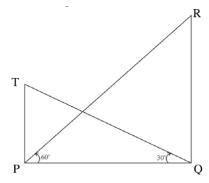
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AI1110 - Assignment 1

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Q10-c: The angle of elevation from a point P of the top of a tower QR, 50m high is 60° and that of the tower PT from a point Q is 30°. Find the height of tower PT, correct to the nearest metre.



Parameter	Symbol	Value
QR	h	50
Angle QPR	α	60°
Angle PQT	β	30°
Base PQ	d	???
PT	h_2	???

TABLE I

Solution: In Δ PQR, using basic trigonometric equation in a right-angled triangle, we know that,

$$\tan(\theta) = \frac{\text{perpendicular}}{\text{base}}$$

$$\Rightarrow \tan(\alpha) = \frac{h}{d}$$

$$\Rightarrow d = \frac{h}{\tan(\alpha)}$$

$$\Rightarrow d = \frac{50}{\tan(60^\circ)} m$$

$$[\because \alpha = 60^\circ \& h = 50m]$$

$$\Rightarrow d = \frac{50}{\sqrt{3}} m - (1)$$

$$\therefore \tan(\beta) = \frac{h_2}{d}$$

$$\Rightarrow h_2 = d \times \tan(\beta)$$

$$\Rightarrow h_2 = d \times \tan(30^\circ)$$

$$\Rightarrow h_2 = \frac{50}{\sqrt{3}} \times \tan(30^\circ) m$$

$$[using(1)]$$

$$\Rightarrow h_2 = \frac{50}{3} m$$

 $\therefore h_2(PT) \approx \fbox{17}$ metres after rounding off. This can be verified by plotting QR , α and β and approximating the length of PT.

Output: The Output of the program used to verify the answer is given below:

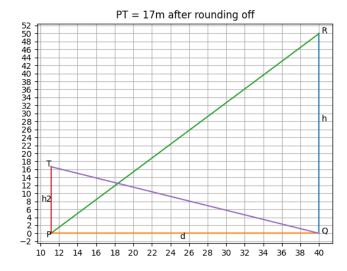


Fig. 0. Plot of the figure and calculated length

Now in ΔPQT , $\beta = 30^{\circ}$.