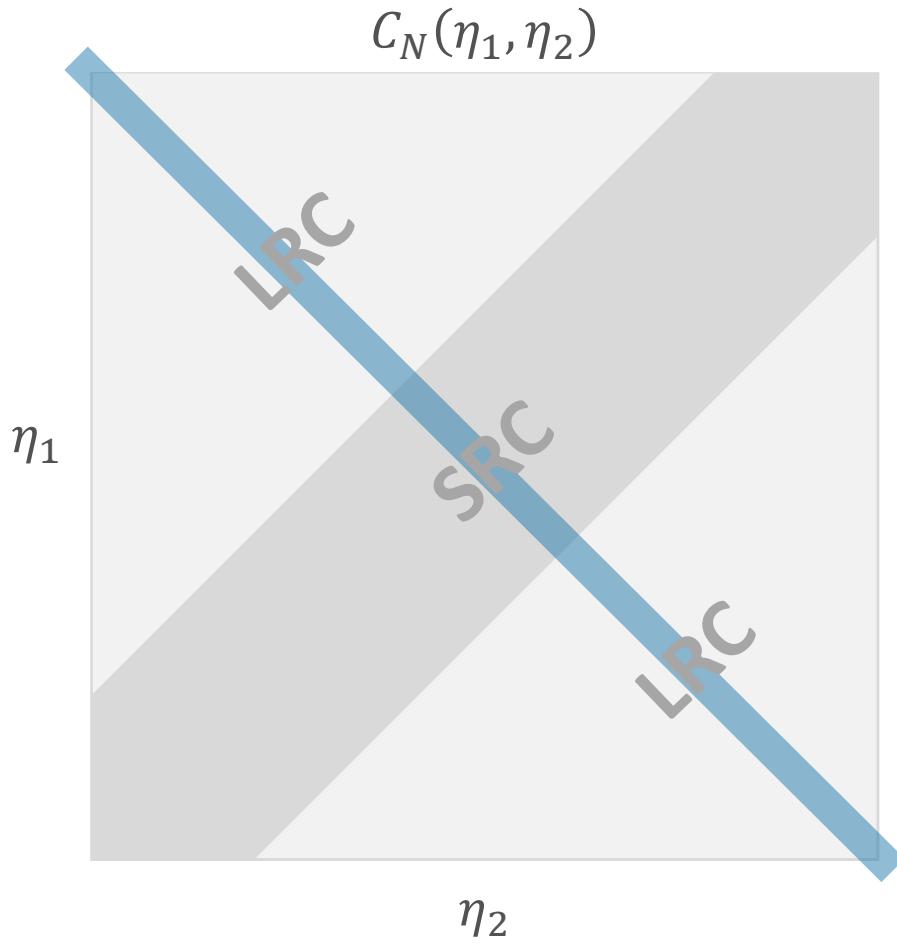
- Expansion of $C_N^{sub}(\eta_1, \eta_2)$

$$C_N^{sub}(\eta_1, \eta_2) = 1 + \langle a_1^2 \rangle \eta_1 \eta_2$$



- Use whole (η_1, η_2) space.

Other methods to measure $\langle a_1^2 \rangle$



- Longest level arm for SRC estimation.

- Expansion of $C_N^{sub}(\eta_1, \eta_2)$

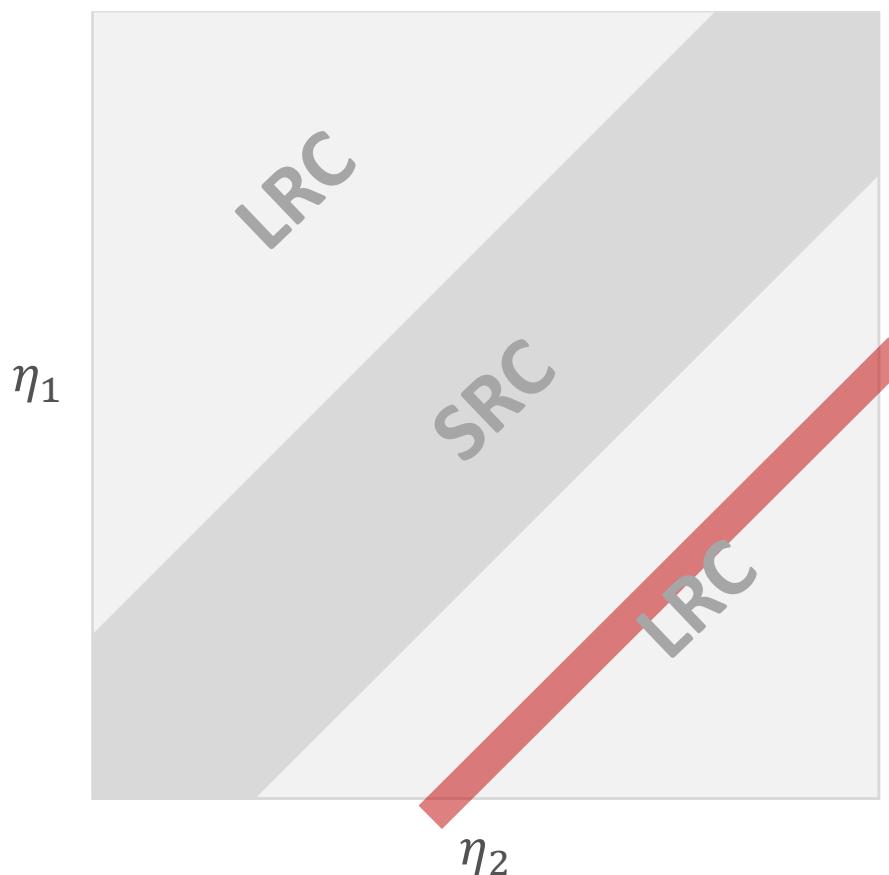
$$C_N^{sub}(\eta_1, \eta_2) = 1 + \langle a_1^2 \rangle \eta_1 \eta_2$$

- Quadratic fit along $C_N^{sub}(\eta_-)$

$$C_N^{sub}(\eta_-) = 1 + \frac{\langle a_1^2 \rangle}{4} (\eta_+^2 - \eta_-^2)$$

Other methods to measure $\langle a_1^2 \rangle$

$$C_N(\eta_1, \eta_2)$$



- Expansion of $C_N^{sub}(\eta_1, \eta_2)$

$$C_N^{sub}(\eta_1, \eta_2) = 1 + \langle a_1^2 \rangle \eta_1 \eta_2$$

- Quadratic fit along $C_N^{sub}(\eta_-)$

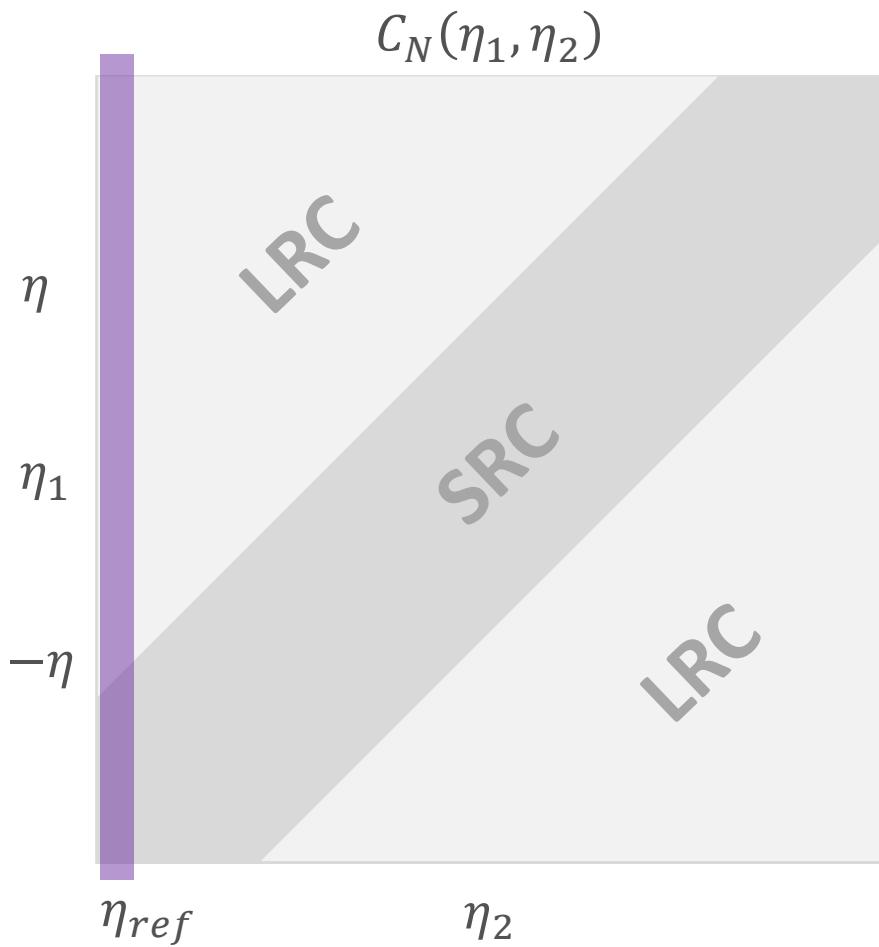
$$C_N^{sub}(\eta_-) = 1 + \frac{\langle a_1^2 \rangle}{4} (\eta_+^2 - \eta_-^2)$$

- Quadratic fit along $C_N^{sub}(\eta_+)$

$$C_N^{sub}(\eta_-) = 1 + \frac{\langle a_1^2 \rangle}{4} (\eta_+^2 - \eta_-^2)$$

- Outside the SRC region, not affected by the SRC removal procedure.

Other methods to measure $\langle a_1^2 \rangle$



- Residual centrality dependence cancels out.

- Expansion of $C_N^{sub}(\eta_1, \eta_2)$

$$C_N^{sub}(\eta_1, \eta_2) = 1 + \langle a_1^2 \rangle \eta_1 \eta_2$$

- Quadratic fit along $C_N^{sub}(\eta_-)$

$$C_N^{sub}(\eta_-) = 1 + \frac{\langle a_1^2 \rangle}{4} (\eta_+^2 - \eta_-^2)$$

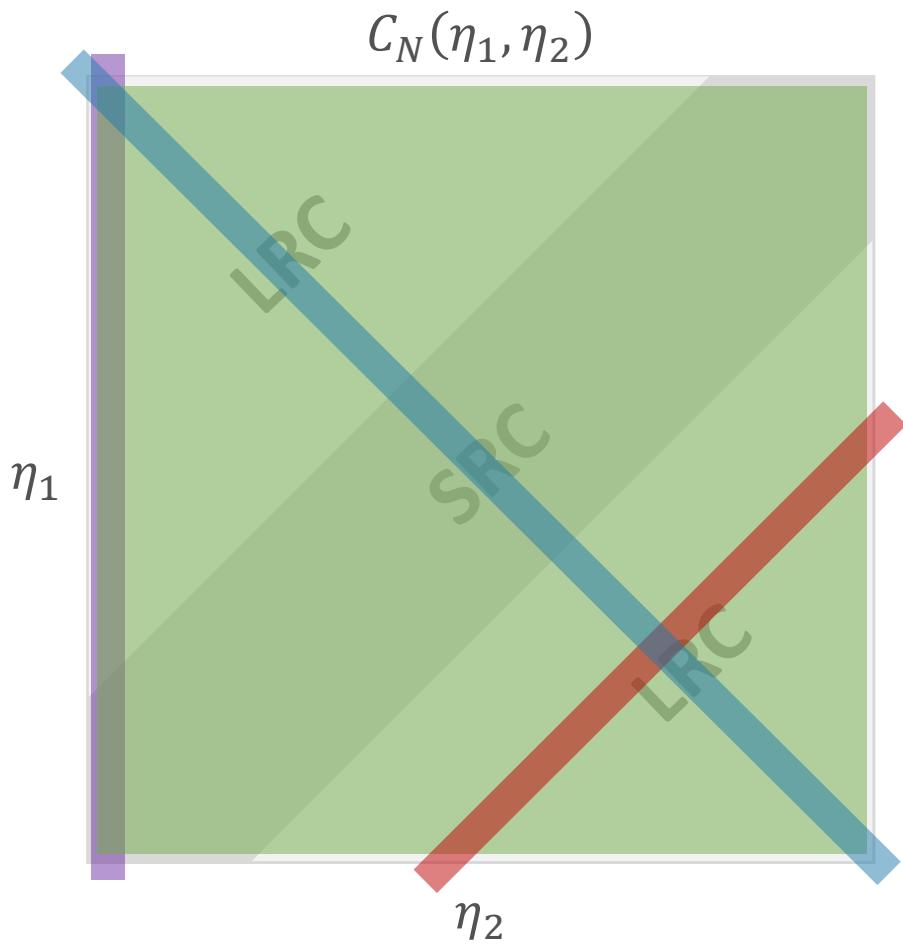
- Quadratic fit along $C_N^{sub}(\eta_+)$

$$C_N^{sub}(\eta_+) = 1 + \frac{\langle a_1^2 \rangle}{4} (\eta_+^2 - \eta_-^2)$$

- Linear fit of $r_N^{sub}(\eta, \eta_{ref}) \equiv \frac{C_N^{sub}(-\eta, \eta_{ref})}{C_N^{sub}(\eta, \eta_{ref})}$

$$r_N^{sub}(\eta, \eta_{ref}) = 1 - 2\langle a_1^2 \rangle \eta \eta_{ref}$$

Other methods to measure $\langle a_1^2 \rangle$



- Four methods have different responses of the analysis procedures, and are largely independent.

- Expansion of $C_N^{sub}(\eta_1, \eta_2)$

$$C_N^{sub}(\eta_1, \eta_2) = 1 + \langle a_1^2 \rangle \eta_1 \eta_2$$

- Quadratic fit along $C_N^{sub}(\eta_-)$

$$C_N^{sub}(\eta_-) = 1 + \frac{\langle a_1^2 \rangle}{4} (\eta_+^2 - \eta_-^2)$$

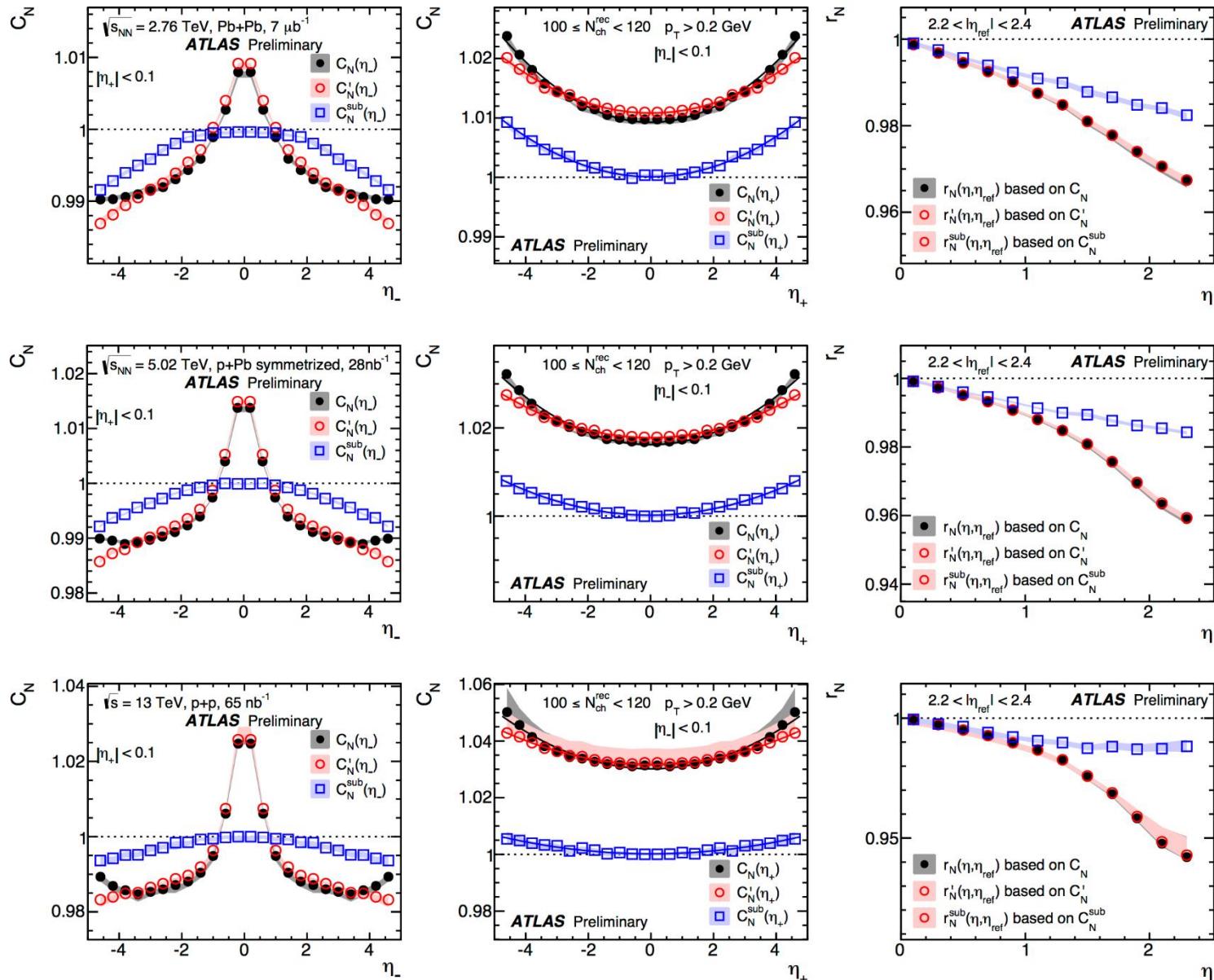
- Quadratic fit along $C_N^{sub}(\eta_+)$

$$C_N^{sub}(\eta_+) = 1 + \frac{\langle a_1^2 \rangle}{4} (\eta_+^2 - \eta_-^2)$$

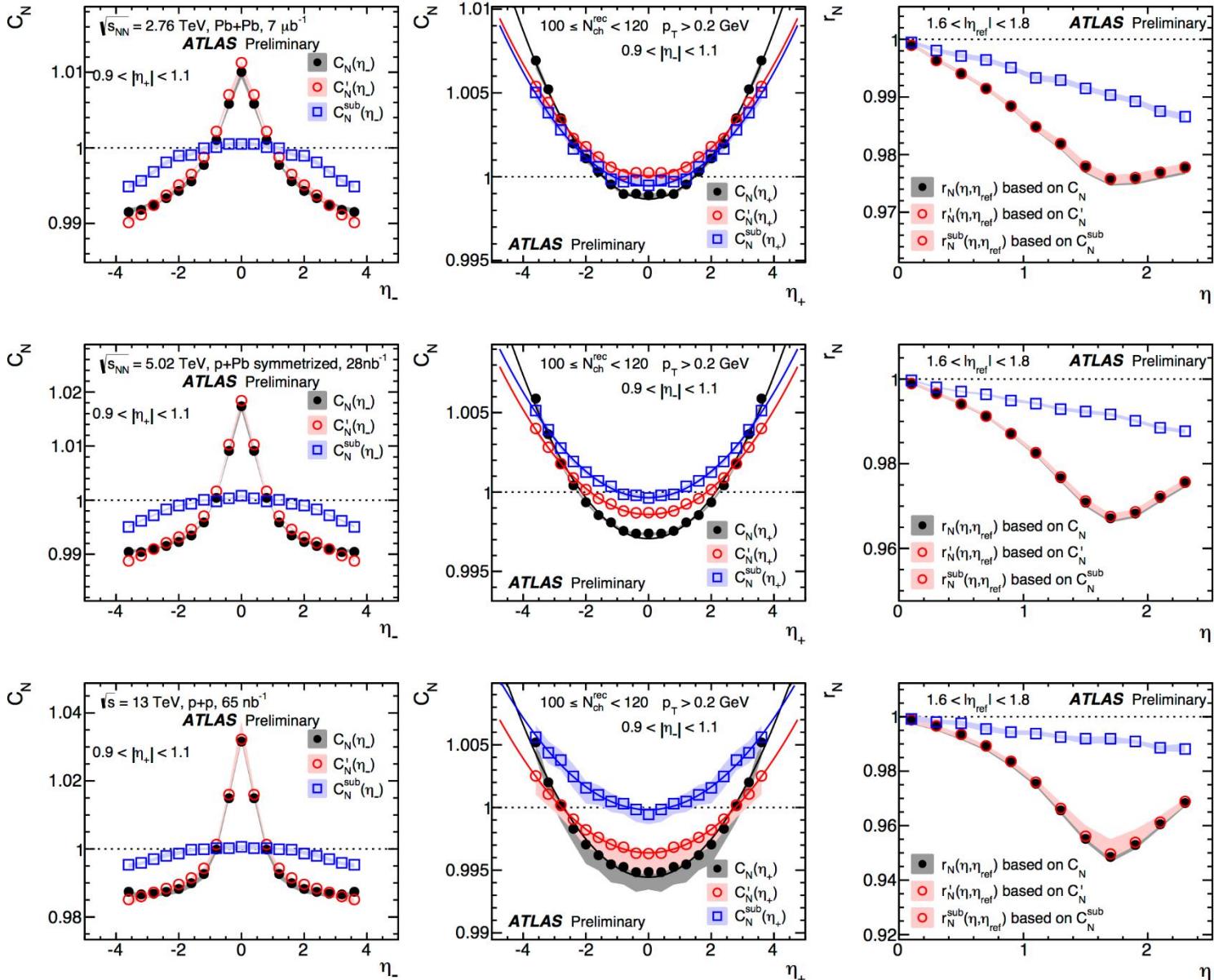
- Linear fit of $r_N^{sub}(\eta, \eta_{ref}) \equiv \frac{C_N^{sub}(-\eta, \eta_{ref})}{C_N^{sub}(\eta, \eta_{ref})}$

$$r_N^{sub}(\eta, \eta_{ref}) = 1 - 2\langle a_1^2 \rangle \eta \eta_{ref}$$

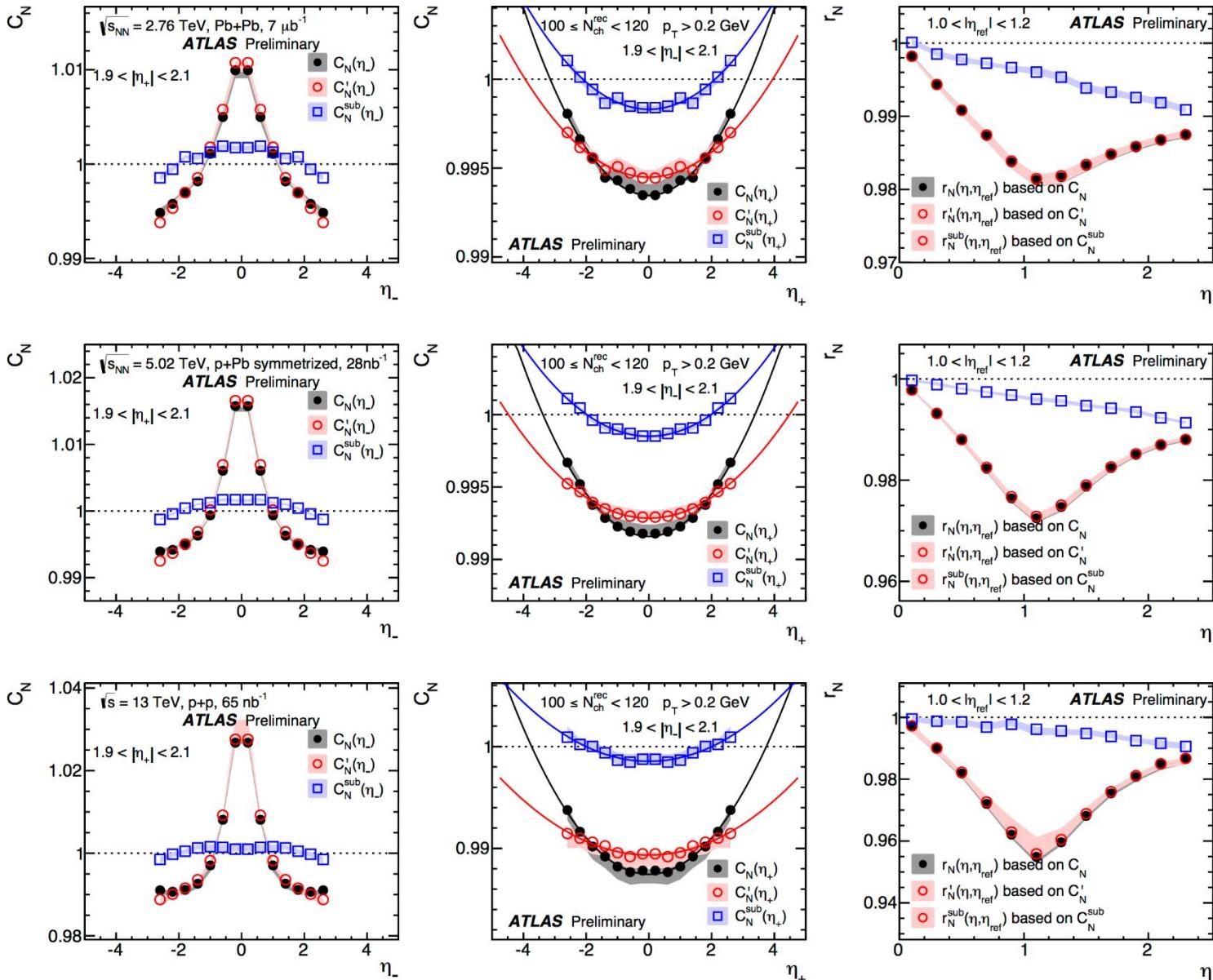
Projection of $C_N(\eta_1, \eta_2)$: position 1



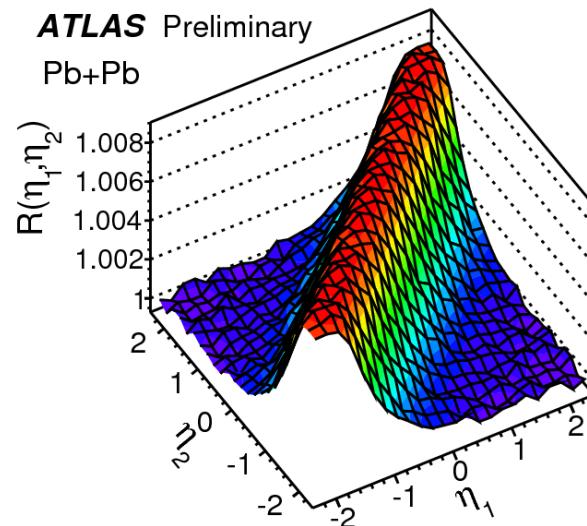
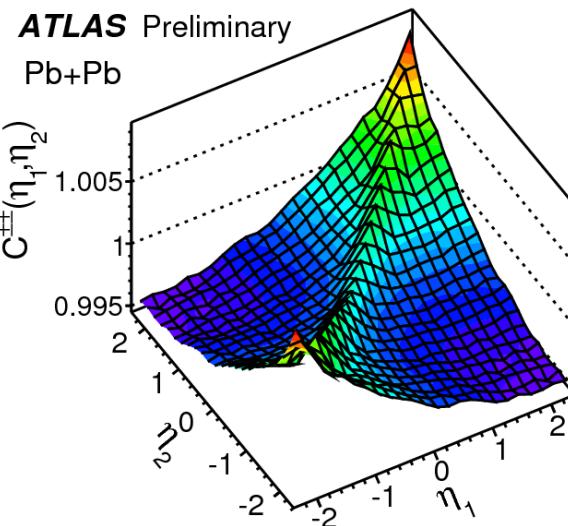
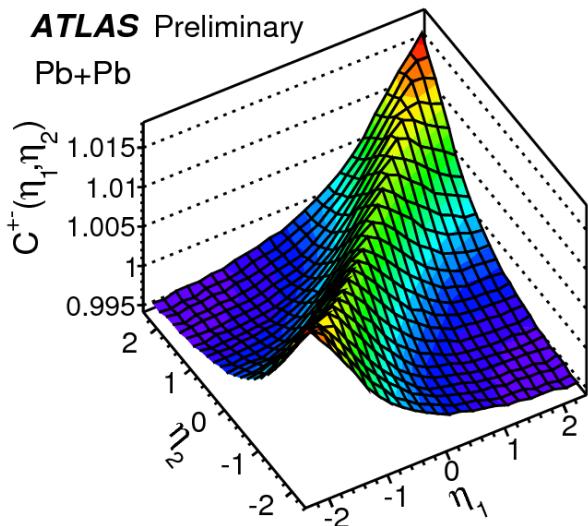
Projection of $C_N(\eta_1, \eta_2)$: position 2



Projection of $C_N(\eta_1, \eta_2)$: position 3



Gaussian width of fitting $R(\eta_1, \eta_2)$

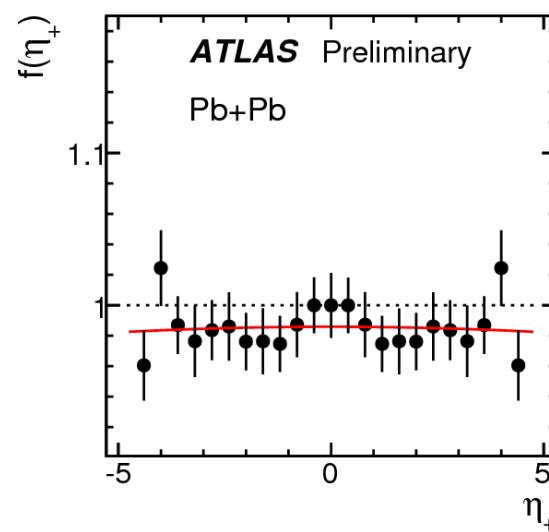
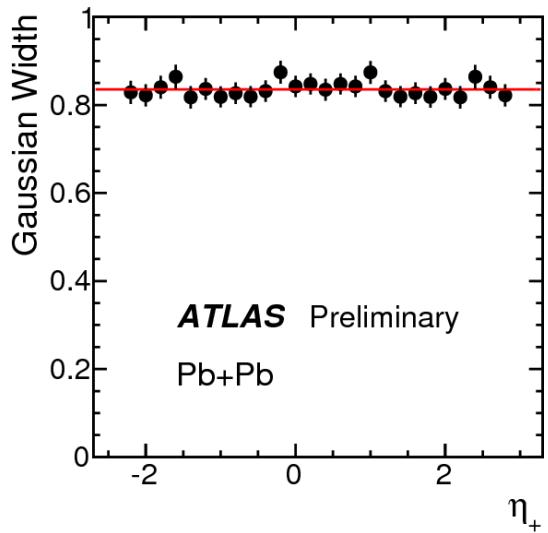


ATLAS Preliminary

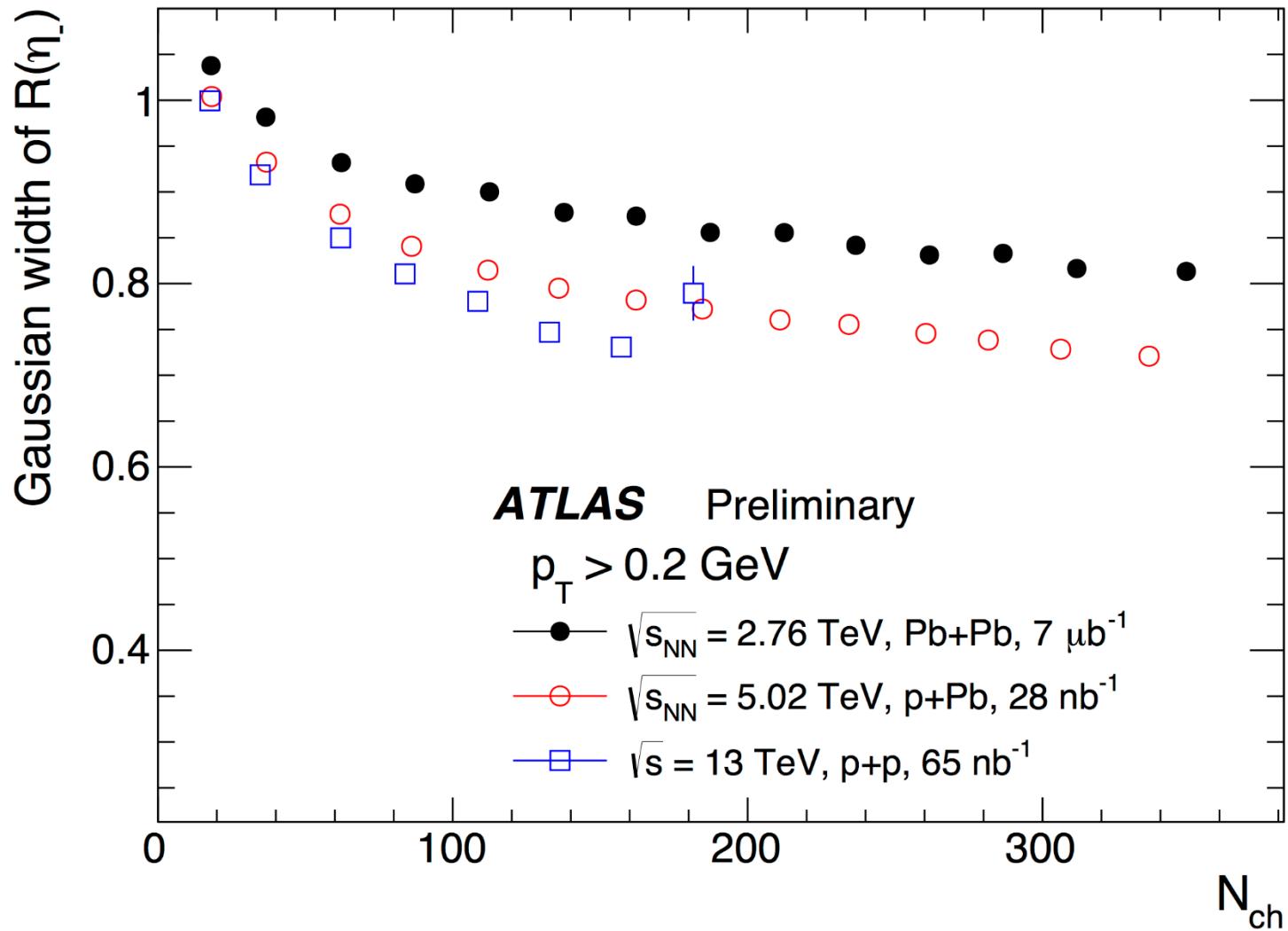
$200 \leq N_{\text{ch}}^{\text{rec}} < 220$

$\sqrt{s_{\text{NN}}} = 2.76 \text{ TeV, Pb+Pb, } 7 \mu\text{b}^{-1}$

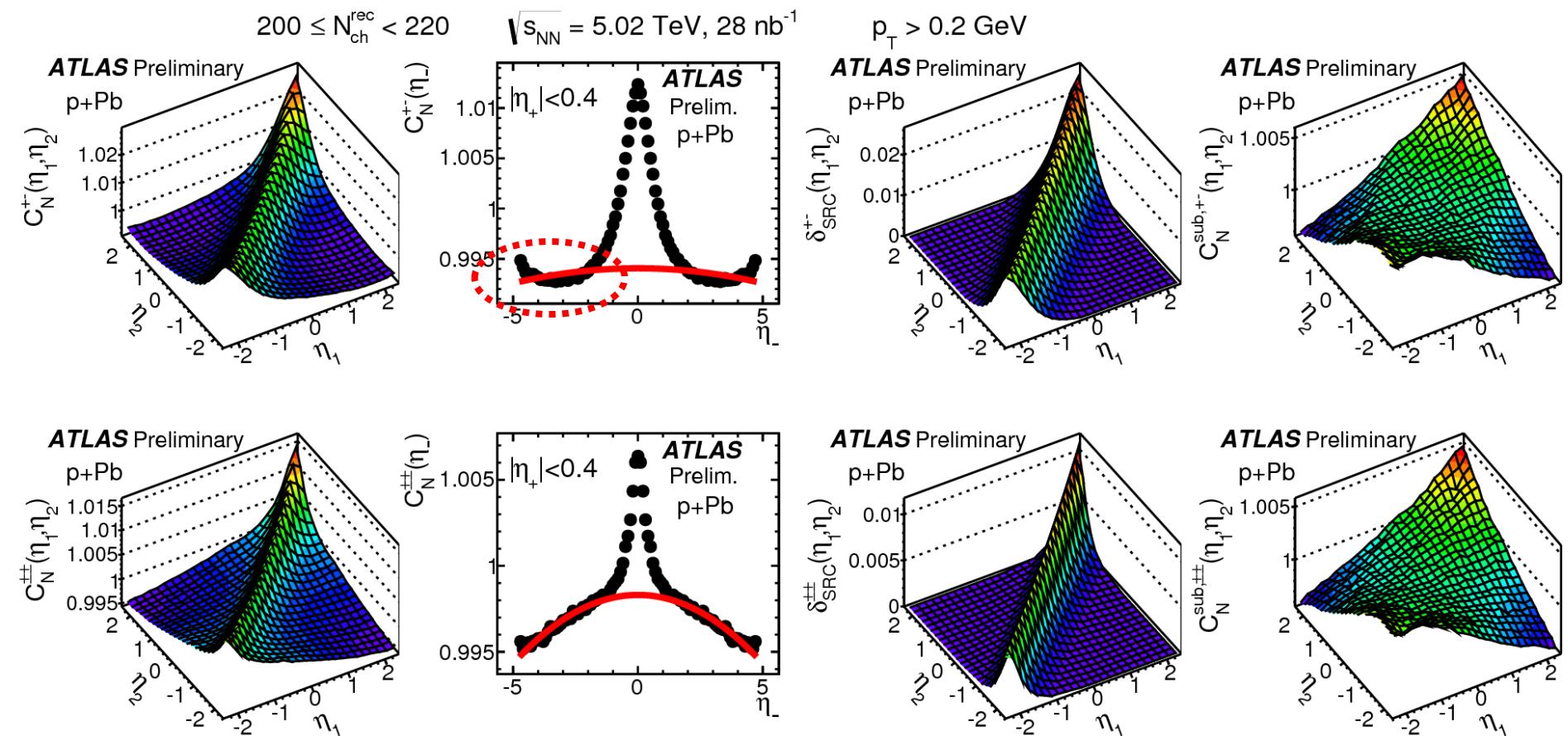
$p_T > 0.2 \text{ GeV}$



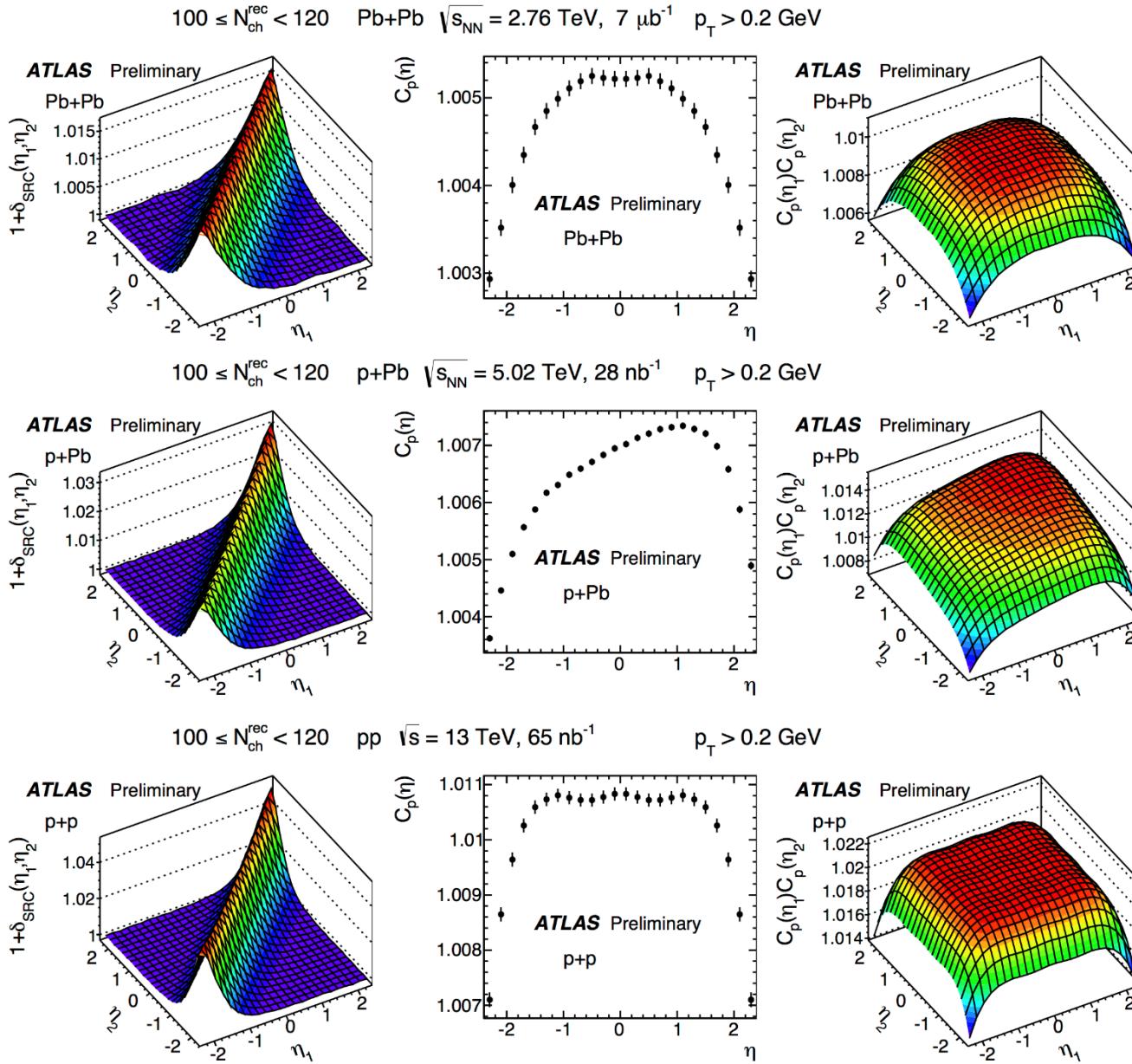
Gaussian width as a function of N_{ch}



Detector acceptance from SRC



Detector acceptance from SRC



Detector acceptance from SRC

- In general, the raw CF $C(\eta_1, \eta_2)$ could be decomposed as

$$C = C_{LRC} + C_{SRC} + C_{SPM}$$

where C_{SPM} is the contribution from single particle mode, and it could be removed through normalizing C_{RAW} by the projections of itself C_{RAW}^{proj} , where

$$C^{proj} = C_{LRC}^{proj} + C_{SRC}^{proj} + C_{SPM}^{proj}$$

- Notice here $C_{LRC}^{proj} = 1$ because $\langle a_m a_n \rangle_{m,n \neq 0}^{proj} = 0$, and because C_{SPM} is supposed to be factorized in the (η_1, η_2) plane, so $C_{SPM} = C_{SPM}^{proj}$. Then we have

$$C_N \equiv C/C^{proj} \approx C_{LRC} + C_{SRC} - C_{SRC}^{proj}$$

where C_{SRC}^{proj} didn't vanish due to the acceptance effects;

- Because of the presence of C_{SRC}^{proj} , the estimated SRC C_{SRC}^{est} will be biased

$$C_{SRC}^{est} = C_{SRC} + C_{SRC}^{bias}$$

where C_{SRC}^{bias} denotes the bias;

- However, if we calculate the projections of C_{SRC}^{est}

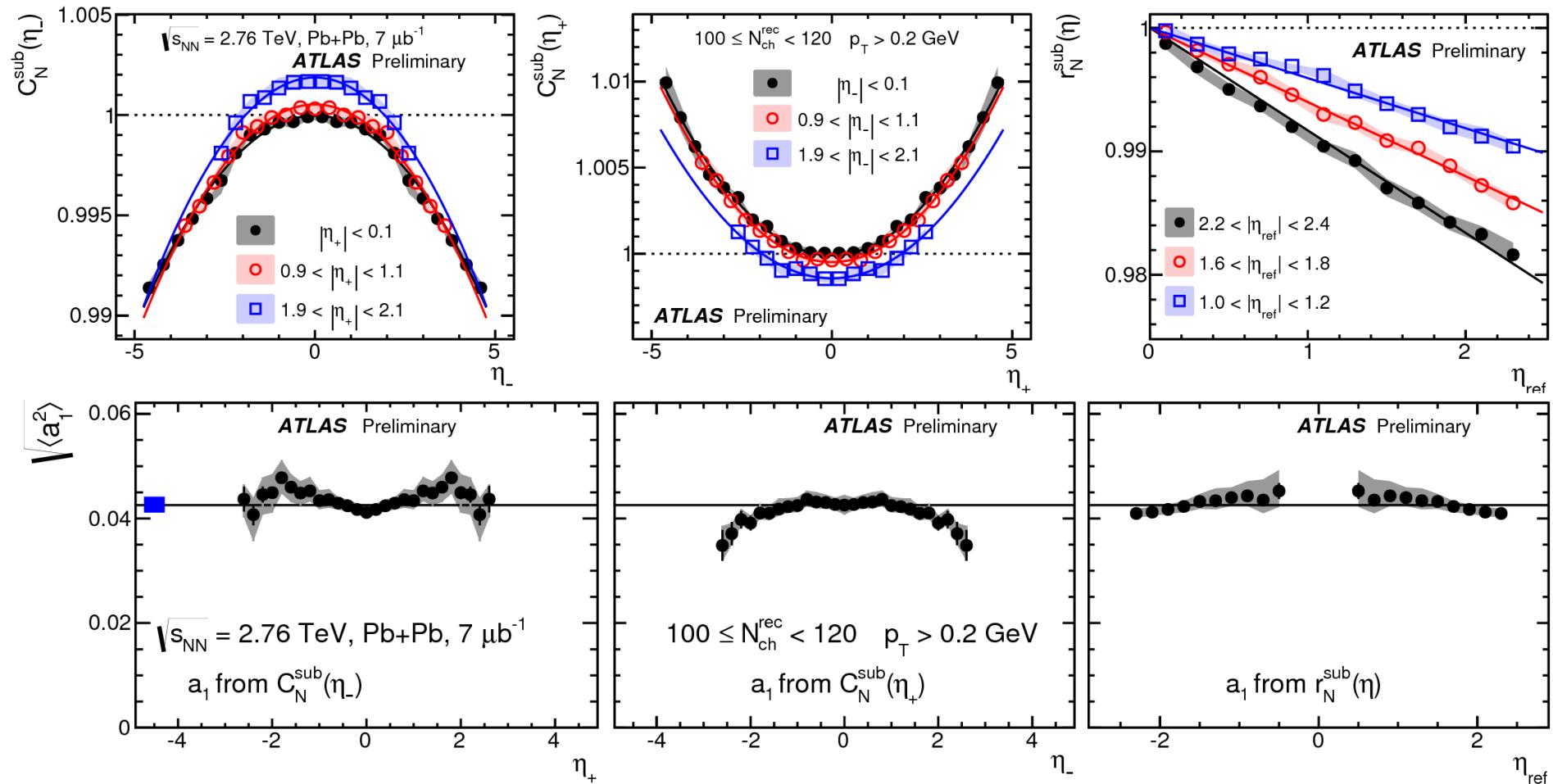
$$[C_{SRC}^{est}]^{proj} = C_{SRC}^{proj} + [C_{SRC}^{bias}]^{proj} \approx C_{SRC}^{proj}$$

where $[C_{SRC}^{bias}]^{proj}$ is negligible as long as the $C_{SRC}^{bias} \ll C_{SRC}$ (it is true in this analysis, if not, more iteration required until this relation holds);

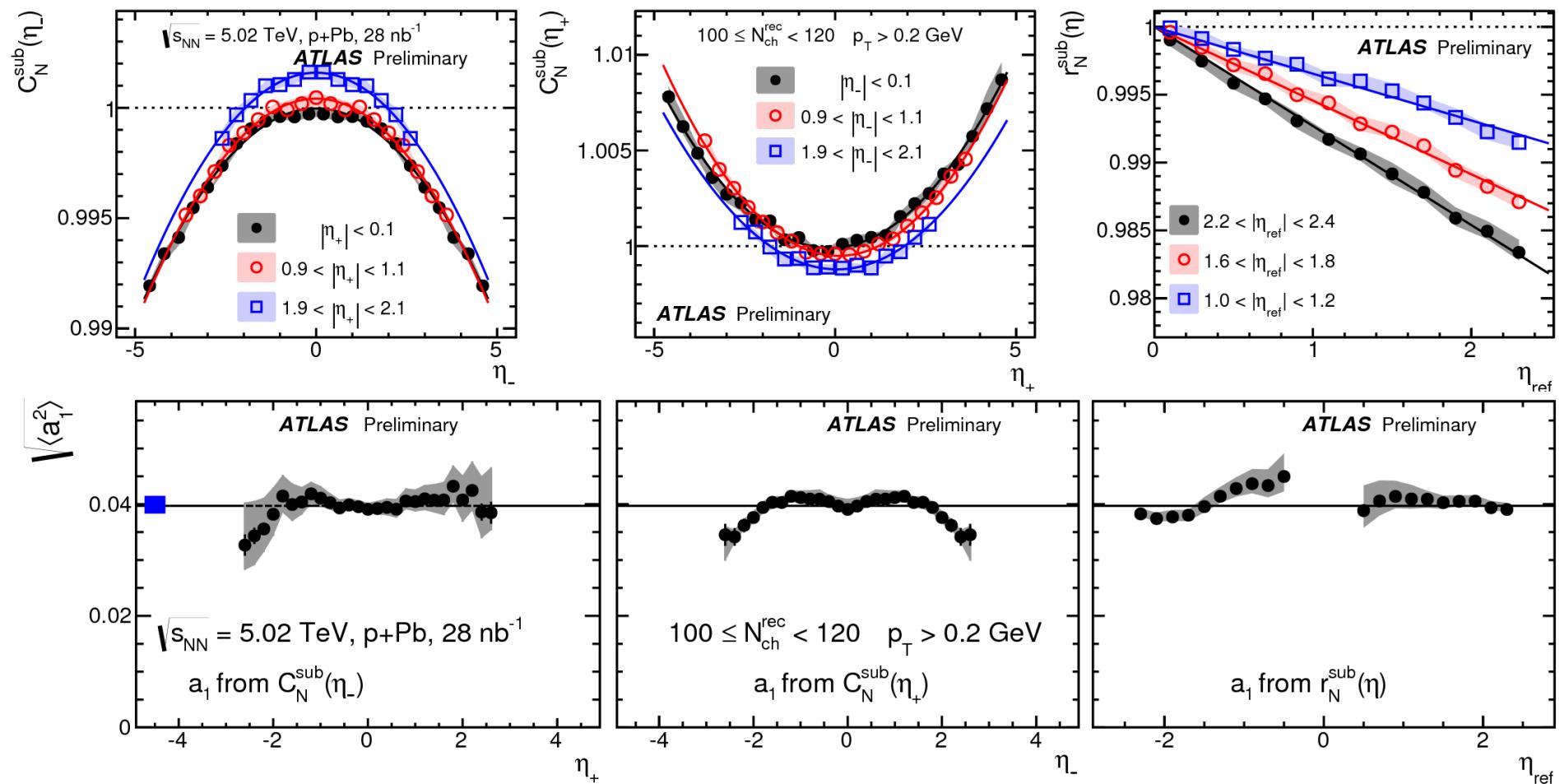
- Finally, the contamination term $-C_{SRC}^{proj}$ could be subtracted from C_N

$$C'_N \equiv C_N + [C_{SRC}^{est}]^{proj} = C_{LRC} + C_{SRC}$$

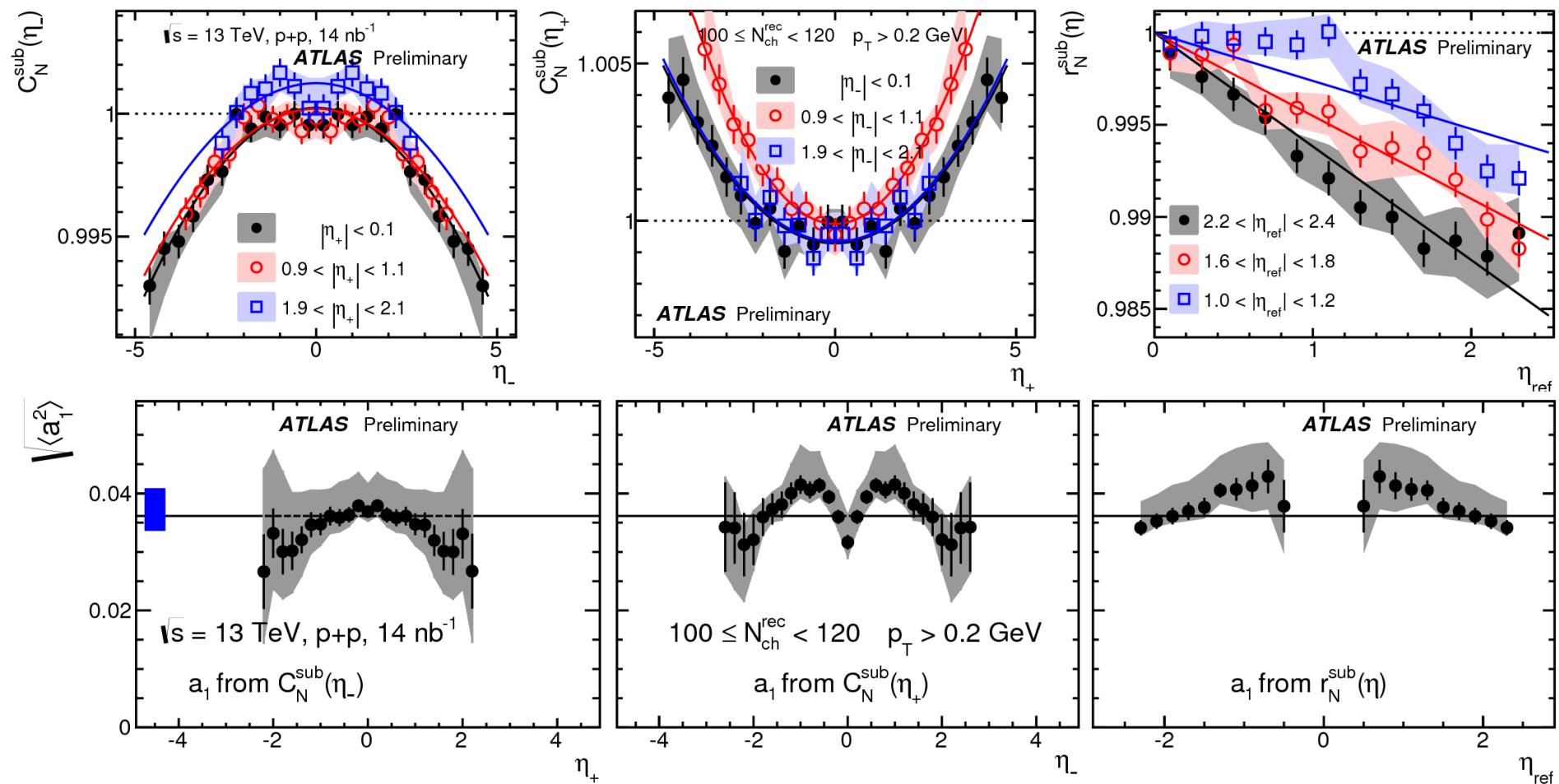
Scan of projections: Pb+Pb



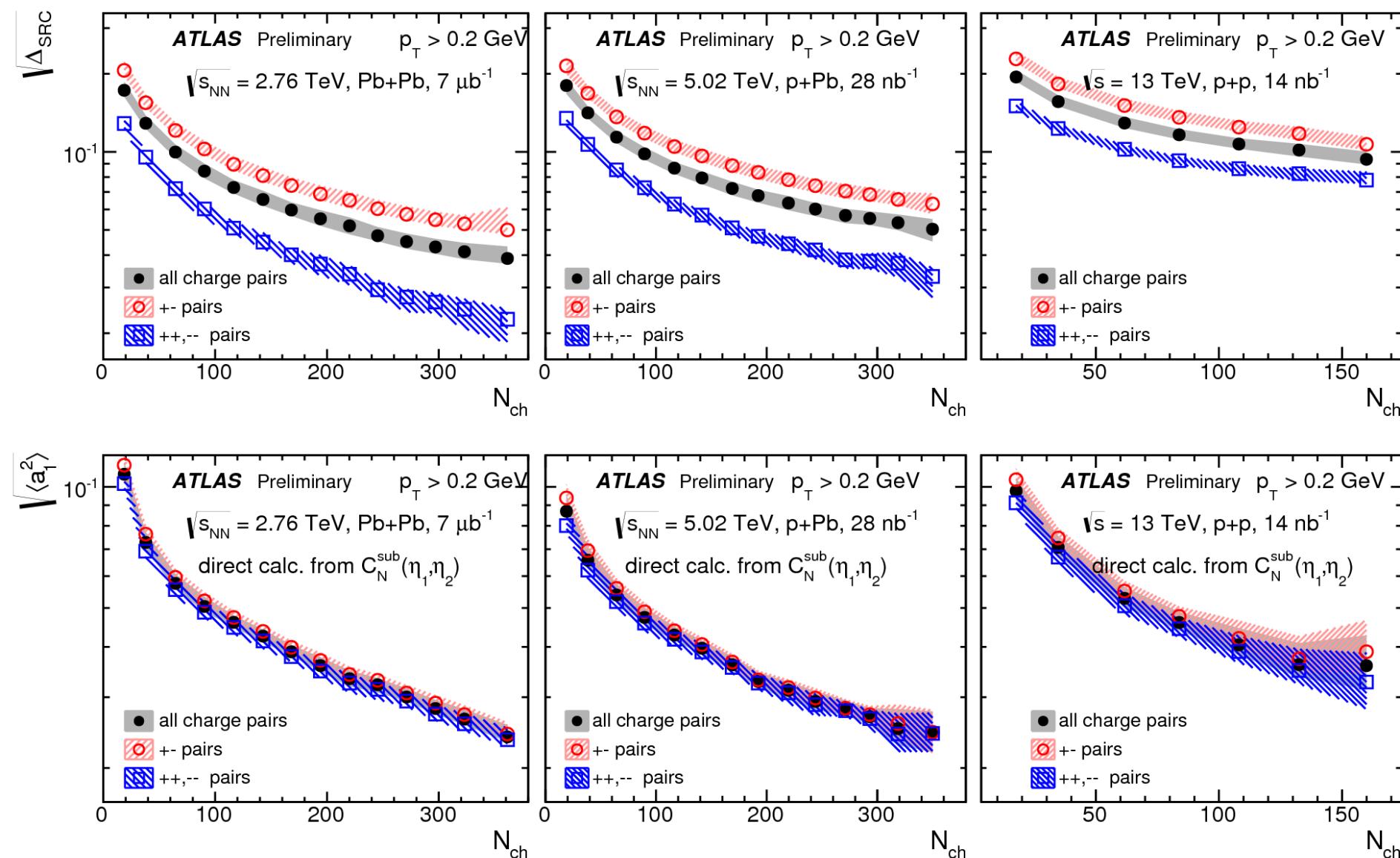
Scan of projections: $p+\text{Pb}$



Scan of projections: pp



Charge dependence



Systematic uncertainty: correlation function

Collision system	Pb+Pb	$p+Pb$	pp
Event-mixing [%]	0.4–0.7	0.4–2.2	0.2–1.4
Run-by-run stability [%]	0.3–0.5	0.3–1.5	0.2–1.5
$z_{\text{ vtx }}$ variation [%]	0.3–0.6	0.3–1.5	0.2–1.6
Track selection & efficiency [%]	0.6–1.2	0.2–1.3	0.3–0.7
MC consistency [%]	0.2–1.6	0.5–2.5	0.7–3.3
Charge dependence [%]	1.0–1.8	0.8–3.8	1.5–2.5
SRC subtraction [%]	1.1–2.1	1.0–5.9	1.2–5.0
Total [%]	1.7–3.2	2.1–7.6	2.5–6.9

Systematic uncertainty: α_1

	Quadratic fit to the $C_N^{\text{sub}}(\eta_-) _{\eta_+ < 0.1}$			Quadratic fit to the $C_N^{\text{sub}}(\eta_+) _{0.9 < \eta_- < 1.1}$		
Collision system	Pb+Pb	$p+\text{Pb}$	pp	Pb+Pb	$p+\text{Pb}$	pp
Event-mixing [%]	0.5–2.2	0.3–1.8	0.2–2.8	0.2–1.7	0.2–1.6	0.2–2.7
Run-by-run stability [%]	0.2–1.3	0.2–1.7	0.2–2.8	0.2–1.5	0.2–1.1	0.2–1.6
z_{vtx} variation [%]	0.3–1.9	0.1–2.2	0.1–1.6	0.1–1.8	0.2–0.7	0.1–0.9
Track selec.& efficiency[%]	0.4–2.1	0.3–0.9	0.8–2.2	0.8–3.7	1.0	0.9–1.2
MC consistency [%]	0.2–3.6	0.4–3.9	0.2–10.0	0.2–4.3	0.2–2.4	0.2–4.7
Charge dependence [%]	0.9–4.2	1.0–10.2	2.8–4.6	0.4–3.8	0.6–3.1	1.2–6.2
SRC subtraction [%]	0.9–2.5	1.2–6.3	1.3–4.8	1.4–2.5	1.2–3.7	1.2–4.6
Total [%]	2.1–5.2	2.7–10.3	10–12	2.4–5.5	2.5–6.8	3.5–11.2
	Linear fit to the $r_N^{\text{sub}}(\eta) _{2.2 < \eta_{\text{ref}} < 2.4}$			Global Legendre expansion of C_N^{sub}		
Collision system	Pb+Pb	$p+\text{Pb}$	pp	Pb+Pb	$p+\text{Pb}$	pp
Event-mixing [%]	0.3–2.3	0.3–1.4	0.1–1.5	0.2–1.8	0.1–1.7	0.1–0.9
Run-by-run stability [%]	0.1–1.2	0.1–1.7	0.2–2.8	0.2–0.7	0.1–1.3	0.1–2.1
z_{vtx} variation [%]	0.2–1.2	0.2–2.1	0.2–2.6	0.1–1.3	0.2–2.5	0.2–1.7
Track selec.& efficiency[%]	0.4–1.3	0.6–0.9	0.7–1.7	0.3–0.9	0.4–0.7	0.8–2.4
MC consistency [%]	0.2–2.6	0.2–3.7	0.8–7.6	0.2–2.5	0.4–3.2	0.1–6.7
Charge dependence [%]	0.4–4.9	0.1–8.8	1.6–5.3	2.3–5.3	1.0–12.7	3.4–8.1
SRC subtraction [%]	1.4–3.2	2.2–3.4	1.7–5.0	1.7–4.3	2.0–8.9	2.7–9.6
Total [%]	2.4–6.2	2.9–8.9	4.4–9.8	3.4–6.4	4.1–12.9	6.2–12.5