Part I

	Total # of parameters in RNN/LSTM layer(s)	Test accuracy %
2-level bi-LSTM	1,446,400	73.00%
2-level bi-RNN	361,600	61.39%
bi-RNN	120,800	68.72%
bi-LSTM	483,200	86.49%
LSTM	241,600	86.03%
RNN	60,400	64.64%

Part II

Question 2

$$\frac{\partial L^t}{\partial f_a} = 0, \ \frac{\partial L^t}{\partial f_p} = 0, \ \frac{\partial L^t}{\partial f_n} = 0$$

Question 3

$$\frac{\partial L^t}{\partial f_a} = f_n - f_p, \quad \frac{\partial L^t}{\partial f_p} = f_p - f_a, \quad \frac{\partial L^t}{\partial f_n} = f_a - f_n$$

Question 4

If we are considering all permutations then we have 5 choices for the anchor, 4 choices for the positive and 3 choices for the negative.

Which gives: (6 P 3) = 120 unique triplets.

If we only consider valid triplets. Then we have 6 choices for the anchor, 2 choices for a positive and 3 choices for a negative. Alternatively, we can see this as 3 choices for an anchor, 2 choices for a positive and 3 choices for a negative times 2.

This gives: 6*2*3 = 2*(3*2*3) = 36 unique triplets.

Question 5

First converting the list of triplets to the embedding space we get:

$$t_1=(f_1, f_2, f_5), t_2=(f_1, f_3, f_4), t_3=(f_2, f_1, f_6), t_4=(f_2, f_3, f_4), t_5=(f_3, f_1, f_5), t_6=(f_5, f_6, f_2), t_7=(f_6, f_4, f_3), t_8=(f_6, f_4, f_2)$$

Question 5.1

$$\frac{\partial L}{\partial f_1} t_1 = f_5 - f_2, \ \frac{\partial L^1}{\partial f_2} = f_2 - f_1, \ \frac{\partial L^1}{\partial f_3} = 0, \ \frac{\partial L^1}{\partial f_4} = 0, \ \frac{\partial L^1}{\partial f_5} = f_1 - f_2, \ \frac{\partial L^1}{\partial f_6} = 0$$

Question 5.2

$$\frac{\partial L}{\partial f_{1}}t_{2}=f_{4}-f_{3}, \ \frac{\partial L^{2}}{\partial f_{2}}=0, \ \frac{\partial L^{2}}{\partial f_{3}}=f_{3}-f_{1}, \ \frac{\partial L^{2}}{\partial f_{4}}=f_{1}-f_{4}, \ \frac{\partial L^{2}}{\partial f_{5}}=0, \ \frac{\partial L^{2}}{\partial f_{6}}=0$$

Question 5.3

$$\frac{\partial L}{\partial f_{1}}t_{3}=f_{1}-f_{2}, \ \frac{\partial L^{3}}{\partial f_{2}}=f_{6}-f_{1}, \ \frac{\partial L^{3}}{\partial f_{3}}=0, \ \frac{\partial L^{3}}{\partial f_{4}}=0, \ \frac{\partial L^{3}}{\partial f_{5}}=0, \ \frac{\partial L^{3}}{\partial f_{6}}=f_{2}-f_{6}$$

Question 5.4

$$\frac{\partial L}{\partial f_{1}}t_{4}=0, \ \frac{\partial L^{4}}{\partial f_{2}}=f_{4}-f_{2}, \ \frac{\partial L^{4}}{\partial f_{3}}=f_{3}-f_{2}, \ \frac{\partial L^{4}}{\partial f_{4}}=f_{2}-f_{4}, \ \frac{\partial L^{4}}{\partial f_{5}}=0, \ \frac{\partial L^{4}}{\partial f_{6}}=0$$

Question 5.5

$$\frac{\partial L}{\partial f_{1}}t_{5} = f_{1} - f_{3}, \ \frac{\partial L^{5}}{\partial f_{2}} = 0, \ \frac{\partial L^{5}}{\partial f_{3}} = f_{5} - f_{1}, \ \frac{\partial L^{5}}{\partial f_{4}} = 0, \ \frac{\partial L^{5}}{\partial f_{5}} = f_{3} - f_{5}, \ \frac{\partial L^{6}}{\partial f_{6}} = 0$$

Question 5.6

$$\frac{\partial L}{\partial f_{1}}t_{6}=0, \ \frac{\partial L^{6}}{\partial f_{2}}=f_{5}-f_{2}, \ \frac{\partial L^{6}}{\partial f_{3}}=0, \ \frac{\partial L^{6}}{\partial f_{4}}=0, \ \frac{\partial L^{6}}{\partial f_{5}}=f_{2}-f_{6}, \ \frac{\partial L^{6}}{\partial f_{6}}=f_{6}-f_{5}$$

Question 5.7

$$\frac{\partial L}{\partial f_{1}}t_{7}=0, \ \frac{\partial L^{7}}{\partial f_{2}}=0, \ \frac{\partial L^{7}}{\partial f_{3}}=f_{6}-f_{3}, \ \frac{\partial L^{7}}{\partial f_{4}}=f_{4}-f_{6}, \ \frac{\partial L^{7}}{\partial f_{5}}=0, \ \frac{\partial L^{7}}{\partial f_{6}}=f_{3}-f_{4}$$

Question 5.8

$$\frac{\partial L}{\partial f_{1}}t_{8}=0, \ \frac{\partial L^{8}}{\partial f_{2}}=f_{6}-f_{2}, \ \frac{\partial L^{8}}{\partial f_{3}}=0, \ \frac{\partial L^{8}}{\partial f_{4}}=f_{4}-f_{6}, \ \frac{\partial L^{8}}{\partial f_{5}}=0, \ \frac{\partial L^{8}}{\partial f_{6}}=f_{2}-f_{4}$$

Question 6

$$\frac{\partial L}{\partial f_{1}} = (f_{5} - f_{2}) + (f_{4} - f_{3}) + (f_{1} - f_{2}) + (f_{1} - f_{3}) = f_{5} - 2f_{2} + f_{4} - 2f_{3} + 2f_{1}$$

$$\frac{\partial L}{\partial f_{2}} = (f_{2} - f_{1}) + (f_{6} - f_{1}) + (f_{4} - f_{2}) + (f_{5} - f_{2}) + (f_{6} - f_{2}) = -2f_{1} - 2f_{2} + f_{4} + f_{5} + 2f_{6}$$

$$\frac{\partial L}{\partial f_{3}} = (f_{3} - f_{1}) + (f_{3} - f_{2}) + (f_{5} - f_{1}) + (f_{6} - f_{3}) = -2f_{1} - f_{2} + f_{3} + f_{5} + f_{6}$$

$$\frac{\partial L}{\partial f_{4}} = (f_{1} - f_{4}) + (f_{2} - f_{4}) + (f_{4} - f_{6}) + (f_{4} - f_{6}) = f_{1} + f_{2} - 2f_{6}$$

$$\frac{\partial L}{\partial f_{5}} = (f_{1} - f_{2}) + (f_{3} - f_{5}) + (f_{2} - f_{6}) = f_{1} + f_{3} - f_{5} - f_{6}$$

$$\frac{\partial L}{\partial f_{6}} = (f_{2} - f_{6}) + (f_{6} - f_{5}) + (f_{3} - f_{4}) + (f_{2} - f_{4}) = 2f_{2} + f_{3} - 2f_{4} - f_{5}$$