On Compositional safety verification with Max-SMT

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Overview

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14: **return** the result of a call to CheckSafe with a narrowed version

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10: **return** None

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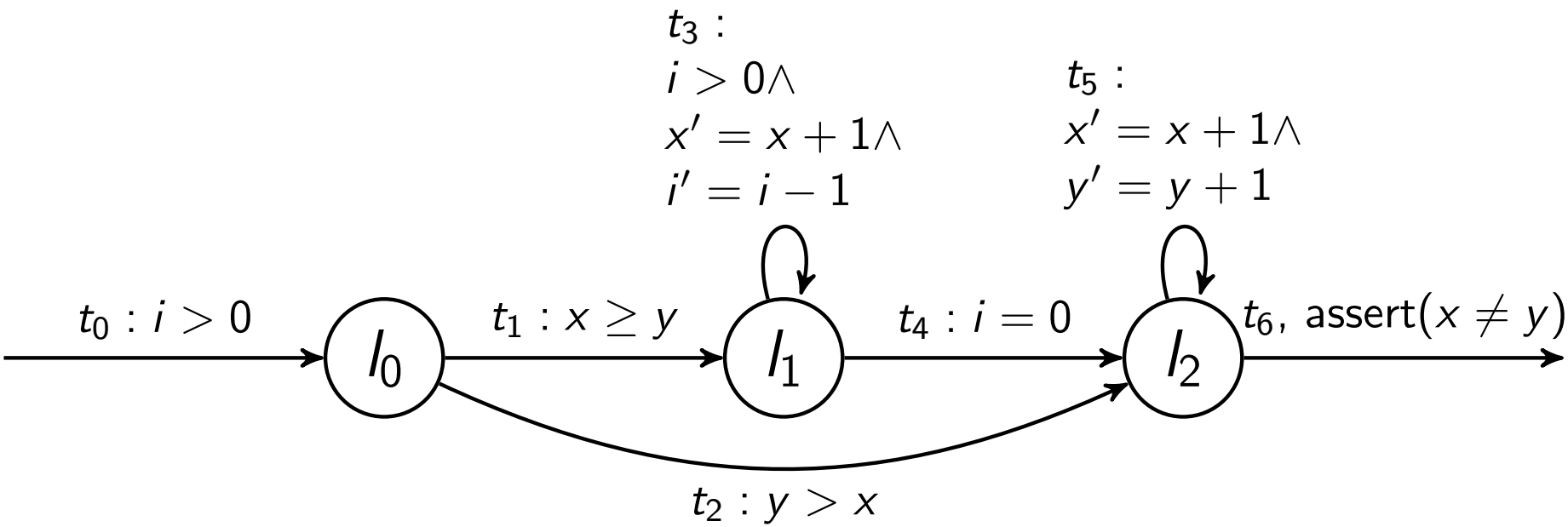
8: Add a conjunct with the negated CII at the end location to the transition

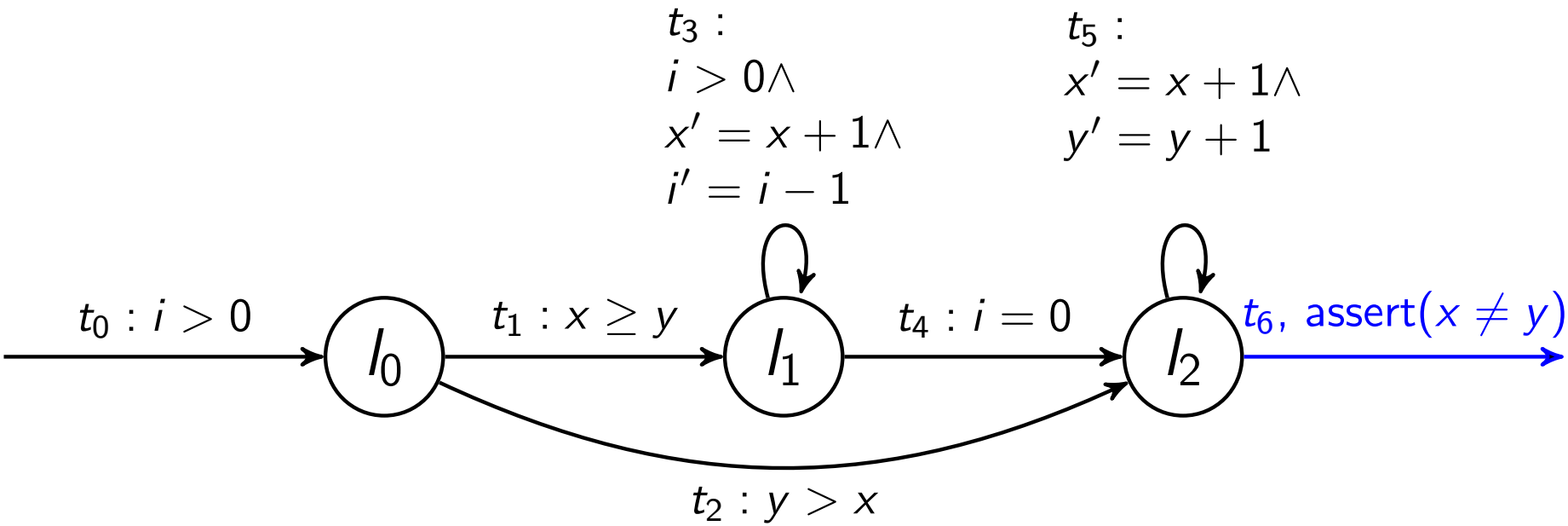
Example program

Program

$\mathcal{V} = \{x, y, i\}$, $\mathcal{L} = \{\ell_0, \ell_1, \ell_2\}$, $\mathcal{T} = \{t_i \mid i \in \{1, \ldots, 6\}\}$



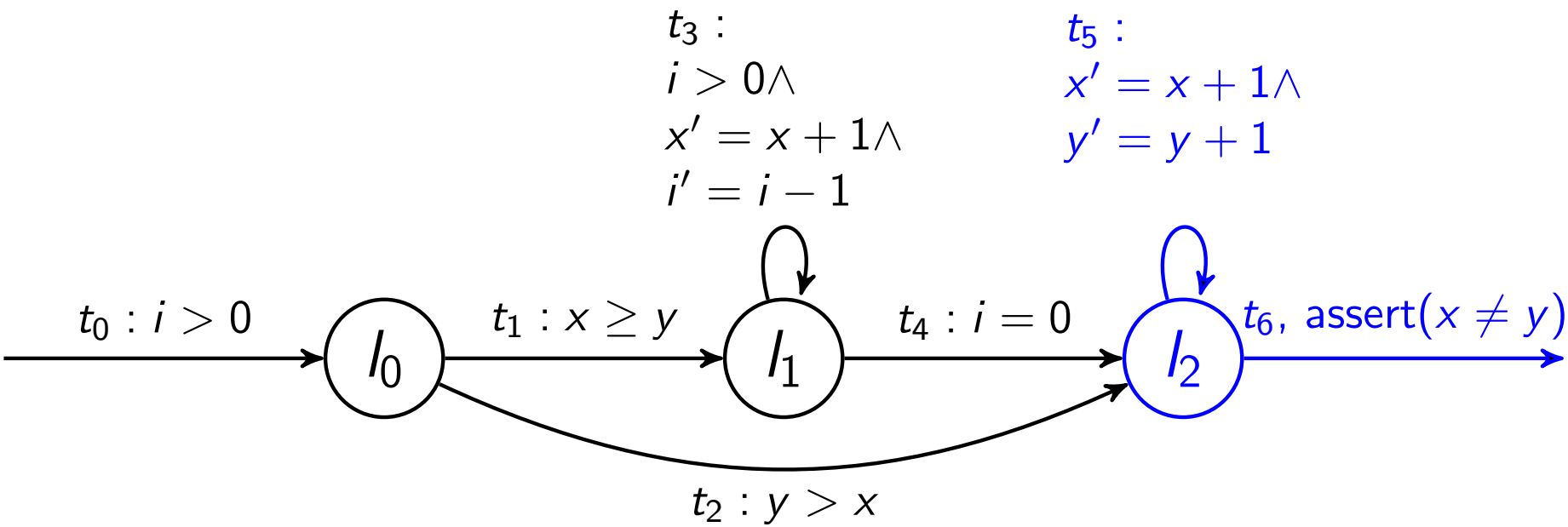
Example execution



Task

Prove that the program is safe for $x \neq y$ at t_6

Example execution



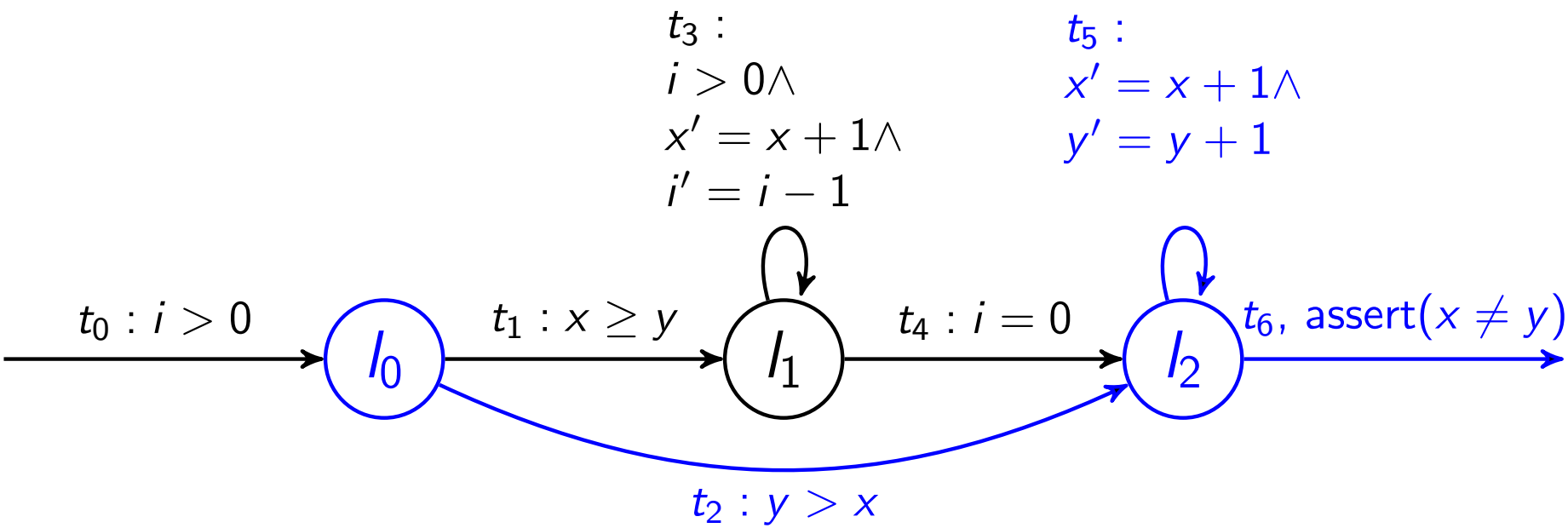
CheckSafe on $\{\ell_2\}$ for $x \neq y$

t_6 does not already imply $x \neq y$

t_6 is not an initial transition

Call CondSafe, get $x > y$ as precondition

Example execution



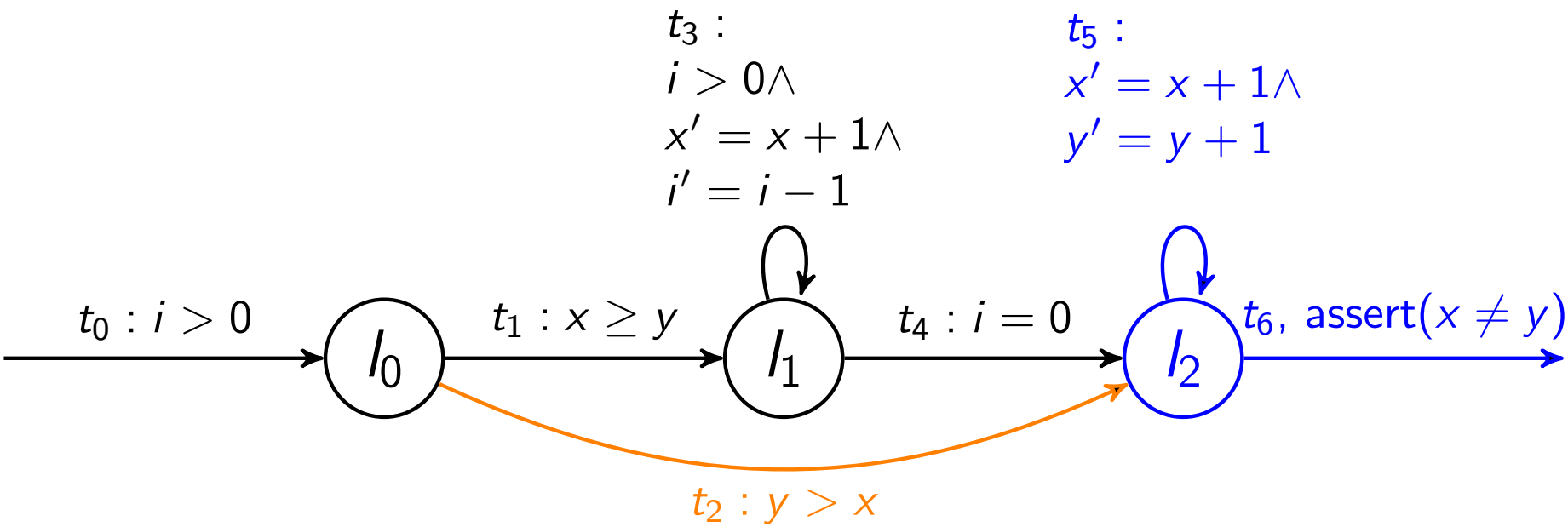
CheckSafe on $\{\ell_0\}$ for $x > y$

t_2 does not already imply $x > y$

t_2 is not an initial transition

Call CondSafe

Example execution

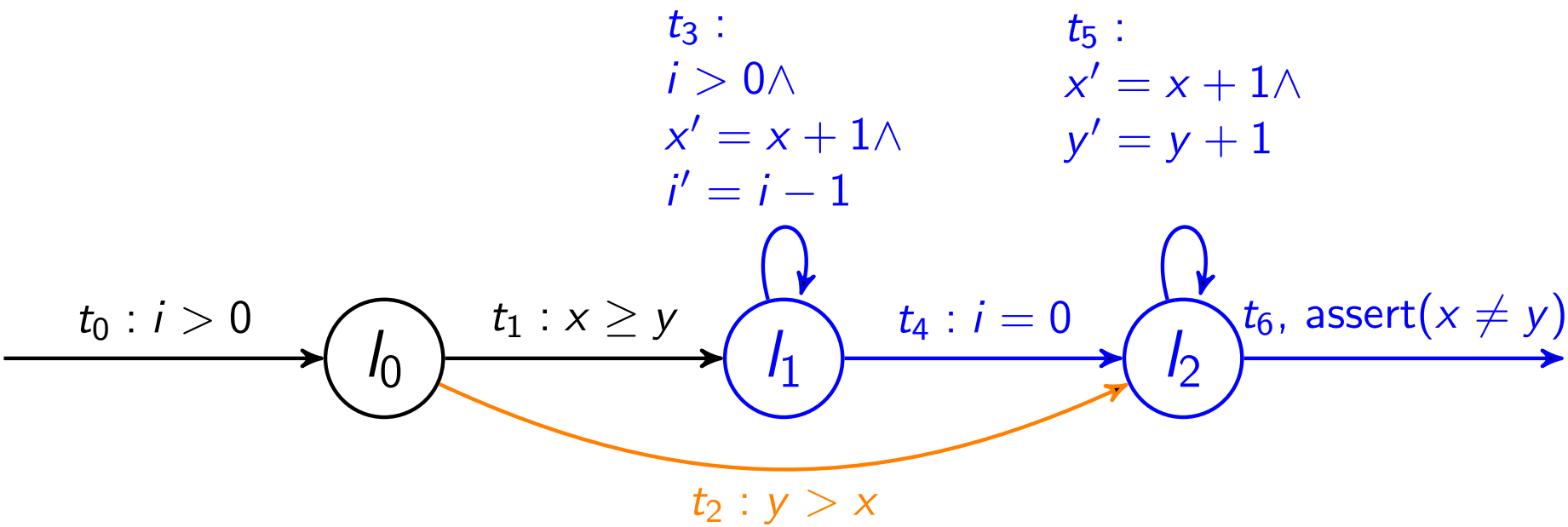


CheckSafe on $\{\ell_0\}$ for $x > y$

No precondition, since $y > x$ contradicts $x > y$

Path is maybe safe, but not for $x > y$

Example execution



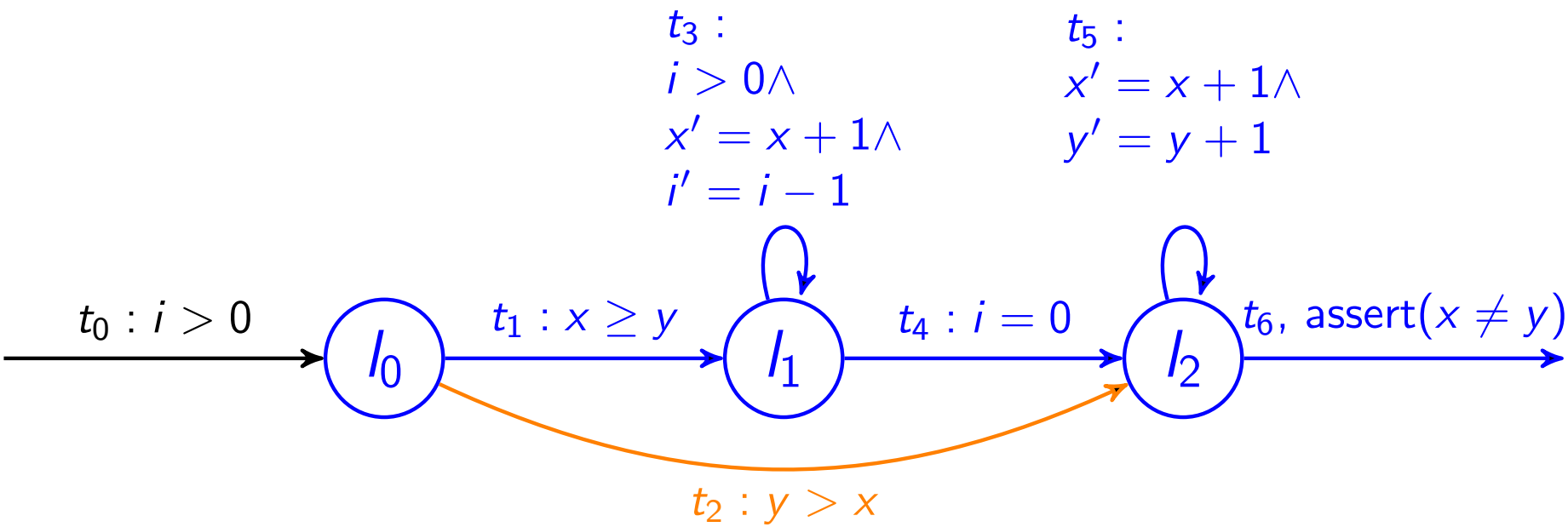
CheckSafe on $\{\ell_1\}$ for $x > y$

t_4 does not already imply $x > y$

t_4 is not an initial transition

Call CondSafe, get $i > 0 \wedge x \geq y$ as precondition

Example execution



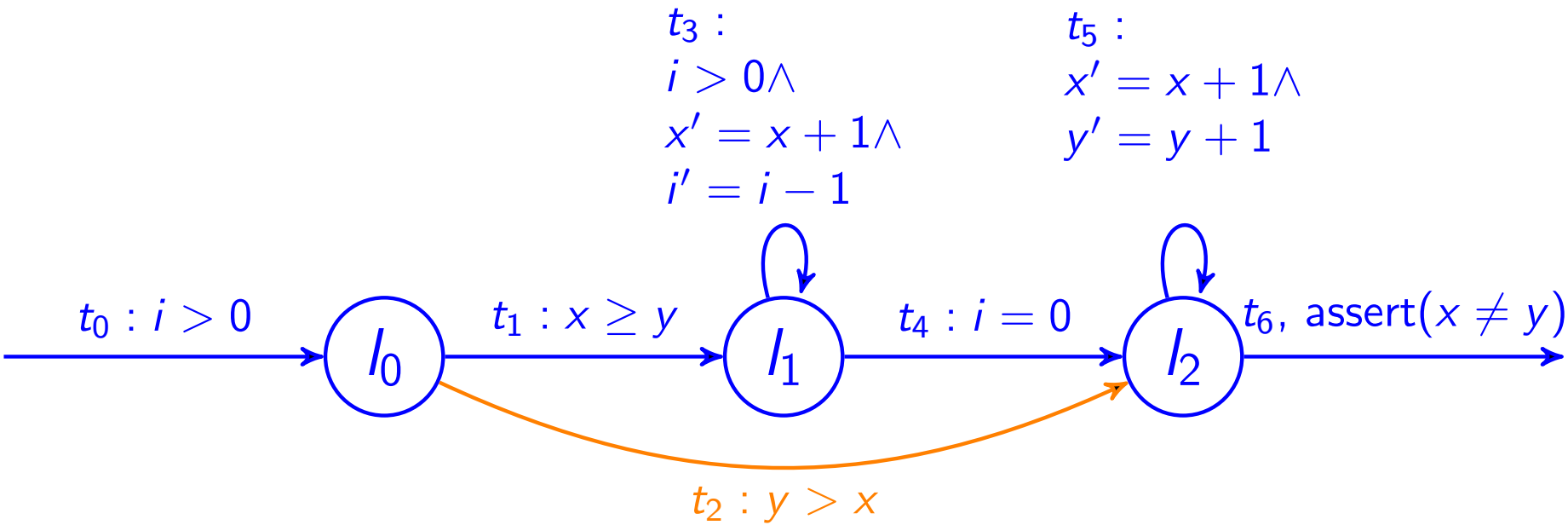
CheckSafe on $\{\ell_0\}$ for $i > 0$

t_1 does not already imply $i > 0$

t_1 is not an initial transition

Call CondSafe, get $i > 0$ as precondition

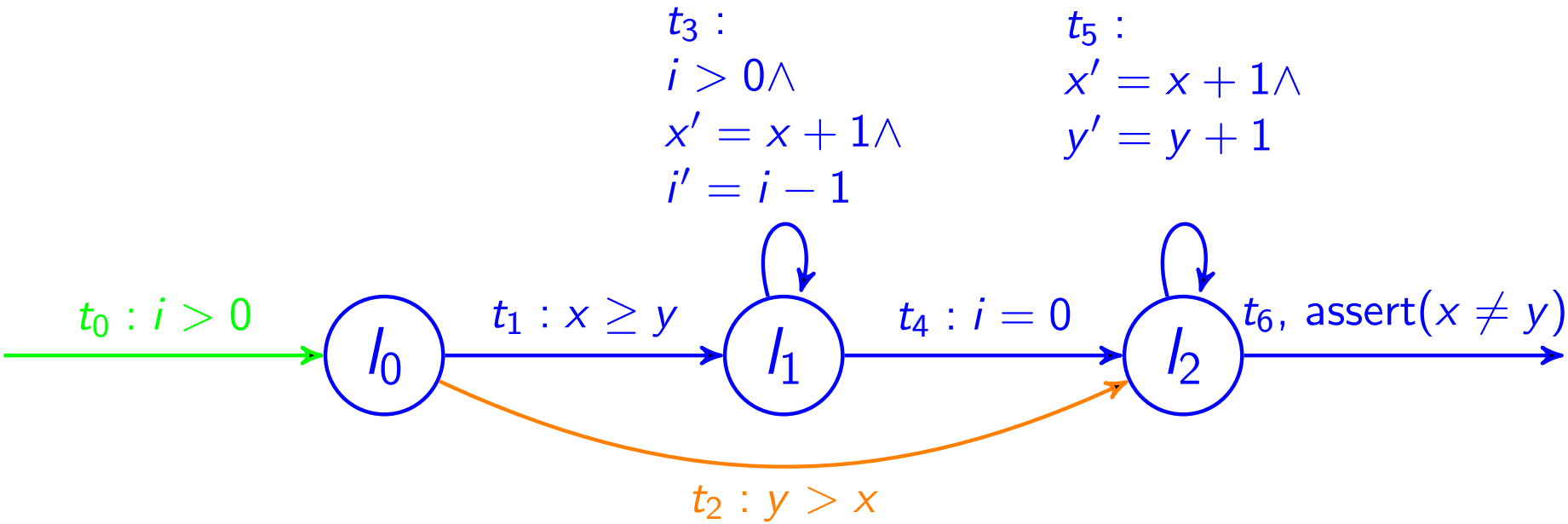
Example execution



CheckSafe on initial SCC for $i > 0$

t_0 does already imply $i > 0$

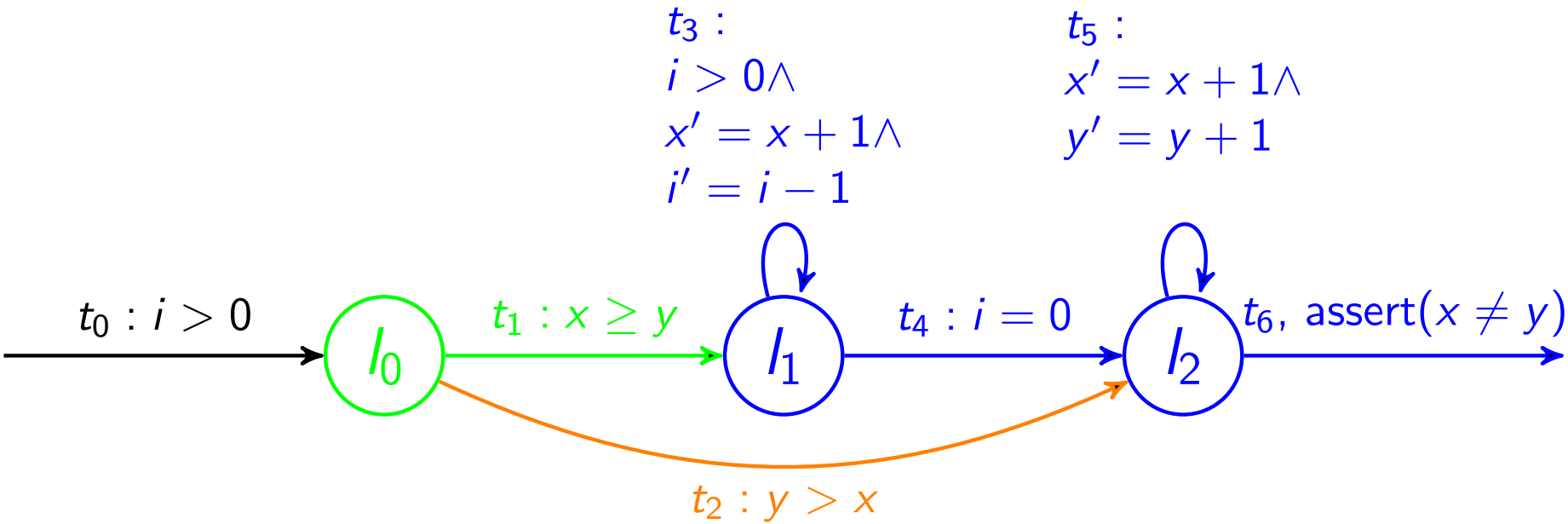
Example execution



CheckSafe on initial SCC for $i > 0$

Path is safe for $i > 0$

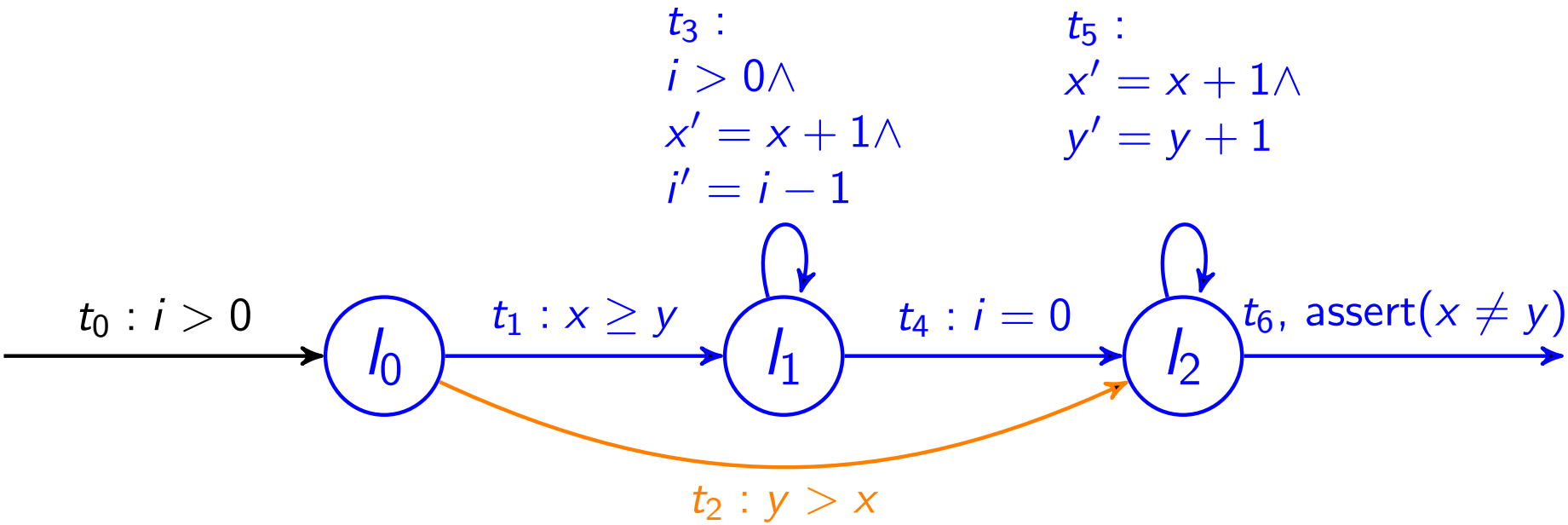
Example execution



CheckSafe on $\{\ell_0\}$ for $i > 0$

Path is safe for $i > 0$

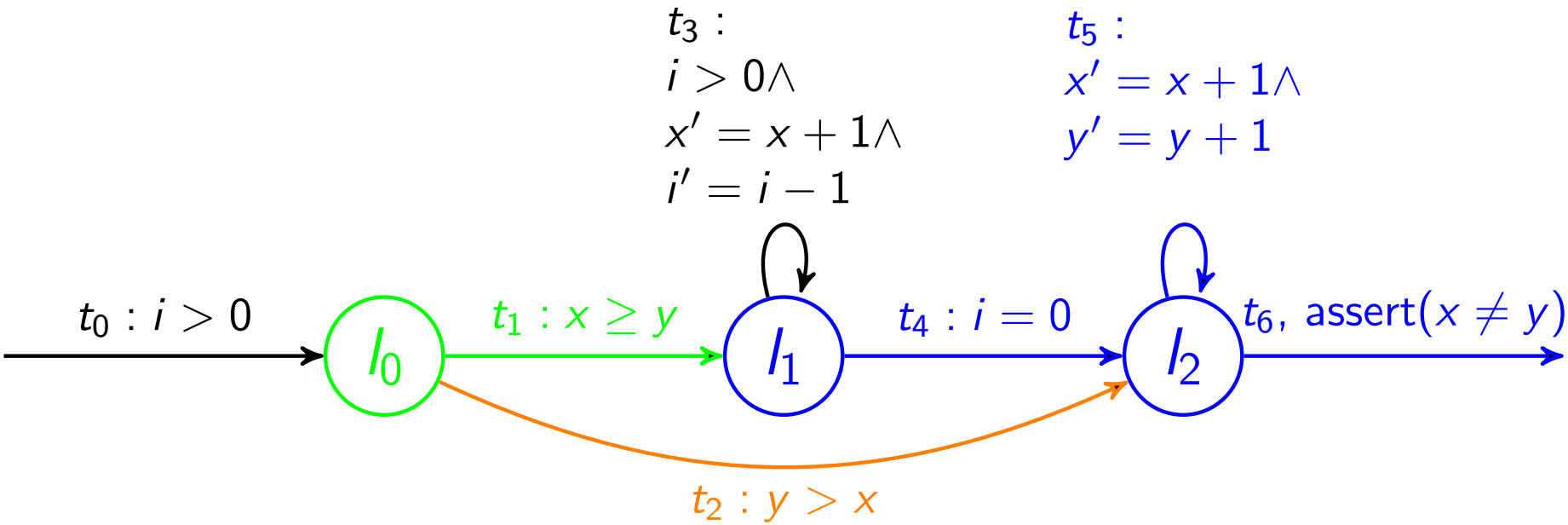
Example execution



CheckSafe on $\{\ell_0\}$ for $x \geq y$

t_1 does already imply $x \geq y$

Example execution



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Path is safe for $x \geq y$

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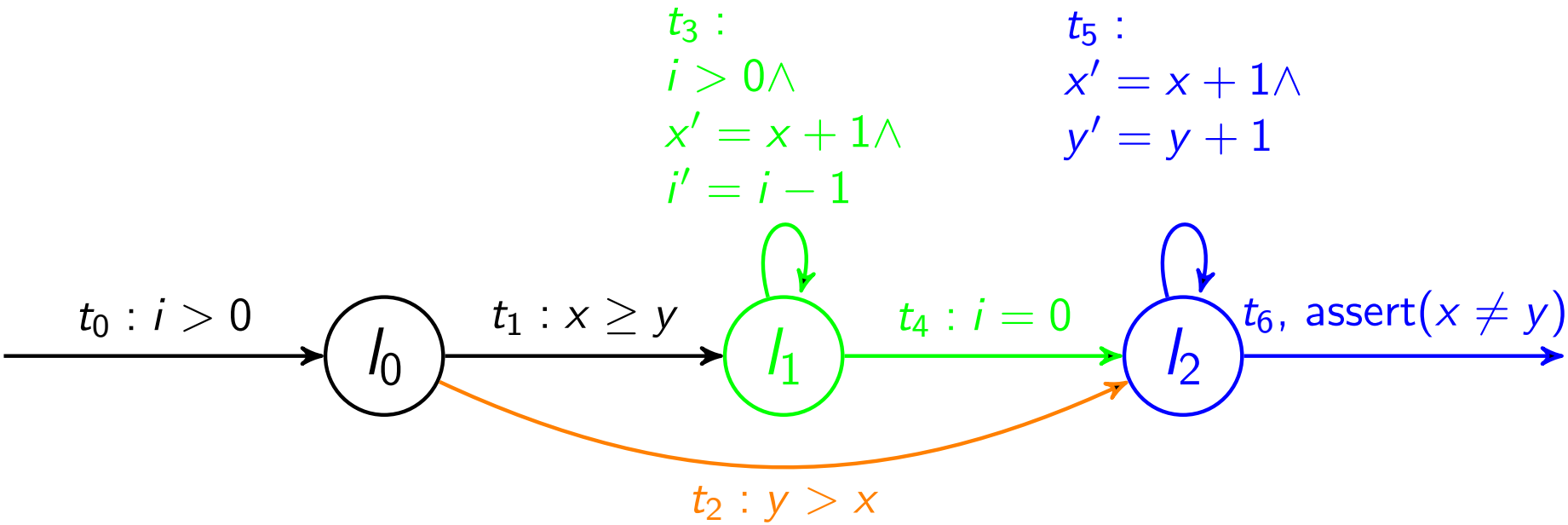

CheckSafe on $\{\ell_1\}$ for $x > y$

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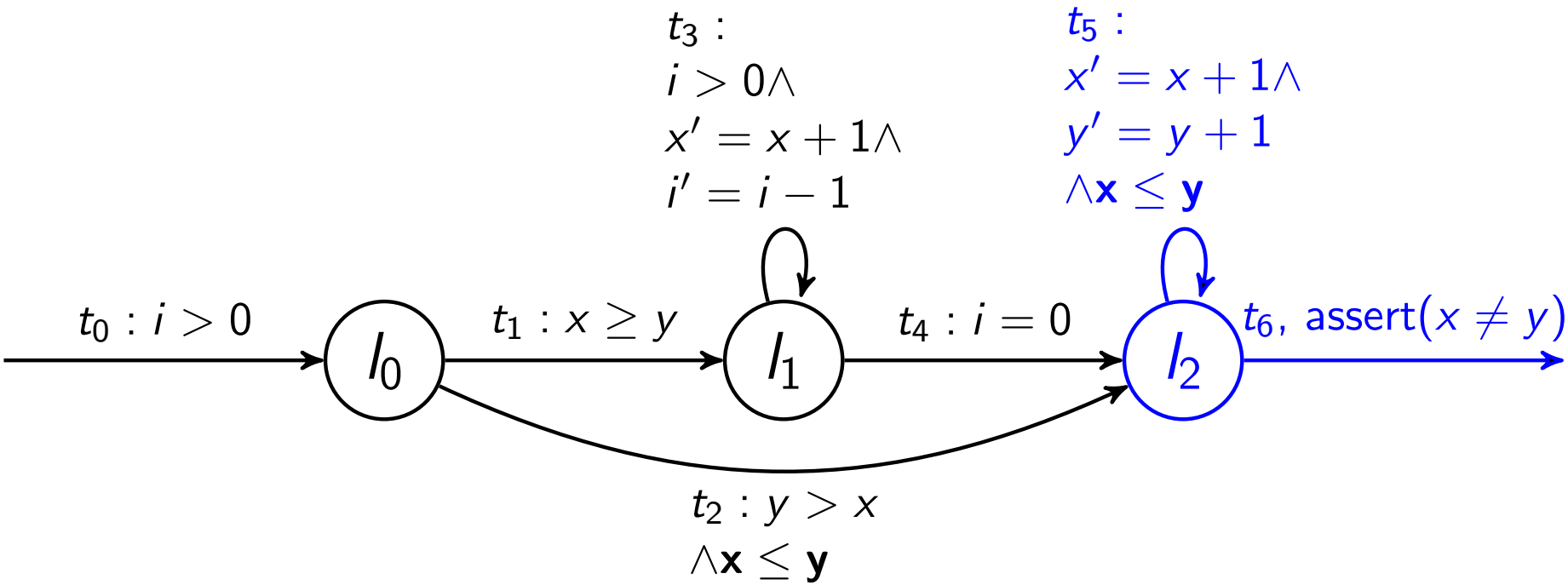
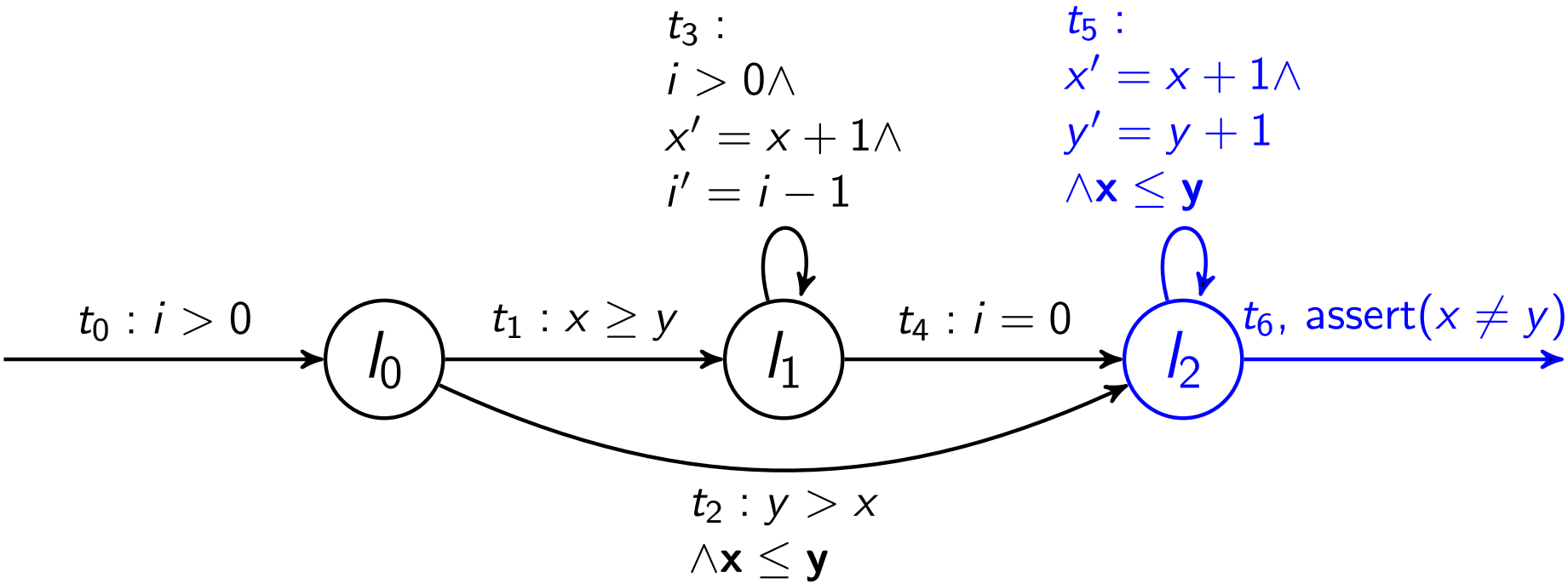


Narrow on $\{\ell_2\}$

Add $x \leq y$ to t_2

Add $x \leq y$ to t_5

Example execution



CheckSafe on $\{\ell_2\}$ for $x \neq y$

Call CondSafe, get $y > x$ instead of $x > y$ as precondition

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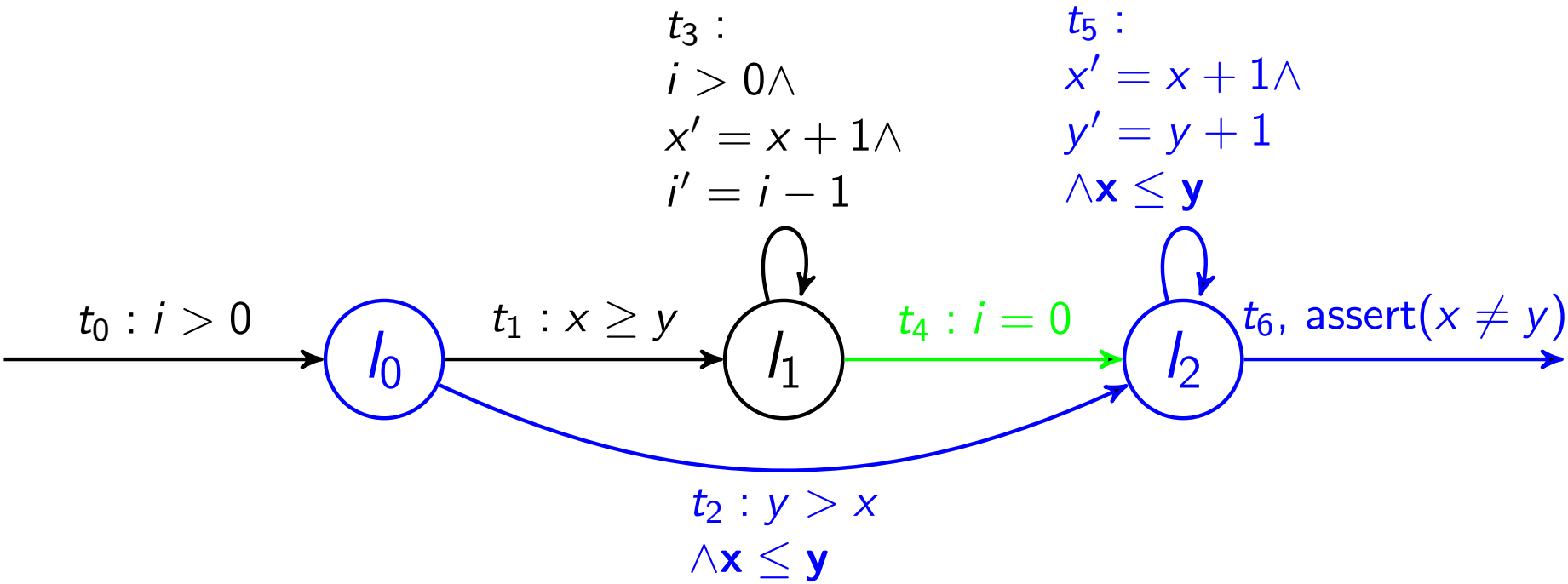
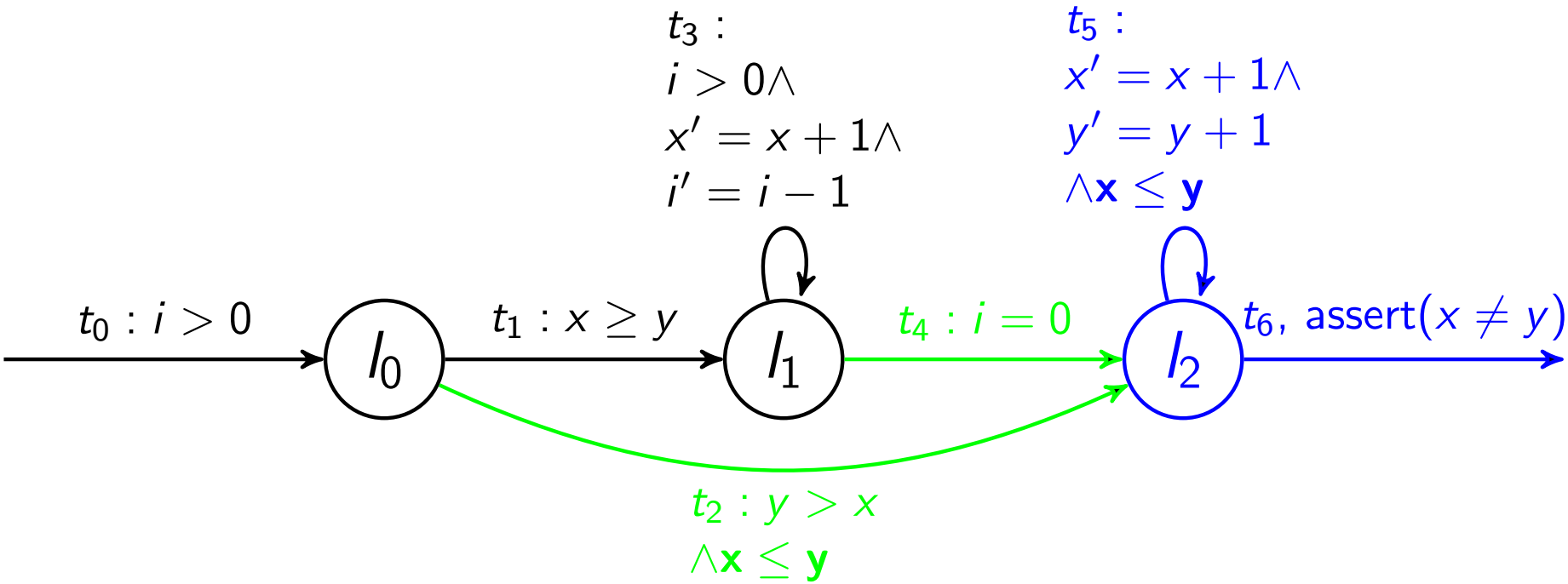


CheckSafe on $\{\ell_0\}$ for $y > x$

t_2 does already imply $y > x$

Example execution



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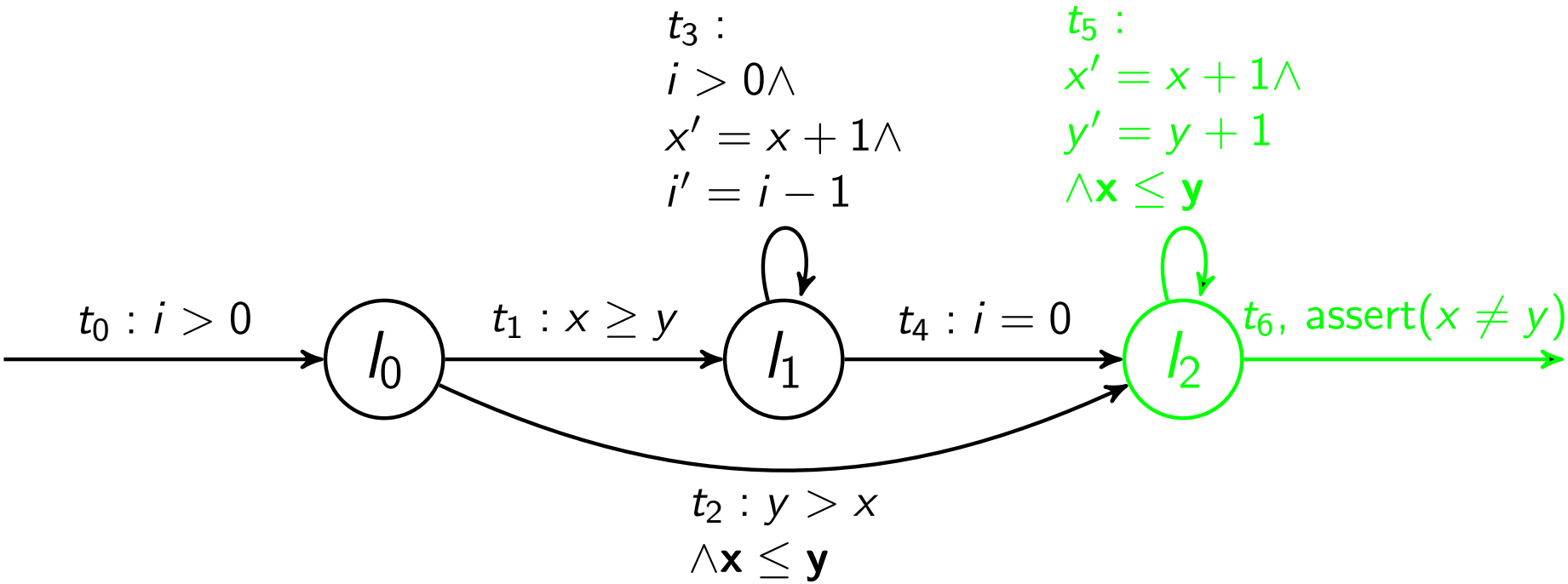

CheckSafe on $\{\ell_0\}$ for $y > x$

Program is safe for $x \neq y$

References

Brockschmidt, Marc and Larraz, Daniel and Oliveras, Albert and Rodriguez-Carbonell, Enric and Rubio, Albert (2015)

Compositional Safety Verification with Max-SMT

Proceedings of FMCAD'15

The End