

## Written Assignment 2

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### 1. (15') Quick Sort

Suppose that the quicksort algorithm is performed on the following array of integers.

6	2	7	3	4	5	1
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- (5 marks) What is the best choice of the pivot for the first round of quicksort?
- (5 marks) If the “median of three” strategy is used for pivot selection, what is the value of the pivot for the first round of quicksort?
- (5 marks) If the “median of three” strategy is used for pivot selection, what is the content of the array after the partition procedure in the first round of quicksort? Please strictly follow the partition algorithm introduced in the class.

### 2. (20') Heap Sort

Sort the array  $\{1, 6, 3, 5, 4, 2\}$  with a **maximum** heap without using extra memory. Write down the content of the array every time an *insert()* or a *deleteMax()* operation completes. The initial state and the array content after the first two insertions are already written for you:

0: initial state

| 1 | 6 | 3 | 5 | 4 | 2 |

1: insert (1)

| 1 | 6 | 3 | 5 | 4 | 2 |

2: insert (6)

| 6 | 1 | 3 | 5 | 4 | 2 |

### 3. (10') Binary Search Trees

Suppose that every node of a binary search tree has 3 pieces of information:

- key: an integer which is the key of the node
- left: a pointer which points to the left child of the node
- right: a pointer which points to the right child of the node

Write the pseudo code for a function, *printKeys*, which prints all the keys on the binary search tree in DESCENDING order.

#### 4. (15') AVL Trees

Construct an AVL tree by inserting the input array {6, 20, 15, 7, 12, 8}. Draw the three trees after inserting the last three elements: 7, 12, and 8, respectively.

#### 5. (40') B+ Trees

5.1. (10') Suppose you are managing employee records on a computer with the following setting:

- Computer hard disk access is block-based and the size of one block is 2048 bytes.
- The size of each employee record is 256 bytes (including the primary key).
- The primary key for an employee record is of type *long long* (8 bytes).
- The size of a pointer is 4 bytes.

You decide to store the data using a B+ tree. Propose the best setting for  $M$  and  $L$ . Show the steps that lead to your proposal.

Note: The definition of  $M$  and  $L$  is as described in the lecture slides.

5.2. (30') In this question, we use a B+ tree with  $M=L=3$ . The initial B+ tree is shown below

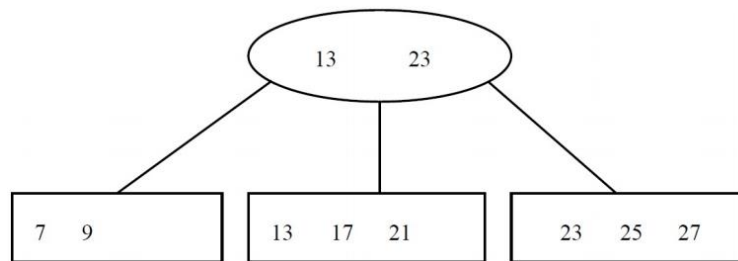


Figure 1: The initial B+ Tree

a) (15') Given an insertion sequence {22, 12, 32}, draw the three B+ trees after each insertion, respectively. Please start from the initial B+ tree shown in Figure 1.

Note: please strictly follow the lecture notes when you do the operations.

b) (15') Given a deletion sequence {23, 9, 7}, draw the three B+ trees after each deletion. Please start from the initial B+ tree shown in Figure 1.

Note: please strictly follow the lecture notes when you do the operations.