ECON 210C PROBLEM SET # 3

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1. Variable labor supply in the RBC model

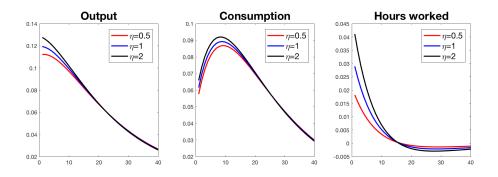


Figure 1. Impulse responses with varying η

	$\eta = 0.5$	$\eta = 1$	$\eta = 2$	Data
σ_Y	1.54	1.64	1.74	1.72
σ_C	0.97	1.02	1.08	1.27
σ_L	0.23	0.37	0.53	1.59

Table 1. Response to a transitory discount factor shock

Larger Frisch elasticity values imply a better fit, as they generate stronger inter-temporal substitution of labor supply, amplifying the effect of shocks. Consumption is still too smooth, and the volatility of hours is too low.

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2. VARIABLE CAPITAL UTILIZATION IN AN RBC MODEL

(a). Firms choose capital utilization U, capital K, and labor demand N.

The production function that we can use directly (since the output is the numeraire) is

$$Y_t = (U_t K_{t-1})^{\alpha} (Z_t N_t)^{1-\alpha}$$

and since the firms own capital, they face the constraint

$$K_t = I_t + (1 - \delta(U_t))K_{t-1}$$

but they also have to pay wages W_tN_t and invest I_t so we can set up the Lagrangian

$$\mathcal{L} = E \sum_{s} \left(\prod_{k=1}^{s} (1 + r_{t+k})^{-1} \right) \left(\left(U_{t+s} K_{t+s-1} \right)^{\alpha} \left(Z_{t+s} N_{t+s} \right)^{1-\alpha} - W_{t+s} N_{t+s} - I_{t+s} + q_{t+s} \left(-K_{t+s} + I_{t+s} + \left(1 - \delta (U_{t+s}) \right) K_{t+s-1} \right) \right) \left(\left(U_{t+s} K_{t+s-1} \right)^{\alpha} \left(Z_{t+s} N_{t+s} \right)^{1-\alpha} - W_{t+s} N_{t+s} - I_{t+s} + q_{t+s} \left(-K_{t+s} + I_{t+s} + \left(1 - \delta (U_{t+s}) \right) K_{t+s-1} \right) \right) \right) \left(\left(U_{t+s} K_{t+s-1} \right)^{\alpha} \left(Z_{t+s} N_{t+s} \right)^{1-\alpha} - W_{t+s} N_{t+s} - I_{t+s} + q_{t+s} \left(-K_{t+s} + I_{t+s} + \left(1 - \delta (U_{t+s}) \right) K_{t+s-1} \right) \right) \right) \right) \left(\left(U_{t+s} K_{t+s-1} \right)^{\alpha} \left(Z_{t+s} N_{t+s} \right)^{1-\alpha} - W_{t+s} N_{t+s} - I_{t+s} + q_{t+s} \left(-K_{t+s} + I_{t+s} + \left(1 - \delta (U_{t+s}) \right) K_{t+s-1} \right) \right) \right) \right) \right) \left(\left(U_{t+s} K_{t+s-1} \right)^{\alpha} \left(Z_{t+s} N_{t+s} \right)^{1-\alpha} - W_{t+s} N_{t+s} - I_{t+s} + q_{t+s} \left(-K_{t+s} + I_{t+s} + \left(1 - \delta (U_{t+s}) \right) K_{t+s-1} \right) \right) \right) \right) \right) \right) \right) \left(V_{t+s} K_{t+s-1} \right) \left(V_{t+s} K_{t+s-1} \right)^{\alpha} \left(Z_{t+s} N_{t+s} \right) \right) \left(V_{t+s} K_{t+s-1} \right) \left(V_{t+s} K_{t+s-1} \right)^{\alpha} \left(Z_{t+s} N_{t+s} \right) \left(V_{t+s} K_{t+s-1} \right)^{\alpha} \left(Z_{t+s} N_{t+s} \right) \right) \right) \left(V_{t+s} K_{t+s-1} \right) \left(V_{t+s} K_{t+s-1} \right) \left(V_{t+s} K_{t+s-1} \right) \left(V_{t+s} K_{t+s-1} \right)^{\alpha} \left(Z_{t+s} N_{t+s-1} \right) \right) \left(V_{t+s} K_{t+s-1} \right) \left(V_{t+s} K_{$$

so we have first order conditions:

for labor we have

$$W_{t} = (1 - \alpha)(U_{t}K_{t-1})^{\alpha} Z_{t}^{1-\alpha} N_{t}^{-\alpha}$$

for investment we have

$$q_t = 1$$

for capital at time t we have

$$q_t = E \left[\frac{1}{1 + r_{t+1}} \left(\alpha U_{t+1}^{\alpha} K_t^{\alpha - 1} (Z_{t+1} N_{t+1})^{1 - \alpha} + q_{t+1} (1 - \delta(U_{t+1})) \right) \right]$$

and finally we have the condition for utilization

$$\alpha U_t^{\alpha - 1} K_{t-1}^{\alpha} (Z_t N_t)^{1-\alpha} = q_t K_{t-1} \delta'(U_t)$$

Combining the investment and capital optimality conditions yields the expression for the rental rate of capital.

$$R_{t+1} = \alpha U_{t+1}^{\alpha} K_t^{\alpha - 1} (Z_{t+1} N_{t+1})^{1 - \alpha} - \delta(U_{t+1})$$

The rental rate depends on utilization because the marginal product of capital and its depreciation rate depend on utilization.

(b). The log linearized version of the utilization optimality condition

$$q_t \delta'(U_t) K_{t-1} = \alpha U_t^{\alpha - 1} K_{t-1}^{\alpha} \left(Z_t N_t \right)^{1 - \alpha}$$

is

$$\check{q_t} + \frac{\delta''(\bar{U})\bar{U}}{\delta'(\bar{U})}\check{U_t} + \check{K}_{t-1} = (\alpha - 1)\check{U_t} + \alpha \check{K_{t-1}} + (1 - \alpha)\left(\check{Z_t} + \check{N_t}\right)$$

We know $\check{q}_t = 0$ from the investment optimality condition and we also know

$$\check{Y}_{t} = \alpha \left(\check{U}_{t} + \check{K_{t-1}} \right) + (1 - \alpha) \left(\check{Z}_{t} + \check{N}_{t} \right)$$

because the production function is given, so we have

$$\check{U}_t = \frac{1}{1+\Lambda} \left(\check{Y}_t - \check{K}_{t-1} \right)$$

(c). The log-linearized production function is

$$\dot{Y}_{t} = \alpha \left(\dot{U}_{t} + K_{t-1}^{\dagger} \right) + (1 - \alpha) \left(\dot{Z}_{t} + \dot{N}_{t} \right)
= \frac{\alpha}{1 + \Delta} \left(\dot{Y}_{t} - K_{t-1}^{\dagger} \right) + \alpha K_{t-1}^{\dagger} + (1 - \alpha) \left(\dot{Z}_{t} + \dot{N}_{t} \right)$$

Isolate \check{Y}_t :

$$\check{Y}_t = \frac{\Delta \alpha}{1 + \Delta - \alpha} \check{K}_{t-1} + \frac{(1 + \Delta)(1 - \alpha)}{1 + \Delta - \alpha} \left(\check{Z}_t + \check{N}_t \right)
= \check{Z}_t + \check{N}_t \quad \text{(when } \Delta = 0)
= \alpha \check{K}_{t-1} + (1 - \alpha) \left(\check{Z}_t + \check{N}_t \right) \quad \text{(when } \Delta = \infty)$$

 $\Delta = 0$ implies the capital stock is impotent, and output thus only depends on technology and labor. $\Delta = \infty$ implies full utilization, so output depends on all three inputs, with weights equal to the Cobb-Douglas coefficients.

In every other case, we have

$$\check{Y}_{t} = \frac{\Delta \alpha}{1 + \Delta - \alpha} \check{K}_{t-1} + (1 - \alpha) \left(\check{Z}_{t} + \check{N}_{t} \right) + \frac{\alpha (1 - \alpha)}{1 + \Delta - \alpha} \left(\check{Z}_{t} + \check{N}_{t} \right)$$

so Z_t and N_t in Y_t matter relatively more (with capital not being fully utilized) relative to the $\Delta = \infty$ case.

3. Homework in Macroeconomics

(a). The Lagrangian for the household's maximization problem is:

$$\mathcal{L} = \left(C_m^{\rho} + C_h^{\rho}\right)^{\frac{1}{\rho}} - \left(\frac{1}{\eta} + 1\right)^{-1} \left(L_h + L_m\right)^{\frac{1}{\eta} + 1} + \lambda \left(WL_m - C_m\right) + \xi \left(L_h - C_h\right)$$

The first order conditions for the interior solutions are:

$$\frac{1}{\rho} \left(C_m^{\rho} + C_h^{\rho} \right)^{\frac{1}{\rho} - 1} \rho C_m^{\rho - 1} = \lambda$$

$$\frac{1}{\rho} \left(C_m^{\rho} + C_h^{\rho} \right)^{\frac{1}{\rho} - 1} \rho C_h^{\rho - 1} = \xi$$

$$\left(L_h + L_m \right)^{\frac{1}{\eta}} = \lambda W$$

$$\left(L_h + L_m \right)^{\frac{1}{\eta}} = \xi$$

(b). From the two first order conditions for labor, we have

$$\mathcal{E} = \lambda W$$

(c). From the two first order conditions for consumption, we have

$$\xi = \lambda \left(\frac{C_h}{C_m}\right)^{\rho - 1}$$

(d). With the budget constraints binding, we have

$$C_h = L_h$$

and from above we get

$$C_h = C_m W^{\frac{1}{\rho - 1}}$$

(e). We now have

$$L_h = C_m W^{\frac{1}{\rho - 1}}$$

and we can assume the budget constraint holds for formal markets to make the substitution

$$C_m = WL_m$$

getting us

$$L_h = W L_m W^{\frac{1}{\rho - 1}}$$

equivalent to

$$L_h = L_m W^{\frac{\rho}{\rho - 1}}$$

and from our first order conditions we have

$$L_h + L_m = (\lambda W)^{\eta}$$

so we can substitute for L_h to get

$$(\lambda W)^{\eta} - L_m = L_m W^{\frac{\rho}{\rho - 1}}$$

so we have

$$L_m(1+W^{\frac{\rho}{\rho-1}})=(\lambda W)^{\eta}$$

and thus

$$L_m = \frac{(\lambda W)^{\eta}}{(1 + W^{\frac{\rho}{\rho - 1}})}$$

(f). We now have

$$\frac{\partial L_h}{\partial W} = \frac{(1 + W^{\frac{\rho}{\rho - 1}})\lambda^{\eta}\eta W^{\eta - 1} - (\lambda W)^{\eta}(\frac{\rho}{\rho - 1})W^{\frac{\rho}{\rho - 1} - 1}}{(1 + W^{\frac{\rho}{\rho - 1}})^2}$$

with

$$\frac{\partial L_m}{\partial W} \cdot \frac{W}{L_m} = \frac{(1 + W^{\frac{\rho}{\rho-1}})\eta - (\frac{\rho}{\rho-1})W^{\frac{\rho}{\rho-1}}}{(1 + W^{\frac{\rho}{\rho-1}})}$$

as the elasticity of L_h with respect to W.

(g). If home production can perfectly substitute for market production, then when wages are lower than the value of the home produced goods, labor will not be supplied to markets. As ρ gets smaller, the Frisch elasticity approaches η . With no substitution, the Frisch elasticity equals η exactly.

(h). We had

$$(C_m^{\rho} + C_h^{\rho})^{\frac{1}{\rho} - 1} C_m^{\rho - 1} = \lambda$$

so substitute the budget constraints

$$((WL_m)^{\rho} + L_h^{\rho})^{\frac{1}{\rho} - 1} (WL_m)^{\rho - 1} = \lambda$$

and use the substitution

$$L_h = L_m W^{\frac{\rho}{\rho - 1}}$$

to get

$$((WL_m)^{\rho} + (W^{\frac{\rho^2}{\rho-1}})L_m^{\rho})^{\frac{1}{\rho}-1}(WL_m)^{\rho-1} = \lambda$$

so now substitute back in to

$$L_m = \frac{(\lambda W)^{\eta}}{(1 + W^{\frac{\rho}{\rho - 1}})}$$

and we have

$$L_m = \frac{\left[((WL_m)^{\rho} + (W^{\frac{\rho^2}{\rho - 1}})L_m^{\rho})^{\frac{1}{\rho} - 1}(WL_m)^{\rho - 1} \right]^{\eta} W^{\eta}}{(1 + W^{\frac{\rho}{\rho - 1}})}$$

and we can simplify to get

$$L_m = \frac{\left[((W^{\rho} + W^{\frac{\rho^2}{\rho - 1}}) L_m^{\rho})^{\frac{1}{\rho} - 1} (W L_m)^{\rho - 1} \right]^{\eta} W^{\eta}}{(1 + W^{\frac{\rho}{\rho - 1}})}$$

and again to get

$$L_m = \frac{\left[(W^{\rho} + W^{\frac{\rho^2}{\rho - 1}})^{\frac{1}{\rho} - 1} L_m^{1 - \rho} (W L_m)^{\rho - 1} \right]^{\eta} W^{\eta}}{(1 + W^{\frac{\rho}{\rho - 1}})}$$

and the L_m terms on the right side cancel so we have

$$L_m = \frac{\left[(W^{\rho} + W^{\frac{\rho^2}{\rho - 1}})^{\frac{1}{\rho} - 1} W^{\rho - 1} \right]^{\eta} W^{\eta}}{(1 + W^{\frac{\rho}{\rho - 1}})}$$

and we can rewrite the numerator to get

$$L_m = \frac{\left[(W^{\rho} + W^{\frac{\rho^2}{\rho - 1}})^{\frac{1}{\rho} - 1} W^{\rho} \right]^{\eta}}{(1 + W^{\frac{\rho}{\rho - 1}})}$$

equivalent to

$$L_m = \frac{\left[(W^{\rho} (1 + W^{\frac{\rho}{\rho - 1}}))^{\frac{1}{\rho} - 1} W^{\rho} \right]^{\eta}}{(1 + W^{\frac{\rho}{\rho - 1}})}$$

and

$$L_m = \frac{\left[(1 + W^{\frac{\rho}{\rho - 1}})^{\frac{1}{\rho} - 1} W^{1 - \rho} W^{\rho} \right]^{\eta}}{(1 + W^{\frac{\rho}{\rho - 1}})}$$

and

$$L_m = \frac{\left[(1 + W^{\frac{\rho}{\rho - 1}})^{\frac{1}{\rho} - 1} W \right]^{\eta}}{(1 + W^{\frac{\rho}{\rho - 1}})}$$

to finally get

$$L_m = \left(1 + W^{\frac{\rho}{\rho - 1}}\right)^{\eta \left(\frac{1 - \rho}{\rho}\right) - 1} W^{\eta}$$

(i). Differentiating, we have

$$\frac{\partial L_m}{\partial W} = \frac{\rho \left(\frac{\eta(1-\rho)}{\rho} - 1\right) W^{\eta + \frac{\rho}{\rho-1} - 1} \left(W^{\frac{\rho}{\rho-1}} + 1\right)^{\frac{\eta(1-\rho)}{\rho} - 2}}{\rho - 1} + \eta W^{\eta - 1} \left(W^{\frac{\rho}{\rho-1}} + 1\right)^{\frac{\eta(1-\rho)}{\rho} - 1}$$

and we have the elasticity as

$$\frac{\partial L_m}{\partial W} \cdot \frac{W}{L_m} = \frac{\rho \left(\frac{\eta(1-\rho)}{\rho} - 1\right) W^{\frac{\rho}{\rho-1}} \left(W^{\frac{\rho}{\rho-1}} + 1\right)^{-1}}{\rho - 1} + \eta$$

which simplifies to

$$\frac{\partial L_m}{\partial W} \cdot \frac{W}{L_m} = \eta + \frac{\rho \left(\eta \left(\frac{1}{\rho} - 1 \right) - 1 \right)}{(\rho - 1) \left(W^{\frac{\rho}{1 - \rho}} + 1 \right)}$$

(j). Very low values of ρ , implying high elasticity between market and home consumption, can help deliver the high labor supply elasticity.

4. q-Theory with Variable Capital Utilization

(a). Firms choose utilization, investment, and labor to maximize the expected value of

$$\sum_{s} \left(\prod_{k=1}^{s} \left(1 + r_{t+k} \right) \right)^{-1} \times Z_{t+s} \left(U_{t+s} K_{t+s-1} \right)^{\alpha} L_{t+s}^{1-\alpha} - W_{t+s} L_{t+s} - I_{t+s} \left[1 + \phi \left(\frac{I_{t+s}}{K_{t+s-1}} \right) \right]$$

given the constraints

$$(-K_{t+s} + (1 - \delta(U_t))K_{t+s-1} + I_{t+s}) = 0$$

This problem is truly dynamic because the adjustment cost links the present and future period investment decisions.

(b). The first order conditions are

$$\begin{split} &\frac{\partial \mathcal{L}}{\partial L_t}: \quad w_t = (1-\alpha)\frac{Y_t}{L_t} \\ &\frac{\partial \mathcal{L}}{\partial L_t}: \quad q_t = 1 + \phi\bigg(\frac{I_t}{K_t}\bigg) + \frac{I_t}{K_t}\phi'\bigg(\frac{I_t}{K_t}\bigg) \\ &\frac{\partial \mathcal{L}}{\partial K_t}: \quad q_t = (1+r_{t+1})^{-1}\bigg(\alpha\frac{Y_{t+1}}{K_{t+1}} + \frac{I_{t+1}^2}{K_{t+1}^2}\phi'\bigg(\frac{I_t}{K_t}\bigg) + q_{t+1}(1-\delta(U_{t+1}))\bigg) \\ &\frac{\partial \mathcal{L}}{\partial U_t}: \quad \alpha\frac{Y_t}{U_t} = q_t\delta'(U_t)K_t \end{split}$$

Combining the second and third equations, we can get an expression for the rental rate of capital:

$$r_{t+1} = \alpha \frac{Y_{t+1}}{K_{t+1}} + \frac{I_{t+1}^2}{K_{t+1}^2} \phi' \left(\frac{I_t}{K_t}\right) + \delta(U_{t+1})$$

The rental rate of capital is a function of utilization because the depreciation rate and the marginal product of capital depend on utilization. It is also a function of q because

5. FISCAL MULTIPLIER IN THE RBC MODEL

(a). The log-linearized system of equations is

$$\begin{split} \check{K}_t &= (1-\delta) \check{K}_{t-1} + \delta \check{I}_t \\ \check{C}_t + \frac{1}{\eta} \check{L}_t &= \check{Y}_t - \check{L}_t \\ E_t \check{C}_{t+1} - \check{C}_t &= \frac{\alpha \frac{\bar{Y}}{\bar{K}}}{\alpha \frac{\bar{Y}}{\bar{K}} + (1-\delta)} (E_t \check{Y}_{t+1} - \check{K}_t) \\ \check{Y}_t &= \alpha \check{K}_{t-1} + (1-\alpha) \check{L}_t \\ \check{Y}_t &= \frac{\bar{C}}{\bar{Y}} \check{C}_t + \frac{\bar{I}}{\bar{Y}} \check{I}_t + \frac{\bar{G}}{\bar{Y}} \check{G}_t \\ \check{G}_t &= \rho_g \check{G}_{t-1} + \epsilon_t^g \end{split}$$

Guess that the policy functions take the form

$$\dot{C}_t = v_{CK} \check{K}_{t-1} + v_{CG} \check{G}_t
\dot{K}_t = v_{KK} \check{K}_{t-1} + v_{KG} \check{G}_t$$

Now plug the policy functions into the system of equations and we are left with the log-linearized consumption Euler equation and labor-leisure condition in terms of parameters, coefficients of the policy functions, and state variables:

$$\begin{split} &(v_{CK}v_{KK}-v_{CK})\check{K}_{t-1}+(v_{CK}v_{KG}+v_{CG}\rho_g-v_{CG})\check{G}_t\\ &=\frac{\alpha\frac{\bar{Y}}{\bar{K}}}{\alpha\frac{\bar{Y}}{\bar{K}}+(1-\delta)}\left[\frac{\bar{C}}{\bar{Y}}v_{CK}v_{KK}+\frac{\bar{I}}{\bar{Y}}(v_{KK}-1+\delta)v_{KK}\frac{1}{\delta}-v_{KK}\right]\check{K}_{t-1}\\ &+\frac{\alpha\frac{\bar{Y}}{\bar{K}}}{\alpha\frac{\bar{Y}}{\bar{K}}+(1-\delta)}\left[\frac{\bar{C}}{\bar{Y}}v_{CK}v_{KG}+\frac{\bar{C}}{\bar{Y}}v_{CG}\rho_g+\frac{\bar{I}}{\bar{Y}}(v_{KK}-1+\delta)v_{KG}\frac{1}{\delta}+\frac{\bar{I}}{\bar{Y}}v_{KG}\rho_g\frac{1}{\delta}\right.\\ &+\left.\frac{\bar{G}}{\bar{Y}}\rho_g-v_{KG}\right]\check{G}_t \end{split}$$

$$\left[v_{CK} - \left(\frac{1}{\eta} + 1\right) \frac{\alpha}{1 - \alpha}\right] \check{K}_{t-1} + v_{CG} \check{G}_t = \frac{-\alpha - \frac{1}{\eta}}{1 - \alpha} \left[\frac{\bar{C}}{\bar{Y}} v_{CK} + \frac{\bar{I}}{\bar{Y}} (v_{KK} - 1 + \delta) \frac{1}{\delta}\right] \check{K}_{t-1} + \frac{-\alpha - \frac{1}{\eta}}{1 - \alpha} \left[\frac{\bar{C}}{\bar{Y}} v_{CG} + \frac{\bar{I}}{\bar{Y}} v_{KG} \frac{1}{\delta} + \frac{\bar{G}}{\bar{Y}}\right] \check{G}_t$$

By comparing the coefficients on \check{K}_{t-1} and \check{G}_t in both equations, we obtain 4 equations

$$v_{CK}v_{KK} - v_{CK} = \frac{\alpha \frac{\bar{Y}}{\bar{K}}}{\alpha \frac{\bar{Y}}{\bar{K}} + (1 - \delta)} \left[\frac{\bar{C}}{\bar{Y}} v_{CK} v_{KK} + \frac{\bar{I}}{\bar{Y}} (v_{KK} - 1 + \delta) v_{KK} \frac{1}{\delta} - v_{KK} \right]$$

$$\begin{split} v_{CK}v_{KG} + v_{CG}\rho_g - v_{CG} &= \frac{\alpha\frac{\bar{Y}}{\bar{K}}}{\alpha\frac{\bar{Y}}{\bar{K}} + (1 - \delta)} \left[\frac{\bar{C}}{\bar{Y}} v_{CK}v_{KG} + \frac{\bar{C}}{\bar{Y}} v_{CG}\rho_g \right. \\ &\left. + \frac{\bar{I}}{\bar{Y}} (v_{KK} - 1 + \delta) v_{KG} \frac{1}{\delta} + \frac{\bar{I}}{\bar{Y}} v_{KG}\rho_g \frac{1}{\delta} + \frac{\bar{G}}{\bar{Y}} \rho_g - v_{KG} \right] \end{split}$$

$$v_{CK} - \left(\frac{1}{\eta} + 1\right) \frac{\alpha}{1 - \alpha} = \frac{-\alpha - \frac{1}{\eta}}{1 - \alpha} \left[\frac{\bar{C}}{\bar{Y}} v_{CK} + \frac{\bar{I}}{\bar{Y}} (v_{KK} - 1 + \delta) \frac{1}{\delta} \right]$$

$$v_{CG}\check{G}_t = \frac{-\alpha - \frac{1}{\eta}}{1 - \alpha} \left[\frac{\bar{C}}{\bar{Y}} v_{CG} + \frac{\bar{I}}{\bar{Y}} v_{KG} \frac{1}{\delta} + \frac{\bar{G}}{\bar{Y}} \right] \check{G}_t$$

Solving numerically, we get

$$v_{CK} \approx 0.66$$

 $v_{CG} \approx -0.09$
 $v_{KK} \approx 0.97$
 $v_{KG} \approx -0.01$

(b). The increase in government expenditure is only temporary, and the boost in output is transitory. Households compensate for the increased government expenditure by decreasing consumption, decreasing savings, and increasing labor supply. The households desired level of steady-state capital remains unchanged. This causes MPL (and wages) to decline while MPK (and interest rate) to increase. This is shown in Figure 5.

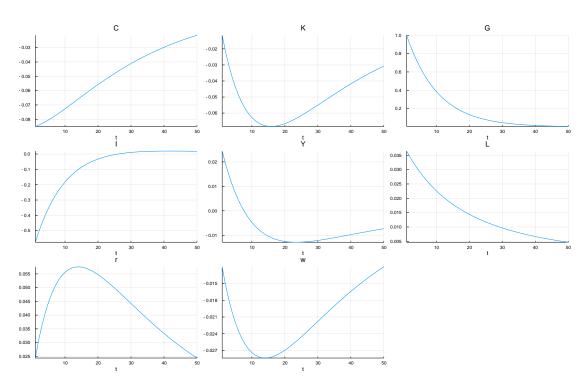


FIGURE 2. Impulse response to a unit shock in government spending.

- (c). The multiplier is about 1.13. The new impulse response is shown in Figure 3.
- (d). We now have

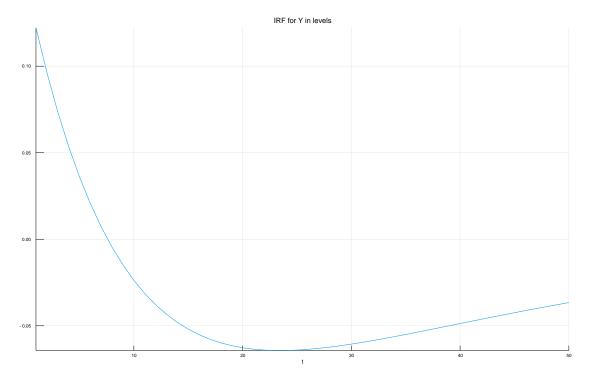


FIGURE 3. Impulse response to a unit shock in government spending in levels.

Solving numerically, we get

$$v_{CK} \approx 0.66$$

 $v_{CG} \approx -0.27$
 $v_{KK} \approx 0.97$
 $v_{KG} \approx 0.003$

Increased output persists, so households decrease consumption and increase labor supply even more as a result of increased savings to get a higher level of steady-state capital. This increase in labor supply causes wages to decline by more and the interest rate to increase more. The level of increase in output is much larger; the multiplier is about 1.4.

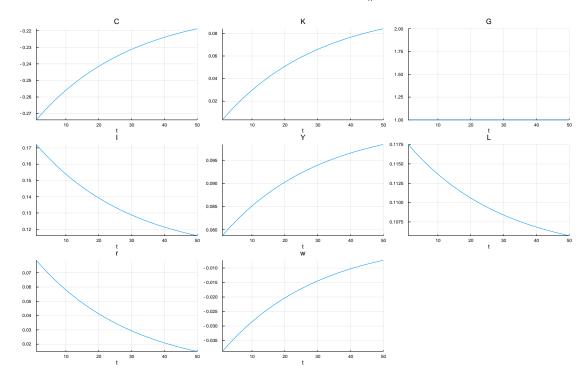


FIGURE 4. Impulse response to the permanent shock

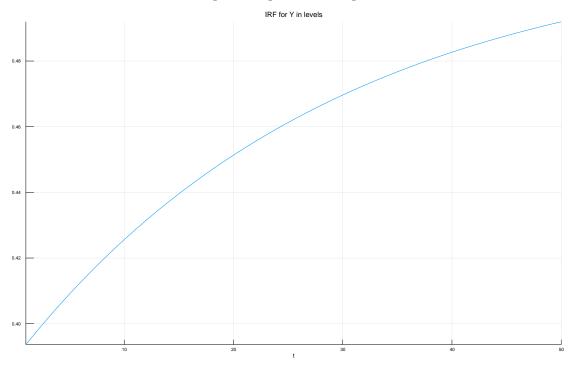


FIGURE 5. Impulse response to the permanent shock in levels