

Recap

Redundancy is Bad

accountNo	balance	customer	branch	address	assets
A-101	500	1313131	Downtown	Brooklyn	9000000
A-102	400	1313131	Perryridge	Horseneck	1700000
A-113	600	9876543	Round Hill	Horseneck	8000000
A-201	900	9876543	Brighton	Brooklyn	7100000
A-215	700	1111111	Mianus	Horseneck	400000
A-222	700	1111111	Redwood	Palo Alto	2100000
A-305	350	1234567	Round Hill	Horseneck	8000000
...

what if we want to

- change balance of A-113
- add new account
- delete account
- update branch address

Functional Dependency

$X \rightarrow Y$

can be read as:

- Y functionally depends on X
- X determines Y
- if we know X then we know Y

Rules

reflexivity: $X \rightarrow X$

augmentation: $X \rightarrow Y \Rightarrow XZ \rightarrow YZ$

transitivity: $X \rightarrow Y, Y \rightarrow Z \Rightarrow X \rightarrow Z$

additivity: $X \rightarrow Y, X \rightarrow Z \Rightarrow X \rightarrow YZ$

projectivity: $X \rightarrow YZ \Rightarrow X \rightarrow Y, X \rightarrow Z$

pseudotransitivity: $X \rightarrow Y, YZ \rightarrow W \Rightarrow XZ \rightarrow W$

What is a trivial functional dependency $X \rightarrow Y$?

Y is a subset of X

Closure

X^+ largest set of attributes that can be derived from X using F

where

X set of attributes

F set of functional dependencies

Super Key

set of attributes that uniquely identifies a tuple in a table

any set X , such that $X^+ = R$

Candidate Key

a.k.a primary key

minimal superkey

any set X , such that $X^+ = R$ and there is no Y subset of X such that $Y^+ = R$

Boyce-Codd Normal Form (BCNF)

for all functional dependencies $X \rightarrow Y$

either

- $X \rightarrow Y$ is trivial

or

- X is a super key

Third Normal Form (3NF)

for all functional dependencies $X \rightarrow Y$

either

- $X \rightarrow Y$ is trivial

or

- X is a super key

or

- Y is single attribute of a candidate key

BCNF vs 3NF

	BCNF	3NF
lossless join	✓	✓
preserves all fds	✗	✓