

## DS 623 PE03

For PE03, your code in the Jupyter Notebook should have the following properties:

- 1) Input:  $v_1$  and  $v_2$  in  $\mathbb{R}^3$  (i.e., two three-dimensional vectors)
- 2) Output:
  - a.  $l_1$  norm of  $v_1$ :
  - b.  $l_1$  norm of  $v_2$ :
  - c.  $l_1$  distance between  $v_1$  and  $v_2$ :
  - d. Triangular inequality:  $\|v_1\|_1 + \|v_2\|_1 \geq \|v_1+v_2\|_1$ ; True/False
    - Display the length of each vector  $v_1$ ,  $v_2$ , and  $v_1+v_2$  with inequality; display “True” if the triangular inequality holds.
  - e.  $l_2$  norm of  $v_1$ :
  - f.  $l_2$  norm of  $v_2$ :
  - g.  $l_2$  distance between  $v_1$  and  $v_2$ :
  - h. Triangular inequality:  $\|v_1\|_2 + \|v_2\|_2 \geq \|v_1+v_2\|_2$ ; True/False
    - Same as in d
  - i. (optional) Area of the parallelogram formed by  $v_1$  and  $v_2$  in  $L_2$ . (hint: area = base x height; you can get height using the property of dot product and  $\sin()$ .)

For this assignment, you can use any NumPy and SciPy operations. Use three decimal places for non-integer values.

Example)

Enter  $v_1$ : `np.array([2, 1, -3])`

Enter  $v_2$ : `np.array([-3, 0, 5])`

Output:

$l_1$  norm of  $v_1$ : 6

$l_1$  norm of  $v_2$ : 8

$l_1$  distance between  $v_1$  and  $v_2$ : 8

Triangular inequality:  $6 + 8 \geq 8$ ; True

$l_2$  norm of  $v_1$ : 3.742

$l_2$  norm of  $v_2$ : 5.831

$l_2$  distance between  $v_1$  and  $v_2$ : 5.477

Triangular inequality:  $3.742 + 5.831 \geq 5.477$ ; True

Area of the parallelogram formed by  $v_1$  and  $v_2$  (in  $l_2$ ): 19.874