

Evidences for collectivity in small systems

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Physics Ph.D. Defense

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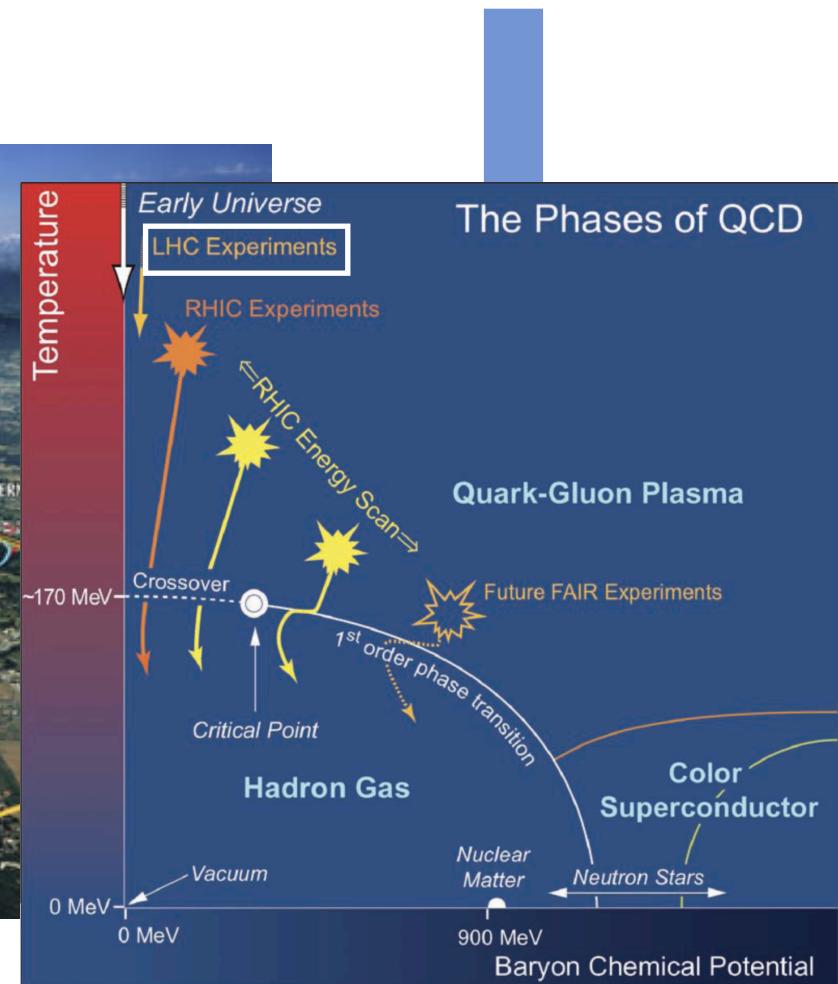
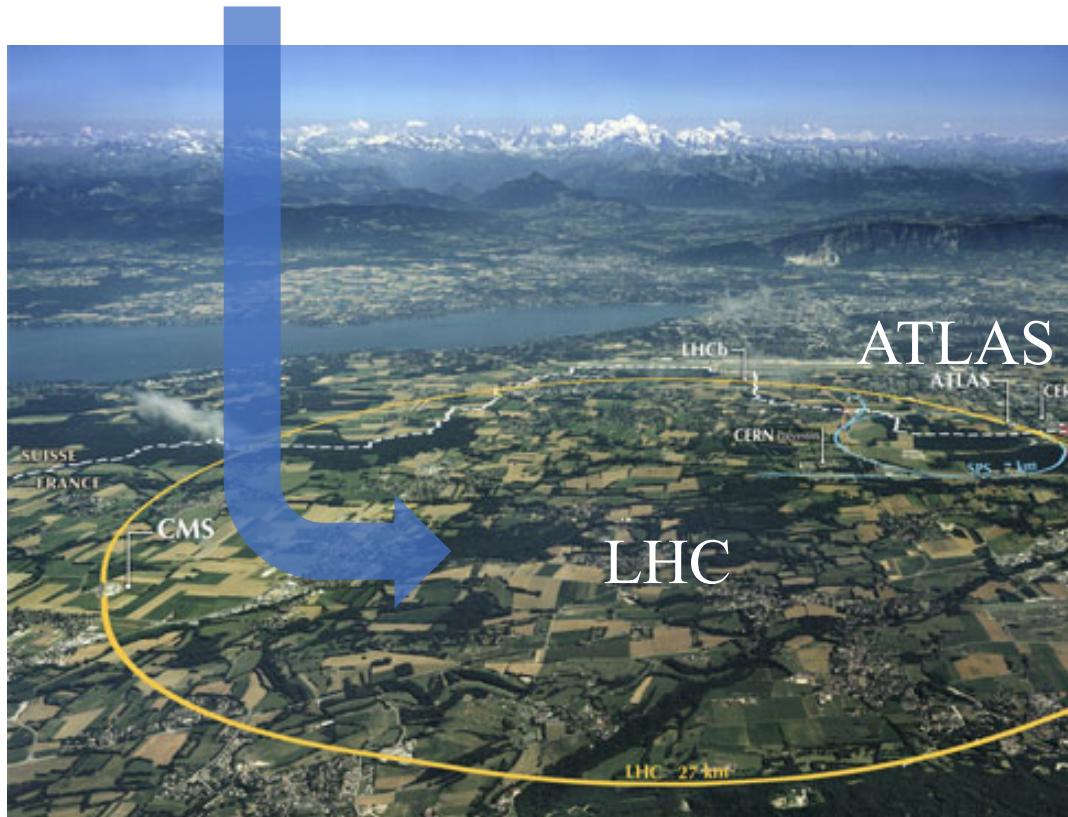
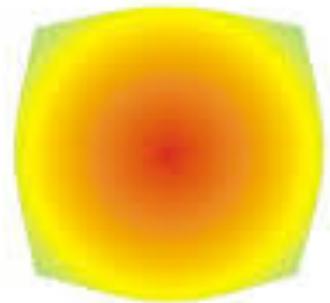


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University

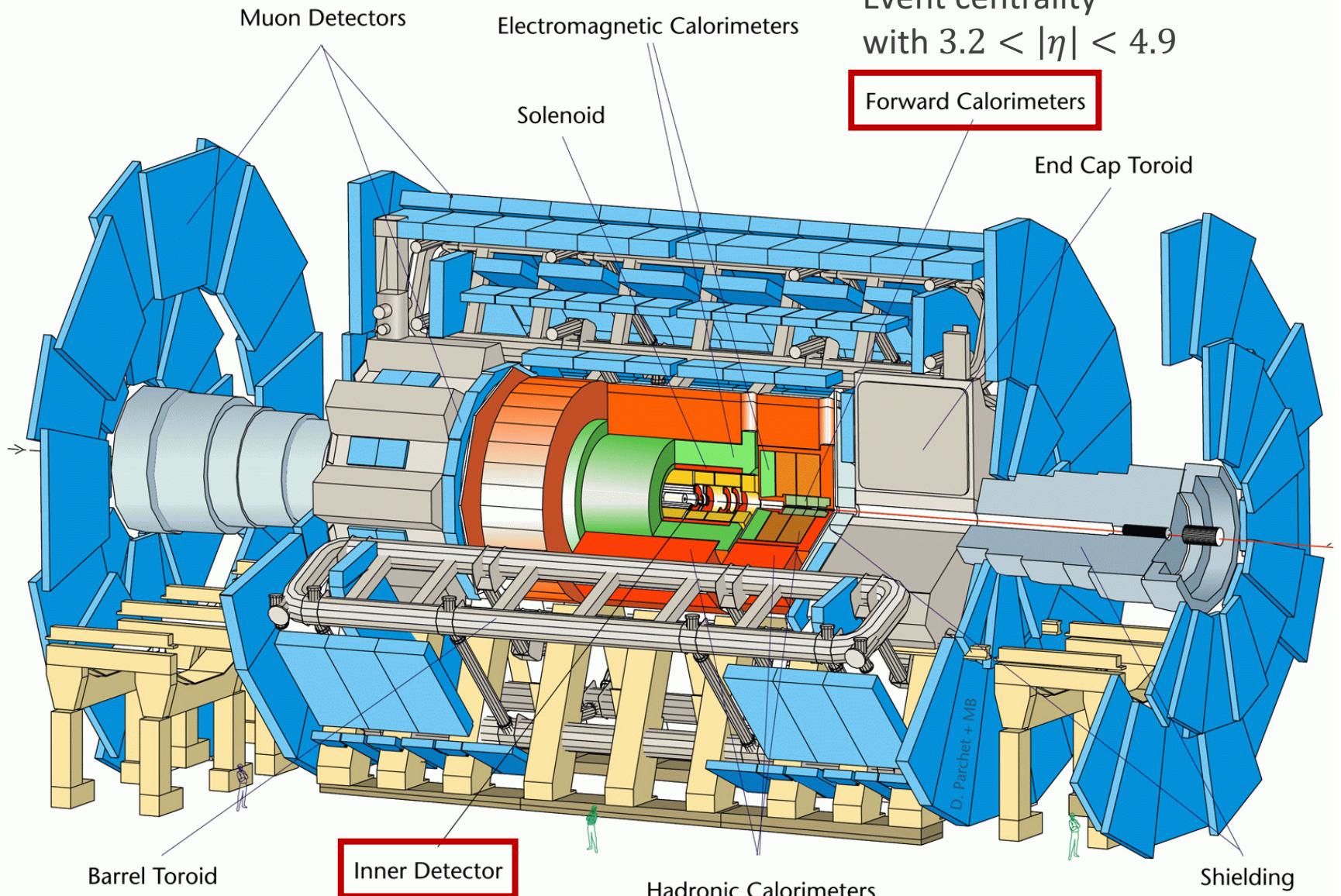
QGP and heavy ion collisions

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QGP

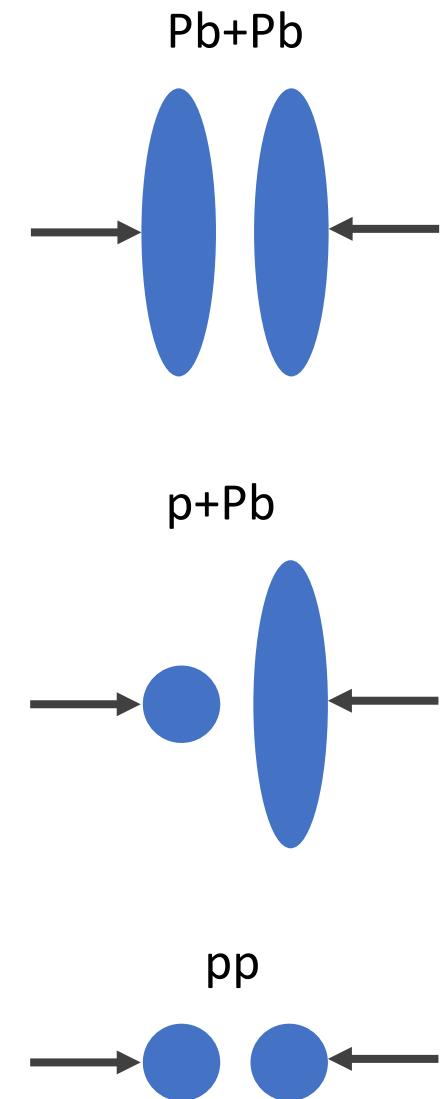
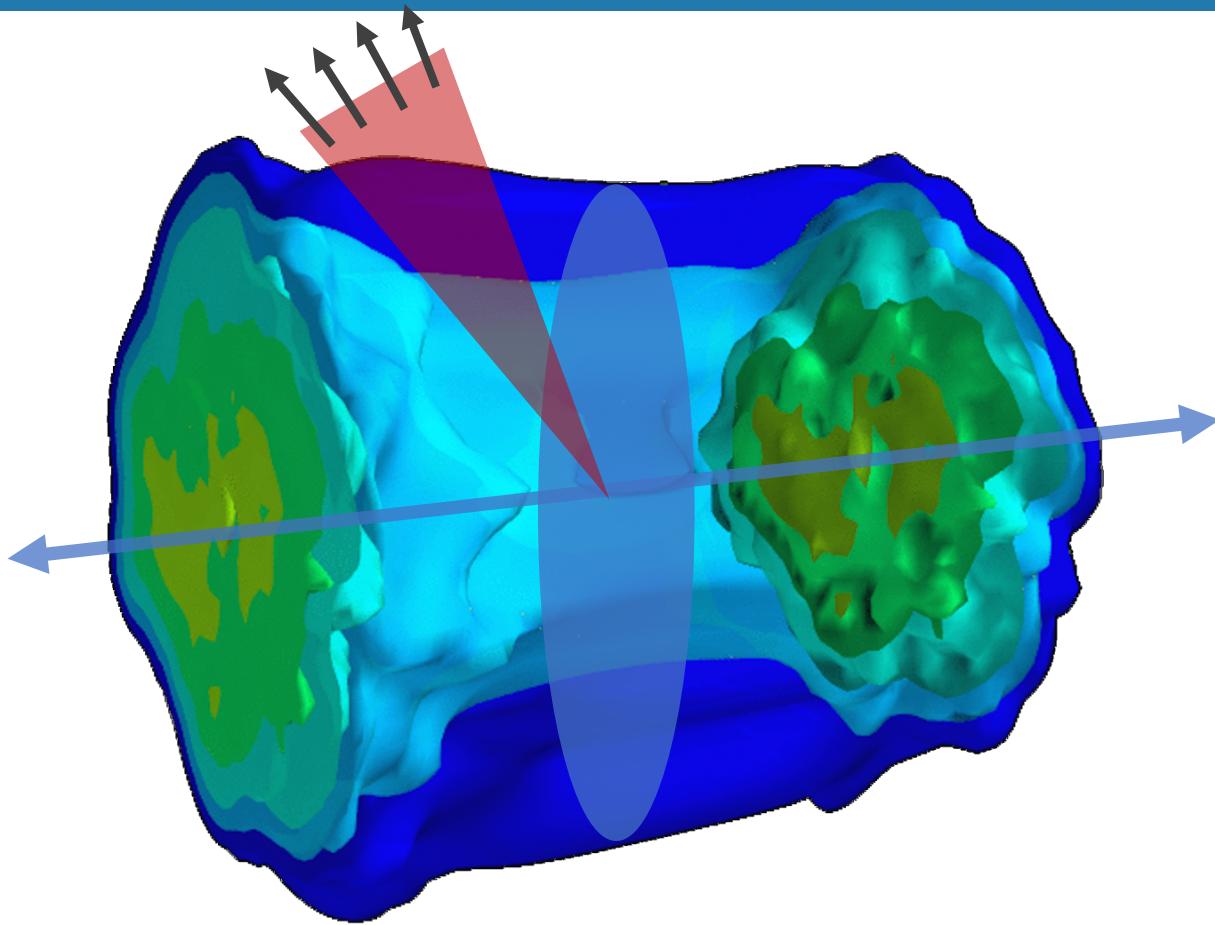


Collectivity



Collectivity

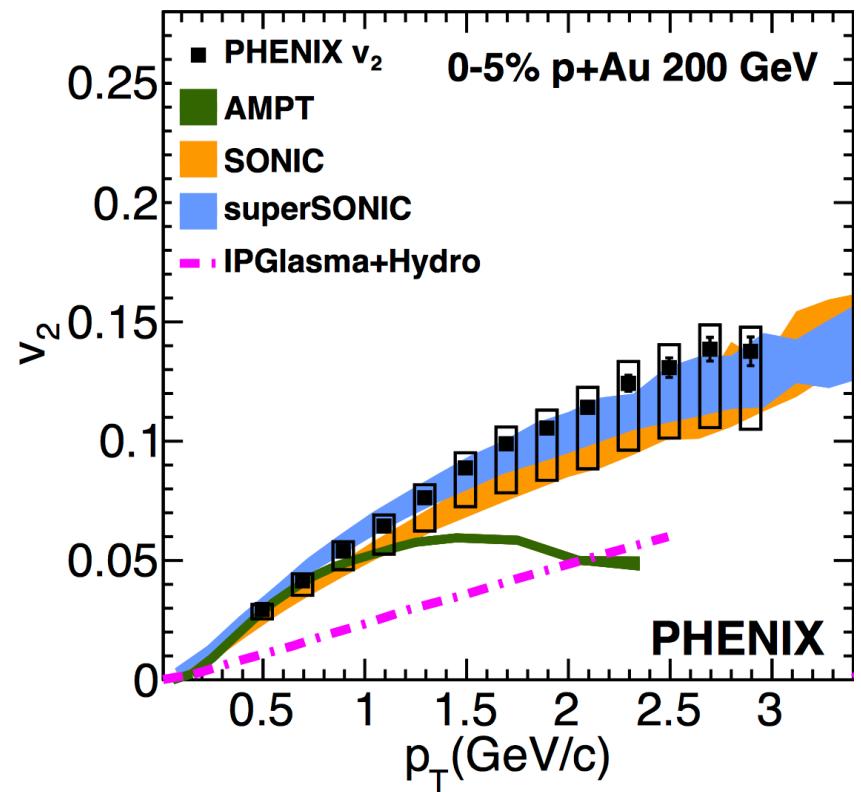
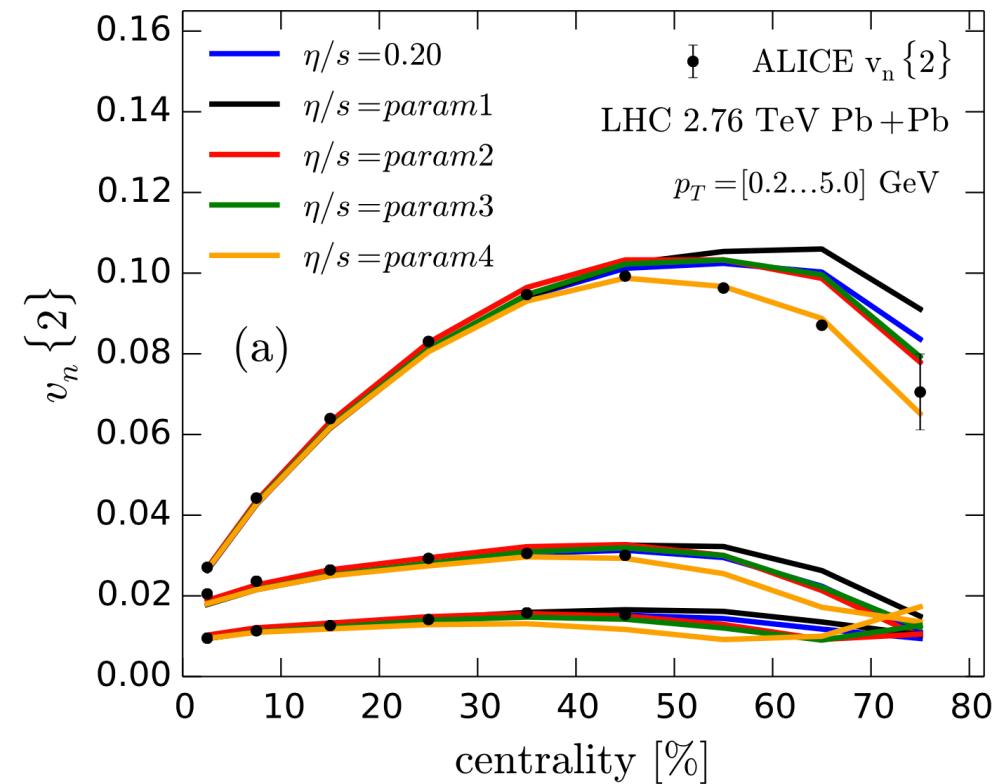
4



- Collectivity: how system evolve as a whole
 - Longitudinal correlation
 - Azimuthal correlation
- Short-range correlations are major background

Why small systems?

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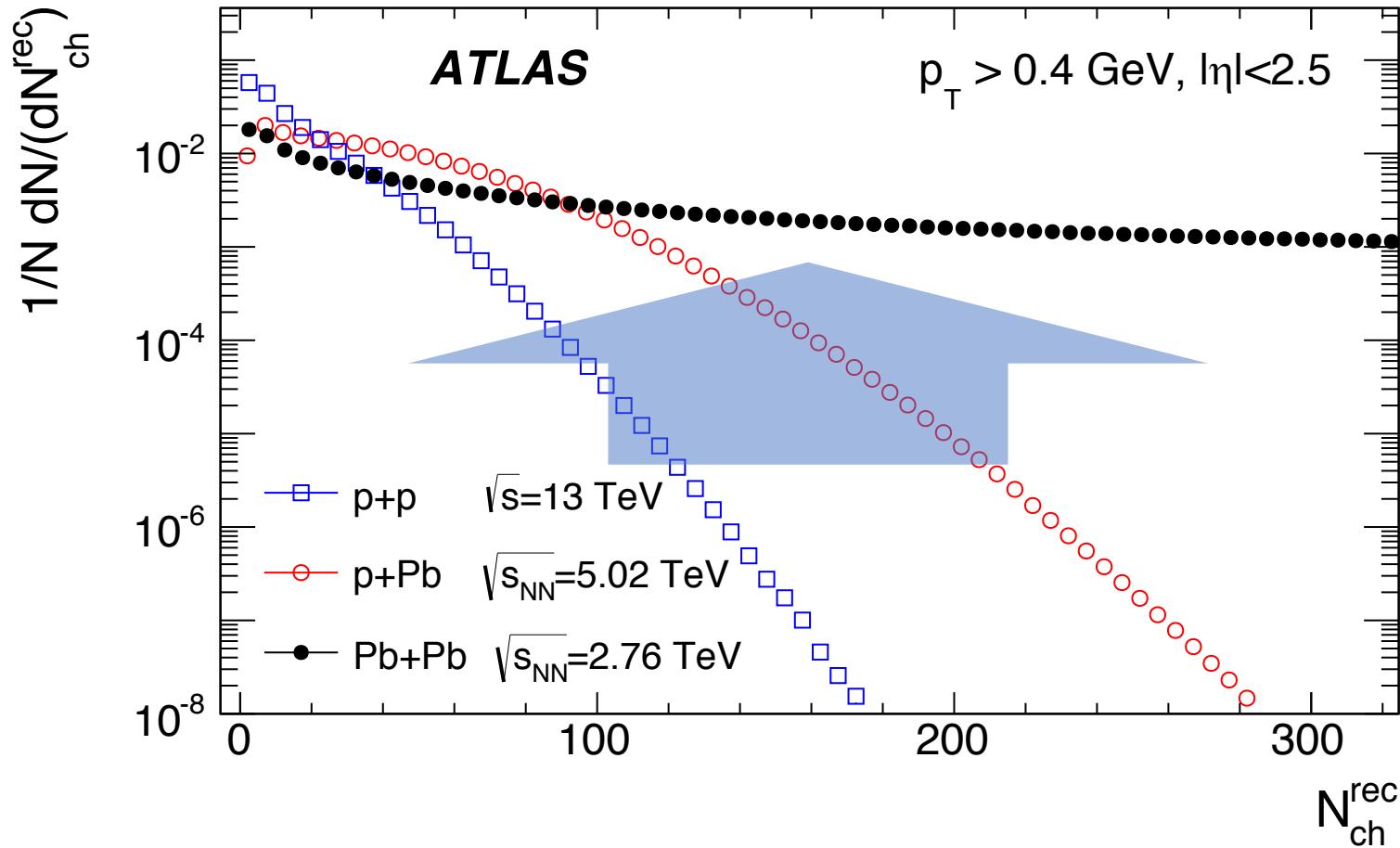


Hydro successful in A+A

Challenge hydro in p+A / pp?

Origins of collectivity?

- Real-time data collection
- Longitudinal correlation
- Azimuthal correlation

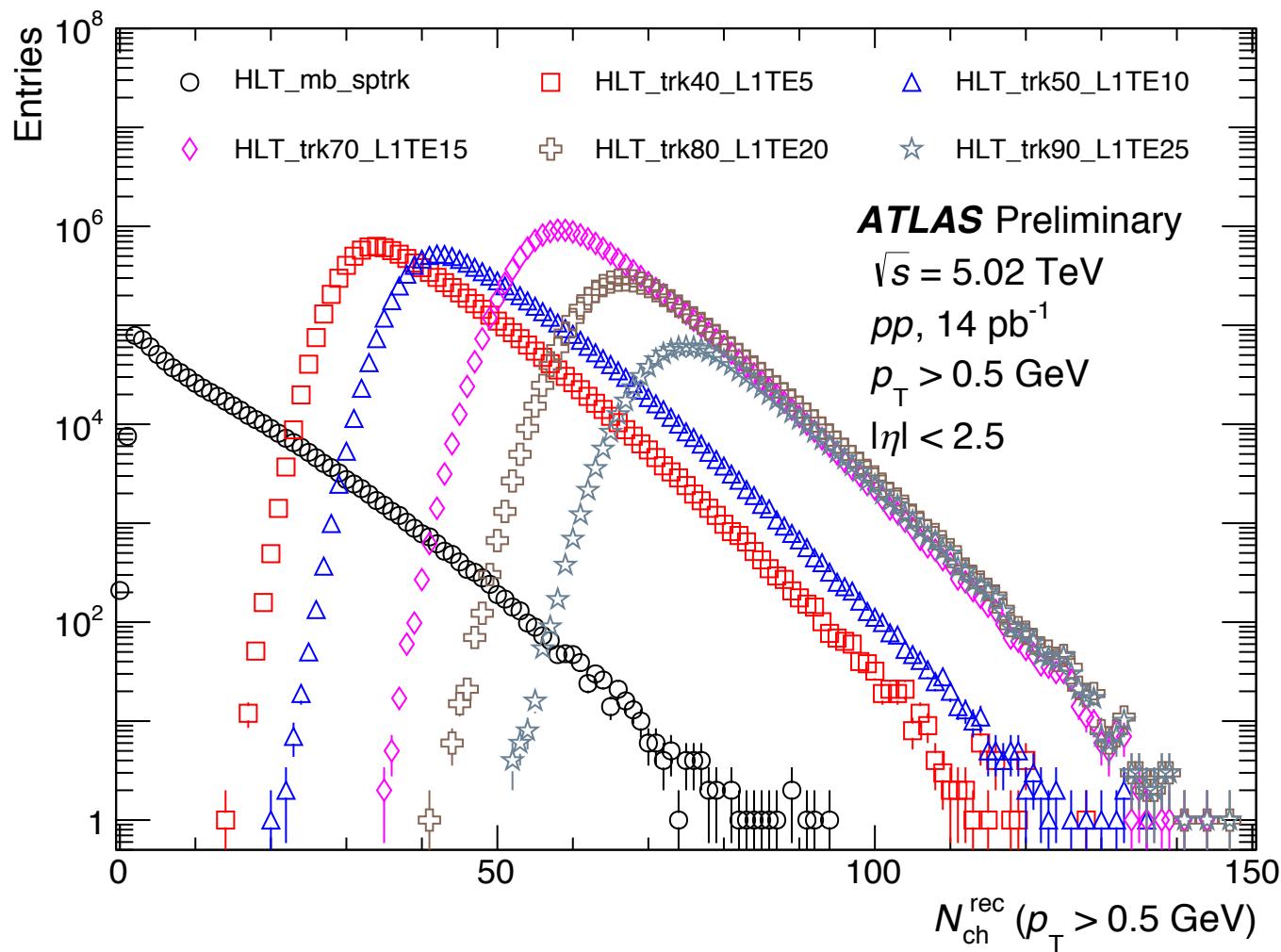


LHC event rate
40 MHz

Triggers

Recording cap
10 kHz

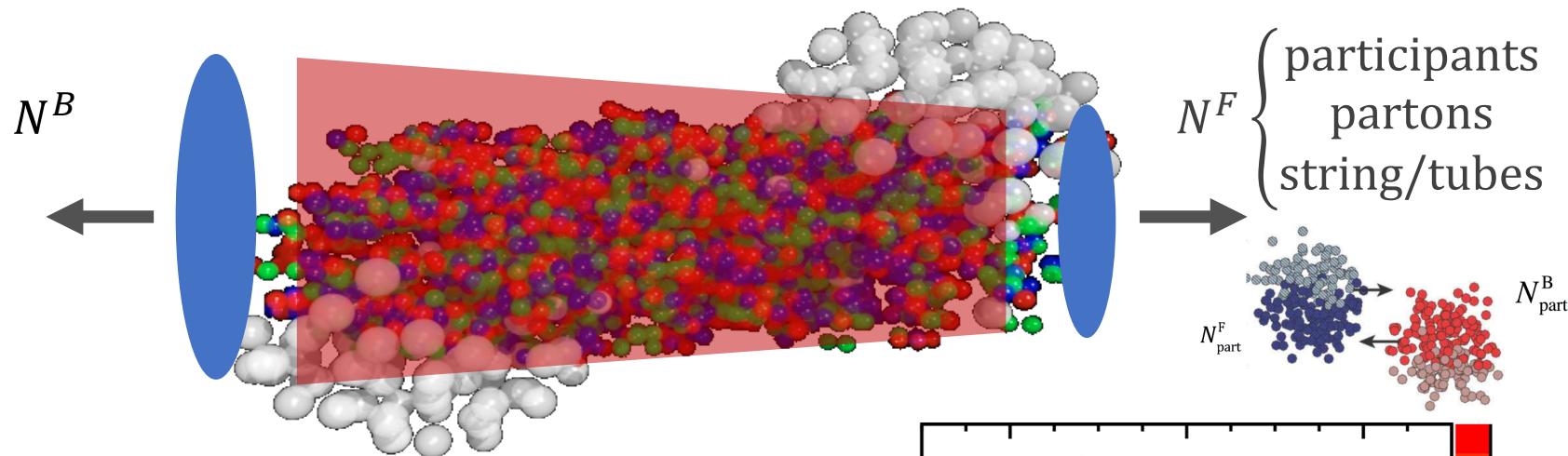
Trigger performance



Multiple HMT triggers applied to pp and $p+\text{Pb}$ data taking

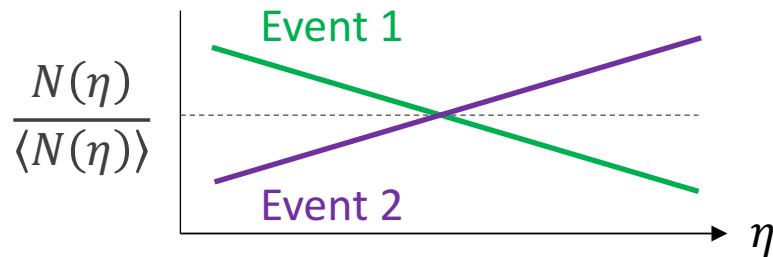
Long-range longitudinal correlation

Nature of sources seeding the long-range collective behaviors?

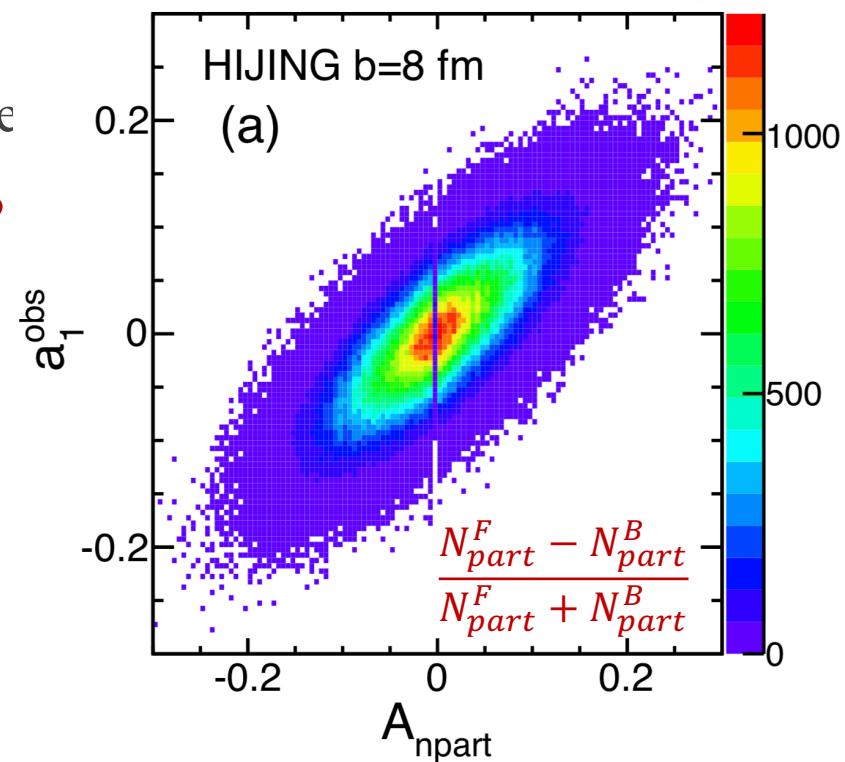


- $dN/d\eta$ shape reflects asymmetry in the number

Event-by-event multiplicity fluctuation?



$$\frac{N(\eta)}{\langle N(\eta) \rangle} = 1 + a_1 \eta$$

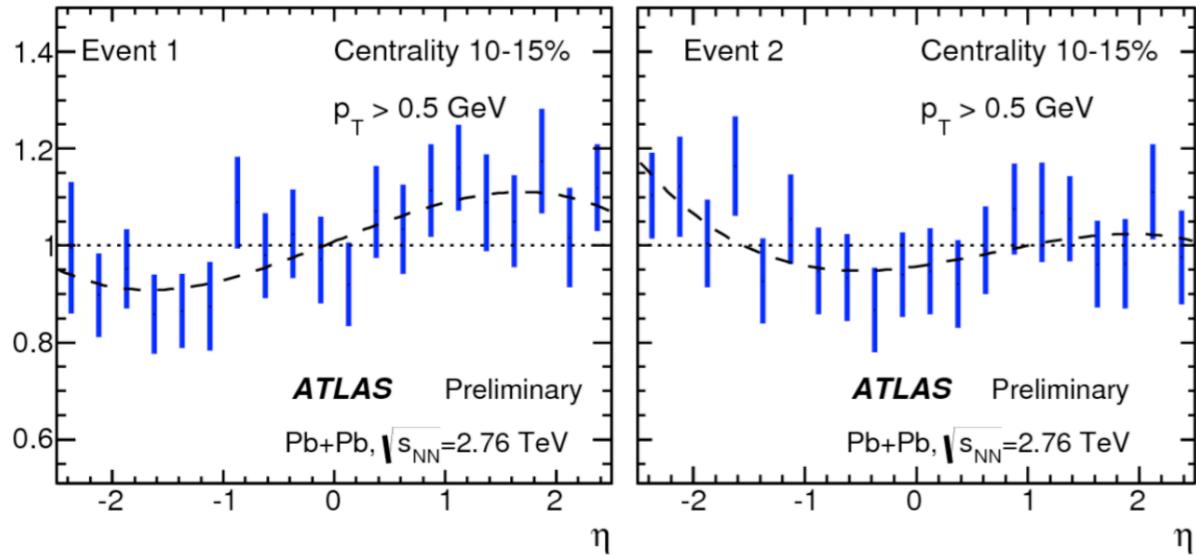


New observable

- Single particle observable

$$R_s(\eta) \equiv \frac{N(\eta)}{\langle N(\eta) \rangle}$$

- Cannot measure single particle in data!



- Two particles observable (correlation function) [Derek, Phys. Rev. C 87, 024906 \(2013\)](#)

$$C(\eta_1, \eta_2) = \frac{\langle N(\eta_1)N(\eta_2) \rangle}{\langle N(\eta_1) \rangle \langle N(\eta_2) \rangle} = \langle R_s(\eta_1)R_s(\eta_2) \rangle$$

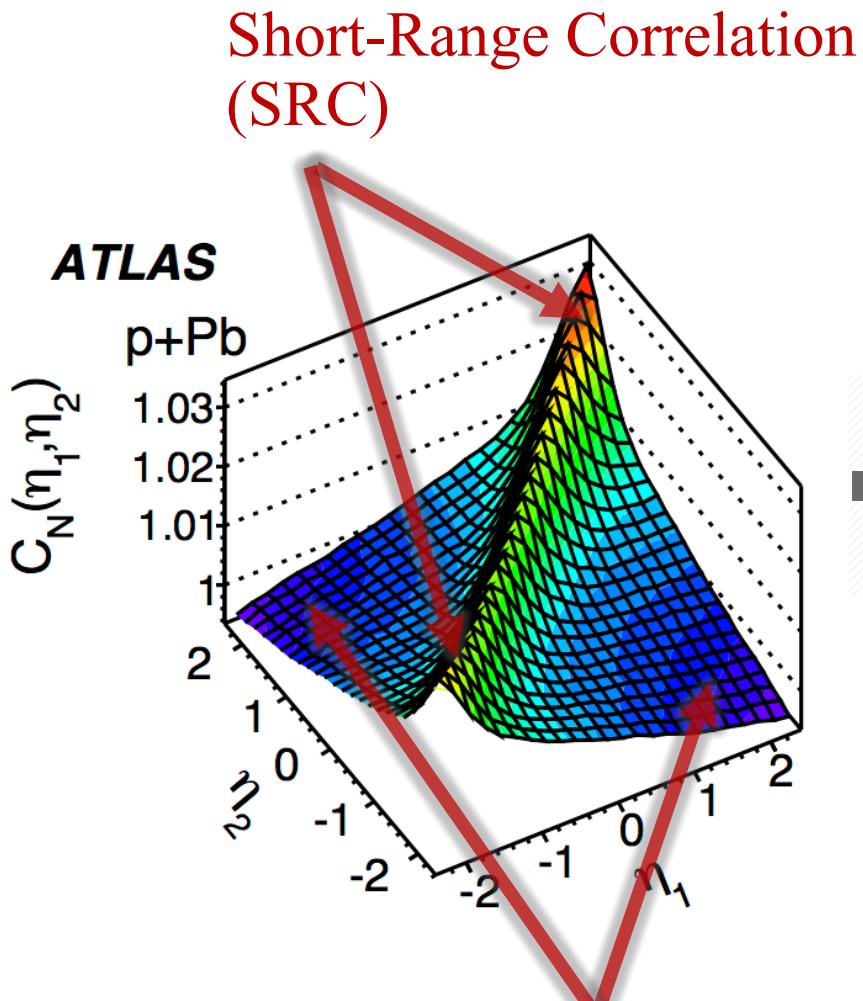
Two-particle correlation is related to single-particle distribution.

- Advantage of correlation function

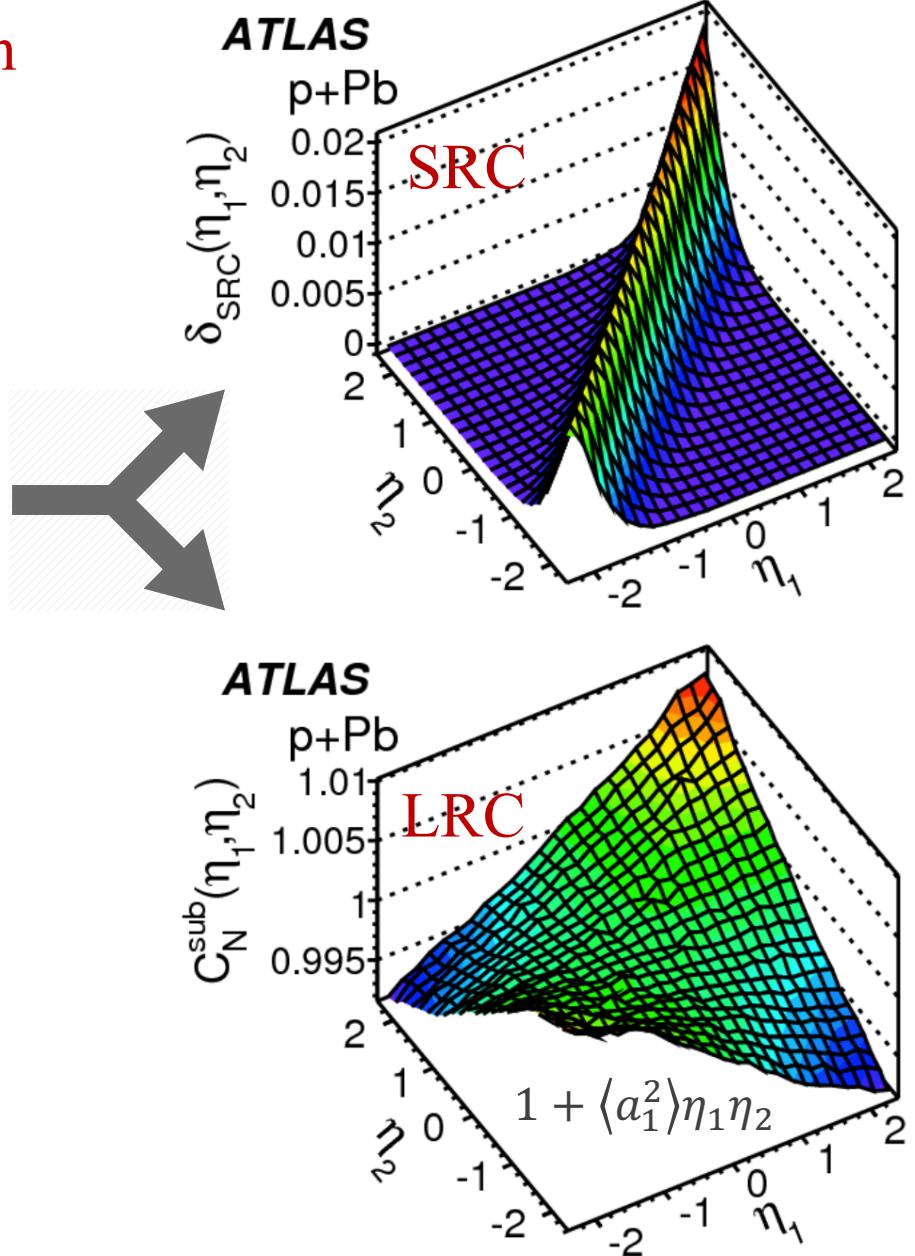
- Disentangles dynamical fluctuation from statistical fluctuation.
- Detector effects automatically removed;

Long-range and short-range correlations

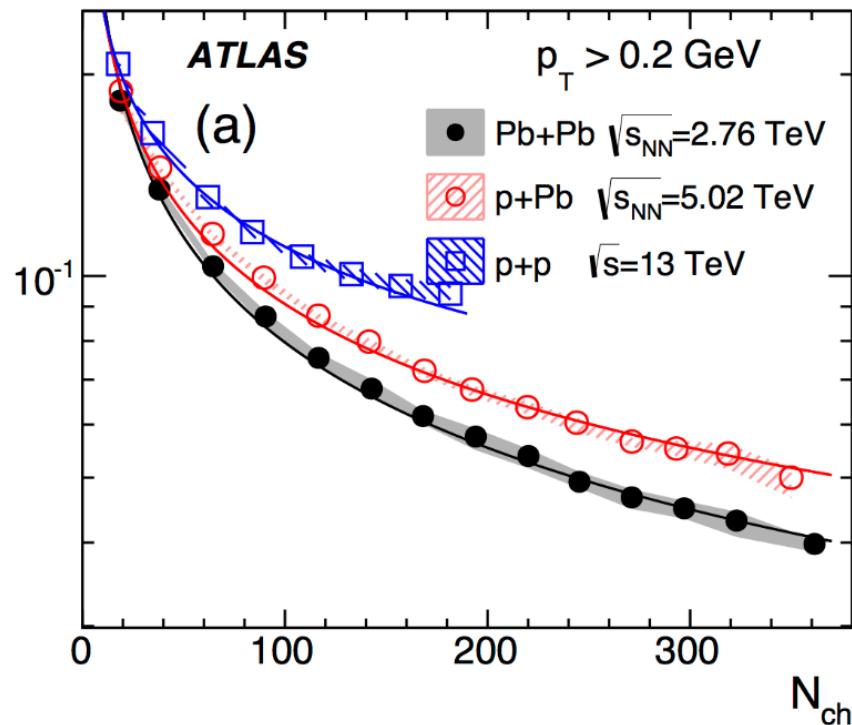
11



Long-Range Correlation (LRC)



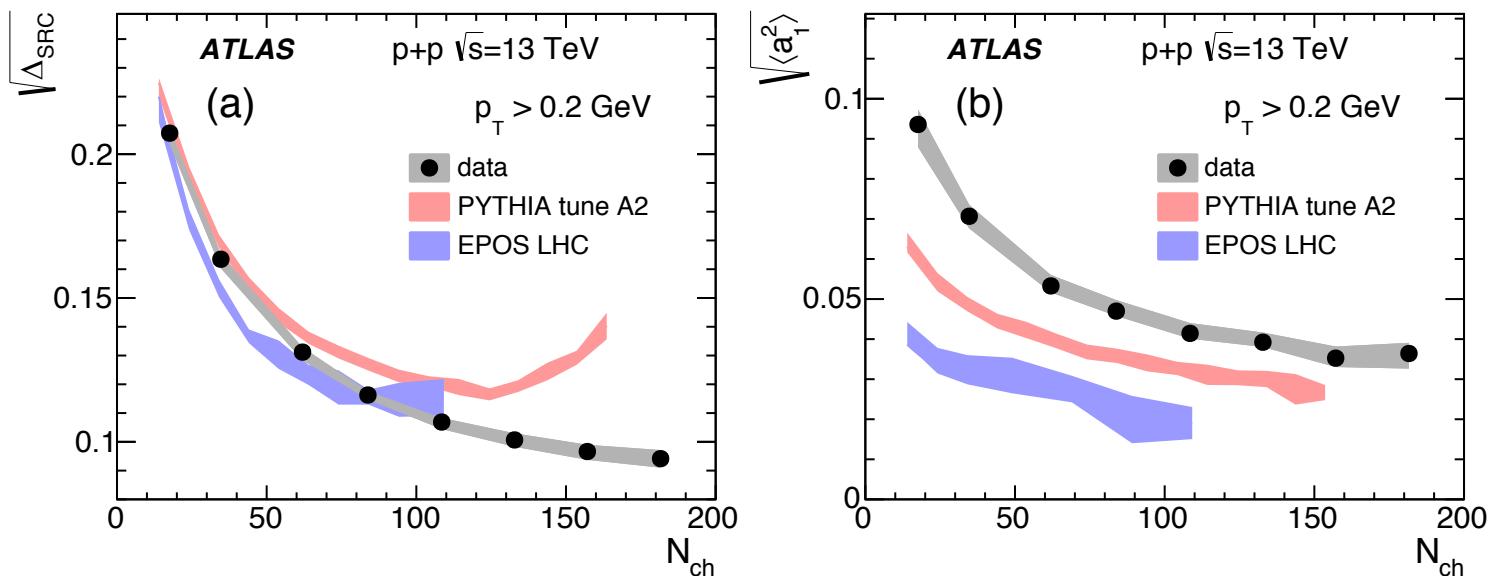
SRC



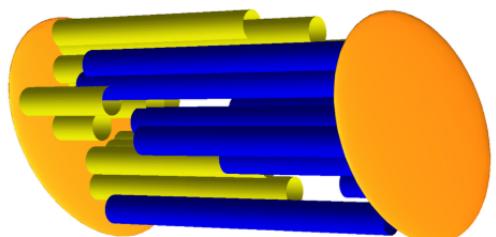
- SRC increases towards peripheral;
- SRC is stronger in small systems;

How will these new results help?

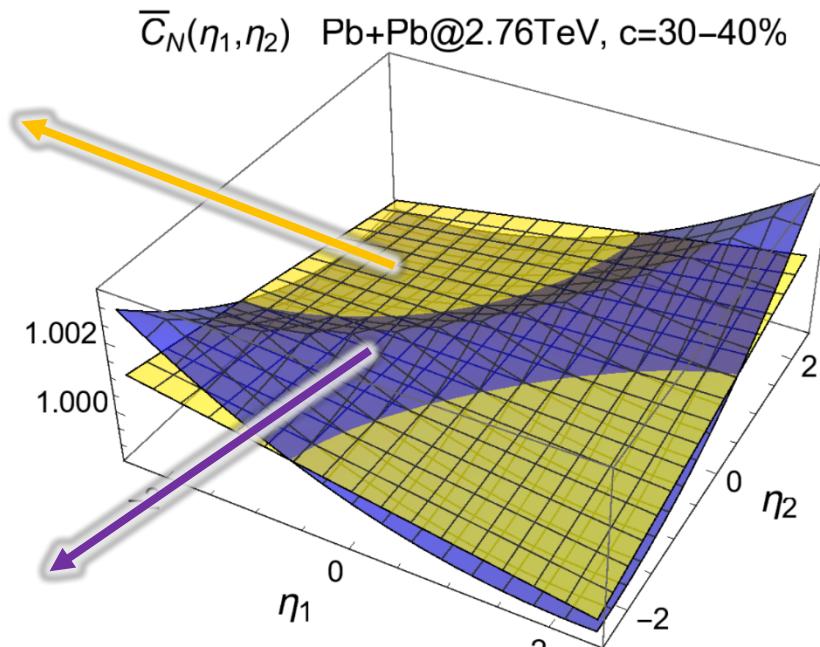
Model and data comparison



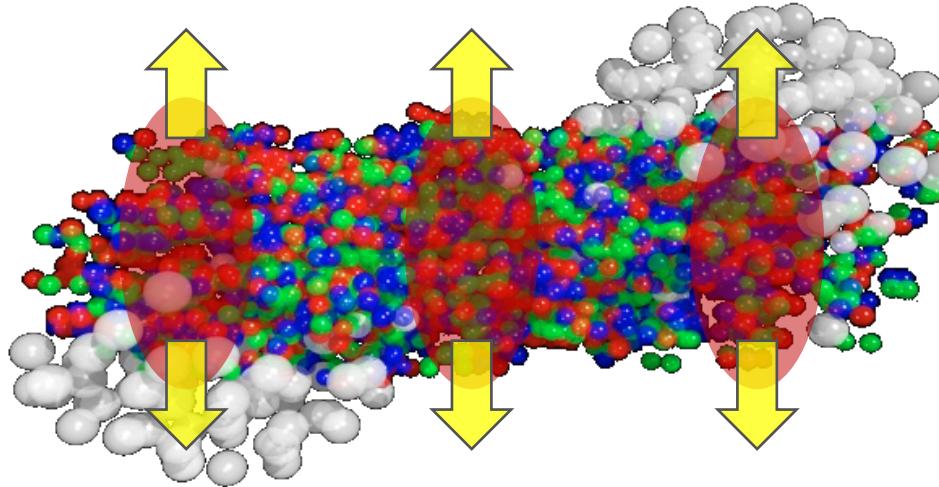
Without length fluctuation



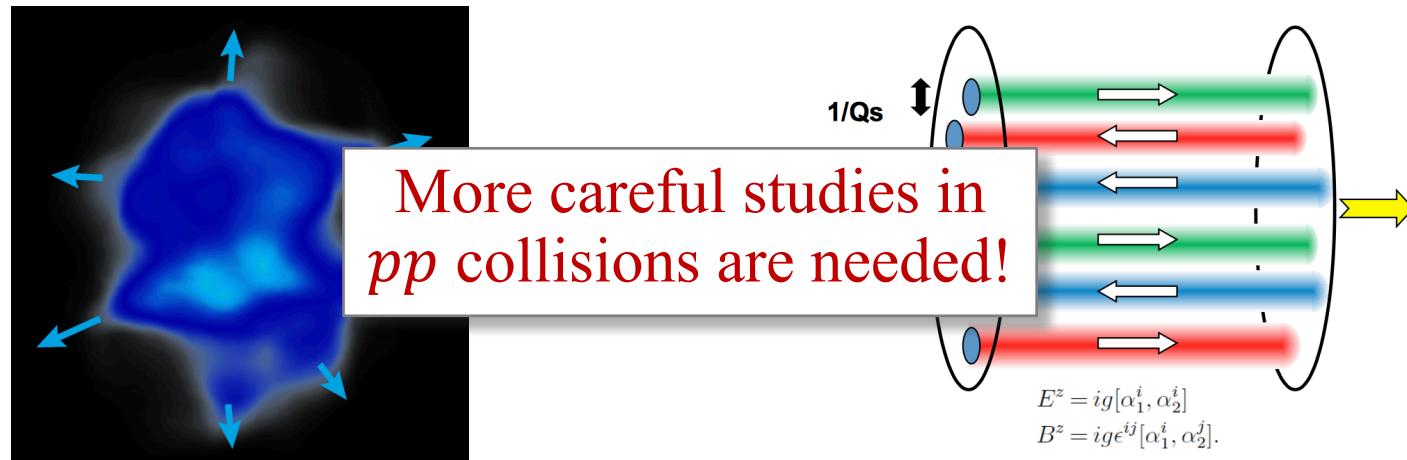
With length fluctuation



Nature of sources seeding the long-range collective behaviors?



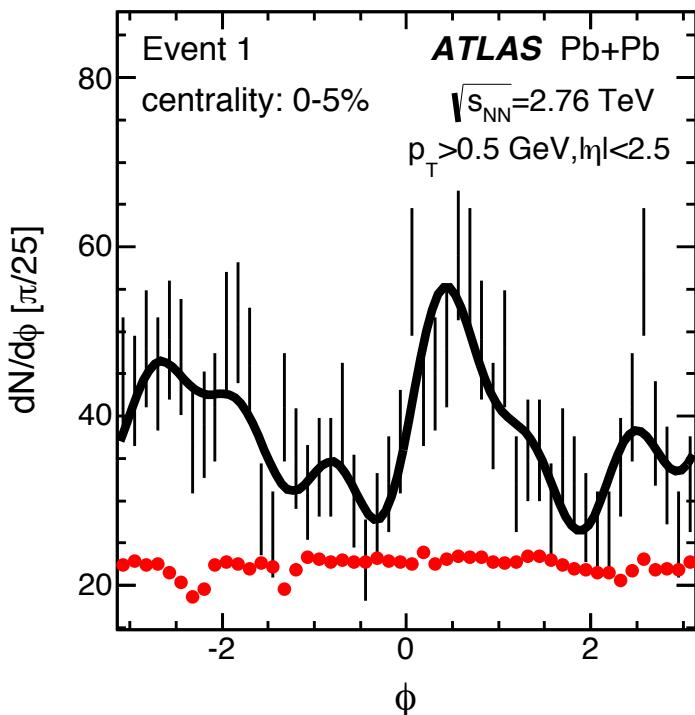
- Azimuthal correlation in A+A: collective hydrodynamic expansion of nuclear matter;



Final state correlations

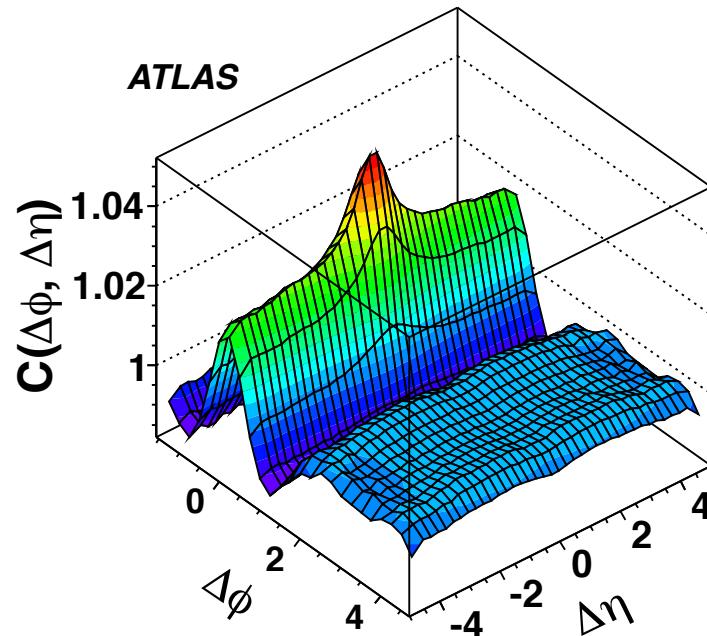
Initial state correlations

- Single particle method



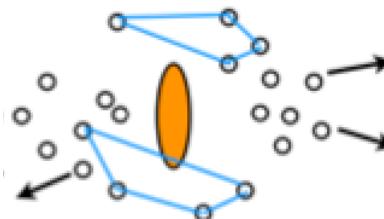
$$\frac{dN}{d\phi} \propto 1 + 2 \sum_{n=1} v_n \cos n(\phi - \Psi)$$

- Two-particle method



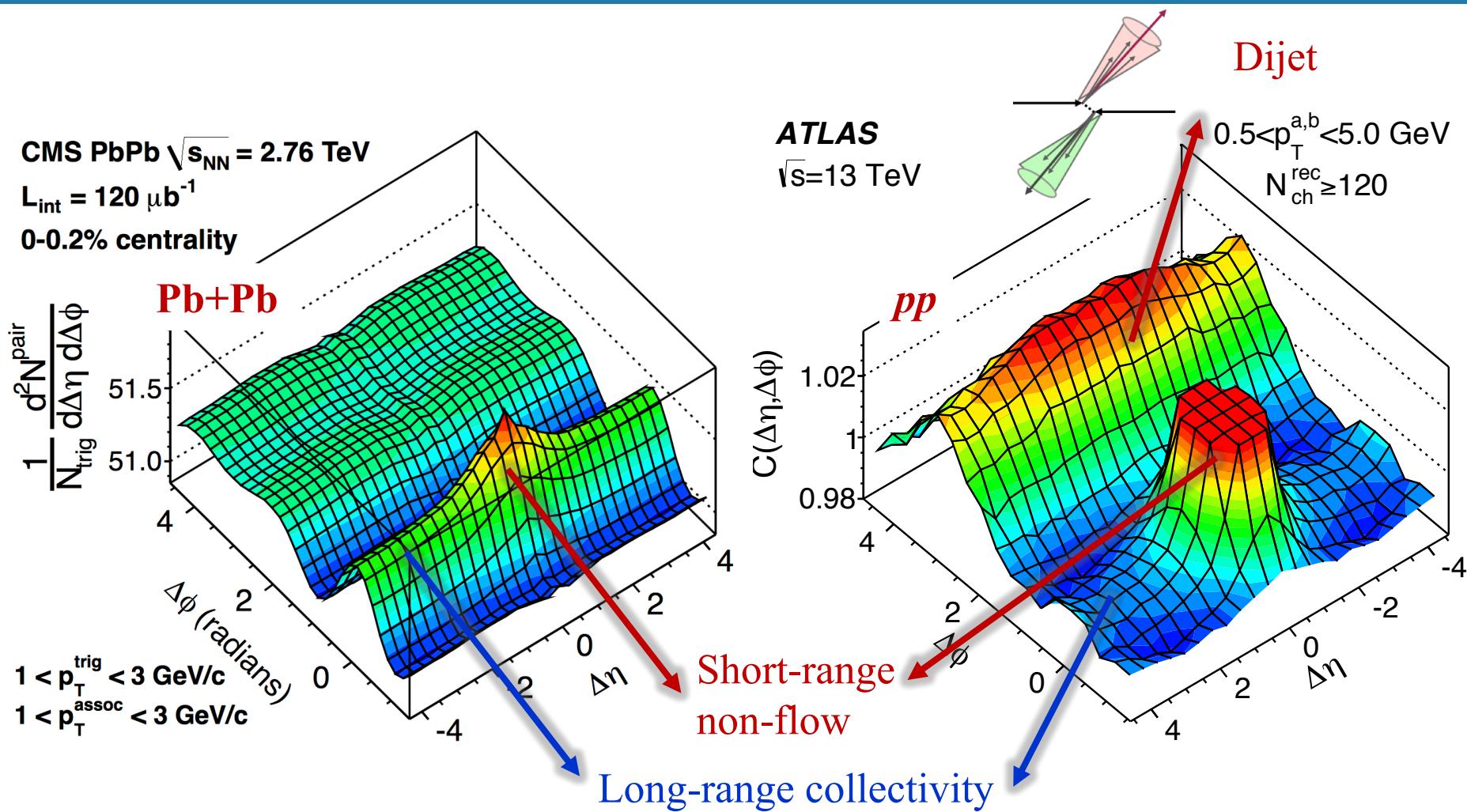
$$\frac{dN_{\text{pairs}}}{d\Delta\phi} \propto 1 + 2 \sum_{n=1} v_n^2 \cos n\Delta\phi$$

- Multi-particle (cumulant) method

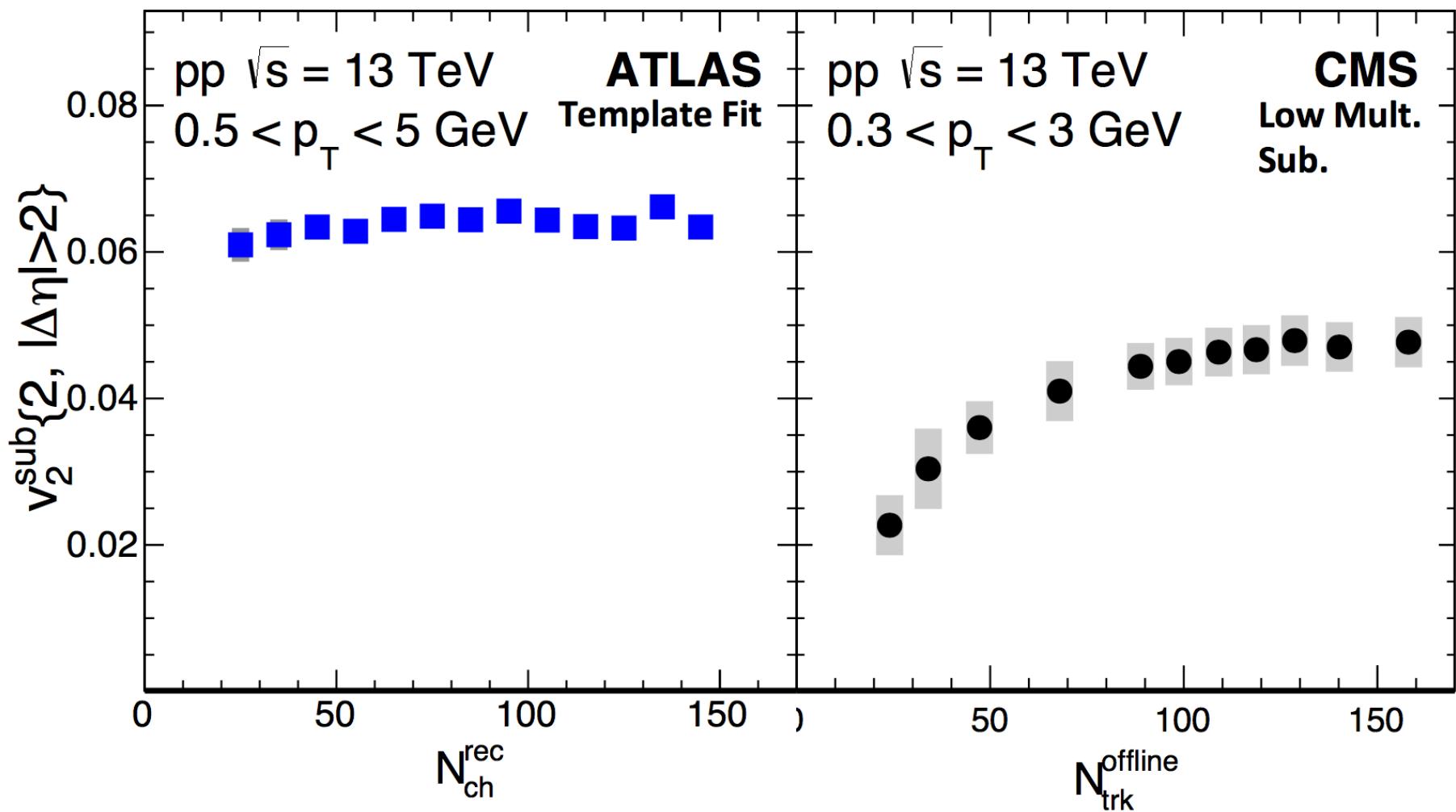


2-particle correlation

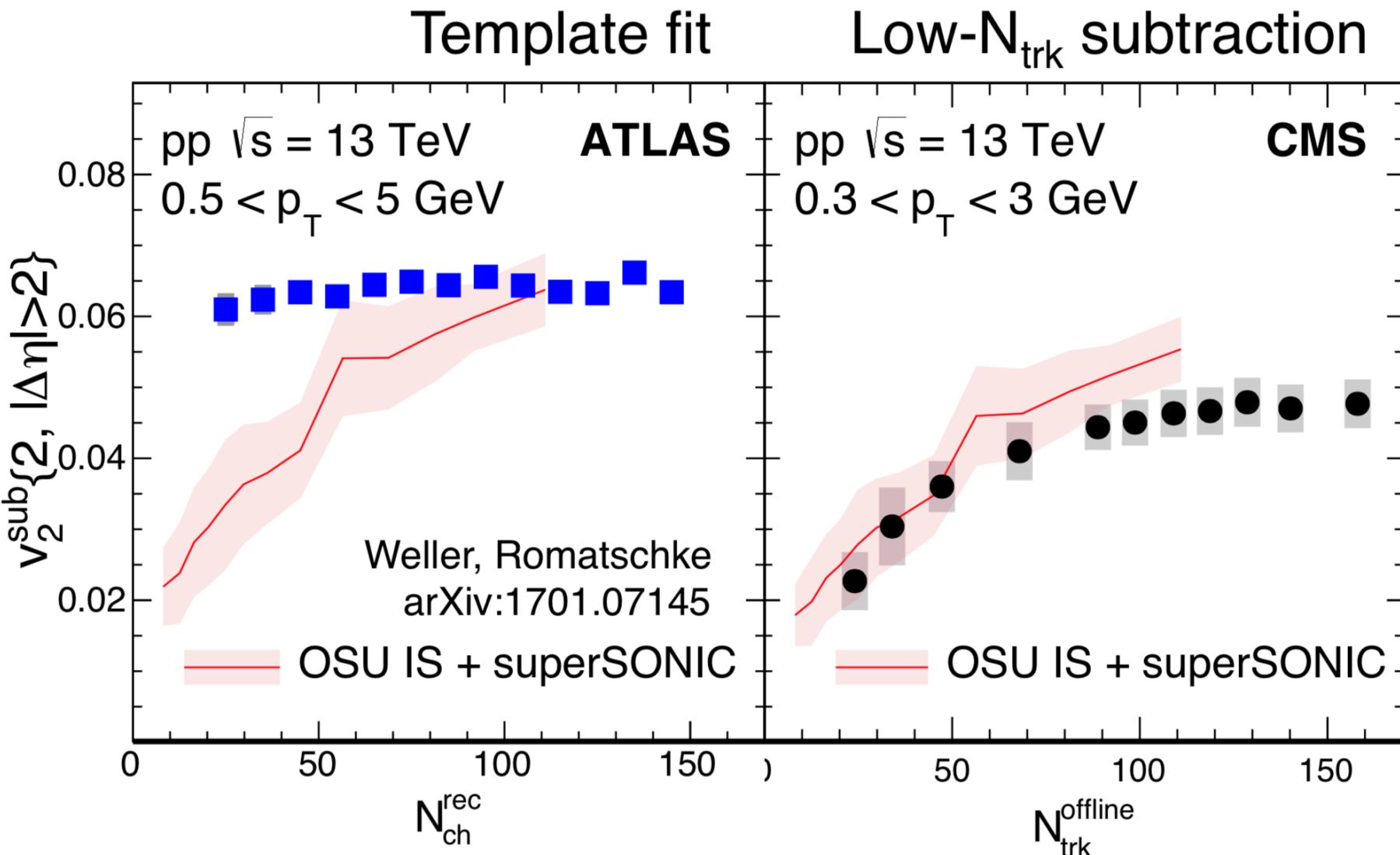
16



- Non-flow mainly from dijet;
- Need to remove dijet.



Different methods \Rightarrow Different results



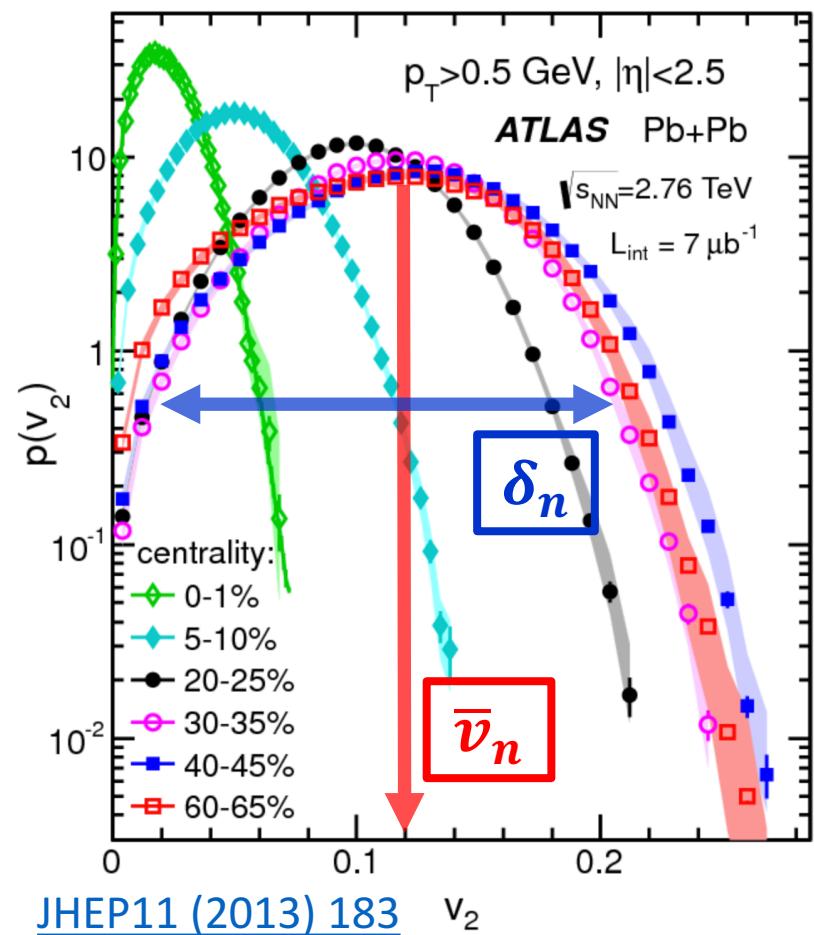
- If hydro, v_2 should go down toward low N_{ch} ;
- New observable needed.

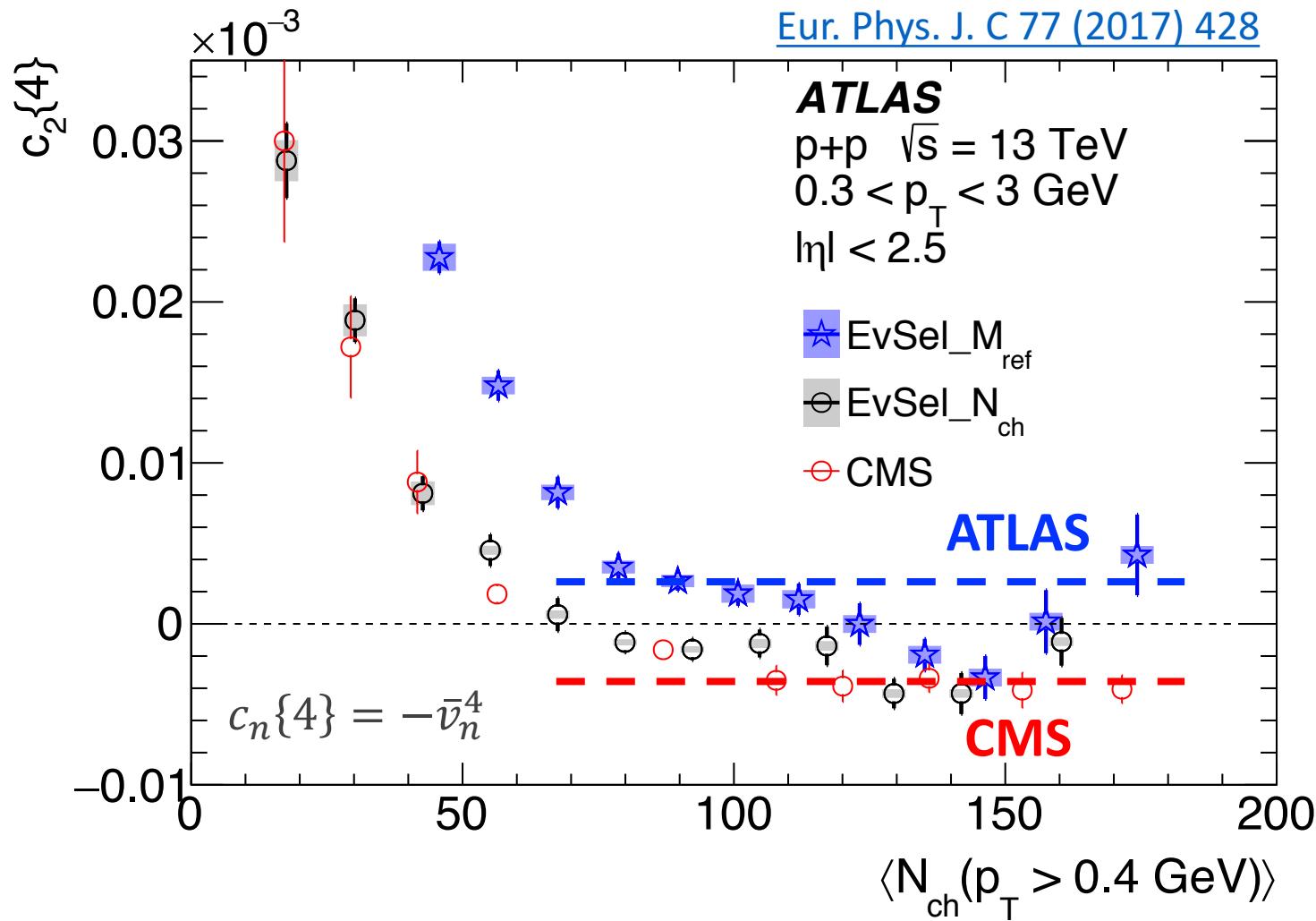
Cumulant method

- Four-particle correlation $\text{corr}_n\{4\} \equiv \langle e^{in(\phi_1+\phi_2-\phi_3-\phi_4)} \rangle$
 - Genuine 4-particle correlation
 - 2-particle non-flow
- Four-particle cumulant $c_n\{4\} \equiv \langle \text{corr}_n\{4\} \rangle - 2\langle \text{corr}_n\{2\} \rangle^2$

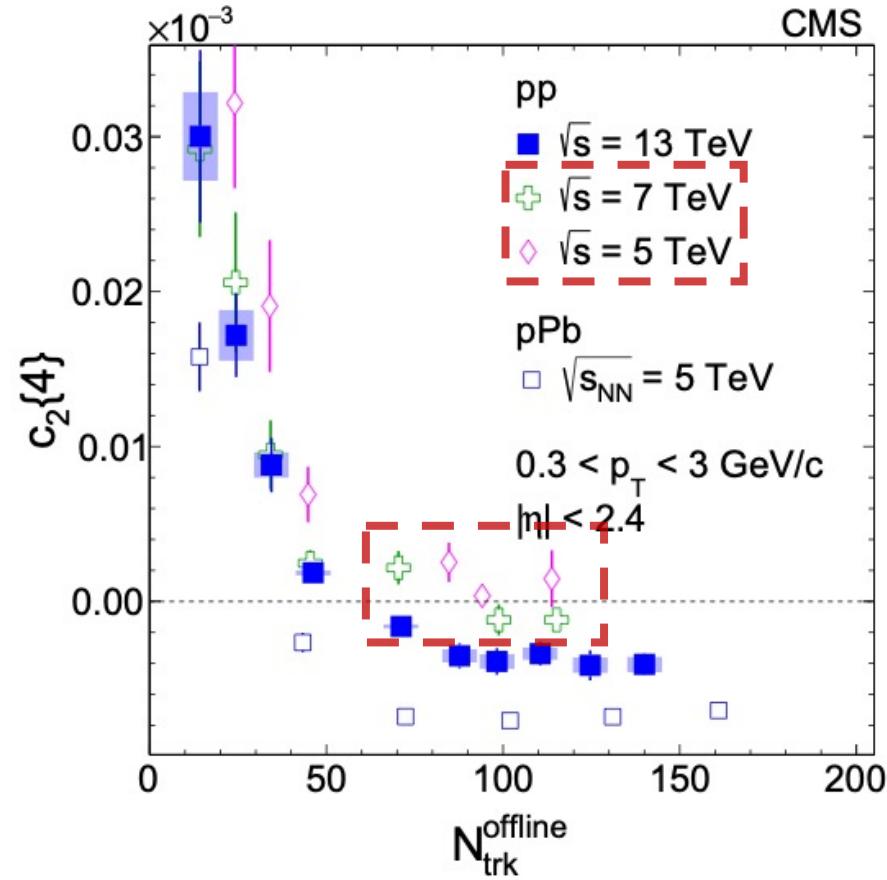
- Flow fluctuates event to event $p(v_n)$;
- $v_2\{2\}, c_2\{4\} \Rightarrow \bar{v}_n, \delta_n$
- Features of cumulant method
 - Suppress non-flow (< 4 particles);
 - If $p(v_n) \sim \text{Gauss}$, then $c_n\{4\} = -\bar{v}_n^4$

Cumulant proved successful in large systems, how about small systems?

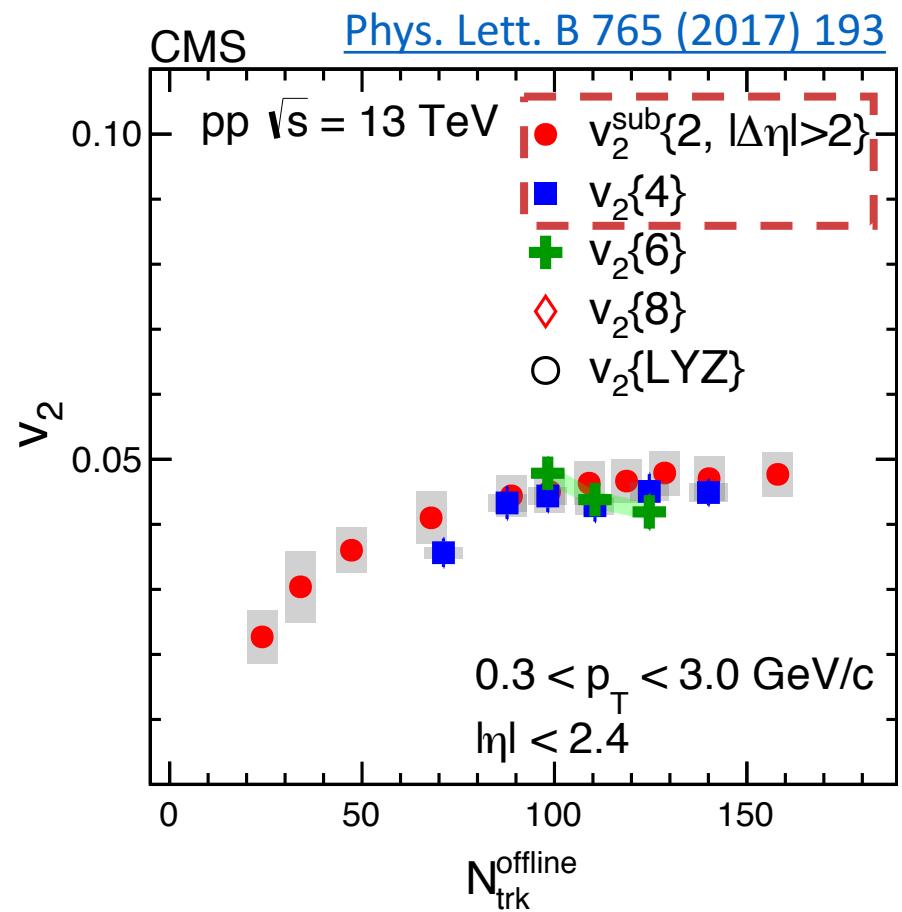




To be **collective**, or not to be **collective**?



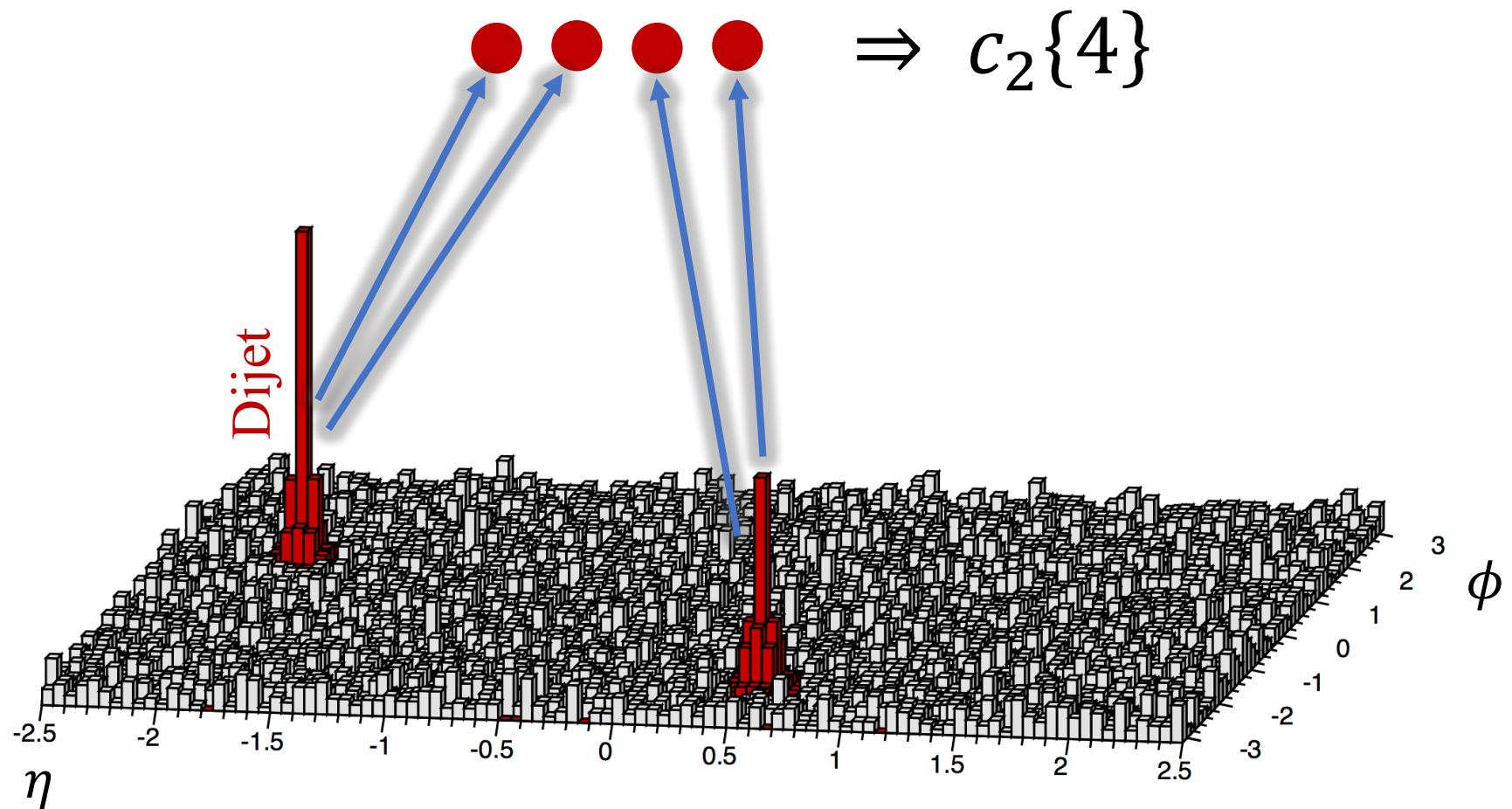
- No hint of collectivity at lower energy?



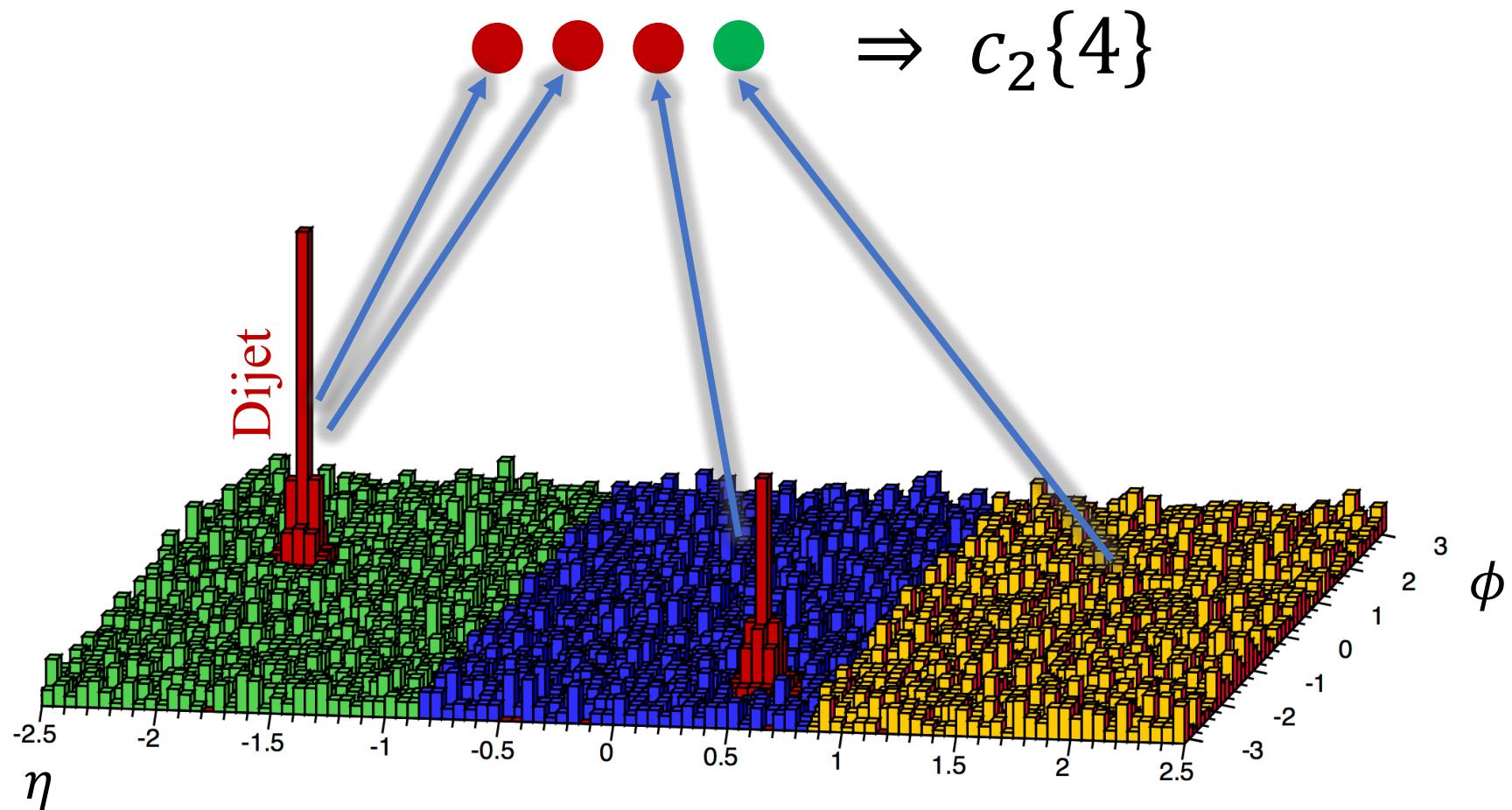
- $v_2\{2\} = v_2\{4\} + \text{flow fluc}$
- Flow fluc ≈ 0 ?

Puzzles needs to be solved before testing models with data.

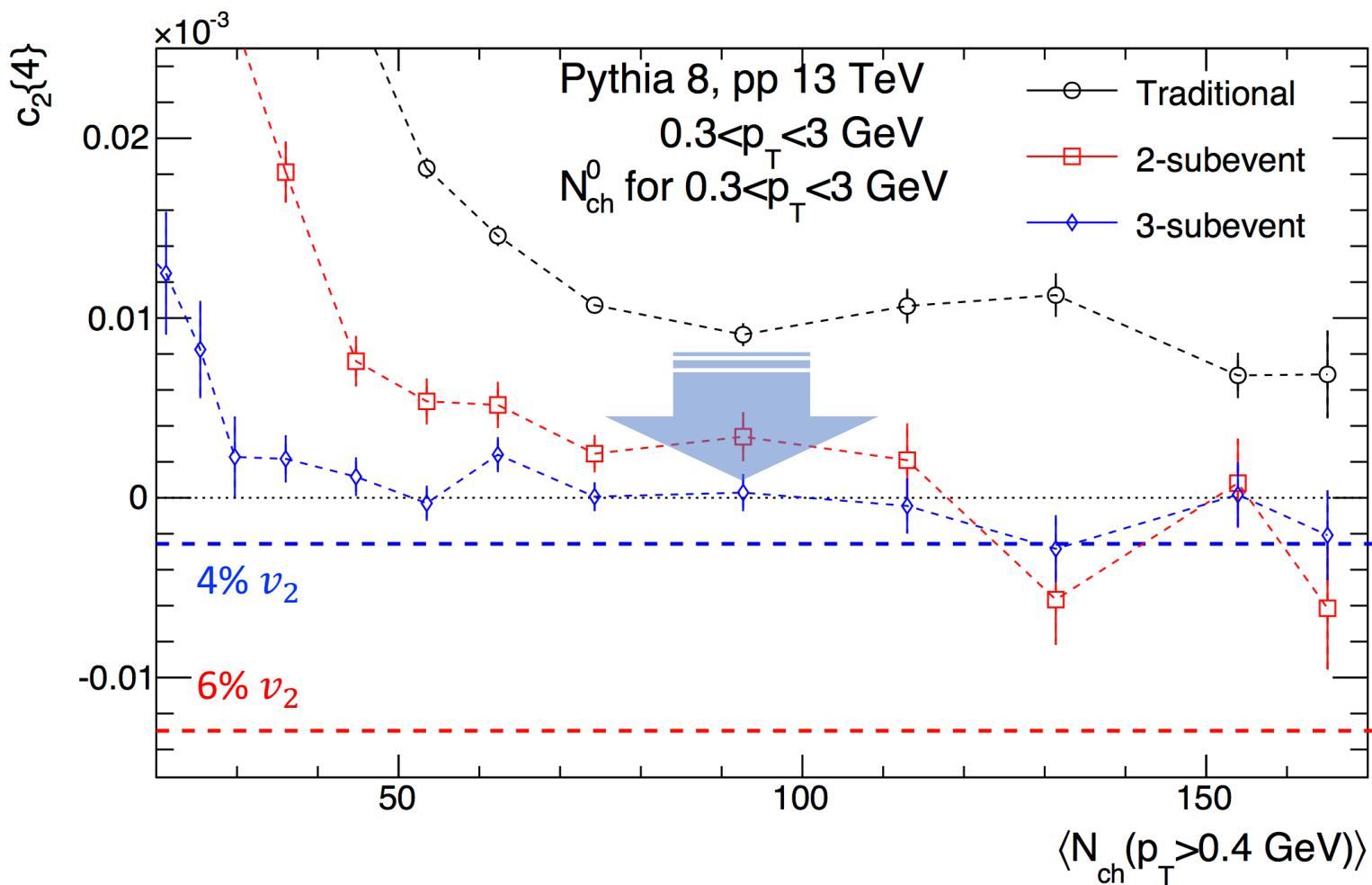
Traditional method



- High probability all four particles come from dijet;
- Solution: higher-order cumulant (statistical significance), or...



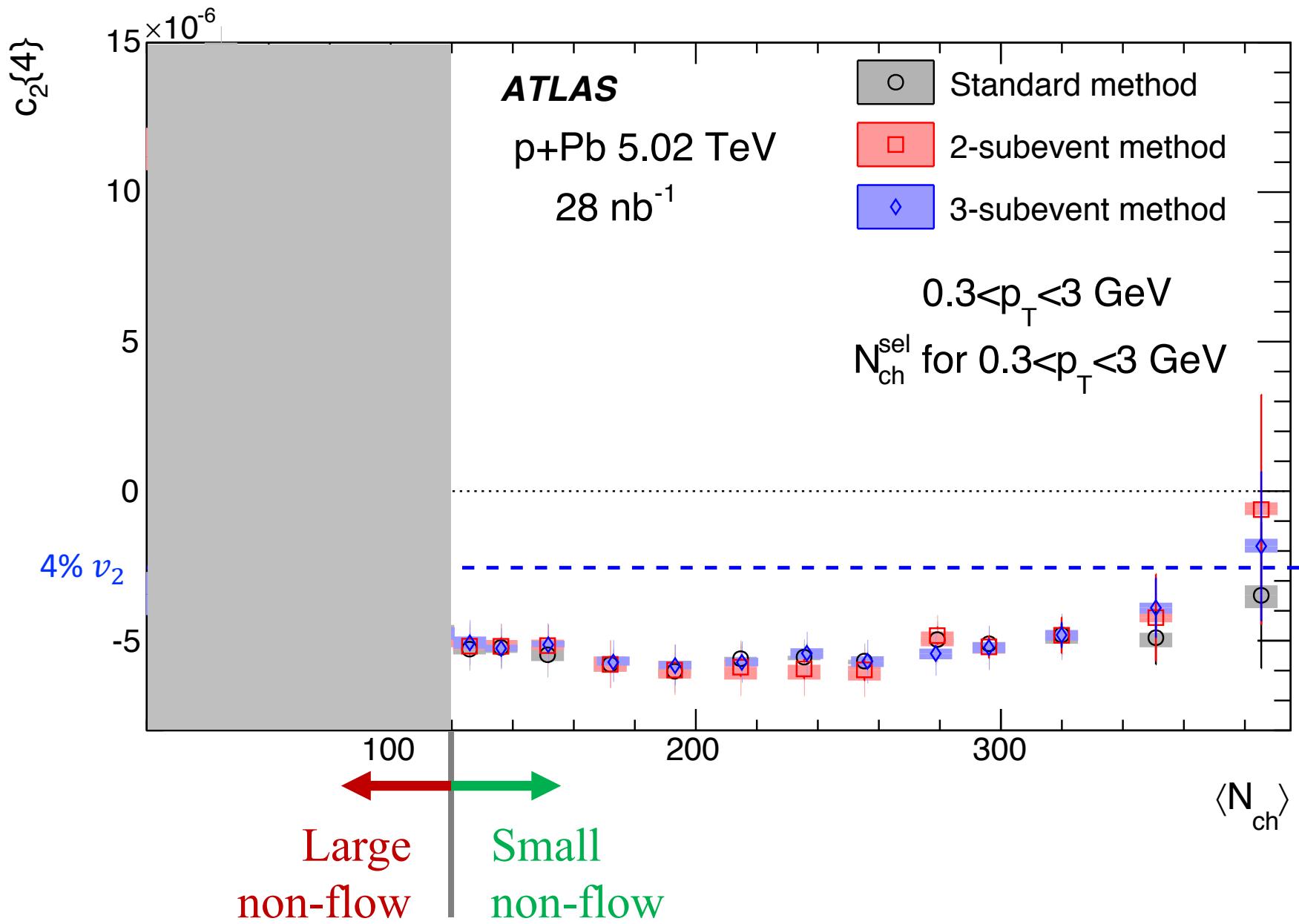
$$3 > 2$$

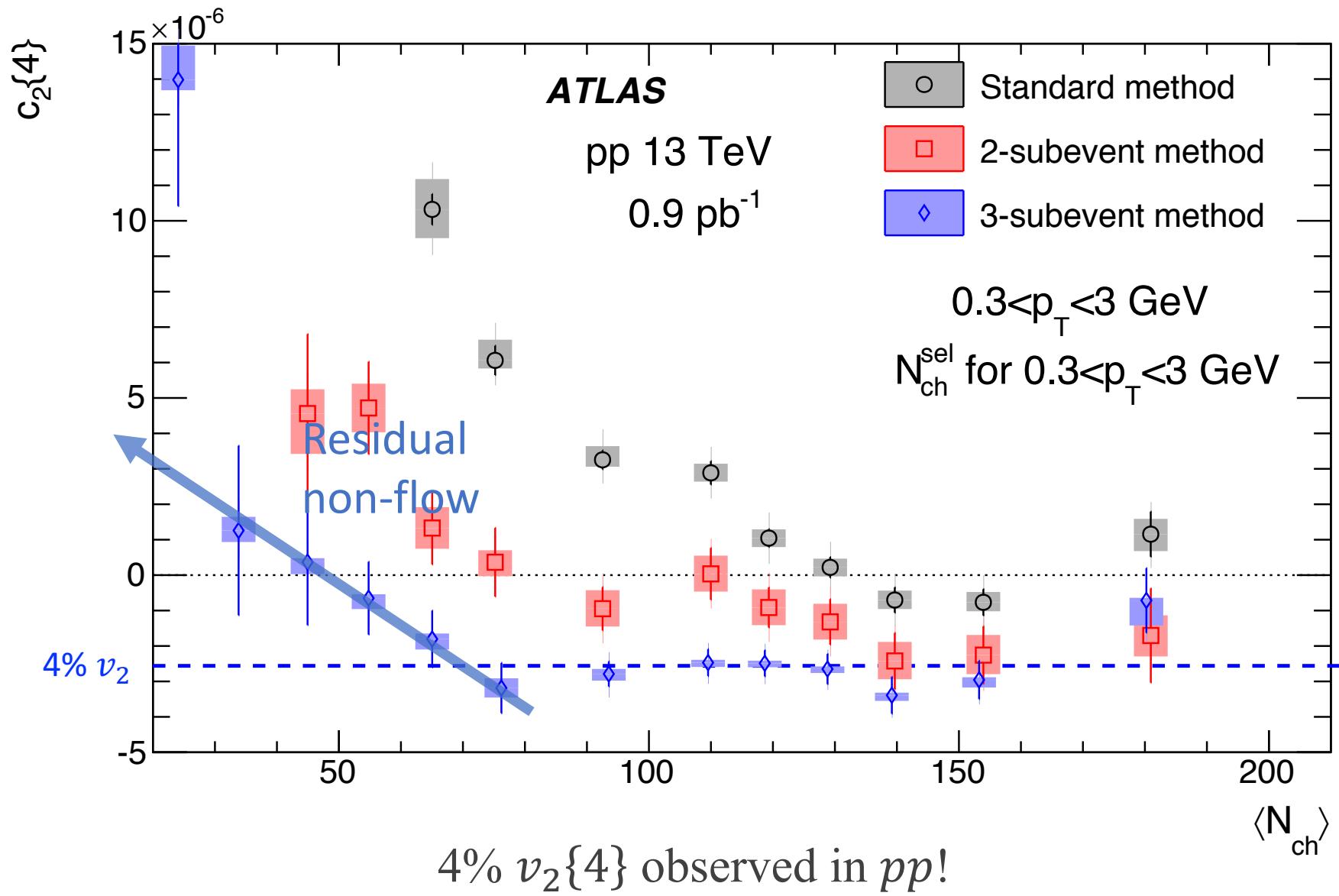


Subevent method can suppress non-flow in PYTHIA

Validation in $p+\text{Pb}$ data

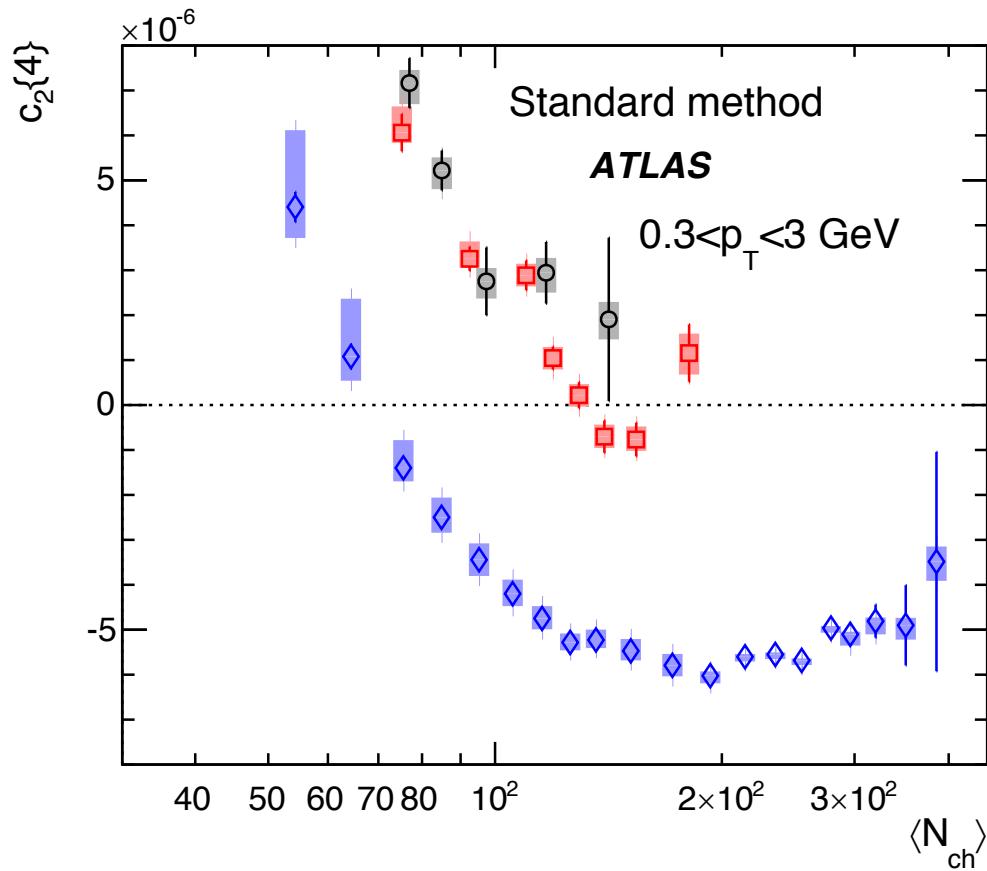
25



$c_2\{4\}$ in pp 

Puzzle 2: energy dependence

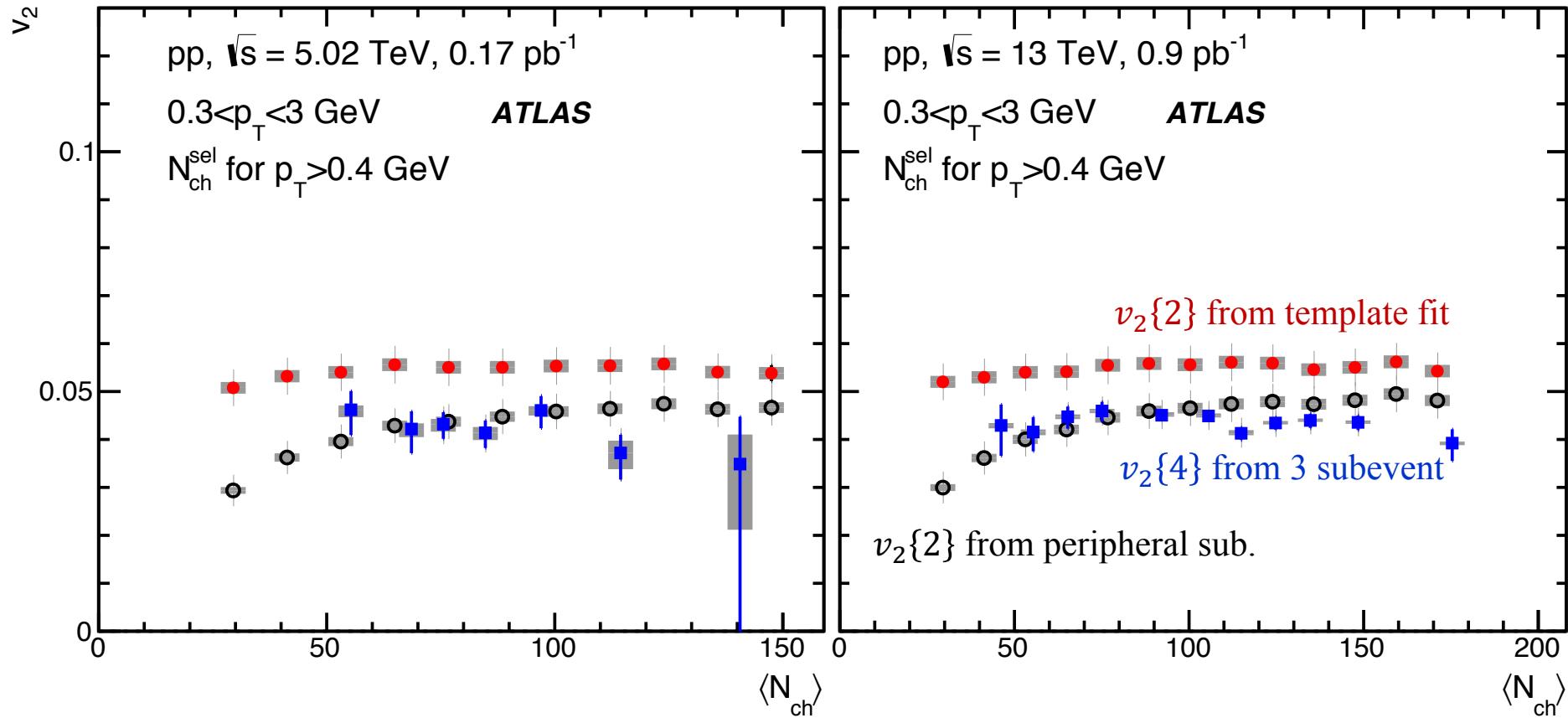
27



- Weak energy dependence in pp ;
- $p+Pb$ has larger flow than pp ;

Puzzle 3: flow fluctuation

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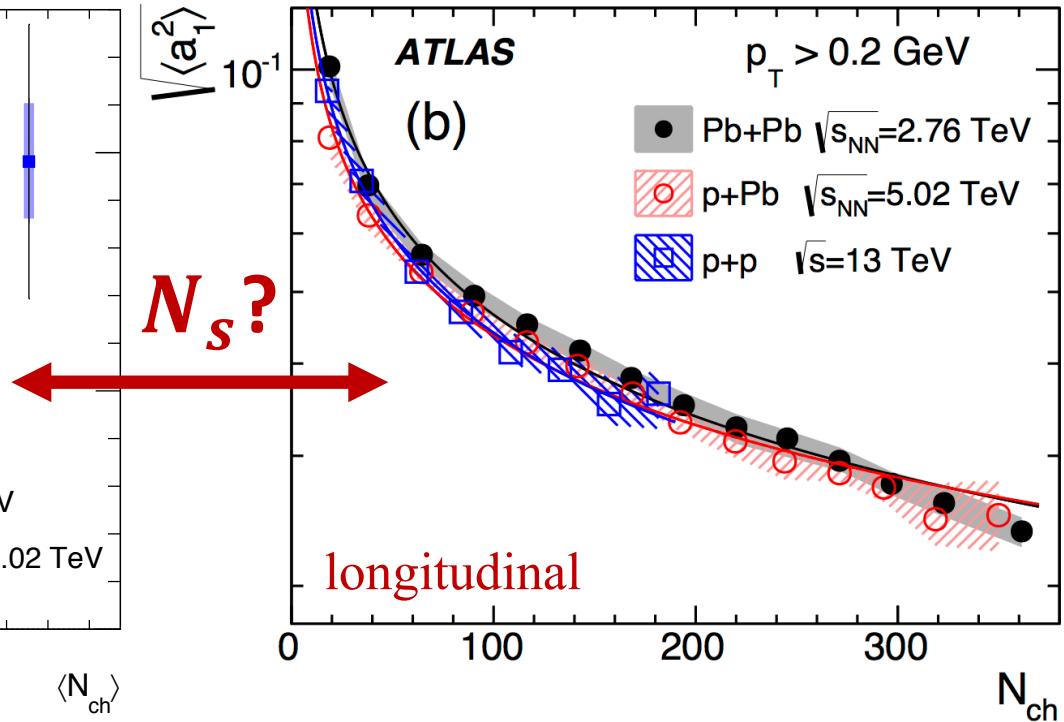
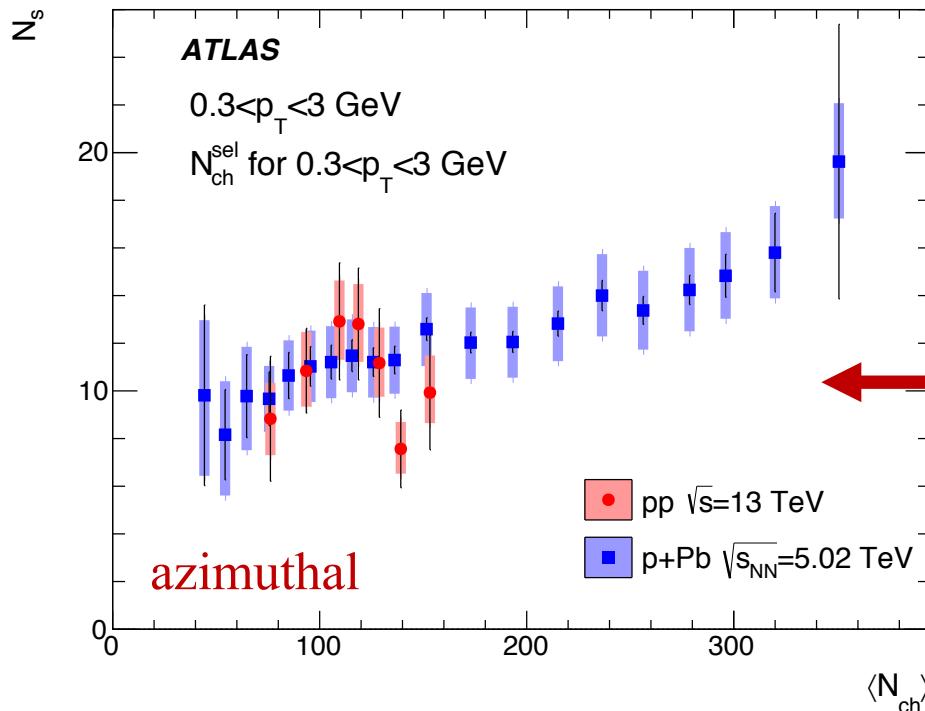


- $v_2\{4\} < v_2\{2\}$ (template fit): flow fluctuation;
- $v_2\{4\} \approx v_2\{2\}$ (peripheral sub.): underestimation of $v_2\{2\}$;
- Subevent cumulant is free of assumptions.

- $\nu_2\{2\} \neq \nu_2\{4\}$: EbyE flow fluctuations associated with fluctuating initial conditions. [Phys. Rev. Lett. 112, 082301 \(2014\)](#)
- Fluctuation can be quantified to the number of sources N_s in the initial stage:

$$\frac{\nu_2\{4\}}{\nu_2\{2\}} = \left(\frac{4}{3 + N_s} \right)^{1/4}$$

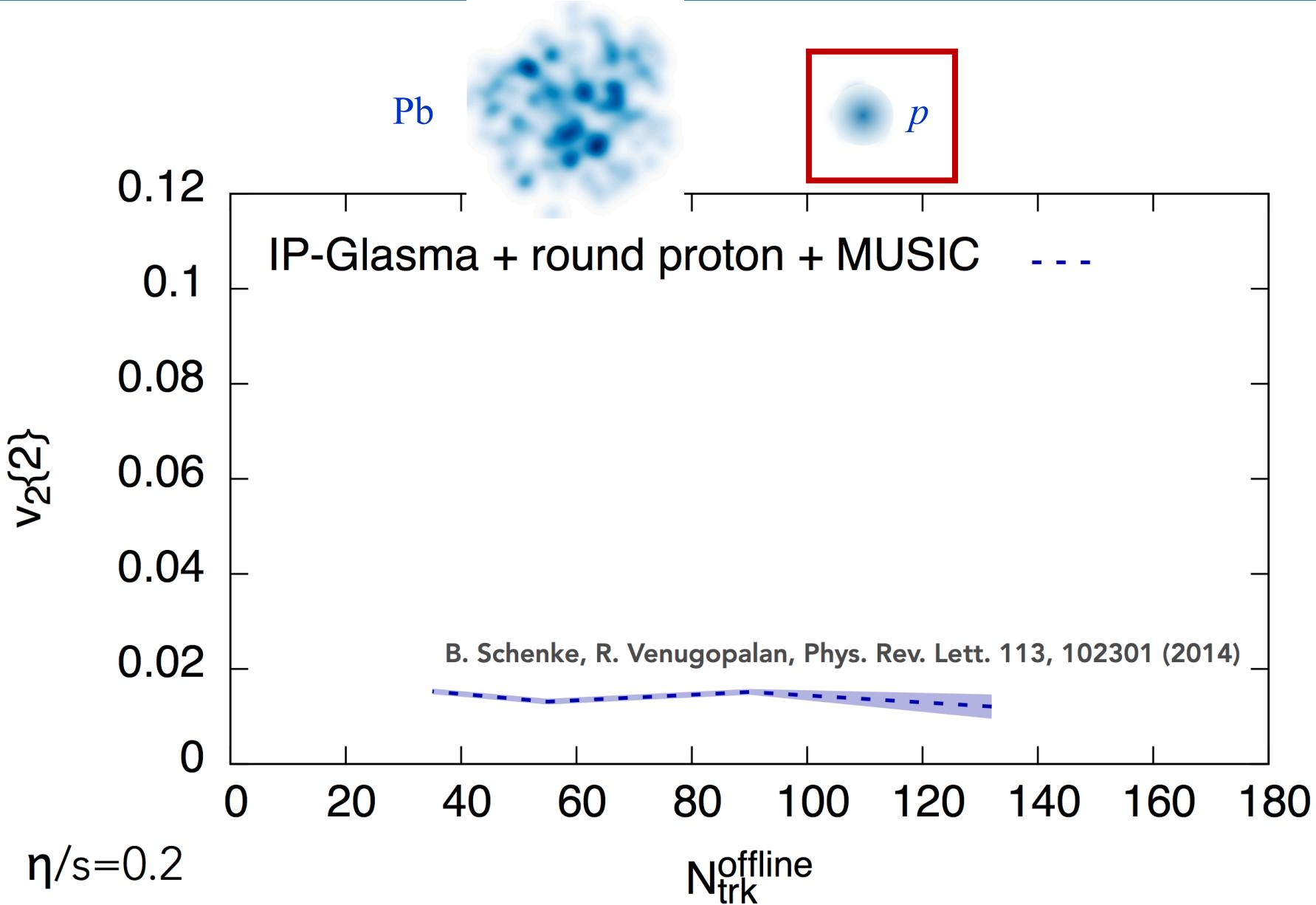
$$\frac{N(\eta)}{\langle N(\eta) \rangle} \approx 1 + a_1 \eta, \quad a_1 \propto \frac{1}{\sqrt{N_s}}$$

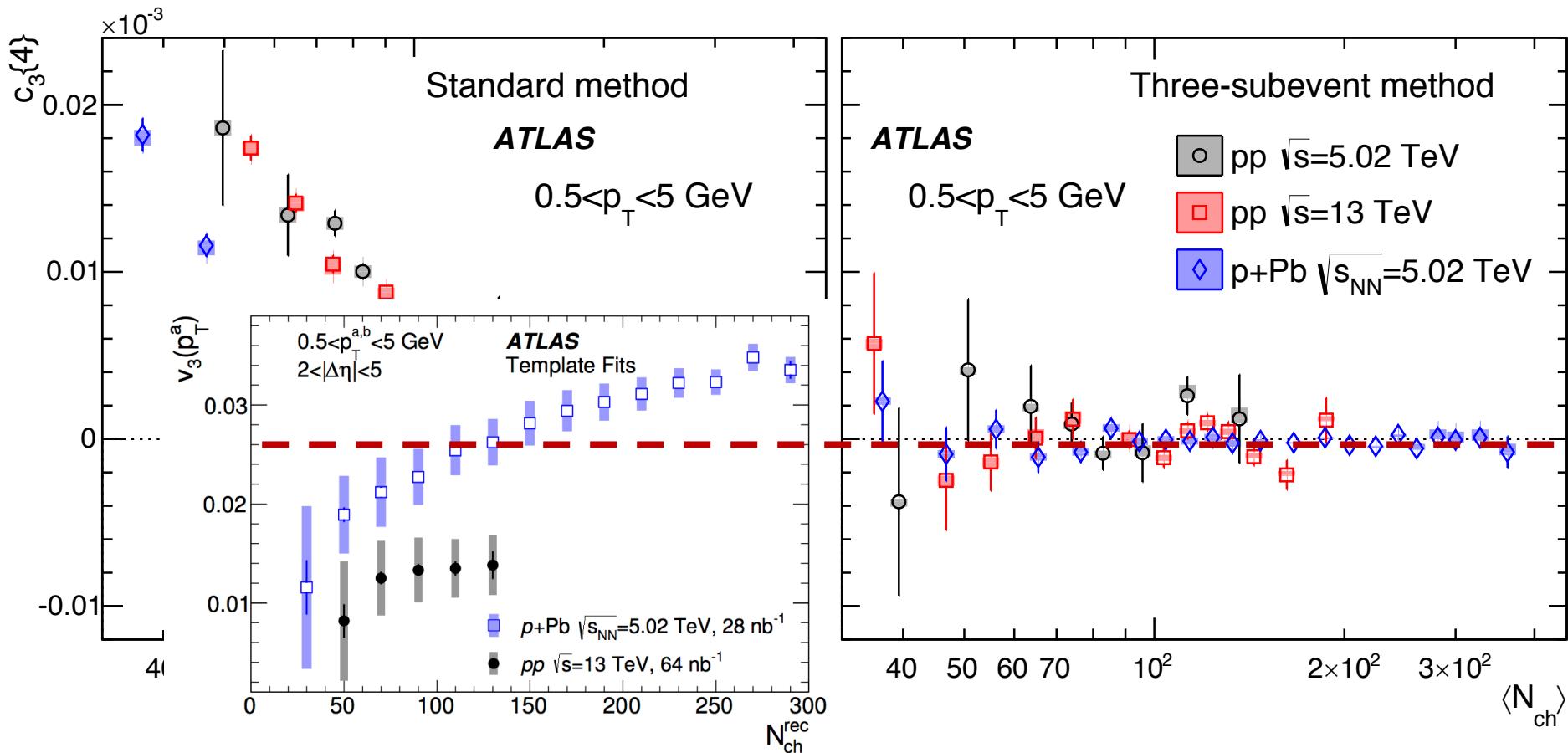


- N_s for $p+Pb$ goes up to 20 at high multiplicity;
- N_s for pp approximately consistent with $p+Pb$ at comparable $\langle N_{ch} \rangle$ value.

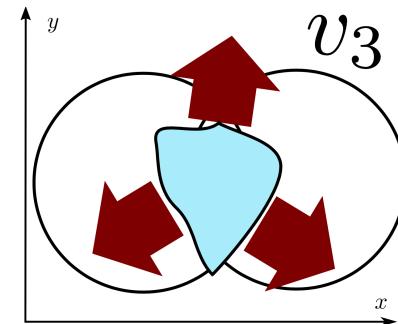
Nucleon substructure fluctuation

30

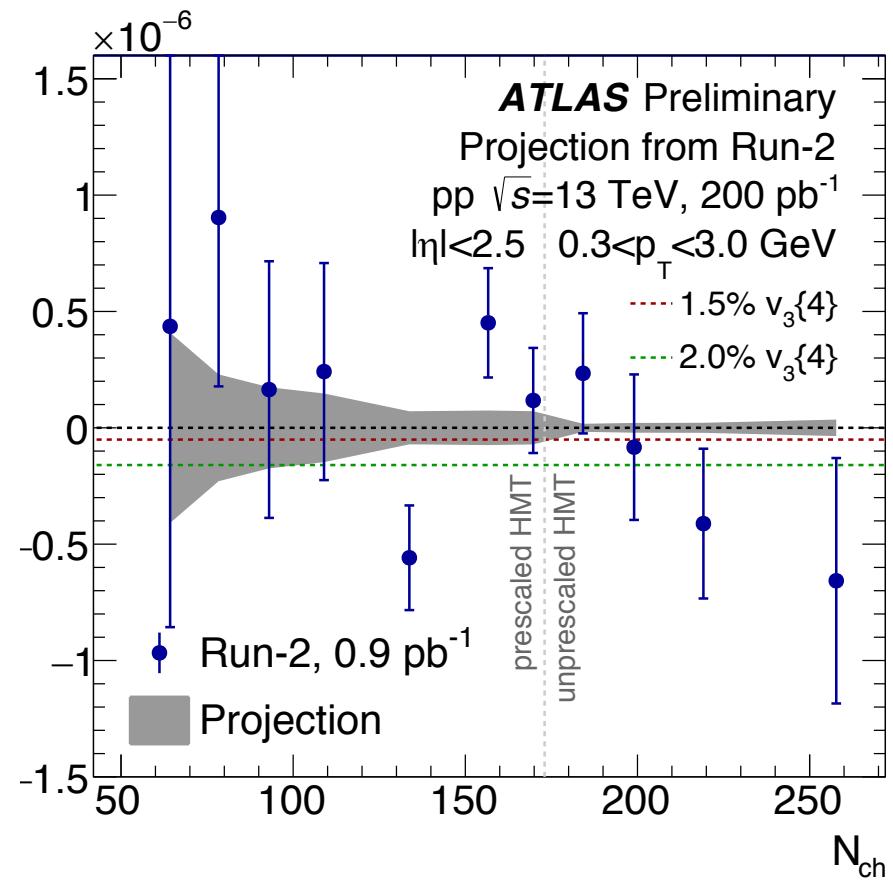
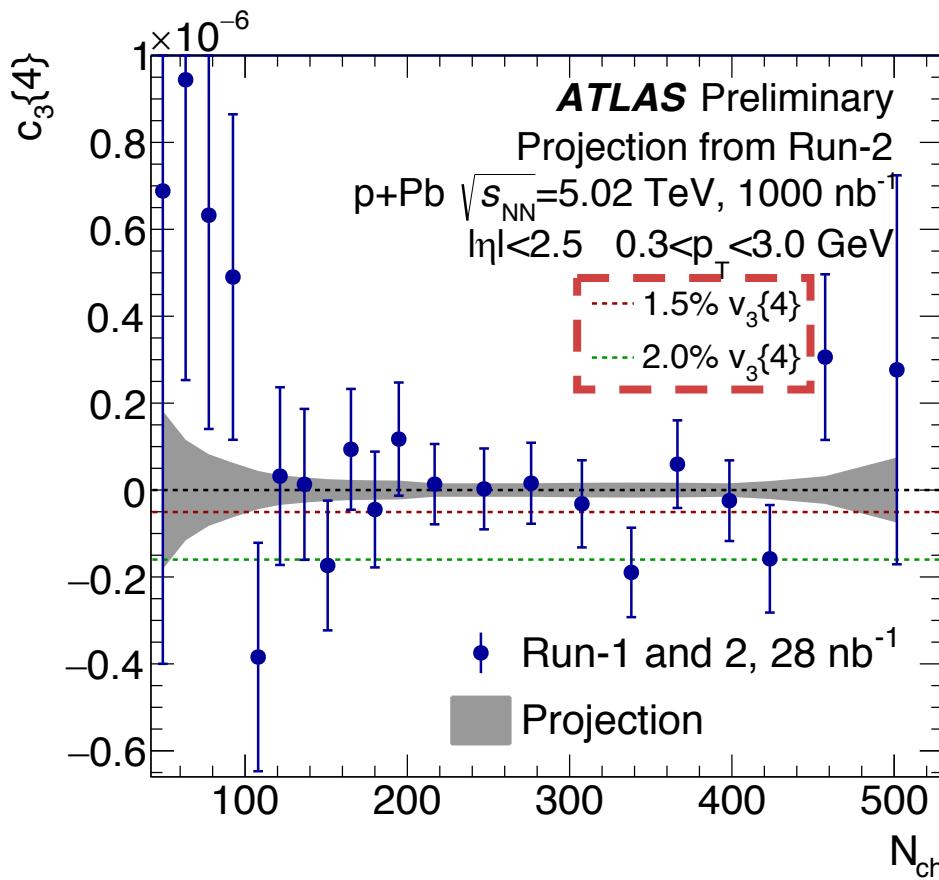




- $c_3\{4\}$ is consistent with 0
 - $\bar{v}_3 \ll \bar{v}_2$?
 - Fluctuation kills $v_3\{4\}$?
 - More statistics needed.



v_3 projected in Run 3



- Opportunity luminosity increase in Run 3;
- Challenges trigger, pileup, tracking...

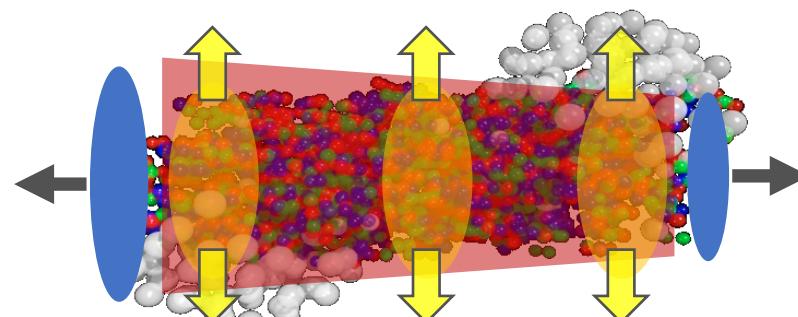
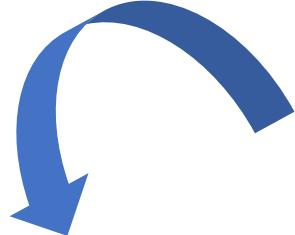


Non-non-flow \neq Flow!

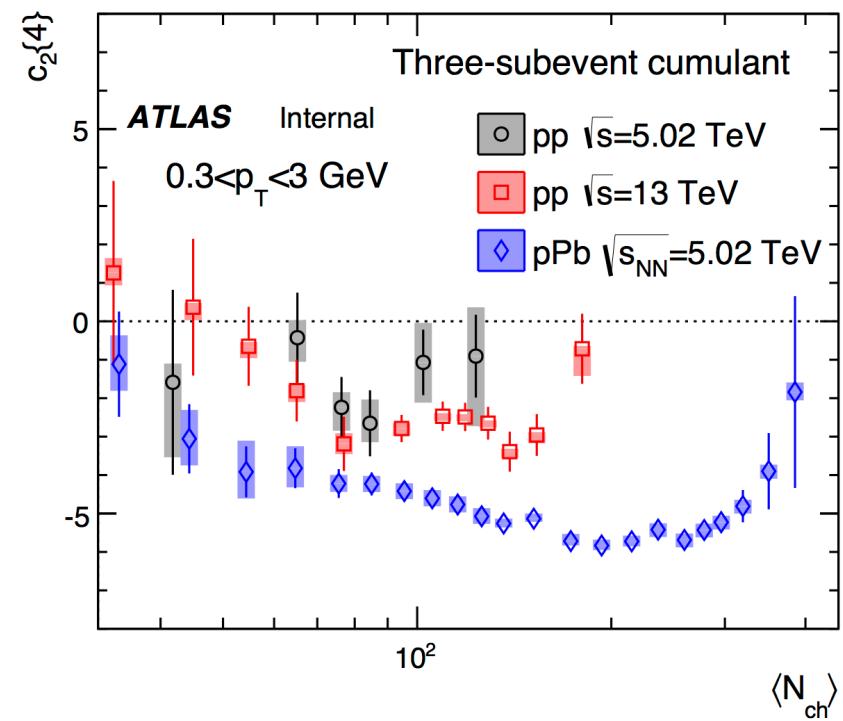
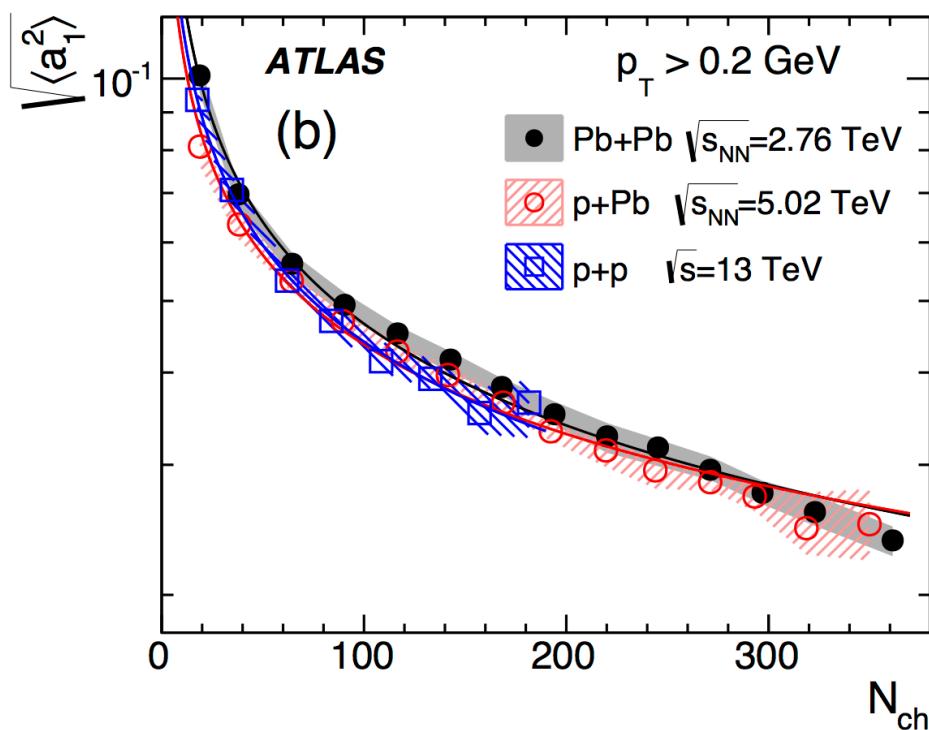
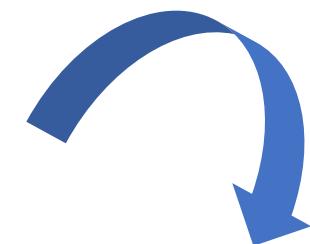
Summary

Nature of sources seeding the long-range collective behavior?

Longitudinal correlation



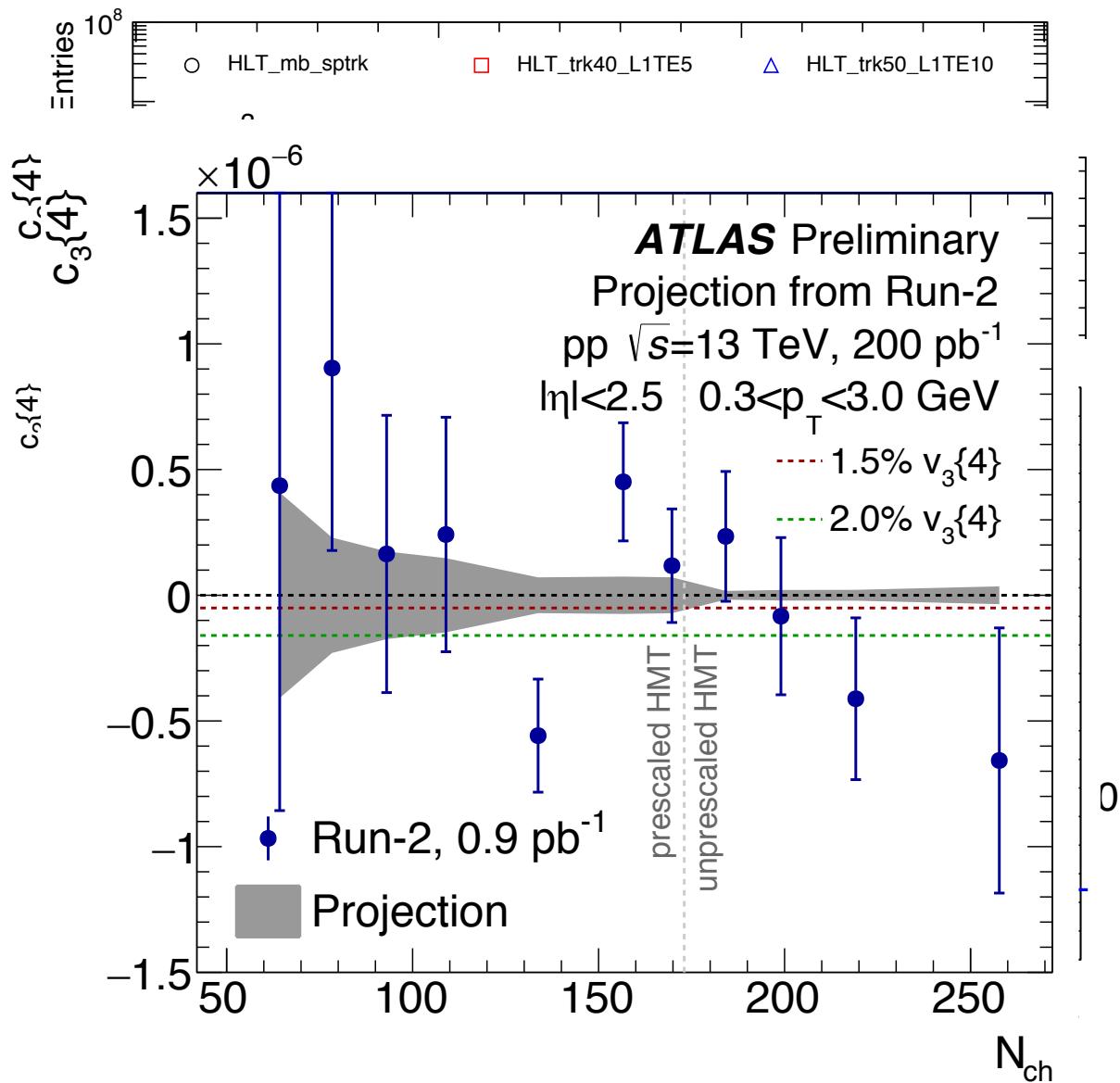
Azimuthal correlation



Evidence of collectivity in small systems!

$pp \sqrt{s} = 7 \text{ TeV}, N \geq 110$

CMS Preliminary



Hypothesis
Collectivity in pp ?

Data Gather
Real-time selection

Data Analysis
Large background

New Algorithm
 $3 > 2$

Conclusion
Collectivity in pp !

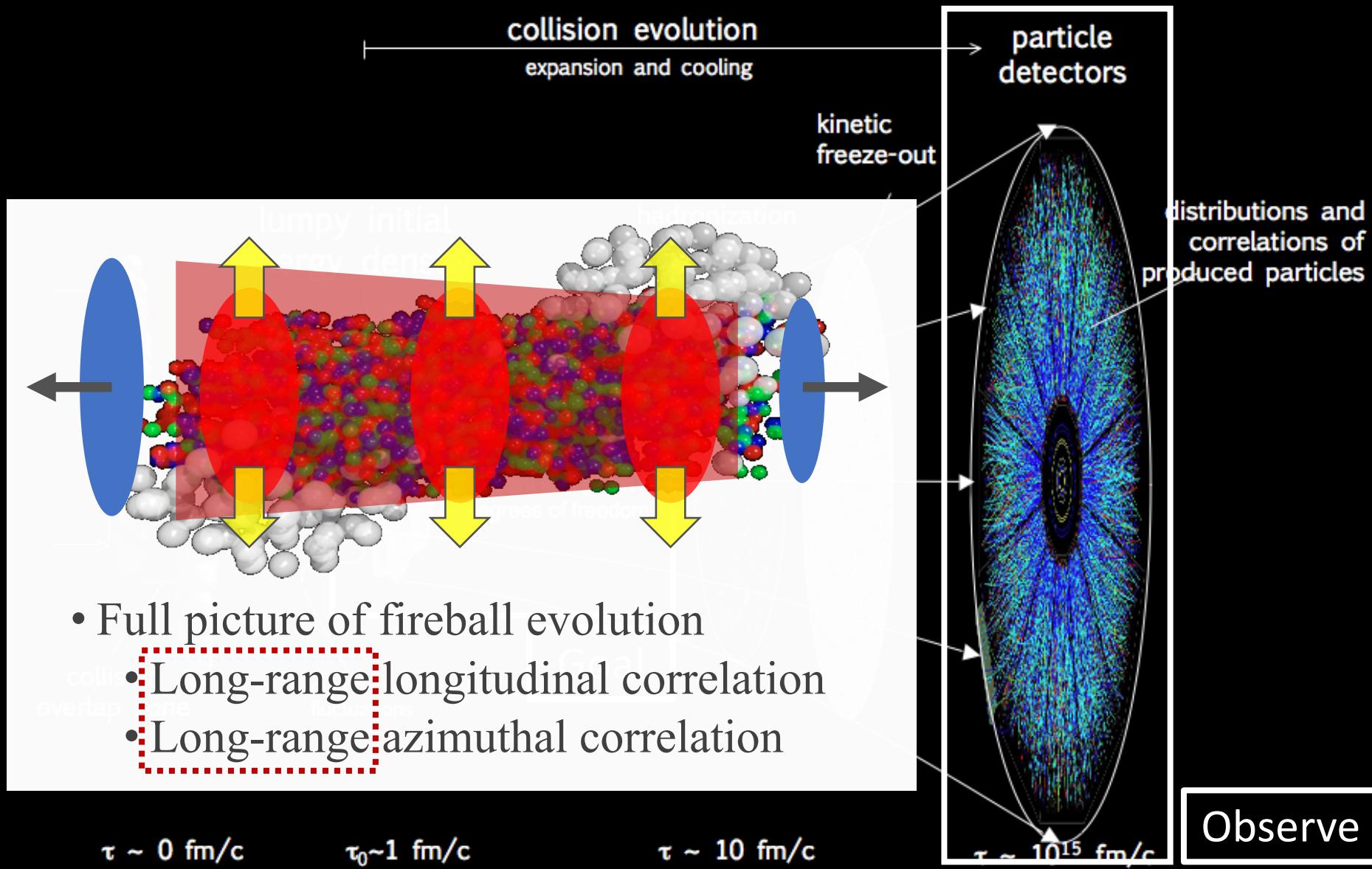
Outlook
More statistics

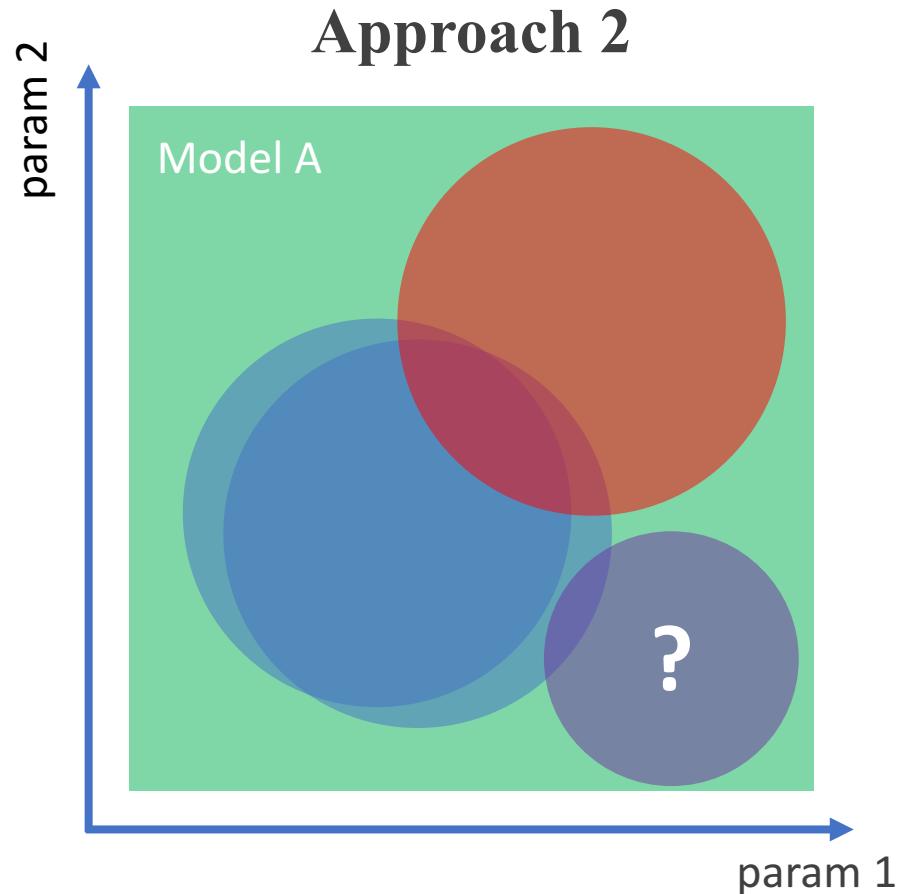
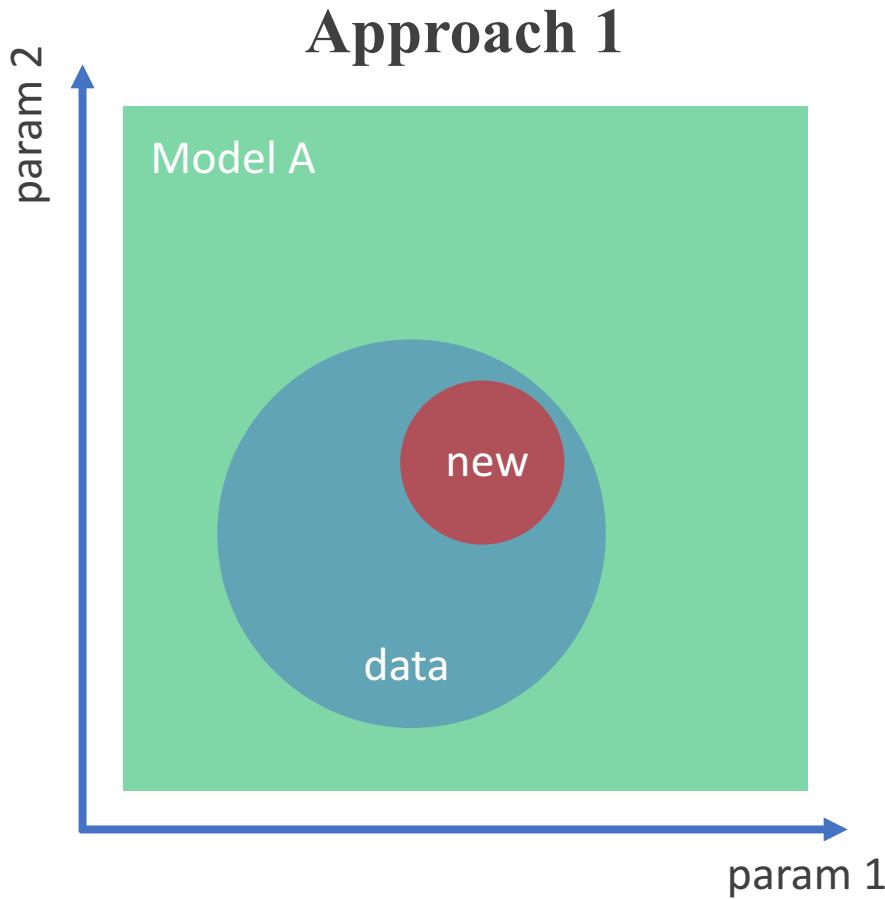
- Longitudinal correlation
 - Phys. Rev. C 93, 044905 (2016) (method)
 - Phys. Rev. C 95, 064914 (2017) (ATLAS)
 - Nucl. Phys. A 956, 769 (2016) (ATLAS proc)
- Subevent cumulant in small systems
 - Phys. Rev. C 96, 034906 (2017) (method)
 - Phys. Rev. C 97, 024904 (2018) (ATLAS)
 - Nucl. Phys. A 967, 472 (2017) (ATLAS proc)
- Centrality fluctuation in large systems
 - Phys. Rev. C 98, 044903 (2018) (method)
 - Submitted to JHEP (2019) (ATLAS)
 - Nucl. Phys. A 982, 323 (2019) (ATLAS proc)
- Cumulants in novel system Xe+Xe
 - Nucl. Phys. A 982, 391 (2019) (ATLAS proc)

Backup

- Forward-backward multiplicity correlation;
- Flow and centrality fluctuation;
- Novel collision system Xe+Xe.

Nuclear collisions and the QGP expansion





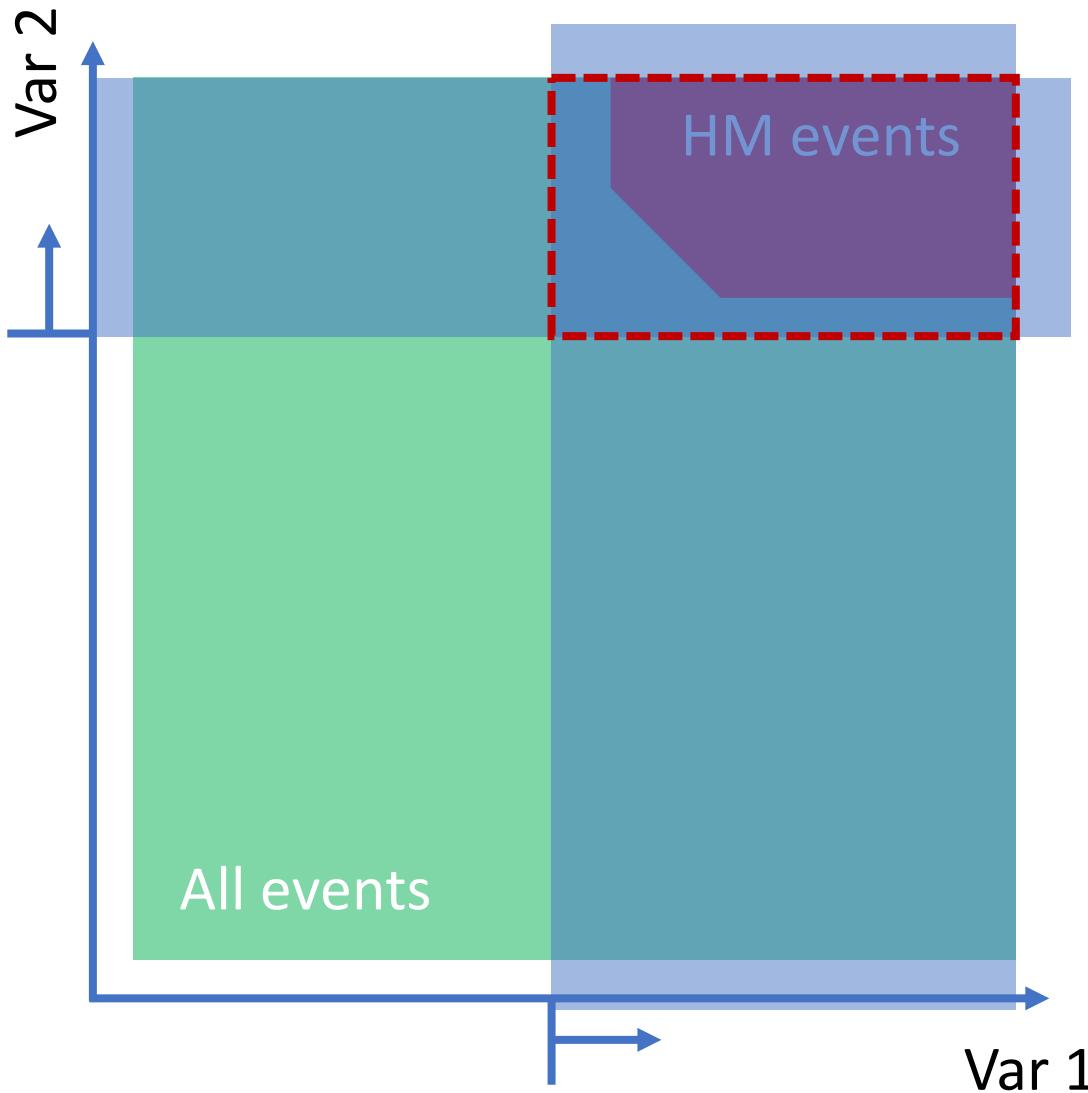
- Improve statistical significance of data

pp and $p+Pb$ events with high statistics

- Independent constrains
 - New observable
 - Collision system
 - Collision energy

Fast online track reconstruction

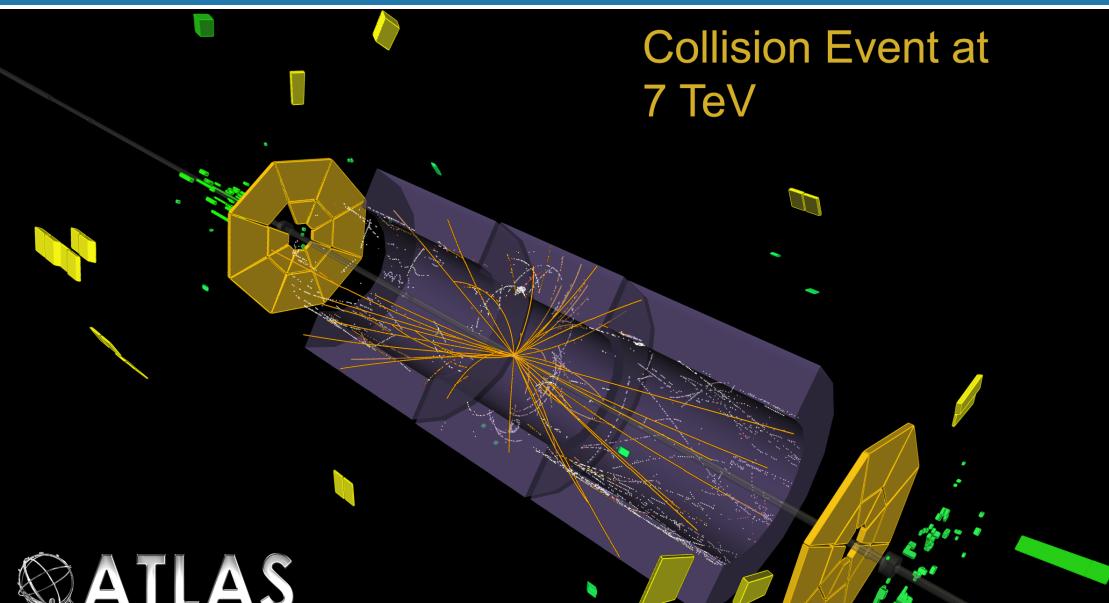
40



Sequence and thresholds of cuts designed to maximize performance.

Event display

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Minimum-bias event
 $N_{ch} \approx 30$

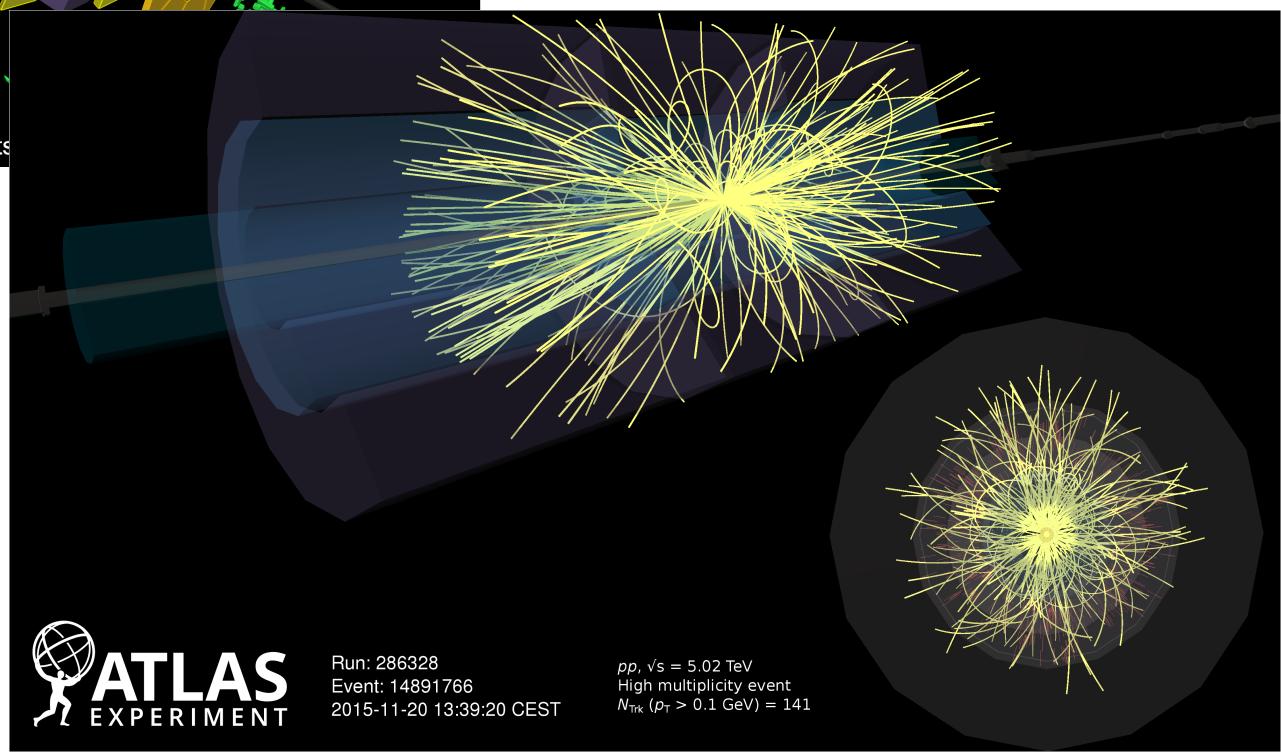
 **ATLAS**
EXPERIMENT

2010-03-30, 12:58 CEST
Run 152166, Event 316199

<http://atlas.web.cern.ch/Atlas/public/EVTDISPLAY/events>

Triggered event

$N_{ch} \approx 140$



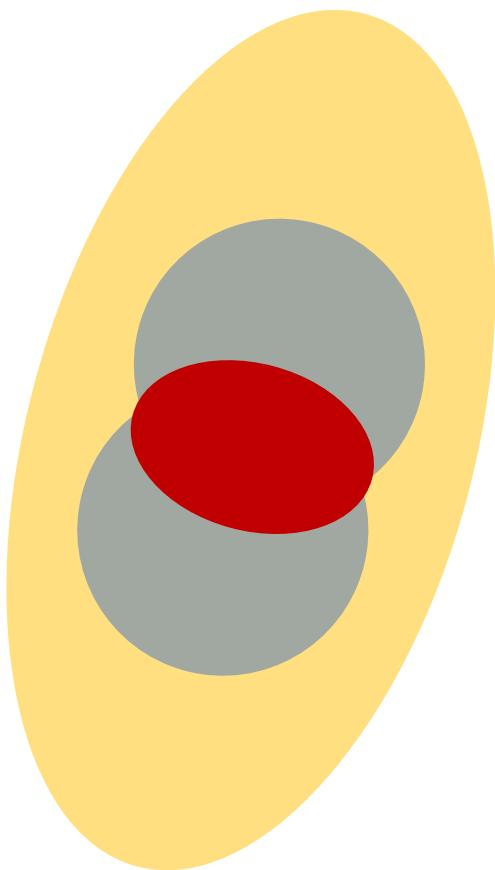
 **ATLAS**
EXPERIMENT

Run: 286328
Event: 14891766
2015-11-20 13:39:20 CEST

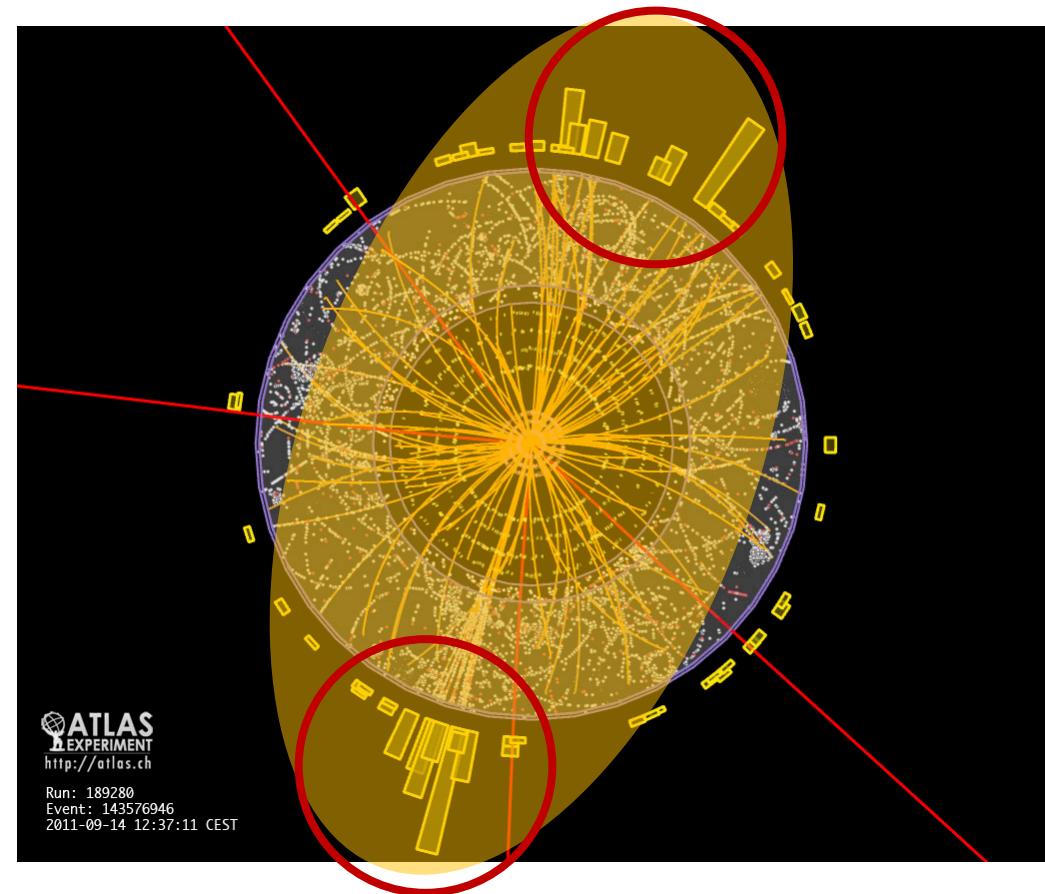
$pp, \sqrt{s} = 5.02 \text{ TeV}$
High multiplicity event
 $N_{\text{Trk}} (p_T > 0.1 \text{ GeV}) = 141$

Signal or background?

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Signal: collectivity

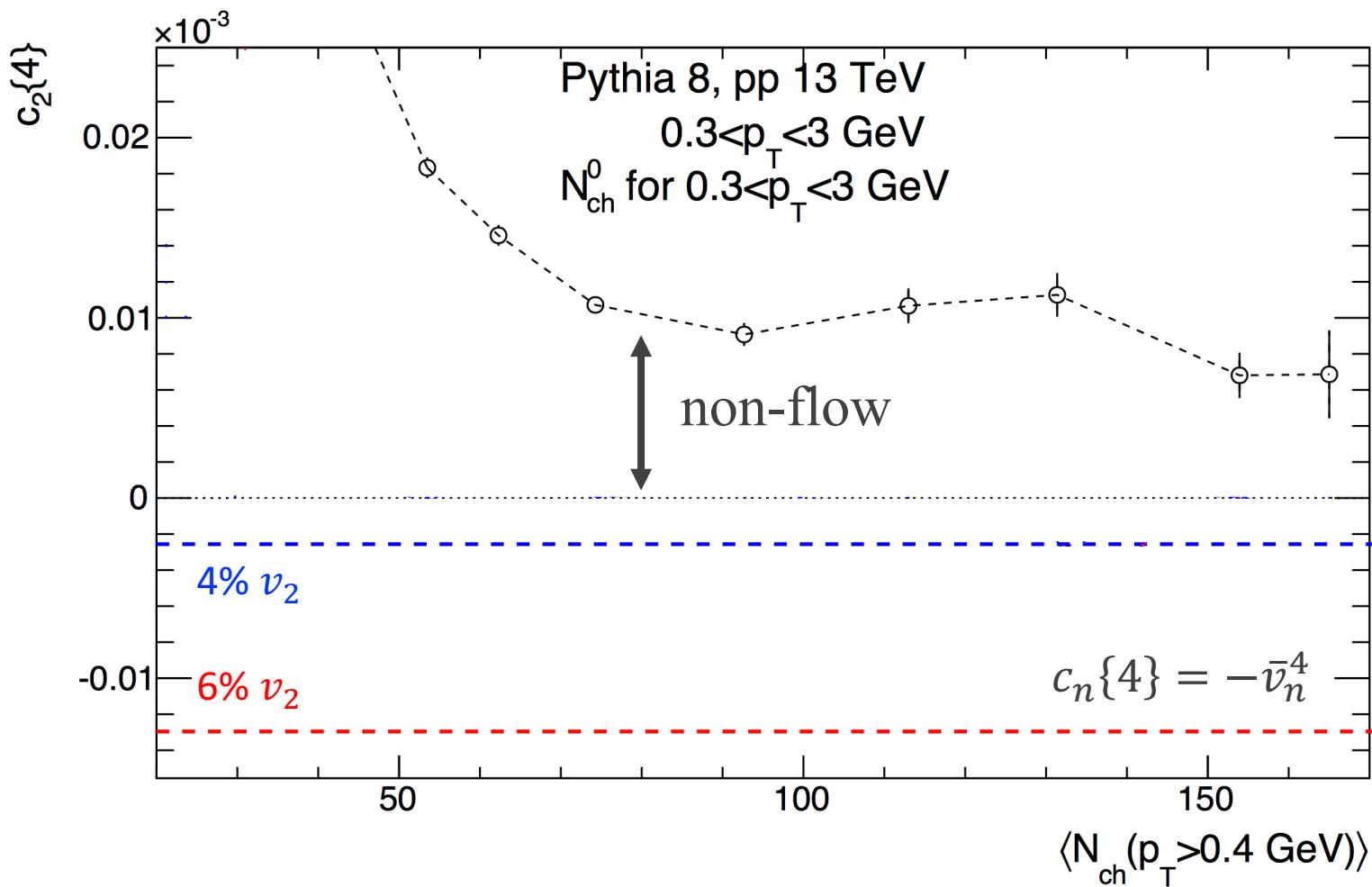


Background: dijets

Maybe background is the one to blame?

Test of background

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Traditional cumulant cannot remove non-flow in pp

Test of residual non-flow

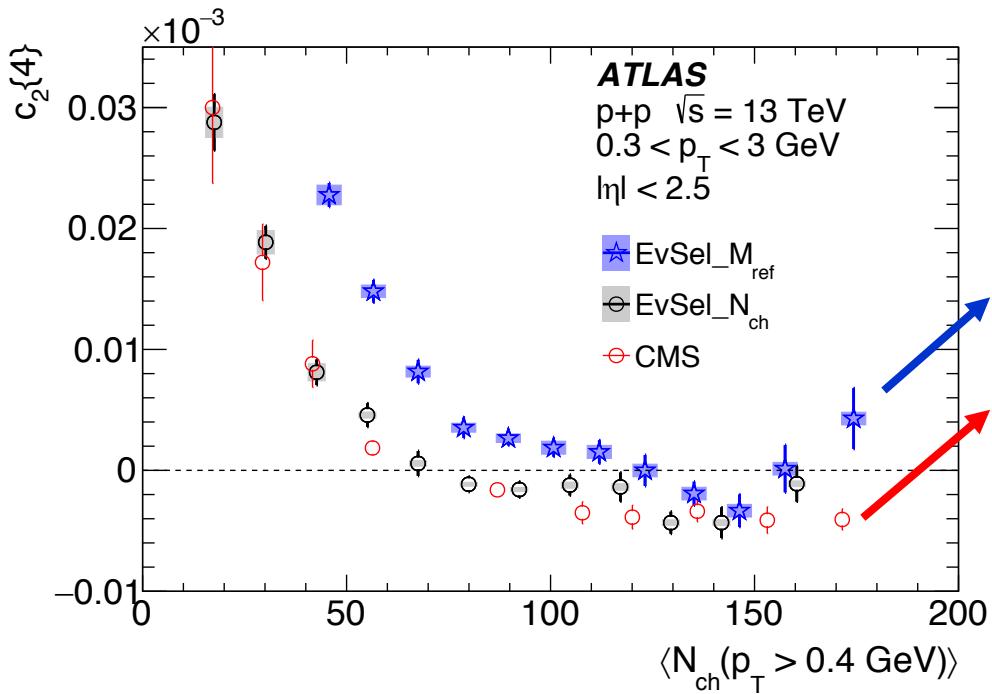
$$c_2\{4\} \equiv$$

$$\langle \text{nonflow} + \text{flow} \rangle_{evt}$$

Non-flow changes greatly EbyE

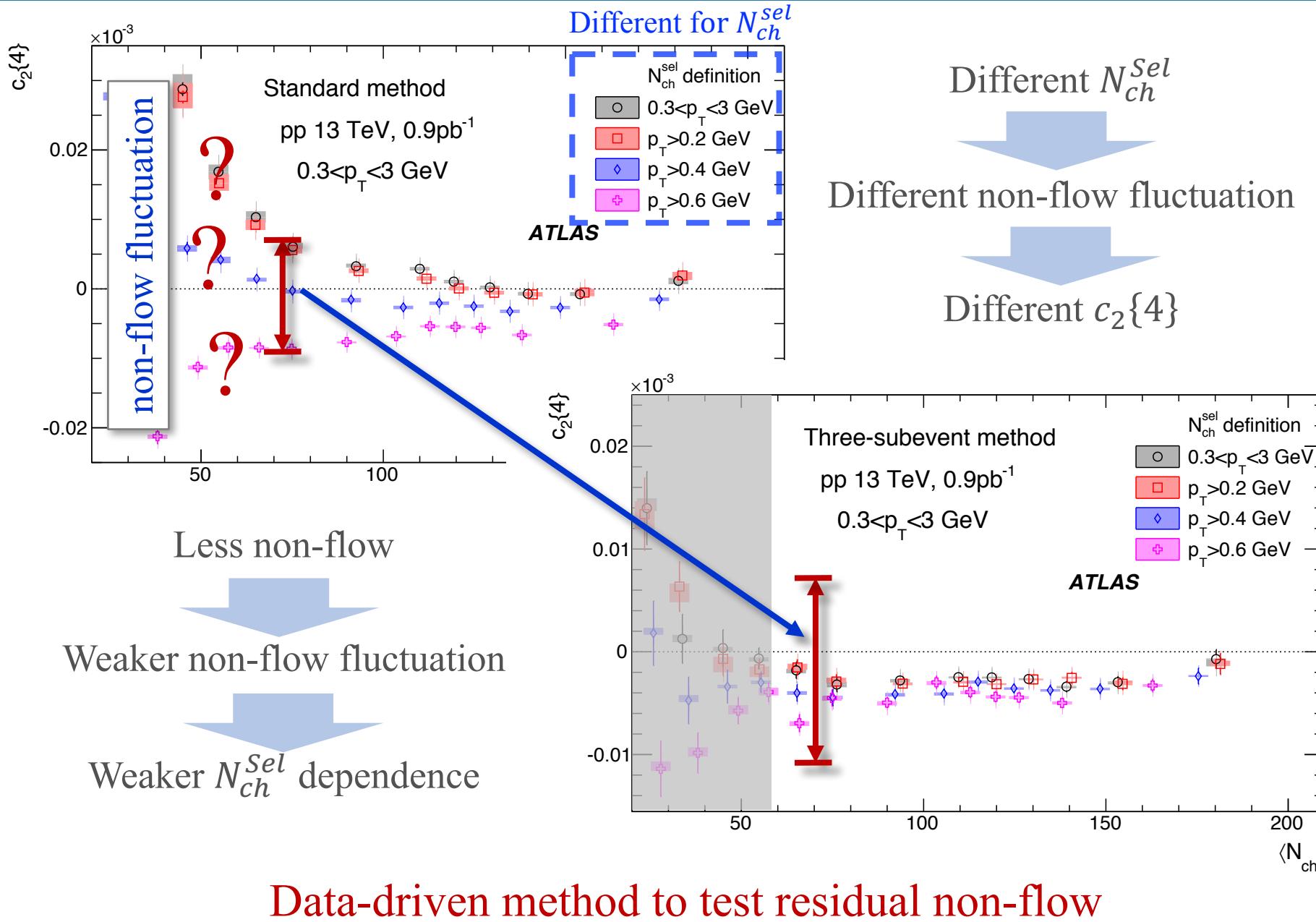
Flow changes little EbyE

non-flow fluc. ← multiplicity fluc. ← how $\langle \dots \rangle_{evt}$ is defined: N_{ch}^{Sel}



- N_{ch}^{Sel} defined with different p_T : very different non-flow fluctuation.
- N_{ch}^{Sel} defined with $0.3 < p_T < 3.0$ GeV
- N_{ch}^{Sel} defined with $p_T > 0.4$ GeV
- Non-flow fluctuation might mimic the flow signal (negative $c_2\{4\}$)!

Puzzle 1: N_{ch}^{sel} dependence

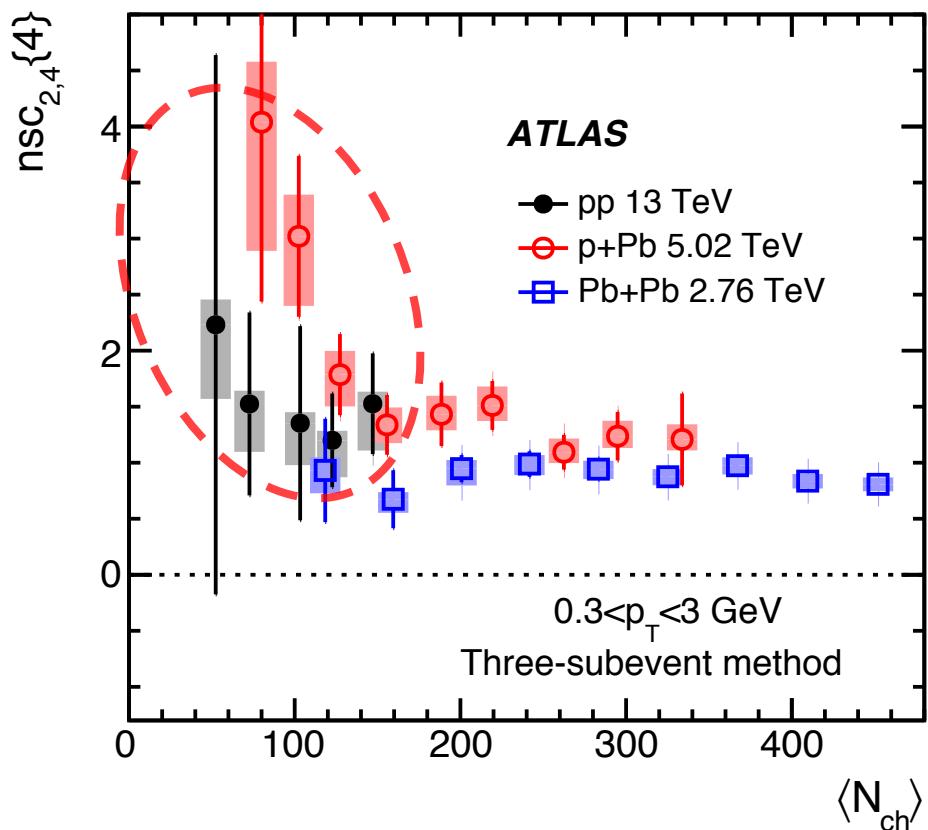
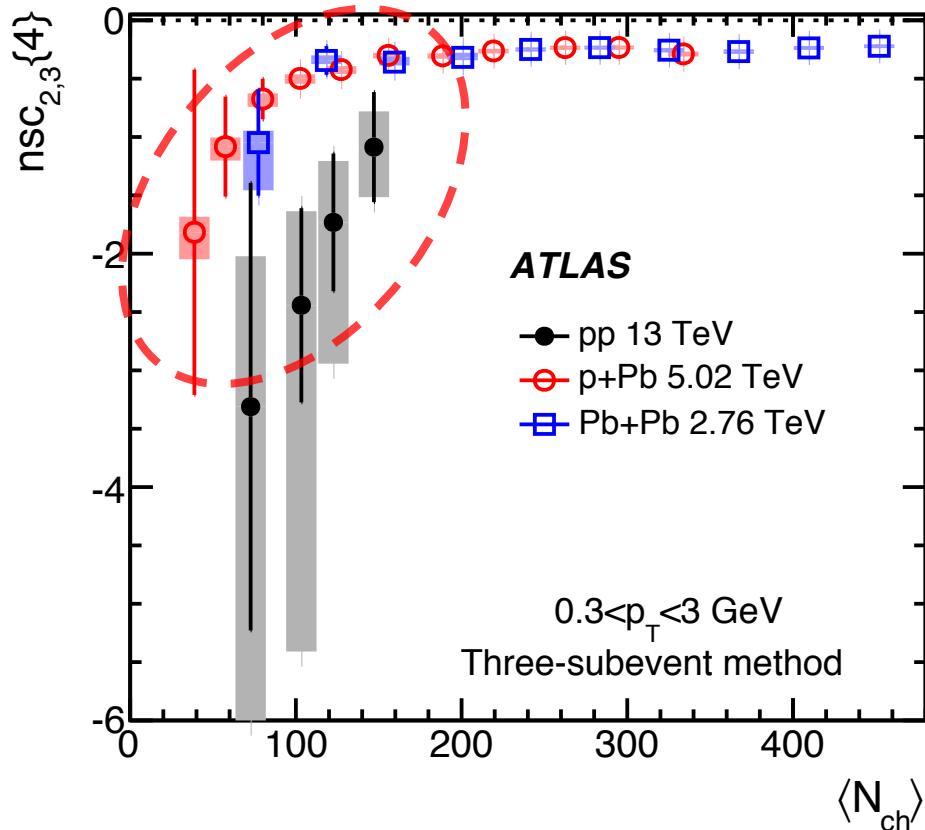


Correlation between v_n and v_m

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$$nsC_{n,m}\{4\} = \frac{\langle v_n^2 v_m^2 \rangle - \langle v_n^2 \rangle \langle v_m^2 \rangle}{\langle v_n^2 \rangle \langle v_m^2 \rangle}$$

[Phys. Lett. B 789 \(2019\) 444](#)



- Same sign, different magnitudes across systems;
- Independent constraints on models.

Forward-backward multiplicity fluctuation

Motivation: a historical view

- Rapidity correlations is an old story



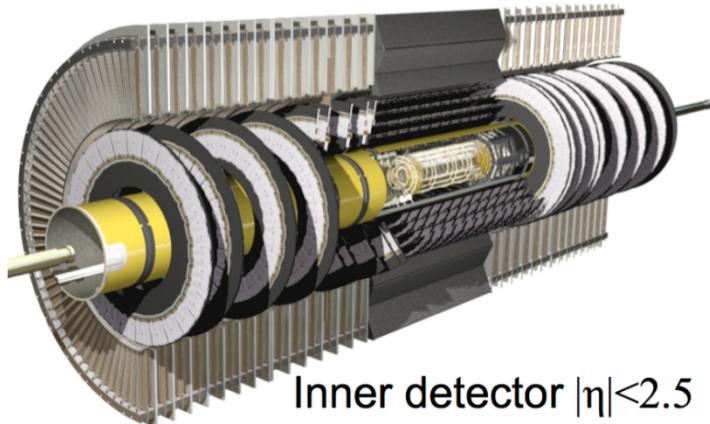
- Physics goal: understand production mechanism in early stage.

- More details see the thesis.

- Why we come back to this analysis?

- Previous methods focused on limited phase space: η and $-\eta$;
 - We used a new observable that covers full η space;
 - Short-range correlation and statistical dilution;
 - We estimated short-range correlation;
 - Few direct comparisons among different systems;
 - We compared from large to small systems.

- Correlation functions calculated using charged particles $p_T > 0.2$ GeV;
- High-multiplicity track (HMT) trigger used to increase statistics;

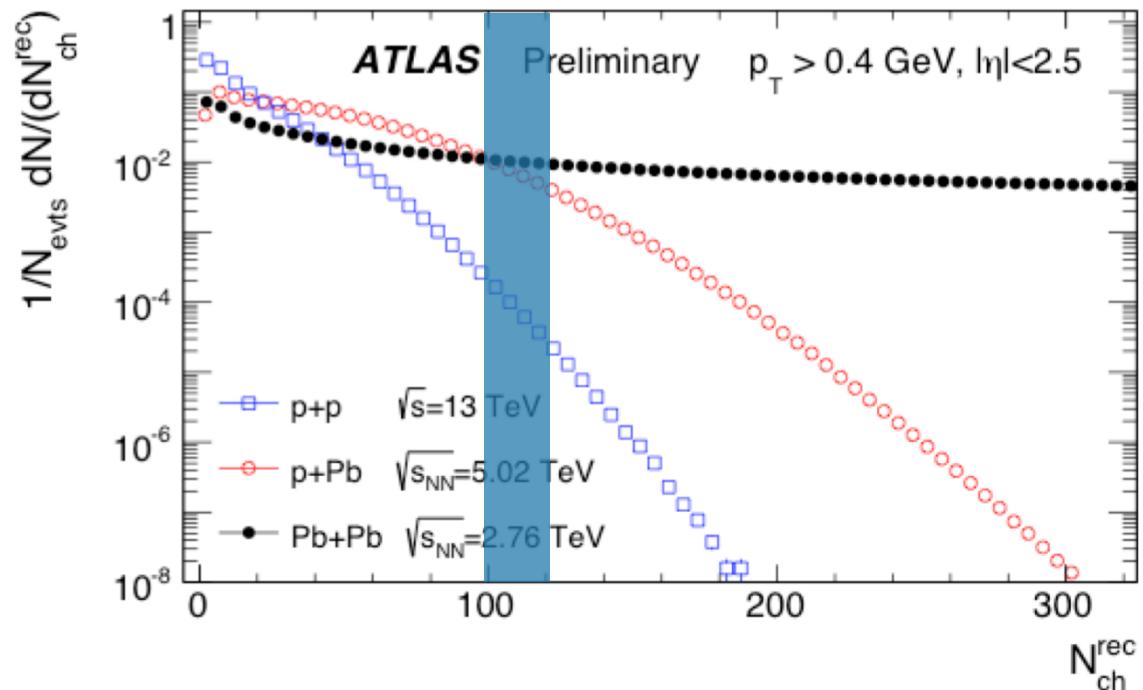


Inner detector $|\eta| < 2.5$

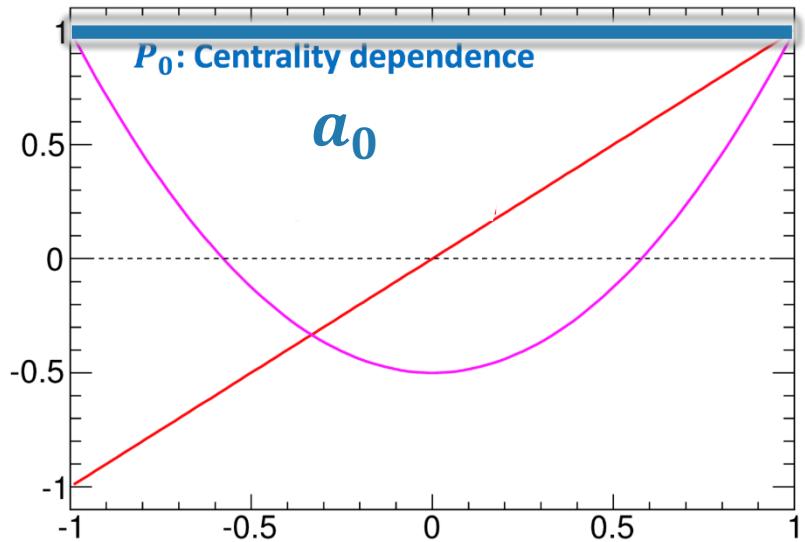
Pb+Pb 2.76 TeV, 2010, MB

p +Pb 5.02 TeV, 2013, MB+HMT

p + p 13 TeV, 2015, MB+HMT

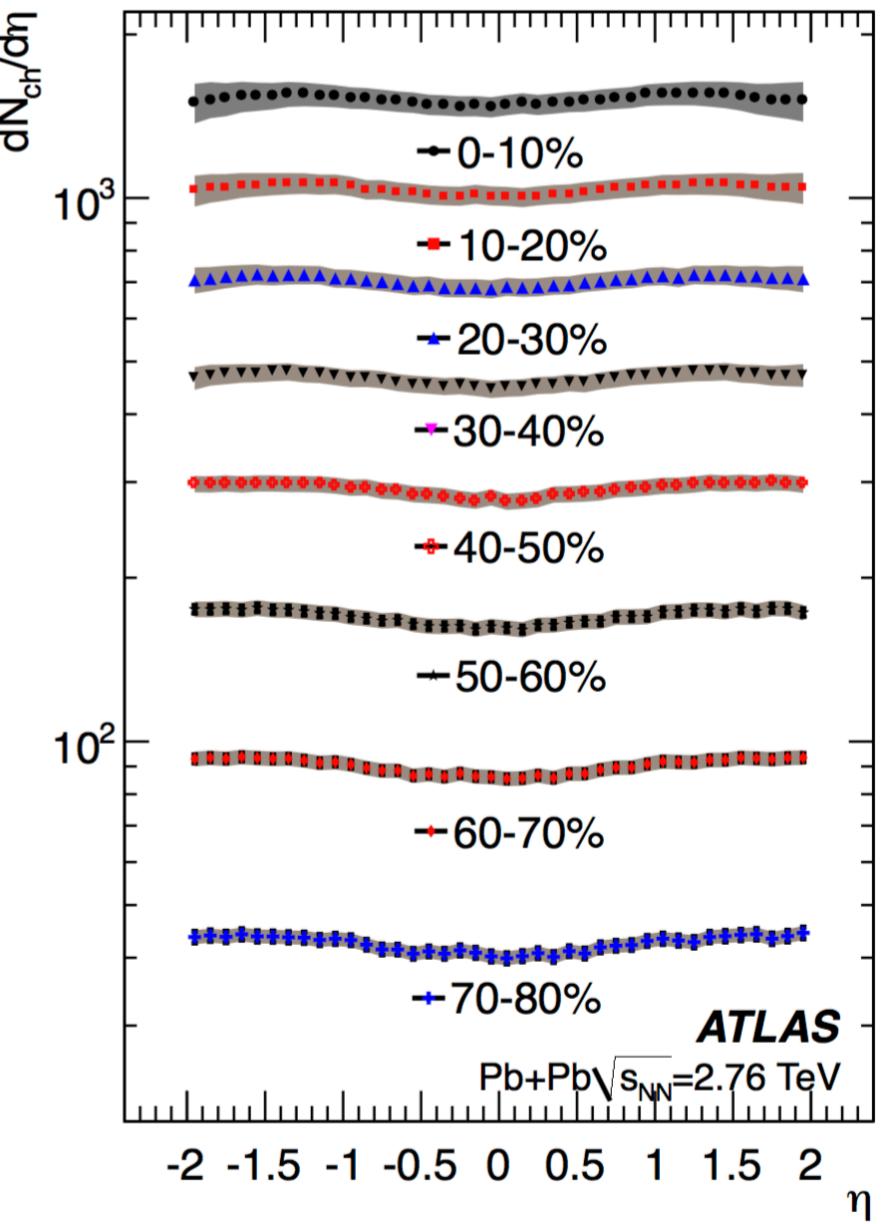


- Analysis carried out in many bins over $10 \leq N_{ch}^{rec} < 300$;
- Results presented as a function efficiency-corrected values N_{ch} .
 - How long-range correlation compare among three systems, at the same N_{ch} ?

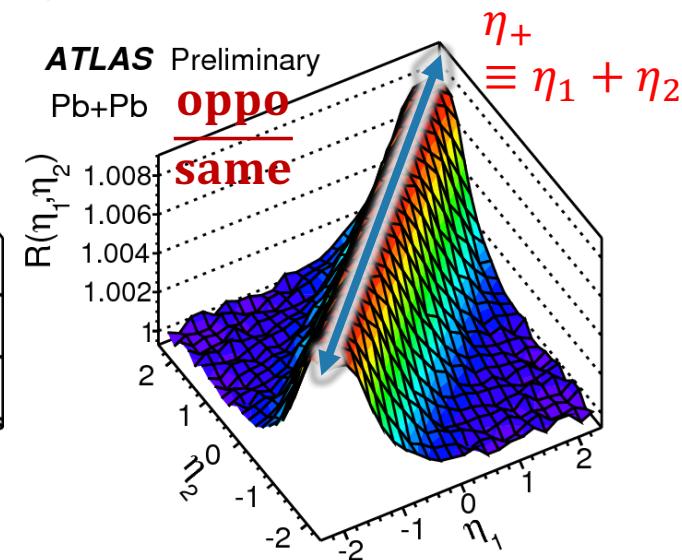
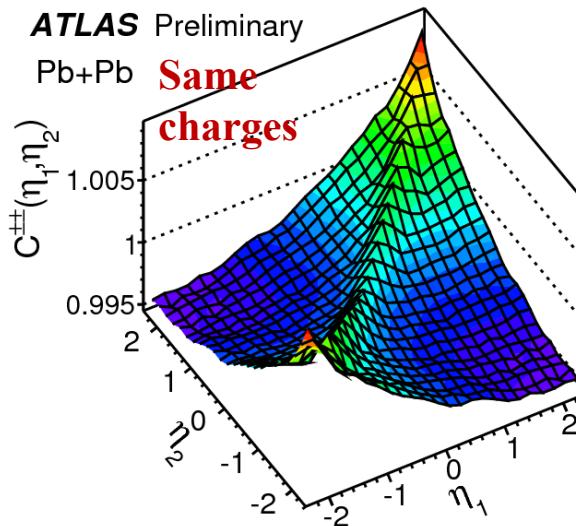
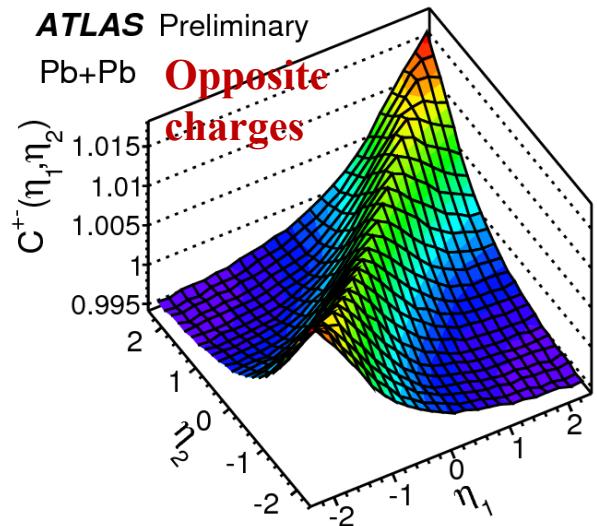


- Analysis focuses on dynamical fluctuation upon average;
- However, average multiplicity changes with centrality;
- The residual centrality dependence is removed by normalizing $C(\eta_1, \eta_2)$

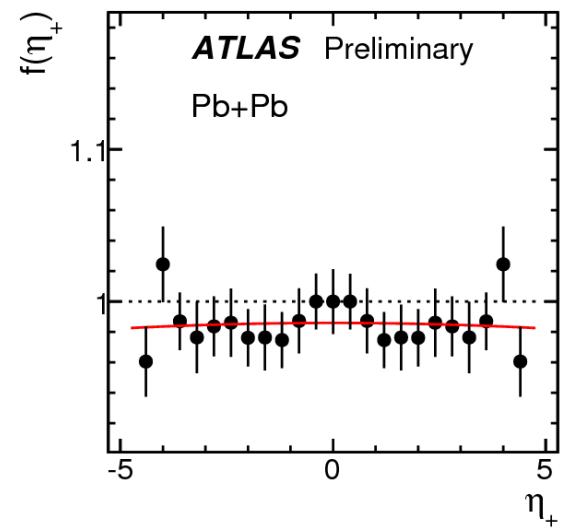
$$C_N(\eta_1, \eta_2) = \frac{C(\eta_1, \eta_2)}{C_p(\eta_1)C_p(\eta_2)}$$



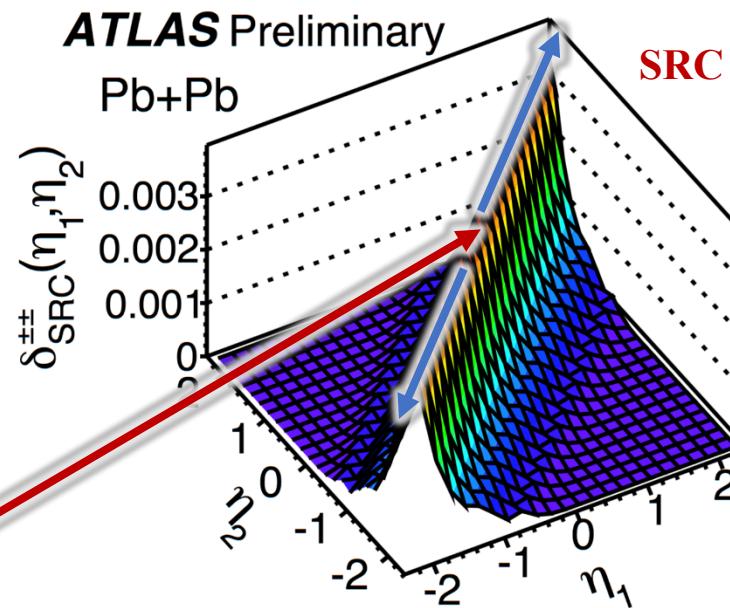
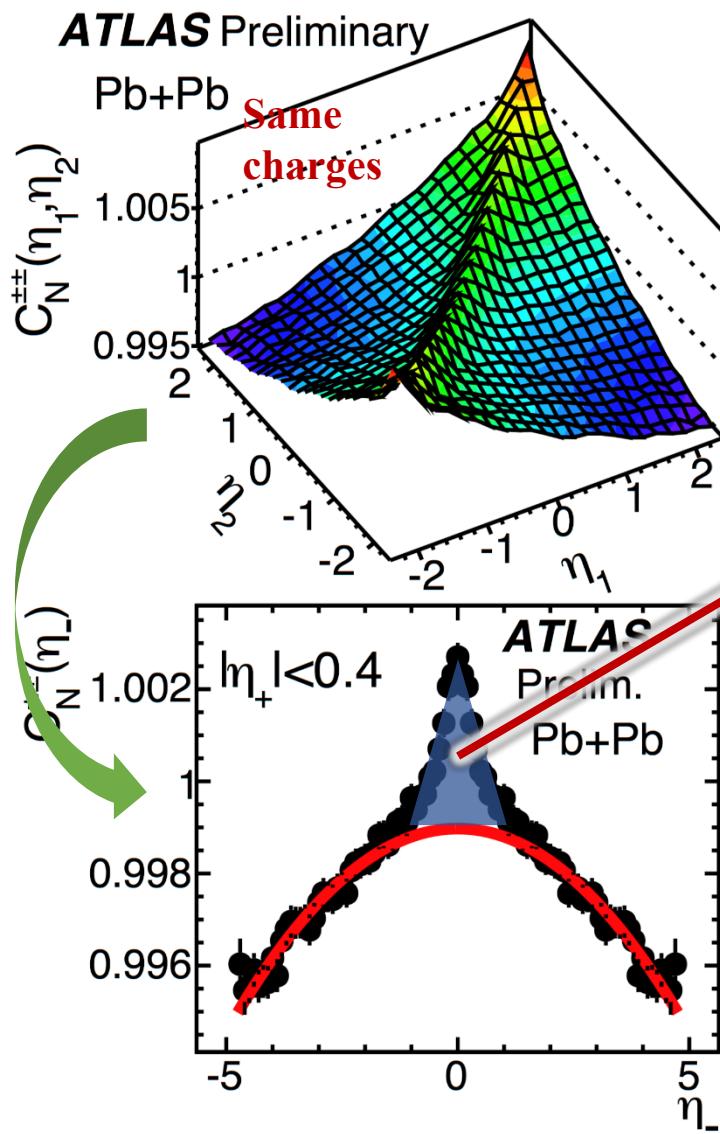
- Particles from the same source (SRC) have strong charge dependence.



- Ratio of opposite to same charges $R(\eta_1, \eta_2)$
 - Very strong Gaussian-like SRC;
 - Very weak LRC: charge-independent;
- Amplitude of $R(\eta_1, \eta_2)$ along η_+ : $f(\eta_+)$, reflects the strength of SRC in the longitudinal direction;
- Assumption: strength of SRC along η_+ is same for same charge and opposite charge.

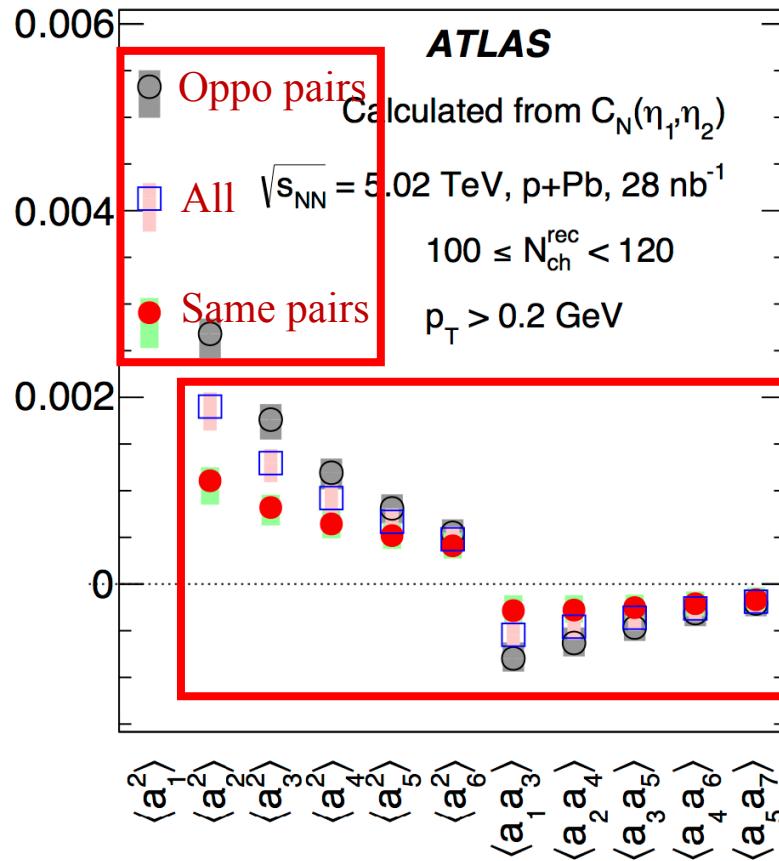


- To estimate SRC, LRC pedestal is estimated first.



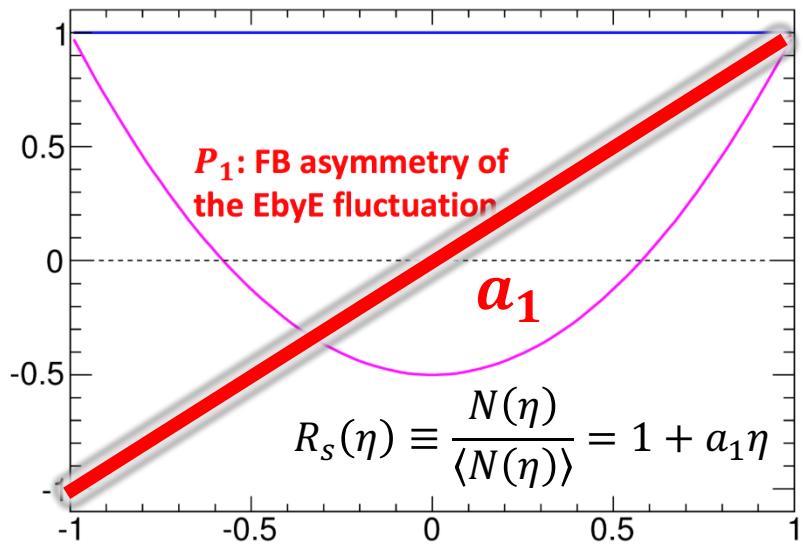
- $C(\eta_1, \eta_2)$ from same charge used to estimate LRC pedestal because of small SRC;
- LRC pedestal is fitted with quadratic function;
- The additional structure upon LRC pedestal determines the shape of SRC;
- The full $\delta_{SRC}(\eta_1, \eta_2)$ is then populated using $f(\eta_+)$ scaling.

Before SRC removal

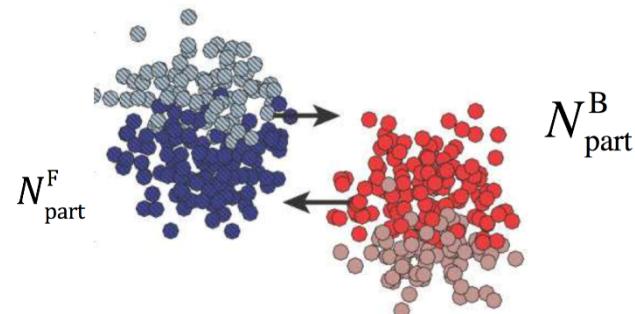
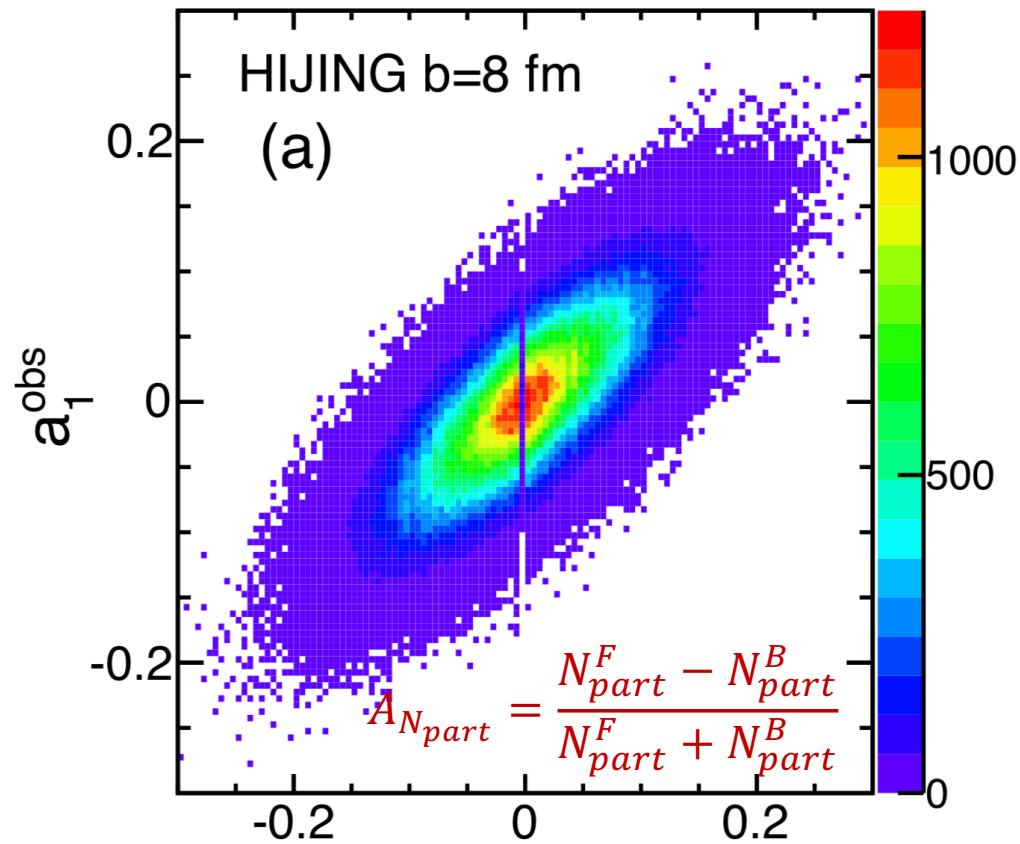


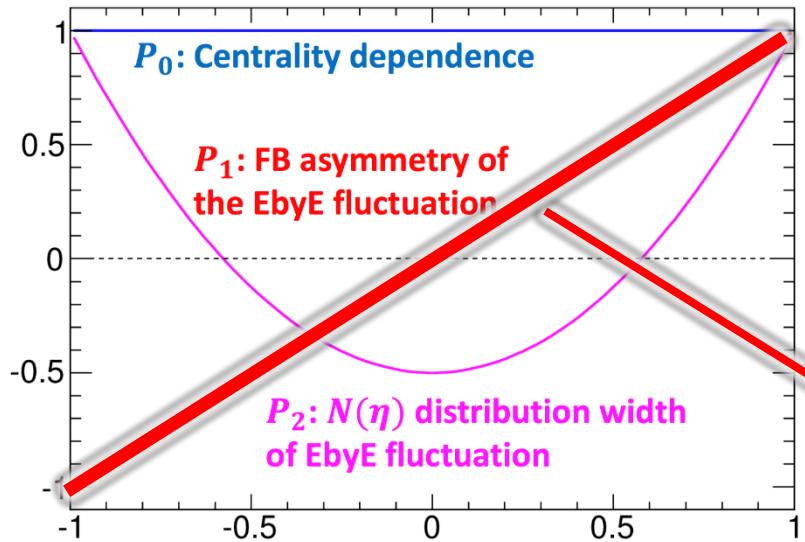
- Higher order coefficients observed;
- Coefficients have charge dependent;
- Results hard to interpret: due to SRC!

- Simpler picture after SRC removal!
- LRC dominated by linear fluctuation;
- LRC is charge independent.



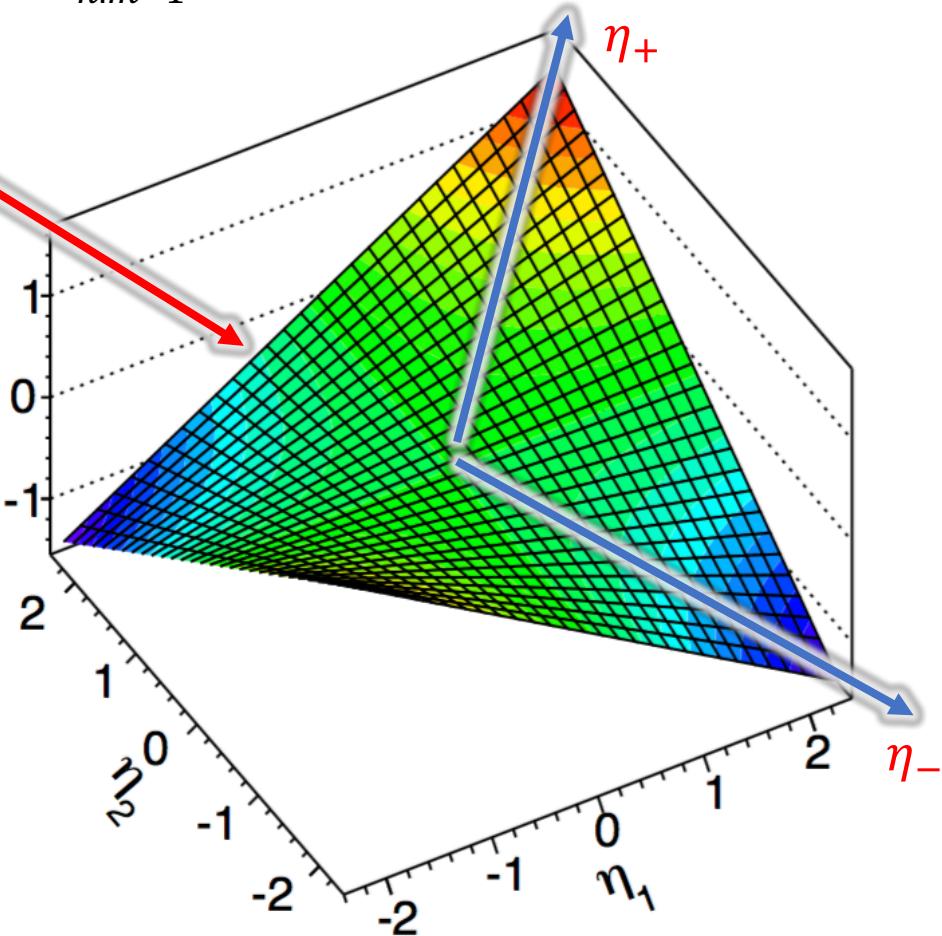
- The linear shape quantifies the FB multiplicity asymmetry;
- HIJING shows strong correlation between final multiplicity asymmetry and initial participant asymmetry;
- As will be shown later, this component dominates the shape fluctuation.





- Expansion of correlation function $C_N(\eta_1, \eta_2)$

$$1 + \sum_{n,m=1}^{\infty} \langle a_n a_m \rangle \frac{T_n(\eta_1)T_m(\eta_2) + T_n(\eta_2)T_m(\eta_1)}{2}$$



- If linear shape dominates:

$$C_N(\eta_1, \eta_2) = 1 + \langle a_1^2 \rangle \eta_1 \eta_2$$

- Expressed as η_+ and η_- :

$$C_N(\eta_1, \eta_2) = 1 + \frac{\langle a_1^2 \rangle}{4} (\eta_+^2 - \eta_-^2)$$

Results: correlation function

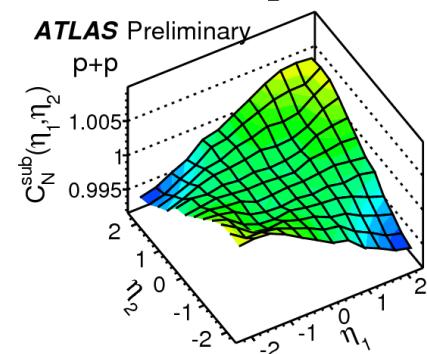
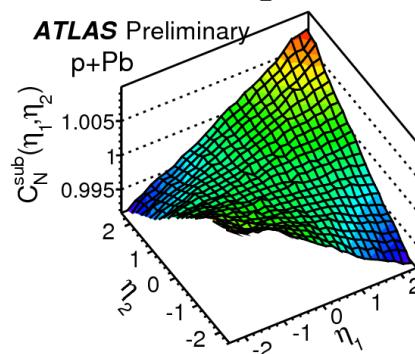
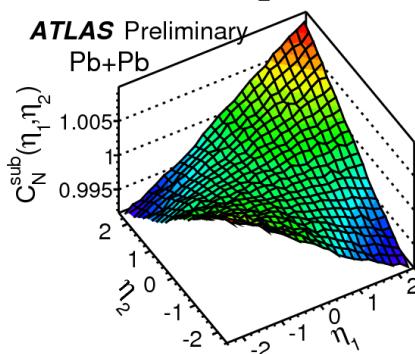
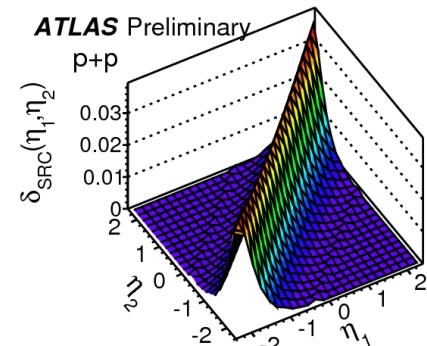
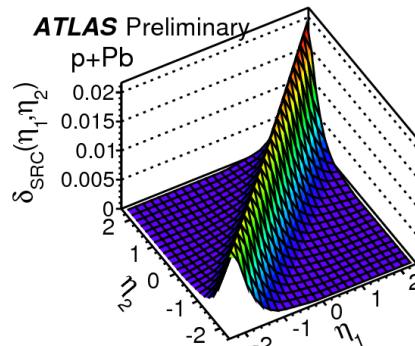
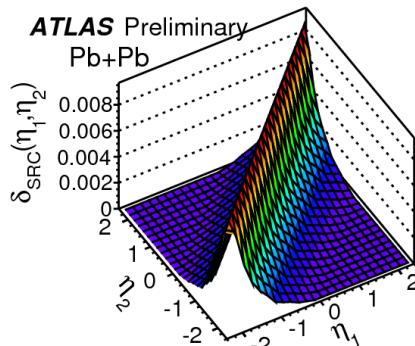
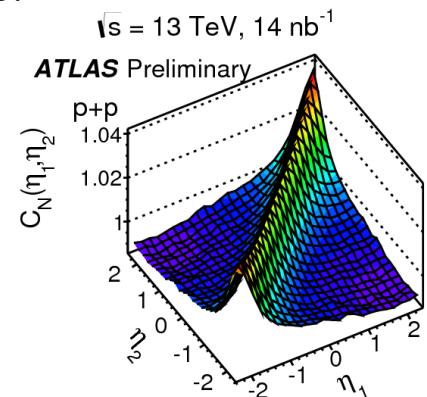
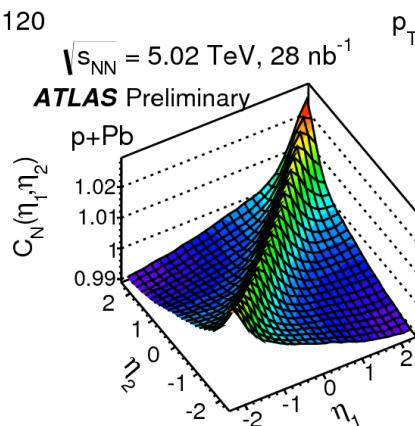
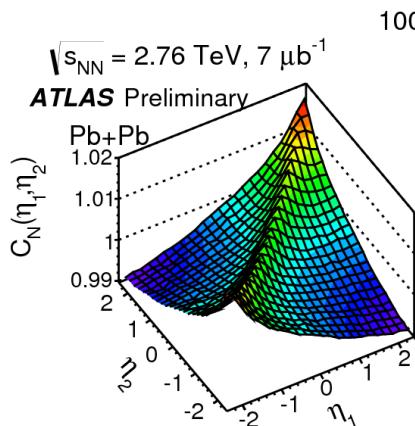
Raw
 $C_N(\eta_1, \eta_2)$

||

Short-range
 $\delta_{SRC}(\eta_1, \eta_2)$

+

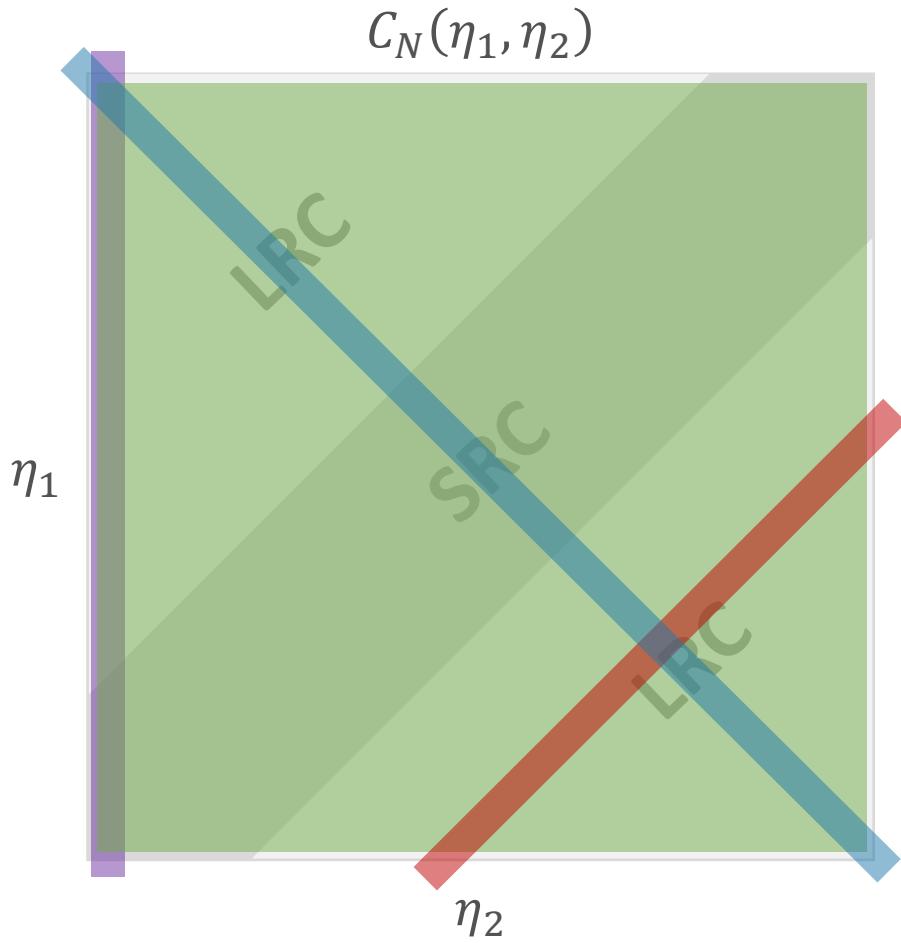
Long-range
 $C_N^{sub}(\eta_1, \eta_2)$



Pb+Pb

p+Pb

pp



- Four methods have different responses of the analysis procedures, and are largely independent.

- Expansion of $C_N^{sub}(\eta_1, \eta_2)$

$$C_N^{sub}(\eta_1, \eta_2) = 1 + \langle a_1^2 \rangle \eta_1 \eta_2$$

- Quadratic fit along $C_N^{sub}(\eta_-)$

$$C_N^{sub}(\eta_-) = 1 + \frac{\langle a_1^2 \rangle}{4} (\eta_+^2 - \eta_-^2)$$

- Quadratic fit along $C_N^{sub}(\eta_+)$

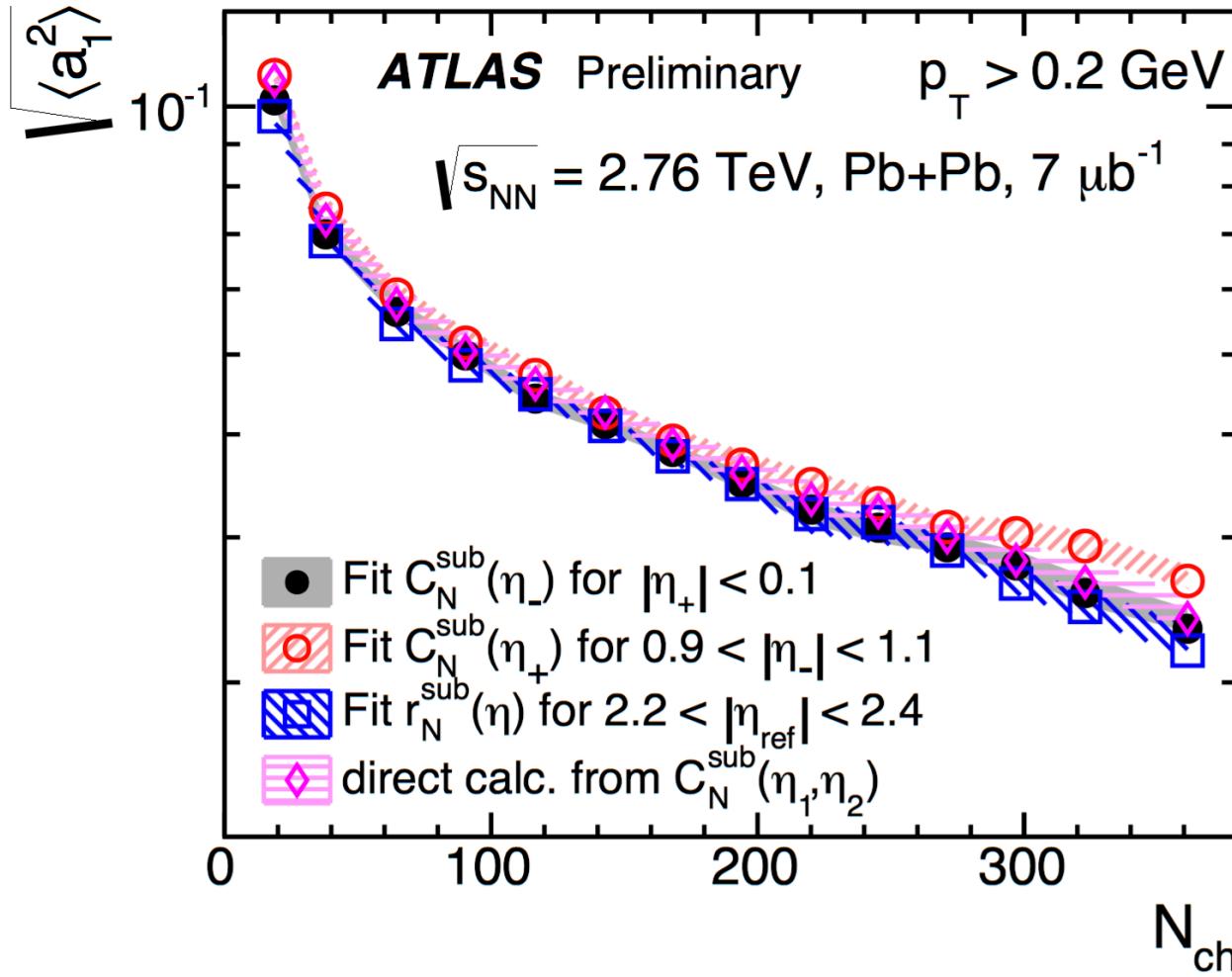
$$C_N^{sub}(\eta_+) = 1 + \frac{\langle a_1^2 \rangle}{4} (\eta_+^2 - \eta_-^2)$$

- Linear fit of $r_N^{sub}(\eta, \eta_{ref}) \equiv \frac{C_N^{sub}(-\eta, \eta_{ref})}{C_N^{sub}(\eta, \eta_{ref})}$

$$r_N^{sub}(\eta, \eta_{ref}) = 1 - 2\langle a_1^2 \rangle \eta \eta_{ref}$$

How stable are the results?

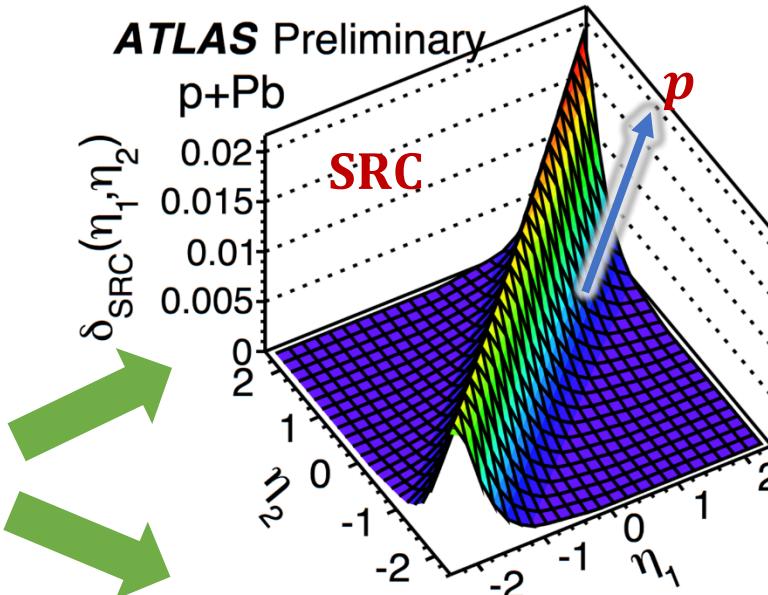
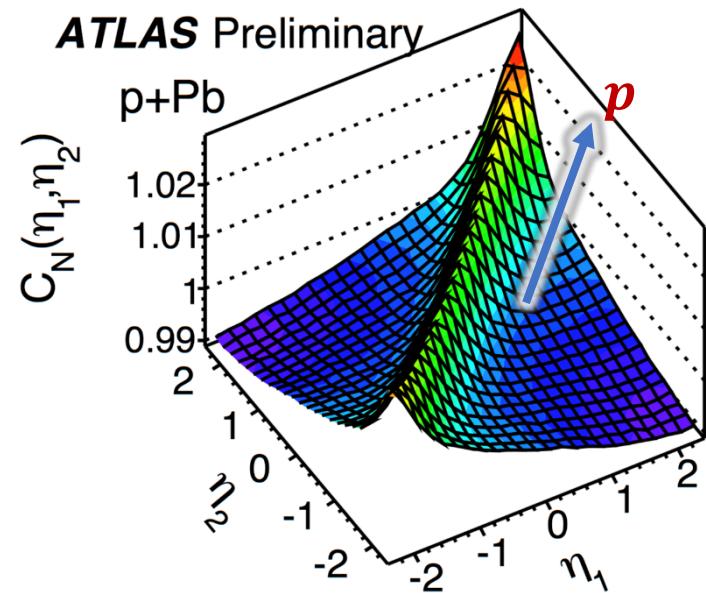
- Four largely independent methods are applied to determine $\langle a_1^2 \rangle$;
- Different methods have different sensitivity to the analysis procedures;



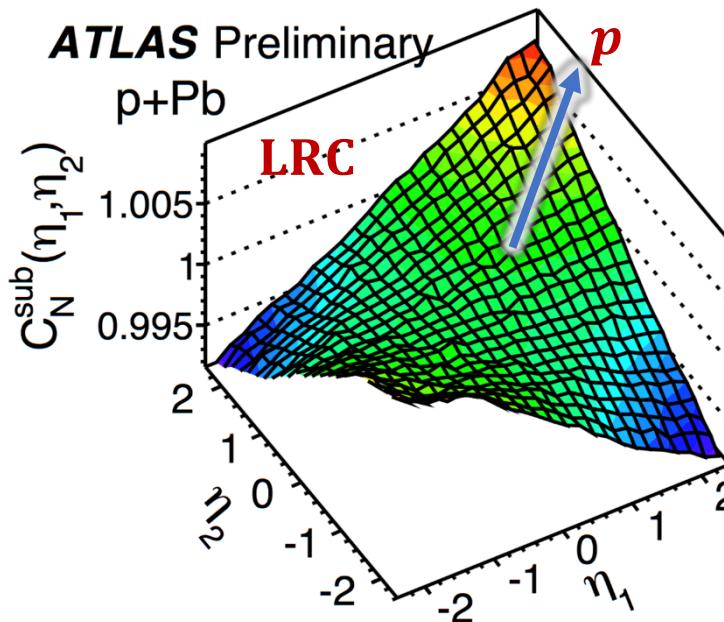
- Four methods give consistent a_1 : conclusions are insensitive to the procedure.

Asymmetry in $p+\text{Pb}$ collision

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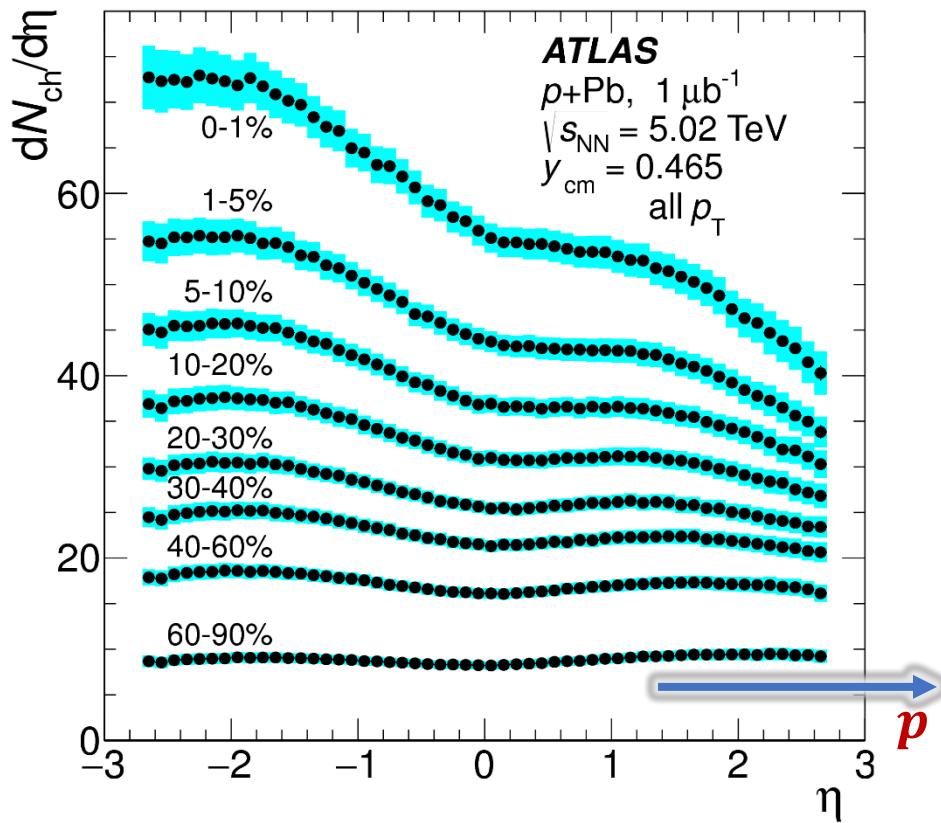
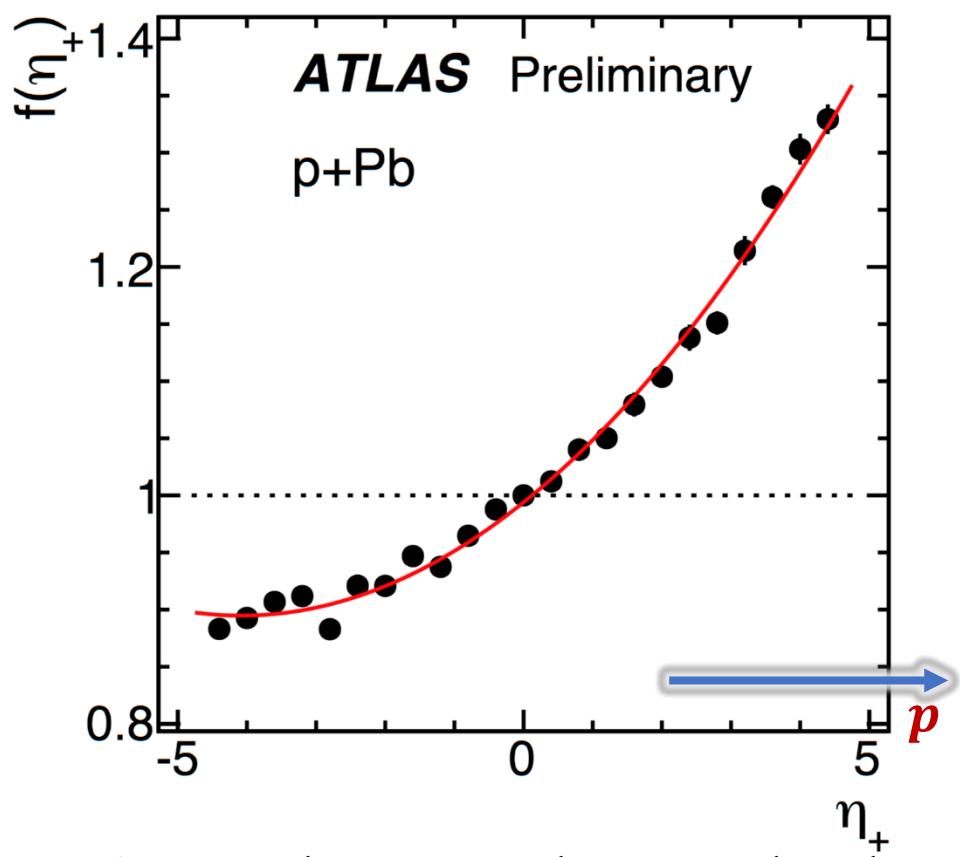


- Asymmetry entirely due to SRC!



- LRC is symmetric.

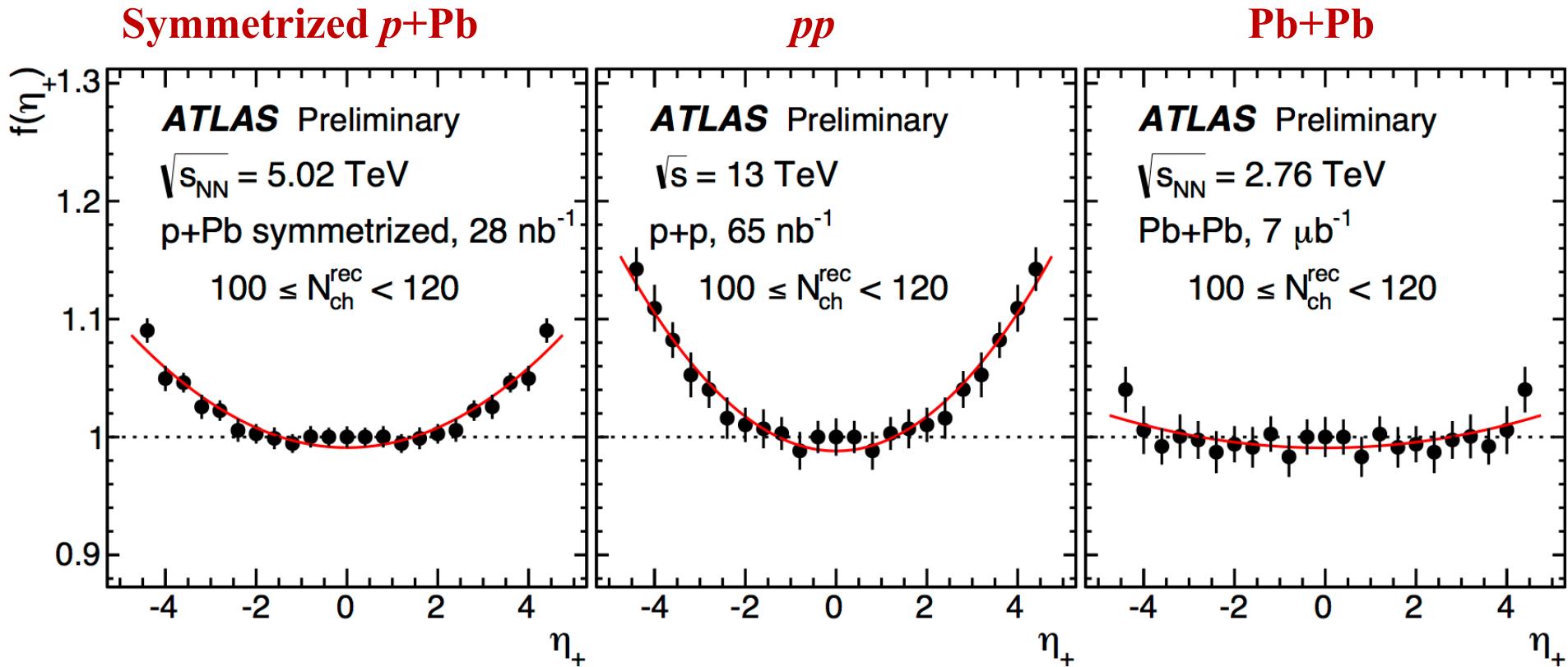
- Asymmetry observed in $p+\text{Pb}$ collision: stronger correlation in the proton-going side.
- Why the asymmetric collision causes asymmetric SRC?



- Assume there are n clusters and each one emits m particles on average;
- Assume n is proportional to local particle density $dN_{\text{ch}}/d\eta$;

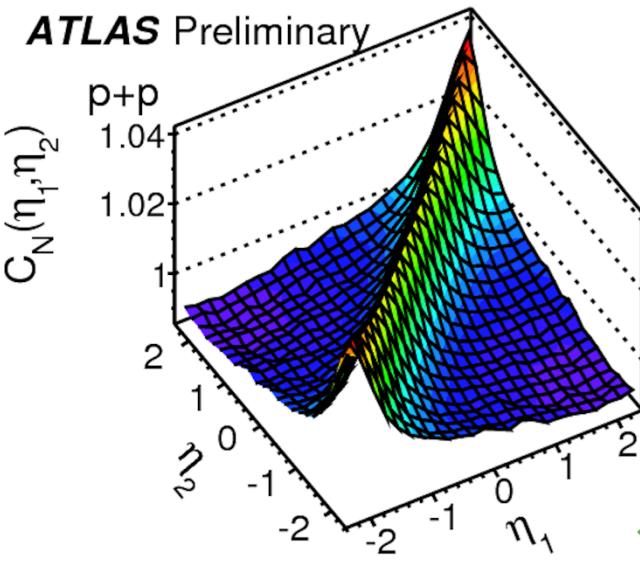
$$\delta_{\text{SRC}} \propto \frac{n \langle m(m-1) \rangle}{(n \langle m \rangle)^2} = \frac{1}{n} \propto \frac{1}{dN_{\text{ch}}/d\eta}$$

Inverse to multiplicity distribution



- For better comparison with pp and $\text{Pb}+\text{Pb}$, $p+\text{Pb}$ is symmetrized;
- In high-multiplicity pp , SRC shape is slightly larger than $p+\text{Pb}$;
- However in $\text{Pb}+\text{Pb}$, SRC shape is more flat.
- EbyE asymmetry of multiplicity (relative to average multiplicity) in high-multiplicity pp is larger than $p+\text{Pb}$ while $\text{Pb}+\text{Pb}$ collision is more symmetric.

Outlook



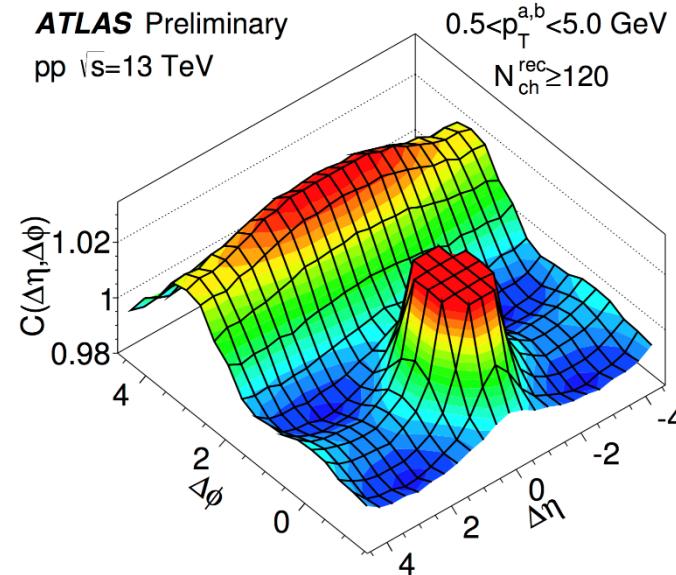
- $C(\eta_1, \eta_2)$ is a very comprehensive observable.

- Reconstruct balance function

$$2B(\Delta\eta) \equiv 2C^{+-}(\Delta\eta) - C^{++}(\Delta\eta) - C^{--}(\Delta\eta)$$

- Test factorization: high- p_T a_n^H and low- p_T a_n^L

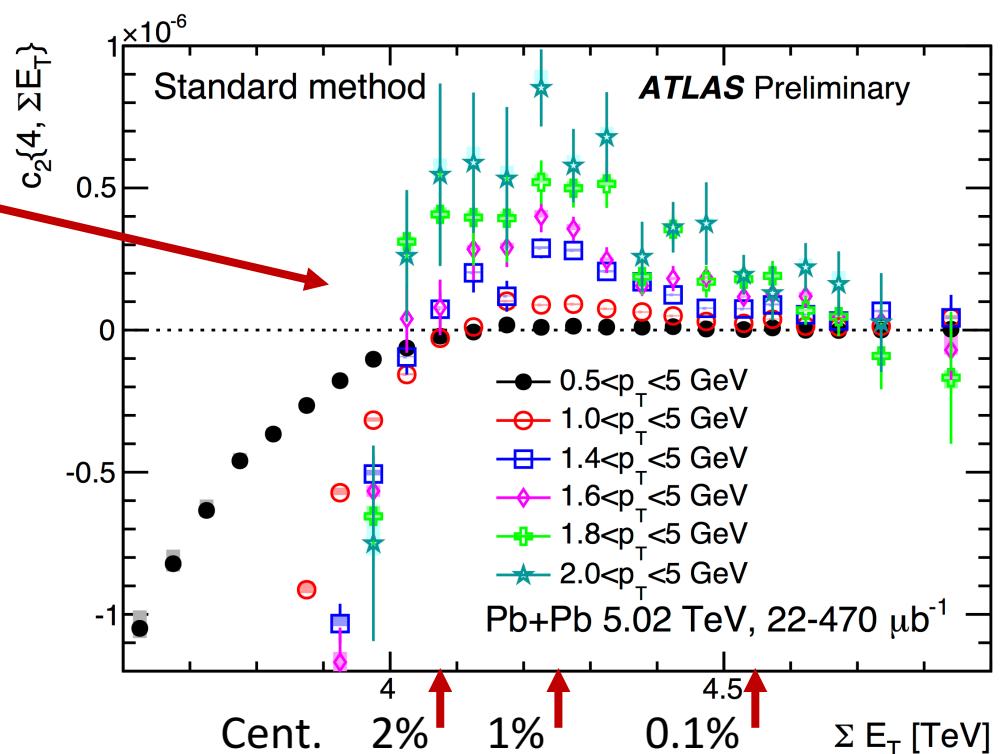
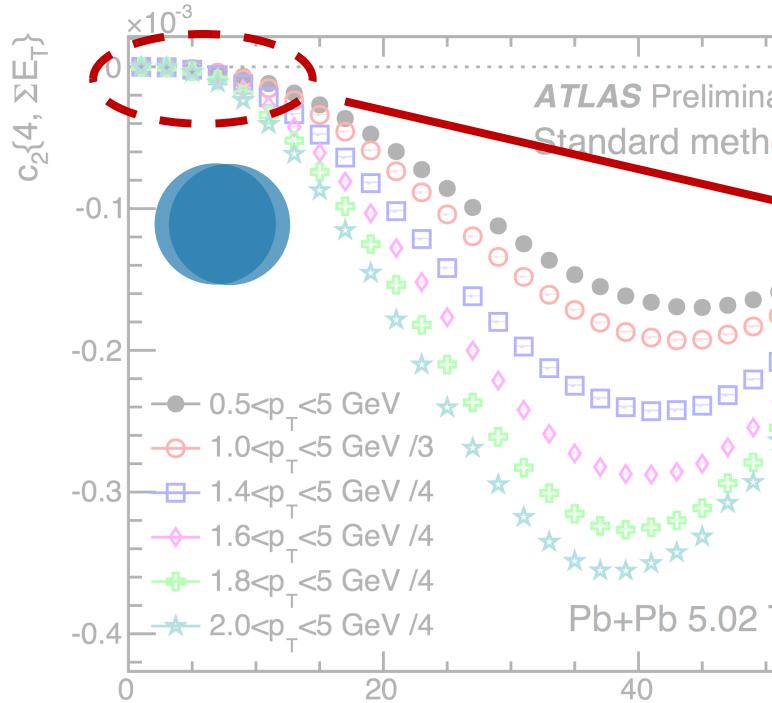
$$r_n \equiv \frac{\langle a_n^H a_n^L \rangle}{\sqrt{\langle a_n^H a_n^H \rangle} \sqrt{\langle a_n^L a_n^L \rangle}}$$



$C(\eta_1, \eta_2)$  $+ C(\Delta\eta, \Delta\phi)$  $C(\eta_1, \eta_2, \Delta\phi) !$

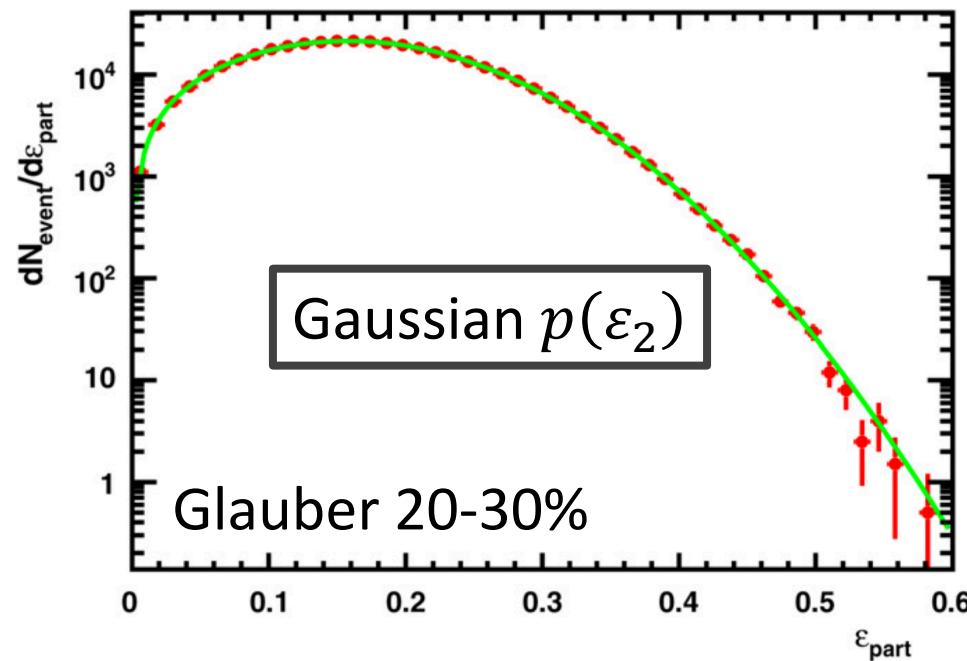
Centrality fluctuation

Ultra-Central Collision (UCC)

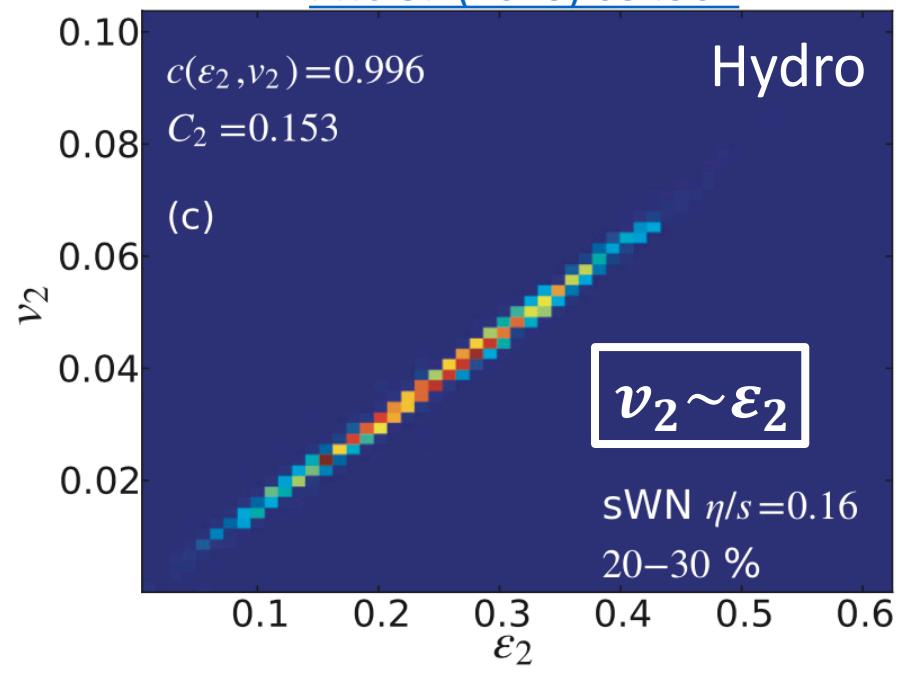


- In UCC: $\bar{v}_2 \rightarrow 0$, largest relative flow fluctuation;
- ATLAS applied UCC triggers: $\times 20$ statistics over MinBias;
- $c_2\{4\} > 0$ in UCC \Rightarrow non-Gaussian flow fluctuation
 - Why?

[PLB 659 \(2008\) 537-541](#)



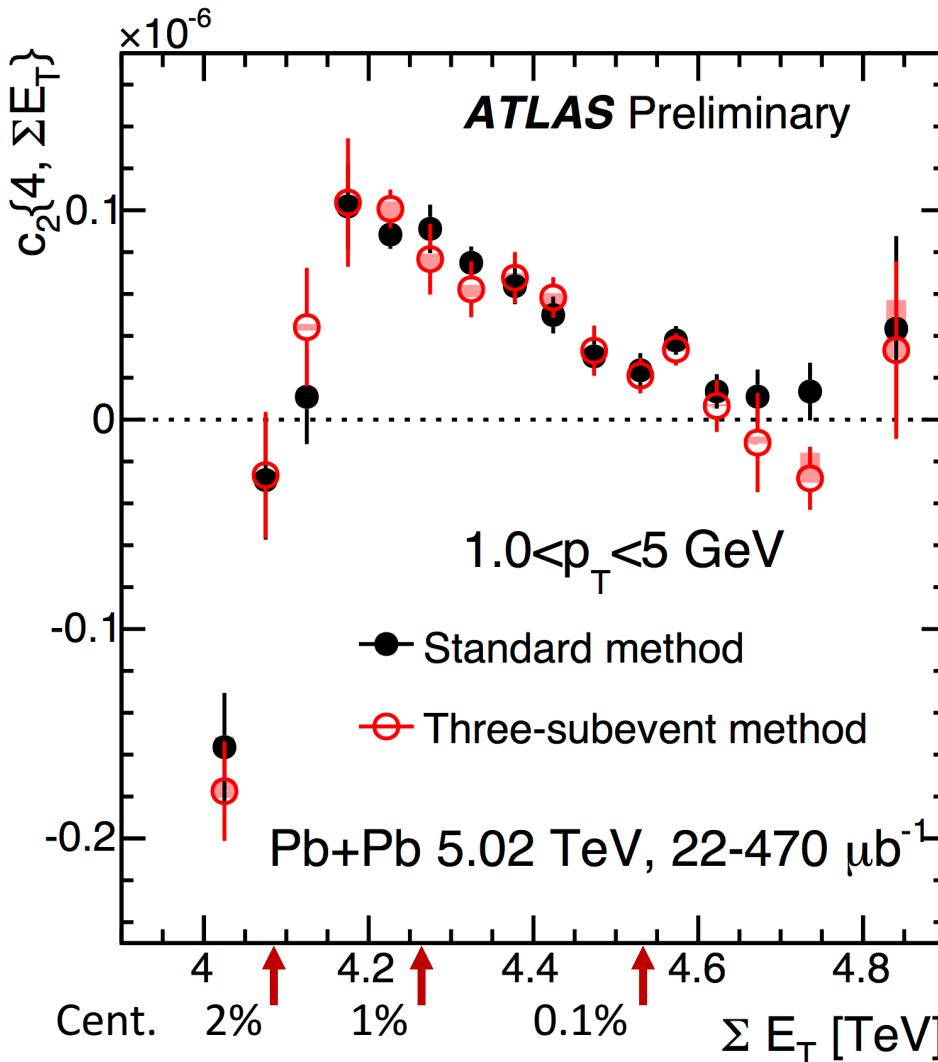
[PRC 87 \(2013\) 054901](#)



- On the model side
 - Gaussian $p(\varepsilon_2) \Rightarrow$ Gaussian $p(v_2) \Rightarrow c_2\{4\} \leq 0$
- But we observed $c_2\{4\} > 0$
 - Non-flow contribution?

$$v_n\{4\} = \bar{v}_n = \sqrt[4]{-c_n\{4\}}$$

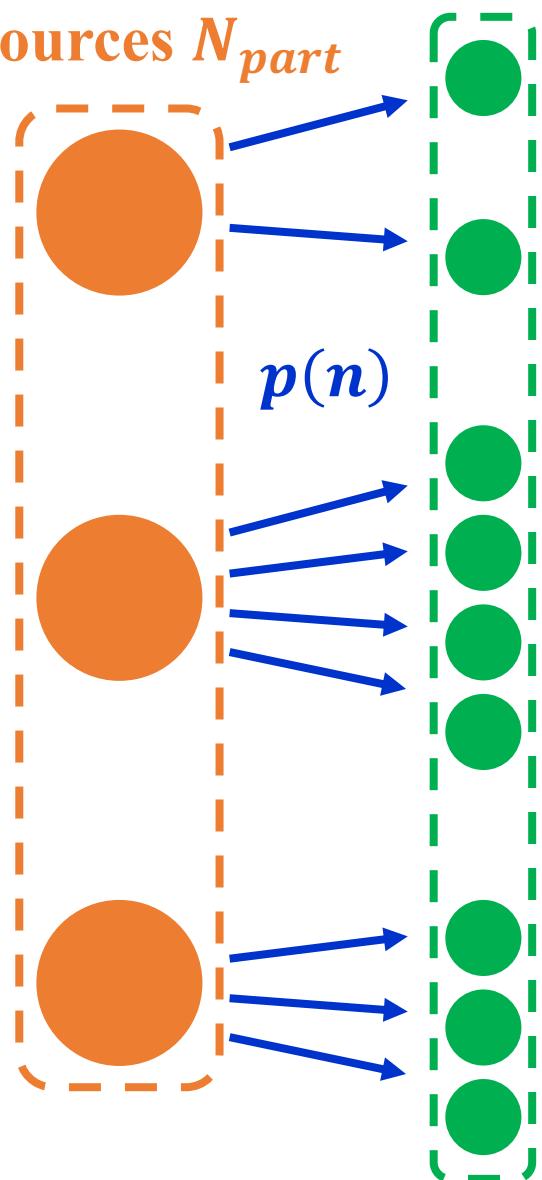
Non-flow contribution?



- Two methods consistent: **not due to non-flow**.
- Pileup effects have also been suppressed.

Initial stage

sources N_{part}



Final stage

particles N_{ch}

Not detector effect!

- Fluctuation of particle production $p(n)$
 - Same N_{part} \Rightarrow different N_{ch}
 - Same N_{ch} \Rightarrow different N_{part}
- In the experiment
 - First calculate $Obs(N_{ch})$
 - Then map to $\langle N_{part} \rangle$
- Flow is driven by initial stage N_{part}
- $Obs(\langle N_{part} \rangle)$ introduces CF
- CF affects all fluctuation measurements, but never been studied in flow

$$c_n\{4\} \equiv \langle\langle 4 \rangle\rangle - 2\langle\langle 2 \rangle\rangle^2$$

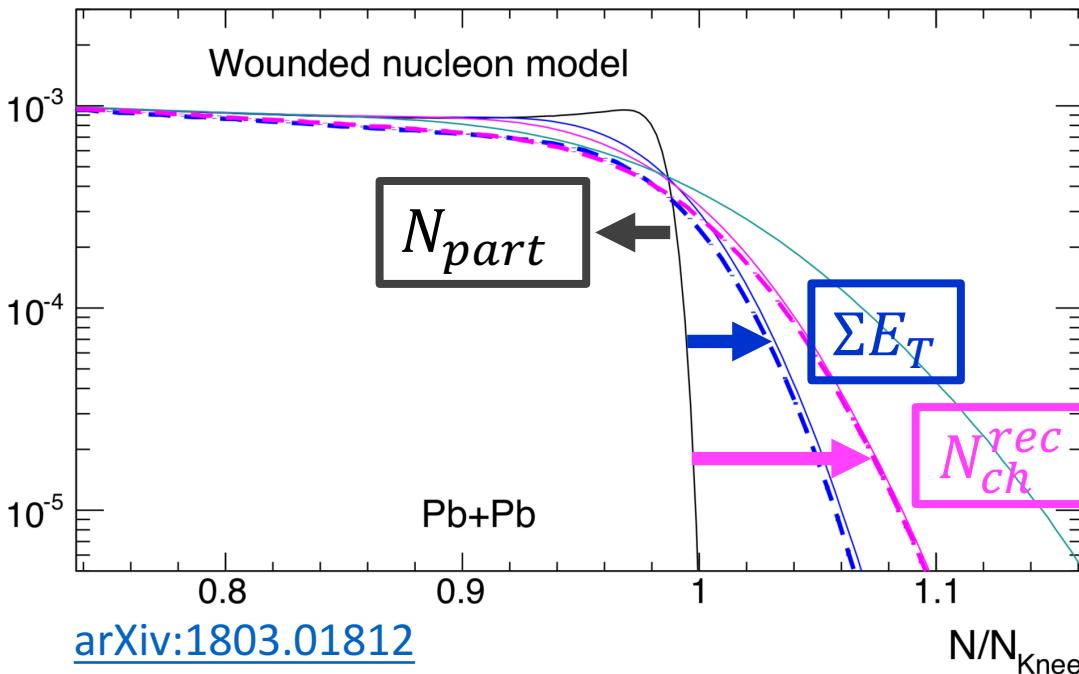
Calculated
event-by-event

Averaged over many events

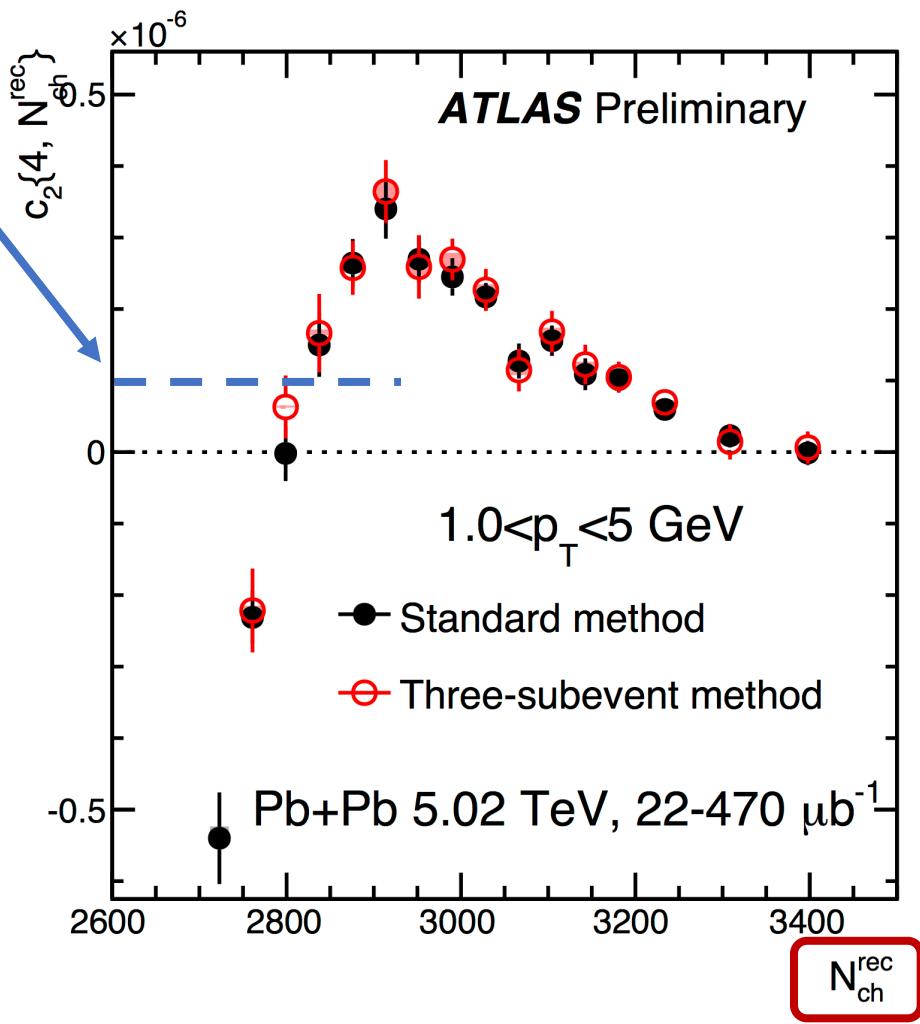
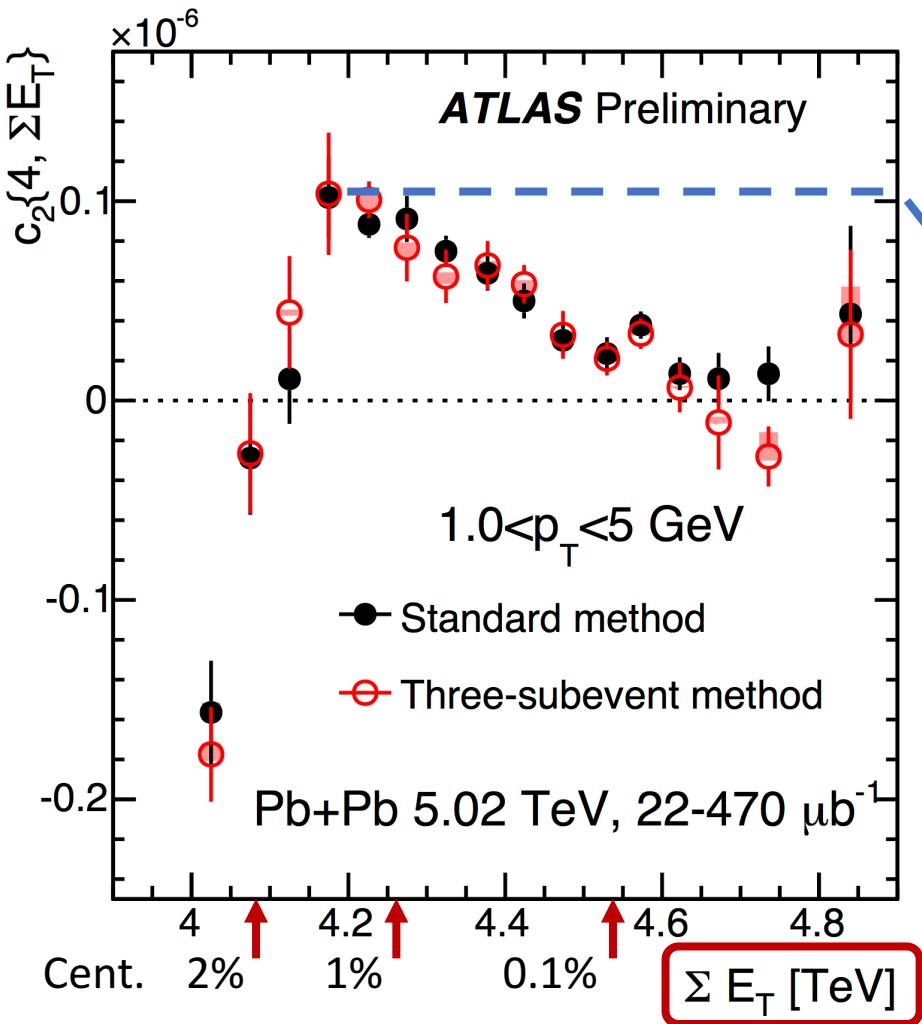
Binning defined by	Observable
FCal: $3.2 < \eta < 4.9$	$c_2\{4, \Sigma E_T\}$
ID: $ \eta < 2.5, p_T$ cut	$c_2\{4, N_{ch}^{rec}\}$

- Particle production depends on η

Test relative CF by comparing $c_2\{4\}$ binned by ΣE_T and N_{ch}^{rec}



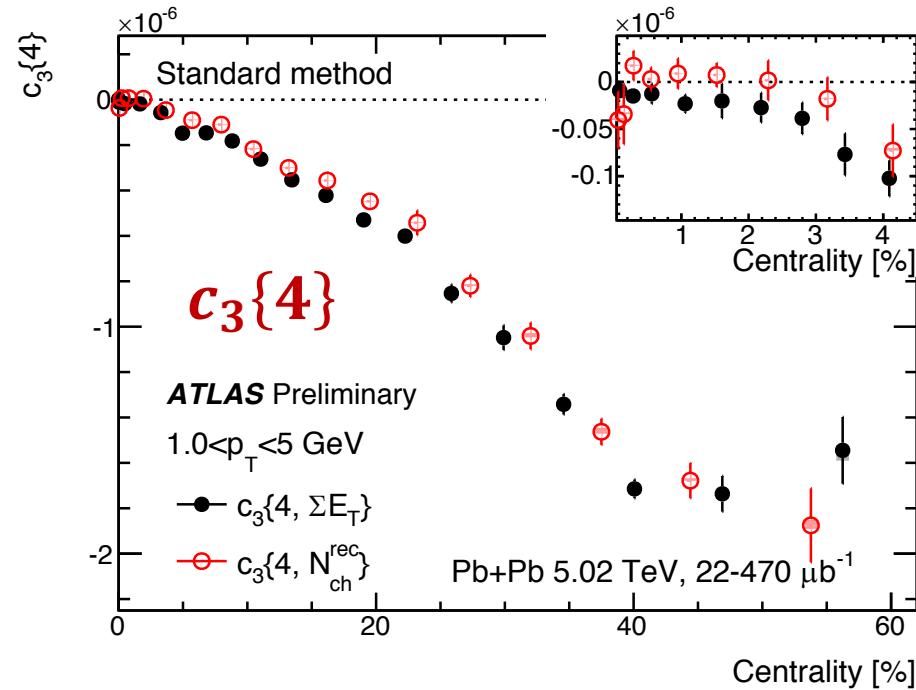
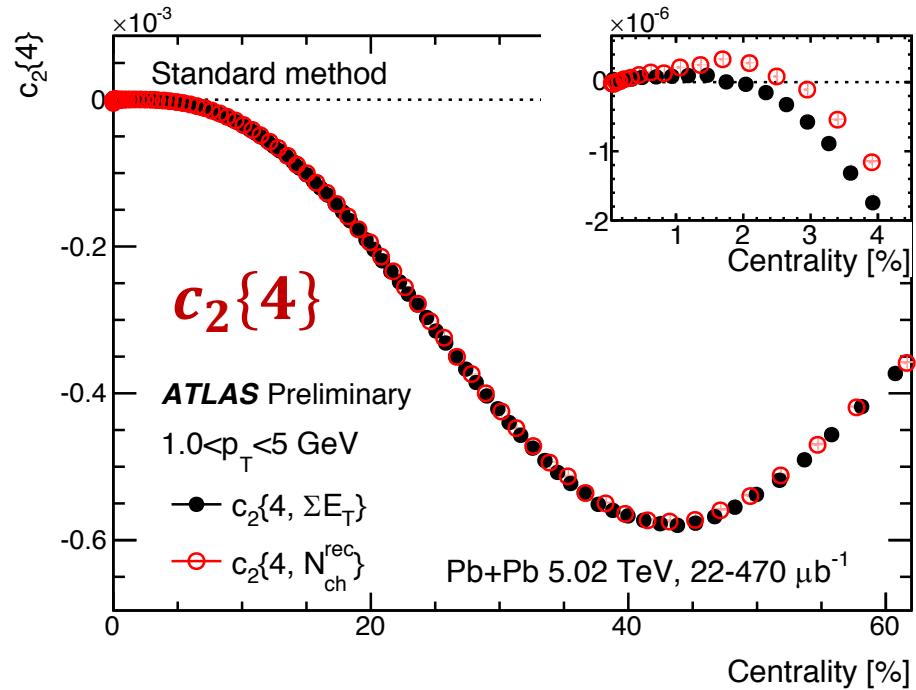
- $p(N_{ch}^{rec})$ broader than $p(\Sigma E_T)$
- CF effect: $\Sigma E_T < N_{ch}^{rec}$
- Prediction
 - $c_2\{4, \Sigma E_T\} < c_2\{4, N_{ch}^{rec}\}$



- $c_2\{4, \Sigma E_T\} < c_2\{4, N_{\text{ch}}^{\text{rec}}\}$: CF affects flow cumulant;
- $c_2\{4\} \rightarrow 0$ in very most-central: smaller CF effect;

From ultra-central to full centrality

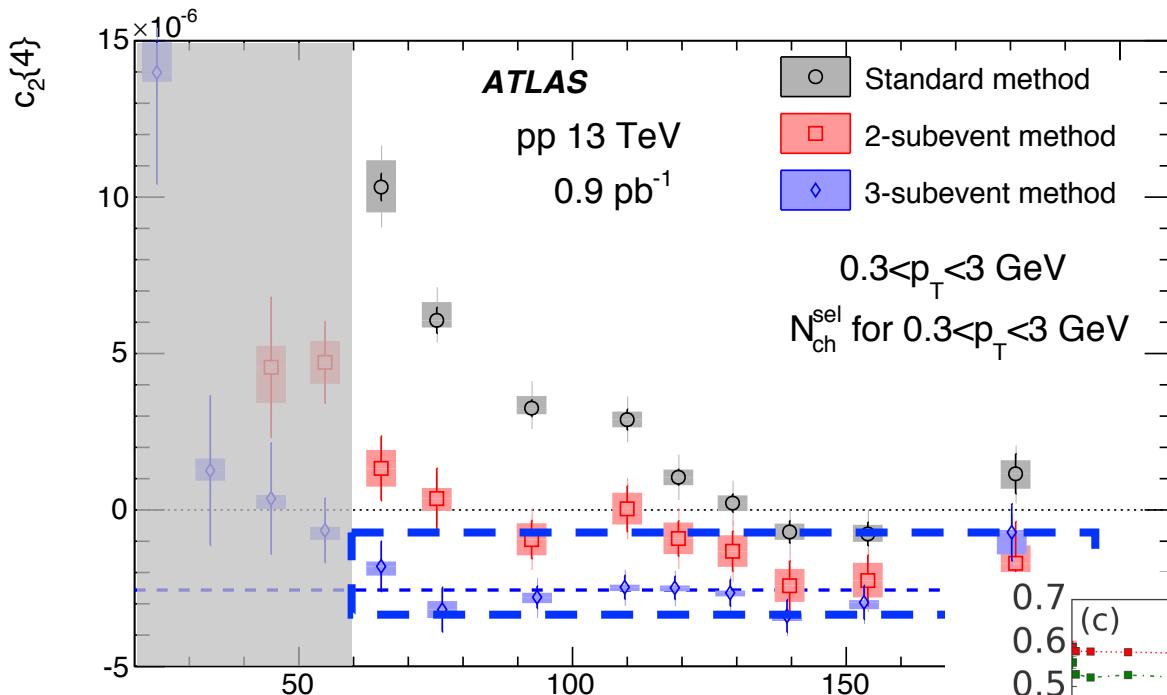
70



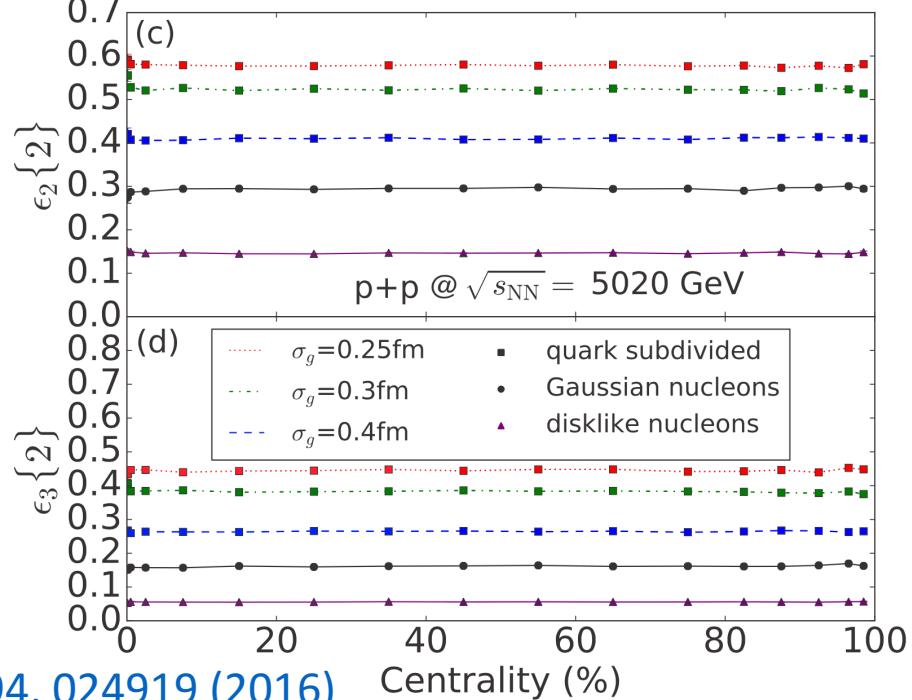
- $c_2\{4\}$: CF mostly affects central;
- $c_3\{4\}$: CF affects most centralities.

Last puzzle: N_{ch} dependence

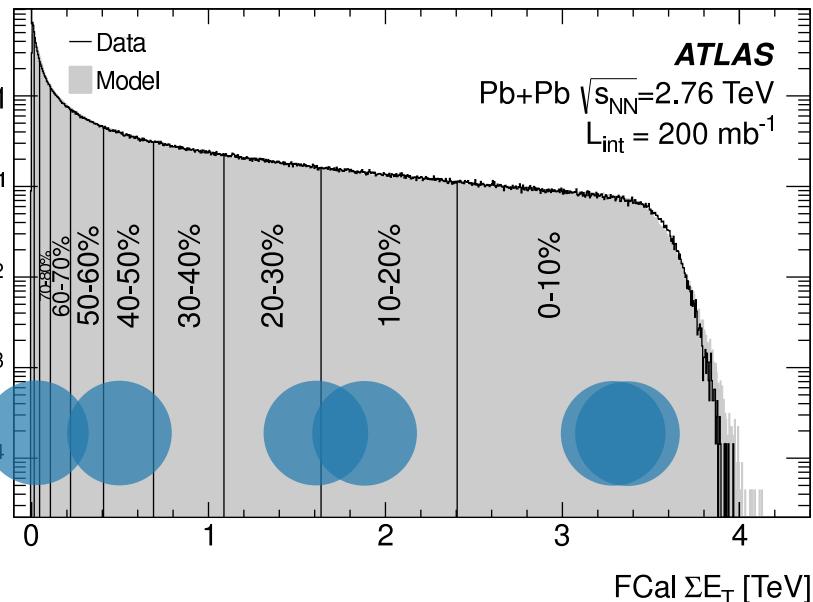
71



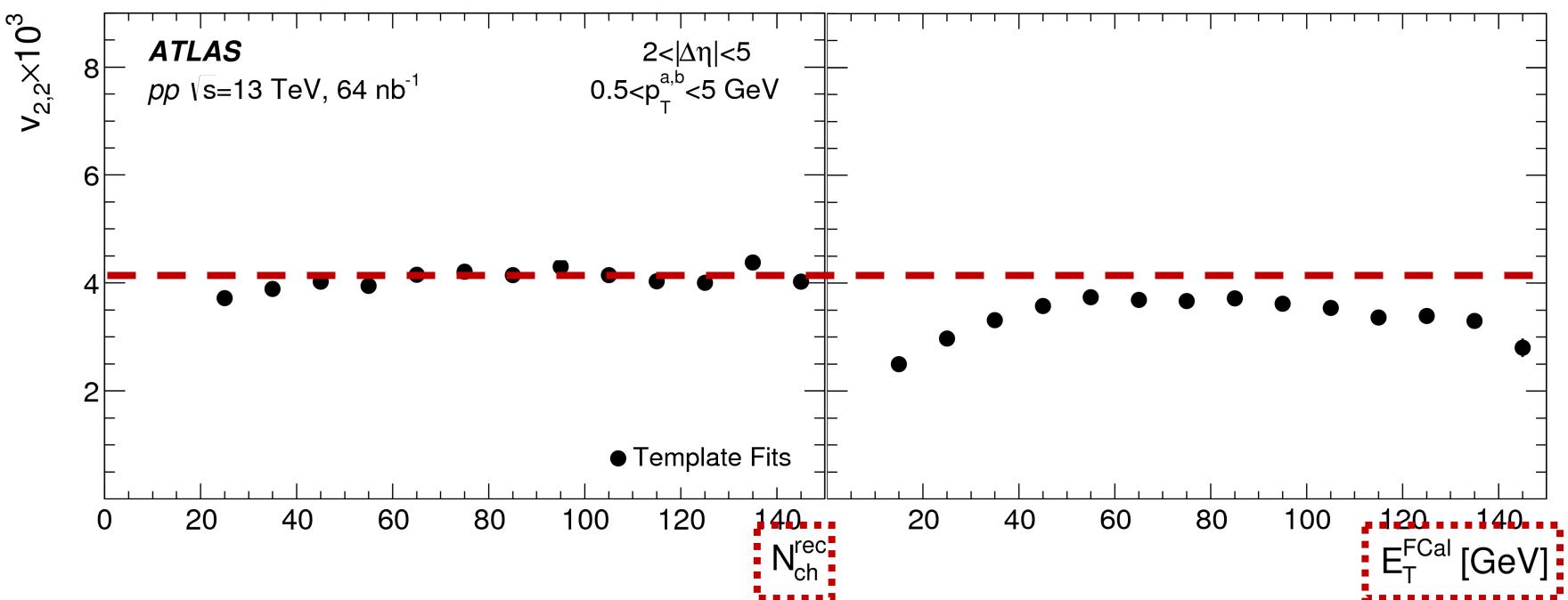
- Weak independence of N_{ch} ;
- Similar observation in model
 - No “geometry” in pp ?
 - N_{ch} not a good indicator for centrality?



Centrality fluctuation

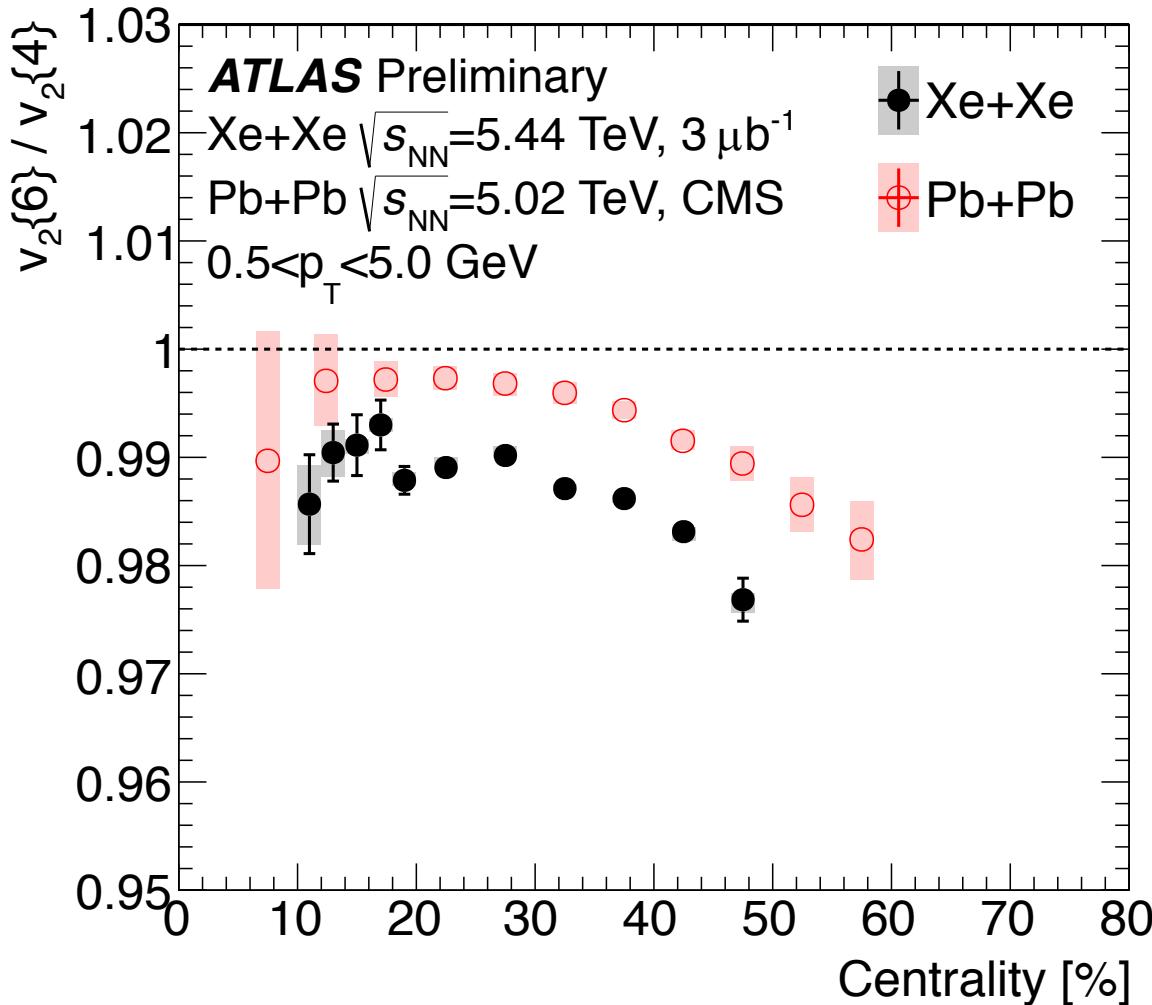


- Centrality quantifies the overlap region of the collision;
- The mapping replies on model and is on the average level;
- Different centrality definitions gives different dependence.



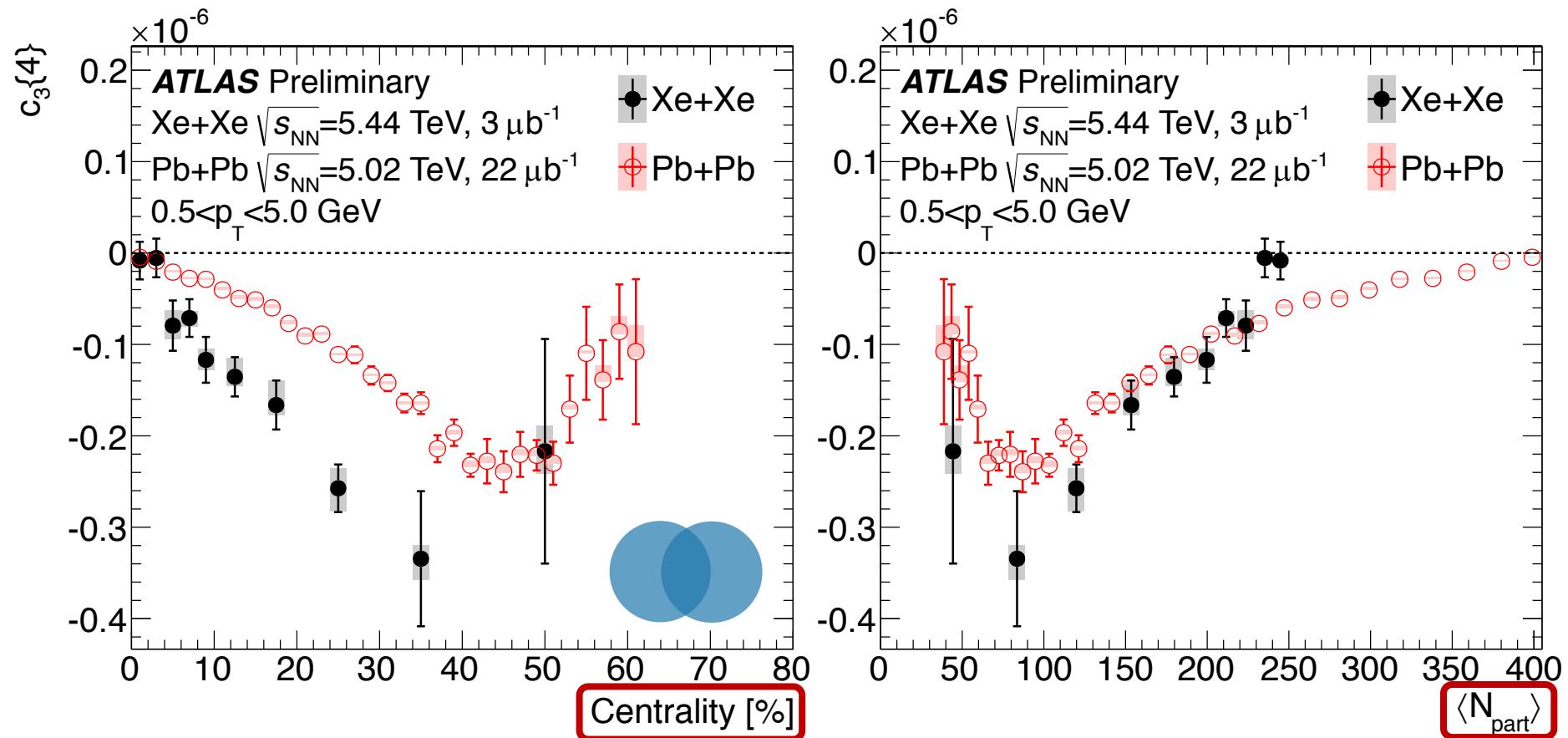
Comparison between Pb+Pb and Xe+Xe

Xe+Xe and Pb+Pb: v_2



- Mass number of Xe is halfway of Pb and p ;
- If $v_2 \sim \text{Gauss}(\bar{v}_n, \delta_n)$: $v_2\{6\}/v_2\{4\} = 1$
- v_2 in Xe+Xe deviates further from Gauss: deformed nucleus?

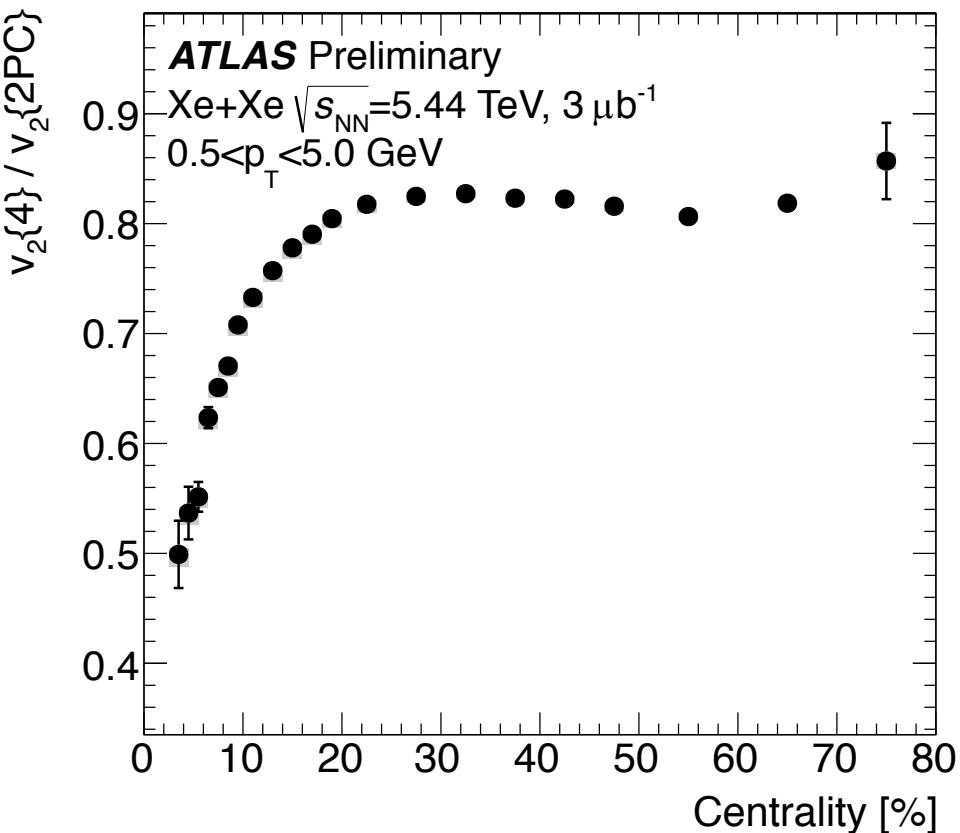
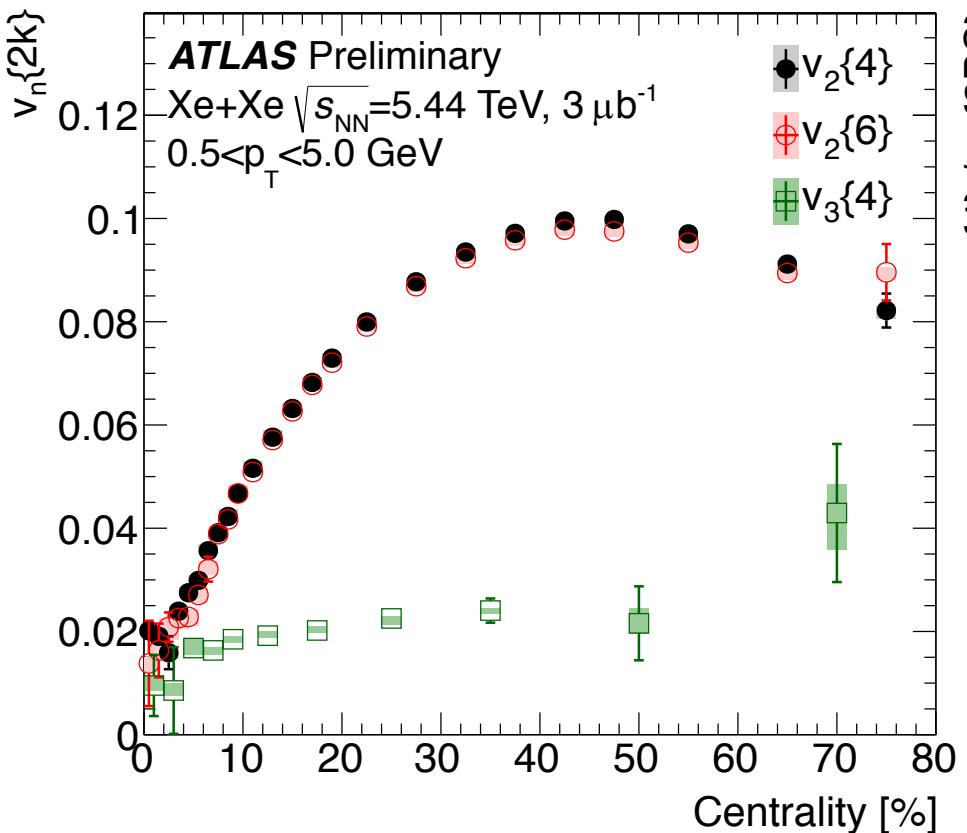
Xe+Xe and Pb+Pb: v_3

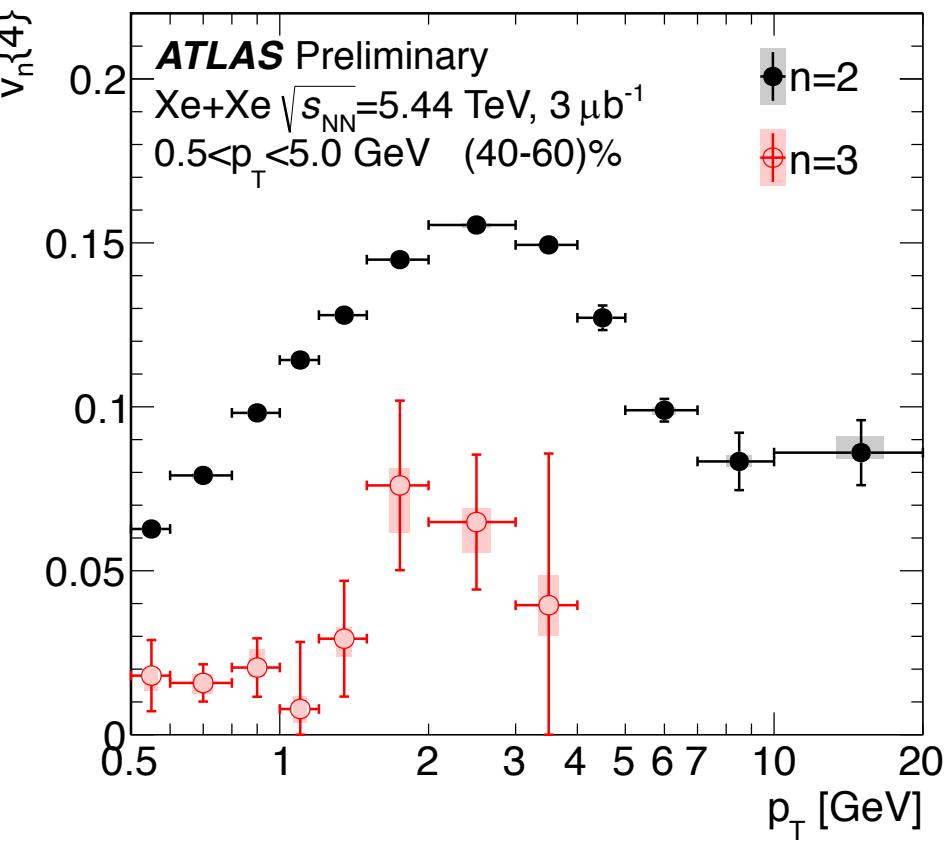
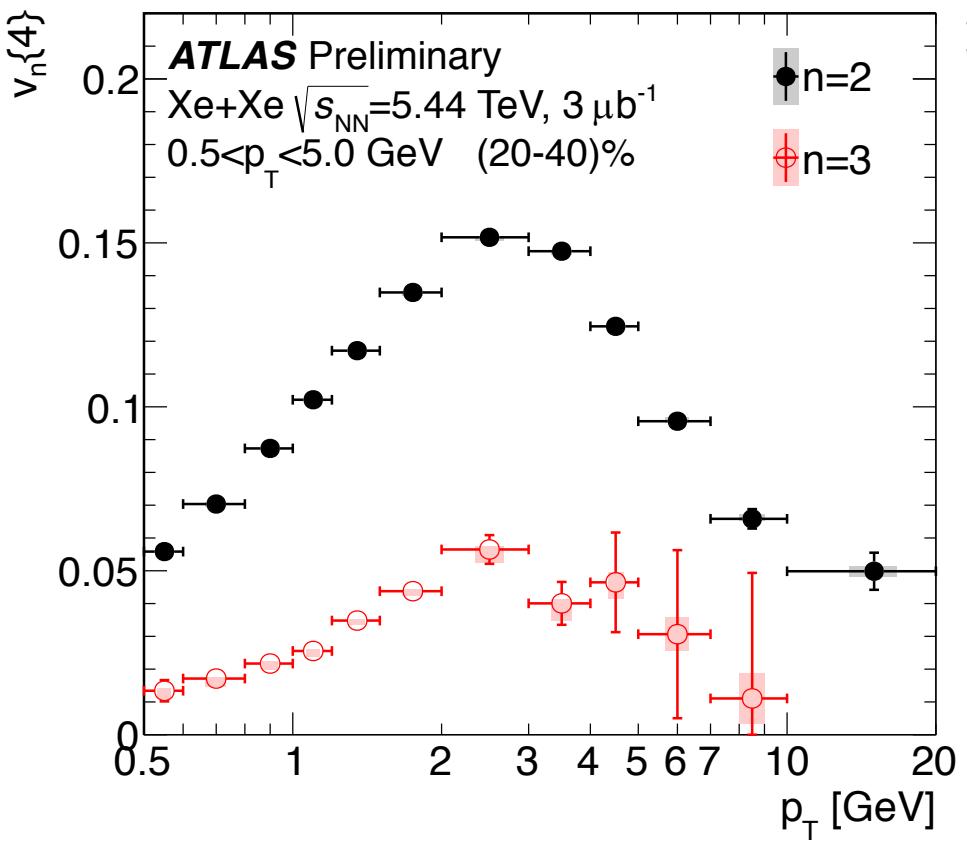


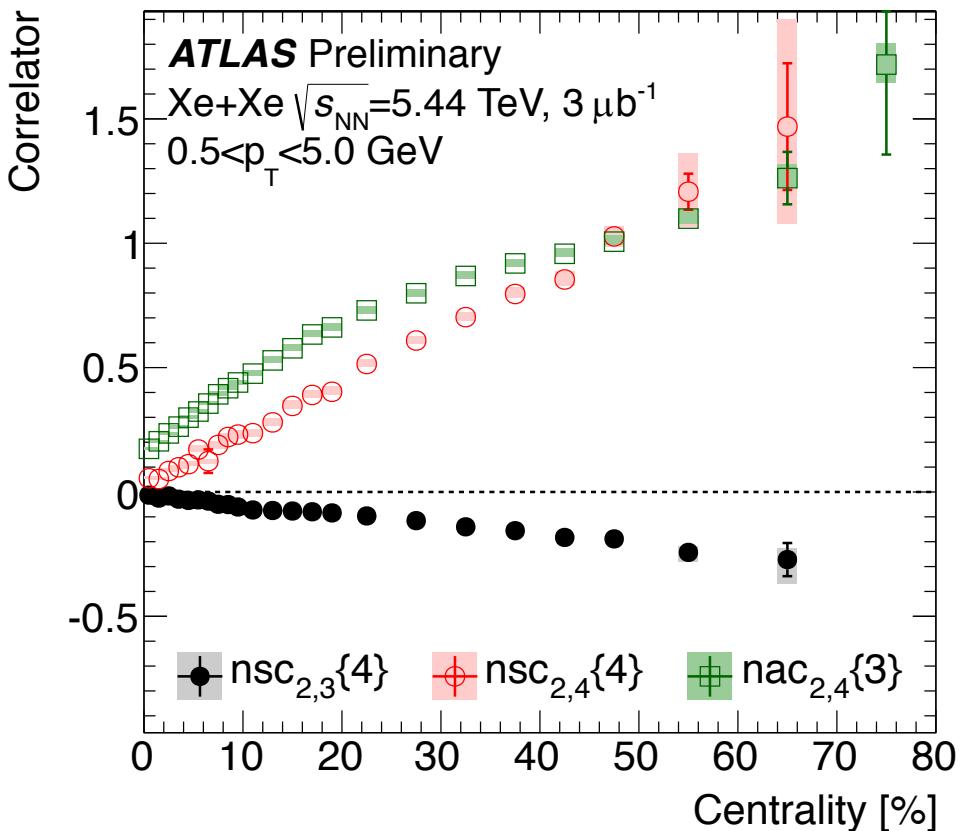
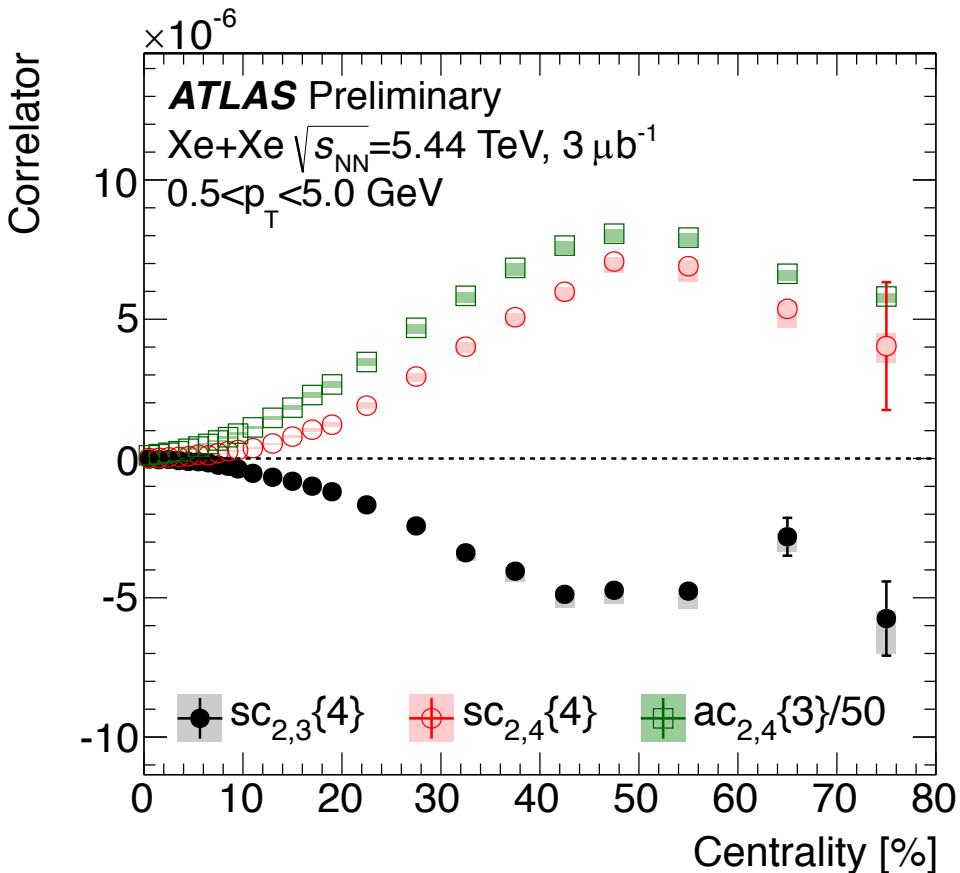
- $c_3\{4\}$ doesn't scale with centrality between Xe and Pb
 - No avg. geometry for v_3 ;
- $c_3\{4\}$ scales with $\langle N_{part} \rangle$
 - Fluctuation driven by # of sources N_{part}
 - Similar observation for $c_4\{4\}$ (see backup)

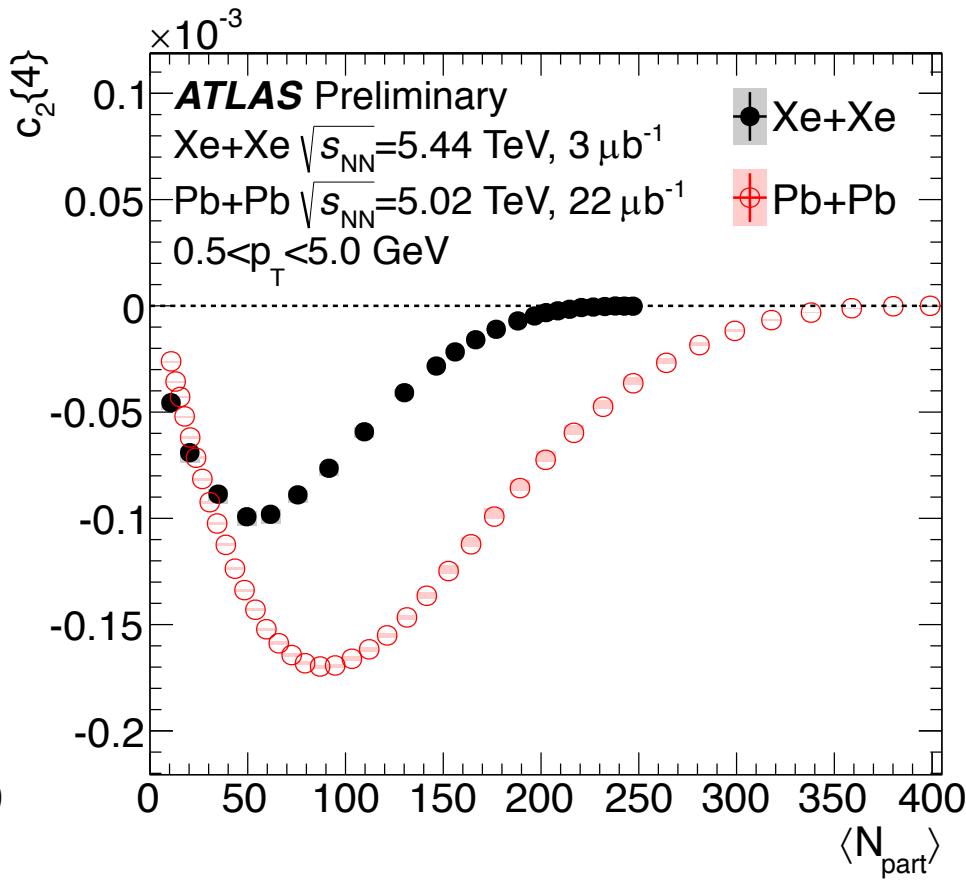
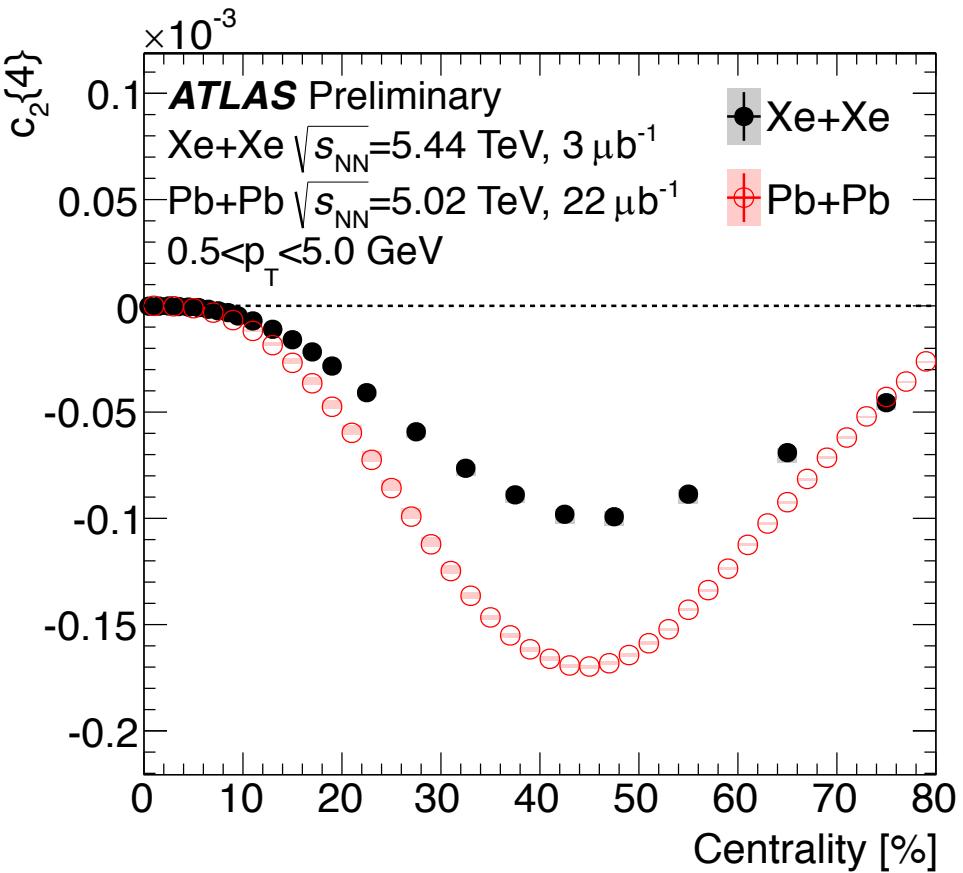
Multi-particle cumulant

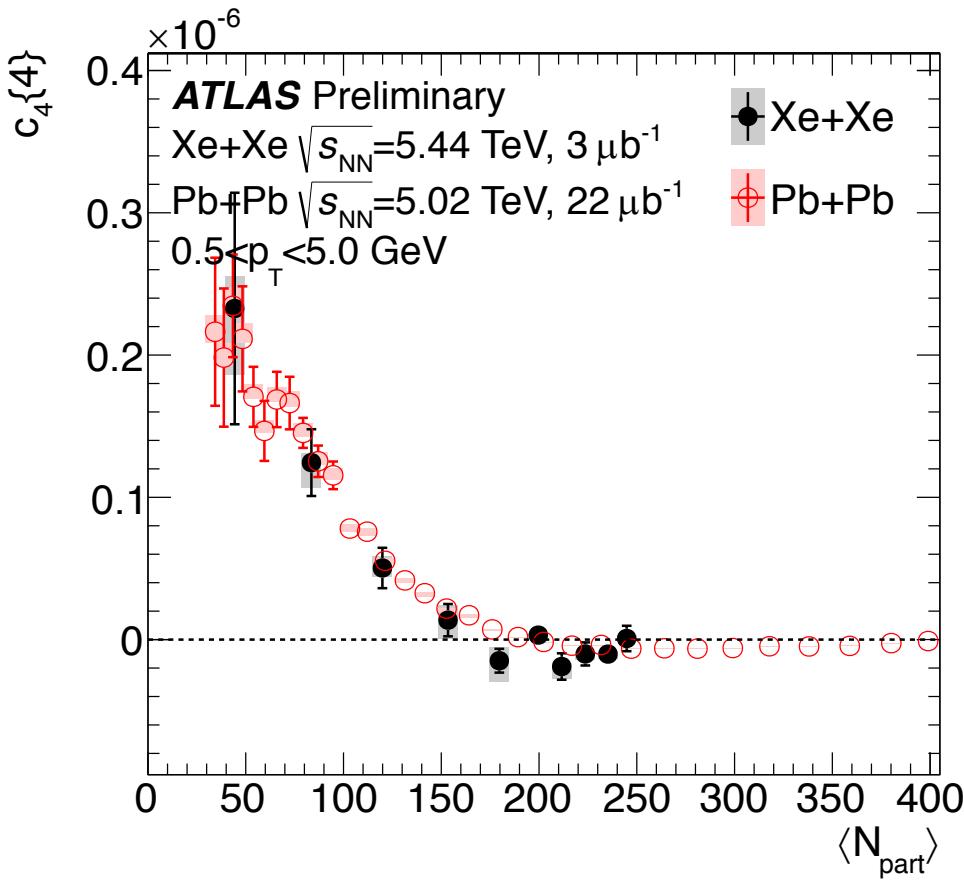
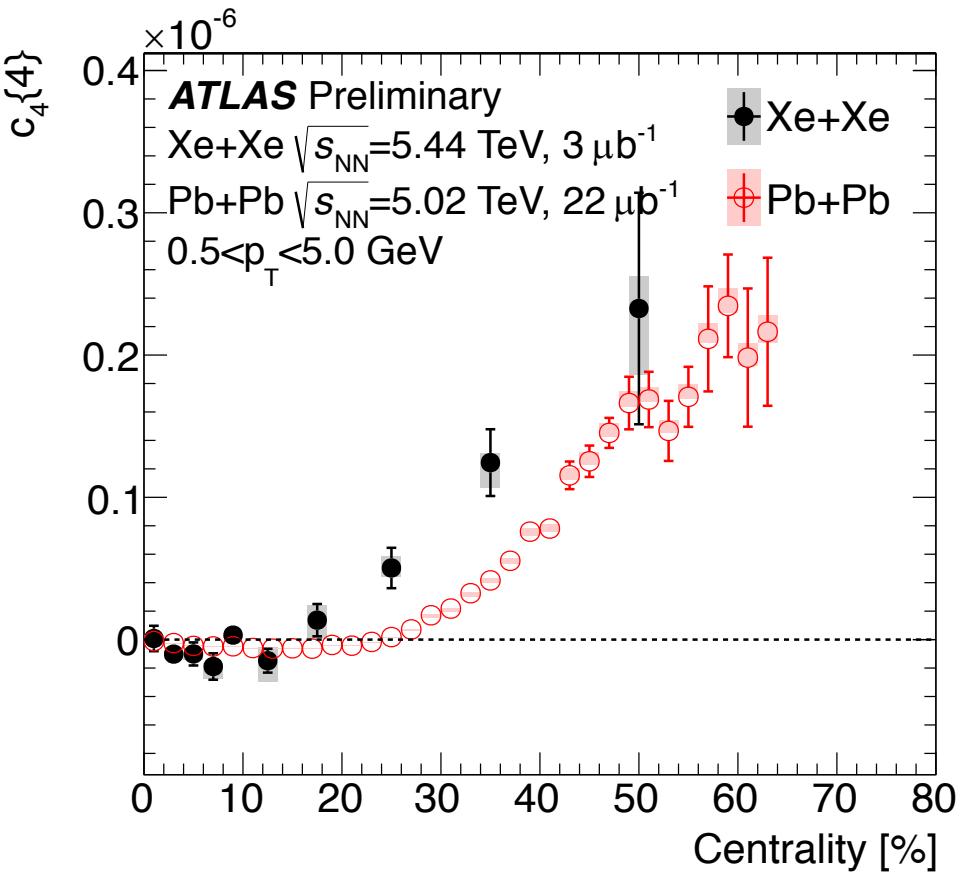
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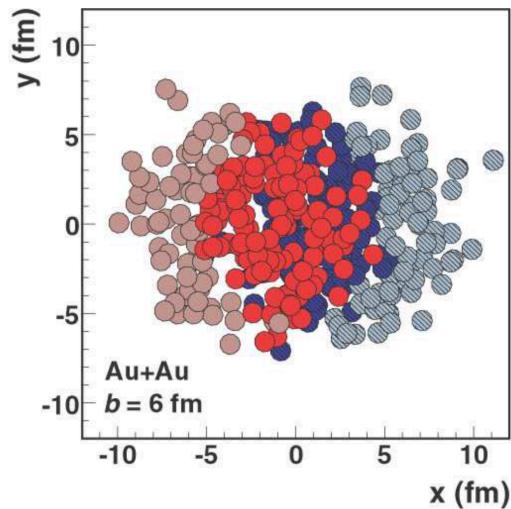






Origins of collectivity

- Final state correlations

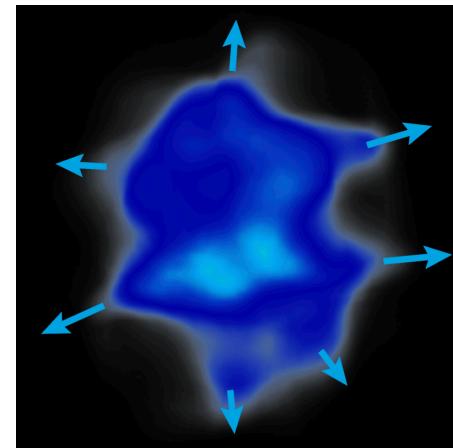


Spatial structure from initial condition

$$\frac{dN}{d\phi} = G \left(1 + 2 \sum_{n=1} v_n \cos n\phi \right)$$

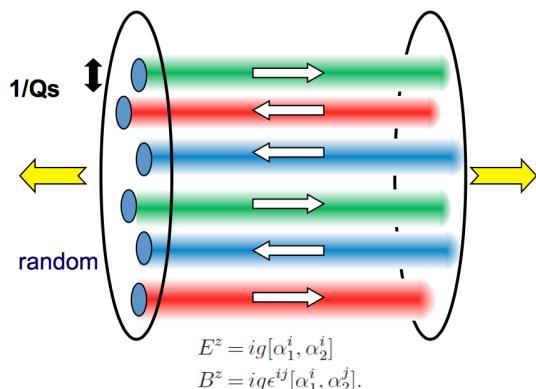


Hydrodynamic flow



Momentum correlations

- Initial state correlations



More careful studies in pp collisions are needed!

Particles are produced with momentum space correlations