

## 1 Problem 21.6

	Source	SS	df	MS
	Blocks	433.3667	9	48.152
a)	Training methods	1,295.0	2	647.5
	Error	112.3333	18	6.241
	Total	1,840.7	29	

b)  $\bar{Y}_{.1} = 70.6$ ,  $\bar{Y}_{.2} = 74.6$ ,  $\bar{Y}_{.3} = 86.1$

c)  $H_0$ : all  $\tau_j$  equal zero,  $H_a$ : not all  $\tau_j$  equal zero.

$$F^* = 103.754 > F(.95, 2, 18) = 3.55. \text{ Conclude } H_a.$$

d)  $\hat{D}_1 = \bar{Y}_{.1} - \bar{Y}_{.2} = -4.0$ ,  $\hat{D}_2 = \bar{Y}_{.1} - \bar{Y}_{.3} = -15.5$ ,  $\hat{D}_3 = \bar{Y}_{.2} - \bar{Y}_{.3} = -11.5$ ,  $s(\hat{D}_i) = 1.1172$ ,  
 $q(.9, 3, 18) = 3.10$ ,  $T = 2.191$ .

$$-6.45 \leq D_1 \leq -1.55, -17.95 \leq D_2 \leq -13.05, -13.95 \leq D_3 \leq -9.05$$

## 2 Problem 21.18

$$\hat{E} = 3.084$$

## 3 Problem 26.10

	Source	SS	df	MS
	States (A)	6976.84	2	3488.42
a)	Cities B(A)	167.6	6	27.933
	Error	3893.2	36	108.1441
	Total	11,037.64	44	

b)  $F^* = 32.257 > F(.95, 2, 36) = 3.26$ .

Conclude  $H_a$ : not all  $\alpha_i$  equal zero. ( $i=1, 2, 3$ ).

c)  $F^* = .258 < F(.95, 6, 36) = 2.36$ .

Conclude  $H_0$ : all  $\beta_{j(i)}$  equal zero.

d)  $\alpha \leq .1$

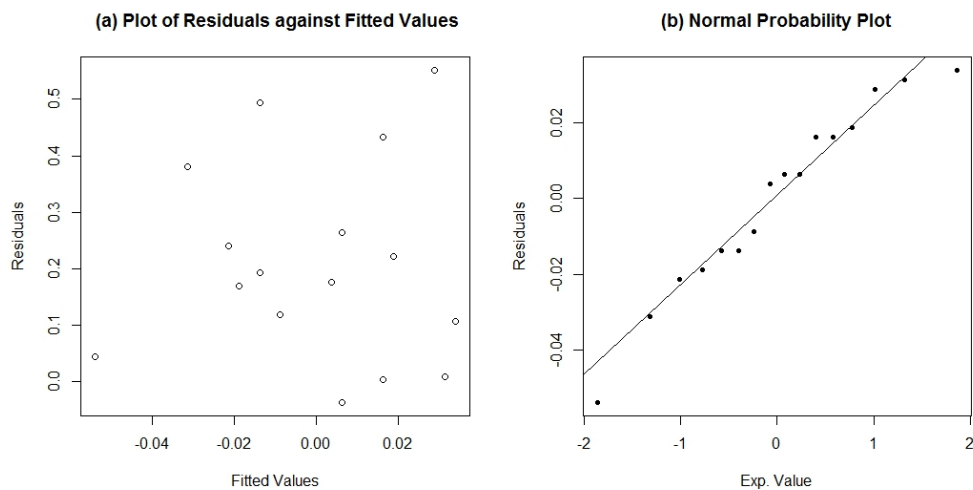
## 4 Problem 26.11

a)  $\bar{Y}_{11.} = 40.2$ ,  $s(\bar{Y}_{11.}) = .4651$ ,  $t(.975, 36) = 2.028$ ,

$$30.77 \leq \mu_{11} \leq 49.63$$

- b)  $\bar{Y}_{1..} = 40.8667$ ,  $\bar{Y}_{2..} = 57.3333$ ,  $\bar{Y}_{3..} = 26.8667$ ,  $s(\bar{Y}_i) = 2.6851$ ,  $t(.995, 36) = 2.7195$ ,  
 $33.565 \leq \mu_1 \leq 48.169$ ,  $50.031 \leq \mu_2 \leq 64.635$ ,  $19.565 \leq \mu_3 \leq 34.169$
- c)  $\hat{L}_1 = \bar{Y}_{1..} - \bar{Y}_{2..} = -16.4666$ ,  $\hat{L}_2 = \bar{Y}_{1..} - \bar{Y}_{3..} = 14.0$ ,  $\hat{L}_3 = \bar{Y}_{2..} - \bar{Y}_{3..} = 30.4666$ ,  $s(\hat{L}_i) = 3.7973$ ,  
 $q(.90, 3, 36) = 2.998$ ,  $T = 2.12$   
 $-24.52 \leq L_1 \leq -8.42$ ,  $5.95 \leq L_2 \leq 22.05$ ,  $22.42 \leq L_3 \leq 38.52$
- d)  $\hat{L} = 12.4$ ,  $s(\hat{L}) = 6.5771$ ,  $t(.975, 36) = 2.028$ ,  $-.94 \leq L \leq 25.74$

## 5 Problem 28.22



The correlation coefficient between the ordered residuals and their expected values under normality is 0.98. The residuals are random and normally distributed.

## 6 Problem 28.23

Source	df	SS	MS
Period	3	0.005 92	0.001 97
Subject	3	0.034 62	0.011 54
Treatment	3	0.4333	0.144 44
Drug X	1	0.228 01	0.228 01
Drug Y	1	0.195 81	0.195 81
XY Interactions	1	0.009 51	0.009 51
Residuals	6	0.009 04	0.001 51
Total	15	0.482 91	

a) The model to be used is:

$$Y_{ijkl} = \mu \dots + \rho_i + \kappa_j + \alpha_k + \beta_l + (\alpha\beta)_{kl} + \varepsilon_{ijkl}$$

b) Hypotheses:

$H_0$  : All  $(\alpha\beta)_{kl} = 0$  (There's no interaction between the two drugs)

$H_1$  : At least one  $(\alpha\beta)_{kl} \neq 0$  (There's interaction between the two drugs)

at 10% significance level

Test Statistics:

$$F^* = \frac{MSXY}{MSE} = \frac{0.00951}{0.00151} = 6.298$$

Decision: If  $F^* > F_{(0.9,1,6)} = 3.776$ , we reject  $H_0$ , otherwise we fail to reject  $H_0$ .

Conclusion: Since  $F^* = 6.298 > 3.776$ , we reject  $H_0$  and conclude that there is interaction effect between Drugs X and Y.

c)  $\bar{Y}_{..1} = 0.0050$ ,  $\bar{Y}_{..2} = 0.1950$ ,  $\bar{Y}_{..3} = 0.1775$ ,  $\bar{Y}_{..4} = 0.4650$ ,  $t_{(0.95,6)} = 1.943$ ,  $s\{\hat{L}\} = 0.0389$

$$\hat{L} = \bar{Y}_{..2} - \bar{Y}_{..1} - \bar{Y}_{..4} + \bar{Y}_{..3} = 0.1950 - 0.0050 - 0.4650 + 0.1775 = -0.0975$$

$$\hat{L} \pm t_{(0.95,6)} s\{\bar{Y}\} \quad \implies \quad -0.0975 \pm 1.943(0.0389) \quad \implies \quad -0.1731 \leq L \leq -0.0219$$