

# Proiect la Probabilitati si Statistica

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## Cuprins

PROBLEMA 1 .....	2
Variabile folosite.....	2
Repartitia binomiala .....	2
Repartitia Poisson.....	3
Repartitia exponentiala .....	4
Repartitia normala.....	8
Ilustrarea grafica a functiilor de masa/densitate.....	14
Functiile de repartitie pentru cele 5 seturi de parametrii diferiti .....	16
Aproximarea functiei de repartitie si de masa a binomialei .....	17
Eroarea maximala absoluta .....	20
PROBLEMA 2.....	23
Justificarea teoretica a simularii cuplului.....	23
Metoda acceptarii si respingerii .....	23
Simularea punctelor prin coordonate polare.....	24

# PROBLEMA 1

## Variabile folosite

```
N = 1000
n = 100 #n repartitie binomiala
p = 0.1 #p repartitie binomiala
lp = 2 #lambda repartitie poisson
le = .3 #lambda repartitie exponentiala
mean = 2 #medie repartitie normala
sd = sqrt(9) #9 = varianta repartitie normala
xd = seq(0, 10)
xc = seq(0, 5, by = 0.5)
```

Funcțiile mean() si var se folosesc pentru aflarea mediei, respectiv variantei.

## Repartitia binomiala

Generarea a N = 1000 variabile aleatoare cu ajutorul repartitiei binomiale:

```
binom = function(n, p) {
  b = c()
  b = rbinom(N, n, p)
  return(b)
}
binom(n, p)
```

```
##      [1] 13 12  9  8 13  4 11 11 11 11  5  7 11  9  9  7  7 13 12  4 13  9 11
##     [24]  7 10  9 13 10 12 11 12  9  8 13  5  8 12 10 10 10 10  6  6  8  9 11
##     [47]  8 12 10 18  6 12  8  7  7  9 11 12  8  5 15  4  9  9 19 11  8 10 11
##     [70] 12 13  7  9 12 11  9 14 10 14 13  8 15 14  5 10  7  9 11 12 12 10  7
##     [93] 10  8 13  6  6 10 12 13  3 14 10 11 11 11 13 12  9 10  7 12  9 14 12
##    [116]  8 15 13 19  5  9  8 12 14 12  8  8 11  7 12 12 13 18 15 10  9  8 16
##    [139] 13 10 11  7  8  8  4  7 11 10 11 18 12 11  8  6 13  5  8  8  8 11  7
##    [162]  6  7 11 12 12 10  9  7  9 14  9  9  9  7  7  8  9  6  9 13 10  4 15
##    [185]  7  8  8  7  6 15  8  8 14 15 11  9  8 11  9  8  8 13  6 13  5 13  9
##    [208] 14  8 12  6  6  8  2  9  5 12  5  6  9  8  6  5  6 13 14  7 11 13 11
##    [231] 15 10  7  9  5 13  8 10 13  4 10 10 11  9 11 11 13  8  4 11  9  7 14
##    [254] 10  8 11 16 13 10  8  8  8  7  6 14 11  8  9 13  6 11  6 13 12 12  8
##    [277] 15  7  6  7  7 15 16  5 14  6 11 10  7  9 11  8  4 12 12  5 10  9  6
##    [300] 10  4  8 13 14 11  8 10 11 10  6 10 17  9  6 11 12 13 13 10  9 11 11
##    [323] 10  8 14 13  7 10 15 12  8 12 12  6  8  3  7  4 13  9 13 12  9  9 15
##    [346] 10 12  6  7 11  5  9  8  9  9 12 14 12  9 10  4  9 11  7  9 12 13 11
##    [369] 11 12  7  9 12 11  9 10 14  6 11  7 16  7 16  8  9  8  3 13 13  5  9
##    [392]  5  9 13  8  6 14 13 15  7 11  8  9  5  7  8  8 13  8  7 18  5 10 10
##    [415] 11  9 11 15  9 10 10 12  7  8  8  8 24 11  6 14 12 12  9  5 16 11 12
##    [438] 13 12  8 17 13 14 14  8 10 12 13  8 11  9  6 13  5 10  6  5 13 10 10
##    [461]  9 10 10 15 11 13  9  5 12 12 10 11  9  9  9  7 13  9  7 16  7 10  6
##    [484] 13 14  7  7  7 12  7  6 15 11  5 10  7 10 11 11 12 16  9  6  9 10  9
##    [507]  9 10  8 16  9 10 10 12 13 11  6 10  9  8 14 10  9  9  5  8  9  9  8
##    [530]  7 14 11  9  7  6 13  8 10 10 11 12 11 13  8 12  9  9 11 18 10 10 12
##    [553] 10 16  9  3 13 11  9  9 10  8 11 12 12 11 10 10  5  8 13  1 10 10  8
```

## Proiect la Probabilitati si Statistica

```
## [576] 11 8 11 15 18 16 7 11 12 7 8 8 10 13 16 9 9 9 9 10 10 8 7
## [599] 15 8 7 12 19 10 5 5 11 10 10 19 10 9 5 13 7 10 5 8 10 11 13
## [622] 11 11 15 11 6 7 9 7 14 12 13 16 13 12 7 8 10 18 7 10 8 7 13
## [645] 9 12 8 9 12 11 11 9 15 15 7 8 8 11 9 6 9 12 13 5 10 3 5
## [668] 4 8 11 9 11 5 15 9 6 8 10 13 8 14 9 12 14 9 3 12 8 10 9
## [691] 9 5 7 7 10 9 10 13 7 11 9 14 14 14 7 11 6 11 12 8 18 7 15
## [714] 15 20 8 9 10 12 13 5 10 9 8 11 7 11 10 15 5 7 10 6 11 10 7
## [737] 8 12 11 12 11 6 10 10 11 12 13 10 4 12 10 7 11 13 11 5 10 9 12
## [760] 7 14 5 5 13 7 9 7 6 13 7 12 8 7 9 13 13 9 9 8 10 14 8
## [783] 4 17 7 12 16 10 4 14 8 8 11 12 8 12 13 10 12 9 9 14 4 7 11
## [806] 17 10 11 8 8 8 9 10 11 8 8 14 10 9 12 10 8 13 13 13 10 10 14
## [829] 8 14 10 9 18 12 13 6 10 15 9 8 11 22 10 10 6 5 10 6 8 10 8
## [852] 8 8 10 8 16 11 12 14 14 8 8 9 14 8 8 9 9 6 16 14 10 7 10
## [875] 7 8 12 17 13 9 12 9 6 4 9 6 9 10 10 8 7 11 8 12 12 8 11
## [898] 8 13 12 7 10 10 8 6 10 7 13 8 5 12 11 10 13 13 11 5 7 8 10
## [921] 9 12 9 7 9 12 12 11 12 9 10 6 10 12 13 14 13 8 11 11 11 6 6
## [944] 11 6 13 4 9 11 6 10 11 11 12 12 8 9 10 10 8 14 11 13 10 12 10
## [967] 8 9 10 9 9 7 10 8 13 7 13 14 9 11 4 13 9 8 15 15 10 7 9
## [990] 10 13 9 10 9 7 12 4 6 14 11
```

```
cat("[Repartitie binomiala] Media este: ", mean(binom(n, p)), "\n")
```

```
## [Repartitie binomiala] Media este: 9.93
```

```
cat("[Repartitie binomiala] Varianta este: ", var(binom(n, p)), "\n")
```

```
## [Repartitie binomiala] Varianta este: 8.605076
```

## Repartitia Poisson

Generarea a N = 1000 variabile aleatoare cu ajutorul repartitiei Poisson:

```
pois = function(l) {
```

```
  p = c()
```

```
  p = rpois(N, l)
```

```
  return(p)
```

```
}
```

```
pois(lp)
```

```
## [1] 4 1 2 1 0 4 2 0 1 0 5 0 2 4 2 0 2 5 6 0 0 2 4 3 0 0 3 3 5 1 1 4 0 0
## [35] 3 0 1 4 0 1 0 0 1 2 0 4 1 3 2 0 4 1 1 1 5 2 1 2 2 3 1 1 4 5 0 1 3 2
## [69] 1 1 1 2 0 2 2 4 2 3 3 2 1 3 0 0 1 4 0 4 2 1 4 1 1 3 1 2 4 1 1 3 1 2
## [103] 1 1 2 3 3 3 3 4 3 2 3 1 0 3 2 4 1 1 0 1 4 2 1 1 2 3 1 2 2 2 1 2 1 3
## [137] 0 1 1 1 1 1 2 3 2 5 1 3 4 3 1 2 4 2 2 3 1 3 1 2 2 5 1 1 2 3 2 2 0 4
## [171] 0 4 4 1 1 2 3 0 0 2 3 1 2 3 0 3 1 2 2 2 1 2 3 2 1 3 2 2 1 2 1 2 1 2
## [205] 1 1 4 3 1 4 2 2 0 3 1 3 4 2 4 5 0 3 2 3 1 2 2 0 2 1 0 1 3 0 1 3 1 3
## [239] 0 1 4 2 5 2 3 3 1 1 7 1 1 1 3 3 1 1 0 2 3 3 3 0 3 2 1 1 4 1 2 0 0 1
## [273] 0 1 1 4 1 0 4 1 0 1 8 4 3 2 3 0 4 2 1 2 4 4 1 3 3 0 4 2 5 0 1 2 3 2
## [307] 2 1 2 3 2 4 4 1 2 3 1 3 3 4 2 1 3 1 1 5 4 1 1 3 3 2 0 0 1 2 0 4 1 3
## [341] 1 3 2 1 0 2 4 3 2 1 1 0 0 5 1 0 3 2 3 0 3 2 4 2 1 2 1 2 2 2 1 2 2 2
## [375] 1 1 3 1 1 1 0 3 0 5 0 3 5 1 2 9 1 1 2 0 2 4 0 4 1 0 1 3 3 2 5 1 2 7
## [409] 2 2 3 3 1 1 3 6 0 3 5 5 2 2 4 0 0 3 5 0 2 2 0 4 3 2 3 1 1 0 4 4 2 3
```

## Proiect la Probabilitati si Statistica

```
## [443] 2 5 1 0 3 1 3 2 4 5 0 3 2 1 2 3 2 1 2 3 4 1 2 1 1 1 3 1 2 4 1 3 2 3
## [477] 1 5 1 4 0 1 0 2 5 0 1 3 2 1 1 2 2 2 1 1 3 1 1 1 2 2 1 2 3 3 3 4 1 1
## [511] 2 2 2 1 3 3 0 5 3 4 2 2 1 1 2 0 1 0 0 1 2 1 3 1 3 3 3 0 4 4 3 1 2 0
## [545] 0 5 4 3 1 0 3 2 1 4 2 3 2 3 2 1 1 2 5 2 1 2 0 4 0 3 1 0 4 2 0 1 3 2
## [579] 1 1 1 2 5 2 2 0 3 2 2 1 3 2 2 1 2 3 3 4 3 1 0 0 3 0 1 1 2 5 4 0 3 0
## [613] 2 1 2 2 3 3 2 1 1 2 3 1 1 0 3 4 0 3 1 1 0 3 1 1 2 3 0 0 2 1 4 4 1 2
## [647] 3 2 1 1 4 2 2 2 3 1 4 2 1 2 2 1 0 1 0 2 2 3 2 2 2 1 0 4 2 2 3 2 1 2
## [681] 3 3 1 3 1 0 3 2 0 0 1 1 1 3 1 2 1 2 1 5 5 1 2 2 1 3 2 2 3 4 1 0 1 3
## [715] 1 0 0 3 1 1 5 3 1 2 2 1 4 3 2 0 0 1 2 2 0 3 2 0 3 3 1 0 1 2 1 1 1 5
## [749] 4 0 1 1 2 2 4 1 2 0 5 0 3 3 3 3 0 0 1 4 2 2 3 4 1 3 1 3 3 2 2 3 4 0
## [783] 2 1 4 1 1 3 1 2 0 4 3 4 1 2 2 1 0 3 2 2 0 1 1 3 1 1 3 4 3 1 0 2 2 2
## [817] 1 1 2 0 1 3 1 2 2 2 0 3 1 3 2 3 0 2 1 2 0 3 1 3 3 2 5 3 3 7 3 1 3 2
## [851] 2 0 2 2 1 3 1 0 0 3 2 3 2 0 1 2 1 1 0 0 2 4 1 2 2 2 0 5 2 4 0 2 2 1
## [885] 5 1 0 1 1 2 3 2 3 1 0 1 1 3 0 1 2 2 3 1 3 2 2 0 2 0 2 2 6 1 0 1 1 3
## [919] 3 1 3 0 6 2 1 3 2 1 2 4 3 3 1 1 0 0 4 0 3 4 4 2 1 0 5 1 2 1 2 0 2 3
## [953] 2 2 2 0 3 4 2 1 5 2 1 2 1 0 2 2 1 1 3 4 2 0 1 1 0 2 2 2 3 1 0 1 2 3
## [987] 4 1 1 1 4 0 2 1 6 2 0 1 1 1
```

```
cat("[Repartitie Poisson] Media este: ", mean(pois(lp)), "\n")
```

```
## [Repartitie Poisson] Media este: 1.915
```

```
cat("[Repartitie Poisson] Varianta este: ", var(pois(lp)), "\n")
```

```
## [Repartitie Poisson] Varianta este: 2.07071
```

## Repartitia exponentiala

Generarea a N = 1000 variabile aleatoare cu ajutorul repartitiei exponentiale:

```
exp = function(l) {
```

```
  e = c()
```

```
  e = rexp(N, l)
```

```
  return(e)
```

```
}
```

```
exp(1e)
```

```
## [1] 9.660303e-01 1.746029e+01 3.800894e+00 5.365652e+00 1.127096e+00
## [6] 5.057977e-01 8.746224e-01 1.328652e+01 2.093809e+00 1.259510e+01
## [11] 2.395577e+00 1.221931e+00 4.487019e+00 8.010773e+00 3.467608e+00
## [16] 5.396251e+00 8.735990e+00 3.554827e+00 5.342406e+00 8.024832e+00
## [21] 1.420007e+00 1.950695e+00 4.205940e+00 1.206512e-01 5.209328e-01
## [26] 2.728045e+00 9.731946e+00 1.120842e+00 3.261637e+00 6.488869e+00
## [31] 4.881213e+00 4.982378e+00 7.105366e+00 4.257556e+00 9.787978e-01
## [36] 4.036137e-01 3.402950e+00 7.388468e-01 1.027786e+00 2.272163e+00
## [41] 2.522231e+00 3.937246e+00 3.719879e+00 1.523405e+00 4.983424e-01
## [46] 5.896474e+00 4.628010e+00 2.147987e+00 3.899766e-01 4.296912e-01
## [51] 3.965271e+00 4.979442e+00 8.219180e-01 5.141716e-01 2.172980e+00
## [56] 1.701479e+00 3.027306e-02 6.647124e-01 1.035234e+01 1.175702e+00
## [61] 5.176764e-02 3.621526e+00 1.474607e-01 3.173036e-01 1.355647e+01
## [66] 5.708633e+00 3.040951e+00 4.123618e+00 2.074986e+00 1.993145e-01
## [71] 2.500315e-01 5.431050e+00 1.032219e+00 5.287877e+00 1.314307e+00
```

# Proiect la Probabilitati si Statistica

```
## [76] 6.932668e+00 2.888006e-01 1.325276e+00 1.674995e+00 1.201895e+00
## [81] 1.324081e+00 5.691163e-01 2.910435e+00 2.591996e+00 1.546721e+00
## [86] 4.033745e-01 3.581048e-01 2.108114e+00 8.559350e+00 5.138077e+00
## [91] 6.661491e+00 5.650547e-01 3.142737e+00 2.560872e+00 1.646064e+00
## [96] 3.535919e-01 3.329757e+00 1.682506e+00 6.869104e+00 3.498088e-01
## [101] 5.099689e+00 4.572197e+00 1.225803e+01 1.875703e+00 3.273673e+00
## [106] 1.063563e+01 4.191177e+00 7.507660e-01 1.549343e-01 8.329574e+00
## [111] 3.054462e+00 1.000618e+00 6.081560e-01 3.284527e+00 6.044891e-01
## [116] 4.233800e+00 7.394689e-01 1.150627e+00 1.231021e+00 3.208838e+00
## [121] 9.563156e+00 3.235495e+00 2.724245e+00 7.114719e-01 5.400376e+00
## [126] 6.125250e+00 2.431897e+00 6.293040e-01 1.737334e-01 1.038028e+01
## [131] 6.834865e+00 6.256753e+00 2.938409e-01 4.990792e+00 8.024595e+00
## [136] 9.600903e-01 1.087562e+00 1.226026e+00 1.570514e-01 6.719280e+00
## [141] 9.431604e+00 6.267107e+00 2.229434e+00 2.998938e+00 2.019419e+00
## [146] 8.731476e+00 1.768919e-01 9.188442e+00 7.600186e+00 9.792467e-01
## [151] 4.762630e+00 3.698346e+00 3.000306e+00 8.394700e-01 1.608128e+00
## [156] 9.183280e-01 8.979764e+00 9.334583e-02 1.198379e+00 6.167570e+00
## [161] 2.659106e+00 6.203430e+00 2.597094e-01 8.715300e+00 1.497837e+01
## [166] 1.928871e+00 2.665233e+00 2.554213e-01 1.094535e+01 2.120304e+00
## [171] 1.092883e+01 2.533213e+00 8.403858e-01 7.972472e-01 1.056072e+00
## [176] 1.486138e+00 5.544278e-01 4.295320e+00 3.073674e+00 1.182854e+00
## [181] 3.859546e-01 5.623039e-01 2.551769e+00 2.286963e+00 1.814965e+00
## [186] 4.295245e+00 1.890816e+00 1.269699e+00 4.756869e+00 1.450138e+00
## [191] 4.476127e+00 4.498241e-01 1.305856e+00 2.304616e+00 3.086435e+00
## [196] 8.368481e-01 3.794023e+00 4.836874e-01 4.369017e+00 3.917318e+00
## [201] 1.022859e+00 1.165046e+00 8.578153e+00 3.510353e+00 4.298162e-01
## [206] 2.021838e+01 5.953929e-01 5.875995e+00 2.270114e+00 1.159124e-01
## [211] 4.834435e-01 3.014155e+00 2.161424e+00 4.408055e+00 2.812294e-01
## [216] 4.071064e+00 4.128408e+00 6.259540e-01 2.065955e+00 5.445871e-01
## [221] 1.597325e+00 4.930486e+00 3.274832e+00 2.730862e+00 7.934398e-01
## [226] 6.759823e-01 6.689765e+00 7.066533e+00 3.249634e-01 2.609180e+00
## [231] 2.380859e+00 2.931618e+00 7.161604e-01 5.682205e+00 1.193583e+00
## [236] 2.381996e+00 3.035466e+00 1.464868e+00 4.922346e+00 2.413197e+00
## [241] 2.100452e+00 1.989335e+00 1.564326e+00 3.146318e-01 1.189198e+01
## [246] 6.649202e+00 1.974776e+00 9.603428e-01 1.921610e+00 5.318710e+00
## [251] 7.290680e+00 7.007590e+00 5.116777e+00 2.787985e+00 9.962106e-01
## [256] 1.257892e+01 6.690690e-01 7.559895e+00 3.602362e+00 3.708345e+00
## [261] 1.840876e+00 1.161045e+00 8.143727e+00 1.574495e-01 7.154399e-01
## [266] 2.211166e+00 2.600913e+00 2.881612e+00 2.423960e+00 5.991948e+00
## [271] 7.476815e-01 6.032015e-01 4.065232e-01 3.861379e+00 2.016656e+00
## [276] 2.048398e-01 3.173891e-01 1.283115e+00 4.856831e-01 1.456633e+01
## [281] 7.672095e-02 1.892753e+00 1.693759e+00 8.053557e-01 2.478525e+00
## [286] 1.589005e+00 3.450344e-03 1.104513e+01 6.510979e+00 1.566534e+00
## [291] 1.205646e+00 1.781136e+00 3.937163e+00 9.583120e-01 1.485703e-01
## [296] 2.632628e+00 3.534919e+00 1.568157e+00 8.344746e-01 1.013682e+00
## [301] 9.474193e-01 4.274046e-01 1.243140e+01 1.459138e+01 3.565356e-01
## [306] 1.513063e-01 1.549405e+00 1.713912e+00 4.145015e-01 3.919630e-01
## [311] 1.602478e+00 6.051172e-01 3.463896e+00 5.608689e+00 2.623825e-01
## [316] 4.346010e-01 1.599255e+00 2.712647e+00 4.335899e+00 2.912413e+00
## [321] 2.318943e+00 1.787231e+00 1.508400e+00 6.249918e+00 1.135783e+00
## [326] 7.994452e+00 1.113924e+00 6.915805e+00 3.091870e+00 2.887776e+00
## [331] 9.669306e+00 6.817961e+00 3.449688e+00 1.868133e-01 2.895122e+00
```

## Proiect la Probabilitati si Statistica

```
## [336] 2.556605e+00 4.256098e+00 1.421904e+00 5.881798e-01 2.744788e+00
## [341] 3.618540e+00 9.070296e-01 1.030374e+00 5.532174e+00 1.069381e-01
## [346] 1.458609e+01 2.402015e+00 3.232314e+00 1.661947e+00 2.455218e+00
## [351] 3.630500e+00 1.930935e+00 7.572757e-01 4.159816e-01 2.802640e+00
## [356] 4.975078e+00 2.034266e+00 4.723938e+00 5.174315e+00 1.137478e+01
## [361] 5.157114e+00 5.364490e+00 1.383327e+00 4.627672e+00 4.226412e-01
## [366] 4.553609e-04 4.571724e+00 1.421222e+00 2.645548e+00 7.249013e+00
## [371] 1.954367e+00 1.725234e+00 1.141770e+00 1.161729e+00 9.396664e+00
## [376] 3.266789e+00 1.395225e+00 1.552524e+00 9.354640e+00 1.617971e+00
## [381] 5.223300e-01 6.782330e+00 1.889127e+00 3.485878e+00 5.060337e+00
## [386] 1.636785e+00 1.490905e+00 3.794500e+00 4.229200e-01 5.224861e+00
## [391] 6.244749e+00 3.773279e+00 5.478140e+00 3.362466e+00 4.812068e+00
## [396] 5.682161e+00 1.998827e+00 9.323981e-02 3.675305e-02 3.619521e-01
## [401] 2.466098e-01 9.061184e-01 7.391211e+00 6.979710e-01 1.724653e-01
## [406] 1.984348e+00 6.589411e+00 6.131510e+00 1.613207e+01 1.305206e+01
## [411] 3.978395e+00 1.076325e+01 6.079041e-02 2.316537e+00 6.509043e+00
## [416] 3.888255e+00 1.224992e+01 2.688997e+00 4.018318e+00 1.436536e+00
## [421] 7.635028e+00 2.500523e+00 4.410702e+00 2.429937e+00 1.418099e+00
## [426] 1.269437e+00 3.061159e+00 5.215976e-01 9.349657e+00 1.418810e+00
## [431] 2.809495e+00 2.327076e+00 1.451622e+00 2.892307e+00 8.559671e+00
## [436] 6.638986e-01 1.702792e+00 1.777896e+00 5.797377e+00 5.332941e-01
## [441] 2.779908e+00 7.740118e+00 6.088890e-02 1.966200e+00 9.305140e+00
## [446] 2.194545e-01 1.572652e+01 2.184104e+00 2.248047e-01 3.323251e+00
## [451] 1.533837e+01 1.765716e+00 7.337239e+00 1.491089e+00 1.336738e+00
## [456] 2.673855e+00 3.037539e-01 1.023323e+00 3.685201e+00 5.838434e+00
## [461] 2.229427e+00 4.741326e+00 3.310703e+00 1.476067e+00 1.365744e+00
## [466] 1.870280e+00 1.059774e+01 2.968239e-01 2.587433e+00 9.245976e+00
## [471] 1.833290e+00 1.182027e+00 2.560240e+00 2.115948e+00 2.078493e+00
## [476] 1.532142e+01 6.752007e+00 2.251409e+00 6.484084e+00 8.634595e-01
## [481] 1.055897e+01 1.244484e+00 8.140923e-02 3.327690e+00 1.321349e-03
## [486] 3.479348e+00 1.790826e+00 8.357722e+00 4.603901e+00 2.474862e-01
## [491] 4.531090e-01 1.721563e+00 8.813797e-01 4.504761e+00 1.498189e+00
## [496] 3.611550e+00 5.946176e-01 3.257615e+00 5.614116e+00 9.331288e-01
## [501] 7.282002e+00 2.257011e+00 1.949893e+00 4.370181e-03 8.001741e-01
## [506] 4.251765e-01 9.021941e-01 6.310337e-01 1.923221e+00 3.493922e+00
## [511] 4.244539e+00 2.317367e+00 1.166734e+00 2.524021e+00 9.000771e+00
## [516] 1.060823e-01 2.153459e+00 2.710168e+00 7.868838e-01 6.518168e+00
## [521] 9.560728e-01 2.277264e+00 6.513610e-01 6.091682e+00 2.049739e+00
## [526] 1.612794e+00 4.536883e+00 5.533839e+00 6.557997e-04 1.782375e+00
## [531] 2.295804e+00 2.077568e+00 7.039189e-01 1.787362e+00 7.243561e-01
## [536] 3.835630e+00 1.043623e+01 1.525775e-01 5.920242e+00 8.311663e-01
## [541] 9.371899e-01 1.684211e+00 3.431269e+00 9.112936e-01 1.400034e+01
## [546] 3.618119e+00 2.603549e+00 6.037858e+00 7.671030e-01 2.003998e+00
## [551] 2.218257e+00 1.353583e+00 3.516159e+00 4.286331e+00 2.222824e+00
## [556] 2.005567e+00 3.940093e+00 2.793943e+01 1.209054e+01 4.250021e-01
## [561] 7.285987e+00 7.112242e+00 6.978508e-01 9.529442e-01 1.421922e-01
## [566] 1.390371e+00 2.125562e+01 2.434584e+00 5.143194e-01 3.308160e+00
## [571] 3.900800e+00 7.304954e-01 3.624188e+00 1.222023e-01 3.909384e-01
## [576] 2.031464e-02 1.077043e+00 6.571816e-01 4.046993e+00 2.287206e+00
## [581] 1.708761e+00 2.972890e+00 6.434084e-01 9.991817e-01 6.583387e+00
## [586] 1.026721e+00 3.172057e+00 1.909479e+00 1.464328e-01 2.615223e-01
## [591] 4.894220e+00 3.885896e+00 5.023923e+00 4.862542e+00 1.455937e+00
```

# Proiect la Probabilitati si Statistica

```
## [596] 1.446162e+00 2.528981e-01 1.527361e+00 4.788278e+00 9.004414e-01
## [601] 3.673263e+00 2.312585e+00 3.193291e-01 3.606482e+00 6.808198e-01
## [606] 7.149987e-01 3.166680e+00 1.593701e+00 7.152905e-01 6.321395e+00
## [611] 2.839781e+00 3.069540e+00 5.216266e+00 2.127445e+00 4.239423e+00
## [616] 6.366306e-01 5.241336e+00 9.170752e+00 2.363141e+00 4.685646e-01
## [621] 3.525184e+00 5.973808e+00 4.967515e+00 4.373132e+00 2.574761e+00
## [626] 2.610616e-01 6.747050e+00 4.251067e-01 4.397368e+00 2.690857e+00
## [631] 1.165713e+00 1.940520e+00 5.000537e+00 1.137054e+00 2.356418e-01
## [636] 6.572567e-01 3.543758e-01 6.716209e-01 4.741752e-01 2.113146e+00
## [641] 2.048200e+00 2.879738e+00 4.388232e+00 8.700801e+00 3.437762e+00
## [646] 2.238617e+00 2.732773e+00 3.196578e+00 3.374192e+00 2.957147e+00
## [651] 5.937302e+00 4.883364e+00 3.211709e+00 9.605858e-02 4.259098e+00
## [656] 1.733260e+00 3.444324e-01 4.627722e+00 5.176432e+00 5.396751e-01
## [661] 9.591567e-01 2.307275e+00 5.961041e+00 8.029941e+00 2.038144e+00
## [666] 1.150532e+01 7.380399e+00 6.633629e+00 2.032972e-01 4.134348e+00
## [671] 2.574211e+00 1.079683e+00 5.288433e+00 2.888189e+00 2.432918e+00
## [676] 4.113811e+00 1.689377e+00 7.701907e-01 3.285397e+00 4.732422e+00
## [681] 9.029168e+00 4.392372e+00 1.391988e-01 9.458405e+00 6.489002e+00
## [686] 1.423698e+00 2.068559e+00 8.598095e+00 2.506591e+00 5.283282e+00
## [691] 9.661001e+00 5.837081e+00 2.632688e+00 3.955207e+00 5.921678e+00
## [696] 2.638333e+00 2.552546e+00 2.699622e+00 5.959607e+00 9.385910e+00
## [701] 2.423110e+00 1.531811e+00 5.729027e+00 8.498637e-01 9.200224e-01
## [706] 7.703536e-01 1.081239e+00 6.941567e-01 6.370547e+00 7.798085e-01
## [711] 2.306122e+00 2.378597e+00 1.160407e+00 1.359950e+00 1.107572e+00
## [716] 3.266528e+00 2.117906e+00 1.933057e+00 1.461991e+00 1.359619e+00
## [721] 7.378000e+00 1.931267e+00 3.845569e-01 2.007000e+01 7.412784e+00
## [726] 1.015219e+01 1.834672e+00 5.646242e-01 1.271816e+00 2.075973e+00
## [731] 3.425830e+00 5.268088e+00 1.680277e+00 2.134293e+00 9.789692e-02
## [736] 9.454872e+00 7.783409e-02 2.735280e+00 5.950785e+00 2.871122e+00
## [741] 4.124925e+00 1.268115e-01 1.586575e+00 1.278259e+00 3.906113e+00
## [746] 2.653109e+00 3.713266e+00 3.094757e+00 8.488276e+00 5.082534e+00
## [751] 1.029421e+00 6.159900e-01 1.063410e+01 1.171016e+00 3.857087e+00
## [756] 1.303137e+00 4.943976e+00 8.629160e+00 5.871288e+00 4.679120e+00
## [761] 2.628374e+00 1.141454e+00 5.879674e+00 5.812180e-01 4.825973e-01
## [766] 1.064245e+00 2.552287e+00 6.572967e-01 2.029018e+00 4.730334e+00
## [771] 3.217053e+00 2.442847e+00 3.345985e+00 4.963505e+00 1.698692e-01
## [776] 5.814369e-01 5.241077e+00 1.825757e+00 5.643375e+00 2.451183e+00
## [781] 1.250317e+01 7.767070e+00 1.087317e+00 4.847911e+00 4.566494e+00
## [786] 4.809560e+00 2.857347e-01 1.349453e+00 1.757421e+00 8.616358e-01
## [791] 2.145290e+00 9.117517e+00 6.515154e-02 1.831738e+00 7.755369e+00
## [796] 5.734304e-01 9.363871e+00 5.161959e-01 7.654493e+00 2.065074e+00
## [801] 1.861293e+00 3.281173e+00 7.141627e-01 2.326546e+00 1.450438e+01
## [806] 2.661574e-01 3.425411e+00 5.518054e+00 6.783765e+00 1.035763e+00
## [811] 5.432831e+00 8.842499e-02 7.485722e+00 2.979705e+00 7.290209e+00
## [816] 4.755092e-01 5.549390e-01 3.883475e-01 6.486762e+00 2.131764e+00
## [821] 2.732632e+00 3.901344e+00 3.903198e+00 7.125697e+00 2.676668e+00
## [826] 2.398156e-01 5.136376e+00 9.768035e-01 6.892214e+00 1.997354e+00
## [831] 5.271415e+00 2.843215e-01 4.026395e+00 2.227608e+00 6.713109e-02
## [836] 2.025444e-01 4.005324e-01 2.391352e+00 3.254843e+00 8.131655e+00
## [841] 6.122827e-01 4.776097e-01 6.000383e+00 1.385205e+00 2.359530e+00
## [846] 7.434415e+00 1.586948e+00 5.246656e+00 1.102264e+00 5.923198e+00
## [851] 2.653786e+00 1.728473e+00 9.139787e+00 1.104535e+00 5.111752e+00
```

## Proiect la Probabilitati si Statistica

```
## [856] 4.623395e-01 2.682934e+00 6.252115e-01 1.713714e+01 3.069696e+00
## [861] 4.248117e+00 1.281669e+00 8.282273e+00 5.707912e+00 5.826510e+00
## [866] 2.319068e+00 9.393473e-01 1.819284e-01 3.009061e+00 8.737457e-01
## [871] 5.832633e+00 1.761631e+00 1.845627e+00 2.097609e+00 9.943076e+00
## [876] 5.692115e-01 6.245717e+00 4.247781e-01 1.475900e-01 1.031526e+00
## [881] 5.658874e+00 1.303200e+00 1.169657e+01 1.395633e+00 5.666872e+00
## [886] 2.462561e+00 4.291382e-01 5.778738e-01 2.711686e+00 1.736331e+00
## [891] 3.106202e+00 2.614753e+00 7.552634e-01 1.407892e+01 3.929302e+00
## [896] 1.329213e+00 7.413743e+00 5.219503e+00 8.159461e-01 5.246396e+00
## [901] 1.705719e+00 2.064154e+00 2.186595e-01 8.125354e+00 2.777894e+00
## [906] 5.748132e+00 9.844658e-01 5.793679e-01 3.728745e+00 3.928065e+00
## [911] 2.354695e+00 3.149101e+00 3.095081e-01 4.272491e+00 4.615789e-01
## [916] 2.266763e-01 1.905071e+00 2.332234e+00 1.690778e+00 4.823453e+00
## [921] 1.311943e+01 2.497235e+00 3.614819e+00 3.898245e-01 1.538486e+00
## [926] 1.891353e+01 1.006686e-01 1.663735e+00 2.363703e+00 4.907170e-01
## [931] 4.982722e-01 6.492361e-01 2.296957e-01 2.223949e-01 2.866338e+00
## [936] 6.803604e+00 4.608733e+00 4.581012e+00 2.708128e-01 3.638680e+00
## [941] 1.832885e-01 4.121140e+00 2.253815e+00 3.258816e-02 1.112030e+00
## [946] 1.450142e+00 2.011312e+00 9.312514e-02 7.616901e+00 1.024023e+01
## [951] 7.561667e+00 1.251447e+00 3.871633e+00 9.037305e+00 1.008411e+00
## [956] 8.890538e-01 5.413461e-01 2.287746e+00 5.621266e+00 2.189454e+00
## [961] 2.995731e+00 1.917711e+00 6.649322e+00 1.674057e+00 1.303665e+00
## [966] 2.059940e+00 1.690913e-01 7.845821e-01 1.699550e+00 7.355366e-01
## [971] 1.784227e+00 6.904115e+00 1.861619e+00 3.816908e+00 8.305684e-01
## [976] 4.041816e+00 1.398251e+00 1.989853e+00 3.573178e+00 6.477112e+00
## [981] 7.150345e+00 2.989735e+00 2.183753e+00 7.687445e-01 1.986896e+00
## [986] 5.450535e+00 3.218021e+00 7.193370e+00 5.763675e+00 8.374398e+00
## [991] 3.126522e+00 2.819172e+00 4.233604e+00 5.786421e-01 1.168129e+00
## [996] 3.155286e-01 5.650221e+00 3.759010e-01 4.962007e-01 1.182788e+00
```

```
cat("[Repartitie exponentiala] Media este: ", mean(exp(le)), "\n")
```

```
## [Repartitie exponentiala] Media este: 3.427255
```

```
cat("[Repartitie exponentiala] Varianta este: ", var(exp(le)), "\n")
```

```
## [Repartitie exponentiala] Varianta este: 10.45688
```

## Repartitia normala

Generarea a N = 1000 variabile aleatoare cu ajutorul repartitiei normale:

```
norm = function(mean, sd) {
```

```
  n = c()
```

```
  n = rnorm(N, mean, sd)
```

```
  return(n)
```

```
}
```

```
norm(mean, sd)
```

```
## [1] 2.3401053244 6.9916625403 2.7099901165 -2.8729504809
```

```
## [5] -0.6547972715 0.1305596923 0.6362818393 2.8832281150
```

```
## [9] 4.8297839813 12.0853098474 4.7350348729 1.3228800263
```



# Proiect la Probabilitati si Statistica

```
## [13] 0.2047020479 1.2610425007 3.2430939006 2.4300289655
## [17] 8.8140639312 3.0389719797 3.5407871718 1.4972826969
## [21] 2.4791878720 4.1042087719 8.3052268250 -3.6080808404
## [25] 1.6327790686 2.2076991778 2.3013202983 0.4710431280
## [29] 2.7838493941 0.9110920755 1.7694713369 4.6078902712
## [33] 2.5208432046 3.1855593761 6.6955978499 2.6776043259
## [37] -0.2712180004 -6.6819874935 7.3549385148 5.3092237822
## [41] 3.4518814563 0.6220693895 3.3427407270 -0.9006419535
## [45] 3.9874133504 2.6160012366 -4.5555621963 -1.5240177075
## [49] 3.9142240976 -3.9067430451 -4.8024783418 5.3587143855
## [53] -4.7109193540 0.3832554303 5.8312768823 1.6213193907
## [57] 8.3025123540 -1.9800973016 -0.0004894438 11.5544292122
## [61] 0.7253988473 0.7091517010 -2.0451775198 5.7154454369
## [65] 5.1427045609 7.5746174396 4.5459455705 -0.5484593000
## [69] 0.9265081758 -3.8687997139 -2.9466389923 -1.0363802309
## [73] -0.6480124328 2.8744635989 4.5787099772 2.9354046803
## [77] 5.1993417803 -0.2993875954 -2.7655788343 4.6868653067
## [81] 4.4826793077 -0.9944273566 -0.3003995015 4.2106950036
## [85] 3.6381451069 -0.4179261421 -1.7787773506 -0.6082477457
## [89] 2.1580188275 1.7800507206 2.2769372703 0.8882654486
## [93] 0.0838379817 2.9408072408 2.5994788059 1.2472283850
## [97] -1.2378819709 0.2737233497 2.3696526382 3.1706334592
## [101] 1.4522167266 6.2039015734 5.6018386686 0.9603124968
## [105] 2.3636138996 5.7805679273 3.6709477720 -0.3106920415
## [109] 3.1103626695 -0.3884627983 4.6563830051 4.4373801099
## [113] 3.8520074744 5.3019499127 2.2969200767 3.4802254256
## [117] 4.3649813856 5.2630616052 4.9998737976 -2.9621572405
## [121] 6.0754792698 6.0763996360 0.0427826220 -2.1248104159
## [125] 0.7252474581 1.0792053859 -0.1981405632 2.1203695153
## [129] 5.4434812759 -1.5130274980 5.4159605915 -2.0139813409
## [133] 4.9874288976 2.3232354549 7.4578282306 2.9383285246
## [137] 1.4328378698 1.6070879633 4.4021376241 1.1555545130
## [141] 0.2064827781 7.0840289311 -0.7411948327 4.0921420031
## [145] 5.8097547225 2.0355408871 3.8814775247 -2.0394132322
## [149] 0.8923647973 3.8914746974 5.0417131550 -3.6763918574
## [153] 3.8953974998 -4.1539485384 5.4666586235 -1.7851957853
## [157] 0.2279803956 0.0107463219 -4.8429692446 1.3956337492
## [161] -0.2377093749 6.4801645279 -1.4652034843 1.7350121717
## [165] 5.2134104886 2.9450545147 3.7637043958 5.1201801154
## [169] 2.2189632183 1.0109808856 6.1338273585 1.3194453760
## [173] 1.8113484883 2.8076080741 2.9000706263 -4.3441116928
## [177] 3.6318502351 3.1979172284 -0.1686287163 2.6896788869
## [181] 2.9559245683 -1.7714814091 2.7945031432 1.9486202311
## [185] -3.8338326275 -0.4452194860 4.9988745819 0.5605061289
## [189] 9.2861528003 -1.7263665016 0.2067566060 -3.2390439229
## [193] 3.8266909814 1.4860256309 1.3962697001 1.3617022246
## [197] 4.4472827650 -8.0389710810 -4.5928616990 3.3428997805
## [201] 3.9599351066 -0.4551647161 0.9737687544 1.8387392753
## [205] 1.5689805667 6.5613255080 8.8065061745 3.4467648635
## [209] 1.7350167074 -1.7052573967 3.8159637388 8.3248118397
## [213] -2.2956130075 5.0557911749 1.8699799729 4.4840634904
## [217] 4.5051725460 3.8745443717 -0.4941502590 2.1053620984
```

# Proiect la Probabilitati si Statistica

```
## [221] -2.3225025793 -0.7663816583 -0.3126144061 3.0165541586
## [225] 2.9379023793 6.0820887215 -0.3478132993 1.6474216781
## [229] 1.5159412269 -1.9603255843 -2.1715248484 3.0363995439
## [233] 4.0257545099 4.2164853223 1.4527801730 4.4171769121
## [237] -0.5778475057 4.9831752852 3.0083502232 -1.5362684020
## [241] -1.6443223040 0.3585647237 -2.2253824710 0.1853435784
## [245] 3.2805486740 3.2694492551 1.7229639686 2.0322749429
## [249] -6.1415662090 2.5196913267 2.0150025576 -3.7904268366
## [253] 3.8096884042 1.5423220907 0.8636344051 1.3758481405
## [257] -1.6514713626 0.3268402945 2.2352312140 -1.4226276567
## [261] 2.1288223312 -0.1654738467 3.3254134341 3.8954788880
## [265] 0.1889668704 5.7982584834 -0.2334793142 2.1411799830
## [269] 6.1112217856 3.2909547613 1.4836238460 4.2147267219
## [273] -0.8058828230 3.7851306282 7.1062398841 6.2563452015
## [277] 4.0306994796 6.4495795360 4.3911515938 0.4253857347
## [281] 1.5895472388 -0.5123343529 -0.1196077449 3.5870651223
## [285] 2.9329406867 3.1356354639 1.3596965545 -0.8322457633
## [289] -3.1915489943 4.5273147722 0.1693761897 -4.6551442517
## [293] 0.1420762271 -0.8235850926 4.4939378905 3.2062697800
## [297] 3.8887395882 0.5499173048 2.6557409475 -2.4262060406
## [301] 2.8563230536 -4.9832462640 1.7242359921 4.5972309635
## [305] 2.7841249365 3.1674358946 -1.3874004331 0.7214614171
## [309] 6.4294377437 5.0271187856 6.1258405486 3.1020855552
## [313] 2.1778781741 1.9643438862 -2.2100038700 -0.2863322637
## [317] 0.0620435176 -4.9177584378 7.5411157246 3.6121327312
## [321] 0.1260679821 -0.6304998635 5.9339943860 4.3268817623
## [325] 5.5161635440 -4.0402086462 3.1673925545 2.7092957586
## [329] 3.8104177135 0.5380889724 2.0813378962 3.6832750596
## [333] -0.0569266200 2.9499647074 3.1405174747 -1.3585700950
## [337] 4.2997158717 2.0900094181 2.4527528473 4.2123115317
## [341] 2.9284164351 1.7059075733 -2.7083610095 1.6468517554
## [345] -0.3713278221 1.6038010087 -1.5947341395 -3.2794504965
## [349] -1.3193632086 4.3214457753 3.0723342724 4.5285606161
## [353] 4.2926195114 2.3429607875 2.2250184199 -0.4558207005
## [357] 6.7955529382 -0.2767116869 4.7381950786 0.8159266080
## [361] -1.7666122535 2.1399043200 7.6181773794 0.9560516849
## [365] 5.9418936779 2.3330370876 1.3753160858 0.9757866330
## [369] -0.1467408638 -1.1763227693 2.9425252975 0.1653255722
## [373] 4.2637852443 2.3618837206 1.9486293526 2.7400759449
## [377] 0.1807159195 2.2823667405 2.2150352609 3.7448788382
## [381] -0.5512695804 1.9582820337 1.2338049777 3.8013053334
## [385] 2.5032388903 2.9250994880 -1.1285778590 9.5347386769
## [389] 2.1912534456 -3.8981962832 1.7365222456 6.0453963707
## [393] -1.4547586566 -0.4555486039 -2.1719996528 3.1589694628
## [397] 2.9814141098 1.6137126862 -2.7087999157 4.8040785765
## [401] -4.7327276208 -3.9074205907 -0.8997694569 5.5885610597
## [405] -0.9759845808 4.5720826151 5.2202144114 3.1813990816
## [409] 1.0332952159 6.1600783593 1.7263156446 3.5822330069
## [413] -3.4258735198 3.2002030452 -1.1312458058 -0.1441467509
## [417] 7.2404982507 2.6538625676 0.4369704863 5.3718943749
## [421] -1.1789314450 9.2524948663 5.4574510370 -3.5374584550
## [425] 3.0881995502 0.2593148895 -0.3041011024 -0.1232571441
```

# Proiect la Probabilitati si Statistica

```
## [429] 0.6821398256 0.8741622211 3.5015875932 1.9891857423
## [433] -3.2537885828 -0.4228053206 8.5091169972 3.6218418870
## [437] 4.8449634134 0.2645251746 4.1693609452 1.5706360664
## [441] 7.1249647870 7.9218645272 -1.2211417566 2.4482180676
## [445] 3.4920429887 1.7011080239 2.4636631708 1.3113817730
## [449] 6.0468173881 1.5557776690 0.5297858763 0.7573778574
## [453] -3.4478799837 -0.0399444042 4.0934570194 0.7691732164
## [457] 0.2186130079 5.5230281744 6.9852019634 -4.4344232270
## [461] 2.5018438497 -1.0454262543 1.3417130262 -0.2967746992
## [465] -0.3669488565 -1.1810212035 8.9844127363 1.2230743711
## [469] 2.2342589500 -0.2287934950 4.4385415452 2.2312327457
## [473] 3.6866374574 2.6719353404 -3.7229069126 2.2664968428
## [477] 4.0914924067 2.4478071414 -0.7212530494 7.2711249925
## [481] -2.1204071056 2.8655862826 3.8871503878 2.4664402289
## [485] 0.8310316573 3.3792357000 1.5663877025 1.6165662701
## [489] 5.4169853131 -3.1932658735 3.8619365899 3.1157263722
## [493] -3.5580462971 1.2526622346 -1.4043436073 5.0304686213
## [497] 1.6579508331 1.4296773279 6.2358360788 2.8020279036
## [501] 6.4755625687 1.4681409328 3.9950620939 -2.9329944565
## [505] 3.0333203707 1.9025565588 2.1909408148 3.6677995977
## [509] 2.8926860877 1.3769883474 -1.5685262889 6.6235752994
## [513] 2.1062490997 3.0827947570 0.4468316943 5.2223555146
## [517] 5.1068701935 5.8087388649 4.8083219364 2.0633275649
## [521] 7.0400378607 5.2312899066 0.6235544379 4.1996146893
## [525] 5.1097203503 0.1555812221 5.7667244042 -3.5155644097
## [529] 7.3919161259 -0.8894295288 3.3691466423 1.0461008676
## [533] -0.8576516377 8.7724955786 0.6739279774 -0.1029288127
## [537] 0.3454611489 3.6864447709 -2.0719823779 1.6286812944
## [541] 3.4466482159 1.7813972997 -1.1983776433 -0.7914586959
## [545] 0.8543159082 -1.8458563519 -0.7540235126 2.9408397843
## [549] 7.3206883465 -0.9401330682 0.1405081539 4.7621331763
## [553] 8.1814947570 0.9614113769 0.2604304486 2.3885681810
## [557] 5.8434160564 1.7021525174 3.0027000124 0.7613441414
## [561] -2.6640209987 4.6555885097 4.5001244727 2.5684281087
## [565] 1.1461082847 -7.7915337386 0.0122992391 1.7297371225
## [569] 2.2601982646 -1.1702949330 -1.2654288863 0.6353111295
## [573] -3.3840048357 5.5314098233 1.7712183289 1.4291178162
## [577] 1.5612518204 -4.4109231181 -1.0006998440 -1.0002587680
## [581] 3.2597818935 5.1095391308 5.5216112592 2.9233255885
## [585] 10.9425349447 -2.5800031054 -1.3718325394 3.1322138414
## [589] 1.8011232642 3.8310194943 2.6278109454 4.2835096579
## [593] 3.8025194527 7.5287704239 3.6501411768 -1.2324662889
## [597] 1.7150321434 4.5759962338 0.7500700088 4.7539311079
## [601] 5.1313994667 4.4194458317 -2.8153767560 -2.4111599905
## [605] 1.7803895735 1.6677006698 3.6482848077 2.2823372775
## [609] 3.7302412844 -1.3057340804 6.3219955629 4.9536211421
## [613] 3.1222728923 1.2153851920 4.5986800976 -0.1118528081
## [617] 5.8441215563 0.2561091911 3.2632805321 -1.4439352929
## [621] 5.9674856519 1.2085685948 3.7471029246 9.0673547180
## [625] 2.7661659545 0.5584043469 3.6752224757 1.6868970128
## [629] -2.8725386379 6.6906697692 4.2259104964 3.4369765526
## [633] 2.3672502890 -0.5780239590 1.9912653111 -3.3733539508
```

# Proiect la Probabilitati si Statistica

```
## [637] -2.6683022392 3.7245332628 2.8991516118 -3.4014443070
## [641] -3.7020026103 2.9517222504 -2.4710966018 -0.4853300114
## [645] 2.6947574521 2.4625549915 4.2080443519 1.3767232468
## [649] -0.1890902931 6.0465452566 1.1702615749 4.7087621913
## [653] -2.9744753050 1.7743988026 -1.0852826323 4.0518797525
## [657] 6.9547335556 -0.6139594613 8.0445115168 -2.5367890725
## [661] 1.5853065708 4.3012193562 0.5625776567 7.2585348758
## [665] 3.9599133635 3.5607866935 3.0255733422 -1.3486935345
## [669] 4.5494415537 -4.8061902589 -2.5633656931 0.6805351604
## [673] -0.9811380777 -2.2797406946 -4.4393572358 3.4731580506
## [677] 8.3515158558 -2.9557656712 4.6646392214 1.7718855397
## [681] 4.3643544218 -2.6806545470 1.3693625241 2.6574973456
## [685] 2.6018070010 2.9910802760 -0.8249123283 4.0948298653
## [689] -0.6881876112 0.2169009655 -0.0640617285 5.6203488285
## [693] 3.6793400066 3.9079303849 2.4185057135 1.5915405846
## [697] -1.1156323761 2.6154565584 0.9015552972 5.7305083969
## [701] 5.2266131328 1.9192596002 3.9328880789 4.2924538474
## [705] -1.9327286160 1.2183111994 0.4656102162 2.9846260796
## [709] 4.4609807146 2.3191827872 1.2529204365 1.3557374303
## [713] 0.3189715365 5.5859129432 -0.2926951500 3.8794805721
## [717] 0.5771173897 -0.1494281523 1.1091161456 5.1606726813
## [721] 7.1478547453 0.9747898268 2.4226236833 5.4864505566
## [725] -2.8125737457 -2.0856299816 1.6886851997 -2.5821403566
## [729] 3.6039580307 8.6695931942 4.8271567296 2.6753847961
## [733] 1.9662294877 9.1254009415 10.7057691125 4.5124485445
## [737] 1.2701453587 5.0954071052 0.9070009728 -5.1879231744
## [741] 3.6719118676 2.1680100413 0.9003198281 0.2026520057
## [745] 1.9888728307 1.9549269750 2.6413362927 1.9646648804
## [749] 1.5568153256 -0.9580742884 0.2516221891 5.0638515426
## [753] 3.0911850664 7.1035693942 -6.3719606231 -3.2293203625
## [757] 4.2909984604 -0.3525399826 8.1915646008 0.1081767832
## [761] 6.8489051999 -4.8400175151 6.3401478643 1.0933606397
## [765] 5.6944515498 5.1200149074 -2.6650799831 0.7029396459
## [769] 1.3475205688 0.9914010173 2.9130299947 6.0525598971
## [773] 6.1579981083 1.2487146639 -2.1844177409 4.5032053807
## [777] 6.2803876887 -0.4368129894 -0.8760983426 2.6633256423
## [781] -1.1080888145 6.3829126292 2.3426776043 0.7283029768
## [785] -0.8617849823 6.0571186576 2.8102125644 0.1709315895
## [789] 3.8203907623 2.0717654734 0.4511866163 -0.1380083231
## [793] 6.3638208094 -2.5416257125 -2.7323984849 1.9123897429
## [797] 2.9143668251 5.2185320834 1.0257997409 3.7252404793
## [801] 2.7029627156 -3.0260045065 1.3230840656 1.1021153655
## [805] 7.6462906708 1.0192051385 2.4350204600 -0.6884934554
## [809] 0.3417611218 3.5608221852 5.1478517715 2.6669919421
## [813] 3.8787376153 0.0055045455 3.1281152597 4.6916292052
## [817] 4.1944928031 2.7782114432 -0.6165634281 3.1605443488
## [821] -3.0797717174 0.3574232885 0.6829820429 -1.0128152667
## [825] 2.9613384655 -2.4970920170 3.7399986954 3.9359879407
## [829] 2.9454446195 1.5950623621 4.9699378234 3.3311520177
## [833] 5.8925242004 6.1575649955 4.4572316556 4.3989333620
## [837] -0.0058668329 1.4088664288 4.4141475152 6.9954942083
## [841] 2.3071670014 1.5406138483 -0.9427608381 6.4395311118
```

## Proiect la Probabilitati si Statistica

```
## [845] 1.2178819337 0.7668552019 3.8353700859 4.0335472980
## [849] -1.0825845885 1.8820294115 6.5868203358 2.9121958827
## [853] 4.5080637972 3.1229619723 3.3510162587 2.5392611787
## [857] 5.1991469458 4.4275505007 1.7215861849 2.2948942930
## [861] 1.8422806779 3.1903564945 5.5579062533 0.1681698371
## [865] 2.1875249567 -2.0470538137 7.2196642751 1.5370256424
## [869] 3.5240925089 3.4908834824 -0.4290112443 6.5331691068
## [873] 3.0953695974 4.8756085842 -1.7114965622 2.6500975423
## [877] 3.6134554127 0.0206685938 2.4108380770 0.1683167490
## [881] 4.9466439299 1.1532716833 1.2199138823 7.1881220229
## [885] 3.0070100528 3.3019867960 -2.5056375731 0.5204208263
## [889] -2.0843602611 5.4050706141 7.9854253044 2.9171246664
## [893] 0.8792986317 2.0406774025 4.8902452876 6.3096218480
## [897] -1.5321418165 3.3031447145 2.0528856143 0.7322510456
## [901] 2.0584181362 -2.0531299659 4.6046994794 -3.1475884727
## [905] 3.2427997936 0.1770502248 -3.9635566051 -2.4115682115
## [909] 1.9420996382 -2.8967819795 1.6912103197 -0.3864737283
## [913] 3.8813125918 -0.4142555185 -1.1718350675 2.4247867421
## [917] 3.6315006164 -0.8496197501 5.0563721266 4.8536459049
## [921] 0.2696506608 5.1163701539 3.1874218807 -0.8030111030
## [925] -2.1732293896 5.3389479776 0.5627289778 2.0244891412
## [929] 0.9100748107 0.0197205646 -0.1400620015 -3.4759711246
## [933] 7.2722735136 0.3488239592 2.8373678073 3.2307134851
## [937] 0.0248283820 1.0033569645 7.6801519179 1.5253344062
## [941] -1.7644693096 -0.5322890239 1.5045268474 3.0057977236
## [945] 1.1719323734 3.8910055273 0.3482716738 -2.9160481736
## [949] -2.7321522740 3.6542621643 5.0883508032 3.4315534702
## [953] 6.1067868149 6.4848447030 1.8197787468 -2.6405433560
## [957] 2.0509870798 -0.7389398402 -1.7987538642 -0.9843469935
## [961] 1.7660974380 -3.8612165884 5.9669356594 5.4054633095
## [965] -0.4002569345 4.1000184177 4.5641221177 -0.1170093934
## [969] 2.1512098152 5.3140129976 2.9642406014 -0.5347084614
## [973] 3.4035727016 3.0679676010 4.2646028130 -3.9907918484
## [977] -1.0190809057 2.4301391807 3.0091736651 0.8195596906
## [981] 2.3775520008 3.9276372864 -4.7625602187 2.4451133357
## [985] 1.5430800999 1.41224444807 0.7450354113 2.2124805994
## [989] 5.6444006753 5.9405727520 0.3162055189 1.4703613898
## [993] -2.6122492608 8.0376436640 1.1333557133 2.9429616533
## [997] 5.0801226590 1.9465595823 -0.5552258971 1.4350813869
```

```
cat("[Repartitie normala] Media este: ", mean(norm(mean, sd)), "\n")
```

```
## [Repartitie normala] Media este: 2.093079
```

```
cat("[Repartitie normala] Varianta este: ", var(norm(mean, sd)), "\n")
```

```
## [Repartitie normala] Varianta este: 9.474343
```

## Ilustrarea grafica a functiilor de masa/densitate

Functia `par()` foloseste la generarea mai multor grafice in aceeasi imagine. Functia `plot()` genereaza un grafic, iar functia `lines` adauga un alt grafic la cel initial. Functia `legend()` creeaza o legenda. Functiile `dbinom`, `dpois`, `dexp`, `dnorm` genereaza densitatea/masa fiecarei repartitii.

```
exercitiul2 = function() {
  old.par <- par(mfrow=c(2, 2))

  plot (xd, dbinom(xd, 4, 0.7), type = "l", col = "blue", xlab = "x", ylab = "Masa", ylim
= c(0, 0.7), main = "Functia de masa [repartitie binomiala]")
  lines (xd, dbinom(xd, 3, 0.5), col = "red", type = "l")
  lines (xd, dbinom(xd, 2, 0.23), col = "yellow", type = "l")
  lines (xd, dbinom(xd, 5, 0.2), col = "green", type = "l")
  lines (xd, dbinom(xd, 2, 0.4), col = "purple", type = "l")
  legend ("topright", c(expression(paste(Beta, "(4, 0.7)")), expression(paste(Beta, "(3,
0.5)")), expression(paste(Beta, "(2, 0.23)")), expression(paste(Beta, "(5, 0.2)")), expre
ssion(paste(Beta, "(2, 0.4)"))), col = c("blue", "red", "yellow", "green", "purple"), lty
= c(1, 1, 1, 1, 1), lwd = c(1, 1, 1, 1, 1))

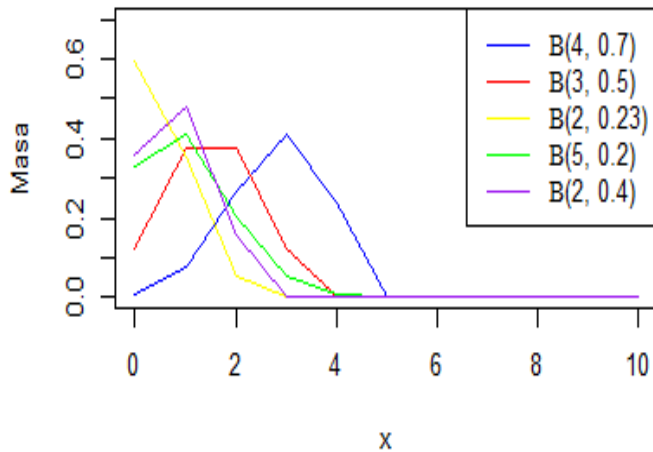
  plot (xd, dpois(xd, 0.7), type = "l", col = "blue", xlab = "x", ylab = "Masa", ylim = c
(0, 0.9), main = "Functia de masa [repartitie Poisson]")
  lines (xd, dpois(xd, 0.5), col = "red", type = "l")
  lines (xd, dpois(xd, 0.23), col = "yellow", type = "l")
  lines (xd, dpois(xd, 0.2), col = "green", type = "l")
  lines (xd, dpois(xd, 0.4), col = "purple", type = "l")
  legend("topright", c(expression(paste(Rho, "(0.7)")), expression(paste(Rho, "(0.5)")),
expression(paste(Rho, "(0.23)")), expression(paste(Rho, "(0.2)")), expression(paste(Rho,
"(0.4)"))), col = c("blue", "red", "yellow", "green", "purple"), lty = c(1, 1, 1, 1, 1),
lwd = c(1, 1, 1, 1, 1))

  plot (xc, dexp(xc, 0.7), type = "l", col = "blue", xlab = "x", ylab = "Densitate", main
= "Functia densitate [repartitie exponentiala]")
  lines (xc, dexp(xc, 0.5), col = "red", type = "l")
  lines (xc, dexp(xc, 0.23), col = "yellow", type = "l")
  lines (xc, dexp(xc, 0.2), col = "green", type = "l")
  lines (xc, dexp(xc, 0.4), col = "purple", type = "l")
  legend("topright", c(expression(paste(Epsilon, "(0.7)")), expression(paste(Epsilon, "(0
.5)")), expression(paste(Epsilon, "(0.23)")), expression(paste(Epsilon, "(0.2)")), expres
sion(paste(Epsilon, "(0.4)"))), col = c("blue", "red", "yellow", "green", "purple"), lty
= c(1, 1, 1, 1, 1), lwd = c(1, 1, 1, 1, 1))

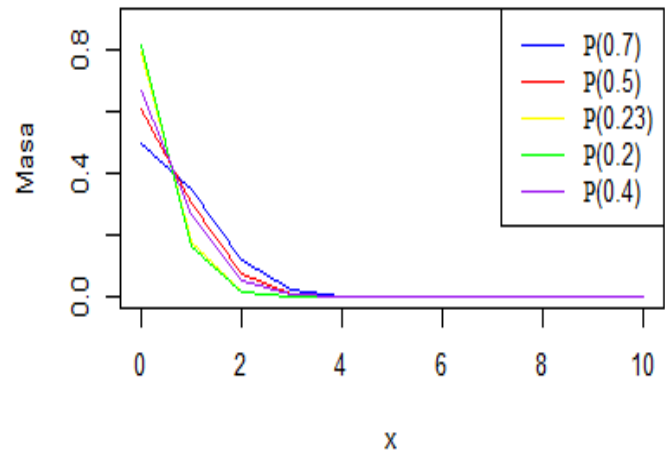
  plot (xc, dnorm(xc, 4, 0.7), type = "l", col = "blue", xlab = "x", ylab = "Densitate",
xlim = c(0, 8), ylim = c(0, 3), main = "Functia densitate [repartitie normala]")
  lines (xc, dnorm(xc, 3, 0.5), col = "red", type = "l")
  lines (xc, dnorm(xc, 2, 0.23), col = "yellow", type = "l")
  lines (xc, dnorm(xc, 5, 0.2), col = "green", type = "l")
  lines (xc, dnorm(xc, 2, 0.4), col = "purple", type = "l")
  legend("topright", c(expression(paste(Nu, "(4, 0.7)")), expression(paste(Nu, "(3, 0.5)"
)), expression(paste(Nu, "(2, 0.23)")), expression(paste(Nu, "(5, 0.2)")), expression(pas
```

```
te(Nu, "(2, 0.4)")), col = c("blue", "red", "yellow", "green", "purple"), lty = c(1, 1,
1, 1, 1), lwd = c(1, 1, 1, 1, 1))
par(old.par)
}
exercitiul2()
```

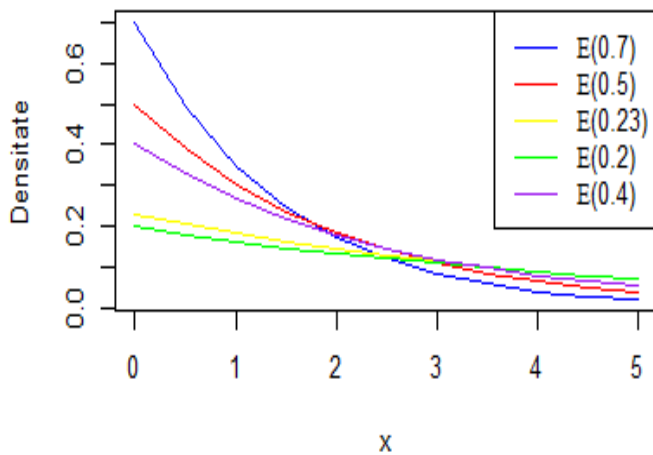
**Funcția de masă [repartiție binomială]**



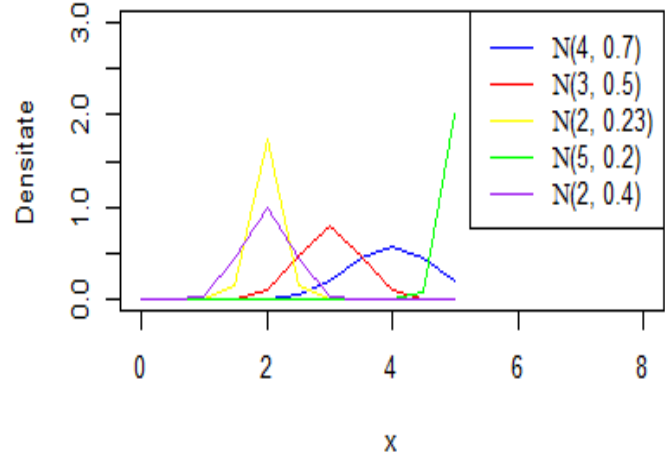
**Funcția de masă [repartiție Poisson]**



**Funcția densitate [repartiție exponențială]**



**Funcția densitate [repartiție normală]**



## Funcțiile de repartitie pentru cele 5 seturi de parametrii diferiti

Funcțiile pbinom, ppois, pexp, pnorm generează repartitiile corespunzătoare.

```
exercitiul3 = function() {
  old.par <- par(mfrow=c(2, 2))

  plot (xd, pbinom(xd, 4, 0.7), type = "l", col = "blue", xlab = "x", ylab = "Repartitie"
, main = "Funcția de repartitie [repartitie binomiala]")
  lines (xd, pbinom(xd, 3, 0.5), col = "red", type = "l")
  lines (xd, pbinom(xd, 2, 0.23), col = "yellow", type = "l")
  lines (xd, pbinom(xd, 5, 0.2), col = "green", type = "l")
  lines (xd, pbinom(xd, 2, 0.4), col = "purple", type = "l")
  legend ("topright", c(expression(paste(Beta, "(4, 0.7)")), expression(paste(Beta, "(3,
0.5)")), expression(paste(Beta, "(2, 0.23)")), expression(paste(Beta, "(5, 0.2)")), expre
ssion(paste(Beta, "(2, 0.4)"))), col = c("blue", "red", "yellow", "green", "purple"), lty
= c(1, 1, 1, 1, 1), lwd = c(1, 1, 1, 1, 1))

  plot (xd, ppois(xd, 0.7), type = "l", col = "blue", xlab = "x", ylab = "Repartitie", ma
in = "Funcția de repartitie [repartitie Poisson]")
  lines (xd, ppois(xd, 0.5), col = "red", type = "l")
  lines (xd, ppois(xd, 0.23), col = "yellow", type = "l")
  lines (xd, ppois(xd, 0.2), col = "green", type = "l")
  lines (xd, ppois(xd, 0.4), col = "purple", type = "l")
  legend("topright", c(expression(paste(Rho, "(0.7)")), expression(paste(Rho, "(0.5)")),
expression(paste(Rho, "(0.23)")), expression(paste(Rho, "(0.2)")), expression(paste(Rho,
"(0.4)"))), col = c("blue", "red", "yellow", "green", "purple"), lty = c(1, 1, 1, 1, 1),
lwd = c(1, 1, 1, 1, 1))

  plot (xc, pexp(xc, 0.7), type = "l", col = "blue", xlab = "x", ylab = "Repartitie", xli
m = c(0, 8), main = "Funcția de repartitie [repartitie exponentiala]")
  lines (xc, pexp(xc, 0.5), col = "red", type = "l")
  lines (xc, pexp(xc, 0.23), col = "yellow", type = "l")
  lines (xc, pexp(xc, 0.2), col = "green", type = "l")
  lines (xc, pexp(xc, 0.4), col = "purple", type = "l")
  legend("topright", c(expression(paste(Epsilon, "(0.7)")), expression(paste(Epsilon, "(0
.5)")), expression(paste(Epsilon, "(0.23)")), expression(paste(Epsilon, "(0.2)")), expres
sion(paste(Epsilon, "(0.4)"))), col = c("blue", "red", "yellow", "green", "purple"), lty
= c(1, 1, 1, 1, 1), lwd = c(1, 1, 1, 1, 1))

  plot (xc, pnorm(xc, 4, 0.7), type = "l", col = "blue", xlab = "x", ylab = "Repartitie",
xlim = c(0, 8), ylim = c(0, 1.1), main = "Funcția de repartitie [repartitie normala]")
  lines (xc, pnorm(xc, 3, 0.5), col = "red", type = "l")
  lines (xc, pnorm(xc, 2, 0.23), col = "yellow", type = "l")
  lines (xc, pnorm(xc, 5, 0.2), col = "green", type = "l")
  lines (xc, pnorm(xc, 2, 0.4), col = "purple", type = "l")
  legend("topright", c(expression(paste(Nu, "(4, 0.7)")), expression(paste(Nu, "(3, 0.5)"
)), expression(paste(Nu, "(2, 0.23)")), expression(paste(Nu, "(5, 0.2)")), expression(pas
te(Nu, "(2, 0.4)"))), col = c("blue", "red", "yellow", "green", "purple"), lty = c(1, 1,
1, 1, 1), lwd = c(1, 1, 1, 1, 1))
```

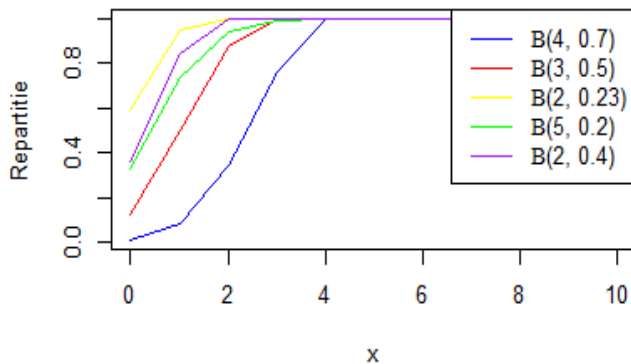


```

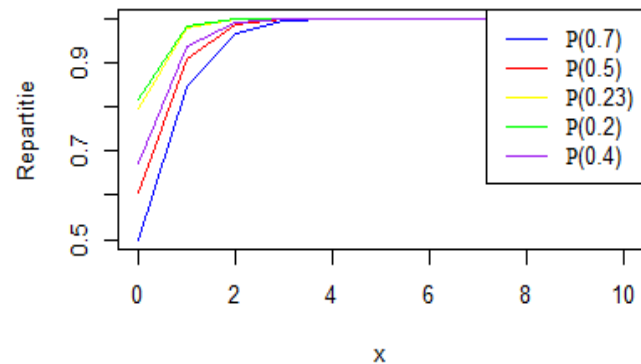
par(old.par)
}
exercitiul3()

```

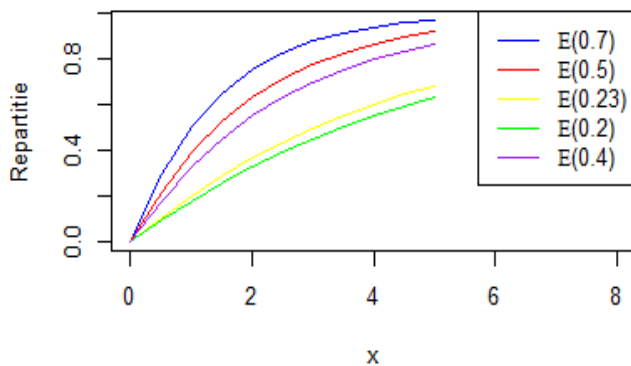
Funcția de repartiție [repartiție binomială]



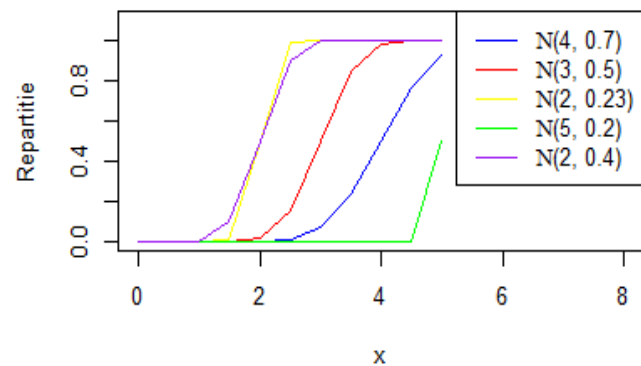
Funcția de repartiție [repartiție Poisson]



Funcția de repartiție [repartiție exponențială]



Funcția de repartiție [repartiție normală]



## Aproximarea funcției de repartiție și de masă a binomialei

```

aproximarea = function(n, p){
  probBin = NULL
  densBin = NULL
  probPois = NULL
  probNorm = NULL
  probNoFC = NULL
  probCP = NULL

  q = 1 - p

  for(k in 1:10){
    probBin[k] = pbinom(k, n, p)
    densBin[k] = dbinom(k, n, p)
    ps = rpois(n, n * p)
    probPois[k] = length(ps[ps <= k]) / n
  }
}

```

## Proiect la Probabilitati si Statistica

```

nm = rnorm(n, n * p, sqrt(n * p * q))
N = (k - mean(nm)) / sd(nm)
probNorm[k] = pnorm(N)

Nc = ((k + 0.5) - mean(nm)) / sd(nm)
probNoFC[k] = pnorm(Nc)

r = abs((k + 1) * (1 - p)) / abs(p * (n - k))
a = 1 / (9 * (n - k))
b = 1 / (9 * (k + 1))
S = a + b * (r ^ (2 / 3))
m = 1 - a
c = (1 - b) * (r ^ (1 / 3))
probCP[k] = pnorm((c - m) / sqrt(S))
}
cbind(densBin, probBin, probPois, probNorm, probNoFC, probCP)
}

```

n = 25 p = 0.05

##		densBin	probBin	probPois	probNorm	probNoFC	probCP
##	[1,]	3.649863e-01	0.6423759	0.68	0.4733693	0.6868201	0.6452200
##	[2,]	2.305177e-01	0.8728935	0.92	0.6747482	0.7954858	0.8733858
##	[3,]	9.301589e-02	0.9659094	0.96	0.9668103	0.9922728	0.9651268
##	[4,]	2.692565e-02	0.9928351	1.00	0.9999736	0.9999992	0.9922684
##	[5,]	5.951987e-03	0.9987870	1.00	0.9998997	0.9999883	0.9985791
##	[6,]	1.044208e-03	0.9998312	1.00	0.9999997	1.0000000	0.9997790
##	[7,]	1.491726e-04	0.9999804	1.00	0.9999970	0.9999995	0.9999705
##	[8,]	1.766518e-05	0.9999981	1.00	1.0000000	1.0000000	0.9999966
##	[9,]	1.756187e-06	0.9999998	1.00	1.0000000	1.0000000	0.9999997
##	[10,]	1.478894e-07	1.0000000	1.00	1.0000000	1.0000000	1.0000000

n = 25 p = 0.1

##		densBin	probBin	probPois	probNorm	probNoFC	probCP
##	[1,]	1.994161e-01	0.2712059	0.24	0.2031114	0.2898639	0.2706080
##	[2,]	2.658881e-01	0.5370941	0.40	0.3882023	0.5188958	0.5383546
##	[3,]	2.264973e-01	0.7635914	0.68	0.6904117	0.8590071	0.7647348
##	[4,]	1.384150e-01	0.9020064	0.88	0.8727431	0.9555870	0.9021393
##	[5,]	6.459368e-02	0.9666001	0.96	0.9660813	0.9852869	0.9662328
##	[6,]	2.392358e-02	0.9905236	1.00	0.9978155	0.9993024	0.9901932
##	[7,]	7.215049e-03	0.9977387	1.00	0.9995168	0.9998638	0.9975741
##	[8,]	1.803762e-03	0.9995425	1.00	0.9999615	0.9999915	0.9994841
##	[9,]	3.785674e-04	0.9999210	1.00	0.9999998	1.0000000	0.9999050
##	[10,]	6.730087e-05	0.9999883	1.00	0.9999999	1.0000000	0.9999848

n = 50 p = 0.05

##		densBin	probBin	probPois	probNorm	probNoFC	probCP
##	[1,]	0.2024867770	0.2794318	0.18	0.2700333	0.4042998	0.2787915
##	[2,]	0.2611013704	0.5405331	0.54	0.3504656	0.4854873	0.5419320

# Proiect la Probabilitati si Statistica

```
## [3,] 0.2198748382 0.7604080 0.74 0.6597806 0.7805109 0.7617348
## [4,] 0.1359752289 0.8963832 0.86 0.8514955 0.9084585 0.8966284
## [5,] 0.0658406372 0.9622238 0.98 0.8991660 0.9420236 0.9618574
## [6,] 0.0259897252 0.9882136 0.98 0.9858225 0.9940889 0.9878222
## [7,] 0.0085981046 0.9968117 1.00 0.9947921 0.9976524 0.9965871
## [8,] 0.0024323585 0.9992440 1.00 0.9999915 0.9999987 0.9991503
## [9,] 0.0005974214 0.9998414 1.00 0.9999845 0.9999963 0.9998103
## [10,] 0.0001289172 0.9999704 1.00 0.9999988 0.9999998 0.9999617
```

n = 50 p = 0.1

```
## densBin probBin probPois probNorm probNoFC probCP
## [1,] 0.02863208 0.03378586 0.08 0.01654694 0.03006247 0.03347043
## [2,] 0.07794290 0.11172876 0.12 0.07722463 0.11451055 0.11092527
## [3,] 0.13856515 0.25029391 0.34 0.13970507 0.19999518 0.24973031
## [4,] 0.18090450 0.43119841 0.46 0.27197177 0.35428172 0.43140627
## [5,] 0.18492460 0.61612301 0.62 0.44468647 0.54337080 0.61685407
## [6,] 0.15410383 0.77022684 0.76 0.65785811 0.74731569 0.77089036
## [7,] 0.10762807 0.87785492 0.92 0.82856185 0.87724122 0.87812696
## [8,] 0.06427788 0.94213279 0.88 0.90746228 0.94216308 0.94206842
## [9,] 0.03332927 0.97546206 1.00 0.96301052 0.97753255 0.97526407
## [10,] 0.01518333 0.99064540 1.00 0.99360233 0.99681914 0.99046300
```

n = 100 p = 0.05

```
## densBin probBin probPois probNorm probNoFC probCP
## [1,] 0.03116068 0.03708121 0.03 0.03858378 0.05958831 0.03669114
## [2,] 0.08118177 0.11826298 0.16 0.13131399 0.17934121 0.11735451
## [3,] 0.13957568 0.25783866 0.26 0.14695558 0.20546279 0.25722355
## [4,] 0.17814264 0.43598130 0.46 0.34404938 0.43116745 0.43621282
## [5,] 0.18001783 0.61599913 0.61 0.61148072 0.70148832 0.61680670
## [6,] 0.15001486 0.76601398 0.86 0.66444773 0.74768467 0.76677287
## [7,] 0.10602554 0.87203952 0.88 0.84093823 0.89299352 0.87238911
## [8,] 0.06487089 0.93691041 0.92 0.89931008 0.93248803 0.93688116
## [9,] 0.03490130 0.97181171 0.98 0.94304203 0.96364024 0.97160682
## [10,] 0.01671588 0.98852759 0.98 0.98173833 0.98940506 0.98831516
```

n = 100 p = 0.1

```
## densBin probBin probPois probNorm probNoFC probCP
## [1,] 0.0002951267 0.0003216881 0.00 0.001843607 0.003078370 0.0003768871
## [2,] 0.0016231966 0.0019448847 0.00 0.005777595 0.008927185 0.0020472627
## [3,] 0.0058916025 0.0078364871 0.03 0.019822617 0.028259575 0.0079372432
## [4,] 0.0158745955 0.0237110827 0.02 0.023439712 0.034195644 0.0237016956
## [5,] 0.0338658038 0.0575768865 0.13 0.061752663 0.083775090 0.0573669670
## [6,] 0.0595787289 0.1171556154 0.13 0.076561092 0.102973984 0.1167730189
## [7,] 0.0888952464 0.2060508618 0.18 0.143245884 0.185346374 0.2056576427
## [8,] 0.1148230266 0.3208738884 0.32 0.235477588 0.286619151 0.3206667053
## [9,] 0.1304162771 0.4512901654 0.41 0.386516916 0.457825060 0.4513689123
## [10,] 0.1318653468 0.5831555123 0.54 0.515517793 0.579786038 0.5834688363
```

**Eroarea maximala absoluta**

```

eroarea = function(n){
  p = seq(0.01, 0.5, 0.01)

  probBin = NULL
  probPois = NULL
  probNorm = NULL
  probNoFC = NULL
  probCP = NULL

  errPois = NULL
  errNorm = NULL
  errNoFC = NULL
  errCP = NULL

  for(i in seq_along(p)){
    maxP = 0
    maxN = 0
    maxNc = 0
    maxCP = 0;

    q = 1 - p[i]

    for(k in 1:10){
      probBin = pbinom(k, n, p[i])

      ps = rpois(n, n * p[i])
      probPois = length(ps[ps <= k]) / n

      nm = rnorm(n, n * p[i], sqrt(n * p[i] * q))
      N = (k - mean(nm)) / sd(nm)
      probNorm = pnorm(N)

      Nc = ((k + 0.5) - mean(nm)) / sd(nm)
      probNoFC = pnorm(Nc)

      r = abs((k + 1) * (1 - p[i])) / abs(p[i] * (n - k))
      a = 1 / (9 * (n - k))
      b = 1 / (9 * (k + 1))
      S = a + b * (r ^ (2 / 3))
      m = 1 - a
      c = (1 - b) * (r ^ (1 / 3))
      probCP = pnorm((c - m) / sqrt(S))

      maxP = max(maxP, abs(probPois - probBin))
      maxN = max(maxN, abs(probNorm - probBin))
      maxNc = max(maxNc, abs(probNoFC - probBin))
      maxCP = max(maxCP, abs(probCP - probBin))
    }
    errPois[i] = maxP;
    errNorm[i] = maxN;
  }
}

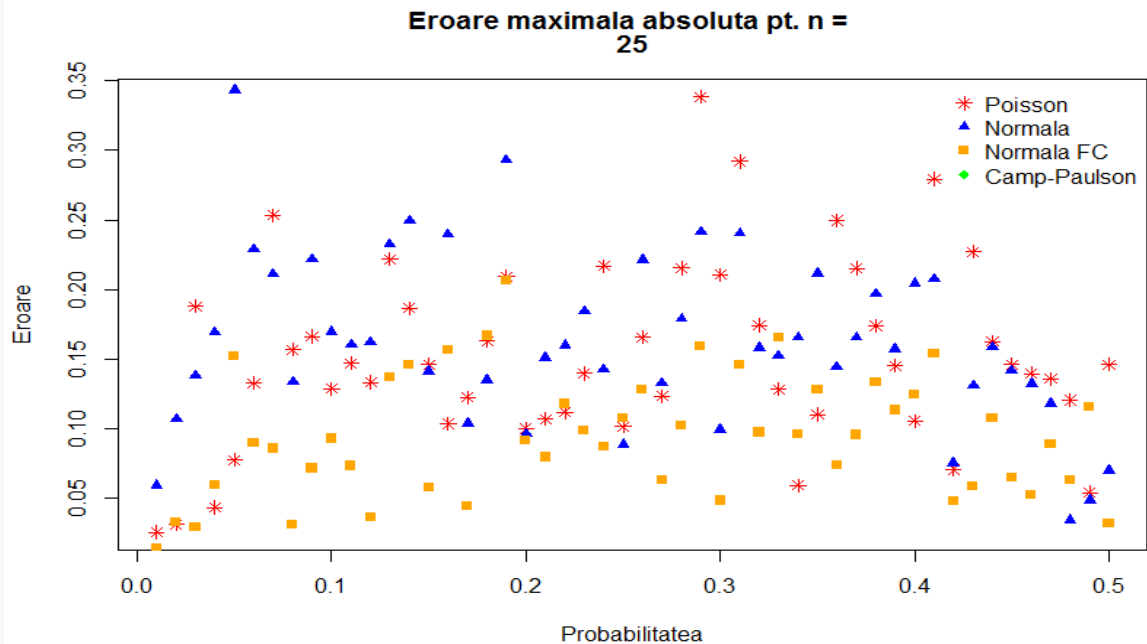
```

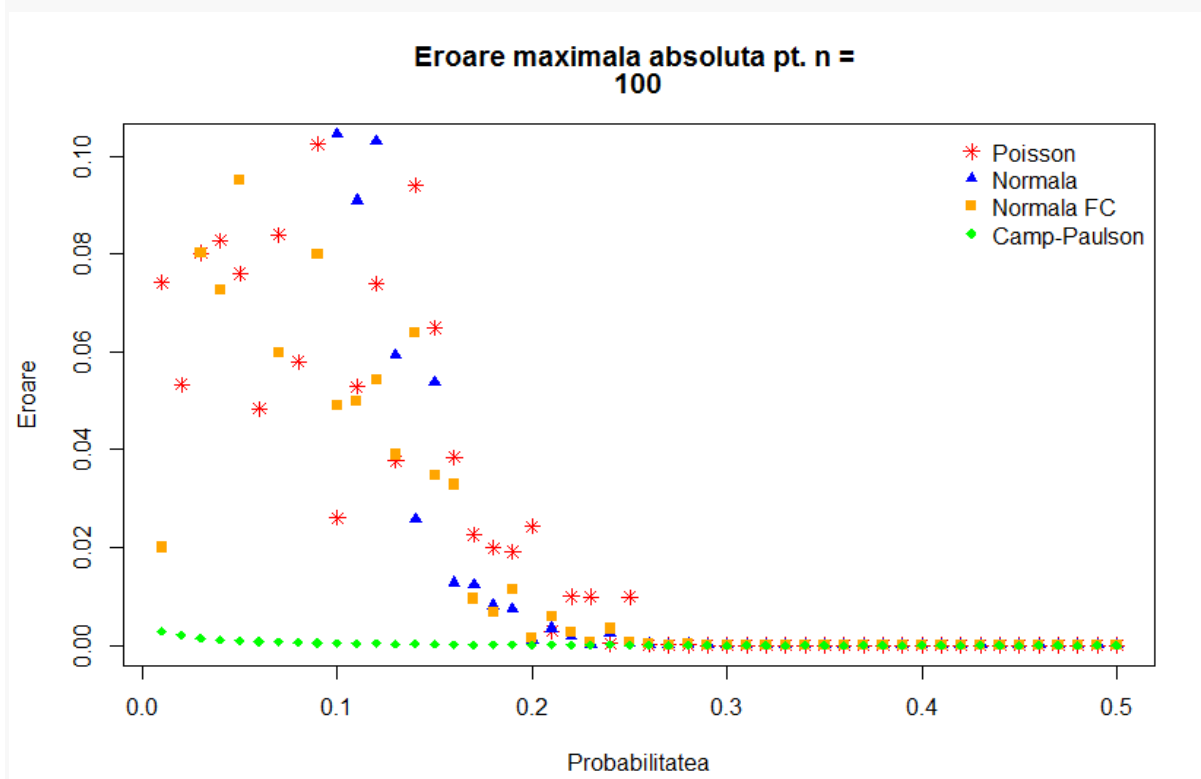
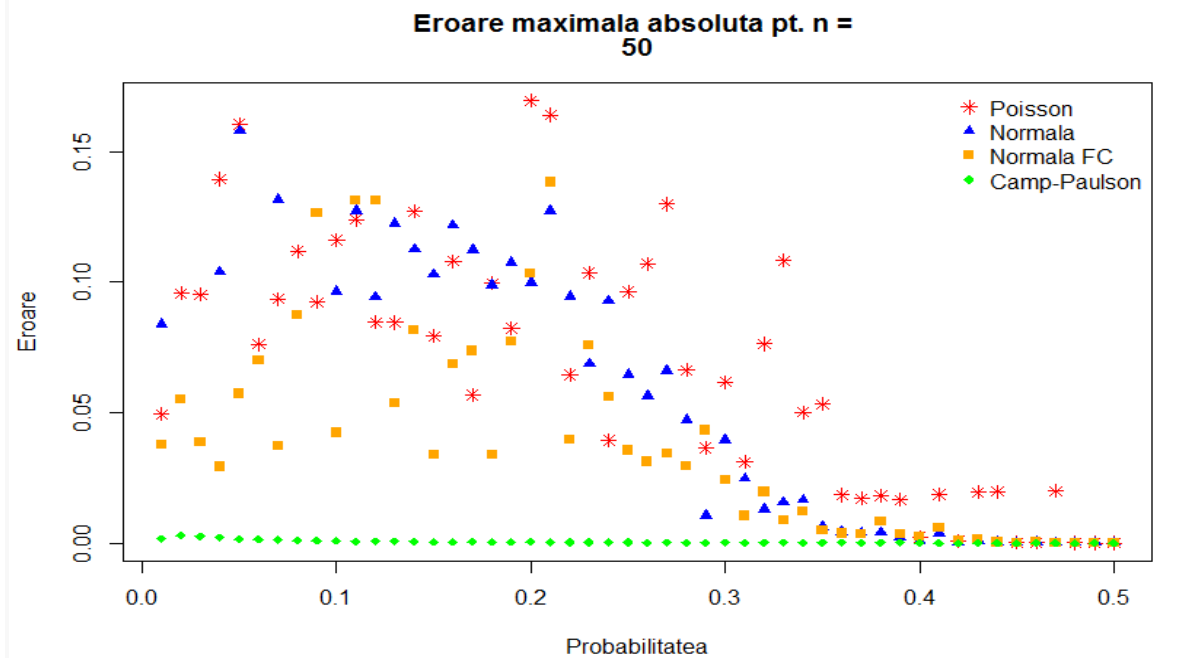
## Proiect la Probabilitati si Statistica

```

    errNoFC[i] = maxNc;
    errCP[i] = maxCP;
}
plot(p, errPois, xlab = "Probabilitatea", ylab = "Eroare", col = "red", pch = 8)
title(main = c("Eroare maximala absoluta pt. n = ", n))
points(p, errNorm, col = "blue", pch = 17)
points(p, errNoFC, col = "orange", pch = 15)
points(p, errCP, col = "green", pch = 18)
legend("topright", pch = c(8, 17, 15, 18), c("Poisson", "Normala", "Normala FC", "Camp-
Paulson"), col = c("red", "blue", "orange", "green"), bty="n")
}

```





Observam ca aproximarea normala cu factor de corectie este mai precisa decat aproximarea normala, aproximarea Poisson are cele mai mari erori dintre toate cele 4 studiate, iar aproximarea Camp Paulson este cea mai precisa. In momentul in care numarul de observatii creste, toate functiile tind sa aproximeze din ce in ce mai bine binomiala  $B(n, p)$ .

## PROBLEMA 2

### Justificarea teoretica a simularii cuplului

Plecam de la doua variabile repartizate uniform pe  $[-1, 1]$  demonstram :

$$X_1 \sim U[-1, 1] \Rightarrow P(X_1 = x_1) = \frac{1}{2}, \forall x_1 \in [-1, 1]$$

$$X_2 \sim U[-1, 1] \Rightarrow P(X_2 = x_2) = \frac{1}{2}, \forall x_2 \in [-1, 1]$$

$$P((X_1, X_2) = (x_1, x_2)) = P(X_1 = x_1, X_2 = x_2) = P(X_1 = x_1)P(X_2 = x_2) = \frac{1}{4}, \forall x_1, x_2 \in [-1, 1]$$

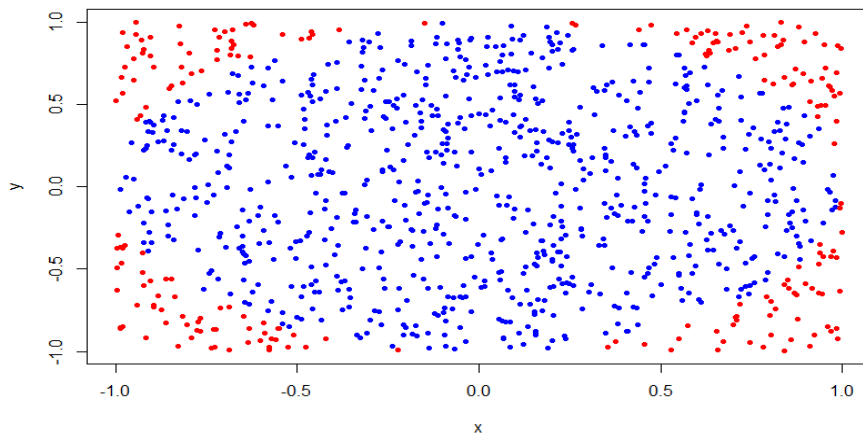
$$P(X_1 = x_1, X_2 = x_2) = \frac{1}{4} = \frac{1}{\text{Aria}([-1, 1]^2)} \Rightarrow (X_1, X_2) \sim U([-1, 1]^2)$$

### Metoda acceptarii si respingerii

Punctele reprezentate cu albastru apartin discului de unitate  $D(1)$ , iar cele reprezentate cu rosu nu apartin.

```
acc_reject = function(){
  x <-c(runif(1, min = -1, max = 1))
  y <-c(runif(1, min = -1, max = 1))
  for (i in 2:N)
  {
    x <-c(x, runif(1, min = -1, max = 1))
    y <-c(y, runif(1, min = -1, max = 1))
  }

  plot(x, y, col = ifelse(x * x + y * y <= 1, "blue", "red"), pch = 20)
}
```



## Simularea punctelor prin coordonate polare

```
polar_coords = function(){  
  theta <- runif(1, min = 0, max = 2 * pi)  
  rho <- runif(1, min = 0, max = 1)  
  x <- c( rho * cos(theta))  
  y <- c(rho * sin(theta))  
  
  for (i in 2:N)  
  {  
    theta <- c(theta, runif(1, min = 0, max = 2 * pi) )  
    rho <- c(rho, runif(1, min = 0, max = 1))  
    x <- c(rho * cos(theta))  
    y <- c(rho * sin(theta))  
  }  
  
  plot(x, y)  
  circle = seq(-1, 1, by = 0.01)  
  lines(circle, sqrt(1 - circle^2), col = "red")  
  lines(circle, -sqrt(1 - circle^2), col = "red")  
}
```

