# On Compositional safety verification with Max-SMT

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#### Overview

Introduction

2 Preliminaries

3 Example execution

#### **Terms**

## Safety verification

Prove that an assertion is always true at a location

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#### Non-compositional safety verification

Safety verification where the whole program is analyzed in one step

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#### Non-compositional safety verification

Safety verification where the whole program is analyzed in one step

#### Compositional safety verification

Safety verification where program parts are analyzed semi-independently and composed

#### Motivation

Scalability ← Loss in precision

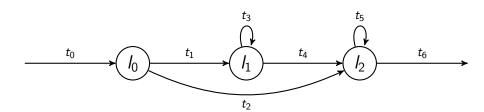
$$\mathcal{L} = \{\ell_0, \ell_1, \ell_2\}$$



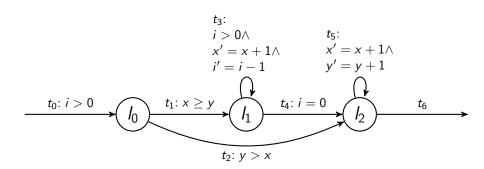




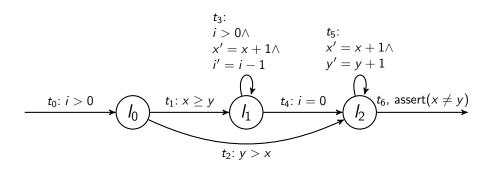
$$\mathcal{L} = \{\ell_0, \ell_1, \ell_2\}$$
 ,  $\mathcal{T} = \{t_i \mid i \in \{1, \dots, 6\}\}$ 



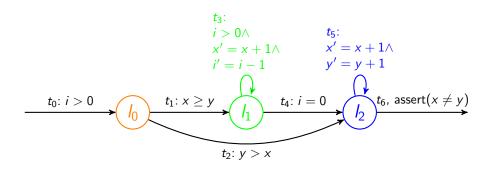
$$\mathcal{L}=\{\ell_0,\ell_1,\ell_2\}$$
 ,  $\mathcal{T}=\{t_i\mid i\in\{1,\dots,6\}\}$  ,  $\mathcal{V}=\{x,y,i\},~\mathcal{V}'=\{x',y',i'\}$ 



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#### CheckSafe

Prove that an assertion is satisfied by backtracking through all entry components



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#### CondSafe

Find a precondition for a component such that all runs satisfying the precondition always imply the postcondition



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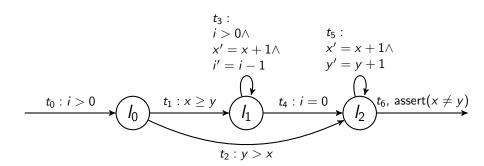
#### CondSafe

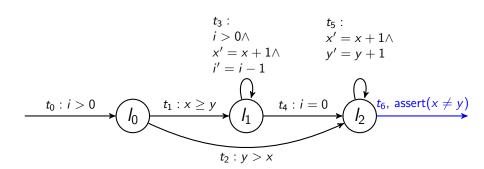
Find a precondition for a component such that all runs satisfying the precondition always imply the postcondition

#### Narrowing

Manipulate the program such that new preconditions can be found

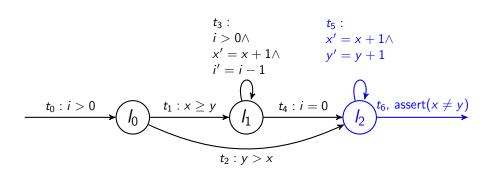
### Example program





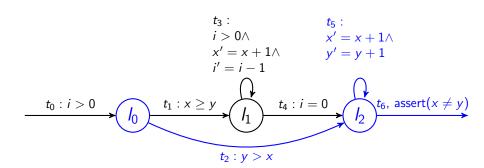
#### Task

Prove that the program is safe for  $x \neq y$  at  $t_6$ 



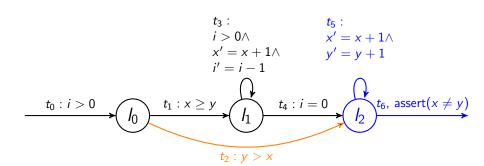
# CheckSafe on $\{\ell_2\}$ for $x \neq y$

 $t_6$  does not already imply  $x \neq y$   $t_6$  is not an initial transition Call CondSafe, get x > y as precondition



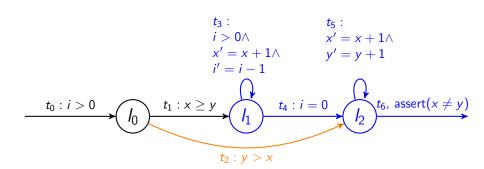
## CheckSafe on $\{\ell_0\}$ for x > y

 $t_2$  does not already imply x>y  $t_2$  is not an initial transition Call CondSafe



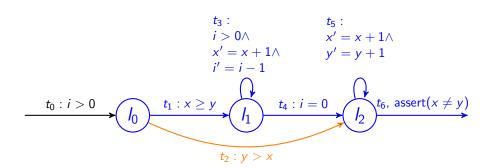
## CheckSafe on $\{\ell_0\}$ for x > y

No precondition, since y > x contradicts x > yPath is maybe safe, but not for x > y



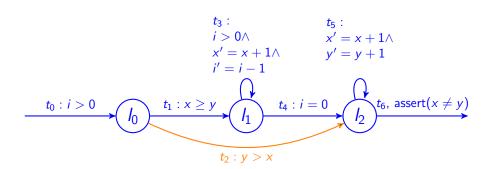
# CheckSafe on $\{\ell_1\}$ for x > y

 $t_4$  does not already imply x > y  $t_4$  is not an initial transition Call CondSafe, get  $i > 0 \land x > y$  as precondition



# CheckSafe on $\{\ell_0\}$ for i > 0

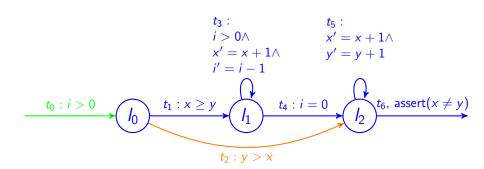
 $t_1$  does not already imply i > 0  $t_1$  is not an initial transition Call CondSafe, get i > 0 as precondition



#### CheckSafe on initial SCC for i > 0

 $t_0$  does already imply i > 0

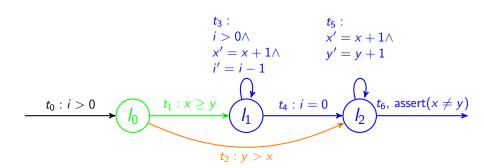




#### CheckSafe on initial SCC for i > 0

Path is safe for i > 0

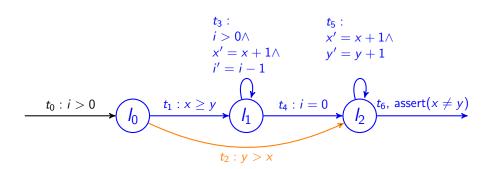




#### CheckSafe on $\{\ell_0\}$ for i > 0

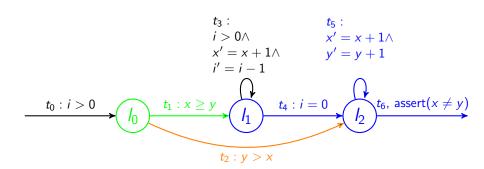
Path is safe for i > 0





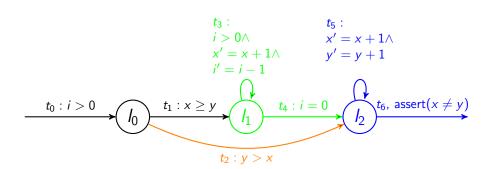
# CheckSafe on $\{\ell_0\}$ for $x \ge y$

 $t_1$  does already imply  $x \ge y$ 



## CheckSafe on $\{\ell_0\}$ for $x \ge y$

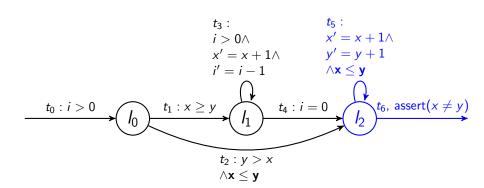
Path is safe for  $x \ge y$ 



#### CheckSafe on $\{\ell_1\}$ for x > y

Path is safe for x > y

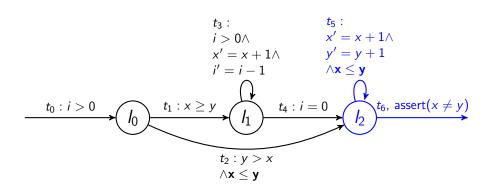




### Narrow on $\{\ell_2\}$

Add  $x \leq y$  to  $t_2$ 

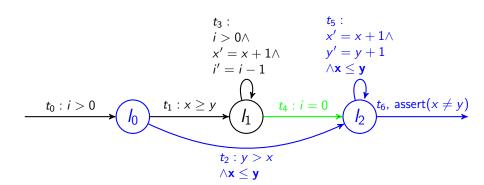
Add  $x \le y$  to  $t_5$ 



### CheckSafe on $\{\ell_2\}$ for $x \neq y$

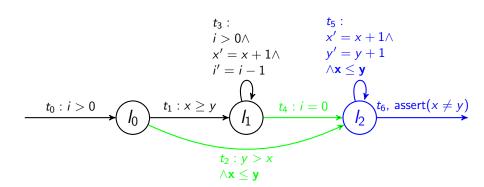
Call CondSafe, get y > x instead of x > y as precondition

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#### CheckSafe on $\{\ell_0\}$ for y > x

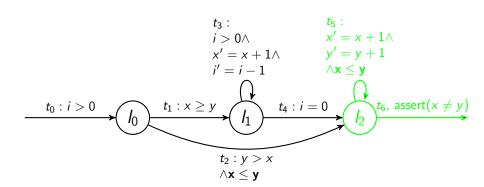
 $t_2$  does already imply y > x



#### CheckSafe on $\{\ell_0\}$ for y > x

Path is safe for y > x





#### CheckSafe on $\{\ell_0\}$ for y > x

Program is safe for  $x \neq y$ 



#### References



Brockschmidt, Marc and Larraz, Daniel and Oliveras, Albert and Rodriguez-Carbonell, Enric and Rubio, Albert (2015)

Compositional Safety Verification with Max-SMT

Proceedings of FMCAD'15

# The End