

MSU AEROSPACE STUDENT



Engineering Report Memo

Date: 03/30/2025

From: Mino Razafimino / omr36

To: Robert Wolz, ASE 4721 Lab Instructor

Subject: Airfoil Memo

References:

XFOIL (2013), Massachusetts Institute of Technology, Boston, Massachusetts, web.mit.edu/drela/Public/web/xfoil/

XFLR5 (2024), Massachusetts Institute of Technology, Boston, <https://www.xflr5.tech/xflr5.htm>

The MathWorks Inc. (2022). MATLAB version: 9.13.0 (R2022b), Natick, Massachusetts: The MathWorks Inc.
<https://www.mathworks.com>

In this memo, a NACA 0012 and Wortman airfoil are analyzed computationally. A wind tunnel test is also conducted, and the values of wake pressure are recorded using the wake-rack system. Through the integration of the pressures obtained, the value of the coefficient of drag at different Reynold's numbers for different angles of attack is obtained with the help of MATLAB.

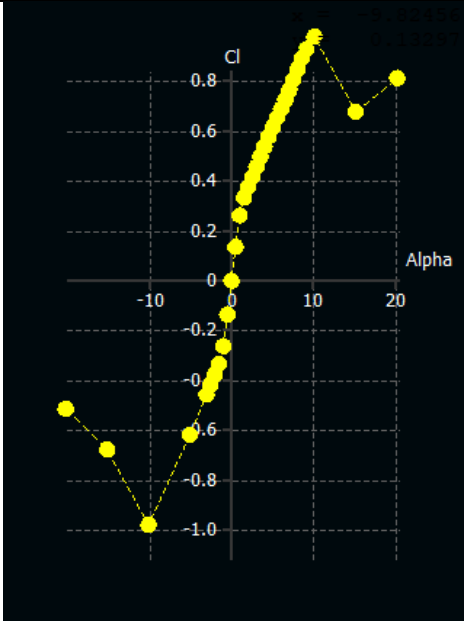
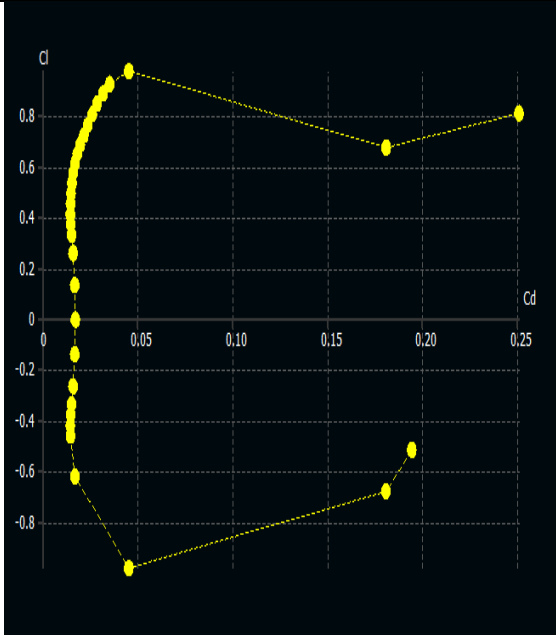
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Discussion:

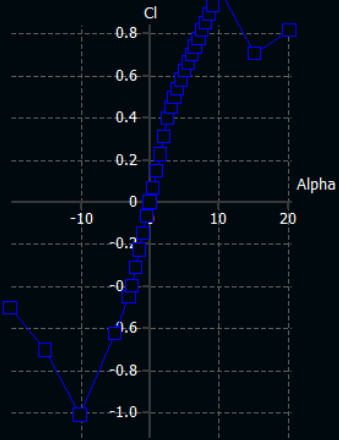

Part 1: NACA 0012 airfoil

Reynold's number	CL vs aplha	Cl vs Cd	L/D max
1e5			38

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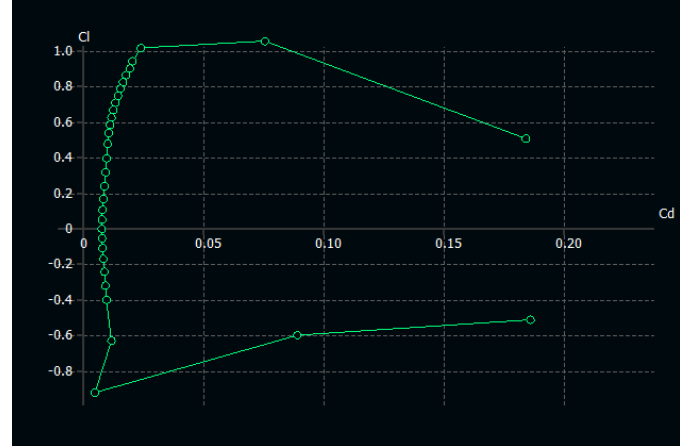
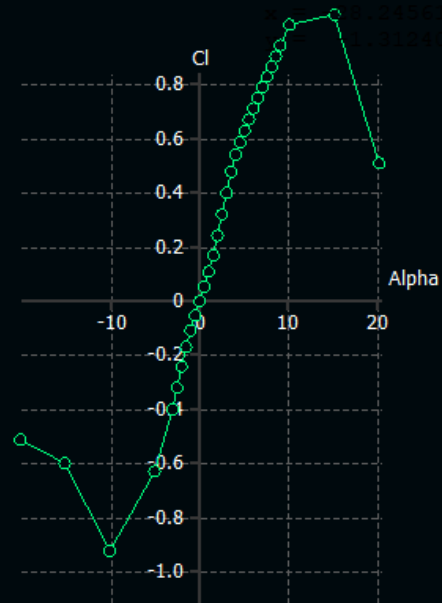
2e5	 <p>A line graph showing the relationship between the lift coefficient (C_l) and the angle of attack (α). The x-axis is labeled 'Alpha' and ranges from -10 to 20. The y-axis is labeled 'C_l' and ranges from -1.0 to 0.8. The data points are connected by a blue line, showing a linear increase in C_l with α up to approximately 10 degrees, after which it begins to curve downwards.</p>		 <p>A line graph showing the relationship between the lift coefficient (C_l) and the drag coefficient (C_d). The x-axis is labeled 'C_d' and ranges from 0 to 0.20. The y-axis is labeled 'C_l' and ranges from -0.8 to 1.0. The data points are connected by a blue line, forming a parabolic shape that opens to the right, with the peak of the parabola at $C_d \approx 0.02$ and $C_l \approx 1.0$.</p>		47
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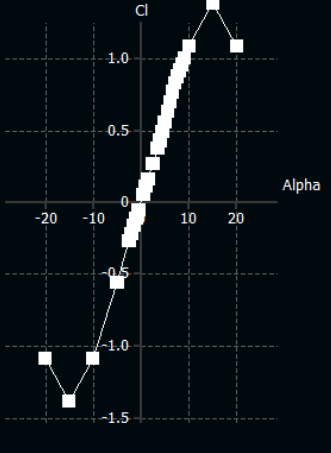
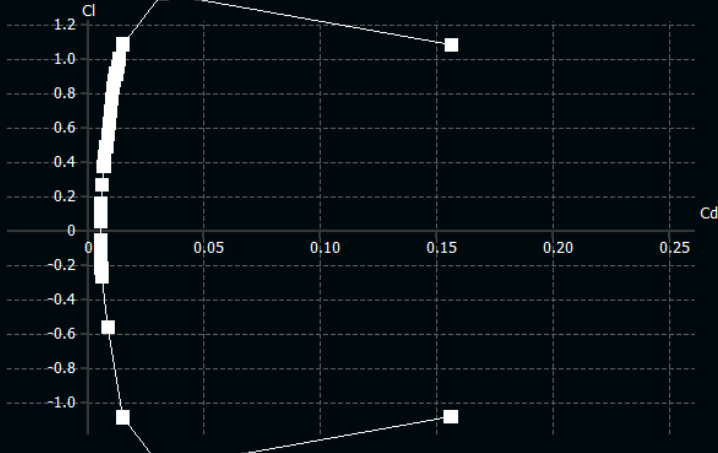
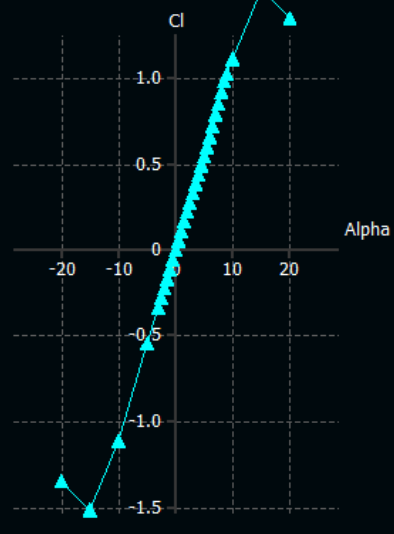
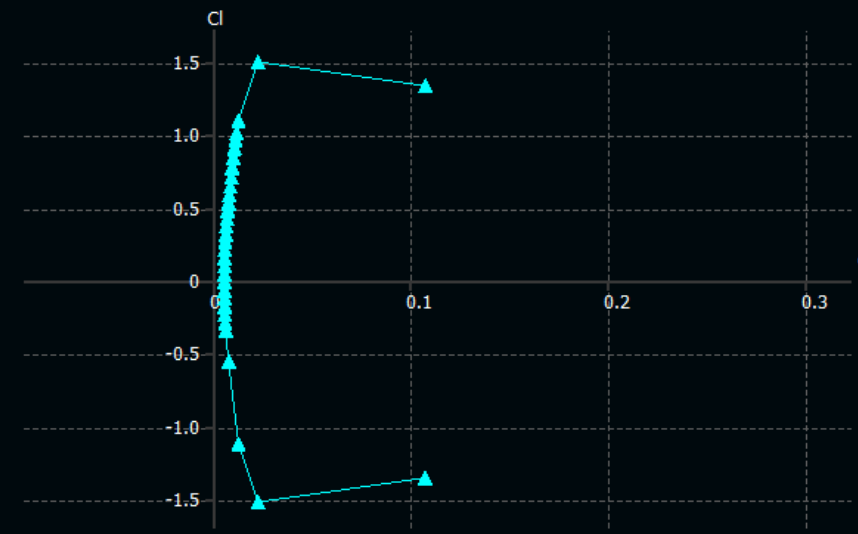
3e5



53

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1e6	 <p>Graph showing the relationship between the lift coefficient (C_l) and the angle of attack (α) for a flow rate of 1×10^6. The x-axis (α) ranges from -20 to 20 degrees, and the y-axis (C_l) ranges from -1.5 to 1.0. The curve shows a linear increase in C_l with α up to approximately 15 degrees, after which it begins to decrease, indicating stall.</p>	 <p>Graph showing the relationship between the lift coefficient (C_l) and the drag coefficient (C_d) for a flow rate of 1×10^6. The x-axis (C_d) ranges from 0 to 0.25, and the y-axis (C_l) ranges from -1.0 to 1.2. The curve shows a hysteresis loop, with C_l increasing as C_d increases up to a point, then decreasing as C_d continues to increase.</p>	75
2e6	 <p>Graph showing the relationship between the lift coefficient (C_l) and the angle of attack (α) for a flow rate of 2×10^6. The x-axis (α) ranges from -20 to 20 degrees, and the y-axis (C_l) ranges from -1.5 to 1.0. The curve shows a linear increase in C_l with α up to approximately 15 degrees, after which it begins to decrease, indicating stall.</p>	 <p>Graph showing the relationship between the lift coefficient (C_l) and the drag coefficient (C_d) for a flow rate of 2×10^6. The x-axis (C_d) ranges from 0 to 0.3, and the y-axis (C_l) ranges from -1.5 to 1.5. The curve shows a hysteresis loop, with C_l increasing as C_d increases up to a point, then decreasing as C_d continues to increase.</p>	92

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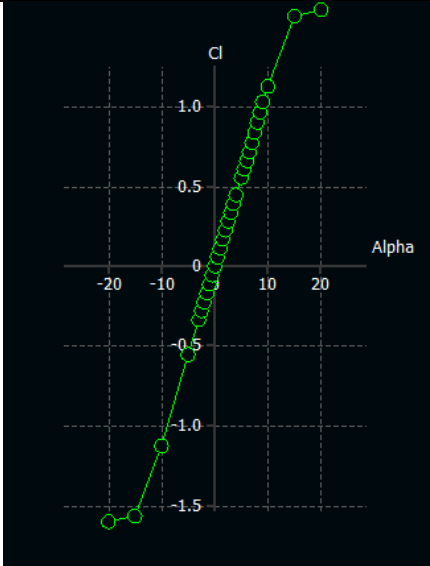

3e6			100
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Figure 1: Table presenting the graphs c_L vs α , c_L vs c_D at the different Reynold's numbers

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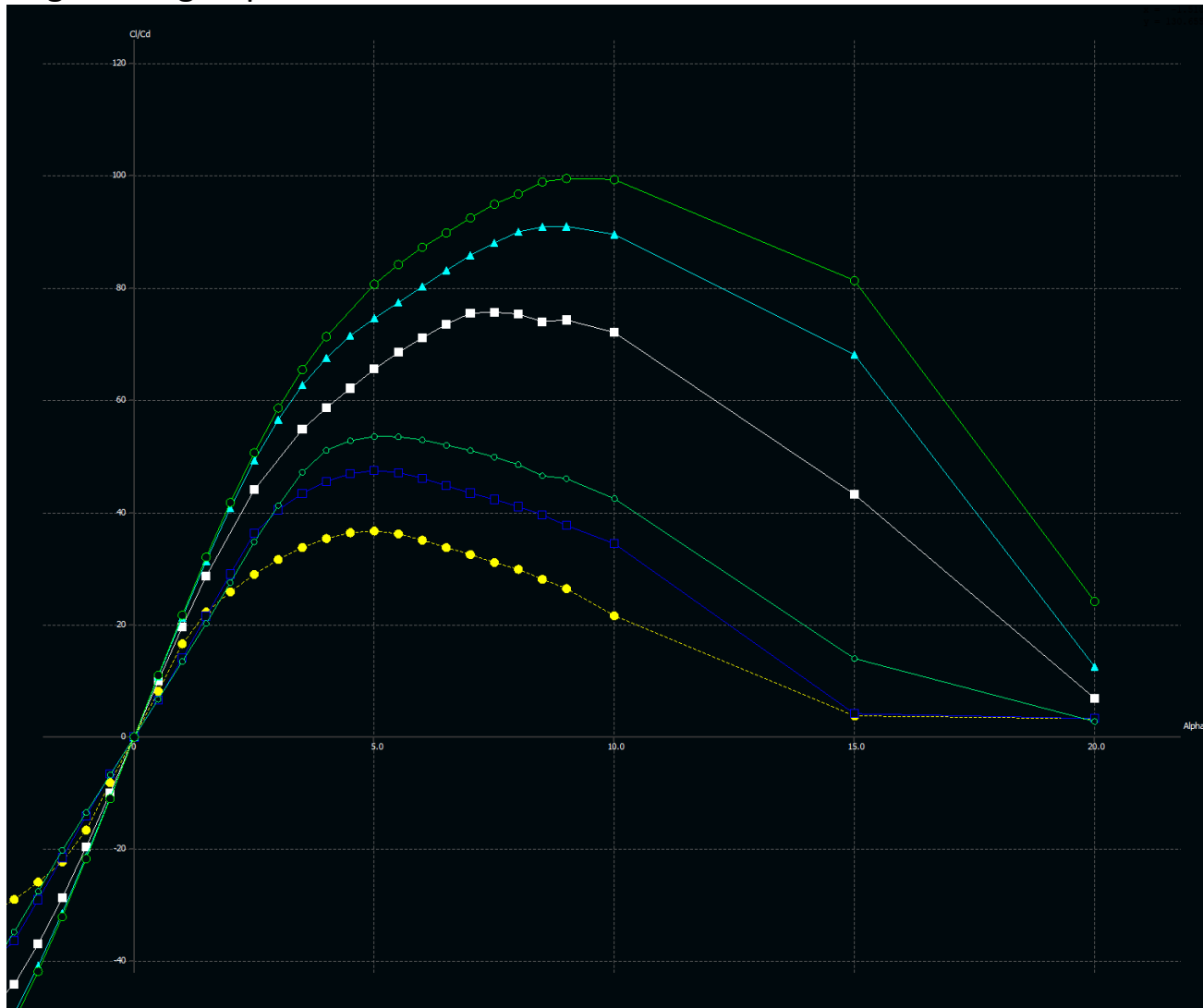


Figure 2: Graph representing cl/cd vs α

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Assuming that $Re = \frac{\rho V c}{\mu}$, $V = \frac{Re * \mu}{\rho * c}$ and $\rho = 1.225 \frac{kg}{m^3}$, $\mu = 0.00001825$, and $c = 3.5 \text{ in} = 0.1016 \text{ m}$, we have:

Re number	V (m/s)
1.00E+05	1.47E+01
2.00E+05	2.93E+01
3.00E+05	4.40E+01
1.00E+06	1.47E+02
2.00E+06	2.93E+02
3.00E+06	4.40E+02

Figure 3: Table representing the values of V at different Reynold's number of an airfoil with 3.5 in chord length

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Part 2: Wortman airfoil

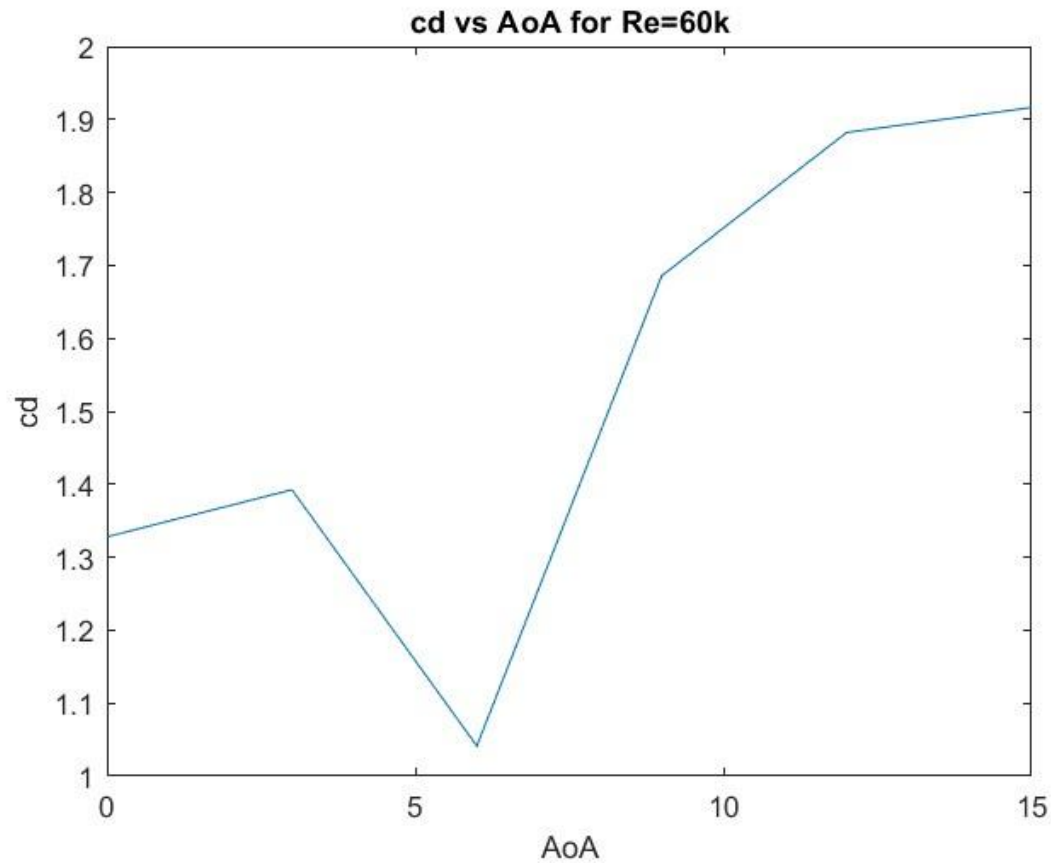


Figure 4: Plot of c_d vs angle of attack at $Re = 60,000$

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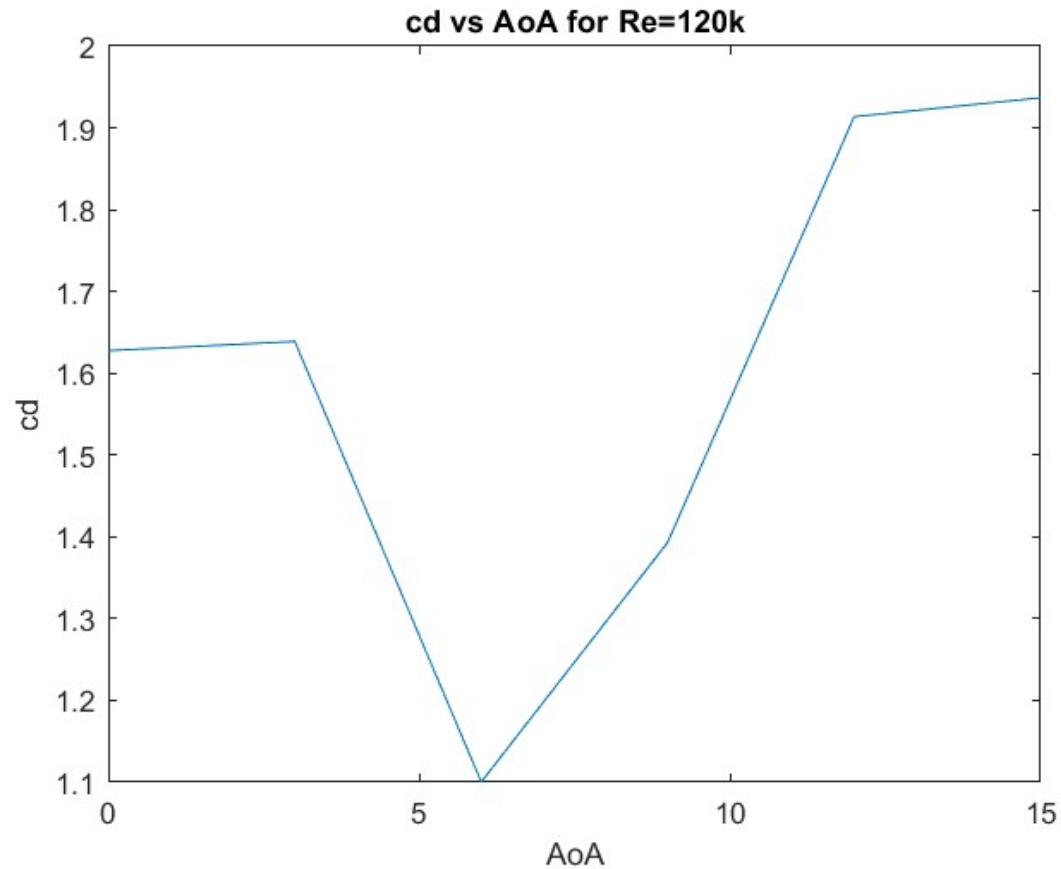


Figure 5: Plot of c_d vs angle of attack at $Re = 120,000$

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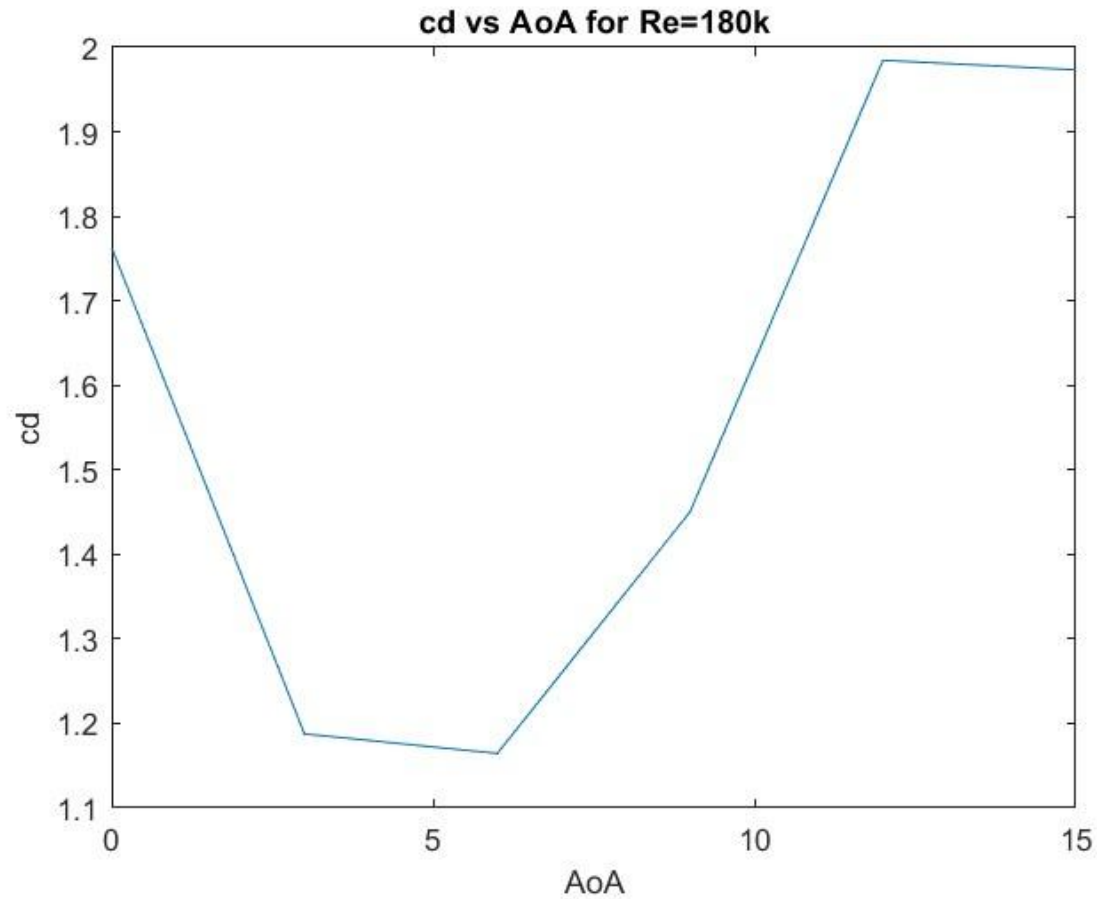


Figure 6: Plot of c_d vs angle of attack at $Re = 180,000$

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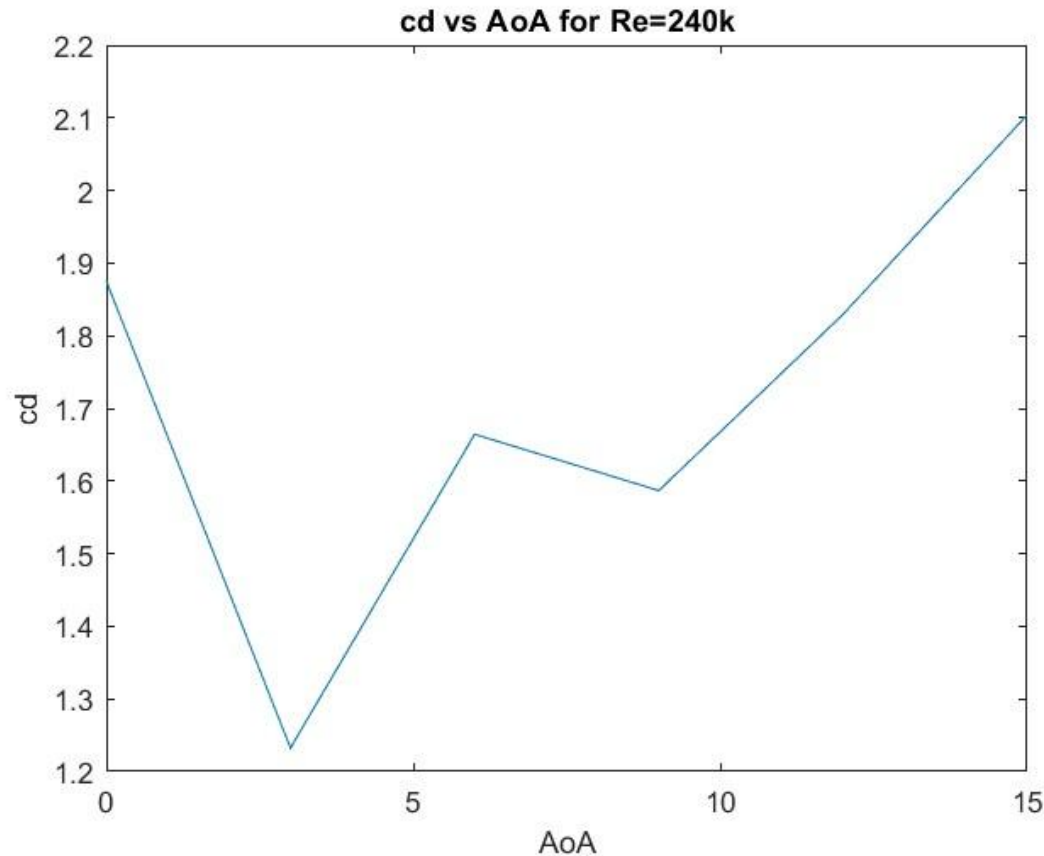


Figure 7: Plot of c_d vs angle of attack at $Re = 240,000$

One observation that can be made is that the coefficient of drag increases as the Reynold's number increases, which makes sense because of the viscous forces that result.

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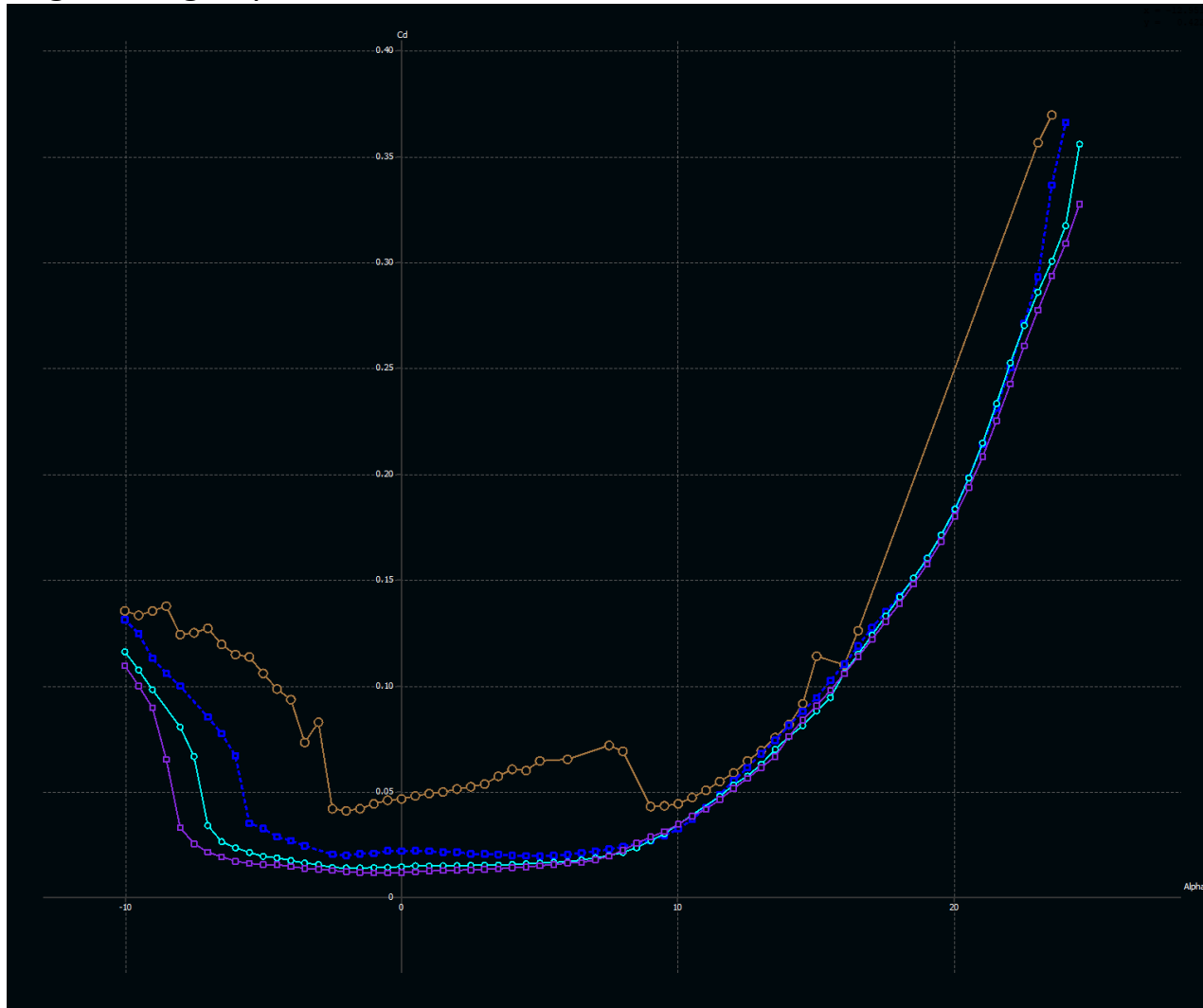


Figure 8: Graph representing c_d vs α for the Wortman airfoil

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The coefficient of drag is generally way lower computationally than what has been computed on MATLAB. This may be due to the position of the wake system on the airfoil. It is capturing the total pressure rather than the momentum deficit.

Conclusion/Recommendations:

Integrating wake rack is an easy method to measure drag of an airfoil. Using a series a Pitot tube to measure total pressure is an efficient alternative to measuring aerodynamic data, but one needs to take the wake rack position into account.

Operating the wind tunnel has been an interesting experience. Getting to manipulate the LabVIEW code that controls the air speed gives us an insight into how testing is conducted in industry and in research. Writing the MATLAB code to produce the graph has also been challenging, but it just shows how efficient MATLAB is in terms of data interpretation given the amount of data collected form the wind tunnel. This assignment has shaped my coding skills.

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Appendix: MATLAB code

```
Re_list = [60, 120, 180, 240];
AoA = [0,3,6,9,12,15];
color = ["b", "g", "r", "c", "m", "y"];
fnumber = 1;
figure(fnumber);
cd_list = [];
for h = 1:numel(Re_list)
    for g = 1:numel(AoA)
        re = string(Re_list(h));
        a = string(AoA(g));
        f = readtable("WakePressure_Re"+re+"k_a"+a+"_xrake5c.dat");
        s = 32;
        data = [];
        wd_array = [];
        integral = [];
        Re = Re_list(h)*1000;
        nu = 0.00001825;
        rho = 1.225;
        q_inf_c = 0.5*Re*Re*nu*nu/rho/0.0889/0.0889; %get dynamic viscosity
        for i = 1:size(f, 1)
            if mod(i,32) ~= 0 %if we are not at the 32nd row
                fdp = f{i, 4};
                tgp = f{i,3};
                sgp = f{s, 3};
                wd = fdp - (tgp - sgp);
                y_location_over_c = f{i, 1}/1000/0.0889; %convert to meters then divide by chord length
                if wd/q_inf_c > 0
                    wd_array = [wd_array, wd/q_inf_c];
                    y_over_c = y_location_over_c;
                    data = [data, y_over_c];
                end
            else
                s = s+32;
            end
        end
    end
end
```

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end

end

```
data = data.';
wd_array = wd_array.';
cm = [data wd_array];
cm = sortrows(cm);
disp(cm);
D = trapz(cm(:,1), cm(:,2)); %integration
disp(D/q_inf_c);
cd_list = [cd_list, D]; %list of drag calculated
plot(cm(:,2), cm(:,1));
```

hold on;

s = 32;

end

title("y/c vs wake_pressure/dynamic pressure for Re="+re+"k")

xlabel("(p-pinf)/qinf")

ylabel("y/c")

legend('0deg', '3deg', '6deg', '9deg', '12deg', '15deg');

hold off

if fnumber ~= 4

fnumber = fnumber+1;

figure(fnumber);

end

end

indices = 0;

fnumber = 5;

%plot cd vs angle of attack

for h = 1:numel(Re_list)

figure(fnumber)

indices = indices+6;

cd = cd_list((indices-5):indices);

plot(AoA, cd);

xlabel("AoA");

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```
ylabel("cd");  
title("cd vs AoA for Re="+Re_list(h)+"k")  
fnumber = fnumber+1;  
end
```