

Repetition Exponentialfunktion

Bestimmen Sie x:

1. $4^x = 16$

$4^2 = 16$ also $4^x = 4^2$

Exponentenvergleich

$x = 2$

2. $4^{2x} = 256$

$4^4 = 256$ also $4^{2x} = 4^4$

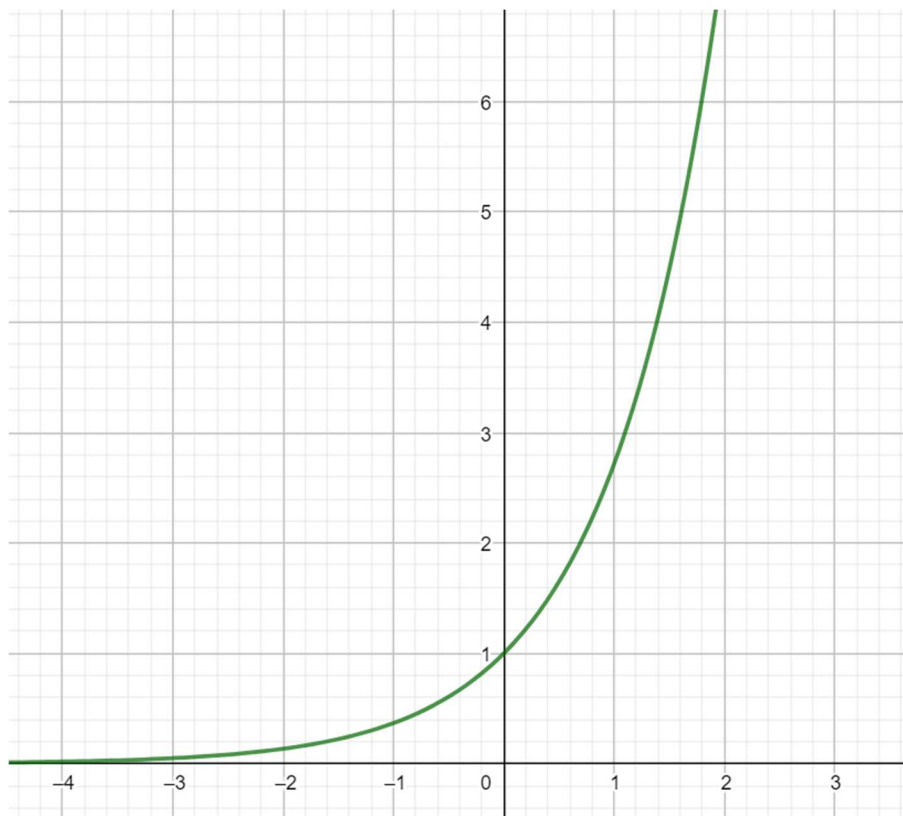
Exponentenvergleich

$2x = 4$: 2

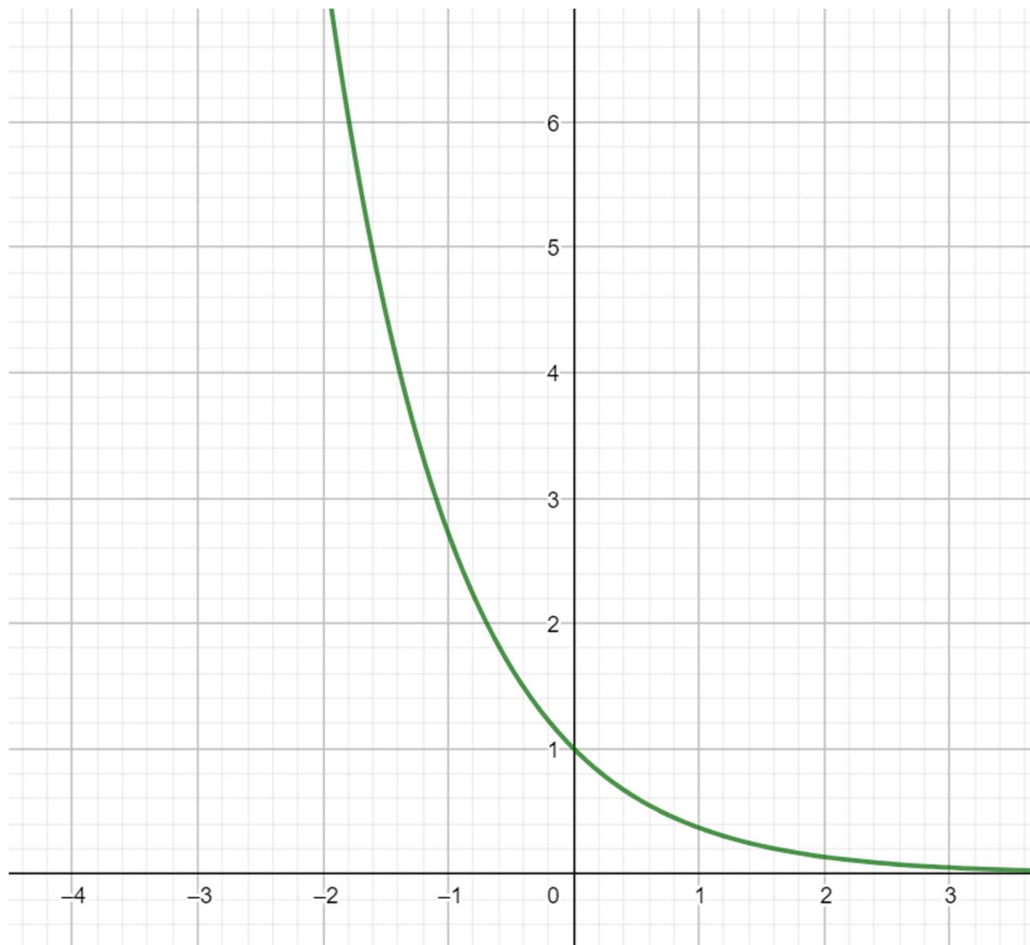
$x = 2$

Zeichnen Sie den Graphen von

3. $f(x) = e^x$



4. $f(x) = e^{-x}$



5. Wenn $e^x = 2^x = 10^x$ ist,
dann ist $x = 0$

6. Bestimmen Sie x für $2^{5x-3} = 512$

$$2^9 = 512 \text{ also } 2^{5x-3} = 2^9$$

Exponentenvergleich

$$5x - 3 = 9$$

$$+ 3$$

$$5x = 8 + 3 = 12$$

$$: 5$$

$$x = \frac{12}{5}$$

7. Bestimmen Sie x für $\sqrt{a^{x-3}} = \sqrt[3]{a^{x+2}}$

$$a^{\frac{x-3}{2}} = a^{\frac{x+2}{3}}$$

Exponentenvergleich

$$\frac{x-3}{2} = \frac{x+2}{3}$$

* 6

$$3(x-3) = 2(x+2) = 3x-9 = 2x+4 \quad -2x$$

$$x-9 = 4 \quad +9$$

$$x = 13$$

8. Bestimmen Sie x für $\sqrt[x+2]{27} = (\sqrt[3]{3})^{2x+1}$

$$27^{\frac{1}{x+2}} = 3^{\frac{2x+1}{3}} \text{ wobei } 3^3 = 27$$

$$3^{\frac{3}{x+2}} = 3^{\frac{2x+1}{3}}$$

Exponentenvergleich

$$\frac{3}{x+2} = \frac{2x+1}{3}$$

* 3(x+2)

$$9 = (2x+1)(x+2) = 2x^2 + 4x + x + 2 = 2x^2 + 5x + 2$$

– 9

$$2x^2 + 5x - 7 = 0$$

abc Formel

$$x_{1,2} = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{-5 \pm \sqrt{25 - 4 \cdot 2 \cdot (-7)}}{4} = \frac{-5 \pm \sqrt{25 + 56}}{4} = \frac{-5 \pm \sqrt{81}}{4} = \frac{-5 \pm 9}{4}$$

$$x_1 = \frac{-5+9}{4} = \frac{4}{4} = 1$$

$$x_1 = \frac{-5-9}{4} = \frac{-14}{4} = -3.5$$