### Question 4.

## **Analytical Proof**

$$\frac{4}{2} \int (x_{1}y) = \begin{cases} 0 & x \neq |0| \\ 255 & x = |0| \end{cases}$$

$$\therefore \int (x_{1}y) = 255 \delta(x - |0|)$$

$$F(u,v) = \iint \int (x_{1}y) e^{-\int 2x} (ux + vy) dx dy$$

$$= \iint 255 \delta(x - |0|) e^{-\int 2x} (ux + vy) dx dy$$

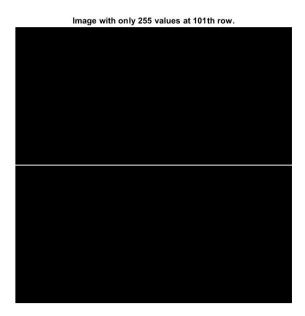
$$= \int 255 \delta(x - |0|) e^{-\int 2x} (ux + vy) dx dy$$

$$= \int 255 \delta(x - |0|) e^{-2\pi \int ux} dx \int e^{-\int 2x} dy$$

$$= 255 e^{-\int 2x + |0|} \chi \delta(v)$$

## Result from Matlab

## 1. Image



# 2. Frequency response

