

CONFUSION MATRIX

Example: Medical Test for Disease

Suppose we tested **100 people**.

- 40 actually had the disease.
- 60 did not have the disease.

Our model's predictions:

	Predicted Positive	Predicted Negative	Total
Actual Positive	TP = 30	FN = 10	40
Actual Negative	FP = 15	TN = 45	60
Total	45	55	100

Calculations

1. **Accuracy** = $(TP + TN) / \text{Total}$
= $(30 + 45) / 100 = \mathbf{0.75 (75\%)}$
2. **Error Rate** = $1 - \text{Accuracy}$
= $1 - 0.75 = \mathbf{0.25 (25\%)}$
3. **Precision (Positive Predictive Value)** = $TP / (TP + FP)$
= $30 / (30 + 15) = 30 / 45 = \mathbf{0.67 (67\%)}$
4. **Recall (Sensitivity, TPR)** = $TP / (TP + FN)$
= $30 / (30 + 10) = 30 / 40 = \mathbf{0.75 (75\%)}$
5. **Specificity (True Negative Rate)** = $TN / (TN + FP)$
= $45 / (45 + 15) = 45 / 60 = \mathbf{0.75 (75\%)}$
6. **F1 Score** = $2 \times (\text{Precision} \times \text{Recall}) / (\text{Precision} + \text{Recall})$
= $2 \times (0.67 \times 0.75) / (0.67 + 0.75)$
 $\approx \mathbf{0.71 (71\%)}$

Summary of Metrics:

- Accuracy = **75%**
- Error Rate = **25%**
- Precision = **67%**

- Recall (Sensitivity) = **75%**
- Specificity = **75%**
- F1 Score = **71%**

	Predicted Positive	Predicted Negative
Actual Positive	30 TP	10 FN
Actual Negative	15 FP	45 TN

Model Complexity