





## **UNIVERSITY OF COLOMBO, SRI LANKA**

#### UNIVERSITY OF COLOMBO SCHOOL OF COMPUTING

#### DEGREE OF BACHELOR OF INFORMATION TECHNOLOGY (EXTERNAL)

Academic Year 2004/2005 – 1<sup>st</sup> Year Examination – Semester 2

# IT2202 – Data Structures and Algorithms Multiple Choice Question Paper

30<sup>th</sup> July, 2005 (TWO HOURS)

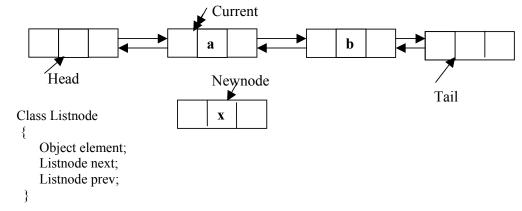
#### Important Instructions:

- The duration of the paper is 2 (two) hours.
- The medium of instruction and questions is English.
- The paper has **45** questions and **12** pages.
- All questions are of the MCQ (Multiple Choice Questions) type.
- All questions should be answered.
- Each question will have 5 (five) choices with <u>one or more</u> correct answers.
- All questions will carry equal marks.
- There will be a penalty for incorrect responses to discourage guessing.
- The mark given for a question will vary from −1 (All the incorrect choices are marked & no correct choices are marked) to +1 (All the correct choices are marked & no incorrect choices are marked).
- Answers should be marked on the special answer sheet provided.
- Note that questions appear on both sides of the paper.

  If a page is not printed, please inform the supervisor immediately.
- Mark the correct choices on the question paper first and then transfer them
  to the given answer sheet which will be machine marked. Please
  completely read and follow the instructions given on the other side
  of the answer sheet before you shade your correct choices.

| 1) | Consider the following four statements.   |  |  |  |
|----|---|--|--|--|
|    | <ul> <li>(i) A stack is an ordered collection of items into which new items may be inserted and from which items may be deleted at the one end called top of the stack.</li> <li>(ii) A stack is an ordered collection of items into which new items may be inserted into an arbitrary location.</li> </ul>   |  |  |  |
|    | <ul><li>(iii) Dynamic implementation stacks using Java language are practically impossible.</li><li>(iv) One of the stack applications is used in complier design.</li></ul>  |  |  |  |
|    | Which one of the following is correct in relation to the stacks?  |  |  |  |
|    | (a) (i) and (iv) only (b) (i), (ii) and (iii) only (c) (i) only (d) (iv) only (e) (i), (ii) and (iv) only   |  |  |  |
| 2) | Consider the following infix expression:  |  |  |  |
|    | $((A+B) * C - (D-E)) ^(F+G)$  |  |  |  |
|    | Which of the following is a / are correct equivalent expression(s) for the above?   |  |  |  |
|    | (a) ^- * + A B C - D E F G+<br>(b) ^- * + A B C - D E F+ G<br>(c) ^- * + A B C - D E + F G<br>(d) - ^ * + A B C - D E + F G<br>(e) ^- * + A B C - D E + F G   |  |  |  |
| 3) | Which of the following statements is/are correct in connection with stacks?   |  |  |  |
|    | <ul> <li>(a) Return and remove the most recently inserted item from the stack, if stack is not empty.</li> <li>(b) Insert a new item to the top of the stack, if stack is full.</li> <li>(c) Elements can be deleted from both ends.</li> <li>(d) Linked list based stack implementations are more convenient than array based implementations.</li> <li>(e) Return and remove the least recently inserted item from the stack, if stack is not empty.</li> </ul> |  |  |  |
| 4) | Which of the following is a / are possible operation(s) in connection with stacks?  |  |  |  |
|    | <ul><li>(a) Reverse the order of elements on stack S using two additional stacks.</li><li>(b) Reverse the order of elements on stack S using additional variables.</li></ul>  |  |  |  |
|    | (c) Reverse the order of elements on stack S using auditional variables.  (d) Sort the elements of stacks using one additional stack.  (e) Reverse the order of elements on stack S using one additional queue.   |  |  |  |
|    | Questions No. 5 and No. 6 are based on the following postfix expression S and the initial values of the variables.  |  |  |  |
|    | $S = AB - C + DEF - + ^$  |  |  |  |
|    | Assume that A=3, B=2, C=1, D=1, E=2, F=3  |  |  |  |
| 5) | If the above S is evaluated using a stack, what is/are the intermediate value(s) on the top of the stack?   |  |  |  |
|    | (a) 3 (b) 0 (c) 2 (d) -1 (e) -2   |  |  |  |
| 6) | What would be the final output of the stack?  |  |  |  |
|    | (a) 1 (b) 2 (c) 0 (d) -1 (e) 3  |  |  |  |
|    |   |  |  |  |

Questions No. 7 to No. 9 are based on the following doubly linked list and its data structure.



- What would be the correct statement(s), when the doubly linked list is empty?
  - (a) Head.next=tail
- (b) Current.next=tail
- (c) Current.prev=Head

- (d) Tail.prev=Head
- (e) Current=nill
- Which of the following correctly describe(s) the steps to delete element **b** from the above doubly linked list?
  - (a) Current.next.next.prev=Current.prev Current.next = Current.next.next
  - (c)Current.next=Current.next.next Current.next.next.prev=Current.next.prev
  - (e) Current = Current.next.next Current.next.next.prev=Current.prev
- (b) Current.next = Current.prev.next Current.next.next.prev=Current.prev
- (d) Current.next=tail Head.next=Current.next.prev
- Which of the following correctly describe(s) the steps in inserting elements x immediately after the element a in the above doubly linked list?

| (a)current.next=x              | (b) current.next=x             | (c) a.next=x  |
|--------------------------------|--------------------------------|---------------|
| xprev=current                  | xprev=current.prev             | xprev=current |
| x.next=b                       | x.next=b                       | x.next=b      |
| b.prev=x                       | b.prev=x                       | b.prev=x      |
| (d) Newnode.next= Current.next | (e) Newnode.next= Current.next |               |
| Newnode.prev=Current           | Newnode.prev=Current.next.prev | /             |
| Newnode.prev.next=Newnode      | Current.next=Newnode           |               |
| Newnode.next.prev=Newnode      | Current.next.prev=Newnode      |               |

A set of basic list terms is given in **Part A** and some definitions are given in **Part B** as follows. 10)

#### Part A

## Part B

- (i) (ii)
- Doubly linked list

Circular linked list

- (iii) Header node
- Iterator class (iv)
- (v) Sorted linked list
- (p) A class that maintains a current position and performs all routines which depend on knowing the position in the list.
- A linked list that allows bidirectional traversal by storing two references per node.
- A list used to maintain items in a linked list in some (r) arrangement.
- An extra node in the linked list that holds no data but serves to satisfy the requirement that every node has a previous node.
- A linked list in which the last cell's reference points to the first.

Choose the best definition from Part B for the above five terms in Part A.

| (a) (i) $\rightarrow$ (t) (ii) $\rightarrow$ (q) (iii) $\rightarrow$ (r) (iv) $\rightarrow$ (p) (v) $\rightarrow$ (s)   | (b) (i) $\rightarrow$ (p) (ii) $\rightarrow$ (t) (iii) $\rightarrow$ (s) (iv) $\rightarrow$ (p) (v) $\rightarrow$ (r)   |
|---|---|
| $(c)$ $(i) \rightarrow (t)$ $(ii) \rightarrow (q)$ $(iii) \rightarrow (s)$ $(iv) \rightarrow (p)$ $(v) \rightarrow (r)$ | $(d)$ $(i) \rightarrow (q)$ $(ii) \rightarrow (t)$ $(iii) \rightarrow (s)$ $(iv) \rightarrow (p)$ $(v) \rightarrow (r)$ |
| (e) (i) $\rightarrow$ (t) (ii) $\rightarrow$ (s) (iii) $\rightarrow$ (p) (iv) $\rightarrow$ (p) (v) $\rightarrow$ (r)   |   |

Questions No. 11 and No. 12 are based on the following straight queue which can be allocated eight integers and five operations.

```
front = 3 rear= 5

Queue = -, -, 2, 4, 5, -, -, -

(for notational convenience "-" used to denote an empty cell)
```

The following operations have to be performed.

- (i) 6 is added to the queue.
- (ii) Two elements are deleted from the queue.
- (iii) 10 and 12 are added to the queue.
- (iv) Two elements are deleted from the queue.
- (v) 2 and 3 are added to the queue.
- 11) What are the final front and rear values when the above operations are performed into a straight queue?

```
(a) front = 7 rear=2 (b) front = 2 rear=7 (c) front = 2 rear=8 (d) front = 5 rear=8 (e) front = 7 rear=8
```

12) What are the final front and rear values when the above operations are performed into a circular queue?

```
(a) front = 7 rear=2 (b) front = 2 rear=7 (c) front = 2 rear=8 (d) front = 5 rear=8 (e) front = 7 rear=8
```

13) Consider the following Java program.

```
Public void pqr ( object x )
    {
    if (isempty( ))
      rear=front= new Listnode( x) ;
    else
      rear=rear.next=new ListNode( x );
    }
```

What is the above Java program segment intended to do?

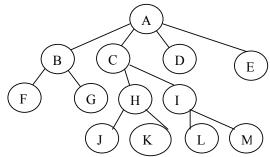
- (a) creating a new node
- (b) deleting nodes from the queue
- (c) only inserting a new item x into an initially empty queue
- (d) only inserting a new item x into an initially non empty queue
- (e) inserting a new item x into the queue
- 14) Consider the following paragraph.

The traversal proceeds as far as possible to the left, then backs up until the first cross road, goes one step to the right and again as far as possible to the left. Repeat this process until all nodes are visited.

What does the above paragraph describe?

(a) Breadth first traversal
(b) Critical path traversal
(c) Shortest path traversal
(d) Depth first traversal
(e) Depth and breadth hybrid traversal

# Questions No. 15 and No. 16 are based on the following tree structure.



- 15) Consider the following five statements.
  - (i) It is a tree.
  - (ii) It is a binary tree.
  - (iii) It is an AVL tree.
  - (iv) It is a binary search tree.
  - (v) It is a strictly binary tree.

Which of the above statements is correct with respect to the above tree?

| (a) (i) only                | (b) (i) and (ii) only | (c) (i), (ii) and (iii) only |
|-----------------------------|-----------------------|------------------------------|
| (d) (i), (ii) and (iv) only | (e) All               |                              |

- 16) Consider the following four statements.
  - (i) Depth of the above tree is equal to 4.
  - (ii) C's proper descendants are I, J, K, L only.
  - (iii) B's siblings are C, D, E only.
  - (iv) K, L, M, N are siblings.

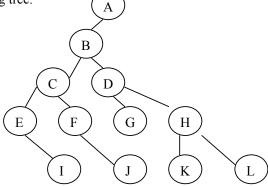
Which of the above statements is correct?

| (a) (i) and (ii) only | (b) (iii) only                | (c) (ii) and (iii) only |
|-----------------------|-------------------------------|-------------------------|
| (d) (ii) only         | (e) (ii), (iii) and (iv) only |                         |

17) Which of the following are **not** hash functions?

| (a) division   | (b) folding    | (c) coupling |  |
|----------------|----------------|--------------|--|
| (d) mid square | (e) extraction |              |  |

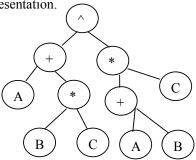
18) Consider the following tree.



Which of the following is/are correct with respect to the above tree?

- (a) Pre-order listing is ABCEIFJDGHKL.
- (b) Pre-order listing is ABCIEFJDGHKL.
- (c) In- order listing is EICFJBGDKHLA.
- (d)In- order listing is EICFJBGKDHLA.
- (e) Post-order listing is IEJFCGKLHDBA.

19) Consider the following expression tree representation.



Which of the following expressions is correct in relation to the above tree?

```
(a) (A*B+C)^((A+B)*C) (b) (A+B*C)^((A+B)*C) (c) (A+B*C)^( A+(B *C)) (d) (A+B^*C)*((A+B)*C) (e) (A+B*C)^( A+B*C)
```

20) Consider the following binary search tree algorithm.

```
Public Bsnode search ( Bsnode p, int el) {

While (p!=null)
    if(el==p.key)
        return p;
    else
    if (el < p.key)
        .....(i)......;
    else .....(ii)......;
```

Identify suitable entries to fill in the blank positions labeled (i), (ii), (iii) of the above algorithm so that it will insert el to the binary search tree.

```
(a) (i) p = p.right (ii) p =p.left; (iii) return null;

(b) (i) p = p.left (ii) p =p.right; (iii) return null;

(c) (i) p = p.left.next (ii) p =p.right.next; (iii) return null;

(d) (i) p = p.right.next (ii) p =p.left.next; (iii) return null;

(e) (i) p = p.right (ii) p =p.left; (iii) return null;
```

21) Consider the following Java program segment.

```
static int ppp ( tree t)
{
if (t==null)
    return -1;
else
return 1+Math.max(ppp(t.left),ppp(t.right));
}
```

What does of the above program segment intend to do?

- (a) Routine to compute the height of the node in a binary tree in a recursive way
- (b) Routine to compute the height of the node in a binary tree in a non-recursive way
- (c) Routine to compute the height of the node in a binary search tree in a recursive way
- (d) Routine to compute the height of the node in a binary search tree in a non-recursive way
- (e) Routine to compute the height of the node in an AVL tree in a non-recursive way.

22) Consider the following polynomial.

$$f(n) = n^2 + 100n + Log_{10} n + 1000$$

What would be the Big –O value of the above polynomial?

| (a) n     | (b) Log n    | (c) n <sup>2</sup> +log n |  |
|-----------|--------------|---------------------------|--|
| $(d) n^2$ | (e) Constant |                           |  |

23) Consider the following statement (Algorithm Segment).

The method one uses to replace the node being deleted by the rightmost node in its left sub tree or leftmost node in its right sub tree.

What does the above statement (algorithm segment) intend to do?

- (a) Deleting a node from an AVL, if deleting node has both a left and a right child
- (b) Deleting a node from a binary tree
- (c) Deleting a node from a general tree
- (d) Deleting a node from a binary search tree, if deleting node is a leaf node
- (e) Deleting a node from a binary search tree, if deleting node has both a left and a right child
- 24) Consider the following table.

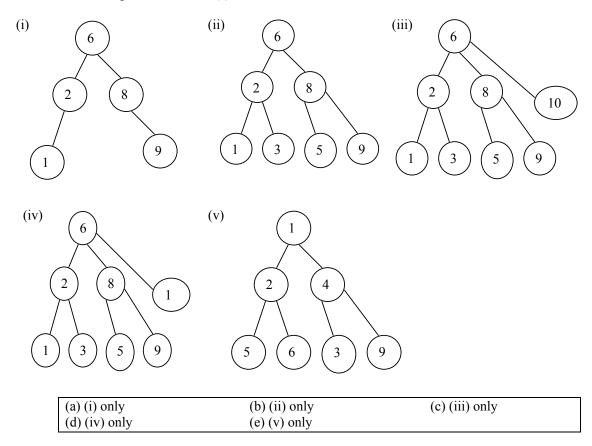
| State on node  | Effect of new node             | Action of new state |
|----------------|--------------------------------|---------------------|
| (i) Balanced   | Increase left sub tree height  | Left-high           |
| (ii) Balanced  | Increase right sub tree height | Right-high          |
| (iii)Left-high | Increase left sub tree height  | Left balance        |
| (iv)Right-high | Increase left sub tree height  | Balanced            |
| (v) Right-high | Increase right sub tree height | Left balance        |

Which of the above would be correct for inserting a new node into an AVL tree?

| (a) (i) only                      | (b) (i) and (ii) only       | (c) (i), (ii) and (iii) only |
|-----------------------------------|-----------------------------|------------------------------|
| (d) (i) (ii) (iii) and (iv) only. | (e) (i) (iii) and (iv) only |                              |

- 25) Which of the following is/are correctly describing a step in the definition of the Heap data structure?
  - (a) All leaves are on two adjacent levels.
  - (b) All leaves on the lowest level occur at the left of the tree.
  - (c) All leaves on the lowest level occur at the right of the tree.
  - (d) All levels above the lowest are completely filled.
  - (e) Balance factor is always -1,0,+1.
- 26) Which of the following statements is/are correct in connection with a graph?
  - (a) Purely array-based representation of a graph is called its path matrix.
  - (b) Graphs may be used as diagrams which illustrate the relationship between pairs of elements in a set of objects.
  - (c) Depth first traversal and Breadth first traversal techniques can be used only for graphs.
  - (d) A multi-graph is a graph where two vertices can be joined by multiple edges.
  - (e) A graph is called a weighted graph if each edge has an assigned number.

# 27) Which of the following is/are AVL tree(s)?



### 28) Consider the following pseudo code algorithm segment.

```
algo-1 ()
 for all vertices u
   num(u)=0;
 edges=null;
 i=1;
while there is a vertex v such that num(u) = 0
 num(v)=i++;
 enqueue(v);
while queue is not empty
    v=dequeue();
   for all vertices u adjacent to v
   if num(u) is 0
   num(u+=i++;
   enqueue(u);
   attach edge (uv) to edges;
output edges;
```

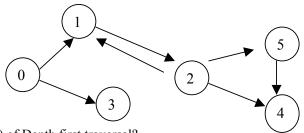
What does the above algorithm describe?

- (a) Array based implementation of queue
- (b) Depth first traversal

(c) Breadth first traversal

- (d) Deleting nodes from a queue
- (e) Inserting nodes to a queue

Consider the following directed graph.



Which of the following is/are **not** (an) output(s) of Depth first traversal?

| (-) 0 11 12 14 15 12  | (1-) () \ 1 \ \ 2 \ \ 5 \ \ 4 \ \ 2   | (-) 0 \2 \1 \2 \1 \5  |
|---|---|---|
| (a) $0 \rightarrow 1 \rightarrow 2 \rightarrow 4 \rightarrow 5 \rightarrow 3$ | (b) $0 \rightarrow 1 \rightarrow 2 \rightarrow 5 \rightarrow 4 \rightarrow 3$ | (c) $0 \rightarrow 3 \rightarrow 1 \rightarrow 2 \rightarrow 4 \rightarrow 5$ |
| ()  | (*) *   | (0) 0 1 0 1 1 1 1 1 1 1   |
| (4) 0-21-22-22-4-22   | $(a) 0 \rightarrow 1 \rightarrow 2 \rightarrow 5 \rightarrow 4 \rightarrow 1$ |   |
| $(d) 0 \rightarrow 1 \rightarrow 2 \rightarrow 2 \rightarrow 4 \rightarrow 3$ | (e) $0 \rightarrow 1 \rightarrow 2 \rightarrow 5 \rightarrow 4 \rightarrow 1$ |   |
| (-) -   | (-) -   |   |

- Which of the following is/are correct in connection with graph data structures? 30)
  - (a) Path matrix can be defined as path [i][j] = adj[i][j] or  $adj_2[i][j]$  or  $adj_3[i][j]$  or.........
  - (b) Transitive closure can be determined by using the path matrix.
  - (c)  $adj_3[i][j] = adj_2[i][j] * adj[i][j]$ .
  - (d) Warshall's algorithm will increase the efficiency of finding the Transitive closure.
  - (e) Warshall's algorithm will increase the efficiency of finding the adjacency matrix.
- 31) Which of the following is/are **not** (an) alternative representation(s) of graphs?
  - (a) An adjacency list (b) An adjacency matrix (c) Depth first traversal (d) Incidence matrix (e) Breadth first traversal
- 32) Which of the following is/are correct in connection with sorting methods?
  - (a) Bubble sort uses sorting by an insertion technique to sort a file of numbers.
  - (b) Quick sort uses sorting by an exchange technique to sort a file of numbers.
  - (c) Shell sort uses sorting by an exchange technique to sort a file of numbers.
  - (d) Heap sort uses sorting by an exchange technique to sort a file of numbers.
  - (e) Selection sort uses sorting by a selection technique to sort a file of numbers.
- 33) A set of five basic graph terms is given in **Part A** and some definitions are given in **Part B** as follows.

#### Part A Part B

- (i) Cycle
- (ii) Critical path Analysis
- (iii) Dijkstra's Algorithm
- (iv) Path Length
- (v) Graph

- (p) A term used to schedule tasks associated with a project
- (q) In a directed graph, a path that begins and ends at the same vertex and contains at least one edge
- (r) Number of edges on the path
- (s) This solves the positive weighted shortest path problem.
- (t) This consists of a set of vertices and a set of edges which connect the vertices

Choose the best definition from Part B for the above five terms in Part A

| (a) (i) $\rightarrow$ (q), (ii) $\rightarrow$ (s), (iii) $\rightarrow$ (p),(iv) $\rightarrow$ (r), (v) $\rightarrow$ (t)        | (b) (i) $\rightarrow$ (t), (ii) $\rightarrow$ (p), (iii) $\rightarrow$ (s),(iv) $\rightarrow$ (r), (v) $\rightarrow$ (q) |
|---|--|
| $(c)$ $(i) \rightarrow (q)$ , $(ii) \rightarrow (p)$ , $(iii) \rightarrow (s)$ , $(iv) \rightarrow (r)$ , $(v) \rightarrow (t)$ | (d) (i) $\rightarrow$ (q), (ii) $\rightarrow$ (p), (iii) $\rightarrow$ (s),(iv) $\rightarrow$ (r), (v) $\rightarrow$ (t) |
| (e) (i) $\rightarrow$ (q), (ii) $\rightarrow$ (p), (iii) $\rightarrow$ (t),(iv) $\rightarrow$ (t), (v) $\rightarrow$ (s)        |  |

|     | {2,8,13,6,7,27,18}   |   |  |  |
|-----|--|---|--|--|
| 34) | If the maximum heap is created using the above set of integers, what would be the value at the 6 <sup>th</sup> position of the heap?   |   |  |  |
|     | (a) 2<br>(d) 13  | (b) 8<br>(e) 7  | (c) 6  |  |
| 35) | If ones sorts the above heap cre-<br>respectively of the shirking arra   |   | ould be the first and last elements  |  |
|     | (a) 18,2<br>(d) 2,18   | (b) 27,18<br>(e) 2, 27  | (c) 27,2   |  |
| 36) | "Many operations can be perfo<br>applicable to the above stateme   |   | ted data". Which of the following is/are                                     |  |
|     | (b) Finding an item wi<br>(c) Computing an aver<br>(d) Finding the middle  | age value   |  |  |
|     | Questions No. 37 and No. 38  | are based on the following set o  | of ten integers.   |  |
|     | {50,22,11,78,16,95,7,75,51,41}   | }.  |  |  |
| 37) | If one uses the quick sort algorithm to sort the above set of integers, how many pivot values are required? You may assume that the pivot element is always selected as the last element of the respective sub arrays. |   |  |  |
|     | (a) 7<br>(d) 6   | (b) 8<br>(e) 5  | (c) 4  |  |
| 38) |  | ithm to sort the above set of integ<br>t the pivot element is always sele | gers, how many pivot values are acted as the first element of the respective |  |
|     | (a) 7<br>(d) 6   | (b) 8<br>(e) 5  | (c) 4  |  |
|     | Questions No. 39 and No. 40  | are based on the following set o  | of eight integers  |  |
|     | {20,60,50,37,16,92,70,35}.   |   |  |  |
| 39) | If one uses the bubble sort algovalues <u>not</u> interchanging during   |   | ch of the following pairs will the data                                      |  |
|     | (a) 20,60<br>(d) 50,37   | (b) 60,50<br>(e) 60,16  | (c) 60,37  |  |
| 40) | How many passes are required   | to sort the above set of integers u                                       | using the bubble sort algorithm?   |  |
|     | (a) 6<br>(d) 9   | (b) 7<br>(e) 5  | (c) 8  |  |
|     |  |   |  |  |

Questions No. 34 and No. 35 are based on the following set of seven integers.

41) Consider the following pseudo code algorithm.

```
found = false;
i=1;
    while (i =< n ) and ( not found)
{
    if key=k[i] then
    {
        search = i;
        found = true;
    else
        i++;
    }
}
if not found
{
search=0;
}</pre>
```

What is the above algorithm intended to do?

(a) Sequential Search

(b) Depth First Algorithm

(c) Shell sort algorithm

(d) Index sequential search

- (e) Breadth first search
- 42) Consider the following program segment with 3 blank positions labeled (i), (ii) and (iii).

Which of the following provide correct answers for the blank positions?

```
(a) (i) { low <> high } (ii) a[mid].compares(x) < 0 (iii) a[mid].compares(x) > 0 (b) (i) { low <= high } (ii) a[mid].compares(x) =< 0 (iii) a[mid].compares(x) > 0 (c) (i) { low <= high } (ii) a[mid].compares(x) < 0 (iii) a[mid].compares(x) >= 0 (d) (i) { low <= high } (ii) a[mid].compares(x) < 0 (iii) a[mid].compares(x) > 0 (e) (i) { low <= high } (ii) a[high].compares(x) < 0 (iii) a[mid].compares(x) > 0
```

43) Consider the following four terms given in **Part A** and some definitions given in **Part B**.

| <u>Part A</u>   | <u>Part</u>       | <u>B</u>  |
|-----------------|-------------------|---|
| (i) Big O       | 4.7               | The notation used to capture the most dominant term in a      |
|                 | f                 | function  |
| (ii) Big Omeg   |                   | A guarantee over all inputs of some size                      |
| (iii) Average c | ase bound (r)     | The bound in which running time is measured as an average     |
|                 | (                 | over all the possible inputs of size N                        |
| (iv) Worst case | e bound (s) A     | An algorithm that causes the running time to $grow$ as $O(N)$ |
| (v) Linear tim  | e algorithm (t) 7 | The notation similar to greater than or equal to when         |
|                 | (                 | considering growth rates                                      |
|                 |                   |   |

Choose the best definition from Part B for the above five hash operations respectively in Part A.

```
 \begin{array}{lll} (a) & (i) \rightarrow (p) & (ii) \rightarrow (r) & (iii) \rightarrow (t) & (iv) \rightarrow (q) & (v) \rightarrow (s) \\ (c) & (i) \rightarrow (p) & (ii) \rightarrow (t) & (iii) \rightarrow (r) & (iv) \rightarrow (q) & (v) \rightarrow (s) \\ (e) & (i) \rightarrow (p) & (ii) \rightarrow (t) & (iii) \rightarrow (r) & (iv) \rightarrow (q) & (v) \rightarrow (s) \\ (e) & (i) \rightarrow (p) & (ii) \rightarrow (t) & (iii) \rightarrow (r) & (iv) \rightarrow (q) & (v) \rightarrow (t) \\ (e) & (i) \rightarrow (p) & (ii) \rightarrow (t) & (iii) \rightarrow (r) & (iv) \rightarrow (q) & (v) \rightarrow (t) \\ (e) & (i) \rightarrow (p) & (ii) \rightarrow (t) & (iii) \rightarrow (r) & (iv) \rightarrow (q) & (v) \rightarrow (t) \\ (e) & (i) \rightarrow (p) & (ii) \rightarrow (t) & (iii) \rightarrow (r) & (iv) \rightarrow (q) & (v) \rightarrow (t) \\ (e) & (i) \rightarrow (p) & (ii) \rightarrow (t) & (iv) \rightarrow (q) & (v) \rightarrow (q) \\ (e) & (i) \rightarrow (p) & (ii) \rightarrow (t) & (iii) \rightarrow (r) & (iv) \rightarrow (q) & (v) \rightarrow (q) \\ (e) & (i) \rightarrow (p) & (ii) \rightarrow (t) & (iii) \rightarrow (r) & (iv) \rightarrow (q) & (v) \rightarrow (q) \\ (e) & (i) \rightarrow (p) & (ii) \rightarrow (t) & (iv) \rightarrow (q) & (v) \rightarrow (q) \\ (e) & (i) \rightarrow (p) & (ii) \rightarrow (r) & (iv) \rightarrow (q) & (v) \rightarrow (q) \\ (e) & (i) \rightarrow (p) & (ii) \rightarrow (r) & (iv) \rightarrow (q) & (v) \rightarrow (q) \\ (e) & (i) \rightarrow (p) & (ii) \rightarrow (r) & (iv) \rightarrow (q) & (v) \rightarrow (q) \\ (e) & (i) \rightarrow (p) & (ii) \rightarrow (r) & (iv) \rightarrow (q) & (v) \rightarrow (q) \\ (e) & (i) \rightarrow (p) & (ii) \rightarrow (r) & (iv) \rightarrow (q) & (v) \rightarrow (q) \\ (e) & (i) \rightarrow (p) & (ii) \rightarrow (r) & (iv) \rightarrow (q) & (v) \rightarrow (q) \\ (e) & (i) \rightarrow (p) & (iv) \rightarrow (q) & (v) \rightarrow (q) \\ (e) & (i) \rightarrow (p) & (iv) \rightarrow (q) & (v) \rightarrow (q) \\ (e) & (i) \rightarrow (p) & (iv) \rightarrow (q) & (v) \rightarrow (q) \\ (e) & (i) \rightarrow (p) & (iv) \rightarrow (q) & (v) \rightarrow (q) \\ (e) & (i) \rightarrow (p) & (iv) \rightarrow (q) & (v) \rightarrow (q) \\ (e) & (i) \rightarrow (q) & (iv) \rightarrow (q) & (iv) \rightarrow (q) \\ (e) & (i) \rightarrow (q) & (iv) \rightarrow (q) & (iv) \rightarrow (q) \\ (e) & (i) \rightarrow (q) & (iv) \rightarrow (q) & (iv) \rightarrow (q) \\ (e) & (i) \rightarrow (q) & (iv) \rightarrow (q) \\ (e) & (i) \rightarrow (q) & (iv) \rightarrow (q) \\ (e) & (i) \rightarrow (q) & (iv) \rightarrow (q) \\ (e) & (i) \rightarrow (q) & (iv) \rightarrow (q) \\ (e) & (i) \rightarrow (q) & (iv) \rightarrow (q) \\ (e) & (i) \rightarrow (q) & (iv) \rightarrow (q) \\ (e) & (i) \rightarrow (q) & (iv) \rightarrow (q) \\ (e) & (i) \rightarrow (q) & (iv) \rightarrow (q) \\ (e) & (i) \rightarrow (q) & (iv) \rightarrow (q) \\ (e) & (i) \rightarrow (q) & (iv) \rightarrow (q) \\ (e) & (i) \rightarrow (q) & (iv) \rightarrow (q) \\ (e) & (i) \rightarrow (q) & (iv) \rightarrow (q) \\ (e) & (i) \rightarrow (q) & (iv) \rightarrow (q) \\ (e) & (i) \rightarrow (q) & (iv) \rightarrow (q) \\ (e) & (i) \rightarrow (q) & (iv) \rightarrow (q) \\ (e) & (i) \rightarrow (q) & (iv) \rightarrow (q) \\ (e) & (i) \rightarrow (q) & (iv) \rightarrow (q) \\ (e) & (i) \rightarrow (q) & (iv) \rightarrow (q) \\ (e) & (i) \rightarrow (q) & (iv) \rightarrow (q) \\ (e) & (i) \rightarrow (q) & (iv)
```

44) Consider the following bubble sort algorithm.

```
\label{eq:public void bubblesort (object [] data ) { } \\ & \text{int } i,j; \\ & \text{for } (i=0; i < \text{data.length-1}; i++) \\ & \text{for } (j=\text{data.length-1}; j>i;--j) \\ & \text{if } ( ((\text{Comparable})\text{data}[j]).\text{compareTo } (\text{data}[j-1]) < 0) \\ & \text{swap } (\text{ data},j,j-1); \\ \} \\ \end{aligned}
```

What would be the best, average and worst-case time complexities of the above algorithm respectively?

```
(a) n , n , n^2 (b) n^2 , \log n , n^2 (c) n , n^2 , n^2 (d) n , \log n , n^2 (e) n^2 , n^2 , n^2
```

45) Consider the five operations in **Part A** and some definitions in **Part B** as follows.

#### Part A Part B (i) Void clear() (p) Return true if the hash table contains the object val; raise NullPointerException if val is null. (ii) Object clone () (q) Return true if the hash table contains the object key; raise NullPointerException if key is null. (r) Return true if the hash table contains the object val; (iii) Boolean contains(val) NullPointerException if val is null. (s) Return the copy of the hash function without cloning its (iv) Boolean containsKey(key) elements (v) Boolean (t) Remove all the objects from the hash table. containsvalue(val)

Choose the best definition from Part B for the above five terms in Part A.

```
(a) (i)\rightarrow(r), (ii)\rightarrow(s), (iii)\rightarrow(p), (iv)\rightarrow(q), (v)\rightarrow(t)

(b) (i)\rightarrow(p), (ii)\rightarrow(s), (iii)\rightarrow(t), (iv)\rightarrow(q), (v)\rightarrow(r)

(c) (i)\rightarrow(t), (ii)\rightarrow(p), (iii)\rightarrow(s), (iv)\rightarrow(q), (v)\rightarrow(r)

(d) (i)\rightarrow(t), (ii)\rightarrow(s), (iii)\rightarrow(p), (iv)\rightarrow(q), (v)\rightarrow(r)

(e) (i)\rightarrow(t), (ii)\rightarrow(s), (iii)\rightarrow(q), (iv)\rightarrow(p), (v)\rightarrow(r)
```

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