

### Introduction

Statistical hypothesis	Statistical hypothesis testing
a hypothesis that is testable on the basis of observed data modeled as the realized values taken by a collection of random variables	a statistical way of testing the assumption regarding a popular parameter

### steps of formulating a hypothesis

1. state the two hypothesis: **Null hypothesis** and **Alternative hypothesis**
2. set the **significance levels** usually  $\alpha = 0.05$
3. carrying out the hypothesis testing and calculate the test statistics and corresponding **P-value**
4. compare P-value with significance levels and then decide to accept or reject null hypothesis

### Errors in Testing

Error Types	Description	denotation	correct inference
Type I error	<b>Reject</b> null when null is true	$\alpha = P(\text{Type I error})$	$1 - \alpha$ (significance level)
Type II error	<b>Not</b> reject null when null is false	$\beta = P(\text{Type II error})$	$1 - \beta$ (= power)

### Chi-Square Test

Types	Description
Test for independence	tests for the independence of two categorical variables
Homogeneity of Variance	test if more than two subgroups of a population share the same multivariate distribution
goodness of fit	whether a multinomial model for the population distribution ( $P_1, \dots, P_m$ ) fits our data

Test for independence and homogeneity of variance share the same test statistics and degree of freedoms by different design of experiment

### Assumptions

1. one or two categorical variables
2. independent observations
3. outcomes mutually exclusive
4. large n and no more than 20% of expected counts  $< 5$

### F-test

Anova Analysis	comparing the means of two or more continuous populations
One-way layout	A test that allows one to make comparisons between the means of two or more groups of data.
two-way layout	A test that allows one to make comparisons between the means of two or more groups of data, where two independent variables are considered.

#### Assumptions about data:

1. each data y is normally distributed
2. the variance of each treatment group is same
3. all observations are independent

### T-test

Types	Hypothesis
<b>Two Sample T-test</b>	If two independent groups have different mean
<b>Paired T-test</b>	if one groups have different means at different times
<b>One Sample T-test</b>	mean of a single group against a known mean

#### Assumptions about data

1. independent
2. normally distributed
3. have a similar amount of variance within each group being compared

### One sample T-test

$$t = \frac{m - \mu}{s/\sqrt{n}}$$

where

m = the mean of sample

s = standard deviation of sample

degree of freedom = n - 1

### Paired T-test statistics

$$t = \frac{m}{s/\sqrt{n}}$$

where

m = the mean of differences between two paired sets of data

n = size of differences

s = the standard deviation of differences between two paired sets of data

degree of freedom = n - 1

### Independent two-sample T-test statistics

$$t = \frac{m_A - m_B}{\sqrt{\frac{s_A^2}{n_A} + \frac{s_B^2}{n_B}}}$$

where

m = the means of group A and B respectively

n = the sizes of group A and B respectively

degrees of freedom = n<sub>A</sub> + n<sub>B</sub> - 2 (given two samples have the same variance)

### Test of independence and Homogeneity of variance

$$\chi^2 = \sum [(O_{r,c} - E_{r,c})^2 / E_{r,c}]$$

where

E<sub>r,c</sub> = (N<sub>r</sub> \* N<sub>c</sub>)/n

df = (r - 1) \* (c - 1)

c = column number

r = row number

### Goodness of fit test

$$\chi^2 = \sum \frac{(O_i - E_i)^2}{E_i}$$

where:

O = observed value of data

E = expected value of data

k = dimension of parameter

df = n - 1 - k

### Carrying out one-way anova test

SST total variance sum(Y<sub>ij</sub> - overall mean of Y)<sup>2</sup>

SSW intra-group variance sum(mean of each observations across different treatments - mean of each treatment)<sup>2</sup>

SSB inter-group variance sum(mean of each treatments - overall mean of Y)<sup>2</sup>

Null hypothesis: the differentiated effect in each treatment group is 0

Alternative hypothesis: not all differentiated effect is 0

SST = SSW + SSB

test statistics:

F<sub>i-1, i(j-1)</sub> = SSB/(I-1)/SSW/I(J-1)

where

I = number of different treatments

J = number of observations within each treatment