

1. 3 points This question is about vectorization, i.e. writing expressions in matrixvector form. The goal is to vectorize the update rule for multivariate linear regression.

(a) Let  $\theta$  be the parameter vector  $\theta = (\theta_0 \theta_1 \dots \theta_n)^T$  and let the  $i$ -th data vector be:  $x(i) = (x_0 x_1 \dots x_n)^T$  where  $x_0 = 1$ . What is the vectorial expression for the hypothesis function  $h_\theta(x)$ ?

$$g(z) = \frac{1}{1+e^{-z}}$$

$$h_\theta(x) = g(\theta^T x)$$

(b) What is the vectorized expression for the cost function:  $J(\theta)$  (still using the explicit summation over all training examples).

$$J\theta = \frac{1}{m} \sum_{i=1}^m ([y(i)\log(h_\theta(x(i))) + (1 - y(i))\log(1 - h_\theta(x(i)))])$$

(c) What is the vectorized expression for the gradient of the cost function?

$$J\theta = \frac{1}{m} \sum_{i=1}^m (h_\theta(x(i)) - y(i))x_{j(i)}$$

(d) What is the vectorized expression for the  $\theta$  update rule in the gradient descent procedure?

$$\theta_j := \theta_j - \frac{\alpha}{m} \sum_{i=1}^m (h_\theta(x(i)) - y(i))x_{j(i)}$$

2. 2 points Derive an equation that can be used to find the optimal value of the parameter  $\theta_1$  for univariate linear regression without doing gradient descent. This can be done by setting the value of the derivative equal to 0. You may assume that the value of  $\theta_0$  is fixed.

$$J\theta = \frac{1}{2m} \sum_{i=1}^m (h_\theta(x(i)) - y(i))^2$$

$$2m * J\theta = \sum_{i=1}^m (h_\theta(x(i)) - y(i))^2$$

*Derivation*

$$-2 \sum_{i=1}^m (h_\theta(x(i)) - y(i))$$

*Comparison to 0*

$$-2 \sum_{i=1}^m (h_\theta(x(i)) - y(i)) = 0$$

$$\sum_{i=1}^m (h_\theta(x(i)) - y(i)) = 0$$

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$$\sum_{i=1}^m(h_{\theta}(x(i)) - y(i)) = 0$$

$$h_{\theta}(x(i)) = y(i)$$