

# LINKED LIST

4.1 Singly Linked Lists and Chains

4.2 Representing Chains in C

4.3 Linked Stacks and Queues

**4.4 Polynomials**

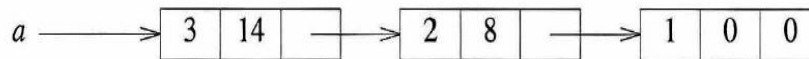
4.5 Additional List Operations

4.7 Sparse Matrixs

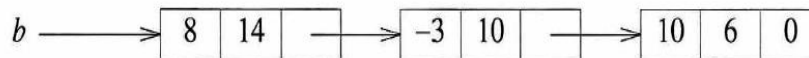
4.8 Doubly Linked Lists

## 4.4.1 Polynomial Representation

- Polynomials:  $a = 3x^{14} + 2x^8 + 1$   
 $b = 8x^{14} - 3x^{10} + 10x^6$
- Using linked lists



(a)



(b)

---

**Figure 4.12:** Representation of  $3x^{14} + 2x^8 + 1$  and  $8x^{14} - 3x^{10} + 10x^6$

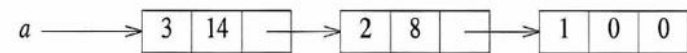
- Type declarations:

```
typedef struct polyNode *polyPointer;
struct polyNode {
    int coef;
    int expon;
    polyPointer link;
};
polyPointer a, b;
```

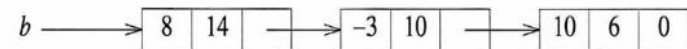
3개의 노드

coef	exp	link
------	-----	------

polyNode



(a)



(b)

Figure 4.12: Representation of  $3x^{14}+2x^8+1$  and  $8x^{14}-3x^{10}+10x^6$

## 4.4.2 Adding Polynomials: $c = a + b$

- Examine their terms starting at the nodes pointed to by  $a$  and  $b$

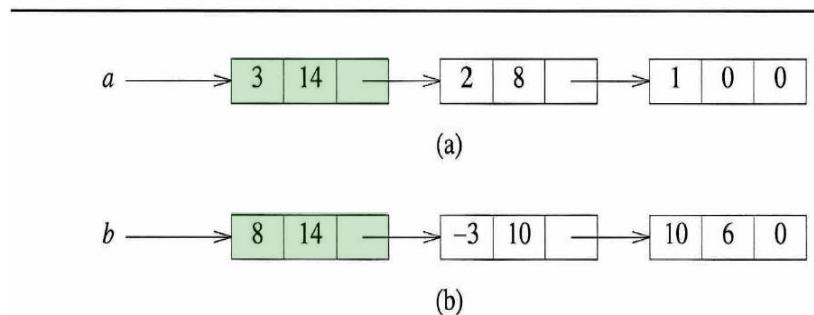


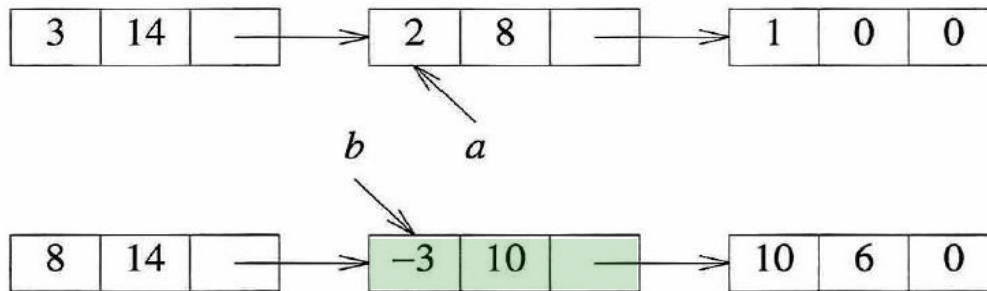
Figure 4.12: Representation of  $3x^{14} + 2x^8 + 1$  and  $8x^{14} - 3x^{10} + 10x^6$

- Case (i):  $a \rightarrow \text{expon} == b \rightarrow \text{expon}$ 
  - add the two coefficients
  - create a new term for the result (c)
  - move the pointers to the next nodes in  $a$  and  $b$

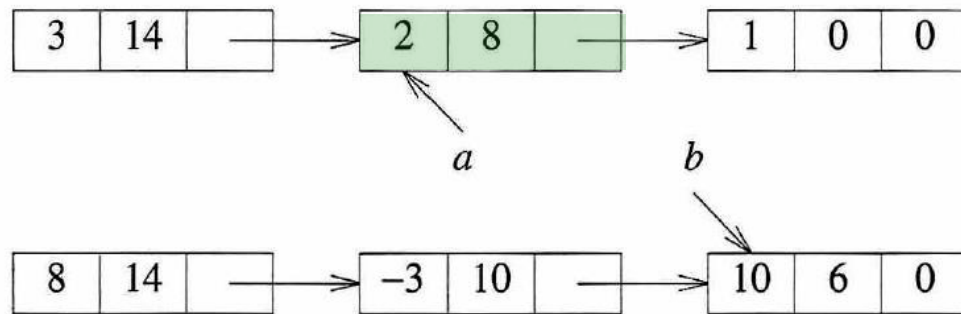
- Case (ii):  $a \rightarrow \text{expon} < b \rightarrow \text{expon}$

link a는 그대로, b만 이동시킴

- 1) create a duplicate term of b
- 2) attach this term to the result (c)
- 3) advance the pointer to the next term in b



- Case (iii):  $a \rightarrow \text{expon} > b \rightarrow \text{expon}$



```

polyPointer padd(polyPointer a, polyPointer b)
{
    polyPointer c, rear, temp;
    int sum;
    MALLOC(rear, sizeof(*rear));
    c = rear;
    while( a && b )
        switch( COMPARE(a->expon, b->expon) ) {
            case -1: /* a->expon < b->expon */
                attach(b->coef, b->expon, &rear);
                b = b->link;
                break;
            case 0: /* a->expon == b->expon */
                sum = a->coef + b->coef;
                if(sum) attach(sum, a->expon, &rear);
                a = a->link; b = b->link; break;
            case 1: /* a->expon > b->expon */
                attach(a->coef, a->expon, &rear);
                a = a->link;
        }
    /* copy rest of list a and then list b */
    for(; a; a=a->link) attach(a->coef, a->expon, &rear);
    for(; b; b=b->link) attach(b->coef, b->expon, &rear);
    rear->link = NULL;
    /* delete extra initial node */
    temp = c; c = c->link; free(temp);
    return c;
}

```

```

#define COMPARE (x, y)
( (x) < (y) ? -1 : (x) == (y) ? 0 : 1 )

```

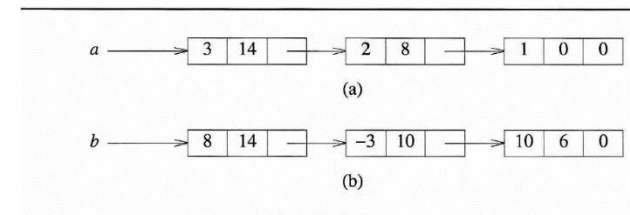
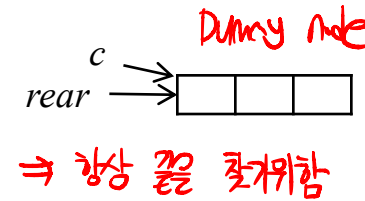


Figure 4.12: Representation of  $3x^{14}+2x^8+1$  and  $8x^{14}-3x^{10}+10x^6$

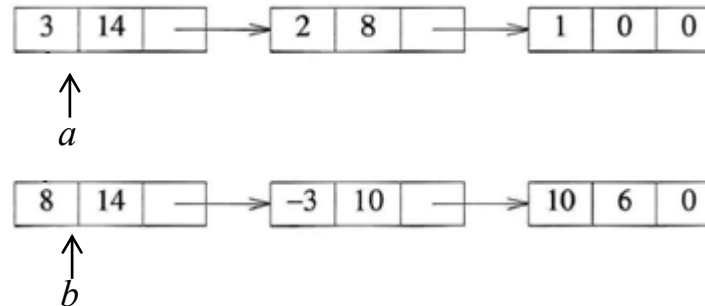
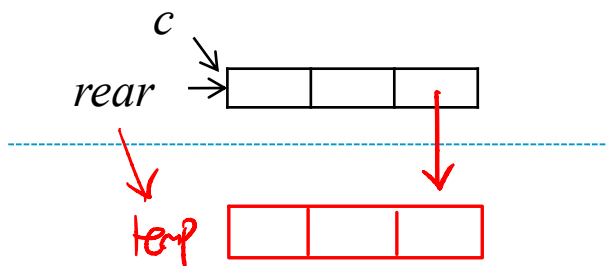
**Program 4.9:**  
Add two polynomials

이의 마지막을 가리키는 rear



```
void attach(float coefficient, int exponent, polyPointer *ptr)
{
    polyPointer temp;
    MALLOC(temp, sizeof(*temp));
    temp->coef = coefficient;
    temp->expon = exponent;
    (*ptr)->link = temp;
    *ptr = temp;                      /* move ptr to the end of the list */
}
```

**Program 4.10:** Attach a node to the end of a list



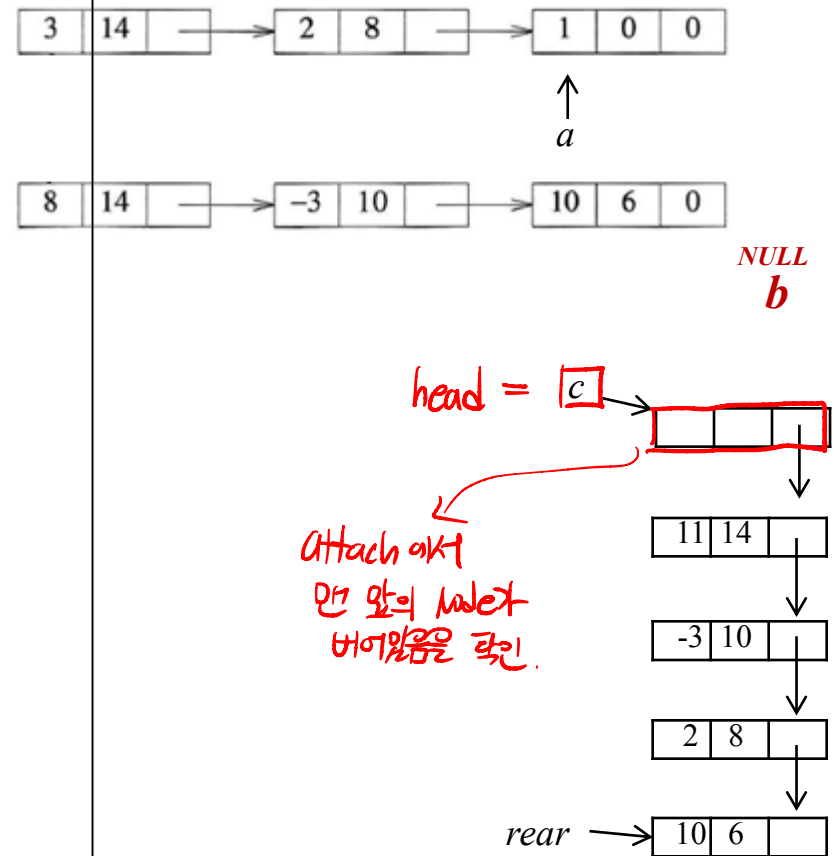
attach( 11, 14, &rear )



```

polyPointer padd(polyPointer a, polyPointer b)
{
    polyPointer c, rear, temp;
    int sum;
    MALLOC(rear, sizeof(*rear));
    c= rear;
    while(a && b)
        switch( COMPARE(a->expon, b->expon) ) {
            case -1: /* a->expon < b->expon */
                attach(b->coef, b->expon, &rear);
                b = b->link;
                break;
            case 0 : /* a->expon = b->expon */
                sum = a->coef + b->coef;
                if(sum) attach(sum, a->expon, &rear);
                a = a->link; b = b->link; break;
            case 1: /* a->expon > b->expon */
                attach(a->coef, a->expon, &rear);
                a = a->link;
        }
    /* copy rest of list a and then list b */
    for(; a; a=a->link) attach(a->coef, a->expon, &rear);
    for(; b; b=b->link) attach(b->coef, b->expon, &rear);
    rear->link = NULL;
    /* delete extra initial node */
    temp = c; c= c->link; free(temp);
    return c;
}

```



```
polyPointer padd(polyPointer a, polyPointer b)
```

```
{
```

```
    polyPointer c, rear, temp;
```

```
    int sum;
```

```
    MALLOC(rear, sizeof(*rear));
```

```
    c= rear;
```

```
    while(a && b)
```

```
        switch( COMPARE(a->expon, b->expon) ) {
```

```
            case -1: /* a->expon < b->expon */
```

```
                attach(b->coef, b->expon, &rear);
```

```
                b = b->link;
```

```
                break;
```

```
            case 0 : /* a->expon = b->expon */
```

```
                sum = a->coef + b->coef;
```

```
                if(sum) attach(sum, a->expon, &rear);
```

```
                a = a->link; b = b->link; break;
```

```
            case 1: /* a->expon > b->expon */
```

```
                attach(a->coef, a->expon, &rear);
```

```
                a = a->link;
```

```
        }
```

```
    /* copy rest of list a and then list b */
```

```
    for(; a; a=a->link) attach(a->coef, a->expon, &rear);
```

```
    for(; b; b=b->link) attach(b->coef, b->expon, &rear);
```

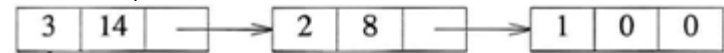
```
    rear->link = NULL;
```

```
    /* delete extra initial node */
```

```
    temp = c; c= c->link; free(temp);
```

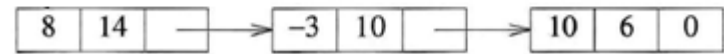
```
    return c;
```

```
}
```



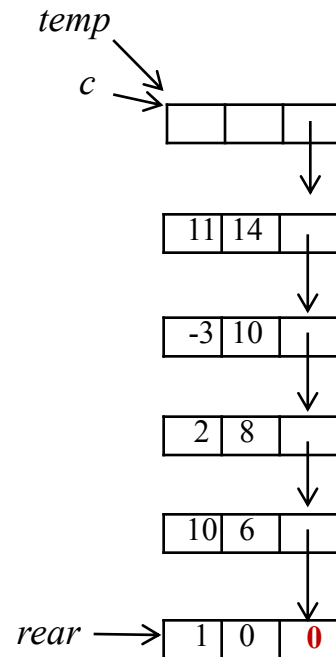
NULL

*a*



NULL

*b*



```

polyPointer padd(polyPointer a, polyPointer b)
{
    polyPointer c, rear, temp;
    int sum;
    MALLOC(rear, sizeof(*rear));
    c = rear;
    while(a && b)
        switch( COMPARE(a->expon, b->expon) ) {
            case -1: /* a->expon < b->expon */
                attach(b->coef, b->expon, &rear);
                b = b->link;
                break;
            case 0 : /* a->expon = b->expon */
                sum = a->coef + b->coef;
                if(sum) attach(sum, a->expon, &rear);
                a = a->link; b = b->link; break;
            case 1: /* a->expon > b->expon */
                attach(a->coef, a->expon, &rear);
                a = a->link;
        }
    /* copy rest of list a and then list b */
    for(; a; a=a->link) attach(a->coef, a->expon, &rear);
    for(; b; b=b->link) attach(b->coef, b->expon, &rear);
    rear->link = NULL;
    /* delete extra initial node */
    temp = c; c = c->link; free(temp);
    return c;
}

```

## Analysis of *padd*:...

$O(a+b)$

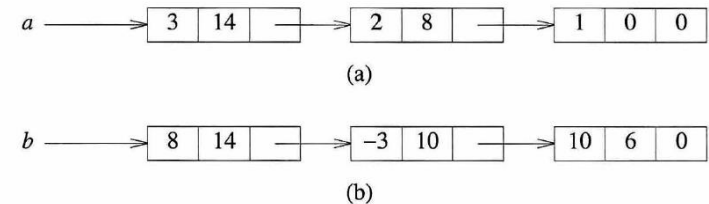


Figure 4.12: Representation of  $3x^{14} + 2x^8 + 1$  and  $8x^{14} - 3x^{10} + 10x^6$

다항식 지우기

## 4.4.3 Erasing Polynomials

↓ a

```
void erase(polyPointer *ptr)
{ /* erase the polynomial pointed to by ptr */
    polyPointer temp;
    while(*ptr) {
        temp = *ptr;
        *ptr = (*ptr)->link;
        free(temp);
    }
}
```



$a == *ptr$



$ptr$

erase( &a )

# LINKED LIST

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4.4 Polynomials

**4.5 Additional List Operations**

4.7 Sparse Matrixs

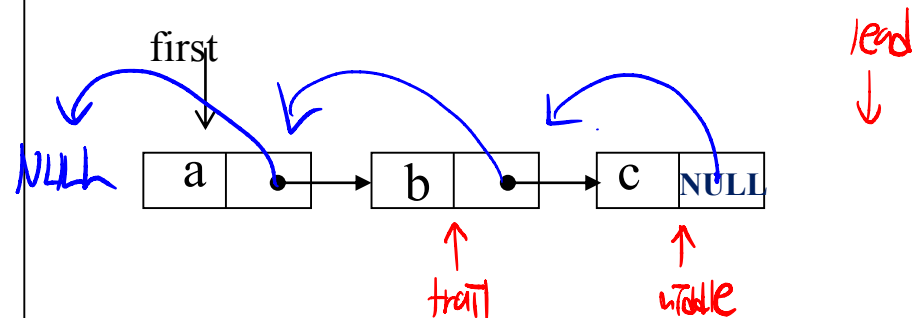
4.8 Doubly Linked Lists

## 4.5.1 Operations For Chains

- Inverting (or reversing) a chain
  - we can do it "in place" if we use three pointers

```
listPointer invert( listPointer lead )
{ /* invert the list pointed to by lead */
  listPointer middle, trail;
  middle = NULL;
  while ( lead ) {
    trail = middle;
    middle = lead;
    lead = lead->link;
    middle->link = trail;
  }
  return middle;
}
```

↪ Invert 한 middle의 first를 가리키게 됨



Time complexity: ...

**Program 4.16:** Inverting a singly linked list

function call:

first = **invert(first)**

- Concatenating two chains :

```

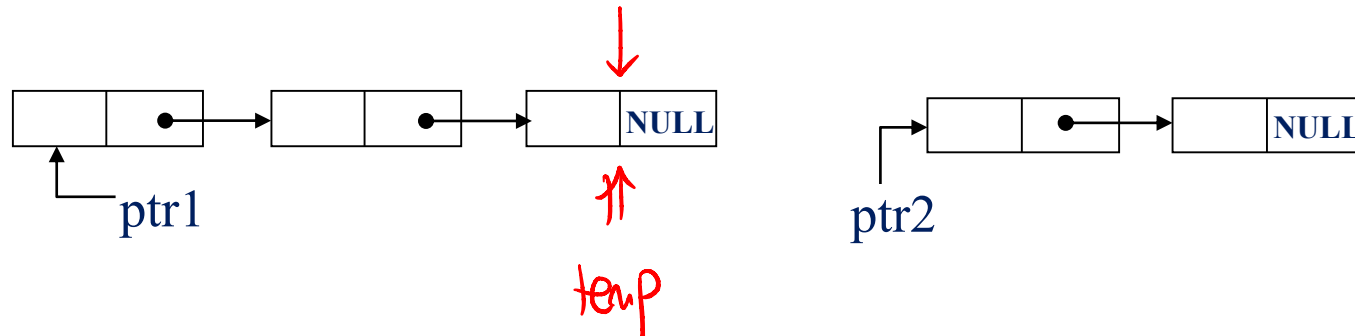
listPointer concatenate(listPointer ptr1, listPointer ptr2) {
    listPointer temp;
    /* check for empty lists */
    if(!ptr1) return ptr2; if(!ptr2) return ptr1;

    /* neither list is empty, find end of first list */
    for(temp = ptr1; temp->link ; temp = temp->link) ;
    /* link end of first to start of second */
    temp->link = ptr2;
    return ptr1;
}

```

시간복잡도 : ptr1의 length

야들 찾아주어야함



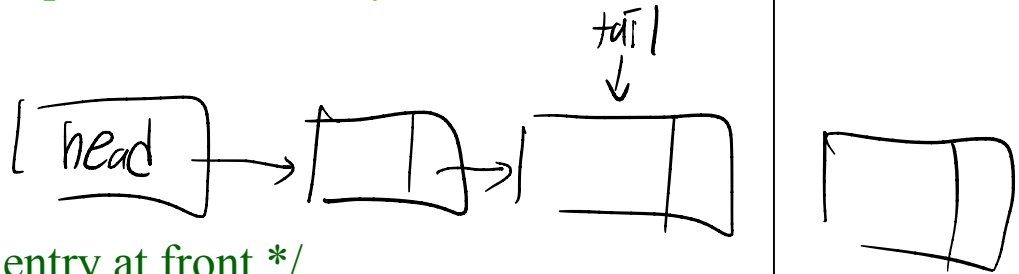
- Time complexity: ...

## 4.5.2 Operations For Circularly Linked Lists

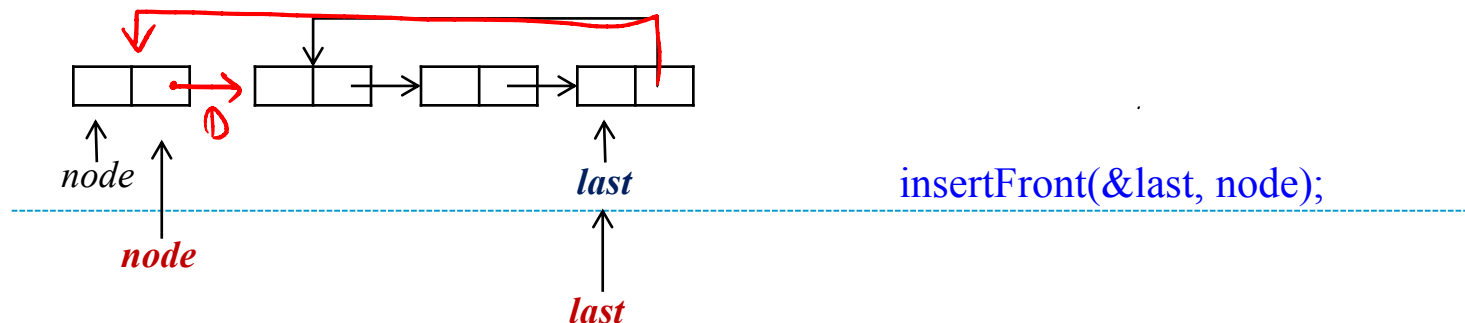
```

void insertFront(listPointer *last, listPointer node)
{ /* insert node at the front of the circular list whose last node is last */
  if (IS_EMPTY(*last)) {
    /* list is empty, change last to point to new entry */
    *last = node;
    node->link = node;
  }
  else {
    /* list is not empty, add new entry at front */
    node->link = (*last)->link;
    (*last)->link = node;
  }
}

```



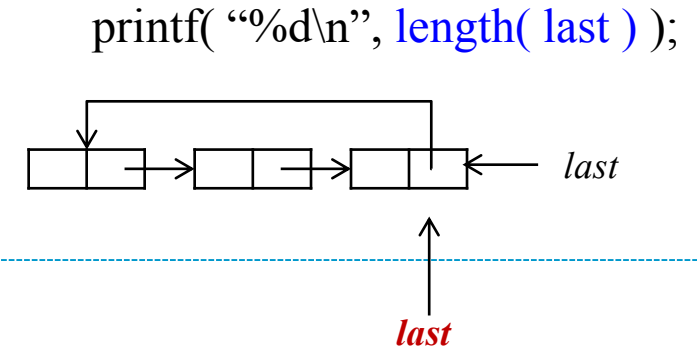
**Program 4.18:** Inserting at the front of a list





- Finding the length of a circular list

```
int length(listPointer last)
{
    listPointer temp;
    int count = 0;
    if (last) {
        temp = last;
        do {
            count++;
            temp = temp->link;
        } while ( temp != last );
    }
    return count;
}
```

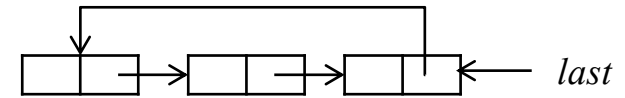


**Program 4.19:** Finding the length of a circular list

↓ length 항상 변

```
if ( search(last, x) ) printf("%d\n", x);
```

```
listPointer search(listPointer last, int x)
{
    listPointer temp = last;
    do {
        if (temp->data == x) return temp;
        temp=temp->link;
    } while (temp != last);
    return NULL;
}
```



# LINKED LIST

4.1 Singly Linked Lists and Chains

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4.4 Polynomials

4.5 Additional List Operations

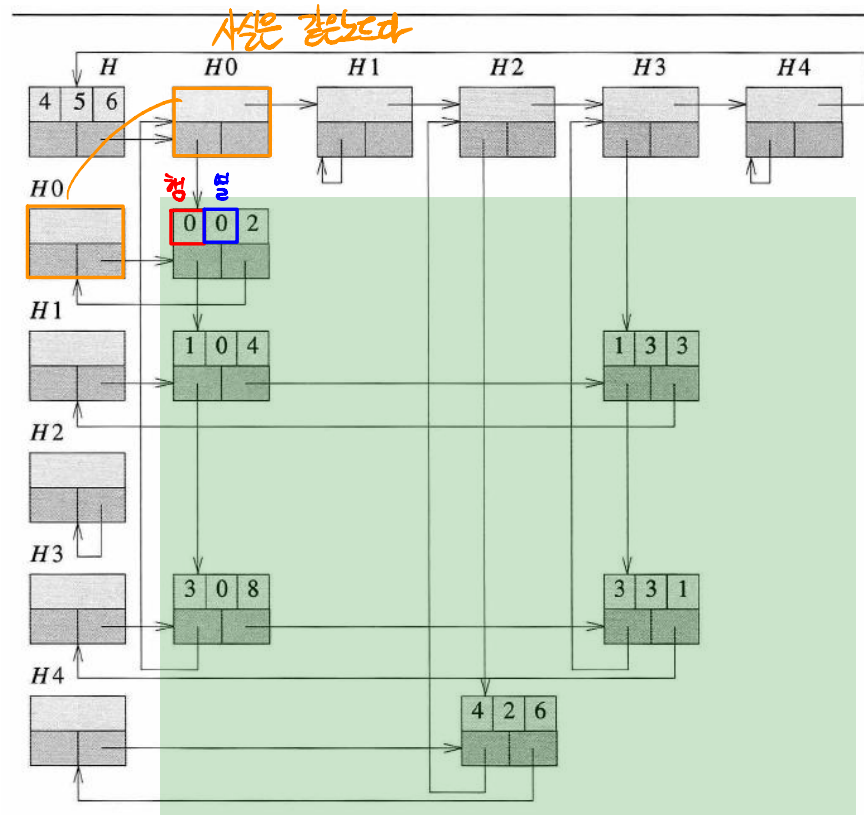
**4.7 Sparse Matrixs**

4.8 Doubly Linked Lists

## 4.7.1 Sparse Matrix Representation

$$\begin{bmatrix} 2 & 0 & 0 & 0 \\ 4 & 0 & 0 & 3 \\ 0 & 0 & 0 & 0 \\ 8 & 0 & 0 & 1 \\ 0 & 0 & 6 & 0 \end{bmatrix}$$

**Figure 4.18:**  
5 x 4 sparse matrix  $a$



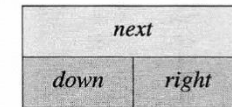
**Figure 4.19:** Linked representation of the sparse matrix of Figure 4.18 (the *head* field of a node is not shown)

- Node structure for sparse matrices

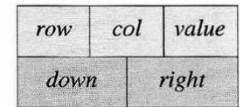
```
#define MAX_SIZE 50  /* size of largest matrix */
typedef enum {head,entry} tagfield;
typedef struct matrixNode *matrixPointer;
struct entryNode {
    int row;
    int col;
    int value;
};
```

```
struct matrixNode {
    matrixPointer down; col
    matrixPointer right; row
    tagfield tag; ← head or element 노드 구분
    union {
        matrixPointer next;
        entryNode entry;
    } u;
};
```

```
matrixPointer hdnode[MAX_SIZE];
```



(a) header node



(b) element node

tag field is not shown

Figure 4.17: Node structure for sparse matrices

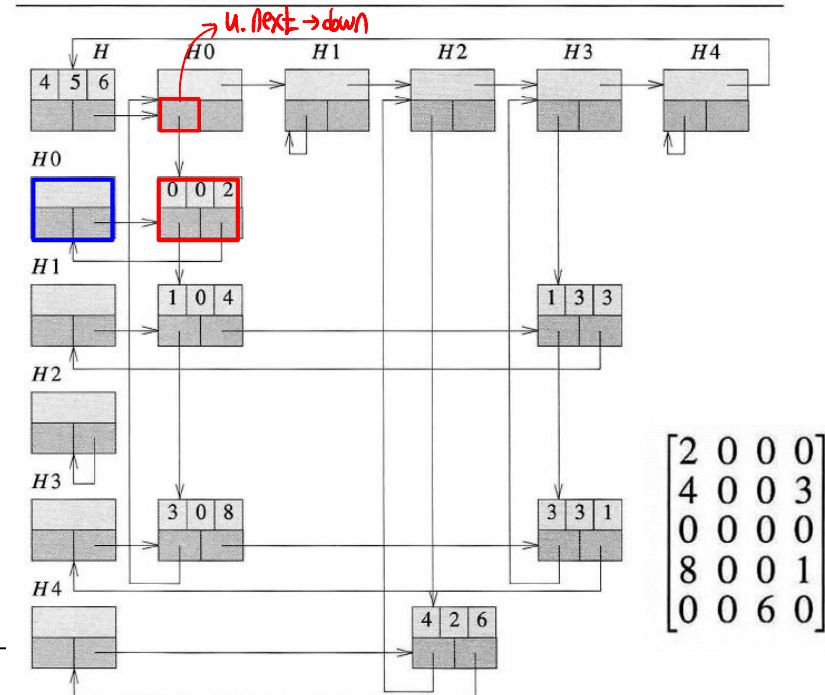
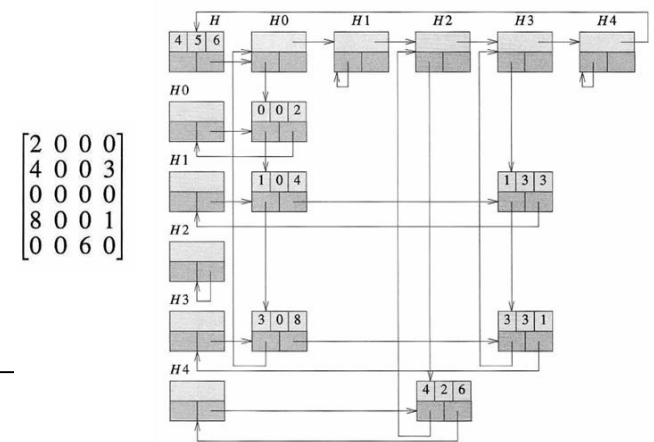


Figure 4.19: Linked representation of the sparse matrix of Figure 4.18 (the head field of a node is not shown)

## 4.7.2 Sparse Matrix Input



```
matrixPointer mread(void)
{ /* read in a matrix and set up its linked representation. An auxiliary global
array hdnode is used*/
  int numRows, numCols, numTerms, numHeads, i;
  int row, col, value, currentRow;
  matrixPointer temp, last, node;

  printf("Enter the number of rows, columns, and number of nonzero terms: "
  scanf("%d%d%d", &numRows, &numCols, &numTerms);
```

5 4 6

Enter the number of rows, columns, and number of nonzero terms:

5 4 6

4                      5                      4                      5

```
numHeads = (numCols > numRows) ? numCols : numRows;
```

```
/* set up header node for the list of header nodes */
```

```
node = newNode();  node->tag = entry;
```

```
node->u.entry.row = numRows;
```

```
node->u.entry.col = numCols;
```

```
if (!numHeads) node->right = node;
```

```
else { /* initialize the header nodes */
```

```
    for (i = 0; i < numHeads; i++) {
```

```
        temp = newNode();
```

```
        hdnode[i] = temp;
```

```
        hdnode[i]->tag = head;
```

```
        hdnode[i]->right = temp;
```

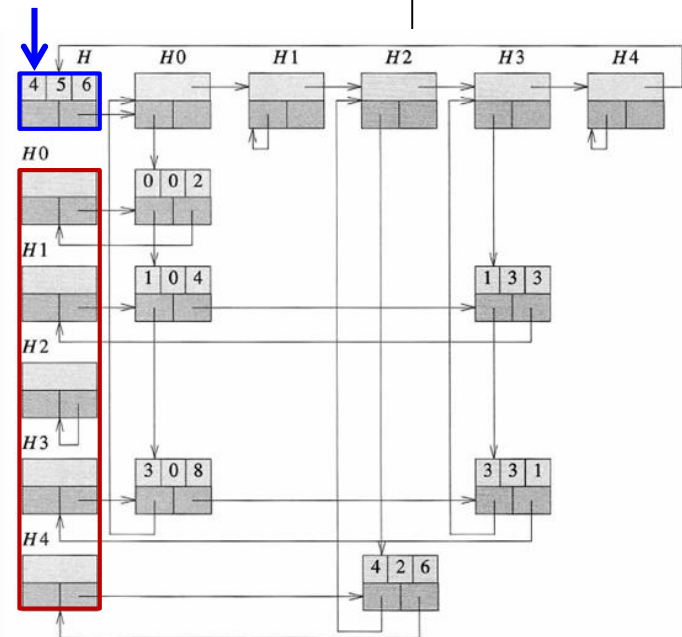
```
        hdnode[i]->u.next = temp;
```

```
    }
```

```
[ 2 0 0 0 ]
[ 4 0 0 3 ]
[ 0 0 0 0 ]
[ 8 0 0 1 ]
[ 0 0 6 0 ]
```

hdnode[i] →

node



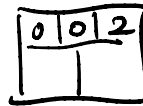
```

currentRow = 0;
last = hdnode[0]; /* last node in current row */
for (i = 0; i < numTerms; i++) {
    printf("Enter row, column and value: ");
    scanf("%d%d%d", &row,&col,&value);

    if (row > currentRow) { /* close current row */
        last->right = hdnode[currentRow];
        currentRow = row;
        last = hdnode[row];
    }
    temp = newNode();
    temp->tag = entry;
    temp->u.entry.row = row; temp->u.entry.col = col;
    temp->u.entry.value = value;

    last->right = temp; /* link into row list */
    last = temp;
    /* link into column list */
    hdnode[col]->u.next->down = temp;
    hdnode[col]->u.next = temp;
}
/* close last row */
last->right = hdnode[currentRow];

```



Enter row, column and value:

0 0 2

1 0 4

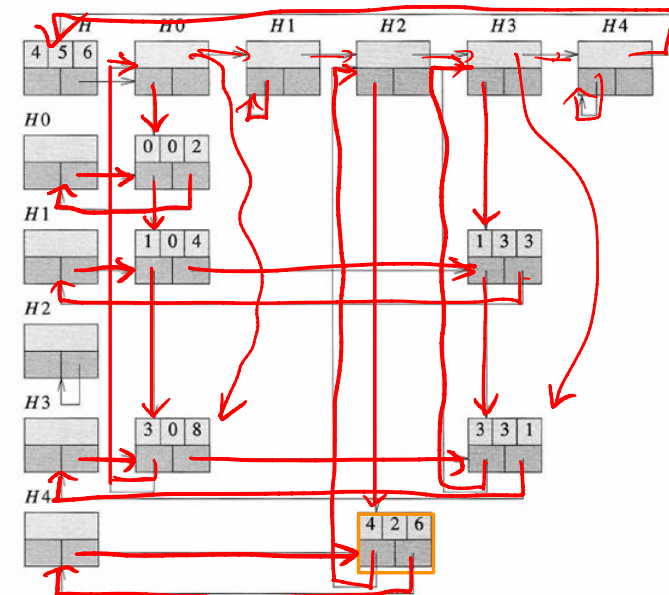
1 3 3

3 0 8

3 3 1

4 2 6

2	0	0	0
4	0	0	3
0	0	0	0
8	0	0	1
0	0	6	0





```
/* close all column lists */
```

```
for (i = 0; i < numCols; i++)
```

```
    hdnode[i]->u.next->down = hdnode[i];
```

```
/* link all header nodes together */
```

```
for (i = 0; i < numHeads-1; i++)
```

```
    hdnode[i]->u.next = hdnode[i+1];
```

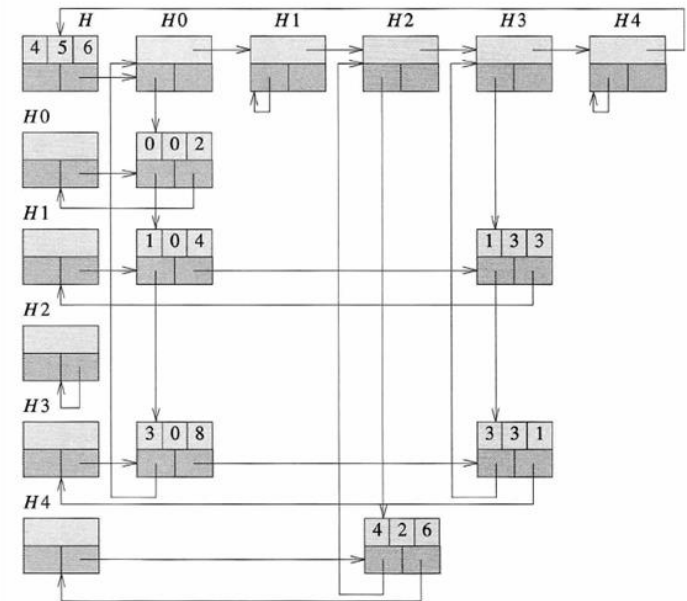
```
hdnode[numHeads-1]->u.next = node;
```

```
node->right = hdnode[0];
```

```
}
```

```
return node;
```

```
}
```

$$\begin{bmatrix} 2 & 0 & 0 & 0 \\ 4 & 0 & 0 & 3 \\ 0 & 0 & 0 & 0 \\ 8 & 0 & 0 & 1 \\ 0 & 0 & 6 & 0 \end{bmatrix}$$


**Program 4.23:** Read in a sparse matrix

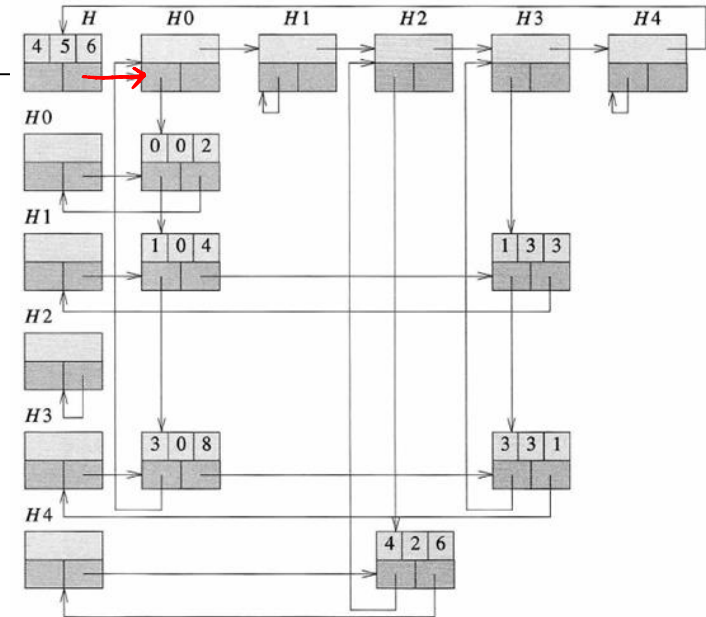
## 4.7.3 Sparse Matrix Output

```

void mwrite(matrixPointer node)
{ /* print out the matrix in row major form */
  int i;
  matrixPointer temp, head = node->right;
  /* matrix dimensions */
  printf("\n numRows = %d, numCols = %d \n",
        node->u.entry.row, node->u.entry.col);

  printf(" The matrix by row, column, and value: \n\n");
  for (i = 0; i < node->u.entry.row; i++) {
    /* print out the entries in each row */
    for ( temp = head->right; temp != head; temp = temp->right )
      printf("%5d%5d%5d \n", temp->u.entry.row,
                                temp->u.entry.col, temp->u.entry.value);
    head = head->u.next; /* next row */
  }
}

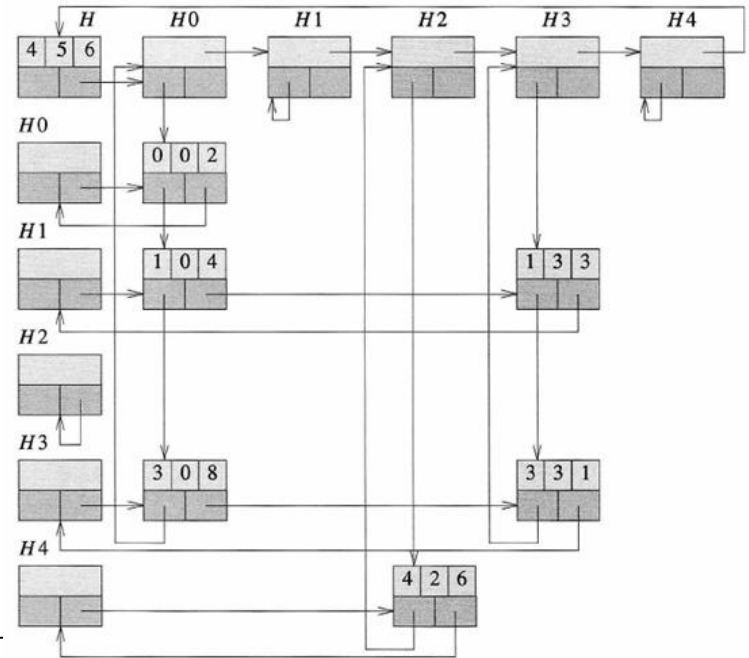
```



**Program 4.24:** Write out a sparse matrix

#### 4.7.4 Erasing a Sparse Matrix

```
void merase(matrixPointer *node)
{
    /* erase the matrix, return the nodes to the heap. */
    matrixPointer x,y, head = (*node)->right;
    int i, numHeads;
    /* free the entry and header nodes by row. */
    for (i = 0; i < (*node)->u.entry.row; i++) {
        y = head->right;
        while ( y != head )
            {x = y; y = y->right; free(x);}
        x = head; head = head->u.next; free(x);
    }
    /* free remaining header nodes. */
    y = head;
    while (y != *node)
        {x = y; y = y->u.next; free(x);}
    free(*node); *node = NULL;
}
```



---

**Program 4.25:** Erase a sparse matrix

# LINKED LIST

4.1 Singly Linked Lists and Chains

4.2 Representing Chains in C

4.3 Linked Stacks and Queues

4.4 Polynomials

4.5 Additional List Operations

4.7 Sparse Matrixs

**4.8 Doubly Linked Lists**

- Doubly linked lists
  - Move in forward and backward direction
  - A node has at least three fields:  
left link field, data field, right link field

```
typedef struct node *nodePointer;  
typedef struct node {  
    nodePointer llink;  
    element data;  
    nodePointer rlink;  
}
```

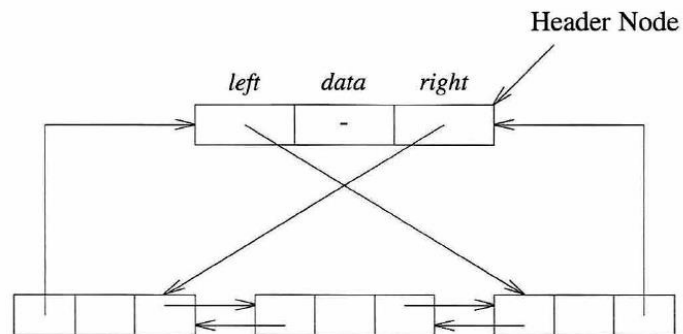
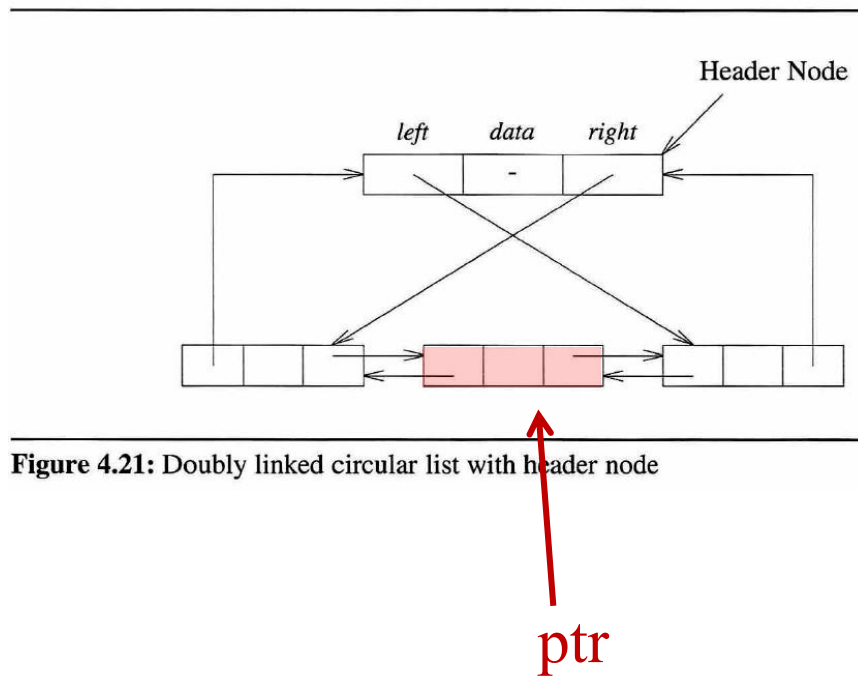
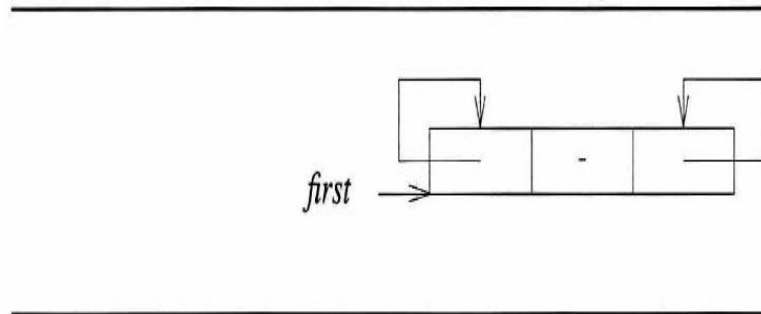


Figure 4.21: Doubly linked circular list with header node

- If *ptr* points to any node in a doubly linked list, then:  
$$ptr = ptr \rightarrow llink \rightarrow rlink = ptr \rightarrow rlink \rightarrow llink$$





**Figure 4.22:** Empty doubly linked circular list with header node

- Insert node <sup>해보기</sup>

```

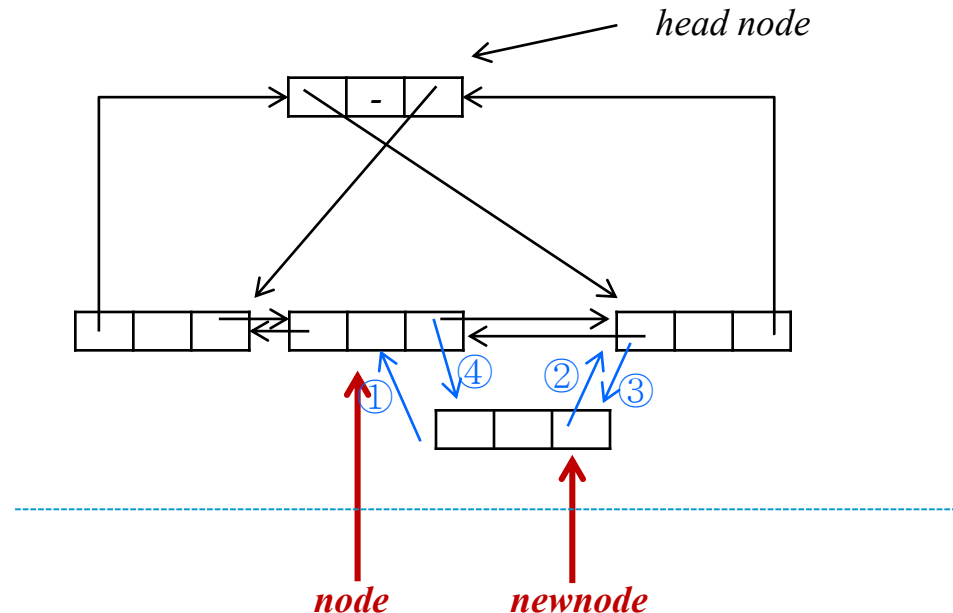
void dinsert(nodePointer node, nodePointer newnode)
{ /* insert newnode to the right of node */
    newnode->llink = node;
    newnode->rlink = node->rlink;
    node->rlink->llink = newnode;
    node->rlink = newnode;
}

```

) newnode 부터 연결

) 기존 node를 연결

**Program 4.26:** Insertion into a doubly linked circular list

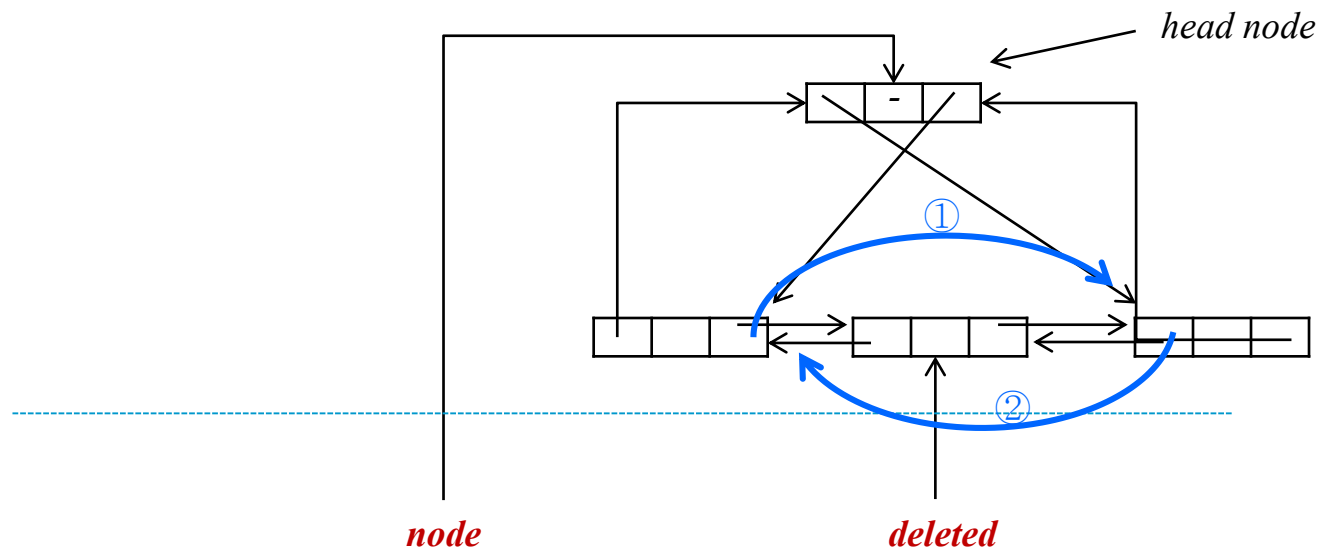


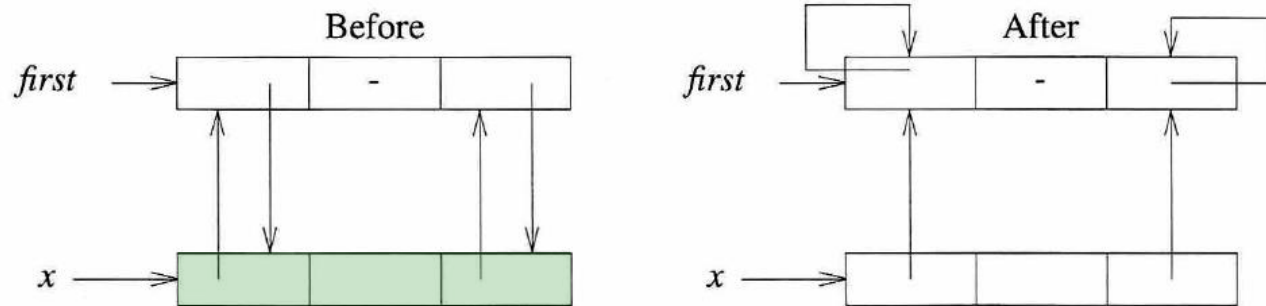


- Delete node

```
void ddelete(nodePointer node, nodePointer deleted)
{ /* delete from the doubly linked list */
  if (node == deleted)
    printf("Deletion of head node not permitted.\n");
  else {
    deleted->llink->rlink = deleted->rlink;
    deleted->rlink->llink = deleted->llink;
    free(deleted);
  }
}
```

**Program 4.27:** Deletion from a doubly linked circular list





**Figure 4.23:** Deletion from a doubly linked circular list **with a single node**

```
deleted->llink->rlink = deleted->rlink;  
deleted->rlink->llink = deleted->llink;  
free(deleted);
```

# LINKED LIST

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