

# An H5-Bridge-Based Asymmetric LLC Resonant Converter With an Ultrawide Output Voltage Range

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**Abstract**—To extend the output voltage range of the conventional *LLC* topology, a small magnetizing inductance and a large frequency modulation window are required. Both would jeopardize the system performances. To resolve this issue, this article proposes a novel H5-bridge-based asymmetric *LLC* resonant converter. By configuring the switch pattern of the H5-bridge, two asymmetric *LLC* resonant tanks could operate in idle, half-bridge, hybrid-bridge, and full-bridge modes. Correspondingly, six operation modes with scaled voltage gains are obtained. Hence, an ultrawide output voltage range is achieved with moderate magnetizing inductance and simplified design of resonant parameters. The switching frequency range is squeezed close to the resonant frequency, which is beneficial for control implementation and circulating current suppression. Furthermore, two resonant tanks facilitate an easier zero-voltage switching (ZVS) of the primary-side MOSFETs and alleviate the current and voltage stresses. The conduction loss is further reduced due to the power-sharing effect between resonant tanks. To achieve a minimized frequency window, the optimized design of two resonant tanks is analyzed. To verify this concept, a 1-kW-rated prototype with 390 V input and 80–450 V output is designed and tested. Primary-side MOSFETs' ZVS are achieved over the entire load range. The designed prototype achieves 97.05% peak efficiency and good efficiency performance over the ultrawide output voltage range.

**Index Terms**—Circuit reconfiguration, H5-bridge, *LLC*, wide output voltage range.

## I. INTRODUCTION

THE frequency-modulated (FM) *LLC* resonant converter is considered as a premium isolated dc–dc solution due to its

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- 1) zero-voltage switching (ZVS) on the primary MOSFETs,
- 2) low electromagnetic interference,
- 3) simple structure with low components count.

Thus, it is considered a candidate for the isolated dc–dc stage in plug-in electric vehicle (PEV) charging and other wide output voltage range applications [1]–[3].

To obtain a wide output voltage range using the conventional *LLC* topology, a small magnetizing inductance ( $L_m$ ) and a wide switching frequency ( $f_s$ ) window are required. The small  $L_m$  leads to large circulating current and conduction loss. Also, increasing  $f_s$  beyond the resonant frequency ( $f_r$ ) bucks the normalized output voltage below unity. However, this leads to the loss of zero current switching (ZCS) on the secondary-side diodes and increased magnetic loss. On the other hand, reducing  $f_s$  below  $f_r$  boosts the normalized output voltage above unity. Nevertheless, low  $f_s$  leads to bulky magnetics and increased circulating loss. In general, operation close to  $f_r$  is defined as the optimal operation range with the optimum overall performance. Therefore, the state-of-the-art research on wide output voltage range *LLC* converters mainly focuses on squeezing the  $f_s$  span with moderate  $L_m$ .

Modifying the equivalent resonant parameters in different modes is able to extend the output voltage range. In [4], an auxiliary transformer with a current source is paralleled with the main transformer to adjust the equivalent  $L_m$ . In [5], an auxiliary capacitor is inserted into the transformer. Thus, the equivalent  $L_m$  can be modulated by  $f_s$ . Similarly, in [6], an *LC* structure is coupled with the transformer, such that the equivalent  $L_m$  could be adjusted by  $f_s$ . In a different perspective, modifying the equivalent  $C_r$  also helps to extend the output voltage range by adjusting the quality factor,  $Q$ . In [7], a controllable parallel resonant capacitor is introduced to the *LLC* topology. By configuring the ON/OFF state of the auxiliary MOSFET,  $Q$  is adjusted to obtain two suitable voltage gain profiles. However, modifying the equivalent resonant parameters might lead to low efficiency at light load [4], [8], increased design complexity [5], and steep gain-frequency profile [6]. Furthermore, it is difficult to optimize efficiency over the entire output voltage range.

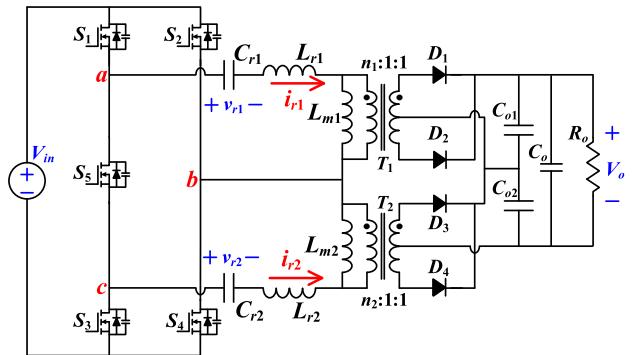
Modifications in the control strategy can also extend the output voltage range. Both phase-shift (PS) control and pulsewidth modulation (PWM) are able to regulate the output voltage with constant  $f_s$ . In [9], an asymmetric PWM mechanism is introduced to regulate the output voltage. Similarly, in [9]–[13],

auxiliary PWM control is introduced to optimize the FM control. In [12], the *LLC* resonant tank operates in  $f_r$ , and a wide output voltage range is achieved by the PWM of the secondary-side MOSFET. In [14], an FM+PS control method is proposed. One phase leg of the rectifier is replaced by a synchronous rectifier (SR). Output voltage could be modulated by the PS between the SR and primary-side square wave. In [15], the normalized output voltage below unity is achieved by PS control. This helps to avoid the ZCS loss of FM with  $f_s$  beyond  $f_r$  and improves the voltage regulation capacity. On the other hand, the variable dc-link voltage also facilitates a squeezed  $f_s$  range [16]–[18]. The output voltage of the front-end PFC converter linearly tracks the output voltage. Thus, the second-stage *LLC* converter can always operate at the maximum efficiency point [19]. However, modifying the control strategy might lead to dc bias in magnetizing current [9] and increased current stress [14]. Moreover, the variable dc-link voltage technique presented in [19] requires a customized front-end ac–dc converter.

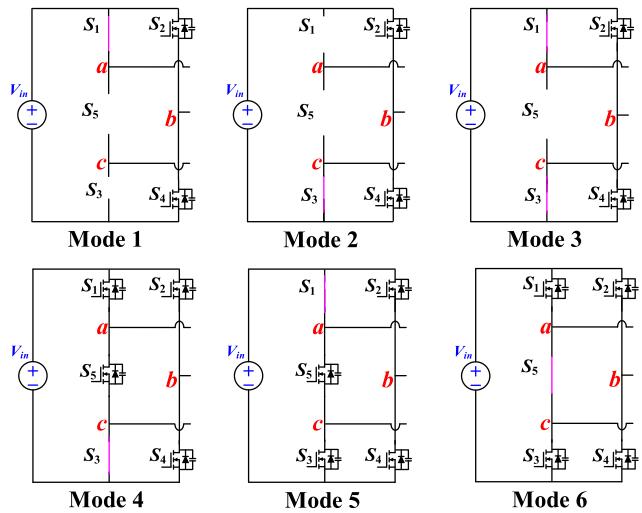
Reconfiguring the primary-side switch network can adjust the root-mean-square (rms) value of the resonant tank input voltage and effective turns ratio. Therefore, the output voltage range of the resonant converter can be extended conveniently. The most intuitive way is to implement the transition of the switching network between half-bridge and full-bridge configurations. Thus, a two-level voltage gain profile (1:2) is derived, and the smooth mode transition method is studied in [20]. Similar switch network reconfigurations are reported in [21]–[23]. In [22], a two-level voltage gain profile (1:1.5) is derived using two identical resonant tanks. In [23], a five-switch bridge is reconfigured to enable a four-step output voltage profile. However, this technique requires two identical resonant tanks, and the voltage range division is coarse. In [24], the transition between full-bridge rectifier and voltage doubler could extend the output voltage range. In [25], the transformer effective turns ratio could be adjusted by configuring the bidirectional auxiliary switch on the primary side. This two-level voltage gain profile facilitates extended output voltage and squeezed  $f_s$  window. In [26], both  $L_m$  and the effective turns ratio could be adjusted by configuring the bidirectional auxiliary switch. Thus, a four-level voltage gain profile is obtained to extend the output voltage range. In [27] and [28], different primary-side switch patterns are proposed to enable multiple voltage levels with modulated duty ratios. Hence, a multilevel voltage gain profile is realized to extend the output voltage range. Nevertheless, this method requires large counts number and complex driving signal.

In this article, an H5-bridge-based asymmetrical *LLC* resonant converter is proposed for wide output voltage range applications. Due to the H5-bridge structure, a six-step voltage gain profile is obtained. This effectively extends the output voltage range with further constrained  $f_s$  range. The advantages of the proposed converter include

- 1) six-step fine voltage gain division and ultrawide output voltage range,
- 2) narrow  $f_s$  range close to  $f_r$ ,
- 3) relatively large  $L_m$  and low circulating current,
- 4) reduced primary-side conduction loss,
- 5) easy realization of ZVS,



**Fig. 1.** Schematic of the proposed H5-bridge asymmetric *LLC* converter.



**Fig. 2.** Primary switch patterns in six modes.

- 6) alleviated current and voltage stresses in the resonant tanks,
- 7) elimination of the resonant current oscillations due to the split filtering capacitors.

## II. TOPOLOGICAL DESCRIPTION

**Fig. 1** shows the schematic of the proposed converter. In comparison with the conventional full-bridge *LLC* resonant converter, an extra MOSFET is added on the primary side to enable a reconfigurable H5-bridge. The output of the H5-bridge is fed to two asymmetric *LLC* resonant tanks with a different set of resonant parameters. In those two resonant tanks, the resonant inductance ( $L_{r1}$  and  $L_{r2}$ ), resonant capacitance ( $C_{r1}$  and  $C_{r2}$ ), magnetizing inductance ( $L_{m1}$  and  $L_{m2}$ ), and transformers' turns ratio ( $n_1$  and  $n_2$ ) are all different. The secondary side is two center-tapped transformer-based full-wave rectifiers. The outputs of those two rectifiers are in series. The rms values of the two *LLC* resonant tanks' input voltages ( $v_{ab,\text{rms}}$  and  $v_{cb,\text{rms}}$ ), could be easily adjusted by configuring the primary-side MOSFETs among ON state, OFF state, and FM state. Hence, a six-step voltage gain profile could be derived.

The switch patterns of the H5-bridge, which correspond to six voltage gain profiles, are plotted in **Fig. 2**. The corresponding

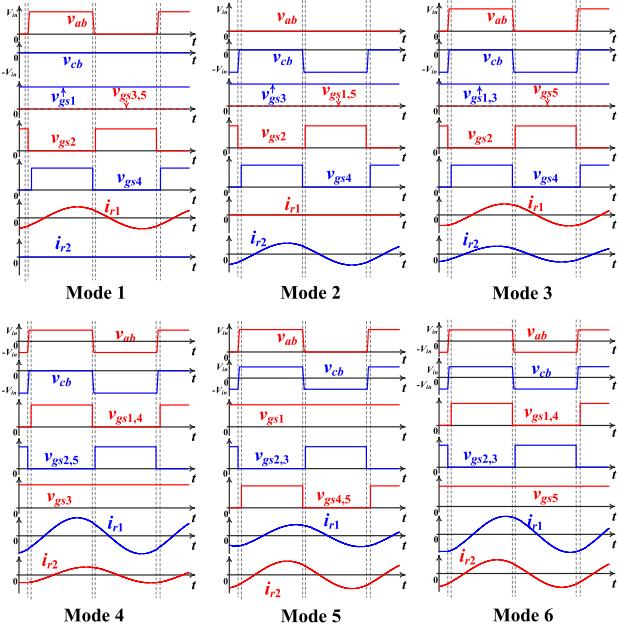


Fig. 3. Key steady-state waveforms in six modes.

key steady-state waveforms are plotted in Fig. 3. As shown in the figure, the proposed topology enables six different operation modes.

*Mode 1:* In this mode,  $S_1$  is always ON, and  $S_{3,5}$  are always OFF.  $S_2$  and  $S_4$  are driven complementarily with certain deadband (FM state). Resonant tank 2 (RT2) is disabled and does not transfer power to the output. Resonant tank 1 (RT1) is in half-bridge mode since its input voltage,  $v_{ab}$ , is a two-level square wave (0 V to  $V_{in}$ ) and  $v_{ab,rms}$  is  $V_{in}/2$ .

*Mode 2:* In this mode,  $S_3$  is always ON, and  $S_{1,5}$  are always off.  $S_2$  and  $S_4$  operate in the FM state. Similarly, RT1 is disabled and does not transfer power to the output. RT2 is in the half-bridge mode since its input voltage,  $v_{cb}$ , is a two-level square wave ( $-V_{in}$  to 0 V) and  $v_{cb,rms}$  is  $V_{in}/2$ . Since  $n_1$  and  $n_2$  are unequal, voltage gain profiles in modes 1 and 2 are different.

*Mode 3:* In this mode,  $S_{1,3}$  are always ON, and  $S_5$  is always OFF.  $S_2$  and  $S_4$  operate in the FM state.  $v_{ab}$  and  $v_{cb}$  are two-level square waves (0 V to  $V_{in}$ ,  $-V_{in}$  to 0 V). Both  $v_{ab,rms}$  and  $v_{cb,rms}$  are  $V_{in}/2$ . Hence, both RT1 and RT2 are in the half-bridge mode. Due to different turns ratio, the power transferred via two resonant tanks are also different. Since  $n_2$  is smaller than  $n_1$ , RT2 transfers more power than RT1 does.

*Mode 4:* In this mode,  $S_3$  is always ON.  $S_{2,5}$  and  $S_{1,4}$  operate in the FM state.  $v_{ab}$  and  $v_{cb}$  are two-level square waves ( $-V_{in}$  to  $V_{in}$ ,  $-V_{in}$  to 0 V).  $v_{ab,rms}$  is  $V_{in}$ , whereas  $v_{cb,rms}$  is  $V_{in}/2$ . Hence, RT1 is in the full-bridge mode, and RT2 is in the half-bridge mode. In this mode, RT1 transfers more power since  $v_{ab,rms}$  equals  $2v_{cb,rms}$ .

*Mode 5:* In this mode,  $S_1$  is always ON.  $S_{2,3}$  and  $S_{4,5}$  operate in the FM state.  $v_{ab}$  and  $v_{cb}$  are two-level square waves (0 V to  $V_{in}$ ,  $-V_{in}$  to  $V_{in}$ ).  $v_{ab,rms}$  is  $V_{in}/2$ , whereas  $v_{cb,rms}$  is  $V_{in}$ . Hence, RT1 is in the half-bridge mode, and RT2 is in the full-bridge mode. Due to the smaller  $n_2$  and larger input voltage rms value, RT2 transfers more power than RT1. Similarly, since  $n_1$

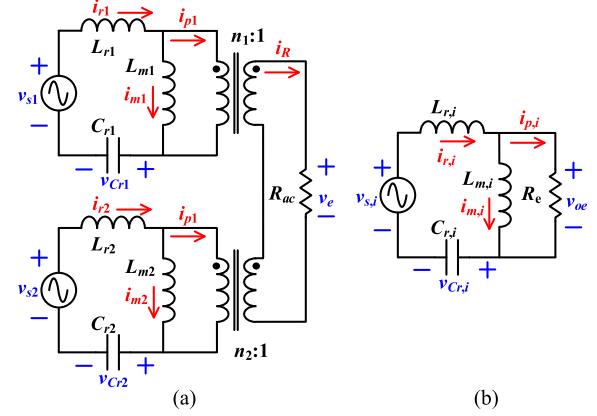


Fig. 4. (a) General equivalent circuit model in six modes. (b) Equivalent circuit model for modes 1 and 2.

and  $n_2$  are unequal, voltage gain profiles in modes 4 and 5 are different.

*Mode 6:* In this mode,  $S_5$  is always ON.  $S_{2,3}$  and  $S_{1,4}$  operate in the FM state.  $v_{ab}$  and  $v_{cb}$  are two-level square waves ( $-V_{in}$  to  $V_{in}$ ).  $v_{ab,rms}$  and  $v_{cb,rms}$  are both  $V_{in}$ . Hence, both RT1 and RT2 are in the full-bridge mode. The proposed converter achieves the largest output voltage in this mode. Since  $n_2$  is smaller than  $n_1$ , RT2 transfers more power than RT1.

### III. MODELING AND ANALYSIS

#### A. Circuit Modeling

Since  $f_s$  range is squeezed and close to  $f_r$ , the first-harmonic-analysis (FHA) method maintains good modeling accuracy. Thus, FHA is adopted to construct the equivalent circuit model in six modes. The general equivalent circuits model of the proposed converter is plotted in Fig. 4(a). As shown in the figure,  $v_{s1}$  and  $v_{s2}$  are the fundamental frequency components of  $v_{ab}$  and  $v_{cb}$ , respectively.  $R_{ac}$  and  $v_e$  are the equivalent load and output voltage. In modes 1 and 2, only one resonant tank is enabled. Therefore, the equivalent circuit model can be simplified, as shown in Fig. 4(b).

In modes 3–6, both RT1 and RT2 are enabled. To simplify the analysis, the output is split according to the power shares of two resonant tank. The resulting circuit model is plotted in Fig. 5(a). In Fig. 5(a), points d and e have equal voltage potential. Thus, the equivalent circuit models in modes 3–6 can be merged, as shown in Fig. 5(b). It can be regarded as two separate LLC resonant converters with  $n_1 i_{p1} = n_2 i_{p2}$

$$R_{e1} = n_1^2 R_{ac1} \quad (1)$$

$$R_{e2} = n_2^2 R_{ac2} \quad (2)$$

$$R_{ac1} + R_{ac2} = R_{ac}. \quad (3)$$

The conventional LLC resonant converters have been well studied in literature. To simplify the analysis, this article mainly focuses on the uniqueness of the proposed converter.

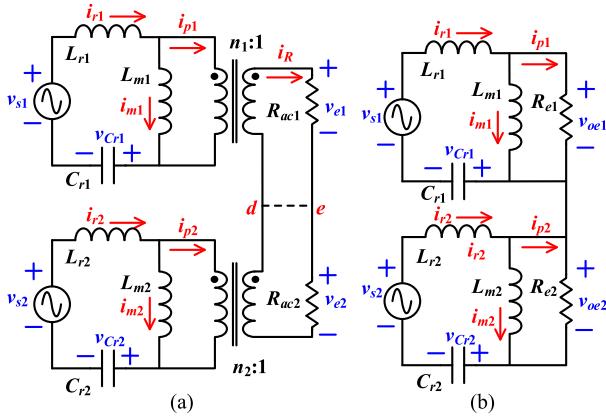


Fig. 5. Equivalent circuit model for modes 3–6 with (a) series load and (b) split load.

### B. Voltage Gain Analysis

**1) Modes 1 and 2:** In mode 1, only RT1 is enabled. Hence, all output voltage is applied to RT1's secondary side, and the following state equation is obtained:

$$\begin{aligned}\frac{dv_{Cr1}}{dt} &= i_{Lr1}/C_{r1} \\ \frac{di_{Lr1}}{dt} &= (v_{s1} - v_{Cr1} - n_1 v_e)/L_{r1} \\ \frac{di_{m1}}{dt} &= n_1 v_e/L_{m1}.\end{aligned}\quad (4)$$

Similarly, the following state equation in mode 2 is derived:

$$\begin{aligned}\frac{dv_{Cr2}}{dt} &= i_{Lr2}/C_{r2} \\ \frac{di_{Lr2}}{dt} &= (v_{s2} - v_{Cr2} - n_2 v_e)/L_{r2} \\ \frac{di_{m2}}{dt} &= n_2 v_e/L_{m2}.\end{aligned}\quad (5)$$

According to (4) and (5), the state equations in modes 1 and 2 are identical to those in conventional *LLC* resonant converter.  $V_o$  is the total output voltage, or the load terminal voltage;  $V_{in}$  is the input voltage, or the source terminal voltage. Therefore, the voltage gains at  $f_r$  in those two modes are

$$G_1 = \frac{V_o}{V_{in}} = \frac{1}{2n_1}, \quad \text{Mode 1} \quad (6)$$

$$G_2 = \frac{V_o}{V_{in}} = \frac{1}{2n_2}, \quad \text{Mode 2}. \quad (7)$$

**2) Modes 3–6:** In modes 3–6, both *LLC* resonant tanks are enabled. According to the circuit model shown in Fig. 5(a), the state equations in modes 3–6 are derived as follows:

$$\begin{aligned}\frac{dv_{Cr1}}{dt} &= i_{Lr1}/C_{r1} \\ \frac{di_{Lr1}}{dt} &= (v_{s1} - v_{Cr1} - n_1 v_{e1})/L_{r1} \\ \frac{di_{m1}}{dt} &= n_1 v_{e1}/L_{m1}\end{aligned}\quad (8)$$

TABLE I  
VOLTAGE GAINS AT RESONANT FREQUENCY IN SIX MODES

Modes	Tanks	$v_{ab,rms}$	$v_{cb,rms}$	Gain
Mode 1	1	$V_{in}/2$	0	$G_0$
Mode 2	1	0	$V_{in}/2$	$(n_1/n_2)G_0$
Mode 3	2	$V_{in}/2$	$V_{in}/2$	$(1+n_1/n_2)G_0$
Mode 4	2	$V_{in}$	$V_{in}/2$	$(2+n_1/n_2)G_0$
Mode 5	2	$V_{in}/2$	$V_{in}$	$(1+2n_1/n_2)G_0$
Mode 6	2	$V_{in}$	$V_{in}$	$(2+2n_1/n_2)G_0$

$$\begin{aligned}\frac{dv_{Cr2}}{dt} &= i_{Lr2}/C_{r2} \\ \frac{di_{Lr2}}{dt} &= (v_{s2} - v_{Cr2} - n_2 v_{e2})/L_{r2} \\ \frac{di_{m2}}{dt} &= n_2 v_{e2}/L_{m2}.\end{aligned}\quad (9)$$

According to (8) and (9), the state equations of two *LLC* resonant tanks are also identical to the conventional *LLC* resonant converter. Therefore, the voltage gains in modes 3–6 equals the sum of the voltage gains of two separate *LLC* resonant converters. It should be noted that the *LLC* resonant tank operates at full-bridge mode or half-bridge mode. The voltage gains at  $f_r$  in modes 3–6 are expressed as follows:

$$G_3 = \frac{1}{2n_1} + \frac{1}{2n_2}, \quad \text{Mode 3} \quad (10)$$

$$G_4 = \frac{1}{n_1} + \frac{1}{2n_2}, \quad \text{Mode 4} \quad (11)$$

$$G_5 = \frac{1}{2n_1} + \frac{1}{n_2}, \quad \text{Mode 5} \quad (12)$$

$$G_6 = \frac{1}{n_1} + \frac{1}{n_2}, \quad \text{Mode 6}. \quad (13)$$

The voltage gains in six modes are summarized in Table I. In the range where  $f_s$  is unequal to  $f_r$ , the voltage gains are

$$G = G_{f_s=f_r} f(Q, m, f_n) \quad (14)$$

$$f(Q, m, f_n) = \frac{mf_n^2}{\sqrt{[(m+1)f_n^2 - 1]^2 + m^2 Q^2 f_n^2 (f_n^2 - 1)^2}} \quad (15)$$

$$Q = \frac{\sqrt{L_r/C_r}}{R_L 8n^2/\pi^2} \quad (16)$$

where  $f_n$  is the normalized frequency, and  $m$  is the inductance ratio. All are identical to those in conventional *LLC* resonant converters. In modes 1 and 2,  $R_L$  equals  $R_o$ . In modes 3–6,  $R_L$  is part of the  $R_o$ . The corresponding voltage gain curves in six modes and the operation range are plotted in Fig. 6. As shown in the figure, the six-step voltage gain profile is generated by six modes. It enables both a much-extended output voltage range and an effectively squeezed  $f_s$  window. Due to the facts a)  $f_s$  is close to  $f_r$ , and b)  $Q$  and  $m$  are properly designed following the flowchart illustrated in Fig. 7, the voltage gains of the proposed converter in six modes are scaled, as indicated in Table I.

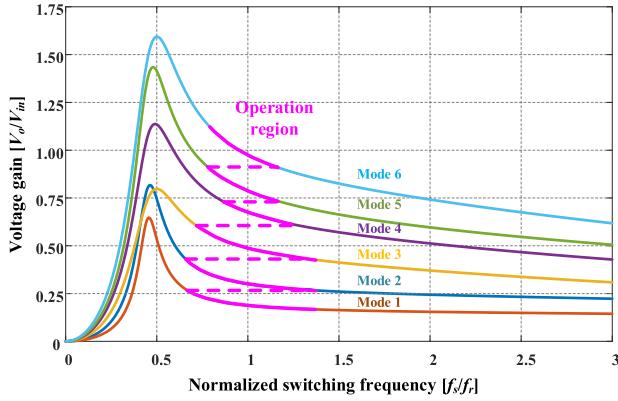


Fig. 6. Voltage gain curves in six modes.

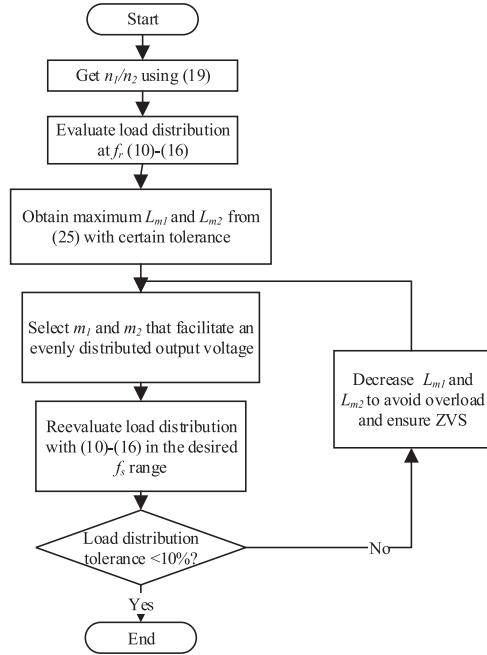


Fig. 7. Flowchart to design quality factor ( $Q$ ) and inductance ratio ( $m$ ).

Since wide output voltage range is achieved by the six-step voltage gain profile with moderate  $L_m$  and narrow  $f_s$  span, the large conduction loss, circulating loss, and bulky magnetic component caused by small  $L_m$  and wide  $f_s$  span are avoided. The conduction loss introduced by the extra MOSFET is smaller than the reduced conduction and circulating loss.

#### IV. CRITICAL DESIGN CONSIDERATIONS

##### A. Narrowest $f_s$ Range and Turns Ratio

To obtain a narrowest overall  $f_s$  range, the  $f_s$  range in six modes should be distributed uniformly. Assuming the peak and valley voltage gains in mode 1 are  $x$  and  $y$ , respectively. According to the voltage gain analysis presented in Section III-B, the peak and valley voltage gains in modes 2–6 can be obtained, as shown in Table II.

TABLE II  
VOLTAGE GAIN RANGE IN EACH MODE

Modes	Peak gain	Valley gain
Mode 1	$x$	$y$
Mode 2	$(n_1/n_2)x$	$(n_1/n_2)y$
Mode 3	$(1+n_1/n_2)x$	$(1+n_1/n_2)y$
Mode 4	$(2+n_1/n_2)x$	$(2+n_1/n_2)y$
Mode 5	$(1+2n_1/n_2)x$	$(1+2n_1/n_2)y$
Mode 6	$(2+2n_1/n_2)x$	$(2+2n_1/n_2)y$

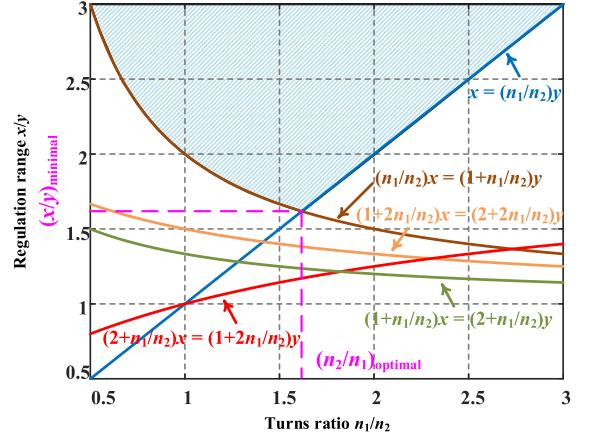


Fig. 8.  $n_1/n_2$ 's impact on required voltage regulation range.

To provide a continuous voltage gain profile, the peak voltage gain in the previous mode should be larger than the valley voltage gain in the next mode

$$\begin{aligned}
 x &\geq (n_1/n_2) y \\
 (n_1/n_2) x &\geq (1+n_1/n_2) y \\
 (1+n_1/n_2) x &\geq (2+n_1/n_2) y \\
 (2+n_1/n_2) x &\geq (1+2n_1/n_2) y \\
 (1+2n_1/n_2) x &\geq (2+2n_1/n_2) y.
 \end{aligned} \quad (17)$$

To make the  $f_s$  range narrowest, the voltage regulation range should be optimized

$$\begin{aligned}
 x/y &\geq [n_1/n_2, 1+n_2/n_1, (n_1+2n_2)/(n_1+n_2), \\
 &(2n_1+n_2)/(n_1+2n_2), (2n_1+2n_2)/(2n_1+n_2)]_{\max}.
 \end{aligned} \quad (18)$$

The impact of  $n_1/n_2$  on required voltage regulation range is shown in Fig. 8. From (18) and Fig. 8, the smallest  $x/y$  and narrowest  $f_s$  range could be achieved with optimal  $n_2/n_1$

$$(n_1/n_2)_{\text{optimal}} = \frac{1+\sqrt{5}}{2} \approx 1.62. \quad (19)$$

##### B. ZVS Condition

The  $i_r$ ,  $i_m$ , and  $v_{in}$  in the conventional LLC resonant converter at  $f_r$  are plotted in Fig. 9.  $I_m$  is the peak value of  $i_m$

$$i_r(T_s/2) = i_m(T_s/2) = I_m \quad (20)$$

$$I_m = \frac{nV_o}{4L_m f_s}. \quad (21)$$

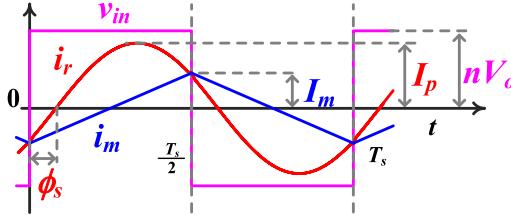


Fig. 9.  $i_r$  and  $i_m$  in the conventional full-bridge LLC converter.

To realize the ZVS of the primary MOSFETs,  $i_r$  should be sufficiently large to fully charge and discharge the MOSFETs' output capacitor during the deadband [29].  $t_d$  is the duration of deadband.  $C_{\text{oss}}$  is the energy-normalized output capacitance

$$I_m t_d > 2C_{\text{oss}} V_{\text{in}} \quad (22)$$

$$t_d \geq \frac{8L_m C_{\text{oss}} f_s V_{\text{in}}}{nV_o}. \quad (23)$$

**1) Modes 1 and 2:** As shown in Fig. 4(b), the equivalent circuit model in modes 1 and 2 is identical to that of the conventional LLC resonant converter. Hence, their ZVS conditions are the same

$$\begin{cases} t_d \geq \frac{8L_{m1} C_{\text{oss}} f_s V_{\text{in}}}{n_1 V_o}, & \text{Mode 1} \\ t_d \geq \frac{8L_{m2} C_{\text{oss}} f_s V_{\text{in}}}{n_2 V_o}, & \text{Mode 2} \end{cases}. \quad (24)$$

Both LLC resonant tanks operate in the half-bridge mode,  $nV_o = V_{\text{in}}/2$

$$\begin{cases} t_d \geq 16L_{m1} C_{\text{oss}} f_s, & \text{Mode 1} \\ t_d \geq 16L_{m2} C_{\text{oss}} f_s, & \text{Mode 2} \end{cases}. \quad (25)$$

**2) Modes 3–6:** In modes 3–6,  $i_r$  of both LLC resonant tanks charge and discharge the MOSFETs'  $C_{\text{oss}}$

$$(I_{m1} + I_{m2}) t_d > 2C_{\text{oss}} V_{\text{in}}. \quad (26)$$

According to the equivalent circuit model in modes (3)–(6) and (21)

$$\left( \frac{n_1 V_1}{4L_{m1} f_s} + \frac{n_2 V_2}{4L_{m2} f_s} \right) t_d > 2C_{\text{oss}} V_{\text{in}} \quad (27)$$

$$n_1 V_1 = n_2 V_2 = V_{\text{in}}/2, \quad \text{Mode 3} \quad (28)$$

$$n_1 V_1 = 2n_2 V_2 = V_{\text{in}}, \quad \text{Mode 4} \quad (29)$$

$$n_2 V_2 = 2n_1 V_1 = V_{\text{in}}, \quad \text{Mode 5} \quad (30)$$

$$n_1 V_1 = n_2 V_2 = V_{\text{in}}, \quad \text{Mode 6}. \quad (31)$$

Therefore, the ZVS conditions for primary-side MOSFETs in modes 3–6 can be obtained and are given as follows:

$$t_d > 16C_{\text{oss}} f_s \frac{L_{m1} L_{m2}}{L_{m1} + L_{m2}}, \quad \text{Mode 3} \quad (32)$$

$$t_d > 16C_{\text{oss}} f_s \frac{L_{m1} L_{m2}}{L_{m1} + 2L_{m2}}, \quad \text{Mode 4} \quad (33)$$

$$t_d > 16C_{\text{oss}} f_s \frac{L_{m1} L_{m2}}{2L_{m1} + L_{m2}}, \quad \text{Mode 5} \quad (34)$$

$$t_d > 8C_{\text{oss}} f_s \frac{L_{m1} L_{m2}}{L_{m1} + L_{m2}}, \quad \text{Mode 6}. \quad (35)$$

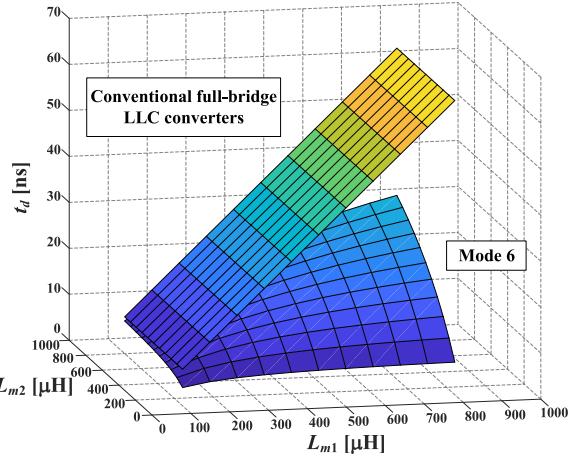


Fig. 10.  $t_d$  to achieve the ZVS of primary-side MOSFETs.

TABLE III  
POWER DISTRIBUTION BETWEEN TWO RESONANT TANKS

Modes	$P_{o1}/P_o$	$P_{o2}/P_o$
Mode 1	100%	0
Mode 2	0	100%
Mode 3	$n_2/(n_1 + n_2)$	$n_1/(n_1 + n_2)$
Mode 4	$2n_2/(n_1 + 2n_2)$	$n_1/(n_1 + 2n_2)$
Mode 5	$n_2/(2n_1 + n_2)$	$2n_1/(2n_1 + n_2)$
Mode 6	$n_2/(n_1 + n_2)$	$n_1/(n_1 + n_2)$

The required  $t_d$  to realize ZVS for conventional full-bridge LLC converters and the proposed converter in mode 6 are compared graphically in Fig. 10. The  $L_{m1}$  and  $L_{m2}$  in Fig. 10 of the conventional LLC converter are same and equal to the  $L_m$  of the conventional LLC converter. It can be found that the  $t_d$  is reduced in our proposed converter. This is because both resonant tanks contribute currents to charge and discharge the  $C_{\text{oss}}$ . This is also beneficial to reduce  $L_m$ .

The conduction loss of primary side is expressed as follows:

$$P_{\text{con}} = i_r^2 r_p \quad (36)$$

where  $r_p$  is the equivalent primary-side resistance, including wire resistance and copper resistance of magnetic components. The conduction loss is reduced because  $i_r$  is split between two LLC resonant tanks.

In mode 1, only resonant tank 1 is enabled, whereas in mode 2, only resonant tanks 2 is enabled. Hence, in modes 1 and 2, the enabled resonant tank carries all the power.

In modes 3–6, both resonant tanks are enabled. Nevertheless, due to the asymmetric resonant parameters, the power shares of two resonant tanks are unmatched. On the secondary side, two resonant tanks' currents are identical. Hence, the power distribution between two resonant tanks equals their voltage distribution. Based on the voltage gain analysis presented in Section III-B, the output voltage difference between two resonant tanks originates from different turns ratios and different  $v_{\text{in},\text{rms}}$ . Correspondingly, the power distribution between two resonant tanks is summarized in Table III.

According to **Table III**, the power delivered via each resonant tank varies with output power and operating modes. The maximum power carried by each resonant tank should be decided by specific  $n_1/n_2$  and power range in each mode.

### C. Electric Stresses

According to **Fig. 8**, the peak current of  $i_r$  and  $I_p$  in the *LLC* resonant converter is derived as follows:

$$I_p = \sqrt{\frac{\pi^2 V_o^2}{4n^2 R_o^2} + \frac{n^2 V_o^2}{16L_m^2 f_s^2}}. \quad (37)$$

**1) Modes 1 and 2:** According to (37) and the equivalent circuits shown in **Fig. 5(b)**,  $I_p$  in modes 1 and 2 is derived as follows:

$$I_p = \sqrt{\frac{\pi^2 V_o^2}{4n_1^2 R_o^2} + \frac{n_1^2 V_o^2}{16L_{m1}^2 f_s^2}} \quad \text{Mode 1} \quad (38)$$

$$I_p = \sqrt{\frac{\pi^2 V_o^2}{4n_2^2 R_o^2} + \frac{n_2^2 V_o^2}{16L_{m2}^2 f_s^2}} \quad \text{Mode 2}. \quad (39)$$

**2) Modes 3–6:** The current delivered to the secondary-side equals  $i_r - i_m$ . Also, at  $t = 0$ ,  $i_r = i_m$ .  $I_{p1}$  and  $I_{p2}$  are the peak values of  $i_{r1}$  and  $i_{r2}$ , respectively

$$\begin{aligned} & \frac{2}{T_s} \int_0^{\frac{T_s}{2}} \left( I_{p1} \sin(\omega_s t - \varphi_{s1}) - \frac{n_1 V_1}{L_{m1} f_s} t + \frac{n_1 V_1}{4L_{m1} f_s} \right) dt \\ &= \frac{V_o}{n_1 R_o} \end{aligned} \quad (40)$$

$$\begin{aligned} & \frac{2}{T_s} \int_0^{\frac{T_s}{2}} \left( I_{p2} \sin(\omega_s t - \varphi_{s2}) - \frac{n_2 V_2}{L_{m2} f_s} t + \frac{n_2 V_2}{4L_{m2} f_s} \right) dt \\ &= \frac{V_o}{n_2 R_o} \end{aligned} \quad (41)$$

$$I_{p1} \sin(-\varphi_{s1}) = -\frac{n_1 V_1}{4L_{m1} f_s} \quad (42)$$

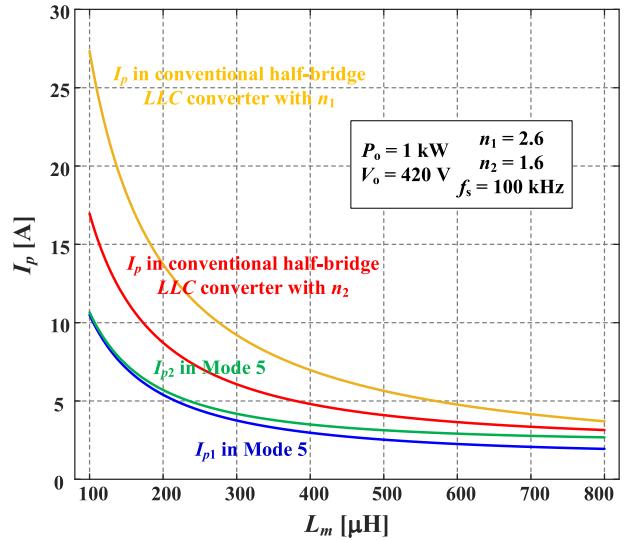
$$I_{p2} \sin(-\varphi_{s2}) = -\frac{n_2 V_2}{4L_{m2} f_s}. \quad (43)$$

Based on the power distribution obtained in Section IV-C,  $V_1/V_o$  and  $V_2/V_o$  are derived. Correspondingly,  $I_p$  in each resonant tank in modes 3–6 is derived as follows:

$$\begin{cases} I_{p1} = \sqrt{\frac{\pi^2 V_o^2}{4n_1^2 R_o^2} + \frac{n_1^2 n_2^2 V_o^2}{16L_{m1}^2 f_s^2(n_1+n_2)^2}} \\ I_{p2} = \sqrt{\frac{\pi^2 V_o^2}{4n_2^2 R_o^2} + \frac{n_1^2 n_2^2 V_o^2}{16L_{m2}^2 f_s^2(n_1+n_2)^2}} \end{cases} \quad \text{Mode 3} \quad (44)$$

$$\begin{cases} I_{p1} = \sqrt{\frac{\pi^2 V_o^2}{4n_1^2 R_o^2} + \frac{n_1^2 n_2^2 V_o^2}{4L_{m1}^2 f_s^2(n_1+2n_2)^2}} \\ I_{p2} = \sqrt{\frac{\pi^2 V_o^2}{4n_2^2 R_o^2} + \frac{n_1^2 n_2^2 V_o^2}{16L_{m2}^2 f_s^2(n_1+2n_2)^2}} \end{cases} \quad \text{Mode 4} \quad (45)$$

$$\begin{cases} I_{p1} = \sqrt{\frac{\pi^2 V_o^2}{4n_1^2 R_o^2} + \frac{n_1^2 n_2^2 V_o^2}{16L_{m1}^2 f_s^2(2n_1+n_2)^2}} \\ I_{p2} = \sqrt{\frac{\pi^2 V_o^2}{4n_2^2 R_o^2} + \frac{n_1^2 n_2^2 V_o^2}{4L_{m2}^2 f_s^2(2n_1+n_2)^2}} \end{cases} \quad \text{Mode 5} \quad (46)$$



**Fig. 11.** Comparison of primary-side peak currents.

$$\begin{cases} I_{p1} = \sqrt{\frac{\pi^2 V_o^2}{4n_1^2 R_o^2} + \frac{n_1^2 n_2^2 V_o^2}{16L_{m1}^2 f_s^2(n_1+n_2)^2}} \\ I_{p2} = \sqrt{\frac{\pi^2 V_o^2}{4n_2^2 R_o^2} + \frac{n_1^2 n_2^2 V_o^2}{16L_{m2}^2 f_s^2(n_1+n_2)^2}} \end{cases} \quad \text{Mode 6}. \quad (47)$$

$I_{p1}$  and  $I_{p2}$  are the peak currents in two resonant tanks, respectively. It can be found that the expressions of peak current in modes 3 and 6 are identical. This is because  $V_1/V_o$  and  $V_2/V_o$  in these two modes are identical.

According to the comparison of primary-side peak currents, as shown in **Fig. 11**, the current stress of the proposed converter is reduced. This reduction is more obvious with larger  $L_m$ , which is the benefit of the proposed converter. Due to the resonance between  $L_r$  and  $C_r$ , a similar result for voltage stress in  $C_r$  could be derived

$$V_{rp} = \sqrt{I_p^2 L_r / C_r} \quad (48)$$

$V_{rp}$  is the peak voltage in  $C_r$ .

### D. Attractive Features

**1) Low Circulating Current Loss:** For *LLC* converters, certain circulating current is required to facilitate the ZVS turning ON of the primary-side MOSFETs. During each mode, the sum of currents of  $L_{m1}$  and  $L_{m2}$  contributes to the charging current to realize ZVS in the deadband, as shown in (26). Accordingly, to make a fair comparison between the proposed converter and conventional *LLC* converter, the following assumption is made:

$$I_{m1} + I_{m2} = I_{m,\text{conv}} \quad (49)$$

where  $I_{m,\text{conv}}$  is the circulating current of the conventional *LLC* converter. It is obvious that  $I_{m1}^2 + I_{m2}^2$  is smaller than  $(I_{m1} + I_{m2})^2$ . Since the circulating loss is proportional to the square of charging currents, we can judge that the circulating loss of the proposed converter is reduced.

For instance, assume each resonant tank resistance is approximately equal to  $R_{\text{tank}}$ . If we use a 3 A current to charge the output

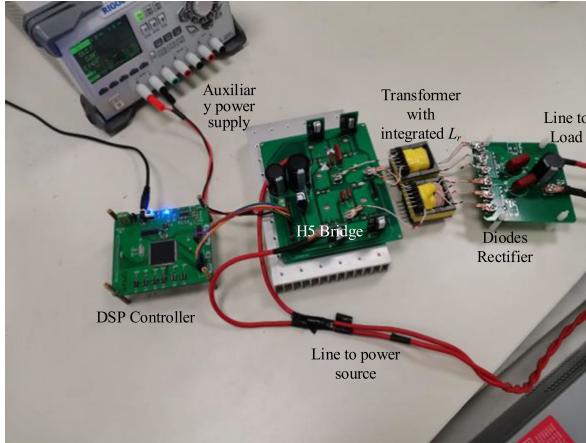


Fig. 12. Photograph of the designed prototype.

capacitor of MOSFETs in the deadband for ZVS, the conduction loss in the resonant tank for conventional *LLC* is  $9R_{\text{tank}}$ ; but in H5 topology, if RT1 has half of charging current, like 1.5 A, and RT2 has another half charging current, total loss of H5 bridge is  $4.5R_{\text{tank}}$ . Conduction loss is reduced about 50%.

**2) Easy Realization of ZVS:** In a different perspective, with the same circulating power loss, the following assumption should hold:

$$I_{m1}^2 + I_{m2}^2 = I_{m,\text{conv}}^2. \quad (50)$$

Accordingly, the following relationship is derived:

$$(I_{m1} + I_{m2}) > \sqrt{I_{m1}^2 + I_{m2}^2} = \sqrt{I_{m,\text{conv}}^2} = I_{m,\text{conv}}. \quad (51)$$

Since  $I_{m1} + I_{m2} > I_{m,\text{conv}}$ , we can judge that the proposed converter enables an easier realization of ZVS.

Similarly, if we limit the circulating loss, like  $9R_{\text{tank}}$ , for the conventional half-bridge *LLC* converter, it provides a device whose  $Q_o = 3t_d/2$ , where  $t_d$  is the deadtime to achieve ZVS. For H5 *LLC*, if RT1 current equals RT2 current, then the total charge will be  $4.24t_d/2$ . The charge is increased about 40%. Thus, the ZVS realization is easier.

**3) Elimination of the Resonant Current Oscillations:** The diode junction capacitance might affect the transformer secondary current. During the commutation process between diodes, the output voltages of both RT1 and RT2 are unclamped. Therefore, an oscillation might occur in  $i_{Lm}$ , which leads to the oscillation in  $i_{Lr}$ . In this article, two series-connected capacitors are installed to clamp the output voltage of RT1 and RT2. Thus, the oscillation is effectively eliminated.

## V. EXPERIMENTAL VERIFICATION

To verify the effectiveness of the proposed converter, a 1-kW, 390V input, 80–450 V output prototype converter for PEV charging applications is designed, as shown in Fig. 12. The specifications and design parameters of the prototype are listed in Table IV.

TABLE IV  
DESIGN PARAMETERS OF THE PROTOTYPE

Symbol	Quantity	Parameters
$V_{in}$	Input voltage	390 V
$V_o$	Output voltage	80 – 450 V
$L_{m1}, L_{m2}$	Magnetizing inductance	287 $\mu$ H, 264 $\mu$ H
$L_{r1}, L_{r2}$	Resonant inductance	78 $\mu$ H, 58 $\mu$ H
$C_{r1}, C_{r2}$	Resonant capacitance	32 nF, 44 nF
$n_1, n_2$	Turns ratio	2.6, 1.6
$Q_{1-6}$	MOSFET switch	SCT3120AL
$D_{1-4}$	Rectifier diode	C3D10060A
$f_r$	Resonant frequency	100 kHz
$f_s$	Switching frequency	70 – 130 kHz
$C_o, C_{o1}, C_{o2}$	Output filter capacitor	1 $\mu$ F, 1 $\mu$ F, 100 $\mu$ F

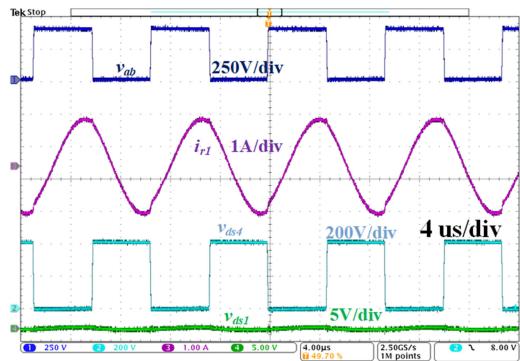


Fig. 13. Steady-state waveforms in mode 1 with  $V_o = 84$  V and  $P_o = 40$  W.

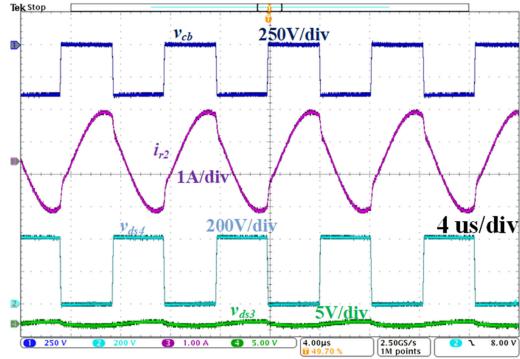


Fig. 14. Steady-state waveforms in mode 2 with  $V_o = 120$  V and  $P_o = 80$  W.

The steady-state waveforms in mode 1 are shown in Fig. 13. In this mode,  $v_{ab}$  is a two-level square wave (0–390 V). RT1 operates in the half-bridge mode.  $S_1$  is always ON. There is no power transferred via RT2.

The steady-state waveforms in mode 2 are shown in Fig. 14. In this mode,  $v_{cb}$  is a two-level square wave (−390 to 0 V). RT2 operates in the half-bridge mode.  $S_3$  is always ON. There is no power transferred via RT1.

The steady-state waveforms in mode 3 are shown in Fig. 15. In this mode,  $v_{ab}$  and  $v_{cb}$  are both two-level square waves (0–390 V, and −390 to 0 V). Both resonant tanks operate in the half-bridge

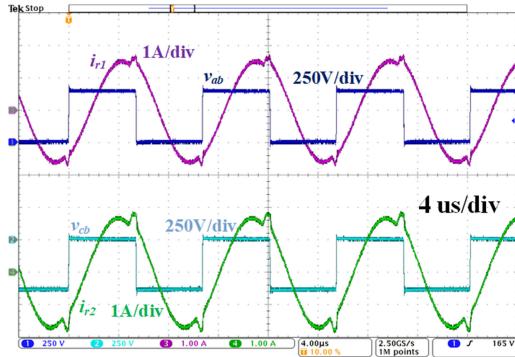


Fig. 15. Steady-state waveforms in mode 3 with  $V_o = 222$  V and  $P_o = 280$  W.

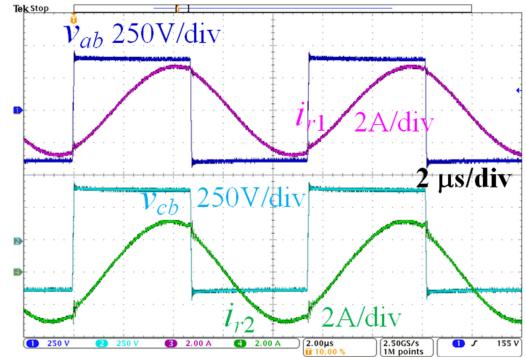


Fig. 18. Steady-state waveforms in mode 6 with  $V_o = 420$  V and  $P_o = 1000$  W.

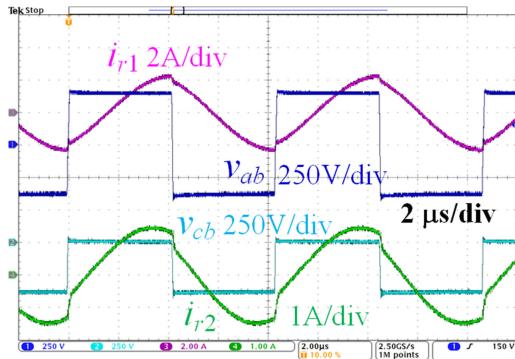


Fig. 16. Steady-state waveforms in mode 4 with  $V_o = 280$  V and  $P_o = 440$  W.

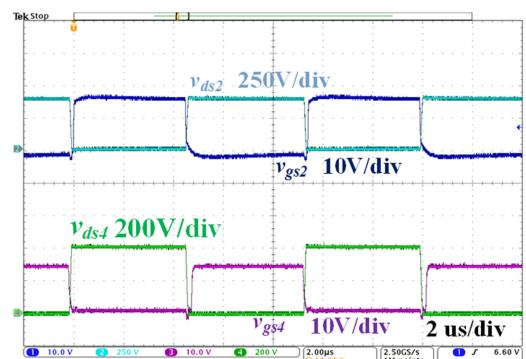


Fig. 19. Steady-state waveforms in mode 1 with  $P_o = 100$  W.

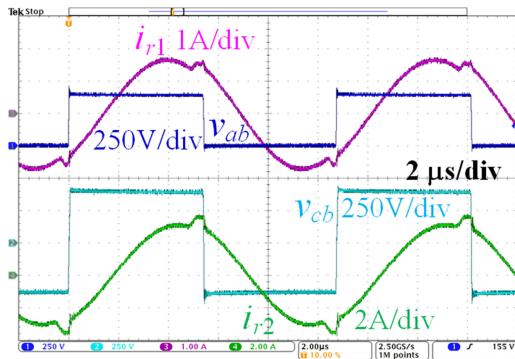


Fig. 17. Steady-state waveforms in mode 5 with  $V_o = 354$  V and  $P_o = 710$  W.

mode. Due to the different turns ratios in two transformers,  $i_{r2}$  is slightly larger than  $i_{r1}$  and RT2 delivers more power than RT1.

The steady-state waveforms in mode 4 are shown in Fig. 16. In this mode,  $v_{ab}$  and  $v_{cb}$  are both two-level square waves ( $-390$  to  $390$  V, and  $-390$  to  $0$  V). RT1 operates in the full-bridge mode, and RT2 operates in the half-bridge mode. Since  $v_{ab,\text{rms}}$  is  $2v_{cb,\text{rms}}$ , RT1 delivers more power than RT2 and  $i_{r1}$  is larger than  $i_{r2}$ .

The steady-state waveforms in mode 5 are shown in Fig. 17. In this mode,  $v_{ab}$  and  $v_{cb}$  are both two-level square waves ( $0$ – $390$  V, and  $-390$  to  $390$  V). RT1 operates in the half-bridge

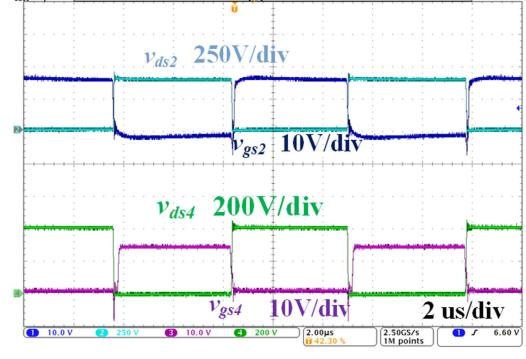


Fig. 20. Steady-state waveforms in mode 4 with  $P_o = 500$  W.

mode, and RT2 operates in the full-bridge mode. In this mode, RT2 delivers more power than RT1 and  $i_{r2}$  is larger than  $i_{r1}$ .

The steady-state waveforms in mode 6 are shown in Fig. 18. In this mode,  $v_{ab}$  and  $v_{cb}$  are both two-level square waves ( $-390$  to  $390$  V, and  $-390$  to  $390$  V). Both resonant tanks operate in the full-bridge mode. Similarly, due to the different turns ratios,  $i_{r2}$  is slightly larger than  $i_{r1}$  and RT2 delivers more power than RT1.

The steady-state waveforms at different loads are shown in Figs. 19–21. From the captured  $v_{ds}$  and  $v_{gs}$ , it can be seen that the primary-side MOSFETs' ZVS are achieved over the entire load range.

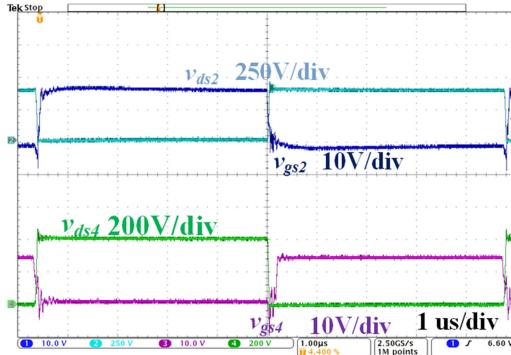
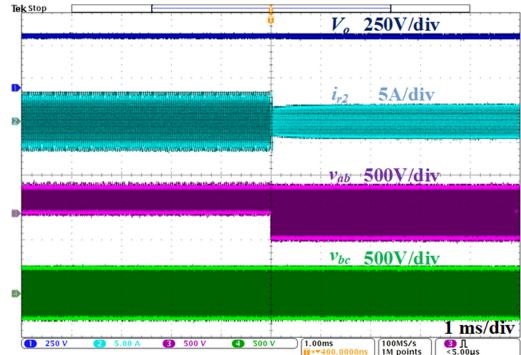
Fig. 21. Steady-state waveforms in mode 6 with  $P_o = 1000$  W.

Fig. 24. Transition from mode 5 to mode 6.

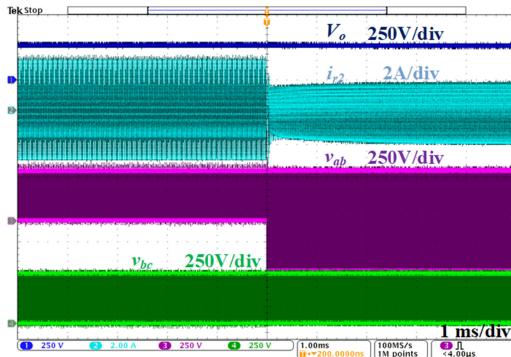


Fig. 22. Transition from mode 3 to mode 4.

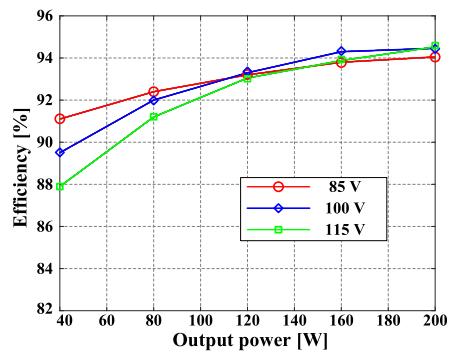


Fig. 25. Measured efficiency curves in mode 1.

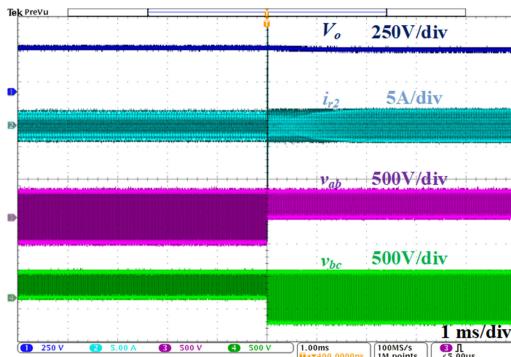


Fig. 23. Transition from mode 4 to mode 5.

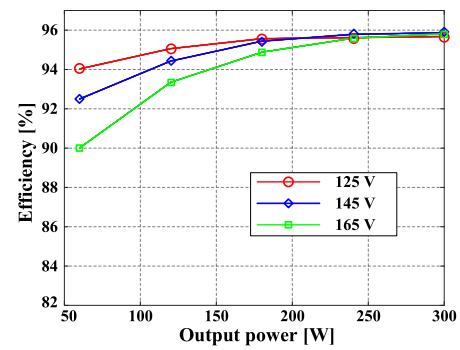


Fig. 26. Measured efficiency curves in mode 2.

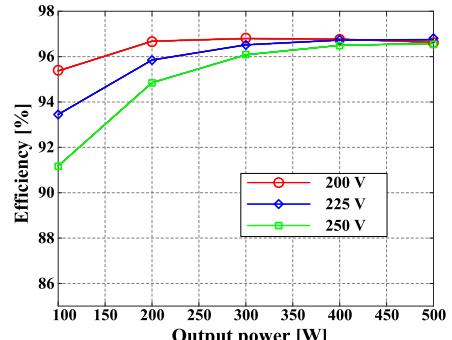


Fig. 27. Measured efficiency curves in mode 3.

The transition waveforms from mode 3 to mode 4, mode 4 to mode 5, and mode 5 to mode 6 are shown in Figs. 22–24, respectively. It can be seen that a general smooth mode transition can be achieved between different adjacent modes.

The measured efficiency data in modes 1–6 with different output voltages are plotted in Figs. 25–30. As shown in the figures, the proposed converter demonstrates 97.05% peak efficiency. An ultrawide output voltage range is achieved. The designed prototype demonstrates good efficiency performance over the ultrawide output voltage range. SiC Schottky diodes (C3D10060A) with zero reverse recovery are employed. Thus,  $f_s$  slightly higher than  $f_r$  is tolerated, as it improves the overall efficiency over the ultrawide voltage range.

**TABLE V**  
COMPARISON WITH EXISTING WIDE OUTPUT VOLTAGE RANGE CONVERTERS

References	LLC [30]	Interleaved LLC [15]	HB-2LLC [24]	SA-VSR [31]	FFPS LLC [32]	Proposed
Modulation	PFM	Phase shift + PFM	PFM	PFM + PWM	Phase shift + PFM	PFM
Main control variable	Switching frequency					
Auxiliary control variable	N/A	Phase shift	Mode status	Duty cycle	Phase shift	Mode status
High frequency MOSFETs	4	8	2	6	4	5
Diodes	2	6	4	2	4	4
Control complexity	Low	High	Medium	High	High	Medium
Input voltage (V)	400	390~410	400	390~410	400	390
Output voltage (V)	50~100	150~500	100~420	100~500	120~180	80~450
$L_m$ ( $\mu$ H)	108	430	151.2	400	154	287
Frequency range (kHz)	120~180	45~100	102~236	70~150	100~200	70~130
Peak efficiency	94.5%	98%	95.21%	95.38%	96.5%	97.05%
Rated power	3 kW	3.5 kW	1.5 kW	1.5 kW	3 kW	1 kW

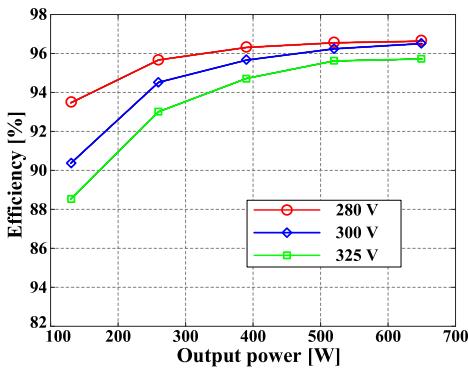


Fig. 28. Measured efficiency curves in mode 4.

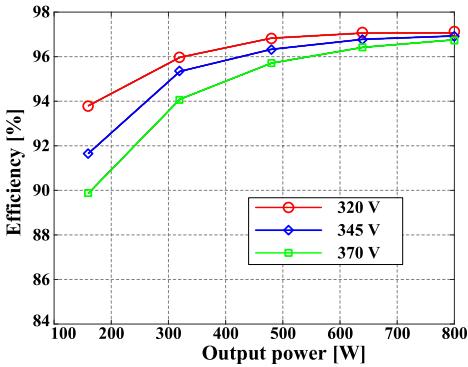


Fig. 29. Measured efficiency curves in mode 5.

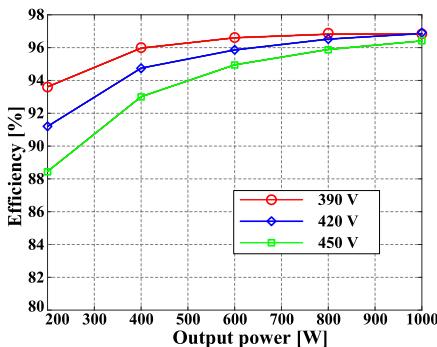


Fig. 30. Measured efficiency curves in mode 6.

A comparison among the proposed topology and some recently reported wide output range topologies is made [15], [24], [30]–[32], and it is summarized in Table V. The proposed topology demonstrates simple pulse-frequency modulation (PFM) modulation, moderate MOSFETs/diodes count, ultrawide output voltage range, narrow frequency band, and good peak efficiency.

## VI. CONCLUSION

In this article, a novel H5-bridge-based asymmetric LLC resonant converter was proposed. This converter is suitable for wide output voltage applications, including PEV onboard chargers. The H5 inverter bridge was reconfigurable. Therefore, two asymmetric LLC resonant tanks could operate in idle, half-bridge, hybrid-bridge, and full-bridge modes. Correspondingly, six modes with a scaled voltage gain profile were obtained. The output voltage range was effectively expanded with moderate  $L_m$  and squeezed  $f_s$  range. Hence, the drawbacks caused by small  $L_m$  and wide  $f_s$  range were avoided. The proposed resonant converter's operating principles, circuit modeling, and key design consideration were detailed. The uniqueness of the proposed converter in comparison with the conventional LLC resonant converter was analyzed.

To validate the proposed concept, a 1-kW rated prototype with 390 V input and 80–450 V output was built and tested. With 100 kHz  $f_r$ , the designed converter had its  $f_s$  constrained in the range of 70–130 kHz. The primary-side MOSFETs could achieve ZVS from 10% load to full load. The designed prototype demonstrated 97.05% peak efficiency and good efficiency over the wide output voltage range. The experimental results validate the effectiveness of the proposed converter in wide output voltage range applications.

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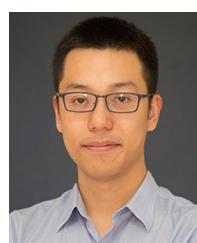
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