# [Draft] Arbeitstitel

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#### Abstract

We propose an extension of spatially extended spiking network models by allowing individual point-locations to emit chemicals and affect the properties of the network. We provide a network model example fulfilling rule 110 up to one error and sketch how this system attempts to correct this error without using backpropagation. The error consists of having a group of neuron A connected to group of neuron B such that a specific activity pattern in A causes activity in B and suppresses activity in a group C. The correction is achieved if the same pattern of activity in A causes activity in C and suppresses activity in B.

## 1 Chemical Spiking Neural Network (CSNN)

Definition 1 (Spatially extended Spiking Neural Network (SeSNN)) Let  $P \subset \mathbb{R}^d$ . A Spatially extended Spiking Neural Network (SeSNN)  $\mathcal{NN}$  within P is a Spiking Neural Network (SNN) with the following additional properties.

- 1. N Neurons ... (use some Spiking Neuron Model, for example: Izkevitch Model (2003)). The set of all neurons is called  $\mathcal{N} = \mathcal{N}(\mathcal{N}\mathcal{N}) = \{n_j : n_j \text{ is a neuron and } j \in \{0,...,N-1\}\}.$
- 2. All N neurons have, as an attribute, an  $\mathbb{R}^d$ -valued position within P.
- 3. Synapses have distance dependent existence probabilities and delays.

#### 1.1 Location Groups and chemical Concentrations

Let  $P = [0,1] \times [0,1] \times [0,1] \subset \mathbb{R}^3$  and  $\mathcal{N}\mathcal{N}$  be a SeSNN within P.

Partition P into  $G \in \mathbb{N}_{>0}$  into equally sized cells. Each cell and the contained neurons define a **location group**  $g_i$ ,  $i \in \{0, ..., G-1\}$ .

Define  $\mathcal{LG} = \mathcal{LG}(\mathcal{NN}) = \{g_j : g_j \text{ is a location group and } j \in \{0, ..., G-1\}\}$  as the **set of all location groups**.

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We say a neuron  $n \in \mathcal{N} = \mathcal{N}(\mathcal{N}\mathcal{N})$  belongs to  $g_i \in \mathcal{LG}$  if  $n_j$  is positioned within the cell corresponding to  $g_i$  and denote it by  $n \in g_i$ . #g corresponds to the number of neurons in  $g \in \mathcal{LG}$ 

The volume occupied by  $g \in \mathcal{LG}$  is denoted by Vol(g).

**Definition 2 (Self-Sustained Activity)** Let  $R, T_I, T_b \in \mathbb{R}_{>0}$ , and  $N \in \mathbb{N}_{>0}$ . We say a location group  $g \in \mathcal{LG}$  is in a state of  $((R, T_I, T_{b^-})$ self-sustained activity at time t if t belongs to a time interval of length  $T_I$  and there is a time interval of length  $T_b$  in which at least  $k \in \mathbb{N}$  neurons  $\frac{k}{\#g} \geq R$  would have been spiking without requiring external activation.

**Definition 3 (Cluster, R-Clusters)** A cluster is set of two or more location groups. Let C be a cluster. If the self-sustained activity of one or more location group belonging to C causes the self-sustained activity of all other groups in C, we say C is a R-Cluster. An R-Cluster of which at least one location with at least one location group is in a state of self-sustained activity is said to be activated.

**R-Cluster activation notation:** Let C be a cluster such that more than one cluster causes the self-sustained activity of the other groups. If  $\{c_0, c_1, ..., c_i\}$  are clusters of C causing self-sustained activity in  $\{c_{i+1}, ..., \}$  if their respective self-sustained activity time-intervals overlap (w.r.t.  $T_b$ ), we denote this statement by:

$$C: \{c_0, c_1, ..., c_i\} \Rightarrow \{c_{i+1}, ..., \}.$$

Feedback effect may be loosely indicated using  $\Longrightarrow$  w.r.t. their intensity or  $\Leftrightarrow$  if

$$C: \{c_{i+1}, ..., \} \Rightarrow \{c_0, c_1, ..., c_i\}$$

if also true. If the inactivity (self-sustained activity) of one more location groups is necessary for (excludes) the self-sustained activity of one more other groups (not necessarily belonging to C) we denote this statement by:

$$C: \{\overline{c_0}, c_1, ..., c_i\} \Rightarrow \{c_{i+1}, ...,\}.$$

$$C: \{c_0, c_1, ..., c_i\} \Rightarrow \{c_{i+1}, ..., \overline{x}\}.$$

if  $c_0$  or x are respectively the specifically non-activated group(s).

## 1.2 Fluid-Network (Bloodstream)

This Network is intended to approximate the circulation of blood within P. A Fluid network B is built similarly to a neural network (and graph) with delays, but with location groups (as nodes) instead of Neurons and vessels instead of synapses (as edges). Instead of transferring voltage spikes from neuron to neuron, the blood network transfers chemical concentration spikes.

B has an entry surface  $B_{in}$  and exit surface  $B_{out}$  at the border  $\partial P$  of P. Vessel diameters may be inter-dependent, i.e. a vessel contraction may lead to the expansion of some other vessels. [TODO: Volume In = Volume out]

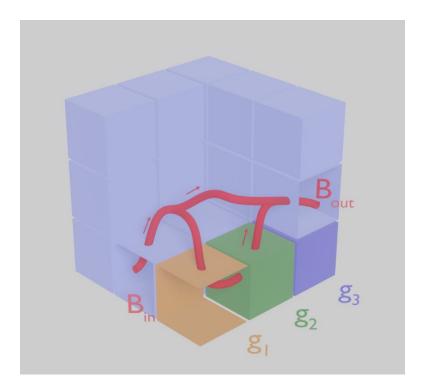


Figure 1: Fluid-Network Example (with 3x3x3 location groups) [TODO: Resize diameters]

**Definition 4 (Attributes)** Let X, Y and Z be sets such that  $X \subset Y$ . An (Y, Z)-valued-attribute (or Z-valued-attribute z) of X is an Z-valued map from Y to Z.

We assume that P can be separated in three non-overlapping subsets: Neurons (Points), denoted by  $P_N$ , Synapse(edges without endpoints), denoted by  $P_S$ , fluid-network vessels (if present), denoted by  $P_F$  and P minus the previous sets, denoted by  $P_R$ .

**Definition 5 (set of chemicals, chemical concentration, chemicals, )** Let C be a non-empty set of  $\mathbb{R}_{\geq 0}$ -valued attributes of P. C may be called a **set of chemicals** of P if for each attribute  $c \in C$  and for each of the following (non-overlapping) subsets of P,  $P_N$ ,  $P_S$ ,  $P_F$ , and  $P_R$ , there exists a time(-step) dependent 'diffusion' function  $f_c(p, c(p, t), t, ...)$ 

$$f: (\mathbb{R}^3, \mathbb{R}_{\geq 0}, \mathbb{R}_{\geq 0}, \ldots) \to \mathbb{R}_{\geq 0},$$

such that

$$c(p, t_{i+1}, ...) = f_c(p, c(p, t_i), t_i, ...)$$

and  $f_c$  fulfills one of the following properties

1. [some mathematical property: diffusion w.r.t a subset of P (including flow for blood vessels)],

2. ... .

If C is a set of chemicals in P, the elements of C are called **chemicals**. A value c(p,t) is called **chemical concentration** (of the chemical c in the point p at time t). The diffusion functions are denoted by  $d_{c,N}$ ,  $d_{c,S}$ ,  $d_{c,F}$  and  $d_{c,R}$  (w.r.t.  $P_N$ ,  $P_S$ ,  $P_F$ , and  $P_R$ ).

**Definition 6 (gas-emission, production (points, neurons))** If P has at least one chemical attribute c and  $p \in P$  can increase the concentration of c in it's neighborhood we say that p is a **gas-emitting point** and that p **produces** c. If  $p \in P_N$  we call the corresponding neuron a **gas-emitting neuron**.

**Definition 7 (gland, production (glands))** An R-Cluster whose activation directly causes the increase of chemical concentrations at particular points in the blood stream is called a **gland**. If a gland increases the chemical concentrations of (say) chemicals  $C_1$ ,  $C_2$  and  $C_3$  at a rate x, we speak of a  $C_1C_2C_3$ -gland and say that this glands **produces**  $C_1$ ,  $C_2$  and  $C_3$  at rate x.

**Definition 8 (chemically sensitive neurons)** Let x be a Neuron with a set of attributes  $A_x$  positioned in  $p \in P$ , and C is a set of chemicals in P. The subset of attributes of x that are chemical concentrations at point p is denoted by  $C_x \subset C$ . If a change in concentration of an element of  $C_x$  causes a change in another element of  $A_x$ , the neuron is called chemically sensitive.

**Definition 9 (Vessel-contraction and expansion)** Vessel diameters can be a function of one more location group diameters

#### 1.3 Definition

A Chemical Spiking Neural Network (CSNN) within  $P \subset \mathbb{R}^3$  is a SeSNN with the following properties.

- 1. One or more Neurons of the SeSNN are chemically sensitive.
- 2. One or more points in P are gas-emitting.

## 2 Example

#### 2.1 Rule 110

Consider the following tuples:

$$p_0 = (0,0,0),$$
  $p_1 = (0,0,1),$   $p_2 = (0,1,0),$   $p_3 = (0,1,1),$   $p_4 = (1,0,0),$   $p_5 = (1,0,1),$   $p_6 = (0,1,1),$   $p_7 = (1,1,1).$ 

Set  $P = \{p_0, p_1, ..., p_7\}$  and define the map  $r_{110}: P \to \{0, 1\}$  by:

$$r_{110}: p_0, p_4, p_7 \mapsto 0,$$
  
 $r_{110}: p_1, p_2, p_3, p_5, p_6 \mapsto 1.$ 



Figure 2: Rule 110 (highlighted:  $p_1 = (0,0,1)$ ). The first row corresponds to the inputs, the second one to the outputs (i.e  $r_{110}(p_1) = 1$ ). [Image source: Wikipedia]

**Definition 10 (Rule 110)** Let  $\mathcal{N}\mathcal{N}$  be a CSNN containing a sufficient number of R-Clusters such that  $\mathcal{I} = \{i_0, i_1, i_2, i_3\}$ ,  $\mathcal{O} = \{o_0, o_1\}$  and  $\mathcal{R} = \{r \in \mathcal{LG}(\mathcal{N}\mathcal{N}), r \notin \mathcal{I} \cup \mathcal{C} \cup \mathcal{O}\}$  are clusters of distinct location groups  $\subset \mathcal{LG} = \mathcal{LG}(\mathcal{N}\mathcal{N})$ .

We say that NN fulfills the rule 110 if the following statements are true:

$$\begin{split} A_0 &= \mathcal{I} \cup \mathcal{O} : \{\overline{i_0}, \overline{i_1}, \overline{i_2}, i_3\} \Rightarrow \{o_0, \overline{o_1}\}, \\ A_1 &= \mathcal{I} \cup \mathcal{O} : \{\overline{i_0}, \overline{i_1}, i_2, i_3\} \Rightarrow \{\overline{o_0}, o_1\}, \\ A_2 &= \mathcal{I} \cup \mathcal{O} : \{\overline{i_0}, i_1, \overline{i_2}, i_3\} \Rightarrow \{\overline{o_0}, o_1\}, \\ A_3 &= \mathcal{I} \cup \mathcal{O} : \{\overline{i_0}, i_1, i_2, i_3\} \Rightarrow \{\overline{o_0}, o_1\}, \\ A_4 &= \mathcal{I} \cup \mathcal{O} : \{\overline{i_0}, \overline{i_1}, \overline{i_2}, i_3\} \Rightarrow \{o_0, \overline{o_1}\}, \\ A_5 &= \mathcal{I} \cup \mathcal{O} : \{\overline{i_0}, i_1, \overline{i_2}, i_3\} \Rightarrow \{\overline{o_0}, o_1\}, \\ A_6 &= \mathcal{I} \cup \mathcal{O} : \{\overline{i_0}, \overline{i_1}, i_2, i_3\} \Rightarrow \{\overline{o_0}, o_1\}, \\ A_7 &= \mathcal{I} \cup \mathcal{O} : \{i_0, i_1, i_2, i_3\} \Rightarrow \{o_0, \overline{o_1}\}. \end{split}$$

### 2.2 Network

From now on let  $\mathcal{N}\mathcal{N}$  be a CSSN such that the parameters  $R, T_I$  and  $T_b$  defining self-sustained activity are constant and containing a sufficient number of R-clusters such that all statements of rule 110 except  $A_1$  are fulfilled. Instead the

following is true:

$$\overline{A_1} = \mathcal{I} \cup \mathcal{O} : \{\overline{i_0}, \overline{i_1}, i_2, i_3\} \Rightarrow \{o_0, \overline{o_1}\};$$

and the weights of  $\mathcal{N}\mathcal{N}$  can be modified such that A1 is true.

#### 2.2.1 Input-Clusters

Each input cluster contains one signal neuron that will emit spikes at different rates, depending if the cluster is active or not. All 8 frequencies are distinct.

#### 2.2.2 Chemicals and Glands

 $\{E,W,T,S,F,R,L_1,L_2,NL_1,NL_2,STL,ASTL\}$  is the set of chemical of  $\mathcal{NN}$  ( Acronyms from: Energy, Wake, Tired, Sleep, Fear, Reward, Learning, Neuron, Short-Term Activation, Anti Short-Term Activation).  $\mathcal{R} \subset \mathcal{LG}$  contains four glands:

- 1. fear-gland (F-gland)
- 2. reward-gland (R-gland, it can only be activated externally by a supervisor)
- 3. wake-gland (WT-gland)
- 4. sleep-gland (S-gland)
- 5. learn-gland  $(L_1L_2$ -gland)
- 6. short-term-chemical-activation-gland (STA-gland)
- 7. anti-short-term-chemical-activation-gland (ASTA-gland)

Each gland has two modes:

- 1. active (producing the corresponding chemicals at a (time-limited) fixed rate)
- 2. inactive

## 2.2.3 Frequency-Network

The input-clusters, output-clusters and the F-Gland are connected in such a way that the addition of all input-spike-signals and output signals are relayed to a specific neuron(s) of the F-Gland (receiver) and a frequency decoder: If the signal contains a frequency, a corresponding neurons 'activates'. A number of neurons of the F-Gland function as an emitter. The F-gland can recognize if the frequencies of the emitter match those of the receiver. Such a **signal-match** 

## 2.2.4 Network-States

Depending on the chemical concentrations in P, at any point in time, we attribute one of the following 'states' to  $\mathcal{N}\mathcal{N}$ 

- 1. wake-state; sub-states:
  - (a) interpreting-state (only the WT-gland is active),
  - (b) rewarded-state (only the WT-gland and R-gland are active),
  - (c) fear-state (only the WT-gland and F-gland are active),
- 2. asleep; sub-states:
  - (a) dream-state (only S-gland in active),
  - (b) fear-state (only the WT-gland and F-gland are active),
  - (c) learning-state (only the WT-gland and F-gland are active),

The only possible transitions are  $1.a \rightarrow 1.b, 1.a \rightarrow 1.b, 1.a \rightarrow 2.a$  (falling-asleep-state),  $1.b \rightarrow 1.a, 1.c \rightarrow 1.a, 2.a \rightarrow 1.a$ (waking-up-state),  $2.a \rightarrow 2.b, 2.a \rightarrow 2.c$ ,  $2.b \rightarrow 2.a$  and  $2.c \rightarrow 2.a$ . We also denote wake and sleep for a state

- 1. The S-gland will activate and the WT-gland will deactivate if T exceeds a threshold in a point  $p \in P$ .
- 2. In the *interpreting-state*, the R-gland will activate if triggered from outside. If the R-concentration exceeds a threshold in a point  $p \in P$ , the WT-gland stops producing T.
- 3. The chemical E is delivered via blood flow. The amount delivered depend on the vessel diameters. Some vessel diameters may shrink to a point where the local network activity is suppressed.
- 4. ... [TODO: chemical properties]

#### 2.2.5 Memory formation

[TODO: precise Definitions]

**L-T-S-Memory**: Activation pattern change caused by long-term changes in synaptic weights or new synapses

**S-T-S-Memory**: Activation pattern change caused by short-term changes in synaptic weights or new short-lived synapses

**S-T-C-Memory**: Activation pattern change caused by changes in chemical concentrations

... [TODO: ]

### 2.3 Correcting the Error

In the following we sketch the behavior of the Network:

#### 2.3.1 Wake State

We assume the the network is in the *interpreting-state*.

- 1. TODO: The network detects an Input ( $\Rightarrow I_3$  is activated) corresponding to  $\{\overline{i_0}, \overline{i_1}, i_2\}$ .
- 2. The activity pattern causes the blood vessels going through  $\mathcal{I}$  to contract and expand proportionally to the activity.
- 3. The activation of  $I_3$  causes the STL-gland to emit (say) only in  $\mathcal{I}$ . The vessel diameters are such that the concentration of STL exceeds a threshold in  $\{i_2, i_3\}$  and not in  $\{\overline{i_0}, \overline{i_1}\}$ .
- 4. TODO Due to the error the R-Gland is not activated which in turn cause the F-Gland to be activated.
- 5. The activation of the F-Gland causes the 'light' activation of the Input cluster. Because of the STA-concentrations, the Input cluster activity corresponds to the last input pattern.
- 6. (See Frequency-Network) Some synapses of the F-Gland grow or shrink randomly until the frequencies of the receiver match those of the current active R-clusters of  $\mathcal{I}$ . A 'match' causes the current F-Gland synapse configuration to freeze, the F-Gland to deactivate and the ASTA-gland to activate for limited time period (which cause the STA-concentrations to go to zero).

## 2.3.2 Wake State

7.

## References

- [1] IZKEVITCH /.../ 2003.
- [2] AUTHORS Shot-Term Memory 20xx.
- [3] .. Rule 110. ..

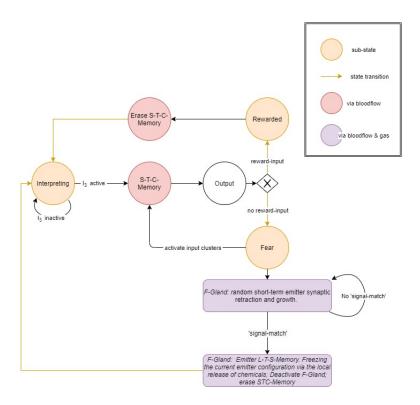


Figure 3: Wake.

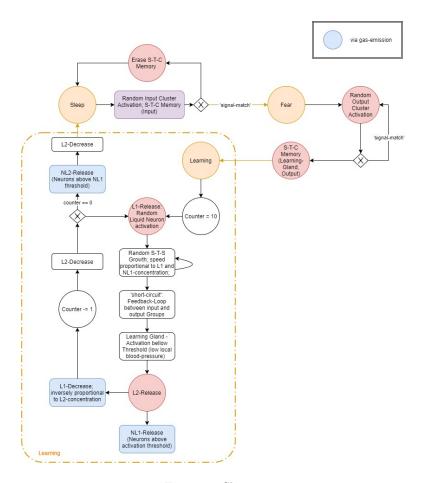


Figure 4: Sleep.

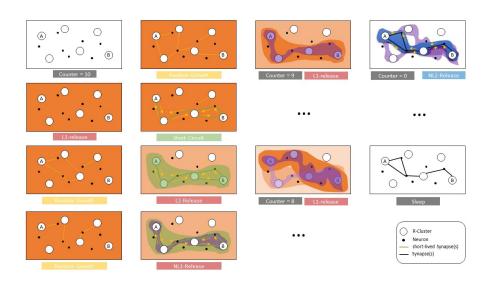


Figure 5: Learning (2D).