

7.

All filters are high pass.

∴ Transfer function of Butterworth high pass filter

$$\Rightarrow H_{HP}(u, v) = \frac{1}{1 + (D_0/D(u, v))^{2n}}$$

$\Rightarrow D_0 = \text{cut off frequency}$

$$\begin{aligned}\Rightarrow \text{Spatial kernel } h_{HP} &= \mathcal{F}^{-1}(H_{HP}(u, v)) \\ &= \mathcal{F}^{-1}(1 - H_{LP}(u, v)) \\ &= \delta(x, y) - h_{LP}(x, y)\end{aligned}$$

\Rightarrow due to presence of delta function there is spike at center.