

## **CHAPTER 4**

# **Linked Lists**

# LINKED LIST

## 4.1 Singly Linked Lists and Chains

## 4.2 Representing Chains in C

## 4.3 Linked Stacks and Queues

## 4.4 Polynomials

## 4.5 Additional List Operations

## 4.7 Sparse Matrixs

## 4.8 Doubly Linked Lists

- Sequential representation

- Successive items are located a fixed distance apart
- Adequate for the tasks:
  - Accessing an arbitrary node in a **table**
  - Insertion or deletion of **stack** and **queue** elements

연속적인 거들이 일정 거리로 떨어져 있다

배열을 사용

- Disadvantage

- For **ordered lists**, operations such as insertion and deletion of arbitrary elements become expensive
- E.g. To add the word GAT the following list :

(BAT, CAT, EAT, FAT, HAT, JAT, LAT, MAT, OAT, PAT, RAT, SAT, VAT, WAT)

⇒ GAT를 넣으려면 다른 원소들을 shift를 해주어야함

- ***Linked*** representations

배열과 달리 메모리 방향

- Items may be placed anywhere in memory

- A linked list is comprised of **nodes**

- Nodes

- data fields + link(or pointer) fields

- Link

- Store the address or location of the next element in that list

다음 데이터를 가리키는 포인터

For any  $i$ ,  
**data[i]** and **link[i]** together  
comprise a node

**first** = 8

data[8] = BAT

link[8] = 3

data[3] = CAT

link[3] = 4

data[4] = EAT

data[link[4]] = FAT

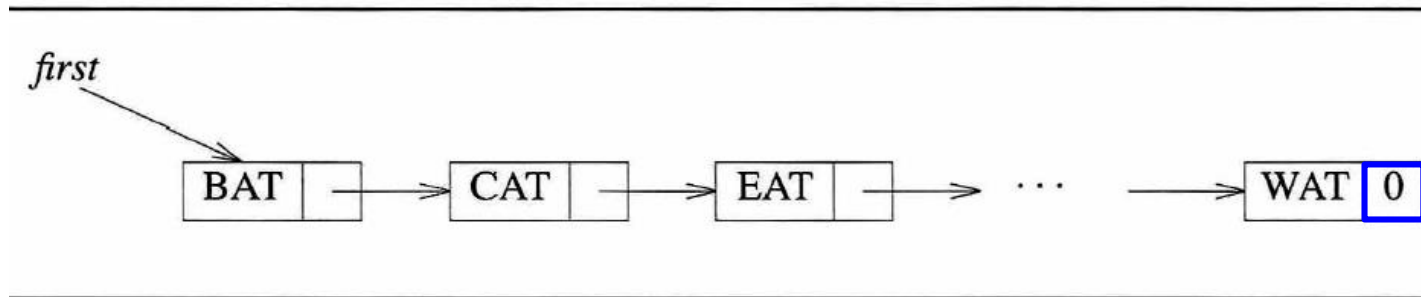
...

	<i>data</i>	<i>link</i>
1	HAT	15
2		
3	CAT	4
4	EAT	9
5		
6		
7	WAT	0
8	BAT	3
9	FAT	1
10		
11	VAT	7
	.	.
	.	.
	.	.

end

→ 데이터 끝 나타냄

**Figure 4.1:** Nonsequential list-representation using two arrays



**Figure 4.2:** Usual way to draw a linked list

first의 link만 알면 됨!

The linked structures are called **singly linked lists** or **chains**.

Insertions and deletions : ...

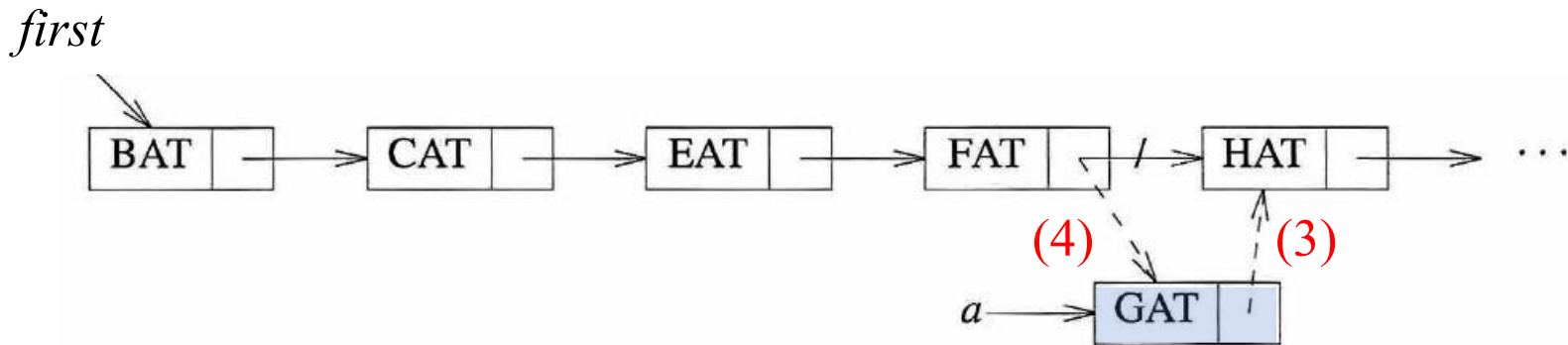
- Linked list: **Insert** (e.g. GAT):

(1) Get a node  $a$  that is currently unused

(2) Set the *data* field of  $a$  to GAT

(3) Set the *link* field of  $a$  to point to the node (HAT)

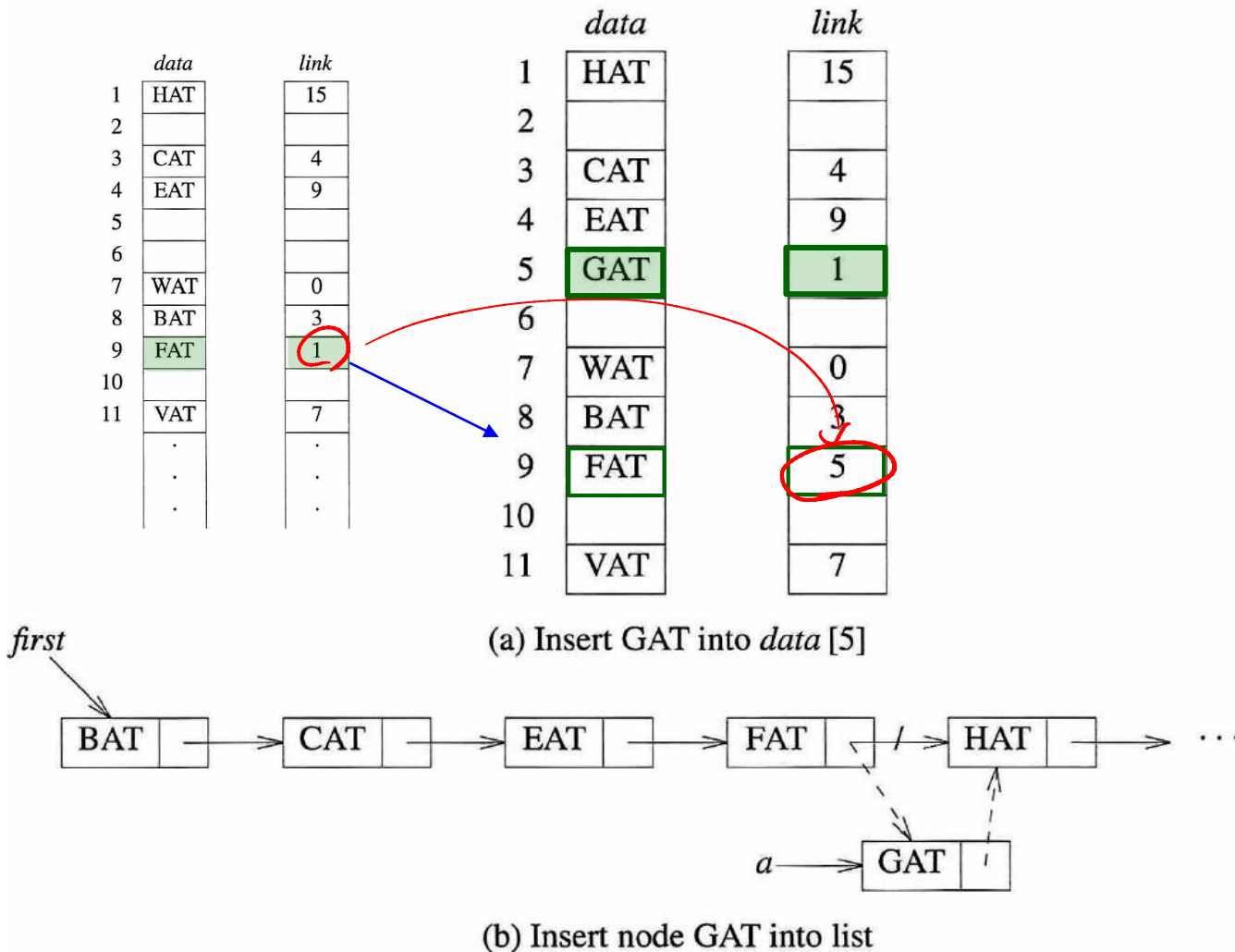
(4) Set the *link* field of the node (FAT) to  $a$



(b) Insert node GAT into list (1)(2)

(3), (4) 바뀌면 안됨!

HAT을 가리키는 바를 옮겨버리게됨

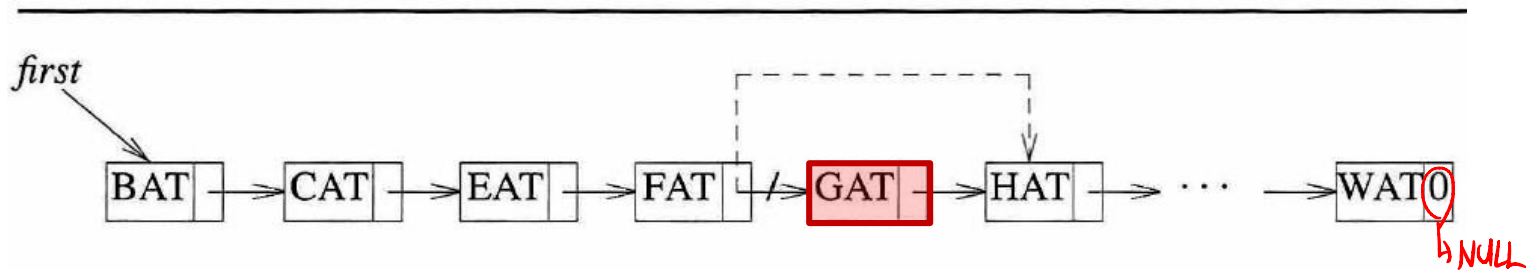


**Figure 4.3:** Inserting into a linked list



• Linked list: **Delete** (e.g. GAT)

- ① – Find the element (FAT) that immediately precedes GAT 이전노드찾고
- ② – Set its link field to point to the position of HAT



**Figure 4.4:** Delete GAT

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- Ex 4.1 [List of words]:

- Define a node structure for the list

```
typedef struct listNode *listPointer;
typedef struct listNode {
    char data [4];
    listPointer link;
};
```

구조체 포인터

```
typedef struct listNode {
    char data[4];
    struct listNode *link;
} listNode;
```

- Create a new empty list

```
listPointer first = NULL;
```

- Test for an empty list empty 이면 참이므로

```
#define IS_EMPTY( first ) ( !(first) )
```

- Allocation; to create new nodes

```
MALLOC( first, sizeof(*first) );
```

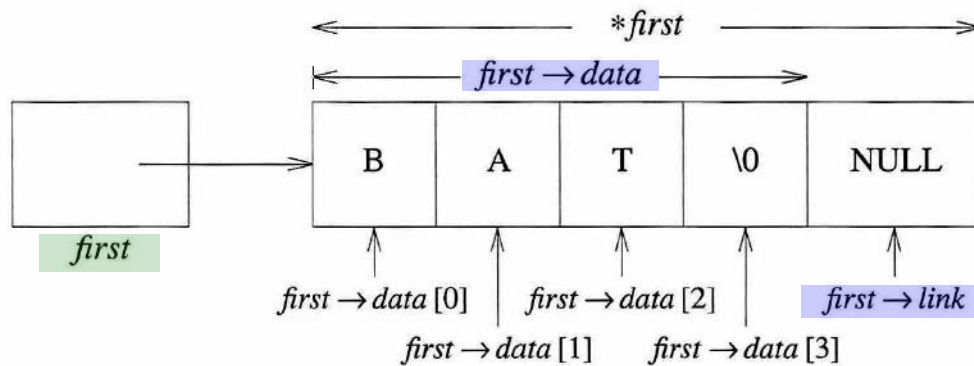
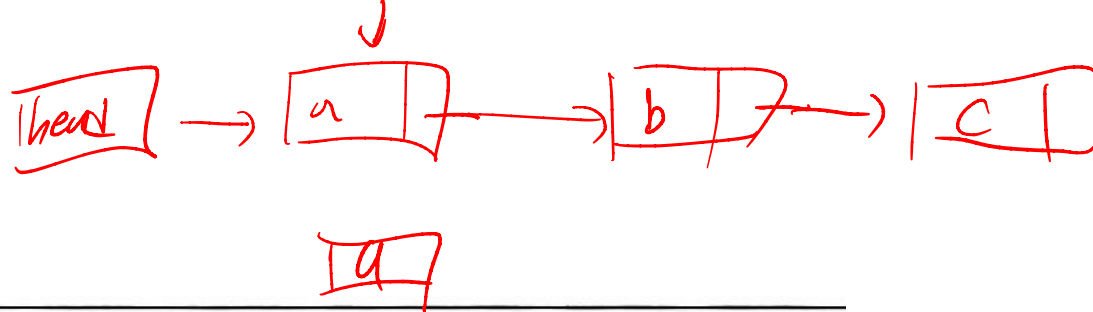
- To place the word BAT into the list

```
strcpy( first -> data, "BAT");
first -> link = NULL;
```

```
...
if( IS_EMPTY( first ) )
    ...
```

```
#define MALLOC(p,s) \
if ( ! ( (p) = malloc (s) ) ) { \
    fprintf(stderr, "Insufficient memory"); \
    exit(EXIT_FAILURE); \
}
```

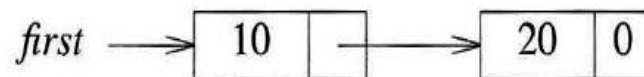
over



**Figure 4.5:** Referencing the fields of a node

```
typedef struct listNode *listPointer;
typedef struct listNode {
    char data [4];
    listPointer link;
};
```

- Ex 4.2 [**Two-node linked list**]
  - To create a linked list of integers : ...



**Figure 4.6:** A two-node list



**Figure 4.6:** A two-node list

```
listPointer create2()
{
    listPointer first, second;

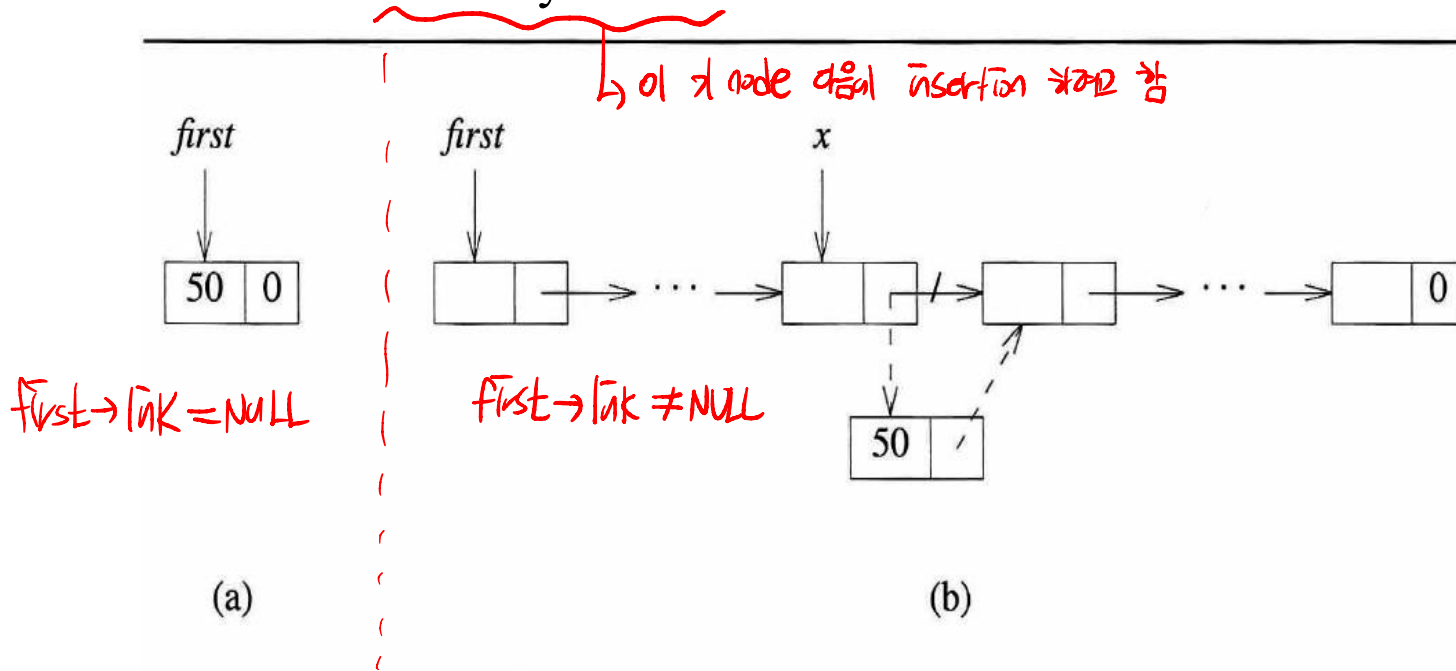
    MALLOC(first, sizeof(*first));
    MALLOC(second, sizeof(*second));

    second->link = NULL;
    second->data = 20;

    first->data = 10;
    first-> link = second;

    return first;
}
```

- Ex 4.3 [**List Insertion**]: `insert (&first, x );`
  - Let *first* be a pointer to a linked list
  - Assume that we want to insert a node with a data field of 50 after some arbitrary node *x*



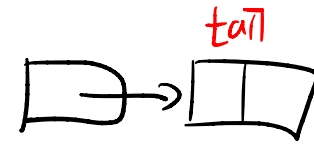
**Figure 4.7:** Inserting into an empty and nonempty list

```

void insert(listPointer *first, listPointer x)
{
    listPointer temp;
    MALLOC(temp, sizeof(*temp));
    temp->data = 50;
    if (*first) {    // noempty list
        temp->link = x->link;
        x->link = temp;
    }
    else {           // empty list
        temp->link = NULL;
        *first = temp;
    }
}

```

삽입하려는 node의 앞 노드



Function call:  
insert (&first, x );



순서 바뀌면  
차이 나타나는  
값을 넣음  
(= 다음 link값)

first만 있을때

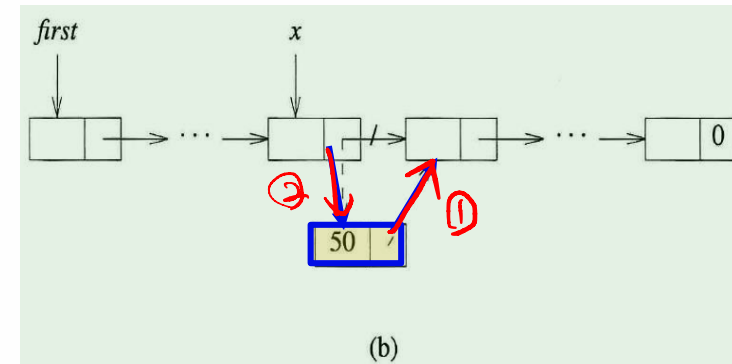
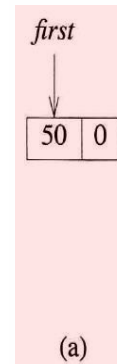


Figure 4.7: Inserting into an empty and nonempty list

Program 4.2: Simple insert into front of list

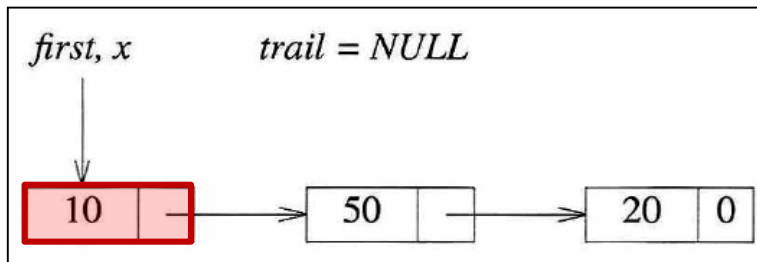


- Ex 4.4 [List Deletion]

- Deleting an arbitrary node from a list depends on the location of the node

- *first* points to the start of the list
- *x* points to the node that we wish to delete
- *trail* points to the node that precedes *x*

delete 하려는 node의 이전노드

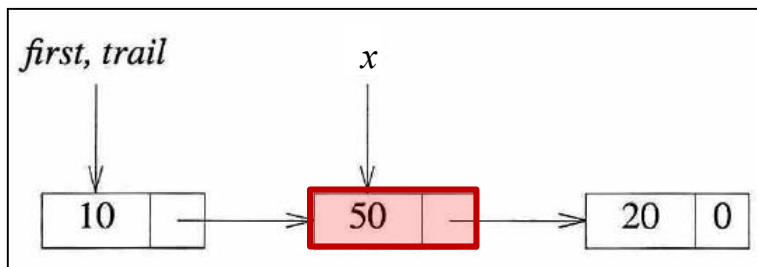


Delete 할 때

두 개의 case로 나누어 생각해야 함



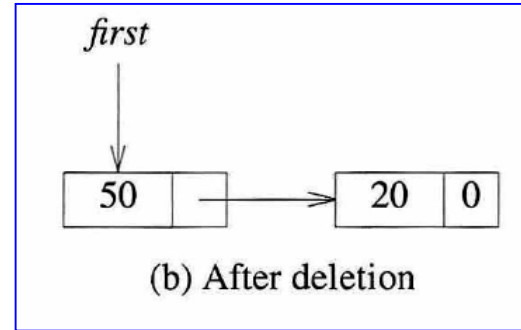
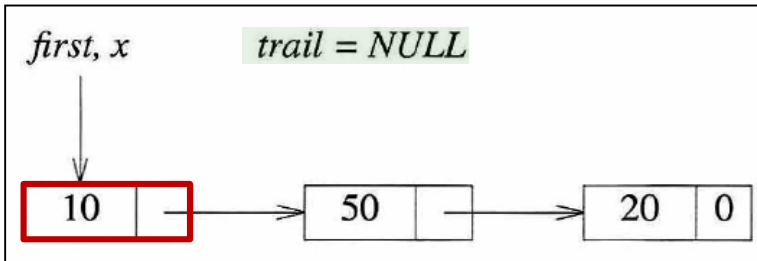
1) The *first* node



2) node other than the *first* node

1) delete the *first* node :

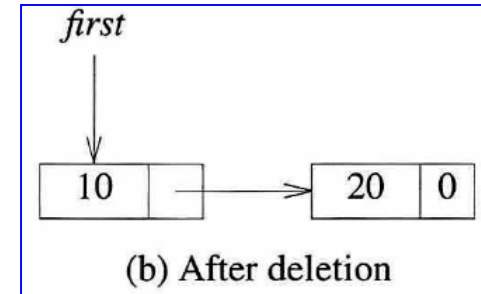
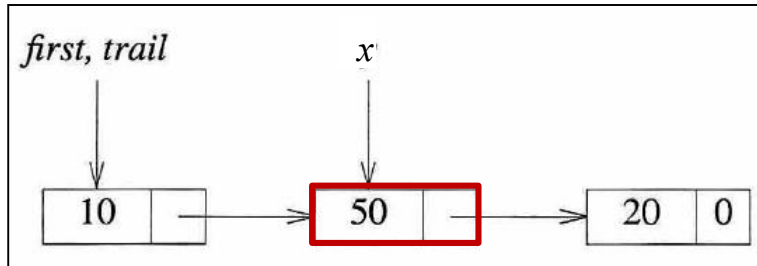
Function call:  
`delete( &first, NULL, x );`



```
void delete(listPointer *first, listPointer trail, listPointer x )
{
    if (trail)
        trail→link = x→link;
    else
        *first = (*first)→link;
    free(x);
}
```

**Program 4.3:** Deletion from a list

2) delete node other than the *first* node : `delete( &first, trail, x );`



```
void delete(listPointer *first, listPointer trail, listPointer x)
{
    if (trail)
        trail → link = x → link;
    else
        *first = (*first) → link;
    free(x);
}
```

**Program 4.3:** Deletion from a list

- Ex 4.5 [Printing out a list]:



```
printList( first );
```

```

void printList(listPointer first)
{
    printf("The list contains: ");
    for ( ; first; first = first->link)
        printf ( "%4d", first->data);
    printf ( " \n" );
}
  
```

*first->link \* NULL 이 될 때까지...*

**Program 4.4:** Printing a list

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"배열"을 이용한 stack, queue의 구현

vs

- A linked stack and a linked queue "연결리스트"를
- Adding/deleting a node: easy

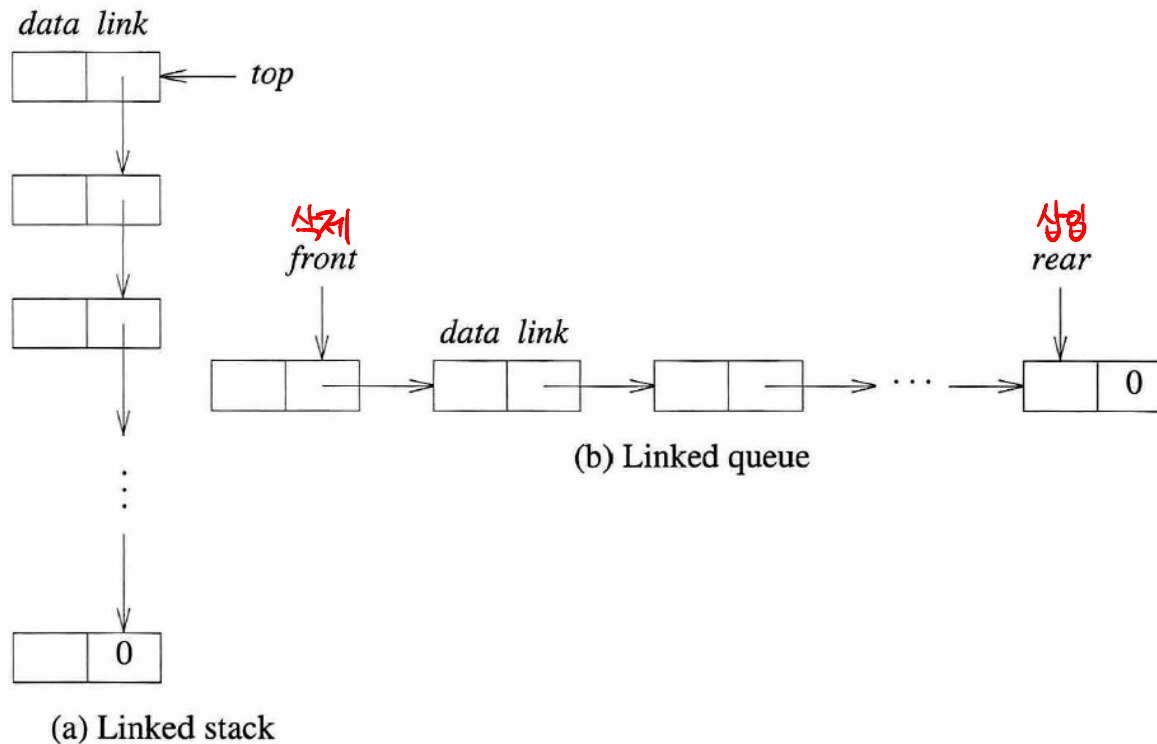


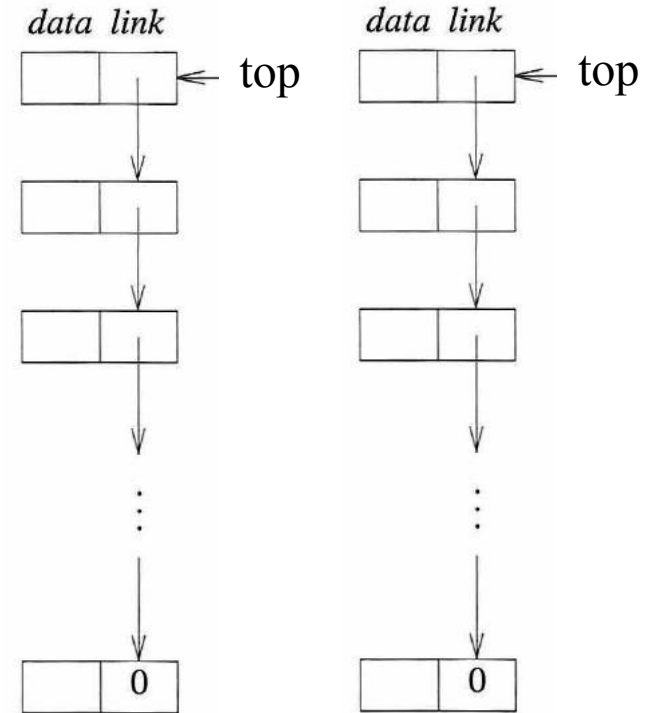
Figure 4.11: Linked stack and queue

*n개의 stack이 여러개 존재할 때*

- Represent ***n* stacks** simultaneously

```
#define MAX-STACKS 10
typedef struct {
    int key;
    /* other fields */
} element;
typedef struct stack *stackPointer;
typedef struct stack {
    element data;
    stackPointer link;
};
stackPointer top[MAX-STACKS];
```

- Initial condition for the stacks
  - $\text{top}[i] = \text{NULL}, 0 \leq i < \text{MAX\_STACKS}$
- Boundary condition:
  - $\text{top}[i] = \text{NULL}$  iff the  $i$ th stack is empty



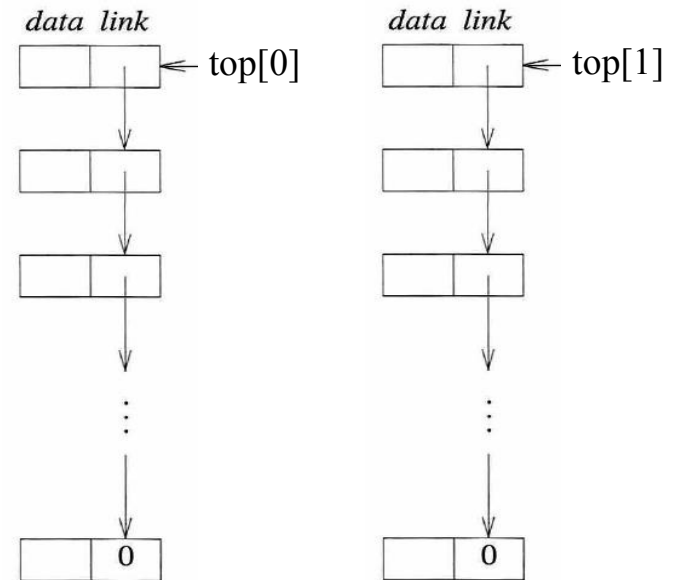
새로운 노드를 머리에 추가하는 형태

- Push in the linked stack

`push(1, item);`

`void push(int → Index i, element item)`  
`{/* add item to the ith stack */`  
`stackPointer temp;`  
`MALLOC(temp, sizeof(*temp));`  
`temp->data = item;`  
`temp->link = top[i];`  
`top[i] = temp;`  
`}`

**Program 4.5:** Add to a linked stack



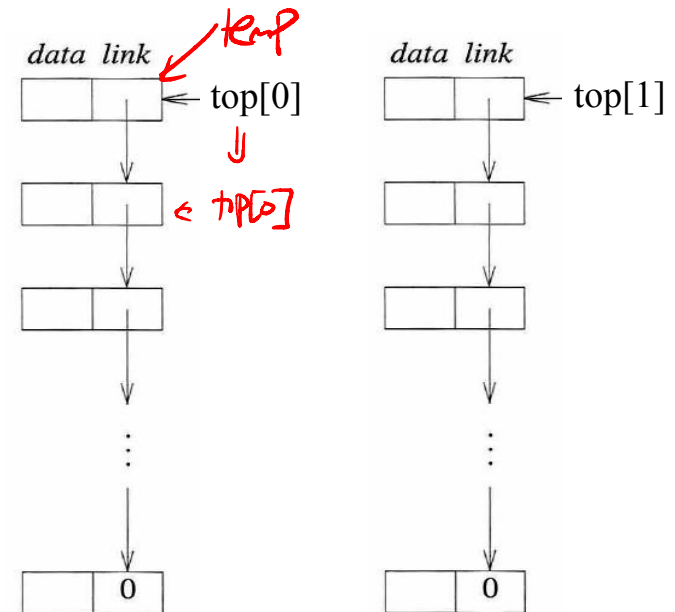


- Pop from the linked stack  
`item = pop(0);`

```

element pop( int i )
{
    /* remove top element from the ith stack */
    stackPointer temp = top[i];
    element item;
    if (!temp)
        return stackEmpty();
    item = temp->data;
    top[i] = temp->link;
    free (temp);
    return item;
}

```

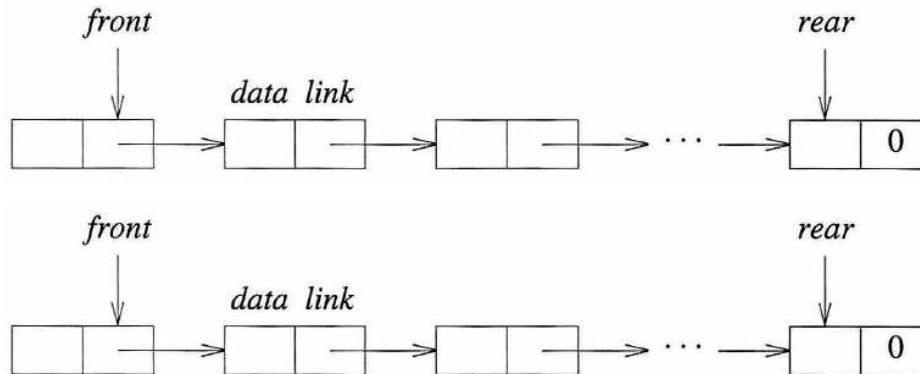


Program 4.6: Delete from a linked stack

- To represent *m* queues simultaneously

```
#define MAX-QUEUES 10 /* maximum number of queues */
typedef struct queue *queuePointer;
typedef struct queue {
    element data;
    queuePointer link;
} ;
queuePointer front[MAX-QUEUES], rear[MAX-QUEUES];
```

- Initial condition for the queues
  - $\text{front}[i] = \text{NULL}, 0 \leq i < \text{MAX\_QUEUES}$
- Boundary condition
  - $\text{front}[i] = \text{NULL}$ , iff the *i*th queue is empty



- Add operation for multiple queues

```
void addq(int i, element item)
```

```
{/* add item to the rear of queue i */
```

```
    queuePointer temp;
```

```
    MALLOC(temp, sizeof(*temp));
```

```
    temp->data = item;
```

```
    temp->link = NULL;
```

```
    if (front [i]) → if (front[i] != NULL)
```

```
        rear[i]->link = temp; rear 쪽에 temp를 추가
```

```
    else → 아무것도 없는 상황이면
```

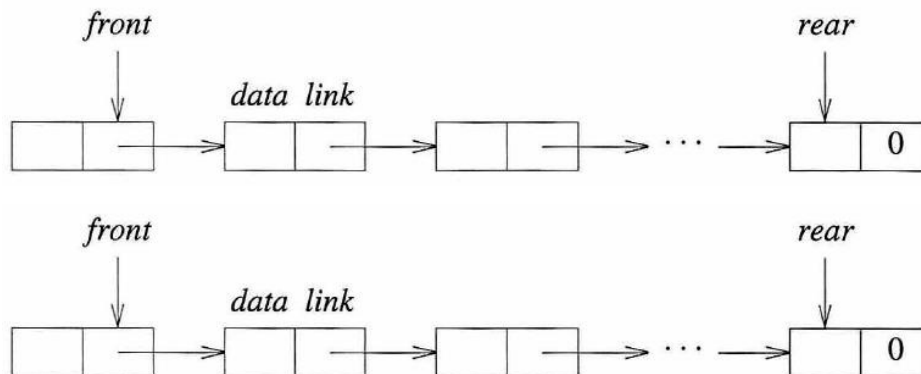
```
        front[i] = temp; front[i]에 temp를 추가하게
```

```
    rear[i] = temp; rear를 옮김
```

```
}
```

addq(0, item);

**Program 4.7:** Add to the rear of a linked queue



- Delete operation for multiple queues

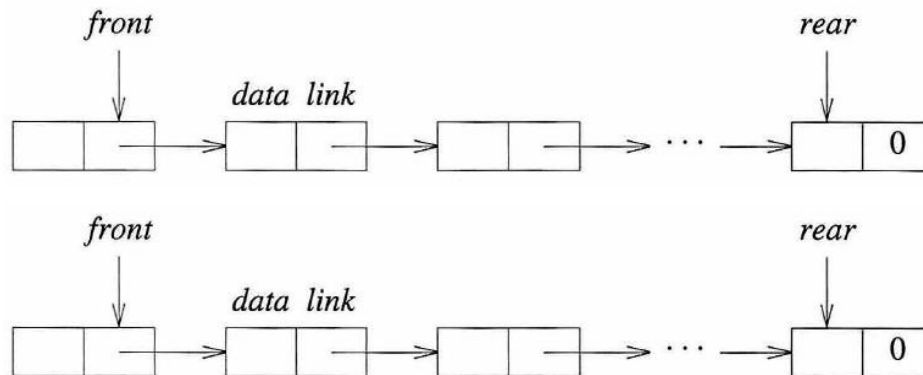
```

element deleteq(int i)
{ /* delete an element from queue i */
    queuePointer temp = front[i];
    element item;
    if (!temp)
        return queueEmpty();
    item = temp->data;
    front[i] = temp->link;
    free (temp) ;
    return item;
}

```

`item = deleteq(i);`

**Program 4.7:** Add to the rear of a linked queue



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