Unit 6: Clustering

IPM Text Analysis

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Today: Cluster press releases

Goal: partition documents such that:

- similar documents are together
- dissimilar documents are apart

Method: Clustering methods

Game Plan:

- 1) What makes two data points (i.e. documents) similar?
- 2) How do we find a good partition?
- 3) How do we interpret the clusters?

Key Terms:

- (Multidimensional) Space
- Distance
- Euclidean Distance
- Cosine Distance
- Cluster Analysis / Clustering
- K-means
- Centroid

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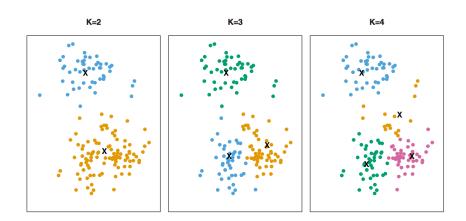
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- 2 K: the desired number of clusters.

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Outputs

- **11** C_k : The set of observations assigned to each cluster.
- $\supseteq \mu_{K}$: The mean for each K a vector representing the average values of all observations in that cluster. Also called centroid.



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The K-means algorithm will assign each observation to the cluster with the closest mean.

Goal: Cluster the following documents:

- I like to eat broccoli and bananas.
- I eat a banana smoothie for breakfast.
- Hamsters and kittens are cute.
- She adopted a cute kitten.

Inputs

1 A document term matrix

	adopt	banana	breakfast	broccoli	cute	eat	hamster	kitten	like	smoothi
1	0	1	0	1	0	1	0	0	1	0
2	0	1	1	0	0	1	0	0	0	1
3	0	0	0	0	1	0	1	1	0	0
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Outputs

1 C_k : Cluster assignment:

■ C₁: [1, 2]

■ C₂: [3, 4]

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Outputs

1 C_k : Cluster assignment:

■ **C**₁: [1, 2]

■ C₂: [3, 4]

2 μ_k : Cluster means / centroids:

	adopt	banana	breakfast	broccoli	cute	eat	hamster	kitten	like	smoothi
μ_1	0.0	1.0	0.5	0.5	0.0	1.0	0.0	0.0	0.5	0.5
μ_2	0.5	0.0	0.0	0.0	1.0	0.0	0.5	1.0	0.0	0.0

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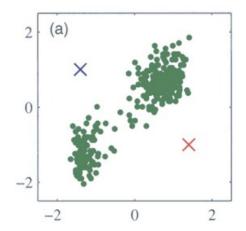
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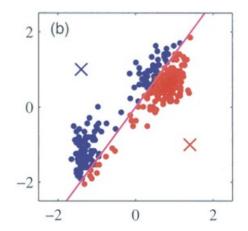
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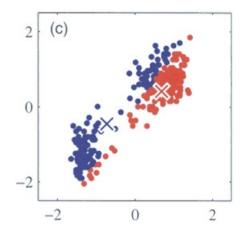
How do we find a good partition?

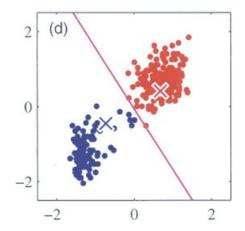
- 1) Randomly initialize K cluster centroids $(\mu_1, \mu_2, \dots, \mu_k)$ in random locations.
- 2) Repeat:
 - Assignment: Assign each observation \boldsymbol{X} to cluster with closest mean μ_k .
 - Update: Calculate new centroids μ_k by averaging all points assigned to each cluster.

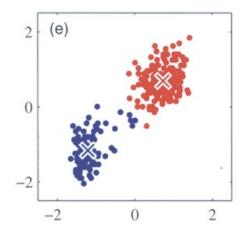
Stop when cluster assignments stop changing.

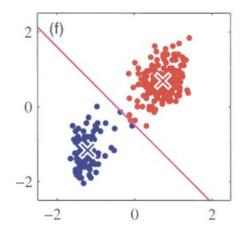


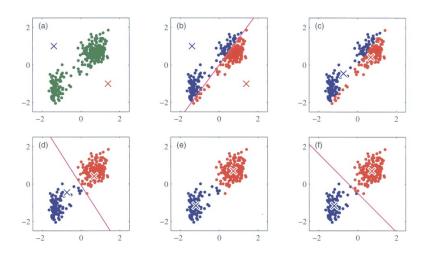












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- 3) Random starting values!
 - Results will depend on the initial (random) cluster centroid assignment (in step 1).
 - Important to run the algorithm multiple times from different random starting values.

Small Decisions with Big Consequences:

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How do we decide?

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Two kinds of validation criteria:

- 1 Quantitative evaluation:
 - A good clustering is one for which the within-cluster variation is as small as possible.
- 2 Qualitative evaluation:
 - A good clustering is one for which clusters are substantially / semantically interpretable.

Quantitative evaluation: within-cluster variation is as small as possible.

- Within-cluster variation: a measure of the amount by which the observations within a cluster differ from each other.
- Common metric: Sum of Squared Euclidean Distance

For a given document X in cluster k, the squared Euclidean distance is:

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Thus our goal is to minimize the total within-cluster sum of squares:

$$\sum_{k=1}^K W(C_k)$$

- Manual identification
 - Sample set of documents from same cluster
 - Read documents
 - Assign cluster "label" by hand
 - I like to eat broccoli and bananas. <>> "food"
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- 3 Be Transparent
 - Provide documents + code
 - Detail labeling procedures
 - Acknowledge ambiguity

To the R code!