

DS 623 PE04

For PE04, you will execute a simple Gram-Schmidt Process in \mathbb{R}^2 . Your code in the Jupyter Notebook should have the following properties:

- 1) Input: two independent nonzero vectors v_1 and v_2 in \mathbb{R}^2 (i.e., two three-dimensional vectors)
- 2) Output:
 - a. $w_1: (w_1 = \frac{v_1}{\|v_1\|})$
 - b. $w_2: (w_2 = \frac{y_2}{\|y_2\|})$ where $y_2 = v_2 - (v_2 \cdot w_1)w_1$
- 3) Verification: verify w_1 and w_2
Have length 1 and the dot product of w_1 and w_2 are zero. (The length and dot product should be close to 1 and 0 respectively.)

For this assignment, you can use any NumPy and SciPy operations. Use three decimal places for non-integer values.

Example)

Enter v1: `np.array([2, 1])`

Enter v2: `np.array([-3, 0])`

Output:

Two orthonormal bases are found below.

w1 - `np.array([0.894, 0.447])`,

w2 - `np.array([-0.447, 0.894])`

Verification:

Length of w1 is 1.000

Length of w2 is 1.000

Dot product is 0.000

If you need more challenge, you can extend it to \mathbb{R}^3 using the following formulae.

- a. $w_3: (w_3 = \frac{y_3}{\|y_3\|})$ where $y_3 = v_3 - (v_3 \cdot w_1)w_1 - (v_3 \cdot w_2)w_2$