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Statistical Computing Practical

The link to my Github repo: https://github.com/Mishka312/StatHonPrac1

Question 1

There are 2 methods to present the rows containing NA values. The first is to use the apply() function across all rows of the airquality dataframe.

```
# Method 1
airquality_na_ <- airquality[apply(is.na(airquality), 1, any), ]
head(airquality_na_)</pre>
```

```
Ozone Solar.R Wind Temp Month Day
5
              NA 14.3
6
      28
             NA 14.9
                        66
                               5
                                   6
                               5 10
10
      NA
             194 8.6
                        69
11
      7
              NA 6.9
                        74
                               5 11
                               5
25
      NA
              66 16.6
                        57
                                  25
26
             266 14.9
                               5
      NA
                        58
                                  26
```

The second method to get the same information is to use a for loop. The range in the for loop is 1 to 6 so that only the first 6 rows are displayed. The official way would be to have the following range '1:nrow(airquality)'.

```
# Method 2
for (i in 1:nrow(airquality)) {
  if (sum(is.na(airquality[i, ])) > 0) {
    print(airquality[i, ])
  }
}
```

```
Ozone Solar.R Wind Temp Month Day
NA NA 14.3 56 5 5
```

Ozone Solar.R Wind Temp Month Day NA 14.9 66 5 Ozone Solar.R Wind Temp Month Day 194 8.6 69 5 10 NA Ozone Solar.R Wind Temp Month Day 11 7 NA 6.9 74 5 11 Ozone Solar.R Wind Temp Month Day 66 16.6 NA 57 5 25 Ozone Solar.R Wind Temp Month Day 26 NA 266 14.9 58 5 26 Ozone Solar.R Wind Temp Month Day 27 NA NA 8 57 5 27 Ozone Solar.R Wind Temp Month Day 32 NA 286 8.6 78 6 1 Ozone Solar.R Wind Temp Month Day 287 9.7 74 6 2 NA Ozone Solar.R Wind Temp Month Day NA 242 16.1 67 6 Ozone Solar.R Wind Temp Month Day 186 9.2 NA 84 6 Ozone Solar.R Wind Temp Month Day 220 8.6 85 6 5 NA Ozone Solar.R Wind Temp Month Day 37 NA 264 14.3 79 6 6 Ozone Solar.R Wind Temp Month Day 273 6.9 87 6 8 39 NA Ozone Solar.R Wind Temp Month Day 42 NA 259 10.9 93 6 11 Ozone Solar.R Wind Temp Month Day 250 9.2 92 43 NA 6 12 Ozone Solar.R Wind Temp Month Day NA 332 13.8 80 6 14 Ozone Solar.R Wind Temp Month Day 322 11.5 79 Ozone Solar.R Wind Temp Month Day NA 150 6.3 77 6 21 Ozone Solar.R Wind Temp Month Day 59 1.7 76 6 22 Ozone Solar.R Wind Temp Month Day NA 91 4.6 76 Ozone Solar.R Wind Temp Month Day 250 6.3 NA 76 6 24 Ozone Solar.R Wind Temp Month Day 56 NA 135 8 75 6 25 Ozone Solar.R Wind Temp Month Day 57 NA 127 8 78 6 26

	Ozone	Solar.R	Wind	Temp	Month	Dav
58	NA					
		Solar.R				
59	NA			-	6	•
	Ozone	Solar.R			Month	Day
60	NA	31				
	Ozone	Solar.R	Wind	Temp	Month	Day
61	NA	138	8	83	6	30
	Ozone	${\tt Solar.R}$	Wind	Temp	Month	Day
65	NA	101	10.9	84	7	4
	Ozone	${\tt Solar.R}$	Wind	Temp	${\tt Month}$	Day
72	NA	139	8.6	82	7	11
		${\tt Solar.R}$				
75		291				
	Ozone	${\tt Solar.R}$	Wind	Temp	Month	Day
83		258				
		${\tt Solar.R}$		-		•
84		295				
		${\tt Solar.R}$		-		•
96		NA				
		${\tt Solar.R}$				
97		NA				
		Solar.R		_		-
98		NA				
		e Solar.F				
102		222				
100		e Solar.F				-
103	NA					3 11
105	Uzone	e Solar.F				
107						3 15
115		e Solar.F				-
115		A 255				3 23
110		e Solar.F				
119						
150		e Solar.F				
19() IN F	145	13.2	2 //	٤	0 21

Question 2

To calculate the average temperature and ozone levels, the NA values need to first be removed. Thereafter, the means are calculated. The average temperature and ozone levels are 77.87 and 42. 13 respectively.

```
mean_Temp mean_Ozone
1 77.87069 42.12931
```

Question 3

A linear regression model was fitted to the data manually and the beta values retrieved. These were -17.58 and 3.92 respectively.

```
X <- as.matrix(cbind(rep(1, nrow(cars)), cars[, 1]))
Y <- as.matrix(cars[, 2])

beta <- solve(t(X) %*% X) %*% t(X) %*% Y
beta

[,1]
[1,] -17.579095
[2,] 3.932409</pre>
```

Question 4

A linear model was once again fitted to the data, this time with R's built in lm() function. The output of this proves that manually fitting a regression model yields the same beta coefficients.

cars

```
speed dist
1
        4
              2
2
            10
3
        7
             4
        7
4
            22
5
        8
            16
6
            10
7
       10
            18
8
       10
            26
9
       10
            34
10
       11
            17
11
       11
            28
12
       12
            14
13
       12
            20
14
       12
            24
15
       12
            28
16
       13
            26
17
       13
            34
18
       13
            34
19
       13
            46
20
       14
            26
21
       14
            36
22
       14
            60
```

```
23
     14
         80
24
     15
         20
25
     15
         26
26
     15
         54
27
     16
         32
28
     16
         40
29
    17
         32
30
    17
         40
31
     17
         50
32
     18
         42
33
     18
         56
     18
34
         76
35
     18
         84
36
     19
         36
37
    19
         46
38
     19
         68
39
     20
         32
40
     20
         48
41
     20
         52
42
     20
         56
43
     20
         64
44
     22
        66
45
     23
        54
46
    24 70
47
     24
        92
48
    24
        93
49
     24 120
50
     25 85
```

```
cars_model <- lm(dist ~ speed, cars)
#cars_model <- lm(speed ~ dist, cars)
summary(cars_model)</pre>
```

Call:

```
lm(formula = dist ~ speed, data = cars)
```

Residuals:

```
Min 1Q Median 3Q Max -29.069 -9.525 -2.272 9.215 43.201
```

Coefficients:

```
Estimate Std. Error t value Pr(>|t|)
(Intercept) -17.5791 6.7584 -2.601 0.0123 *
speed 3.9324 0.4155 9.464 1.49e-12 ***
```

```
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Residual standard error: 15.38 on 48 degrees of freedom Multiple R-squared: 0.6511, Adjusted R-squared: 0.6438 F-statistic: 89.57 on 1 and 48 DF, p-value: 1.49e-12

The beta coefficients output by the lm() function are the same as those produced using the matrix calculations.

Prac 3: Tidyverse

The tidyverse packages and the flights data sets need to be imported.

Below are 2 methods to display the flights dataset

head(flights)

```
# A tibble: 6 x 19
  year month day dep_time sched_dep_time dep_delay arr_time sched_arr_time
                                           <dbl> <int>
 <int> <int> <int> <int>
                                <int>
                                                                 <int>
1 2013
       1
                     517
                                                                   819
         1
2 2013
                                   529
                                              4
                1
                      533
                                                    850
                                                                  830
3 2013
          1
                1
                      542
                                    540
                                              2
                                                    923
                                                                   850
4 2013
         1
                1
                      544
                                    545
                                              -1
                                                    1004
                                                                  1022
5 2013
                1
                      554
                                    600
                                              -6
                                                     812
                                                                  837
                                                                  728
6 2013
                1
                      554
                                    558
                                              -4
                                                     740
```

#alternatively glimpse(flights) could be used.

[#] i 11 more variables: arr_delay <dbl>, carrier <chr>, flight <int>,

tailnum <chr>, origin <chr>, dest <chr>, air_time <dbl>, distance <dbl>,

hour <dbl>, minute <dbl>, time_hour <dttm>

18CHAPTER 7. BELOW ARE 2 METHODS TO DISPLAY THE FLIGHTS DATASET

Reducing base r code using dplyr

The 10 lines of code below makes use of dplyr functions. Doing the equivalent using base R functions required approximately 18 lines of code, almost double the dplyr code amount.

The code below yields the average and standard deviation of distance for each carrier. Furthermore, the mean distance is arranged ascendingly. This shows that carrier YV has the lowest average distance.

A tibble: 16 x 3

	carrier	mean_distance	sd_distance
	<chr></chr>	<dbl></dbl>	<dbl></dbl>
1	YV	229	0
2	9E	476.	334.
3	EV	522.	294.
4	US	536.	553.
5	MQ	566.	223.
6	FL	691.	142.
7	00	733	NA
8	WN	942.	496.
9	B6	1062.	681.
10	DL	1220.	644.
11	AA	1350.	626.
12	UA	1462.	778.
13	F9	1620	0
14	AS	2402	0
15	VX	2495.	98.2
16	HA	4983	0

Reasons for perculiar standard deviation entries

Some values were NA and 0. This can be explained by looking at the number and types of entries that this calculation is based on.

Carrier OO has a NA value for its standard deviation since it there is only one value. R, by default, considers the 0 sd of a single element.

The other carriers (AS, F9, HA and YV) have more than one entry. However, all entries are of the same value. Hence, The standard deviation is 0.

```
# A tibble: 1 x 1
  distance
     <dbl>
    2402
flights %>%
  filter(month == 1,
        carrier == "F9") %>%
 select(distance) %>%
 distinct()
# A tibble: 1 x 1
  distance
    <dbl>
1 1620
flights %>%
 filter(month == 1,
        carrier == "HA") %>%
 select(distance) %>%
distinct()
# A tibble: 1 x 1
  distance
     <dbl>
     4983
flights %>%
  filter(month == 1,
        carrier == "YV") %>%
 select(distance) %>%
 distinct()
# A tibble: 1 x 1
  distance
    <dbl>
     229
1
```

Carriers along columns

To have carriers along the columns, the pivot_wider function is required. Although this may be helpful in some scenarios, there are an excessive amount of NA values embedded within the new, tranformed data frame.

```
flights %>%
  pivot_wider(names_from = carrier, values_from = flight)
```

A tibble: 336,776 x 33

	year	${\tt month}$	day	${\tt dep_time}$	${\tt sched_dep_time}$	${\tt dep_delay}$	${\tt arr_time}$	${\tt sched_arr_time}$
	<int></int>	<int></int>	<int></int>	<int></int>	<int></int>	<dbl></dbl>	<int></int>	<int></int>
1	2013	1	1	517	515	2	830	819
2	2013	1	1	533	529	4	850	830
3	2013	1	1	542	540	2	923	850
4	2013	1	1	544	545	-1	1004	1022
5	2013	1	1	554	600	-6	812	837
6	2013	1	1	554	558	-4	740	728
7	2013	1	1	555	600	-5	913	854
8	2013	1	1	557	600	-3	709	723
9	2013	1	1	557	600	-3	838	846
10	2013	1	1	558	600	-2	753	745

[#] i 336,766 more rows

[#] i 25 more variables: arr_delay <dbl>, tailnum <chr>, origin <chr>,

[#] dest <chr>, air_time <dbl>, distance <dbl>, hour <dbl>, minute <dbl>,

[#] time_hour <dttm>, UA <int>, AA <int>, B6 <int>, DL <int>, EV <int>,

[#] MQ <int>, US <int>, WN <int>, VX <int>, FL <int>, AS <int>, `9E` <int>,

[#] F9 <int>, HA <int>, YV <int>, 00 <int>

Proportion of flights

The proportion of flights that experienced a departure delay but not an arrival delay can be calculated by first filtering for flights where dep_delay > 0 and arr_delay < 1. Thereafter, this number of flights should be divided by the total number of flights. Approximately 10.5% of flights recover from their departure delay.

n 1 0.1052391

Using the flights and airlines datasets together

To identify routes, one considers the origin and destination. Then count the total number of unique airlines (carriers) use this route, and filter for routes that support more than one carrier.

```
##origin and destination
airlines
```

```
# A tibble: 16 x 2
   carrier name
   <chr> <chr>
 1 9E
           Endeavor Air Inc.
 2 AA
           American Airlines Inc.
 3 AS
           Alaska Airlines Inc.
 4 B6
           JetBlue Airways
           Delta Air Lines Inc.
 5 DL
 6 EV
           ExpressJet Airlines Inc.
 7 F9
           Frontier Airlines Inc.
 8 FL
           AirTran Airways Corporation
 9 HA
           Hawaiian Airlines Inc.
10 MQ
           Envoy Air
11 00
           SkyWest Airlines Inc.
12 UA
           United Air Lines Inc.
13 US
           US Airways Inc.
14 VX
           Virgin America
15 WN
           Southwest Airlines Co.
16 YV
           Mesa Airlines Inc.
```

flights

```
# A tibble: 336,776 x 19
                 day dep_time sched_dep_time dep_delay arr_time sched_arr_time
    year month
   <int> <int> <int>
                        <int>
                                       <int>
                                                  <dbl>
                                                           <int>
                                                                          <int>
 1 2013
                                         515
                                                     2
                                                             830
                   1
                          517
                                                                            819
 2 2013
                   1
                          533
                                         529
                                                      4
                                                             850
                                                                            830
             1
                                                      2
 3 2013
             1
                   1
                          542
                                         540
                                                             923
                                                                            850
 4 2013
                   1
                          544
                                         545
                                                     -1
                                                            1004
                                                                           1022
             1
5 2013
                   1
                          554
                                         600
                                                     -6
                                                             812
                                                                            837
 6 2013
                          554
                                         558
                                                     -4
                                                             740
                                                                            728
             1
                   1
 7 2013
                   1
                          555
                                         600
                                                     -5
                                                             913
                                                                            854
8 2013
                                         600
                                                     -3
             1
                   1
                          557
                                                             709
                                                                            723
9 2013
                          557
                                         600
                                                     -3
                                                             838
                                                                            846
                                                                            745
10 2013
                          558
                                         600
                                                     -2
                                                             753
             1
                   1
# i 336,766 more rows
```

- # i 11 more variables: arr_delay <dbl>, carrier <chr>, flight <int>,
- tailnum <chr>, origin <chr>, dest <chr>, air_time <dbl>, distance <dbl>,
- hour <dbl>, minute <dbl>, time_hour <dttm>

```
common routes <- flights %>%
  group_by(origin, dest, carrier) %>%
  summarise(flight_count = n(), .groups = 'drop') %>%
  group_by(origin, dest) %>%
  summarise(unique_carriers = n_distinct(carrier), .groups = 'drop') %>%
  filter(unique_carriers > 1)
common_routes
```

```
# A tibble: 128 x 3
   origin dest unique_carriers
   <chr> <chr>
                          <int>
 1 EWR
          ATL
                               4
                               2
 2 EWR
          AUS
 3 EWR
          BDL
 4 EWR
                               2
          BNA
 5 EWR
          BOS
                               3
                              2
 6 EWR
          BWI
                              2
 7 EWR
          CHS
                              2
8 EWR
          CLE
9 EWR
          CLT
                              3
                              2
10 EWR
          CVG
```

i 118 more rows

The carrier_routes output shows the average delay per carrier per route. the full airline names are also included by using the left_join() function.

```
carrier_routes <- flights %>%
 right_join(common_routes, by = c("origin", "dest")) %>%
 group_by(origin, dest, carrier) %>%
 summarise(mean_arr_del = mean(arr_delay, na.rm = T), .groups = "keep") %>%
 drop_na() %>%
 ungroup() %>%
 left_join(airlines, by = "carrier")
carrier_routes
# A tibble: 342 x 5
  origin dest carrier mean_arr_del name
  <chr> <chr> <chr>
                             <dbl> <chr>
                              -6.25 Endeavor Air Inc.
 1 EWR
         ATL
               9E
2 EWR
         ATL
               DL
                              10.0 Delta Air Lines Inc.
3 EWR
         ATL EV
                             19.5 ExpressJet Airlines Inc.
 4 EWR
         ATL
              UA
                             10.5 United Air Lines Inc.
5 EWR
         AUS
              UA
                              4.28 United Air Lines Inc.
         AUS
 6 EWR
              WN
                             -11.2 Southwest Airlines Co.
7 EWR
         BDL
               EV
                               6.78 ExpressJet Airlines Inc.
8 EWR
         BDL
               UA
                              22.6 United Air Lines Inc.
                              17.7 ExpressJet Airlines Inc.
9 EWR
         BNA
               ΕV
10 EWR
         BNA
                              -2.13 Southwest Airlines Co.
```

i 332 more rows

30CHAPTER~12.~USING~THE~FLIGHTS~AND~AIRLINES~DATASETS~TOGETHER

Identifying inconsistencies

By using the unique function, all unique entries in the data frame are displayed. This brings light to mispellings and other typographical and data-related errors. The output shows that there are 3 unique entries for gender. One, 'femal' is a typing error.

Disease status has 3 unique entries, however, 2 are equivalent. These are "healthy" and "Healthy". They are considered unique since R is case sensitive.

```
erroneous_df %>%
 apply(2, unique)
$id
 [1] "id_1" "id_2" "id_3" "id_4" "id_5" "id_6" "id_7" "id_8" "id_9"
[10] "id_10" "id_11" "id_12" "id_13" "id_14" "id_15" "id_16" "id_17" "id_18"
[19] "id_19" "id_20" "id_21" "id_22" "id_23" "id_24" "id_25" "id_26" "id_27"
[28] "id_28" "id_29" "id_30" "id_31" "id_32" "id_33" "id_34" "id_35" "id_36"
[37] "id_37" "id_38" "id_39" "id_40" "id_41" "id_42" "id_43" "id_44" "id_45"
[46] "id_46" "id_47" "id_48" "id_49" "id_50"
$age
[1] "50" "34" "70" "33" "22" "61" "69" "73" "62" "56" "71" "44" "45" "46" "24"
[16] "76" "47" "28" "48" "54" "27" "26" "38" "55" "36" "58" "72" "31" "51" "64"
[31] "60" "29" "42" "79"
$gender
[1] "male"
            "female" "femal"
$height
 [1] "174.4" "197.7" "174.1" "194.5" NA "180.4" "170.5" "157.4" "196.8"
[10] "165.1" "153.0" "197.4" "186.0" "157.1" "177.5" "179.3" "170.2" "182.4"
```

[1] "master"

"bachelor"

"PhD"

"highschool"

```
[19] "165.4" "161.0" "168.5" "199.2" "157.7" "154.6" "184.5" "181.0" "194.6"
[28] "183.6" "186.9" "176.1" "183.0" "191.1" "189.3" "199.0" "172.0" "165.6"
[37] "150.5" "159.2" "192.1" "161.6" "162.0" "153.8" "162.3" "186.6" "192.4"
[46] "174.9"
$weight
[1] "69.4" "62.3" "55.6" "69.5" "78.6" "60.8" "72.2" "60.9" "75.1" "67.7"
[11] "82.5" "68.7" "67.8" "76.7" "87.0" "61.1" "70.6" "63.3" "81.5" "59.2"
[21] "93.2" "87.3" "83.4" "80.9" "68.6" "76.5" "93.7" "79.1" "92.0" "65.6"
[31] "85.4" "79.7" "74.1" "78.2" "95.7" "95.1" "63.7" "66.1" "99.3" "81.0"
[41] "96.9" "73.3" "70.3" "83.0" "57.6" "61.9" "98.1"
$blood_type
[1] "O" "A" "B" "AB"
$disease_status
[1] "diseased" "healthy" "Healthy"
$cholesterol
[1] "228" "223" "213" "198" "166" "151" "195" "199" "189" "196" "221" "156"
[13] "185" "230" "234" "174" "236" "235" "180" "165" "220" "160" "153" "250"
[25] "184" "242" "212" "179" "224" "233" "181" "214" "248" "191" "162" "203"
[37] "173" "187" "164" "247"
$glucose
[13] " 88" "109" " 71" " 90" " 94" " 87" "113" " 93" " 97" "118" " 99" "108"
[25] " 89" "116" " 79" " 84" " 75" " 81" "106" " 82" " 76" "120"
$smoker
[1] "yes" "no"
$exercise
[1] "occasional" "regular"
                             "none"
$income
[1] "84820" "81547" "22588" "72490" "74533" "25338" "41469" "57315" "63629"
[10] "88662" "62615" "56261" "58499" "82232" "77584" "77275" "38468" "54510"
[19] "91326" "78611" "31402" "29586" "21441" "58269" "84173" "88295" "37940"
[28] "43750" "69750" "92356" "82518" "91455" "68866" "51178" "68275" "27689"
[37] "35418" "81318" "62405" "86851" "25654" "47553" "74474" "51409" "22607"
[46] "55360" "96351" "21516" "41927" "55810"
$education
```

```
$region
[1] "North" "South" "West" "East"

$marital_status
[1] "divorced" "single" "married" "widowed"
```

The following output shows that all columns are of equal length.

```
erroneous_df %>%
  apply(2, length)
```

id	age	gender	height	weight
50	50	50	50	50
blood_type	disease_status	cholesterol	glucose	smoker
50	50	50	50	50
exercise	income	education	region	marital_status
50	50	50	50	50

The following output shows that all rows are of equal length.

```
erroneous_df %>%
apply(1, length)
```

The following code gives the indices of all the NA values.

```
NA_positions <- which(is.na(erroneous_df), arr.ind = TRUE)</pre>
```

Prac 2: Lowess algorithm

Generating simulated data

```
set.seed(1)
x \leftarrow seq(1, 100, 1)
e \leftarrow rnorm(100, mean = 0, sd = 0.2)
y < -\sin(x / 10) + e
f = 2/3
dists <- dist(x)</pre>
dists_m <- as.matrix(dists)</pre>
y_hat <- numeric(length(x))</pre>
#eval=FALSE
k <- ceiling(f*length(x))</pre>
w <- numeric(k)
for (i in 1:length(x)) {
  ifelse(k\%2==0,
          neighbs_dist <- dists_m[i, c(floor(i - (k)/2): ceiling(i + k- (k)/2))],
          neighbs_dist <- dists_m[i, c(floor(i - (k+1)/2): ceiling(i + k- (k+1)/2))])
  ifelse(k\%\%2==0,
          x_{\text{neighbs}} \leftarrow c(floor(i - (k)/2): ceiling(i + k - (k)/2)),
          \label{eq:condition} $$x_neighbs \leftarrow c(floor(i - (k+1)/2): ceiling(i + k- (k+1)/2)))$
```

```
y_neighbs <- x[c(x_neighbs)]

x_and_dist <- cbind(x_neighbs, neighbs_dist)

for (j in i:length(neighbs_dist)) {
    W <- diag(((abs(neighbs_dist)/max(neighbs_dist))**3)**3)
}

betas <- solve(t(x_neighbs) %*% W %*% (x_neighbs)) %*% t(x_neighbs) %*% W %*% (y_neighbs)

y_hat[i] <- betas[1] +betas[2] * x[i]</pre>
```

Implementing the Lowess algorithm

```
#eval = FALSE

customLowess <- function(x, y, f) {
   k <- ceiling(f*length(x))

   distances <- numeric(length(x) -1)
   closes <- numeric(k)

for (i in length(x)) {
   distances[i] <- x[i] - x[-i]
   sort(distances, decreasing = F)
   closest <- distances[1:k]
}</pre>
```

```
model2 <- lowess(x, y, iter = 0)
plot(model2$x, model2$y, main = "lowess smoothing result")</pre>
```

lowess smoothing result

